Title

Spatio-temporal "global" neurodynamics in both continuous and discrete pictures for human brains

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Abstract

The neural manifold in state space represents the mass neural dynamics of a biological system. A challenging modern approach treats the brain as a whole in terms of the interaction between the agent and the world. Therefore, we need to develop a method for this global neural workspace. The current study aimed to visualize spontaneous neural trajectories regardless of their measuring modalities (electroencephalography [EEG], functional magnetic resonance imaging [fMRI], and magnetoencephalography [MEG]). First, we examined the possible visualization of EEG manifolds. These results suggest that a spherical surface can be clearly observed within the spatial similarity space. Once valid (e.g., differentiable) and useful (e.g., low-dimensional) manifolds are obtained, the nature of the sphere, such as shape and size, becomes a possible target of interest. Because these should be practically useful, we suggest advantages of the EEG manifold (essentially continuous) or the state transition matrix (coarse-grained discrete). Finally, because our basic procedure is modality-independent, MEG and fMRI manifolds were also compared. These results strongly suggest the need to update our understanding of neural mass representations to include robust "global" dynamics.

Keywords

Neural manifold, state space, EEG, fMRI, MEG, mass global dynamics

Introduction

Generally, the neural manifold represents the state space for mass neural activity as a system in general (Iyer et al., 2022; Jazayeri & Afraz, 2017). A traditional approach spatiotemporally divides the brain into parcels or modules in relation to a specific perceptual or cognitive function. In addition, the integration of segregated modules into a global neural workspace is important for understanding brain function. A challenging modern approach would be to treat the brain as a whole in terms of the interaction between the agent and the world (Friston et al., 2021; Mathys et al., 2011) in which the essential function of the brain is simply the interpretation of sensory inflow and motor outflow over multiple (hierarchical) representational spaces (Barack & Krakauer, 2021; Kriegeskorte & Wei, 2021). In this view, whole-brain dynamics as an agent of the entity would need to be visualized for both its common and unique features among participants. While previous studies have often examined neural manifolds for a relatively local population of neurons (Nieh et al., 2021; Sadtler et al., 2014), others have indicated more global neural dynamics as a whole-brain state transition both in functional magnetic resonance imaging (fMRI) (state-space landscape) (Ezaki et al., 2017; Watanabe et al., 2014) and electroencephalography (EEG microstate) (Lehmann, 1971; Pascual-Marqui et al., 1995). This strategy produces a state vector at each moment within the phase space (Jazayeri & Afraz, 2017; Ros et al., 2014; Shaw et al., 2019). Tracking the trajectory of the state vector (i.e., a point) further embodies the neural manifolds as an assembly. The current study aimed to visualize spontaneous neural trajectories regardless of the measuring modality (EEG, fMRI, or magnetoencephalography [MEG]) to provide further insight into neural mass representation, given its robust global dynamics.

EEG canonical microstates as attractors

The current approach is motivated by EEG microstate (EEGms) analysis. EEGms have been robustly reported as quasi-stable potentials lasting 60–120 milliseconds that represent whole-brain state dynamics (i.e., network activity) (Michel & Koenig, 2018). The common procedure for EEGms analysis comprises two stages. At the *clustering* stage, the fluctuation in the standard deviation among all electrodes represents the global field power (GFP) for each recording. The local maxima of the GFP (i.e., peaks) are assumed to best represent periods of momentary stability as the state in the voltage topography (Zanesco, 2020), while local minima are assumed to be transient moments between the states. For example, imagine a chain of mountains as a landscape in which each mountain represents a unique phase. The peak is the "limit" representation of the mountain, while the bottom is between the mountains. Therefore, every spatial pattern at the GFP peaks was accumulated for the participant group (the GFP peak dataset). An unsupervised learning algorithm, such as K-means, clusters the GFP peak dataset into optimal classes. Finally, group-wise common topographies are obtained as templates for each class (typically msA, B, C, and D). This clustering procedure aims to extract a few "attractors" in the state dynamics (Férat et al., 2021; Milz et al., 2017) that are often expressed as the cluster centroids on an abstract space (possibly high dimensional) (Koenig & Brandeis, 2016; Zanesco, 2020). Therefore, the continuous spatiotemporal dynamics of the EEG state can be depicted as a transition among these attractors (four canonical EEGms in the current case)(Mishra et al., 2020). This coarse-graining discretization produces a state-transition matrix or directed graph (consisting of nodes and edges) through the *labeling* stage.

The labeling procedure measures the similarity between the templates obtained and every time point (including the GFP peak points) of the participants and labels all data points as one of them (e.g., msA) in a "winner-take-all" manner (Mishra et al., 2020; Pascual-Marqui et al., 1995). Because each topography should last for a while on the order of milliseconds, the original EEG data with multiple channels are simply visualized as a state transition pattern among four states, such as C, D, B, A, and D. As a result, the EEGms analysis typically reveals the frequency of the state ("occurrence"), the lasting of the state ("duration"), and transition patterns among the states ("transition probability") for each recording session or participant.

Continuous or discrete

These depicted features of EEGms can be compared among participant groups (e.g., patients with a disorder and controls) as potential biomarkers (de Bock et al., 2020; Perrottelli et al., 2021) because this discretization of dynamics is relatively stable, regardless of some variations in the analysis algorithms (Wegner et al., 2018). However, these features can sometimes go alone and overemphasize the static traits, that is, the state transition might be assumed as the actual depiction of discrete EEG state dynamics, possibly with "jumping" (Mishra et al., 2020; Shaw et al., 2019). Although EEGms analysis and calculated features are useful tools, especially for comparing people in a simpler manner, we need to consider the possible continuous representation of EEG state dynamics as a whole, that is, the neural and statistical manifolds within the phase (state) space. This approach would ensure detailed characterization of the atypical EEG dynamics for a specific population. In this sense, continuous-or-discrete is not the opposite but the tandem approach.

The current study

First, we examined the possible visualization of EEG manifolds from a simple thought experiment to actual manifold learning. Once valid (e.g., differentiable) and useful (e.g., low-dimensional) manifolds are obtained, the nature of the manifold, including shape and size, becomes a possible target of interest. Furthermore, if we are interested in group-wise dynamics in the EEG state, hyper alignment across participants is required to standardize the individual manifold. Because these should be practically useful, we suggest advantages of the EEG manifold (essentially continuous) or the state transition matrix (coarse-grained discrete). Finally, because our basic procedure is modality-independent, MEG and fMRI manifolds were also compared. Based on these results, we seek to find the neural trajectory as analogous to the trajectory of body state (e.g. hand positions and joint angles) where both are moving toward an agent-dependent "meaningful position" within a certain space: the former represents phase-shifting to a task-specific neural state, while the latter practically means to reach to a cup.

Materials and Methods

The following results were obtained from several datasets, including our own multiple data (different EEG caps, MRI scanners, subjects, and experiments) and some other external open datasets (e.g., Babayan et al., 2019; Niso et al., 2016). Although we do not specifically mention the source for each result, we have confirmed that the depicted results are not dependent on the data, regardless of the measuring procedure, devices, subjects, and preprocessing policy.

Results and Discussion

Characteristics of the individual manifolds

The traditional understanding of EEGms is the momentary state transition among the four typical topologies (spatial representations as canonical msA, B, C, and D). These simplified features for neurophysiological dynamics often help to predict other cognitive or mental variables (da Cruz et al., 2020; Michel & Koenig, 2018)). In contrast, the EEGms transition could simply be a discretization over spatiotemporally continuous dynamics (Mishra et al., 2020). If a "smooth trajectory" (i.e., no jumping) within a certain state space is observed (Shaw et al., 2019), a "smooth surface" as a neural manifold might also emerge where canonical templates serve as a basis as Figure 1A suggests (Fig. 1B for polarized assumption). The term "manifold" has been used to imply relatively low-dimensional and smooth dynamics (Iyer et al., 2022). For that

purpose, we first examined the intrinsic dimensionality of the EEG channel space by applying principal component analysis. Figure 1C suggests that the three dimensions are intuitively sufficient to represent global state dynamics because the cumulative proportion of variance almost equals or exceeds 80% at the third PC. To visualize a latent manifold, possible dimensional reductions (e.g., Moon et al., 2019 for more general biological data) from the original channel space (in this case, 32D from 32 electrodes) to a sufficiently low-dimensional space (e.g., 3D in contrast to 2D) were examined (Fig. 1D). Although we may see method-dependent state spaces respectively, a "manifold" in a more strict sense (i.e., smooth or "geometrically differentiable" surface) was only observed within the similarity space by a multi-dimensional scaling (MDS)(e.g., Kriegeskorte & Wei, 2021). Interestingly, this simple spherical surface represented all possible EEG states using a standard MDS procedure (Fig. 2).

The state comprises elements at a given moment in the definition (Fig. 2A). Because the elements (32 channel voltage values in the current case) are vectorized, the assembly of states can be seen as a matrix (32 × number of states). As previously mentioned, the conventional EEGms analysis pipeline extracts templates from this matrix (specifically, the GFP peak dataset). The resultant cluster centroids were restored to their original channel configuration (Fig. 2B, upper panel with spatial interpolation from the lower panel). Since the modified k-means was introduced to produce polarity-ignored EEGms templates (Pascual-Marqui et al., 1995), the produced maps can be reversed for polarity-assumed templates, where the frontal is red for positive templates and blue for negative templates (Asai et al., 2022). In addition to EEGms, the assembly of states as a matrix can be time-series EEG data (Fig. 2C; for example, 500 time points). We can calculate the spatial correlation among all states for a similarity score as correlation matrix ranging from -1 to 1 (Fig. 2D, 500 × 500, in this case). If we see something in its patterns (e.g., nonlinear waves or "ripples"), the time-series dynamics as a trajectory might create a closed shape as a manifold. The MDS algorithm dissolves the distance matrix (converted from the correlation matrix) into xyz positional configurations for all states using singular value decomposition. As a result, the exemplified 500 points (for 1 s at 500 Hz sampling) in this state space are *temporally* continuous (Fig. 2E). Furthermore, since this state space is defined as a spatially similarity space, a temporally continuous trajectory within this also means *spatio-temporally* continuity (Fig. 3C).

Finally, when we gathered as many states as possible (e.g., for 30 s), the neural manifold emerged as a sphere. The canonical EEGms templates with polarity (Fig. 2B) are located on the sphere surface (Fig. 3A), where each state is colored in a winner-takes-all manner (left, Fig. 5) or where the current state moves on this manifold (right). The norms of the state vectors within this space are distributed toward almost 1 (Fig. 3B), such that the spherical surface, whose radius is almost 1, could be a definition of a whole-brain EEG manifold. When we visually confirmed the actual movement of the state on this manifold, it was clearly temporally continuous (i.e., no jumps) (c.f., Shaw et al., 2019), especially when the sampling rate was high (Fig. 3C). If the sampling rate is sufficiently high for EEG dynamics, there should be no large displacements from the previous time point if we assume spatiotemporally continuous dynamics. The comparison in the framewise displacement among the distributions for different sampling rates indicates that is the case (Fig. 3C upper) where the displacement "1.5" or "2," for example, means the jump to antipodal point in the current case (e.g., from Japan to Brazil).

Because the canonical templates indicate attractor states (Milz et al., 2017) or attractor position in our case, given a typical EEGms analysis for the GFP peak dataset, we expected a relationship among GFPs, distances to templates, and norms of state vectors (Koenig & Brandeis, 2016; Zanesco, 2020). Although GFP (or log GFP) was non-linearly correlated with the norms of state vectors (Fig. 4A), this positive relationship indicates that when the GFP of the state is higher, the state is located nearer to the spherical surface within the MDS space (and is located nearer to the templates in the definition because templates are located on the surface; Fig. 3A). When each state was colored in a winner-take-all manner, msC was the strongest attractor among the four with the highest GFPs (rightward in Fig. 4BC) (Bagdasarov et al., 2022; Zanesco et al., 2020) whereas msD was concentrated on the sphere surface with the largest norms (upward in Fig. 4B).

The globe as the common space

Thus far, we have suggested that the individual EEG state moves mainly on a spherical surface from one attractor to another (Fig. 3). If we consider that "sphericalness" is somehow related to the so-called "concentration on the sphere" in high dimensional space (Vershynin, 2018), the width of the surface might imply the latent dimensionality of EEG manifolds (the dimension is higher, the shell gets thinner). Theoretically, the grand-averaged EEG state (averaged over the participants) must be completely flat in voltage and located at the origin as an electrophysiologically impossible state. This could be analogous to the relationship between "average face" as a physiognomically rare phase (Grammer et al., 2002). However, when we are interested in the groupwise dynamics of the EEG state, the "hyperalignment" is required to match the individual spaces. Individual manifolds were depicted as spheres (Fig. 5). The number of templates (k problem in clustering) means how many parcels are expected for the surface (e.g., "four color theorem, (Appel et al., 1989) (Fig. 5AB for comparison between 4(8)- and 6(12)-template models with polarity) where the template state ("attractor") should be located on the center in each region so that "winner-take-all" can be rephrased as "closer-take-all" (or, we selectively see template-near states only with high spatial correlations such as r > 0.8 in Fig. 5C). In addition, if necessary, we may create a polarity-ignored manifold from conventional absolute similarity (e.g., a spatial correlation matrix); figure 5D suggests that this is no longer a sphere. Furthermore, more templates or "landmarks" (in the current case) could be reproduced from the canonical templates as we created the polarized templates (Fig. 2B). The averaged state from the two (= 2 vectors) should be located approximately between their two positions on the spherical surface because they are all within a similarity space (Fig. 5E). These landmarks including canonical template-families can be further used to define the "standard space" where the following hyperalignment algorithm would run.

Hyperaligning the registration of point groups over participants/sessions onto the same standard space is not difficult in the current case because the individual manifolds are all spheres with the same radius (each configuration is data-driven). Figure 6 shows our hyperalign procedure ("sequential MDS") even for huge accumulated EEG states over participants/sessions. This was essential because applying MDS over grand-all states requires unrealistic computation time or immediately causes memory overflow, especially for electrophysiological EEG states (for example, a 100 Hz 5 min recording produces 30,000 states). First, we need "seeds" for the standard space. In a typical situation, some minutes of resting data for some participants are sufficient; for example, a 100 Hz recording for 1 min over five participants produces 30,000 states in total. Once the conventional MDS completes all these states, each point for each state shapes a sphere. Because not all points are required in the subsequent process (the more increases the accuracy of registration but requires more time), a sufficient number of points, such as 50 points, can be selected through grid sampling. Here, we can add templates (canonicals or canonical families, as mentioned above) to these and apply the MDS again over these states (e.g., 50 selected states and eight polarized templates). Although each position is no longer on the grid because the configuration is data-driven and the centroid is relocated to the origin (i.e., relative within the dataset), these can be used as our standard space (i.e., reapplying MDS to these does not change the configuration).

We are now ready to apply point-by-point registration within the standard space (Fig. 6, lower). A new state was then added to the standard state (58 points). The MDS was applied to these 59 states and configured. If the number of standard points is large enough for one new point, the relative positions (i.e., distances) among the standard points do not change, although the configuration is slightly different from the original standard configuration (e.g., the centroid moves slightly). Therefore, a rigid transformation with reflection between the two configurations for standard states (original and temporally rearranged) can determine the position of the new state within the original standard space. Consequently, every new state can be located within the same space using this algorithm. This is a sequential process to allow as many states as possible to be located through sMDS (for example, for high-frequency sampled data) and is also useful for hyperalignment over participants. Another implementation is real-time neurofeedback to participants based on the determined position of the current state (xyz coordinates). Finally, we obtained individual but standardized manifolds for comparison (Fig. 6, upper right), where the templates were positioned at the same coordinates and the current state moved spatiotemporally around the templates in a continuous manner.

As a result of our sequential MDS algorithm, we can see and compare individual manifolds or trajectories even for an external large dataset where a different EEG cap with more channels was used (Babayan et al., 2019), and we were able to replicate it (Fig. 7A as view ① for a typical participant). In addition, the state distribution is indicated as a heatmap from the same view (Fig. 7B) or a scatter plot on the sphere (Fig. 7C, when all norms are normalized to 1.0, or we can threshold shorter norms as noisy states). Furthermore, if we want to see the entire surface of the "globe" at a glance, various "map projection" methods are applicable with inevitable method-dependent biases. Figure 7D shows the global field power (darker indicates higher GFP) for each state on the azimuthal equidistant projection (the distance and azimuth from the center are retained, so that the globe is represented as a perfect circle on the plane). Figure 7E represents four (eight) regions for each polarized canonical EEGms class (i.e., map projection of Fig. 7A), whereas Figure 7F is for Figure 7B. By analyzing a large dataset, we found that regardless of gender or age, individual manifolds always exhibit a sphere with a slight bias. Therefore, we detected mistakenly recorded EEG data by checking their individual spheres whose shapes were largely distorted (Fig. 7G-L). In addition, regarding preprocessing, we confirmed that only the band-pass filter is necessary (e.g., 2-20 Hz) for making spheres, although additional rigorous pipelines might help to modify noisy states that should be located near the origin of the space (Fig. 3B) as off-manifold "impossible" states (Sadtler et al., 2014). Figure 8 indicates another utility of spherical bias detection for our EEG-fMRI simultaneous recording data, where EEG signals were originally heavily biased by gradient and phase-encoding artifacts from the fMRI scans (Bullock et al., 2021; Chowdhury et al., 2019). Regardless of the single- or multi-band fMRI scans or phase-encoding directions (AP or PA), the largely biased manifolds were gradually restored toward a sphere through corrections and preprocessing stages (Fig. 8A, B, C, D).

Discretization of continuous trajectories

A traditional EEGms analysis produces a transition probability matrix among canonical states or a state transition plot (e.g., a network plot), typically a 4 × 4 asymmetrical matrix and a directed graph with four nodes and 12 edges without self-recursive loops. These can then be updated (Fig. 9). First, we must polarize the states because the topographically positive and negative states are located on opposite sides of the sphere (Fig. 1). Second, we may increase the optimal number (k) of classes (Fig. 5B) because more classes represent more continuous trajectories (through a trade-off with coarse graining simplification). Finally, the directed graph can be depicted as pseudo 3D for the sphere because the positions of the nodes are determined through MDS, as mentioned above. Figure 9 illustrates the relationship among k, the transition matrix, and directed graphs. As expected, if k increases, the matrix becomes sparser (the transition route is fixed to some extent), but the graph represents a more spherical surface (e.g., k=1000), where we see an essential link between continuous and discrete pictures. The optimal k and the definition of the templates ("landmarks") should be an important topic for future study, with going beyond some conventional statistical criterion. Figure 10 indicates age-related transition changes in the pseudosphere from a large external dataset (Babayan et al., 2019). Here, six landmarks (two for the north/south poles and four for the equator) were additionally reproduced from canonical 4 templates (Fig. 5E). The grand average of over 200 participants' resting-state EEG suggests robust common trajectories (Fig. 10, upper left): essentially positive-negative transitions (i.e., between both topographical polarities) with specific A-B and C-D rotations. When the aged groups were subtracted from the grand average, C-D trajectories were characterized in our eyes: the younger as increased C-D rotations and the older as decreased C-D rotations (but increased trajectory on the equator).

Modality independent procedure for the neural manifolds

Thus far, we have introduced a procedure for a standardized EEG manifold in which the current state is moving. This routine can be used as a modality-independent method for neural manifolds (Moon et al. 2019). Once the spatial correlation matrix was obtained (Fig. 2CD), MDS produced manifolds (Fig. 2E). Figure 11A represents MEG (Niso et al., 2016) manifold, where the state vector is, for example, 300D, whereas Figure 11B represents the fMRI manifold, where the state vector is approximately 900,000D, although both manifolds are

embedded within the 3D similarity space without careful examination of its intrinsic dimensionality. We observed ripples and spheres again in the minimally preprocessed data (e.g., bandpass filter) for both. In addition, if we can apply the same procedure to other neural manifolds, EEG microstate analysis may also be applicable for extracting attractor states (Ezaki et al., 2017). This may also be the case for MEG (Tait & Zhang, 2022) and fMRI. In the case of fMRI, the GFP peak dataset was also defined (Fig. 11C). After standard k-means clustering was performed, some templates (as cluster centroids) could be seen when k was set to 6 (Fig. 11D). Among these, a remarkable template should highly resemble a default mode network (DMN). However, our DMN template has some unique characteristics compared to those in the literature. First, our DMN is structure-oriented, although it is only an averaged low-resolution EPI image. Second, the contrast between activation suppression (red and blue) on the gray matter is much clearer. Third, "polarized" DMNs (positive/negative) are extracted simultaneously (this is also true for other templates). Even after applying k-means over the spatially smoothed images (e.g., a 5 mm FWHM Gaussian filter), these characteristics might be maintained (Fig. 12 when k was 12). Since several whole-brain templates are available, the spatial similarity (Pearson's correlation) with Smith ICA (independent component analysis (ICA) templates was depicted (Smith et al., 2009, 2013). Although the relationship is not one-by-one (Fig. 12A), our templates are congruent with the existing well-known network templates; however, ICA is presumably not for the definition of the momentary "states." We minimally observed the default mode, executive, visual, and audio-motor networks (Fig. 12B for DMNs in the same plot definition).

Manifolds for phase-locked trajectories to be visualized

Finally, we suggest using this spherical neural manifold in future research. As our sphere was standardized, every state was located within the sphere for comparison. Therefore, we can compare simple trajectories rather than sensor-wise activities for experimental conditions, individual differences, and learning effects (Bradley et al., 2022; Iyer et al., 2022). Figure 13A shows the EEG manifold where some landmarks or "realms" are defined and condition-wise trajectories move around the regions (in this case, for the oddball task in Fig. 13A lowers). This is also applicable to the fMRI manifold (Fig. 13B for the n-back task). We now understand whole-brain neural dynamics both in a continuous and discrete manner (Fig. 2 and 9) as inseparable representations of the dynamic phase transition of the biological system.

Conclusions

The current study aimed to depict neural dynamics regardless of the measurement modality. Because neural dynamics are essentially continuous and thus infinite (i.e., a sphere), handling it is not easy without top-down mathematical approximate modeling. Our policy might be a bottom-up approach in which data-driven visualization is preferred. These results strongly imply continuous spatiotemporal dynamics on a spherical surface. Therefore, the problem is how to handle qualitative flow (i.e., global travelling). We suggest possible coarse-graining quantifications, including trajectories on the neural manifolds and the transition matrix between attractors. To validate and compare them further, we will demonstrate possible applications in our future work.

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Figure 1. Visualizing manifolds

(A)

A state

(voltage map)

(B) Canonical microstate templates

msA msB msC msD msA' msB' msC' msD'

(C) "Autocorrelation" (spatial similarity among all states)

t

(D) t1, 2, 3, 4 .... 500 →

t1, 2, 3, 4 ....

500 →

Correlation for distance matrix

Singular Value Decomposition

(E)

A second (500Hz)

Figure 2. Standard MDS procedure

Figure 3. Spherical EEG manifolds

Figure 4. GFP, norms of state vector, and template-similarity.

(A) Four canonical templates model

A B C D

View ① View ② View ③

"Winner-take-all"

(B) Six canonical templates model

A B C D E F

View ① View ② View ③

"Closer-take-all"

=

(C) Template-near states only (4 templates)

(D) Polarity-ignored manifold (4 templates)

(E) Heuristically produced landmarks (from the four to more templates)

Figure 5. Variations of templates, manifolds, and landmarks.

Individual configuration

 Standardized configuration

MDS-projected individual states and common templates

Subject #1   Subject #2   Subject #3

Reproduced individual spherical manifold on standard space

Subject #1   Subject #2   Subject #3

Preparing "standard brain"

Original configuration
(as many "states"
as possible)

Grid sampling
(minimum "landmarks"
for all possible states)

Reapply MDS
(fixing landmarks
configuration)

Gathering as "trajectory" on standard space

Subject #1   Subject #2   Subject #3

Sequential (point-by-point) MDS of time series and rigid transformation

Time 1   Time 2   Time 3

Figure 6. Hyper alignment over participants/sessions (sequential MDS)

Figure 7. Robust individual spheres and useful spherical-bias detection

Figure 8. Spherical check of EEG signals under fMRI scans on each step.

Figure 9. Exemplified state transition matrix and directed graphs (for pseudo sphere).

Figure 10. Age-related trajectorial changes on the pseudo-sphere.

Figure 11. Modality-independent procedure.

Figure 12. Spatially smoothed fMRI templates with Smith ICA templates

Figure 13. Event-locked (phase-locked) state dynamics on manifolds.