Evidence of an optimal error rate for motor skill learning

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Abstract

When acquiring a motor skill, learners must practice the skill at a difficulty that is challenging but still manageable to gradually improve their performance. In other words, during training, the learner must experience success as well as failure. Does there exist an optimal proportion of successes and failures to promote the fastest improvements in skill? Here, we build on a recent theoretical framework for optimal machine learning, extending it to the learning of motor skills. We then designed a custom task whose difficulty dynamically changed along with human subjects' performance, constraining the error rate during training. In a large behavioral dataset (N=194), we observed evidence that learning is greatest at around a ~30% error rate, matching our theoretical predictions.

Author Summary

Practicing a motor skill involves successfully performing intended movements and learning

from mistakes. Is there an optimal proportion of mistakes during training that leads to fast and

efficient skill learning? Inspired by recent theoretical work on principles of machine learning, we

mathematically derive an "optimal error rate" for a class of motor skills. We then experimentally

validate our predictions. We find both theoretical and empirical evidence suggesting that ~30%

is the optimal error rate for motor learning, which has a range of practical implications from

physical rehabilitation to athletic coaching and training.

Introduction

Acquiring a new motor skill involves reducing errors (Krakauer & Mazzoni, 2011; Ohlsson, 1996;

Tseng et al., 2007). Consider learning to shoot free throws in basketball: After a miss, the player

uses the observed error information (e.g., "I missed to the right") to fine-tune future attempts (e.g.,

re-orienting the shot slightly left). Such performance errors during motor skill learning drive

improvements in both accuracy and precision and, given enough time and practice, can lead to

automaticity and expertise (Haith et al., 2022; Shmuelof et al., 2012; Yang et al., 2022).

Importantly, one's error rate during training can relate to if, and how well, they learn a skill. In the

extreme, if one *never* experienced success, their motor system may have no template upon which

to improve their skill (Sanger, 2004). On the other hand, learning would be unnecessary if one

always experienced success (e.g., the hoop moved to wherever the ball was thrown). Thus, it is

reasonable to assume that there is a "sweet spot" error rate that may generate the most efficient

learning process (Guadagnoli & Lee, 2004). Indeed, in the context of simple non-motor skills (e.g.,

perceptual decision-making) it has recently been proposed that an optimal proportion of success

and failure − an optimal "error rate" − can maximize the learning rate of a perceptual skill, such

as binary categorization of sensory input (Wilson et al., 2019). Here, we extend this logic to the

domain of sensorimotor skill learning.

In any task, errors become more likely as the difficulty of the task increases. Since the difficulty

of the task can often be externally modulated, controlling an individual's error rate during training

requires dynamically controlling the difficulty of the task in response to their performance,

exemplified by classic psychophysical methods like "staircasing" (Cornsweet, 1962). But how

does task difficulty influence learning? In an influential framework proposed by Wilson and

colleagues (2019), it was shown that learning using a gradient descent algorithm mathematically

specifies an optimal error rate with very few additional assumptions needed. In this recent and

influential study, the authors considered the context of a binary discrimination task, and, using

their framework, predicted an optimal error rate of ~15%, a value which was confirmed by multiple

model simulations over a range of binary decision-making tasks.

Can a similar framework be applied to motor skill learning? The first relevant issue is the putative

relationship between motor skill learning and gradient descent. It has been suggested that motor

skill learning, at least in the form of gradual improvements in skill that reduce errors and improve

precision (Diedrichsen & Kornysheva, 2015; Sternad, 2018), does indeed operate via a gradient

descent process (Greenstreet et al., 2025; Haith, 2025; Pierella et al., 2019). In many motor skills,

the learner begins with an initially noisy policy and gradually refines this policy, reducing the

variability of their actions as their skill improves (Haith, 2025; Sternad, 2018). For example, a

novice darts player may make errors that span the whole width of the dartboard initially. But, as

they improve, they gradually decrease their variability to hone in on a particular region of the

board.

Here, we hypothesized that the framework proposed by Wilson and colleagues (2019) might apply

to motor skill learning of the form described above, even though motor errors are both signed and

continuous (rather than binary and unsigned, as in perceptual discrimination tasks). First, we

analytically extended their model to demonstrate that a roughly 32% error rate may be the optimal

error rate for motor skill learning, given some basic assumptions. After specifying this prediction,

we developed a customized "Pong" task that required precise online visuomotor control and

collected behavioral data on the task from a large sample of human participants (N = 194). Using

a custom dynamic error-control algorithm, we modified the size of people's Pong paddle on a

trial-by-trial basis to impose different error rates on their performance and measured their

improvements in the task.

Strikingly, the results of the behavioral experiment appeared to support our predictions – we

found reliable evidence that individuals with an error rate around ~32% showed the most learning

in the task, directly in line with our model simulations. The current work provides a theoretically

grounded specification of a putative optimal error rate for motor learning, and may thus inform

both practical applications (e.g., sport pedagogy, clinical rehabilitation protocols) and theories

concerning the underlying neural algorithms for motor skill learning.

Results

A mathematical derivation of the optimal error rate for motor skill learning in one dimension

The derivation below largely parallels the derivation of the optimal error rate for binary

discrimination tasks, as outlined by Wilson and colleagues (2019). In an idealized motor learning

task, an agent prepares an action a in response to some set of internal conditions or policy π and

external stimuli or state s. Thus,

$\boldsymbol{a} = \Phi(\boldsymbol{\pi}, \boldsymbol{s}, \phi)$ (1)

where $\Phi(\cdot)$ represents the function that transforms $\boldsymbol{\pi}$ and $\boldsymbol{s}$ into motor actions, and ϕ is a set of

internal, tunable free parameters trained by learning.

Whenever an action is executed, it is evaluated in terms of the discrepancy between the actual

movement outcome $\boldsymbol{a}$ and the intended outcome $\boldsymbol{i}$. This discrepancy is a motor error $\boldsymbol{e}$

$e = a - i$ (2)

Here, motor learning consists of minimizing this error (distance from the center of a dart board,

a golf hole, or a basketball hoop; in our Pong task, the distance of the puck from the center of the

paddle). We further assume that errors are normally distributed around the target action and that

there is no systematic bias (i.e., the mean of the policy is the optimal solution). Thus, $\boldsymbol{e}$ can be

rewritten as a Gaussian with zero-mean and a standard deviation of σ

$e \sim N(0, \sigma)$ (3)

While we assume a normal distribution, any symmetrical, zero-mean error distribution can be

used and will converge to an optimal error rate that depends on the specific choice of error

distribution.

Both laboratory and naturalistic motor tasks typically have some degree of error tolerance, Δ,

which still permits task success despite noise. This tolerance can take many forms: the radius of

the green or the hole in golf, the radius of the dartboard when shooting darts, the width of the

basketball hoop; or, in our Pong task, the center-to-edge length of the paddle.

Under these conditions, the error rate at any point in the task can be formalized as:

$ER = 2 \int_{-\infty}^{\Delta} p(e|0, \sigma) \, de = 1 - erf(\Delta/\sigma) = 1 - erf(\beta\Delta)$ (4)

where $p(\cdot)$ is the standardized error distribution, here a normal distribution, $erf(x)$ is the Gauss

error function, and $\beta = 1/\sigma$ is the agent's motor precision. In our case, β would be the inverse of

the root-mean-squared-error (RMSE) centered around the intended outcome *i* (i.e., the center of

the paddle in Pong, or the center of the target).

The goal of learning is to reduce error, which would require tuning the parameters ϕ in order to

generate an action *a* as close to *i* as possible. This amounts to tuning the parameters of the policy

to increase the precision of the policy around the optimal solution, thereby increasing β

(Greenstreet et al., 2025; Haith, 2025; Sternad, 2018). Assuming tuning of these parameters is

done through a gradient descent process, we can formalize the learning process over time as:

$\frac{d\phi_i}{dt} = -\eta \frac{dER}{d\phi_i} \; for \; each \; parameter \; \phi_i$ (5)

where η is the stepwise learning rate of the gradient descent algorithm. Given Equation 4, the

derivative of the error rate $\frac{dER}{d\phi_i}$ can be rewritten via the chain rule:

$\frac{dER}{d\phi_i} = \frac{\partial ER}{\partial \beta} \cdot \frac{d\beta}{d\phi_i} \; for \; each \; parameter \; \phi_i$ (6)

The first term of the right-hand side is the only term which depends on Δ, the task error tolerance

(which can be experimentally controlled), as the second term only reflects how precision changes

with the tuning of the relevant internal parameters outside of experimental control. Thus, to

maximize the learning rate in Equation 5, we must maximize $\frac{\partial ER}{\partial \beta}$ by optimizing the task error

tolerance Δ at each time point *t* in training (see *Methods*). Using Equation 4, $\frac{\partial ER}{\partial \beta}$ is given by:

$\frac{\partial ER}{\partial \beta} = \frac{\partial}{\partial \beta}\left(1 - erf(\beta\Delta)\right) = -\Delta e^{-(\beta\Delta)^2}$ (7)

To maximize Equation 7, we must find its critical points by taking the derivative with respect to

the error tolerance Δ and setting this derivative to zero:

$$\frac{\partial}{\partial\Delta}\frac{\partial ER}{\partial\beta} = \frac{\partial}{\partial\Delta}\left(-\Delta e^{-(\beta\Delta)^2}\right) = -e^{-(\beta\Delta)^2} + (-2\beta\Delta)\cdot(-\beta\Delta)e^{-(\beta\Delta)^2} = 0 \qquad (8)$$

Simple algebraic manipulation of Equation 8 leads to:

$$\beta\Delta^* = \frac{1}{\sqrt{2}} \qquad (9)$$

which can be plugged directly into Equation 4 to solve for the optimal error rate:

$$ER^* = 1 - erf\left(\frac{1}{\sqrt{2}}\right) \approx 0.3173 \qquad (10)$$

In other words, in this framework, the optimal error rate for motor learning in a one-dimensional

task is 31.73%, and an optimal training schedule should aim to maintain performance at a 68.27%

success rate throughout.

Figure 1. Derivation of an optimal error rate for motor learning. Figure largely adapted from Wilson et al.
(2019). (A) Probability distributions of a given motor error e, within a certain error tolerance Δ. Shaded area
represents the probability of a failure, or the error rate. Across training, the magnitude of errors shrinks,
resulting in increased precision β. (B) As the error tolerance Δ increases (i.e. decreasing difficulty), fewer
actions result in failures, leading to a decrease in the error rate. (C) The learning rate is given by the
derivative of the error rate (ER) with respect to the agent's precision β. Maximal learning occurs at an error

tolerance Δ^* which changes with skill/training (β). (D) Same as C but replotted with the corresponding error
rates on the x-axis. The optimal error rate remains constant, regardless of precision β, at ~31.73%.
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Skill improvement in a modified Pong task is optimized when performance is maintained near a 30%

error rate

We aimed to test our theoretically grounded "optimal error rate" for motor learning using a motor

skill task fashioned after the video game Pong. In this task, participants (N=194) controlled the

vertical position of a rectangular paddle using a mouse or touchpad to intercept a small white

puck that moved across the screen at various angles. If participants successfully intercepted the

puck with the paddle, their movement was considered successful, and they were awarded 10

points. If the puck intersected the vertical axis of the paddle without striking the paddle, a red "0"

flashed on the screen, indicating failure.

To scale the difficulty of the task with participants' evolving skill level and thus maintain as close

to a fixed error rate as possible during training, the paddle's size dynamically changed across

trials according to the distribution of participants' errors from the center of the paddle over the

most recent 20 trials (see *Methods* for details). Participants were randomly sorted into 4 groups,

each with an imposed error rate: 15%, 30%, 50%, and 65%. It should be noted that, while the

dynamic paddle size aimed to constrain participants' error rates to these pre-specified levels,

variation in error rate was possible, and each participant indeed experienced their own unique

error rate during training (Fig. 2B).

After an initial 20-trial calibration phase in which the puck was calibrated to move at a reasonable

speed (see *Methods*), and 10 baseline trials where both the puck speed and paddle size were held

constant, participants completed 70 training trials in which the paddle size varied with their

performance. To track performance improvements across the task, we computed the root-mean-

squared-error (RMSE) of the puck's final position relative to the center of the final position of the

user-controlled paddle for every 10-trial bin. As a proxy for precision, we inverted this RMSE to

yield β – β is low when precision is low, and high when precision is high. Since every participant

entered the task at various degrees of skill, we corrected these β values using the 10-trial baseline

in order to measure each participant's *improvement* (i.e., learning) across the length of the task.

A "learning index" (LI) was quantified as the average β over all 70 training trials.

Baseline rates of successful puck interception were not different between groups, and the

average success rate in the baseline was 77% (SD:17%). The dynamic updates to the paddle size

(see *Methods*) successfully constrained participants' error rates across groups (Fig. 2). We note

that the 65% error rate group did have modestly but significantly greater success than the

intended 35% success rate (t(48)=3.03, p=0.004), averaging 41.6% success (SD: 6.1%) after the

baseline. Participants' true error rates, defined as the percentage of miss trials during the 70-trial

baseline phase, on average undershot the intended error rate by 3.1% (SD: 6.6%), or 2.2 (SD: 4.6)

trials. These details were not particularly consequential, as our goal was simply to generate a

wide distribution of different error rates across participants to test our theoretical predictions of

learning rate.

Figure 2. Task description. (A) Participants played a modified version of Pong, where they could control
the paddle's vertical position with their mouse in order to intercept the moving puck. (B) The paddle's length

was dynamically controlled on each trial by an algorithm designed to control the error rate across trials.
Each participant was randomly assigned to one of four groups, each with a specific error rate ("ER"; 15%,
30%, 50%, 65%). The algorithm was largely successful in limiting the success rates of participants in each
group. Shading reflects mean ± 1 S.E.M.
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Regardless of error rate group, participants improved their precision (inverse RMSE, β) during the

training phase (Fig. 3A). Participants' precision in the final 10 trials was significantly greater than

their precision in the first 10 training trials (t(386)=2.36, p=0.02, d=0.24), and participants' overall

improvement, or Learning Index (LI; β averaged across all 70 training trials) was significantly

greater than zero (t(193)=4.33, p=2.4×10^{-5}, d=0.31).

Different error rate groups exhibited different time courses and degrees of improvement (Fig. 3B,

C). As predicted, the 30% error rate group exhibited the greatest LI over all four groups: Their LIs

were significantly greater than the 15% group (t(89)= 3.11, p=0.003, d=0.65), and marginally

greater than the 65% group (t(87)=1.58, p=0.12, d=0.33), but not significantly greater than the 50%

group (t(94)=0.98, p=0.32, d=0.20). Critically, as noted above, group-wise comparisons were not

particularly appropriate given individual variation in actually realized error rates.

Figure 3. Optimal learning when training has an error rate of ~31.7%. (A) All participants significantly improved over the course of training. β values are the baseline-corrected inverse RMSE for each 10-trial bin (arbitrary units). (B) Each group displayed different degrees and time courses of improvement. (C) Learning index reflects the average β across all 7 training bins for each subject. The group with the intended learning rate of 30% exhibited the greatest learning. (D) Individual subjects' error rates plotted against their individual learning index. The smooth curve reflects the theoretically predicted learning rates for each error rate. *Inset:* Spearman correlation between subjects' true LI and theoretically predicted LIs for their experienced error rate during training. Shading in panels A & B and error bars in panels C reflect standard errors of the mean (SEM).

Our main analysis involved comparing each participant's LI to the theoretical learning rate predicted by our model (Fig. 3D). Supporting our theoretical predictions, participants' learning rates significantly correlated with the learning rate predicted for their experienced error rate during training (Pearson correlation: R=0.25, p=0.001; Spearman correlation: ρ=0.23, p=0.0003).

In conclusion, our theoretical prediction of an optimal motor skill learning error rate of ~32% was supported in a large dataset consisting of people performing and improving at a continuous

visuomotor skill task. These data are consistent with the theoretical framework proposed by

Wilson et al. (2019), here generalized to the novel case of motor learning.

Discussion

Here, we developed a new theoretical framework on optimal motor skill learning and employed a

novel Pong-based motor skill task to provide behavioral evidence supporting our theoretical

prediction that the optimal error rate for learning this and similar (one-dimensional) motor skills

should be ~32%. By controlling human subjects' error rates during our Pong task, we could

influence how well they learned throughout the course of training. Our theoretical predictions,

which were closely based on recent work on optimal learning for binary classification tasks

(Wilson et al., 2019), were supported both by showing the strongest learning in the group with the

near-optimal error rate and by revealing a significant correlation between the model predictions

and the empirical data across a range of individuals' actual error rates (Figure 3). We propose

that if an error rate of approximately ~32% is maintained throughout training of a simple (one-

dimensional) motor skill, one may expect to observe the greatest improvements in said motor

skill. This discovery echoes work on "error-less" learning paradigms, where high success rates

are maintained throughout training, and the difficulty of the task increases as the learner

improves (Capio et al., 2013; Maxwell et al., 2001). Given the link between our theoretical

predictions and the measured behavioral results, we also speculate that principles of gradient

descent could be helpful for understanding the underlying psychological and neural algorithms

for motor skill learning (Greenstreet et al., 2025).

Why does the error rate during training influence learning?

In the mathematical framework proposed by (Wilson et al., 2019)and extended here, the

relationship between training difficulty and learning is a necessary consequence of tuning the

parameters responsible for generating responses that reduce errors via gradient descent. Such

an approach leaves a key question unanswered: "How does training difficulty result in changes in

learning rate?" Multiple psychological explanations could be useful for addressing this question.

First, the "Challenge Point" framework (Guadagnoli & Lee, 2004) proposes that an agent's

performance at a motor skill is a source of information for future learning and action attempts.

Highly expected outcomes, such as success when the task is easy, yield very little information as

the agent can fully predict the consequences of their action. However, highly unexpected

outcomes, such as success when the task is extremely difficult, are rare but can provide a high

degree of information. When facing high difficulty, the potentially large amount of information

available to the learner risks being uninterpretable: Was success due to sheer luck and/or external

factors? What aspects of this motor plan made it more successful than previous attempts? The

optimal "challenge point" occurs at a critical difficulty where a considerable amount of

information can be learned from success while also maintaining a moderate degree of difficulty,

such that outcome information is interpretable. In other words, this requires balancing the

expectation of success (which decreases with increased difficulty and should be low to maximize

potential information) with the functional difficulty (which should also be low to maximize the

amount of interpretable information learned from feedback). The balance of minimizing both the

expectation of success and the functional difficulty to optimize the amount of interpretable

information available for learning results in a fixed optimal error rate during training (Wilson et al.,

2019).

Another psychological explanation focuses on the role of reward and motivation in error-based

learning. Motivation to perform well in a task can drive increased sensitivity to errors (Bengtsson

et al., 2009), which in turn can prompt faster learning (Wu et al., 2006). Additionally, rewarding

feedback tends to increase motivation (Bissonette & Roesch, 2016) and can accelerate motor

learning (Nikooyan & Ahmed, 2015). Thus, the recent history of successes and failures may prime

an "optimal" degree of motivation, where errors occur in concert with rewarded trials, keeping the

agent's error sensitivity and motivation for success high. Put another way, if the task is too easy,

learning would be minimal; but, if the task is too difficult, successes are too infrequent to generate

the benefits to motivation and error sensitivity that are crucial for maintaining a high learning rate.

The balance of these two opposing forces could also result in an optimal error rate for learning.

The mathematical framework employed here does not allow us to differentiate or speak to these

explanations, nor other higher-level psychological theories not mentioned here. The formation of

internal models for motor learning requires obtaining information about how observed sensory

outcomes relate to internally generated action plans (Abdelghani et al., 2008; Pierella et al., 2019;

Thoroughman & Shadmehr, 2000) in line with the Challenge Point hypothesis (Guadagnoli & Lee,

2004). But reward feedback has also been shown to enhance motor learning (Galea et al., 2015;

Izawa & Shadmehr, 2011; Nikooyan & Ahmed, 2015), supporting a motivational account as well.

Thus, both explanations are plausible and may reflect how different brain regions (e.g., the

cerebellum and basal ganglia, respectively) contribute to the fine tuning of motor learning-related

parameters (Greenstreet et al., 2025; Seidler et al., 2013). In general, we position our current

findings at a more fundamental, algorithmic level.

Extensions and limitations of the current framework

In our experiment, we chose a simple motor task where motor errors are generally assumed to

be normally distributed. However, in some tasks, such as interval timing (Swanton & Matell, 2011),

the distribution of errors may not be normal and may follow other known distributions. As noted

by Wilson and colleagues (2019), the current approach still applies as long as performance

improvements in those tasks are subserved by a gradient descent algorithm, but it would produce

a different optimal error rate specific to that distribution of errors. In other words, an optimal error

rate using non-Gaussian error distributions could be computed using the same equations

described here. In tasks where the error distribution is unknown or cannot be mathematically

described, empirical observation or alternative methods of estimating the distribution must be

applied in order to compute the optimal error rate.

We also restricted our consideration to a simple one-dimensional motor skill task (errors were

only in the vertical dimension). However, many motor tasks involve errors in multiple dimensions

(e.g., a dart or archer's arrow may miss the bullseye in both the vertical and horizontal

dimensions), which must be concurrently trained. Future work must be done to extend the optimal

error rate framework to these more complex, naturalistic tasks. An important question which

must be considered is whether learning in each dimension is fully independent, or if learning in

one dimension affects learning in the others; the answer to this question would allow us to better

model the error reduction processes involved in learning complex motor skills when multiple

dimensions must be concurrently controlled (Haith et al., 2022; Pierella et al., 2019). Additionally,

distributions of errors in each dimension may not follow similar mathematical descriptions,

requiring more complicated multi-dimensional integrals to optimize the error rate. Nonetheless,

the general mathematical framework demonstrated here can, in theory, be applied to such multi-

dimensional tasks.

Lastly, our task only examines motor learning as defined as the gradual reduction in errors and

improvement of precision over time through practice, which arguably represents only one

component of skill learning (i.e., improvements in "motor acuity"; Krakauer et al., 2019). Other

components of motor learning, including motor adaptation, may be better modeled as changes

in the mean of the policy, rather than gradual refinement of the precision of the policy (Greenstreet

et al. 2025). Explicit strategies, especially early in learning, can cause a learner to abruptly reduce

their errors or discover new solutions (Mazzoni & Krakauer, 2006; Taylor & Ivry, 2011), abruptly

shifting the mean of the policy instead of gradually learning via gradient descent. Explicit

strategies, short-term memory, and cognitive insights during skill learning likely arise from

separate cognitive processes not considered here, though they still make important contributions

to skill learning (Haith & Krakauer, 2013; Hillman et al., 2025; McDougle et al., 2016, 2022;

McDougle & Hillman, 2025). The model presented here is primarily concerned with how the

learner learns to decrease the standard deviation of the policy around this mean, assuming the

mean has already been discovered, thereby improving precision and reducing task-relevant

variability (Haith, 2025; Sternad, 2018).

Future Applications

Our results demonstrate that the error rate during training affects the rate of improvement of a

simple visuomotor skill. We think this insight might be broadly applicable across applied

domains. Rehabilitation paradigms, for example, have already recognized the need to adjust the

difficulty of practice to optimally challenge patients and maximize the therapeutic benefit of

training sessions (Lee et al., 2023; Metzger et al., 2014). In sports coaching, the principle of

progressively increasing the difficulty of practice has been widely applied and shown to facilitate

improvements in skill (Marraffino et al., 2021; Wickens et al., 2013; Zahran et al., 2020).

Optimistically, these approaches, in both sports pedagogy and rehabilitation, may benefit from

the theory used here to mathematically uncover the sweet spot of training difficulty for maximum

skill improvement.

Summary

We demonstrate that an optimal error rate for performance improvements in a motor skill may

exist and suggest that this optimal error rate is around ~32%. By testing a large cohort of human

participants in a novel motor skill task (a modified version of Pong), we also provide empirical

support for this prediction and demonstrate the potential importance of maintaining a particular

error rate throughout training to maximize performance improvements. This approach may have

broader implications in other domains concerned with optimizing the acquisition, refinement, and

rehabilitation of motor skills.

Methods

Participants

200 participants (46% female; age: 27±5) were recruited online through Prolific. Recruitment was

restricted to right-handed or ambidextrous individuals in the United States between the ages of

18 and 35, who had at least 40 prior Prolific submissions. All participants provided informed

consent, in accordance with procedures approved by the Yale University Institutional Review

Board. Due to participant data not posting to the database, two participants did not have any data

recorded. Four participants were further excluded due to not making any recorded movements

during the task. In analyses of learning indices (see *Statistical Analyses*), subjects whose learning

index deviated by 1.75 times the group interquartile range (IQR) from the median were excluded.

This excluded 10 subjects. The final experimental sample was 184 subjects.

Task Design and Protocol

Participants were recruited on Prolific to play a modified version of the game Pong, written using

PhaserJS 3 (phaser.io). Participants controlled a 15-pixel wide rectangular paddle, initially set to

200 pixels (px) in length and fixed 10 px from the left edge of the workspace, inside a 1000 px by

800 px arena enclosed within a white border. Movements of subjects' mouse or trackpad in the

coronal plane directly translated to displacements of the paddle's vertical position (i.e.,

movements away from the body = up; toward = down). Participants were instructed to move the

paddle to intercept a small circular puck (14 px diameter) which would move toward their paddle

at an angle, bouncing off the walls of the arena. They were specifically instructed to try to cause

the puck to hit the middle of the paddle, as this is the strategy most likely to result in success.

This task required participants to integrate visual sensory information regarding the position of

the puck into their movements of the paddle in order to successfully intercept the puck.

Each trial consisted of the puck crossing from 25 pixels left of the right side of the arena to the

left side of the arena where the participant's paddle was located, crossing a horizontal distance

of 975 px. At the start of each trial, the paddle's vertical position was always centered, and the

puck began at a random vertical position sampled from a uniform distribution extending ±375 px

from the center of the screen. The launch angle of the puck could be ±30-45°, to ensure that the

trajectory of the puck was unpredictable. The puck began moving 1000ms after the start of the

trial. If participants successfully intercepted the puck, a green "+10" text prompt would appear in

the center of the screen for 1000 ms, indicating success. Otherwise, if the puck hit the edge of

the arena without being intercepted by the paddle, a red "+0" text prompt was displayed in the

center of the screen for 1000 ms, indicating failure. A running points total was displayed above

the arena and participants were told to maximize the points they earned. After presentation of

reward feedback, the paddle was re-centered, and the puck appeared in a new location to start

the next trial.

Calibration and Error-control Algorithm

The experiment began with a 20-trial calibration phase, in which the horizontal speed of the puck

was calibrated to be comfortable for each participant. The vertical speed of the puck was

determined by the launch angle on a given trial. Since the duration of each trial was dependent

on the horizontal speed of the puck, we needed to calibrate this speed to ensure every participant

had ample time to react to the puck and adjust the paddle. The speed was calibrated using a

staircase procedure: if the participant failed to intercept the puck, the horizontal speed was

reduced by 75 px/s; if the participant successfully intercepted the puck, the speed increased by

75 px/s. The speed was initialized at 800px/s. The minimum allowed speed was 100px/s, but this

was never achieved by any participant. This procedure resulted in a 72% (SD: 12%) success rate

during the calibration phase.

Since this calibration phase often ended with a speed that slightly exceeded the comfortable

range for the participant, the speed was cut to 80% of the final speed achieved. At this point, a

10-trial baseline began in which the puck speed and the paddle size were held constant. This

allowed us to assess each participants' initial degree of skill in the game. Mean success was 77%

(SD:17%). At this point, the final 70-trial training phase began, and the paddle size was allowed to

dynamically update according to a custom algorithm that monitored the recent distribution of

errors to constrain participants' error rates. Each participant was randomly assigned to one of

four groups, each with their own intended error rate: 15%, 30%, 50%, and 65%. On every trial, the

puck's final vertical position relative to the final vertical position of the center of the paddle was

added to a sliding 20-trial buffer, regardless of whether the trial was successful or not. After

excluding outliers (defined as 3 times the median absolute deviation from the median; this is

identical to the MATLAB *rmoutliers* function), we computed the root-mean-squared-error (RMSE)

of this 20-trial history. From this we inferred a zero-mean Gaussian distribution with the RMSE as

the standard deviation and, using the CDF of the Gaussian distribution, we computed a paddle

size that would result in the intended error rate. This outlier criterion was chosen to minimize the

number of excluded trials and only detect extreme outliers that could vastly impact the RMSE

calculation for the duration of the 20-trial buffer, as determined by pilot experiments.

Statistical Analysis

The primary dependent measure on each trial was the task error, defined as the difference

between the final vertical position of the puck and the final vertical position of the center of the

paddle. Errors from every ten trials were binned to compute the RMSE, and these RMSEs were

inverted in order to estimate precision, β. We note that the overall pattern of results does not

change if the inverse of the standard deviation of the errors, an alternative measure of precision,

was used instead of the inverse RMSE. RMSE was preferred since participants were instructed to

aim to intercept the puck in the middle of the paddle, so any biases were random and

unintentional. Each subject's baseline (trials 21-30) precision was subtracted from every

subsequent bin in the training phase in order to quantify improvement. Average improvement, or

the learning index (LI), was quantified as the average β of all training bins after baseline

correction. Statistical outliers, defined as 1.75 times the interquartile range (IQR) away from the

median of each of the four error rate groups, were excluded. This excluded 10 people (5.15%),

leaving us with a final experimental sample of 184.

Theoretical Modeling

Equation 4 gives an expression for the error rate (ER) as a function of the agent's precision β and

the current error tolerance of the task Δ. To maximize the learning rate through gradient descent

(Eq. 5), we must optimize $\frac{\partial ER}{\partial \beta}$, which, through differentiation is given by:

$\frac{\partial ER}{\partial \beta} = 2\Delta \cdot p(-\beta\Delta)$　　　　　　　　　　　　　　　　(8)

Optimization of this expression requires setting the derivative with respect to Δ to zero:

$\quad 0 = \frac{\partial}{\partial\Delta}\left(\frac{\partial ER}{\partial\beta}\right) = \frac{\partial}{\partial\Delta}\left(2\Delta \cdot p(-\beta\Delta)\right)$ $\hfill$ (9)

$\quad = 2p(-\beta\Delta) - 2\beta\Delta \cdot \dfrac{\partial}{\partial(-\beta\Delta)}p(-\beta\Delta)$

$\quad$ This can be solved such that the optimal tolerance $\Delta^\star$ for a given β is given by

$\quad \beta\Delta^\star = \frac{p(-\beta\Delta^\star)}{p'(-\beta\Delta^\star)}$ $\hfill$ (10)

$\quad$ where $p'(x)$ is the derivative of the distribution of errors with respect to the argument x. The

$\quad$ optimal error tolerance $\Delta^\star$ changes with precision β, but the quantity $\beta\Delta^\star$ remains constant,

$\quad$ implying that the optimal error rate $ER^\star$ from Equation 4 is constant, namely:

$\quad ER^\star = 2F(-\beta\Delta)$ $\hfill$ (11)

$\quad$ For a 1D motor task where errors are normally distributed, this optimal error rate is

$\quad ER^\star = 1 - erf\left(\frac{1}{\sqrt{2}}\right) \approx 0.3173$ $\hfill$ (12)

$\quad$ The theoretical predictions plotted in Figure 1 and Figure 3D were computed in the manner

$\quad$ described above. Since the integral of a Gaussian from $-\infty$ to x cannot be analytically solved, it

$\quad$ was estimated using a 100,000-rectangle Reimann sum from -10 to x, a computationally costly

$\quad$ but highly accurate estimate of the integral. 30,000 values of Δ from 0 to 3 in increments of 0.0001

$\quad$ were used to generate the traces in Figure 1 as well as to generate a function that translated Δ

$\quad$ values into theoretically predicted learning rates $\frac{\partial ER}{\partial\beta}$, using the *approxfun* function in R (Becker,

$\quad$ 2018). Since the units of these predicted learning rates are arbitrary, we fit scaling and offset free

$\quad$ parameters that allowed the predictions to match the observed precision improvements of our

$\quad$ subjects using R's optim function most closely, and the resulting trace was plotted in Figure 3C.

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