Distance v.s. Resolution: Neuromapping of Effective Resolution onto Physical Distance

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This manuscript was compiled on August 4, 2023

The main focus of this work is on determining the effective resolution of a face image on the retina when the face is at a particular distance from the eye. Despite its straightforward articulation, arriving at a satisfactory solution might be unexpectedly challenging. The relationship between viewing distance and effective resolution cannot be easily obtained through contrast sensitivity, Snellen acuity, or even photoreceptor packing density in the fovea. We used theoretical considerations to establish preliminary guidelines and then showed participants images of different resolutions at various viewing distances. At each distance, participants were expected to perform an "odd one out" task. During the experiment, participants were asked to identify the image that differed from the others in a 2×2 grid, with image resolution as the sole variable. As the study progressed, viewing distance was gradually reduced, and participants became more adept at distinguishing finer resolution disparities between the three standard images and the outlier. The data collected enabled us to determine the upper and lower limits of the available effective resolution for human vision under normal conditions, as a function of viewing distance. One of the interesting observations is that human performance in blur detection is notably superior to what a theoretical model based on projected image size, cone density, and foveal extent predicts, especially at close ranges. Therefore, we propose that future theoretical models must account for non-uniform in–fovea density and the less pronounced decline in acuity outside the fovea to establish a reliable relationship between viewing distance and perceived image characteristics. The `<distance:effective-resolution>` mapping has practical applications, as it allows for a direct comparison of human face recognition performance across different levels of blur and viewing distance. It also enables us to systematically compare human performance to that of machine vision systems using resolution as a common factor.

Effective Resolution | Acuity | Visual Pathway | Physical Distance.

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1. Introduction

In comparison to up-close viewing, the perception of facial characteristics from a distance presents a new set of challenges, including changes in the relative sizes (reduction in the available resolution) and geometry and orientations of the features as well as the addition of irrelevant background information. Because of these variations, it is auxiliary to adopt distinct strategies to comprehend how the visual system interprets facial information from a distance. Given the changes in the social environment between close-up and distant viewing, the impact of distance and available spatial resolution on facial recognition task must also be taken into account. The level of the interaction decreases over a distance, as does the capacity to interpret non-verbal cues. Therefore, it is scientifically interesting to consider how the physical proximity in terms of transferred information content affect people's capacity for distant face recognition. Particularly relevant is the resultant information bottleneck that transpires when faces are viewed at a distance, which can be quantified in terms of the number of pixels (spatial resolution) that can be represented by the available photoreceptors. Unfortunately, there is no simple/linear relationship between the physiological capacity of human vision and the *effective* resolution that is perceived in a given recognition task.

Previous research has investigated the roles of different spatial frequencies, a topic that is relevant to face recognition as a function of distance. These investigations have demonstrated that low spatial frequencies permit configural processing, whereas high spatial frequencies assist in featural analysis by providing information about details at closer viewing ranges (1–4). Due to the anticipated impact of local diffusive filtering in distant viewing conditions, it is expected that the degradation of local featural details will be more pronounced compared to larger scale configural information (5, 6). In fact, reduced image resolution can even improve configural processing provided that all resources

To be submitted to *Nature Human Behaviour*, August 2023.

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are used for the amalgamation of high-level image cues (2). The visual information in a picture may be made simpler with low spatial frequencies present, which also makes it simpler for the brain to infer the connections between various characteristics. It is instrumental to comprehend the context of an image when the details are less apparent because the brain can concentrate on the general structure and connections between the dependent long-range elements. This is quite natural to see in human visual system in which low resolution seems to be essential at the early stages of their development to maintain a successful holistic processing (7).

One plausible hypothesis suggests that under long-range viewing conditions, configural processing may play a crucial role in the recognition process, while featural information could be largely obliterated as a result of local diffusions. However, as the viewing distance diminishes, holistic processing comes into play and is enhanced by the presence of featural cues, thereby yielding higher effective resolutions beyond what can be achieved solely through available photoreceptors. This specific issue forms the focal point of our research, as we aim to explicitly delve into the precise timings and mechanisms by which these processing techniques and strategies are adopted by the human visual system in relation to varying distances (8). On the contrary, it is quite customary in literature to observe the comparison of deep networks with human performance across various visual tasks, particularly those that involve degraded conditions representative of real-life viewing scenarios (9). The prevailing approach has been to employ Gaussian "blur" as the primary axis of quality degradation, enabling direct comparisons between human observers and machine systems. However, an intermediate axis concerning effective resolution emerges as an integral component, as it encapsulates the human processing mechanisms that map the corresponding level of blur to the physical distance. Unraveling the intricacies of this translation process not only enhances our comprehension of these comparative analyses but also ultimately facilitates and enhances the precision of the overall comparison framework. Hence, among our alternative objectives, lies the pursuit of establishing the intricacies underlying this translation process, thereby contributing to the ongoing refinement of comparison frameworks.

A. Related work. Face perception and recognition under degraded conditions has been an intensively investigated research area in recent years. The effects of low resolution on face recognition is primarily reviewed in (10). In (11), more insight in face recognition accuracy is derived as a function of distance and illumination. Authors have concluded that a systematic increase of recognition performance with decreasing distance and increasing illumination can be observed. However, no references are made regarding the information communicated with the visual system as a function of distance viewing. A recent account of human face recognition performance was provided in (12), which reveals that the salience distribution across a face changes qualitatively with increasing distance. Their results indicate the importance of relationships between internal facial features and external head contours for recognition, which has implications for both human and artificial visual systems (13).

Face recognition as a function of range has attracted only a low profile attention by a number of contributions from the literature (11, 14, 15). Some of these studies focused specifically on examining the impact of resolution on the featural and configural cues within facial images (16–18), elucidating their consequential influence on recognition performance and underscoring the overarching significance of holistic facial feature processing.

There exists a diverse set of applications that present an ample opportunity to investigate a rich array of research questions. These applications include but are not limited to courtrooms and eyewitness identification (15, 19). Additionally, surveillance settings often utilize near-infrared face recognition technology, particularly under-illuminated environments, to recognize faces from a distance (20). Since the resolution of the subtended image on the retina is expected to decrease when the subjects are viewed at a distance, low-resolution face recognition has been paid a particular attention in literature. Particularly, the threshold (minimal) resolution is investigated, above which the performance fairly stays steady and while below which the performance deteriorates rapidly (21, 22). In addition to low quality, various non-linear degradations are reported to be challenging for face recognition performance and hence require a special attention (23). A characteristic shared among previous studies is the utilization of a uniform parameter axis to manipulate degradation, such as scaling or blurring, resulting from remote viewing conditions, while leaving the actual mapping between perceived resolution of the viewed face as a function of distance unexplored.

B. Motivation. One of the motivations of this study is that by having a proven functional relationship between the viewing distance and available image resolution for the human visual system, one would be able to conduct a principled comparison of the human recognition performance with respect to machine performance. This will not only help us understand how much are humans able to see with increasing distances/ranges but also would be conducive to guiding bio-inspired neural network designs taking into account the limitations of the human optical/visual system. Furthermore, addressing the challenges posed by impoverished images and their inherent prevalence in long-range viewing conditions would enable us to implicitly assess the performance of individuals with low vision by appropriately adjusting the distance axis. This valuable information holds significant relevance in the development of rehabilitation programs and assistive devices aimed at improving overall health and well-being.

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In fact, the mapping between the viewing angle and distance as well as the effective resolution is not necessarily obvious and may highly be dependent on the athmospheric conditions (haze, smoke, etc.), the subject's acuity, object perception capabilities and strategies, ventral and dorsal processing (fast/slow) (24). In fact, part of the research objectives of this study is to investigate this relationship under controlled experimental set-ups. Another part of this study is aimed at exploring the integration process within the human brain, specifically focusing on longer viewing time periods that allow for the perceptual differentiation between similar objects. In other words, as viewing distances increase, individuals tend to allocate more time to integrate multiple snapshots of the same observed optotype, gradually enhancing their effective resolution over time. Conversely, for shorter viewing distances, subjects require less processing time to adapt their optical/visual system and achieve the sufficient effective resolution at a given distance. Analyzing this integration process in terms of latency reveals distinct strategies adapted by humans, manifesting itself in the form of *distinct patterns of failed and correct decisions*.

Based on our review over the previous research literature, it appears that a comprehensive theoretical framework is missing that explains the effective resolution v.s. distance mapping as a function of the processing time. It seems that the establishment of any framework would rely heavily on the presence of a robust predictive model, which encompasses accurate modeling of physiological and cognitive processes, as well as a meticulously designed experimental setup to ensure proper validation. Collaboration among experts from diverse fields is crucial to address this gap and advance human-computer interaction and multimedia systems in line with human perceptual and cognitive capabilities.

2. Theory

A. Resampling and Low frequency representation of Images. To be able to assess the resolution of the observed object perceived by our visual system, we realize that, using standard signal processing techniques, we can resample the image plane to reduce the resolution while keeping the image size (receptive field) constant. The process of downsampling the image plane may cause high frequencies to smear and eventually lead to what is called as "aliasing" (25); hence we apply low-pass filtering (typically operationalized with a Gaussian kernel convolution of size σ (sigma)) before this resampling/resizing operation. Here the 2D size of the kernel employed determines the extent of low-pass filtering and thus the *effective resolution* of the resulting image. To be able to measure human optical system performance in terms of resolution, we need to create stimuli whose resolution is reduced to a desired pixel value (accompanied with a reduction factor) using such signal processing techniques. This practice is undertaken to establish the relationship between σ and the reduction factor through adjusting the size of the Guassian kernel and the image size. The prominent question that arises to address the kernel size can be characterized as follows.

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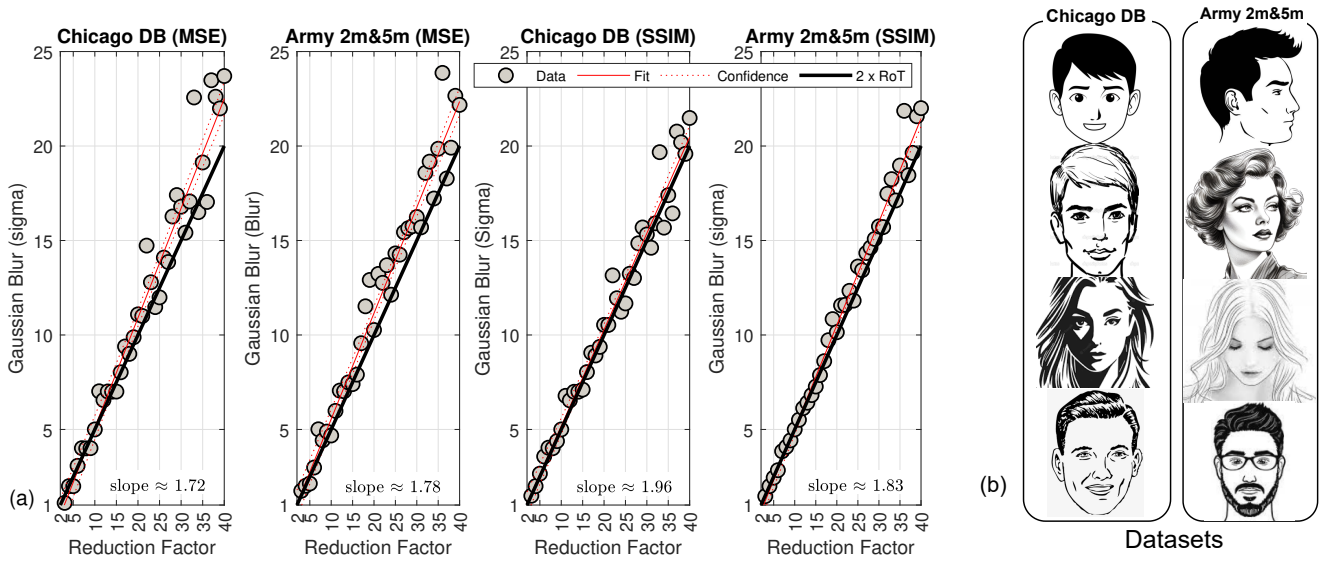

Fig. 1. (a) shows the reduction factor v.s. Gaussian Blur (kernel size expressed in terms of σ) for both datasets (Chicago DB and Army 2m&5m using similarity measures MSE and SIMM. (b) shows some examples from the two datasets (Images are not real to conceal identity information) used to conduct this experiment. RoT: Rule of Thumb.

Given an image resampled (down-sampled and then up-sampled back to the same size using one of the interpolation methods such as *bicubic*), what is the corresponding Guassian kernel size (amount of blur) that leads to the maximum similarity (such as minimum pixel-wise mean square error (MSE) or maximum structural *similarity* index (SSIM)) between the resampled version and the original image convolved with this kernel - low-pass filtered version of the image.

In our study, we have run extensive tests for two different face datasets, namely Chicago DB (26) (a total of 1203 images) and Army 2m&5m (a total of 1350 images) having resolutions 2444×1718 and 400×330, respectively. We have resampled these images with varying reduction factors and investigated the means (as well as the confidence intervals) of the best Gaussian kernel size (σ) that minimizes the MSE or maximizes SSIM. In Fig. 1 (a), we have plotted the Gaussian blur (σ) parameter as a function of reduction factor whereas Fig. 1 (b) provides a few example faces from each database for visualization.

Particularly interesting case is Fig. 1 (a) where we clearly demonstrate that each resolution choice ended up with almost the same linear relationship between σ and the reduction factor. Consequently, this relationship can be captured by a simple rule of thumb (RoT); Convolving an image with a Gaussian kernel results in resolution reduction (in each dimension) by a factor of almost 2σ. The black bold line in the plots shows this rule of thumb against the empirically determined red lines (and dotted line for confidence interval) for different resolutions. Furthermore, a notable observation emerges in terms of perceptual appropriateness: the SSIM, as a similarity measure, exhibits superior alignment with the anticipated $2\times$ rule of thumb, in comparison to the MSE.

B. Optical limits, acuity and effective resolution. The maximum degree of spatial partitioning discrimination in the eye's object space is referred to as visual acuity (27). The standard definition of ordinary human visual acuity, also called *letter acuity*, is said to be matched when the foveal resolution reaches a 20/20 Snellen Fraction (SF) (or 6/6 internationally). For instance, an optical system that is able to achieve double this acuity level is described as 20/10 or half of this acuity as 20/40. Acuity can be expressed in terms of cycles per second (cpd) where the cycle period is the minimum distance between the two peaks of a periodic signal (typically sinusoidal) with high contrast. Foveal acuity (F) is simply a linear function of the SF and can be given as $F = 30$ cpd $\times$ SF.

In our work, the receptive field was partitioned into two distinct regions: the photoreceptors inside the fovea (IF) and those outside the fovea (OF). To maintain simplicity, our analysis solely focused on the cones (with the minimal assumed impact of rods). Notably, when it comes to long-range viewing, the significance primarily lies within the inner portion of the fovea. The summarized assumptions regarding the theoretical derivation of the mapping between effective resolution and physical distance can be found in Table 1.

In addition to these assumptions, we also assume clear atmospheric conditions that do not lead to any refraction outside the human optical system. We did not take into account the effect of rods and evaluated performance in illuminated conditions to maximize the perceived acuity. The effect of hyperacuity such as Vernier acuity is not taken into account during our experiments as they are not specifically designed for testing hyperacuity dynamics as a function of distance (For instance, there is no displacement in pixels or counters that marks the boundaries of presented faces). In fact, hyperacuity depends on the neural visual system's power to extract small distinctions within the spatial patterns of the optical picture on the retina, whereas conventional acuity is primarily constrained by the eye's optics and retinal mosaic. Finally, we would like to remark that hyperacuity is more related to location rather than resolution. Thus, its effect is presumed to be quite minor as far as the objectives of the study are concerned.

	Outside Fovea (OF)	**Inside Fovea (IF)**
Object Size/Observation Distance	The object's image falls on both the inside and outside the fovea. This scenario mostly includes near-distance viewing.	The object's image falls on the fovea region. This scenario mostly includes far-distance (>4feet) viewing.
Neurophysiology	Varying visual acuity as a function of eccentricity (centered around the region of interest -ROI). This is typically modeled based on an ADF whose parameters are found through empirical means. Non-uniform cone and rod distributions.	Constant acuity inside the fovea (examples include 20/20, 20/40, etc. . .). Uniform cone and rod distributions.
Gaze Directions/frequencies	Multiple and frequent gaze direction shifts. These shifts are sufficiently separated to allow neurofusion/splining of multiple images in the higher levels of visual cortex.	Approximately a single gaze direction (or very close multiple gaze directions) and rare gaze shifts (saccades). No or only minor fusion/splining in the brain.

Table 1. Two regions of the receptive field on the basis of the fovea's anatomy.

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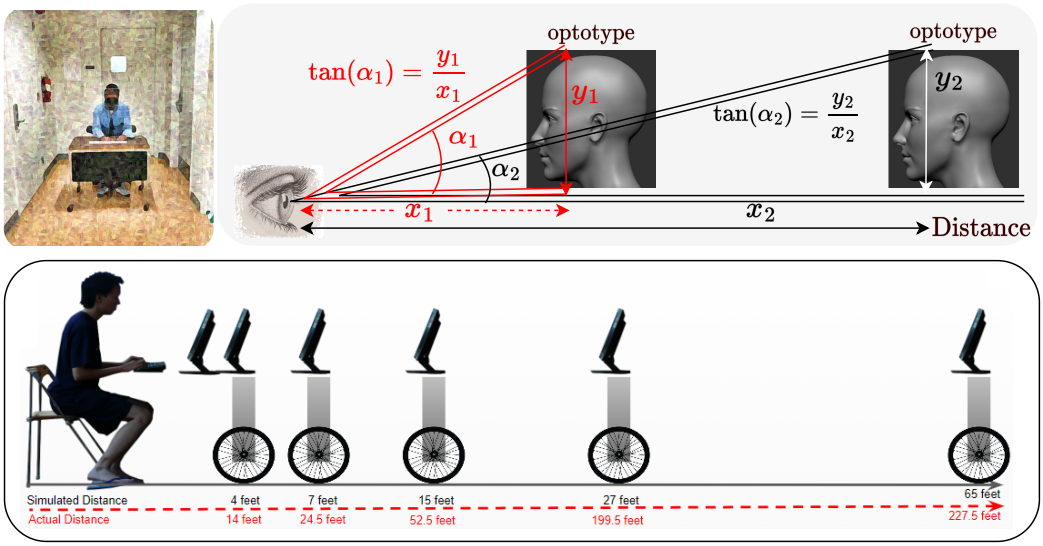

Fig. 2. Distance and size of the optotype (face) determines the angular resolution (sight angle). Through basic trigonometry, effective resolution can be computed roughly both in terms of cpd and dots/pixels per unit distance. The relationship between the viewed face image, the distance between the eye and the optotype, and the subtending angle naturally follows a triangular configuration, leading to an arctangent relationship.

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The interior foveal region (fovea pit etc.) manifests a non-homogenous distribution of cone density, which leads to varying degrees of acuity both inside and at the periphery of the foveal region. The effective resolution values (expressed in terms of pixels) are calculated in general based on an Acuity Distribution Function (ADF) and the distances resulting from a standard geometry using angular resolution between the optotype (for example faces) and the eye's retina (fovea pit in particular). We have estimated that an inch-long interpupillary distance ends up landing on the fovea with $\sim 2^o$ angular resolution (threshold angular resolution (TAR)) at around 2.1 feet distance. To make sure that the entire face (inter-temple distance of around 2 inches) will land on the fovea with high probability, we set our minimum viewing distance in our experiments between the optotype and fovea to be around 4 feet. One of the other reasons to choose our minimum distance to be a bit far from 2.1 feet is because of near-distance non-linear effects, such as refraction index of the lens and harder fusion process of different image parts of a binocular vision which may require different gaze directions to pick up necessary information.

We have originally assumed a non-uniform cone distribution inside the fovea (including the fovea pit) and the effects of rods to be minimal (as stated in Table 1). However, as we shall demonstrate that a uniform cone distribution might be a good rule of thumb under certain conditions. We have also assumed 20/20 acuity which corresponds to around 1arcmin ($\sim$30 cycles per degree (cpd) - Nyquist limit max. angular resolution) inside the fovea and calculated the resulting effective resolution for distances greater than 4 feet up to 50 feet (with constant fovea size, uniform cone distribution and 1 arcmin angular resolution, corresponding to max 71.61px and min 5.73px values, respectively). We note that the model is able to accommodate different acuities as well such as 20/10 and 20/40. We finally remark that, at all distances larger than 4 feet, the faces chosen as optotypes will always land on or inside the foveal region, particularly the pit region where the photoreceptor density is the highest.

C. Modeling the Effective Resolution via Acuity Distribution: An improved Model. In order to holistically capture the peculiarities of the human acuity, it is necessary to consider peripheral acuity in addition to foveal acuity. Acuity Distribution Functions (ADF) are introduced to describe angular resolution variation over the retina as a function of gaze eccentricity (28). We have modeled the acuity degradation (or angular displacement from the center of gaze fixation) according to the following ADF function for gaze eccentricities $e > e_0$ (29),

$$ADF(e) = \frac{S}{e - e_0 + \frac{S}{F}} \qquad [1]$$

where $e_0 = 2^o$ is the average TAR assumed, S is the roll-off slope at the peripheral region (cpd/^{o}) and assumed to be 65 cpd/^{o} in our work. We would like to remind that previous empirical data shows that this parameter is typically between 55 and 80 (30). We will be adjusting this parameter based on the data we collected in our experiments

and 65cpd/^{o} is found to be a reasonable choice for the collected dataset. Finally, F is the acuity at 0 degrees gaze eccentricity ($e = 0$), which is assumed to be 30cpd for 20/20 normal vision acuity. For constant cone distribution inside the fovea, we would assume $ADF(e) = F$ for $e \leq e_0$. However, constant cone distribution is recognized to be an oversimplification of the long range human visual experience (31). As a result, we recommend implementing a more concentrated cone distribution in the fovea pit for $e \leq e_0$. To achieve this, we begin by searching for the correct SF β that will satisfy the equation given below

$$B^{\frac{S}{F}} - B^{\frac{S}{30\times\beta}} = e_0 \qquad [2]$$

where the selection of "base B" depends on the available acuity. A good rule of thumb used in this study is given by $B = 2\times$ SF. Let us denote the solution to above equality as β^*, then the ADF function for $e \leq e_0$ can be described as

$$ADF(e) = \frac{S}{\log_B\left(e + B^{\frac{S}{30\times\beta^*}}\right)} \qquad [3]$$

where exponentiation is introduced to model the cone packing, density of which wanes from the central pit of the fovea to the foveal avascular zone and finally to the outer periphery that extends to the macula.

Since we assume no atmospheric refraction, we hypothesize that the light emitted from an optotype can be represented by a straight line. In Fig. 2, through standard trigonometry, we observe that there is an arctangent functional relationship between the viewing distance (x), object/optotype size (y) and the viewing angle α. Let d be the inter-pupil distance and D be the physical distance between the optical system and the optotype. Then using the trigonometric arguments, we can estimate the gaze eccentricity in terms of degrees as

$$e = \arctan\left(\frac{d}{D}\right) \qquad [4]$$

Another way to express effective resolution is in terms of dots/pixels per unit distance. According to the Nyquist-Shannon sampling theorem (32), to be able to perfectly reconstruct a full-spectrum signal, we need to sample the signal at least twice the highest frequency content of the signal unless the frequency spectrum of the signal shows sparsity. We measure frequency in terms of cpd in our context and hence the minimum sampling frequency that would allow reconstruction without *aliasing* is given by $2 \times AFR(e)$. Accordingly, we can compute the effective resolution (ER) in terms of pixels as a function of distance (D) as follows,

$$ER(D) = \frac{d}{D \times \tan\left(\frac{1}{2\times ADF(e)}\right)} = \frac{d}{D \times \tan\left(\log_B\left(\arctan\left(\frac{d}{D}\right) + B^{\frac{S}{30\times\beta^*}}\right)^{\frac{1}{2\times S}}\right)} \qquad [5]$$

In Fig 3 (a), we have provided the acuity (cpd) as a function of eccentricity (degrees) for three different SFs, namely 20/15, 20/20 and 20/30 for both uniform and non-uniform foveal cone distributions. As can be seen the eccentricity axis is in logarithmic scale to magnify the difference of the two assumptions in the foveal region which is assumed to be below $e_0 = 2^o$ angular resolution. On the right, in Fig. 3 (b), we have plotted $ER(D)$ function output as a function of distance in feet for 20/20 acuity and uniform foveal cone distribution for two different values of S. As can be seen for close viewing ranges, particularly smaller than 2.38 feet, the effective resolution is influenced by the near-range effects for practical values of S such as 75.

3. Methods

A. Subjects. We have collected our data from twenty normally-sighted individuals. Our pool includes 11 females, 2 non-binary and 7 males (ages ranging from 18 to 59 years: An average of 28.4) from an external circle of friends/students/unfamiliar individuals who are paid to participate in the experiment. Clinical Snellen charts as well as Freiburg Visual Acuity Test (FrACT)* (33) were used to evaluate each subject's visual acuity (in logMAR units), which was shown to yield results that concur closely with traditional means. Acuity tests were measured to be around 20/20 with only minor variations between them (varying between 20/11 and 20/26). Additionally, the Pelli-Robson charts were used to evaluate each subject's contrast sensitivity to compare with FrACT. The experiments take place within a well-lit long corridor (with a minimum range of 65 feet), wherein various data points are recorded. These include the responses indicating correctness, the time elapsed between the onset of stimulation and key pressing

*Available for Macintosh and Windows free of charge at http://www.michaelbach.de/fract.html

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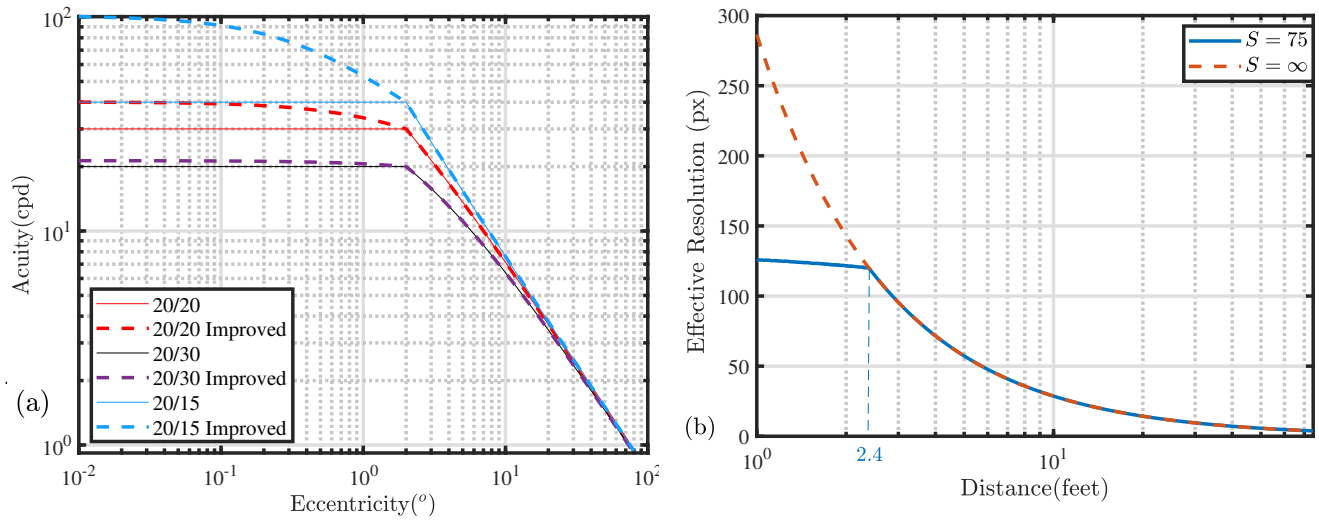

Fig. 3. (a) Here we plot acuity (resolvable frequency) in terms of cpd as a function of eccentricity (in degrees). (b) Effective resolution function output $ER(D)$ as a function of viewing distance D expressed in terms of feet and plotted in logarithmic scale. The plot also shows the effect of the parameter S on the effective resolution in pixels.

(response time - exposure duration), and the sequence of images presented to the subjects. Additionally, several metadata parameters, such as age, gender, experiment time, and display configuration (including luminance), are also gathered. The experiment was conducted in a controlled setting, and the participants were instructed and monitored throughout the experiment. The study conformed to the Code of Ethics of the World Medical Association (Declaration of Helsinki) and the experiments were approved by an Institutional Review Board (IRB) at the Massachusetts Institute of Technology, Cambridge, MA, USA. Each individual provided their written, informed permission prior to testing.

B. Instrumentation. We have utilized the **PsychoPy** platform for implementation, which is a free platform relying on Python-based frameworks. A 23.7-inch LG UltraFine 4K Display monitor (3840×2160 native resolution) at 60Hz refresh rate is leveraged to create 187 pixels interpupillary distance in the face images presented on the screen. The original set of images (100 identities, only male men are included) are selected from the Chicago Face Database (26). The only source of light pertaining to the presentation of stimuli in the test environment was the display monitor with adjusted luminance above 200 candela per square meter (cd/m^2) – An average of 245 for 20 trials. The participant was positioned at one end of a well-illuminated corridor with their chin resting on a chin-rest (see also Fig. 2). A table was set up in front of them, equipped with a keyboard to enable them to react to the stimuli. The subject's best refractive correction was used to view the stimulus display binocularly through the chin rest. The presentation display is gamma-corrected before the experiments.

C. Experimental Protocol Description. In our experimental design, we aimed at finding the distances at which human subjects can differentiate different quality images degraded with Gaussian blur through a task-based interaction. The monitor was placed on a cart at the furthest distance from the participant (65 feet with the physical available space. See Fig. 2). We presented 2×2 arrays of 4 images (all of the same person, only one of the four is blurred (see example shown in Fig. 4 (b)), each image size is 1360×957 pixels such that inter–pupil distance is approximately 1 inch, around 187 pixels on the display screen), and participants are given a task to identify which of the 4 images seemed blurrier than the rest (forced-choice paradigm) without time restriction. We collect responses and recorded the total time taken to generate these responses. Once completed (satisfying a certain statistical condition – Binomial test), the monitor was moved closer, to the next distance point, and the arrays of images starting from the last failed blur level were presented again. This way, we reduced the likelihood of missing any potential perceptual threshold of quality degradation. To control the bias, we used a randomized block design, in which the order of image presentation was randomized for each participant. We also leveraged a within-participant design, in which each participant saw every image, to ensure that the results were consistent across subjects. The location of the blurred image, within each array, were also randomized at every distance point. Across the arrays, there were 16 blur levels (See also Table 2) with 6 repetitions for each, with a different but fixed set of faces. The process that led to the choice of blur levels that are used in our experiment is detailed in the next subsection.

In Fig 5, we have provided the flow diagram of the experimental logic in detail. We primarily begin with the largest distance (=65 feet) and $\sigma = 46.8$ and decrement them based on the responses to the blocks of 6 consecutive

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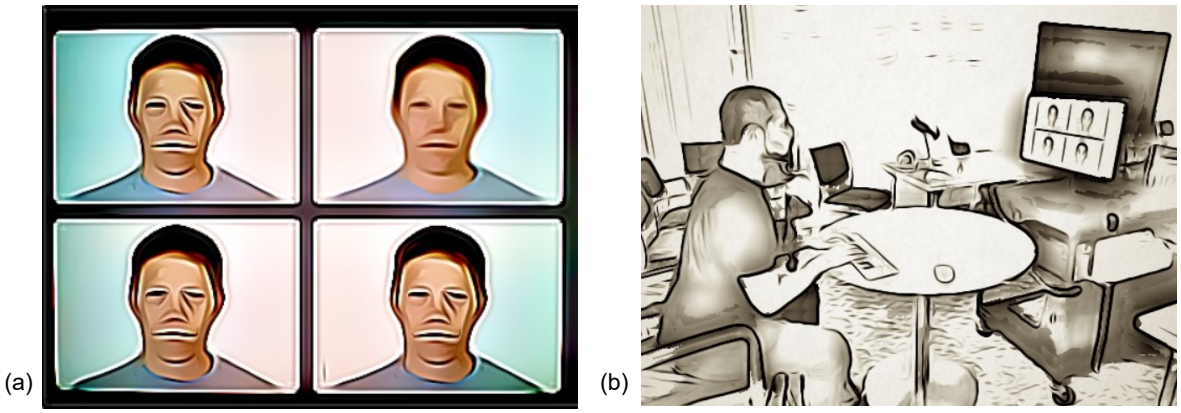

Fig. 4. (a) 4×4 Image matrix presented to the participant where the blurred image's location is randomized. For this example it is on the top right of the quadrant. (b) Participant viewing the displayed images at a given distance with chin rest, completing the selection task, which can or wrong decisions.

image queries in each block. *Passes* and *Failures* are decided based on an online Binomial test which will be detailed in subsection E. In case of failure, the buffer in the diagram is leveraged to store the results of the subjects' responses from the previous block of test images which are used to decide on passing/failing on to the next distance instance based on a threshold p value. Once the subjects are able to pass the block, we do not go back and check again to increase our confidence. This practice is shown to dramatically reduce the experimentation time. In our experiments, the threshold p value is chosen to be 0.01. This implicitly implies 5 or more successful responses in the first trial would be a hard pass, whereas less than two successes would lead to a hard failure. If the subject responds to 2, 3 or 4 queries successfully in the first trial, then a second trial is executed in which a total of 8 (considering both consecutive trials which amounts to 12 trials) or more successes would eventually lead to a final pass decision, otherwise a failure will be reported.

In Fig. 4 (a), we have shown an example 4×4 image matrix where the top-right image is degraded with blur whereas the the rest of the images are original, separated by a spacing of 0.35 inches. We also show in 4 (b) how the subject is exposed to these images with the help of a cart simulating the physical distances. For navigation between the locations of presented images, we have labeled four keys in the keyboard, namely, "e" for bottom-left, "f" for top-left, "j" for bottom-right and "o" for up-right for subjects to use and point their choice in the query image space.

D. Selection of Distance Samples. Having established the theoretical relationship captured by the ADF, we use exponential sampling (34) on the effective resolution axis to sample 15 distinct points and eventually find the corresponding 15 distance samples utilizing the inverse function $EF^{-1}(.)$ to be used in our experiments. Note that we might have sampled the effective resolution axis uniformly but that has given a pretty skewed distribution of distance samples towards a shorter range (close distance) due to steep roll-off characteristics of the arctangent functional

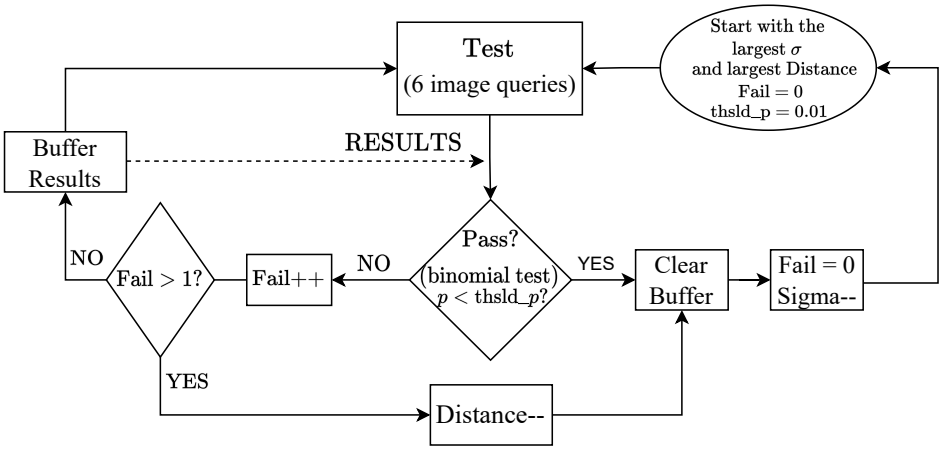

Fig. 5. Logical flow diagram of the experiment conducted.

Pixels	Pixels (rounded)	Distance (feet)	Distance (inches)	Distance (inches, /16)†	Reduction Factor (reducing from 187px width)	RoT Gaussian Sigma‡
71.6197	*72*	*4*	*48.0*	*48" 0*	*2.61*	*1.3*
58.1093	*58*	*4.93*	*59.2*	*59" 3*	*3.22*	*1.6*
47.1959	*47*	*6.07*	*72.8*	*72" 13*	*3.96*	*2.0*
38.4535	*38*	*7.45*	*89.4*	*89" 6*	*4.86*	*2.4*
31.4122	*31*	*9.12*	*109.4*	*109" 7*	*5.95*	*3.0*
25.7625	*26*	*11.12*	*133.4*	*133" 7*	*7.26*	*3.6*
21.2050	*21*	*13.51*	*162.1*	*162" 2*	*8.82*	*4.4*
17.5324	*18*	*16.34*	*196.1*	*196" 1*	*10.67*	*5.3*
14.5791	*15*	*19.65*	*235.8*	*235" 13*	*12.83*	*6.4*
12.2062	*12*	*23.47*	*281.6*	*281" 10*	*15.32*	*7.7*
10.2976	*10*	*27.82*	*333.8*	*333" 13*	*18.16*	*9.1*
8.7608	*9*	*32.7*	*392.4*	*392" 6*	*21.35*	*10.7*
7.5251	*8*	*38.07*	*456.8*	*456" 13*	*24.85*	*12.4*
6.5302	*7*	*43.87*	*526.4*	*526" 7*	*28.64*	*14.3*
5.7296	*6*	*50*	*600.0*	*600" 0*	*32.64*	*16.3*
2.0000	2	>50§	NA	NA	93.50	46.8

Table 2. One-to-one relationship between Effective Resolution, distance and Gaussian Blur (σ).

relationship. In addition, having many samples in the short range also led to the parameter of the Gaussian blur (σ) to be the same for some of the samples (due to close–enough sampling and rounding to one digit beyond the decimal point). To be able to have much wider coverage of distance samples for the long range, we have used exponential sampling which samples lower resolutions (farther distances) more heavily than high resolutions (shorter distances). Since in our study we are more interested in longer ranges, typically set to be higher than 4 feet, sampling long distances more heavily provides better resolution to the estimation process. The parameter of the exponential sampling, called "exponentialliness" (Φ) is set to 20 in our case (34), where the sampling function that uses this parameter can be described more specifically by

$$expSampling(x, \Phi) = \frac{mx - mn}{\Phi} \times (10^x - 1) + mn \qquad [6]$$

where x is selected from the range $[0, \log_{10}(\Phi + 1)]$ uniformly, mx is the maximum limit of the range (71.61px in our case) and mn is the minimum limit of the range (5.73px in our case). Note that as exponentialliness tends to unity ($\Phi \to 1$), our sampling converges to uniform sampling on the effective resolution axis with lower and upper limits $[mx, mn]$. Accordingly, we select our distances using exponential sampling and they are shown in Table 2. Note that reduction factor in resolution is assumed to be 2 as argued in the previous section.

E. Statistical Significance: Binomial Test. In a Binomial test, the null hypothesis is about finding the target response being purely a chance game, which could occur with probability $\frac{1}{n^2}$ for a $n \times n$ array of image presentations. Accordingly, in a one-tailed binomial test, p-value is defined to be the probability of finding the observed number of successes (s) or a higher value, given that the null hypothesis is true. More specifically, we have

$$p \triangleq 1 - \sum_{i=0}^{s-1} \binom{m}{i} \left(\frac{1}{n^2}\right)^i \left(1 - \frac{1}{n^2}\right)^{m-i} \qquad [7]$$

where m is the total number of queries in an experiment. One of the challenges to tackle for calculating the p value is that the average number of successes for multiple participants need not be integers. For example, in the case of multiple participants, the unbiased estimator for the accuracy of success is typically chosen to be the mean value, which might not necessarily be an integer. In order to address non-integer means, the utilization of Newton's binomial theorem (NBT) is employed (35). When dealing with a non-integer value represented as s, and to ensure numerical stability, we employ the incomplete beta function, which is equivalent to NBT, for the computation of the p value. In

†"Distance (inches, /16)" - this is the inch distance easier to use with a ruler/measuring tape.
‡The Gausian sigma is calculated by Factor/2 as a rule of thumb (as explained in the previous section).
§This distance was not derived from our model, but the estimation is. We added it to test our lowest boundary.

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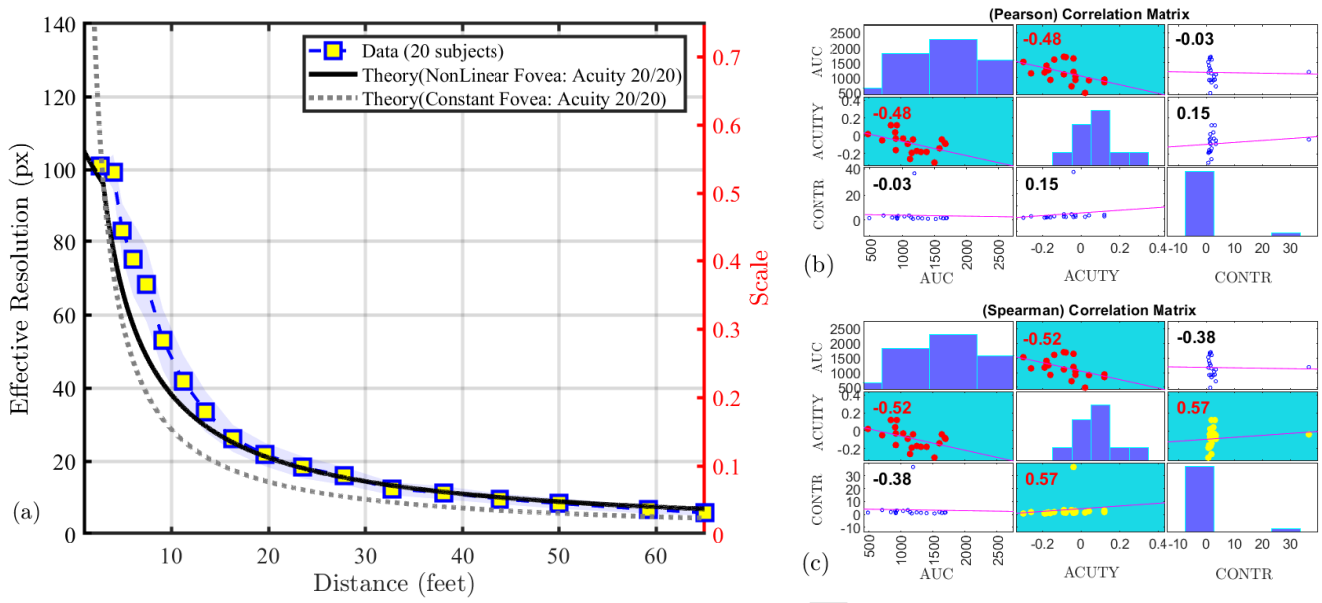

Fig. 6. (a) The relationship between effective resolution and distance (in feet) is depicted. The subjects' data is represented with 95% confidence intervals, accompanied by two theoretical curves: One assuming a constant fovea and the other assuming a non-linear distribution of photoreceptors, both based on SF 20/20, fovea width of 1.6^o and ADF with slope parameter $S = 55$. The same plot includes an alternative scale on the ordinate axis, representing the corresponding image size that subtends the retina. (b)-(c) Additionally, we examine the correlation between the area under the curve of effective resolution and distance (AUC) with ACUITY (in logMAR units) and contrast sensitivity (CONTR). Both Pearson's and Spearman's correlation coefficient values are provided for these analyses. px: pixels.

other words, for any real values of m, s, n and $p = \mathcal{I}_{\frac{1}{n^2}}(s, m-s+1)$, where

$$\mathcal{I}_x(z,w) = \frac{B_x(z,w)}{B_1(z,w)} \text{ with } B_x(z,w) = \int_0^x t^{z-1}(1-t)^{w-1}dt. \quad [8]$$

Suppose that $n = 2$, and we conduct m trials where we aim to achieve statistical significance at a threshold of 0.01. If we have four or more successes, the resulting p-value would be 0.005. However, if we only have three or more successes, the p-value would be 0.169. This means that we would need at least four successes to meet the required statistical significance. Similarly, if we were to perform 12 trials and aim to reach a threshold of 0.01, a minimum of 8 successes would be required. This is because if we obtain 7 successes, the resulting p-value would amount to 0.0143. However, with 8 successes, the p-value would decrease to 0.00278, surpassing the significance threshold of 0.01.

4. Experimental Results

A. Main Result: Available Effective Resolution. We begin our results by establishing the fundamental relationship between the effective resolution and physical distance (in feet) in Fig. 6 (a). Our illustration shows the mean performance of 20 subjects with 95% confidence interval. Note that based on the discrete test distance samples, we find an interval in which the effective resolution actually lies. Thus, the data points for each participant in the plot are the mean of the upper and lower resolution limits that are listed in Table 2. For instance, if the subject, at distance 133.4 inches, stumbles upon between 31.41 and 25.76 pixels of effective resolution, the data point (average) for that distance is computed to be 28.55 for that participant. The same result is complemented by two theoretical curves: One assuming a constant fovea and the other assuming a non-linear distribution of photoreceptors (with $S = 65$, $B = 2.1$), both based on SF 20/20. The same plot includes an alternative scale parameter on the right ordinate axis, representing the relative image size for a given distance. More secifically, the scale of the image that falls onto the retina is calculated based on the ratio of the effective resolution to the interpupillary distance of 187 pixels on the display screen. This way, we effectively illustrate that if one is to use scaling to replicate physical distance, the corresponding available effective resolution can be easily determined (read off) from the shared left ordinate axis of the same plot.

The obvious observation is that the proposed fovea physiology model serves as a more accurate descriptor for the functional relationship between effective resolution and distance, encompassing both short and long ranges. However,

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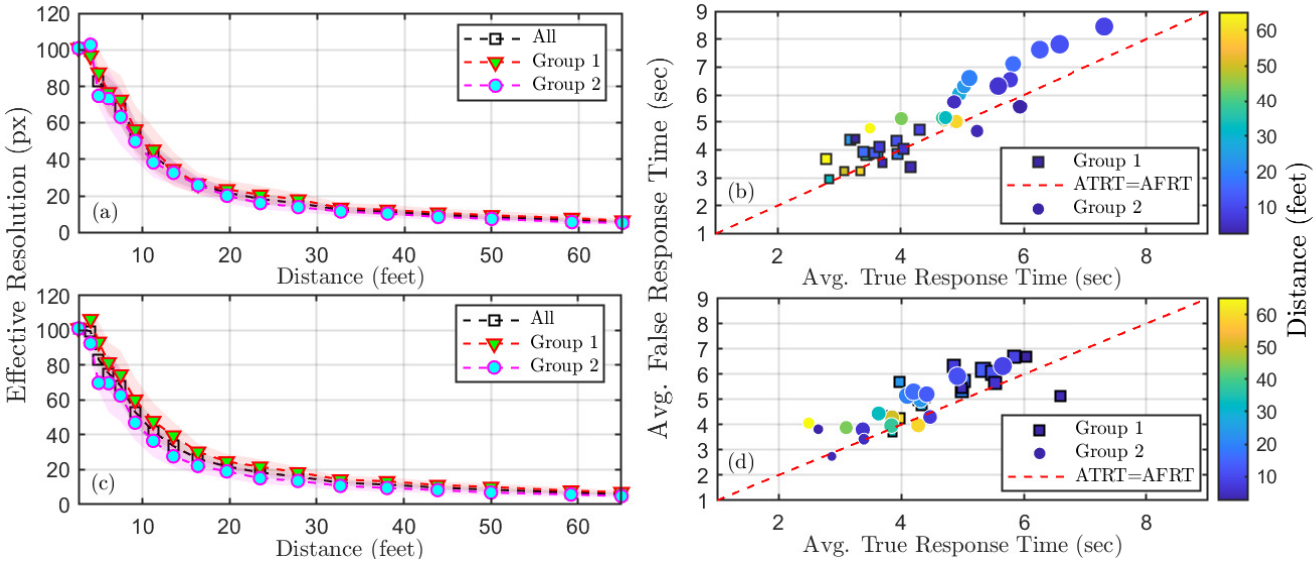

Fig. 7. (a) The effective resolution, in relation to distance (measured in feet), for two groups of participants who were clustered based on their error patterns. (b) The average true and false response times (ATRT and AFRT, respectively), varying with distance (measured in feet), exhibit almost linear covariation, situated a little above the ATRT=AFRT line. The data is partitioned by clustering the participants' error performances. (c) Effective resolution versus distance for two groups of participants who were clustered based on their acuity. (d) Same plot as in (b) for acuity-based clustering of participants.

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it is noteworthy that for shorter distances, subjects surpassed the predictions of both theoretical models, primarily due to the synergistic impact of parafoveal perception and foveal acuity. This implies that further refinement of the theory may be required to provide a more comprehensive explanation for the observed outcomes.

In Fig. 6 (b)-(c), we present a correlation analysis. Primarily, we leverage the area under the curve (AUC) of the functional relationship between effective resolution and distance as a performance indicator. Our investigation presents the potential correlations between AUC, acuity (measured in logMAR units), contrast sensitivity (CONTR), age, and monitor luminance. Notably, we find that statistically significant correlations are observed solely between AUC, acuity, and contrast sensitivity. The corresponding Pearson's and Spearman's correlation coefficient values are presented within the same visual representations for these analyses. As anticipated, enhanced acuity corresponds to higher AUC, indicating a positive association. Interestingly, subjects demonstrate nearly identical contrast sensitivity levels, despite exhibiting dramatic variations in their detection performance.

B. Error Patterns, Acuity and Strategies. In order to shed light on the performance discrepancies observed among the participants in our experiments, we conducted additional analysis to investigate the following question: "Do subjects employ different strategies based on the viewing distance?". Multiple trajectories could be explored to evaluate behavioral patterns that are most indicative of subjects' strategies aimed at maximizing the likelihood of accuracy. Two possible trajectories to consider are (1) error patterns and (2) average latencies of true and false responses. Our hypothesis is that if subjects differ in their strategy to choose the right option, it should be reflected upon the error patterns they are generating. Thus, we focus on the former trajectory by clustering the error patterns of all participants. To accomplish this, we aggregate each subjects' responses to create the confusion matrix as a 16-dimensional feature vector for each individual, and employ k-means clustering while optimizing the number of clusters based on the *Calinski-Harabasz* and *Silhouette* criteria[¶]. Following the clustering process, we analyze each class separately and compare their AUC and response latencies.

We have observed the presence of two distinct groups among the participants, each exhibiting identifiable differences in their strategies. In Fig. 7 (a), we have plotted the effective resolution against physical distance in feet for both Group 1 and Group 2. It is evident from the plot that both groups perform similarly well in the blur-detection task. To further explore the potential variations in strategies adopted by these groups, we conducted an analysis comparing the average response latency for True and False responses for each group. This relationship, depicted in Fig. 7 (b) with markings (circles and squares) representing the groups and color-coded data points representing specific distances, reveals interesting insights. Group 1, compared to Group 2, appears to allocate less time to the response generation process while achieving a similar or better AUC performance. This indicates that Group 1 employs a more

[¶] Five clusterings are conducted, and the final cluster labels are determined through Majority voting. In all instances, it was found that the ideal number of clusters is two, with each group consisting of 10 individuals, resulting in equally sized clusters.

efficient strategy, achieving comparable results in less time. Additionally, it is noteworthy that both groups generally spend more time on average for false responses compared to true responses which is particularly true for Group 2.

It has been observed that there is a slight distinction in the average acuity levels between these groups, with mean values of -0.132 and -0.038 in units of logMAR, respectively. In order to demonstrate that the discrepancy between the groups is not solely due to acuity (physical advantage), a separate clustering analysis based solely on acuity was conducted, resulting in the equal partitioning of subjects. The threshold for this partitioning turns out to be -0.085 logMAR. In Figure 7 (c) and (d), the effective resolution as a function of distance and the average response times for true and false responses are illustrated for the acuity-based groupings. It can be observed that there are more significant differences in AUC performances, which aligns with the predictive model that utilizes acuity as a parameter. Additionally, Figure 7 (d) clearly indicates that clustering based on acuity does not lead to easily distinguishable subject groups, suggesting that latency performance is not solely determined by acuity but also influenced by subsequent higher order processing and associated strategies.

By employing both clustering methods, we conducted a comprehensive analysis, comparing AUC, Average True and False response times, contrast sensitivity, Acuity, and Age across different groups. The findings are presented in a star plot depicted in Fig. 8. First and foremost, it is apparent from the plot that the average time devoted to making accurate and erroneous decisions on the queries predominantly reflects the manifestation of these distinct strategies. Additionally, the star plot unveils intriguing insights, indicating that clustering based on error patterns (Fig. 8 (a)) exposes distinct strategies adopted by various age groups, regardless of their acuities and contrast sensitivities being similar. Conversely, when clustering is solely based on acuity (Fig. 8 (b)), the star plot reveals a positive correlation between higher acuity/contrast sensitivity and the improved AUC. In this clustering scenario, the groupings exhibit less distinction in terms of average group age. However, an intriguing observation emerges as the group achieving better AUC also requires more processing time, which is not the case when the clustering is performed based on error patterns. The latter can be attributed to the varying levels of confidence exhibited by the two distinct groups, which are characterized by their unique error patterns, leading to differences in the generation of true and false responses.

In order to examine the development of adapted strategies in relation to distance, we conducted a statistical analysis (correlation) of the average response latencies for true and false responses in both groups. Fig. 8 (a) and (b) also display bar plots indicating the average and standard error of latencies for expanding viewing ranges of $0-8$, $0-15$, $0-40$, and $0-65$ feet. It is worth noting that in our experiments, 15 feet corresponds to approximately 50 feet for real-size faces, which is considered the crucial initial recognition step marking the end of the social space (36). As observed, the differences between the groups become progressively more noticeable when clustering is performed based on error patterns, while the distinction remains consistently insignificant when clustering is based on acuity. Another intriguing finding is that the groups with a weaker statistically significant correlation between true and false response latencies demonstrate higher performance in terms of AUC. This suggests that the failures observed may be attributed to the adoption of strategies that differ from those employed during making accurate blur detection decisions.

5. Discussions

In our study, we focused on testing the performance of human blur-detection task using a limited database of male faces. However, it remains to be explored whether the relationship between effective resolution and physical distance applies to objects and natural scenes in a general sense. While it is expected that image stimuli may not significantly impact the blur-detection task at larger viewing ranges, the situation might be different at close ranges. Factors such as contrast differences, specialized processing, face recognition peculiarities, and object choices can influence performance and lead to variations in decision-making processes and strategies employed. Despite conducting a computational experiment comparing the spatial frequency distribution of identities presented to different groups, no significant differences were observed. We believe that this particular outcome has the potential to serve as an initial foundation from which to embark upon a more extensive exploration on the interplay between the contextual content of stimuli and its impact on the intricacies of the blur-detection task.

As highlighted within the main content of the manuscript, our theoretical model heavily relies on several foundational assumptions grounded in the physics of light propagation, such as the assumption of rectilinear light paths, a functionally defined distribution of cones adhering to a packing density, characterized by the acuity distribution function, and the negligible influence of rods, among others. Within the framework of these assumptions, we have proposed a few improvements, notably by incorporating a non-uniform distribution of cones within the fovea, specifically within the foveal pit, and by determining the parameters of this function based on prior research (37), resulting in a more accurate alignment with the collected empirical data. However, despite these refinements, a disparity persists between our predictive model and the experimental data, particularly evident in short-duration viewing conditions associated with the peripheral vision encompassing the parafoveal region. Given that this discrepancy primarily manifests in the

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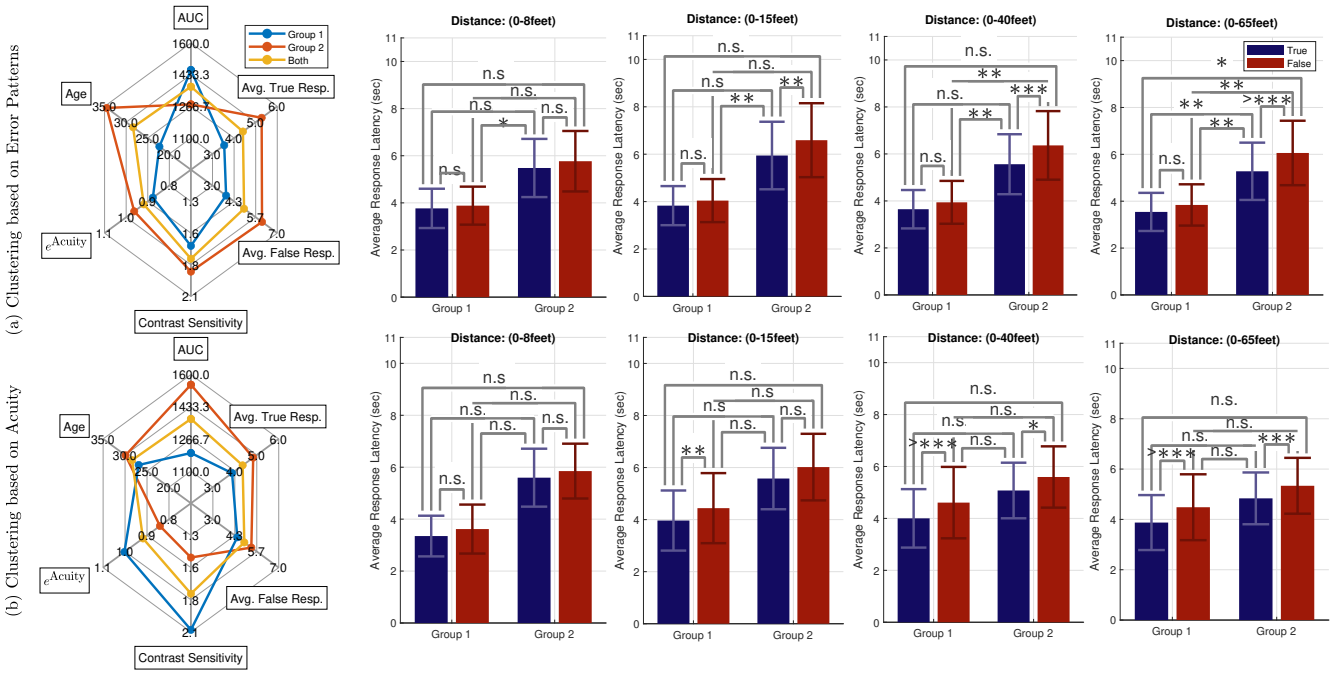

Fig. 8. (a) The first row displays a star plot representing AUC, Avg. True Response time, Avg. False Response time, contrast sensitivity, Acuity (more accurately e^{Acuity}: closer to 0, better the acuity), and age for the two groups identified through error pattern clustering. Additionally, the top row includes a bar plot illustrating statistical tests on average response latency for true and false responses separately using expanding windows of data (covering the first 8 feet, 15 feet, 40 feet, and 65 feet) over time. (b) The identical set of plots derived from clustering based on subjects' acuities.

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peripheral region, we posit that it may be attributed to the non-additive effects arising from the combined influences of foveal and parafoveal vision (38). An intriguing avenue for future research could be the design and execution of additional experiments aimed at elucidating the dynamics of the aforementioned combined effects, thereby leading to the development of more refined and comprehensive mathematical frameworks.

In the previous section, we have discussed the effect of human strategies, hypothesized to reflect upon the response latency results directly. For example, we have clearly demonstrated that the differences in the errors made by the subjects cannot be explained solely by their age, acuity or contrast sensitivity. Despite the consequences of adapting different strategies are quantified, the reasons behind this visible differences are not discussed. One interesting rationale is to check as to whether there would be any difference between binocular and monocular vision as it is known that binocular summation process may improve the performance of defocus-induced blur (39). Depending on the different acuity levels of the two eyes, interocular suppression, which involves the suppression of blurred or low-contrast images in one eye by clear images in the other eye, can be observed. Later studies have shown that this supression is believed to play a role in the effectiveness of monovision correction (40), which could be helping one of the identified groups showcase a rather different behavior.

An intriguing avenue to explore the enigmatic nature of strategies adopted by humans could involve the utilization of an eye-tracking device. By monitoring and analyzing gaze movements, it becomes possible to differentiate the saliency maps generated by the two distinct groups. This analysis would involve parameters such as the frequency and patterns of saccades, the trajectories followed during the scanning, and the duration of fixations, particularly within shorter viewing distances. Naturally, such an endeavor would necessitate an examination of the smallest intentional saccade humans can accurately execute, as other microsaccadic movements are unlikely to play a significant role in the development of any strategy. Additionally, it would be of interest to investigate the threshold size at which humans cease their scanning movements, representing the maximum observation distance suitable for studying the human blur-detection process.

One immediate application of our mapping work is to alleviate the discrepancy between the rudimentary scaling image processing technique employed to emulate physical distance and the veritable information content that can be processed at a given distance. By translating the influence of physical distance on the observed stimuli into a quantification based on the information-bearing pixels, as opposed to a simplistic scaling approach, which is a recognized measure for neural network performance analysis, we can facilitate a more nuanced and meaningful comparison of neural network performance in relation to distance, capitalizing on the intricacies of the human visual

system. Ultimately, this enables a comprehensive comparative analysis of human recognition performance alongside computational tools, enriching our comprehension of the respective capabilities and limitations inherent in both domains. Furthermore, acquiring knowledge about human strategies is of utmost importance in constructing more effective training regimens for neural networks. This is supported by recent studies, such as (41), which align with our own findings, indicating that humans likely utilize not only shape and texture information, which may be compromised at longer viewing distances, but also higher-level "concepts" for various classification tasks (42). Therefore, conducting further investigations to uncover the underlying reasons behind these diverse strategies can assist us in training neural networks in accordance with the training protocols to which humans are exposed.

6. Conclusions

Main objective of our study is to determine the effective resolution (a quantitative measure of available information) of face images on the retina at various viewing distances. Through a combination of theoretical considerations and experimental tasks, we observed that the relationship between viewing distance and effective resolution is more complex than initially anticipated. Our findings revealed that human performance in detecting image blur surpasses the predictions of theoretical models based on image size, cone density, and foveal extent, particularly at closer viewing ranges. This suggests the surging need for future theoretical models to account for non-uniform cone density within the fovea and better characterization of the acuity outside the fovea. By establishing a mapping between viewing distance and perceived image characteristics, our work came to have practical implications, allowing for direct comparisons of human face recognition performance under different levels of blur and viewing distances. Moreover, it facilitates systematic comparisons between human and machine vision systems by employing resolution as a common factor. Furthermore, by examining the strategies employed by humans in the blur-detection task, we aim to explore and stimulate the development of novel training strategies for neural networks, with the goal of enhancing their generalization capabilities and improving robust recognition performance. These findings highlight the importance of considering the nuanced factors affecting effective resolution and human decision making processes with varying viewing distances and pave the way for further advancements in understanding and simulating human visual perception.

ACKNOWLEDGMENTS. This research is based upon work supported in part by the Office of the Director of National Intelligence (ODNI), Intelligence Advanced Research Projects Activity (IARPA), via [2022-21102100009]. The views and conclusions contained herein are those of the authors and should not be interpreted as necessarily representing the official policies, either expressed or implied, of ODNI, IARPA, or the U.S. Government. The U.S. Government is authorized to reproduce and distribute reprints for governmental purposes notwithstanding any copyright annotation therein.

We would like to also acknowledge Sinha Lab members for participating the pilot version of our experiments, MIT (UROP) undergraduate student Mahmoud Abdelmoneum for helping us running some of the experiments, participants of the vision sciences society conference for sharing their comments and critics.

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