Title

DISCOVERY OF DYNAMIC CONNECTIVITY STRUCTURE IN BRAIN CORTICAL NETWORKS FROM MASSIVE SPIKING DATA

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ABSTRACT

We introduce a probabilistic model to discover the dynamic connectivity structure in a network of spiking cortical neurons. The model is evaluated on ground truth synthetic data and compared to alternative methods to ensure quality and quantification of model predictions. When applied to large-scale recordings of spiking activity in a mammalian visual cortex, the model reveals the latent dynamic functional interactions in cortical networks that is typically omitted from analysis.

SIGNIFICANCE STATEMENT

Complex cognitive functions in a mammalian brain are distributed across many anatomically and functionally distinct areas and rely on highly dynamic routing of neural activity across the network. While modern methods enable recording from large neuronal populations, however development of probabilistic methods to extract dynamic interactions is lagging. Here, we introduce a machine learning model that when applied to large-scale recordings of spiking activity in a mammalian visual cortex, reveals the latent dynamic functional interactions in cortical networks at a cellular level. Our approach provides a conceptual link between slow brain-wide network dynamics studied with neuroimaging and fast cellular-level dynamics enabled by modern electrophysiology that may help to uncover often overlooked dimensions of the brain code.

INTRODUCTION

Information processing in a mammalian brain is distributed across many anatomically and functionally distinct areas[1]. The inter-areal functional and anatomical connectivity can be reconstructed using electron microscopy[2], gene co-expression[3], projection tracing methods[4,5], and functional neuro-imaging[6]. Further analysis of the temporal variation of neural activity across this connectome[7] using functional neuroimaging[8-11] have indicated that complex cognitive functions rely on highly dynamic routing of neural activity within this anatomically constrained structural backbone[12]. Neuroimaging, however, captures activity averaged over large populations (over 500K neurons per voxel) at relatively slow time scales (minutes to hours) that typically shows relatively low dimensionality[13] hence hindering mechanistic explanation. Further insights into dynamic routing of information flows across the brain are expected with adoption of recent technological advances in multielectrode arrays[14,15] and volumetric 2-photon imaging[16] that enable simultaneous recording from large neuronal populations at a cellular level with single spike temporal resolution that reveals rich and high-dimensional dynamic interactions[17,18]. Descriptive statistical approaches[15,19,20] that summarize the pairwise millisecond-timescale synchrony of spiking within recorded neuronal population indicate a directional flow of functional connectivity[15] ascending along the anatomical hierarchy[5] and reveal distinct engaged modules across the cortical hierarchy[20-22]. However, both descriptive statistical[15,19,20] as well as modern probabilistic models[23-25] typically extract interactions as time-independent "static" variables[15,20,26] or consider temporal dynamics of the whole population[21,22,27-30].

Here, to uncover the dynamic routing of information in cortical networks, we develop an unsupervised probabilistic model - Dynamic Network Connectivity Predictor (DyNetCP). Our approach is fundamentally different from most of latent variable models that infer the dynamics of the entire recorded population in a low-dimensional latent feature space[27-30]. Instead, to enable interpretation as directed time-dependent network connectivity across distinct cellular-level neuronal ensembles, DyNetCP extracts latent variables that are assigned to individual neurons.

RESULTS

Model architecture

Classical machine learning approaches like variational autoencoders[27] successfully train dynamic models of brain activity across entire recorded neural population. However, to uncover cellular-level dynamic connectivity structure, development of such models is becoming difficult in the absence of experimental or synthetic datasets with known ground truth (GT) to justify the choice of model parameters as well as to verify the results of model inference. To address this challenge, here, learning of the directed dynamic cellular-level connectivity structure in a network of spiking neurons is divided into two stages (Fig.1A). First, the static component, infers the static connectivity weight matrix $\mathbf{W_{st}}$ (Fig.1A, left) via a generalized linear model (GLM). Next, $\mathbf{W_{st}}$ is used to influence the dynamic offset weight term $\mathbf{W_{off}}$ learned via a recurrent long-short-term-memory (LSTM) algorithm (Fig.1A, right). The final dynamic weight $\mathbf{W_{dyn}} = \mathbf{W_{st}} + \mathbf{W_{off}}$ is averaged across all trials. Dividing the problem into two stages enables independent verification of static weights and dynamic offsets against GT synthetic and experimental data as well as a direct comparison of DyNetCP performance to existing models.

The model operates on trial-aligned binned neural spikes. We collect N neurons recorded for T time bins binned at d bin width across M trials in tensor $X \in \{0,1\}^{M\times N\times T}$, where each entry $\mathrm{x}_j^t(i) \in \{0,1\}$ represents the presence or absence of a spike from neuron j at time t in trial i. The spiking probability $P\left(x_i^t = 1 \middle| x^{t-M:t}\right)$ of neuron i at time t is modelled as follows:

$$P(x_i^t = 1|x^{t-M:t}) = \sigma\left(\underbrace{\left[\sum_{j=1}^{N}\sum_{d=1}^{M} w_{j\to i}^{d} x_j^{t-d} + b_i\right]}_{Static} + \underbrace{\left[\sum_{j\in e(i)}\sum_{d=1}^{M} w_{j\to i}^{d,t}\left(x_i^{1:t-1}, x_j^{1:t}\right) x_j^{t-d}\right]}_{Dynamic}\right) \quad \text{Eq.1}$$

where σ is the sigmoid function, $w_{j\to i}^{d} \in \mathbb{R}^{M}$ and weights $w_{j\to i}^{d,t}$ are static and dynamic connectivity weights between neuron j and neuron i, and $b_i \in \mathbb{R}$ are biases.
Given spiking data as input, the model produces two sets of output weight matrices. The first set, $\mathbf{W_{st}}$, encodes an estimate of the static network structure and contains one weight per pair of neurons averaged across the trial time. These represent the time-averaged influence the spikes of the whole population have on spiking probability of a given neuron. The second set, $\mathbf{W_{dyn}}$, contains a single weight for every pair of neurons for every point in time during the experimental trial. These weights, which are a function of the input spiking data of all neurons in a population, represent a time-varying offset to the static weights. Hence, they encode temporal changes in activity patterns, and are used to determine when a given connection is being active and when it is unused. Therefore, in this formulation, the model learns time-varying connectivity patterns that can be directly linked to the underlying network structure at a cellular level.

Static connectivity inference

The static component of DyNetCP (Fig.1A, left) learns static connectivity weights $w_{j\to i}^{d} \in \mathbb{R}^{M}$ that encode static network structure averaged over the time of the trial t. We adopt a multivariate autoregressive GLM model[24] without temporal kernel smoothing that learns $\mathbf{W_{st}}$ as a function of a time lag d. This formulation is similar to the conventional spike train cross-correlogram[15,19] (CCG) (Fig.1B, black) that can be jitter-corrected[31] (Fig.1B, red) to minimize the influence of a potential stimulus-locked joint variation in population spiking that often occurs due to common input from many shared presynaptic neurons. However, instead of constructing the statistical CCG histogram for each pair individually, the model given in Eq.1 infers coupling terms from spiking history of all N neurons jointly. The static component of DyNetCP is implemented for all neurons using a 1-dimensional convolution. Each convolutional filter contains the static weights used to predict the spiking probability for a single neuron as a function of the spiking history of all other neurons. The bias term b_i in Eq.1 is initialized to the logit function σ (i.e., inverse sigmoid) applied to the spike rate of each neuron calculated for a given time bin.

Dynamic connectivity inference

The dynamic component of DyNetCP (Fig.1A, right) is encoded within the dynamic connectivity weights $w_{j\to i}^{d,t}$ which are a function of input spike trains $x_i^{1:t-1}$ and all other $x_j^{1:t}$. Each of these weights represents an offset to the time-averaged static weight at time t for a connection at time lag d (Eq.1). Hence, assuming the spikes of neuron i at a time lag d are influenced by spikes from all $x_j^{1:t}$, the total influence applied to the spiking of neuron i from neuron j at time t is $\left(w_{j\to i}^{d} + w_{j\to i}^{t,d}\right)x_j^{t-d}$. Unlike the static weights, these dynamic weights are allowed to change throughout an experimental trial as a function of the spiking history of the connected neurons.
The architecture of the dynamic part (Fig.1C) consists of several stages including generation of Fourier features, recurrent long-short-term-memory (LSTM) model, multilayer perceptron (MLP), embedding, and positional encoding. First, we shift each spike train such that each entry lies in $\{-1, 1\}$ and then represent each spike train using Fourier features[32] that were recently introduced in the computer vision domain to facilitate the learning of high-frequency functions from low-dimensional input. Specifically, we encode every spike $x_j^i(t)$ using the following transformation:

$$\gamma\left(x_j^i(t)\right) = [\cos(2\pi b_1 x), \sin(2\pi b_1 x), \dots, \cos(2\pi b_m x), \sin(2\pi b_m x)]^T \qquad \text{Eq.2}$$

Here, we use $m = 64$ features, where coefficients $b_1, \dots, b_m$ are linearly spaced between –1 and 1. We evaluate the use of Fourier features within the model on synthetic data consisting of a simulated network of neurons, where one neuron induces spiking in a second neuron during the middle 250 ms of each trial (SM, Fig.S1B). DyNetCP without Fourier features is unable to properly localize the period where induced spiking is occurring, while the model with Fourier features can do so correctly.
The spike train features for each neuron are then input into separate LSTMs to produce an embedding per neuron per time step. Each of these LSTMs uses a separate set of weights and has a hidden dimension of 64. The LSTM embeddings are passed through two MLPs, f_{send} and f_{recv}, where f_{send}

produces an embedding which represents the outgoing neural signal to other neurons and f_{recv} produces an embedding which represents the incoming signal from other neurons. Each of these MLPs consists of one linear layer with output size 64 and a ReLU activation. For each pair $n_j \rightarrow n_i$ of neurons being modeled, the send embedding $h_{s,j}(t)$ is concatenated with the receive embedding $h_{r,i}(t-1)$ as well as a time encoding $h_T(t)$ which represents the trial time and is represented as

$$h_{T(t)} = \begin{cases} sin\left(t/10000^{k/D_\tau}\right), k \text{ is even,} \\ cos\left(t/10000^{(k-1)/D_\tau}\right), k \text{ is odd,} \end{cases} \qquad \text{Eq.3}$$

where D_τ is the size of the positional encoding which we set to 128. Note that the send embedding contains spiking information through time t, i.e., it contains information about the most recent spikes, which is necessary to properly represent synchronous connections. Importantly, the receive embedding only contains spiking information through time $t-1$ such that the output spiking probability is not trivially recoverable. Finally, this concatenated embedding is passed through a 2-layer MLP with hidden size 384 and a ReLU activation, producing the dynamic weight vector $w^t_{j\rightarrow i}(t)$ which contains dynamic weight offsets for each delay $d \in \{1, \dots, M\}$.

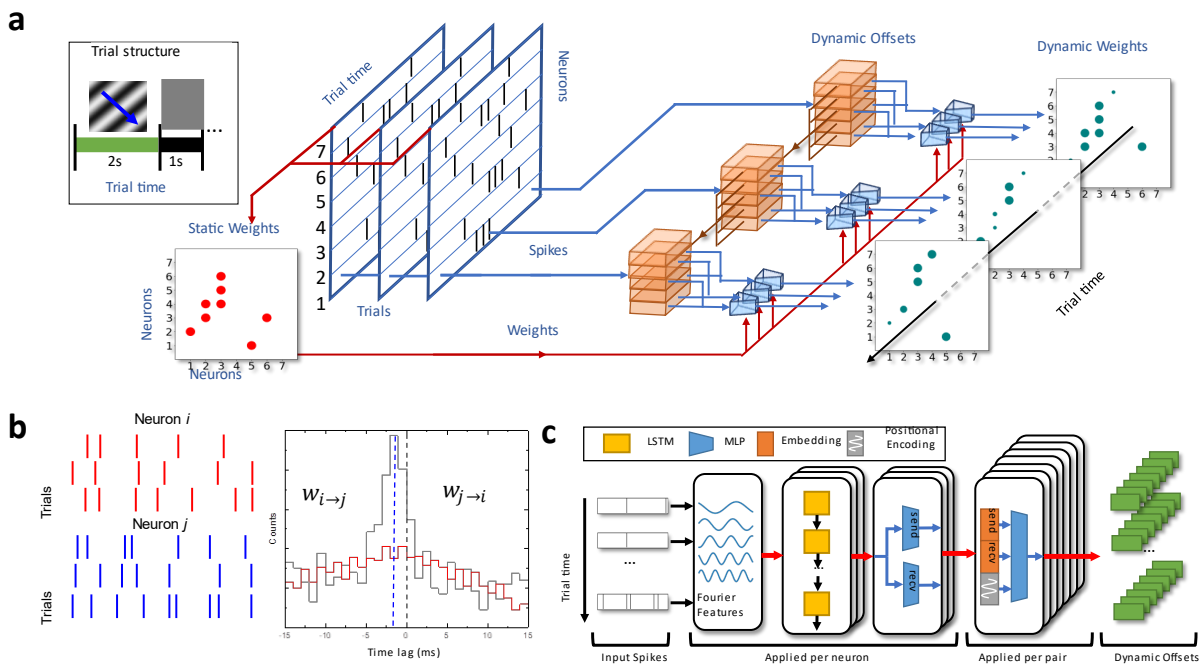

Figure 1. Model architecture and components design

A) Two-stage model architecture consisting of a static and a dynamic part. **Inset:** structure of the "drifting grating" visual stimulation trial. **B)** Schematics of spike trains recorded from neuron i and neuron j for three trials and corresponding CCG (black histogram) and time-shaffled CCG (red). **C)** Components of the dynamic part of DyNetCP model.

Performance benchmarking of static connectivity inference relative to descriptive statistics
Since DyNetCP learns the weights from spiking of all neurons jointly instead of constructing a CCG for each pair individually, it is instructive to compare the results. For this comparison, we used a subset of the Allen Brain Observatory-Visual Coding Neuropixels (VCN) database[15] that contains spiking activity collected in-vivo from 6 different visual cortical areas in 26 mice (SM, Table S1) passively viewing a "drifting grating" video (top left inset in Fig.1A). For representative pairs of local and distant units (session 771160300), the jitter-corrected[15,19,31] CCG is shown in Fig.1B, C, respectively. For a pair of local units (spatially close units from Layer 5 of the VISam area) comparison of static DyNetCP (Fig.2A, red curve) with jitter-corrected CCG (Fig.2A, black curve) shows close correspondence (Pearson correlation coefficient r_p=0.99 and p-value P_p<0.0001). Residual analysis (Fig.2A, bottom panel) shows a mean value of 0.01±0.02 SEM (Fig.2A, top right panel) that is smaller than the CCG values on the flanks (bottom right panel) (mean:0.11±0.06 SEM). An apparent time lag of the low-latency peak indicates a functional delay and defines the directionality of the connection. For such a local connection the peak is narrow with a functional delay of -2ms. For a pair of spatially distant units (units in VISam and VISp areas) a comparison of static DyNetCP (Fig.2B, red curve) with jitter-corrected CCG (Fig.2B, black curve) also shows close correspondence (r_p=0.99 and P_p<0.0001). For such a distant connection the peak is wider with a functional delay of -6ms. Further examples of comparisons of both models can be found in the accompanying Jupyter Notebook.

Performance benchmarking of static connectivity inference relative to probabilistic methods
We compare the performance of DyNetCP to a recent GLM-based cross correlation method (GLMCC)[26] that detects connectivity by fitting a parameterized synaptic potential filter (Fig.2C, magenta). For these experiments, we use the synthetic dataset consisting of 1000 Hodgkin-Huxley (HH) neurons with known GT synaptic connections[26]. We focus specifically on recovering ground-truth (GT) excitatory connections. The $\mathbf{W_{st}}$ inferred by DyNetCP for a representative pair of neurons (Fig.2C, red) reproduces well the short-latency narrow peak and the flanks of the postsynaptic potential (PSP) filter learned by GLMCC (Fig.2C, magenta). Comparing to CCG histogram (Fig.2C, black), the DyNEtCP is performing much better than GLMCC (r_p=0.67 and P_p<0.001), however the results are not as directly interpretable as GLMCC that outputs synaptic weight from the PSP fitting. Both models, however, can infer presence or absence of the connection by examining the height of the low latency peak. For the DyNetCP a putative excitatory (or inhibitory) synaptic connection can be considered statistically significant[15,19,20,26] (connection is present) when the spike rates exceed a certain threshold α_s, and the magnitude of the peak (or trough) exceeds the peak weight threshold α_w compared to the standard deviation (SD) of the noise in the flanks.

To facilitate a performance comparison, we here choose thresholds α_w, α_s, and α_p to maximize the Matthews Correlation Coefficient (MCC), which accounts for a tradeoff between recovering true positive (TP) pairs while admitting less false positives (FP) (Methods). Fig.2D compares the performance of DyNetCP and GLMCC on a synthetic dataset, while the number of spikes present for learning is varied via a threshold pair spike parameter α_p that is the number of spikes that both neurons generate in a time window of interest. Increasing α_p ensures statistically significant inference about the presence or absence of a connection[26]. As the pair spike threshold α_p increases, the MCC for both models shows a maximum around α_p=80 corresponding to the optimal balance. For a conservative value of α_w=7SD (blue), the MCC for the DyNetCP model is 63%, approaching the performance of GLMCC (68%, black). When α_w is relaxed to 5SD (red), DyNetCP recovers a larger number of TP with a reasonable increase of FP connections (SM, Fig.S3), increasing MCC up to 74%, thus outperforming GLMCC. Overall, as long as DyNetCP has access to a sufficient number of spikes for inference, it can restore GT static connectivity on par with or even better than GLMCC (Fig.2E). Importantly, as opposed to GLMCC, the formulation of static DyNetCP model provides a weight matrix $\boldsymbol{W_{st}}$ which is compatible with the subsequent inference of time-dependent dynamic weights $\boldsymbol{W_{dyn}}$.

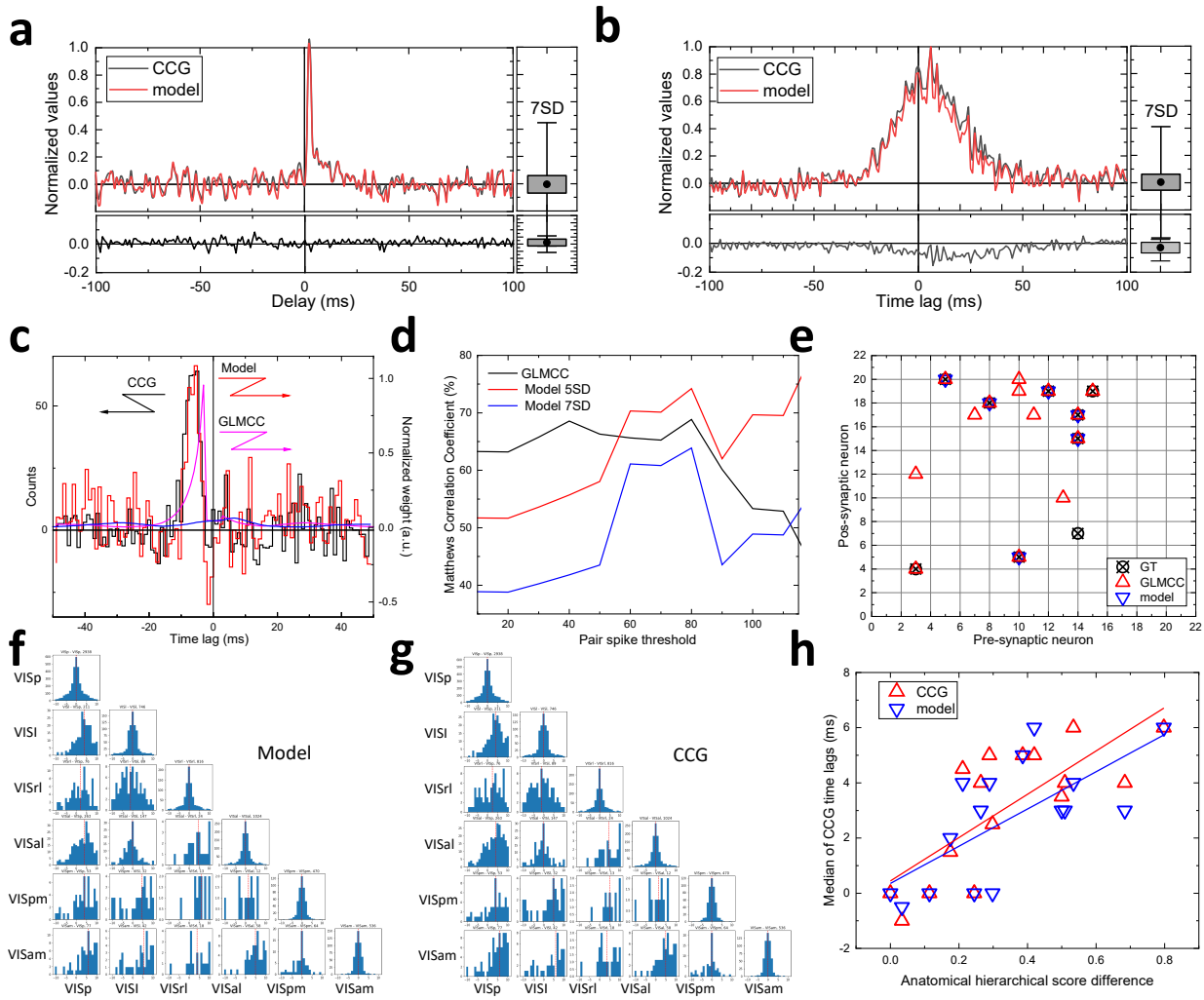

Figure 2. Performance benchmarking of static connectivity inference relative to probabilistic methods

A) Comparison of static DyNetCP (red curve) with jitter-corrected CCG (black curve) for a representative pair of local units (session 771160300, spatially close units from Layer 5 of the VISam area). Residuals (bottom panel) and residual analysis (right panels, box: SD, whiskers: 1-99%, dot: mean). **B)** Comparison of static DyNetCP (red curve) with jitter-corrected CCG (black curve) for a representative pair of spatially distant units (session 771160300, units from VISam and VISp areas). **C)** Comparison of jitter-corrected CCG (black), GLMCC (magenta), and DyNetCP (red) weights for a pair of excitatory HH neurons from a synthetic dataset. **D)** MCC calculated for GLMCC (black) and for DyNetCP with α_w =5SD (red) and 7SD (blue). **E)** Static connectivity $\mathbf{W_{st}}$ for a subset of excitatory HH neurons with GT (crossed circles) compared to connections recovered by GLMCC (red triangles) and DyNetCP (blue triangles). **F)** Histograms of the functional delays inferred by static DyNetCP across all 26 sessions of VCN dataset for each visual area combination. Dashed red line indicates the median of the distribution. **G)** Histograms of the functional delays extracted from the jitter-corrected CCG for all pairs across all 26 sessions for each visual area combination. Dashed red line indicates the median of the distribution. **H)** Comparison of median functional delays vs anatomical hierarchy score difference extracted by DyNetCP (blue triangles) and by jitter-corrected CCG (red triangles) (VCN dataset, n=26 animals).

Static connectivity inferred by the model is biologically interpretable.
Recently jitter-corrected CCG was used to extract cellular-level functional hierarchy across mouse visual cortices[15,20]. Classical CCG (as well as GLMCC), however, recovers static network structure by modeling pairwise correlations and hence must be run separately for each pair in the dataset without considering the relative influence of other pairs in the network. In contrast, DyNetCP learns connections of an entire network jointly in one pass. It is, therefore, instructional to compare the hierarchical interactions between visual cortices inferred by DyNetCP to CCG results using the same large-scale in-vivo VCN dataset[15]. The DyNetCP trained on all units of VCN database (SM, Table S1) extracted 5023 pairs with $\mathbf{W_{st}}$ peak amplitudes above α_w of 7SD, whose shape is statistically indistinguishable (typical r_p>0.9 and P_p<0.0001) from the corresponding jitter-corrected CCG. Following the previous methodology[15,20], functional delays corresponding to the time lags of $\mathbf{W_{st}}$ peaks are determined for all recorded pairs across all six cortical areas and the median time lags averaged across pairs within a given visual area (Fig.2F) are identified as the area's functional delay. Similar results are obtained with the jitter-corrected CCG analysis (Fig.2G). The median functional delays predicted by DyNetCP by learning from all units in a single animal (Fig.2H, blue) show strong correlation (r_p=0.73, P_p<0.0001) with the visual area anatomical hierarchical score difference[5], very closely (r_p=0.99, P_p<0.0001) replicating the correlation (r_p=0.76 and P_p<0.0001) observed with the descriptive pairwise CCG-based analysis (Fig.2H, red) confirming previous observation of hierarchical organization of inter-area functional delays[15]. Therefore, the static DyNetCP is able to predict median functional delays by learning from all units at once that closely replicate results obtained with a descriptive pairwise jitter-corrected CCG-based analysis[15].

Performance benchmarking of dynamic connectivity inference relative to alternative methods
Once the static connectivity $\mathbf{W_{st}}$ is established and verified, the dynamic stage of DyNetCP learns $\mathbf{W_{dyn}}$ that is strongly temporally modulated (SM, Movie 1). While no GT data are currently available to verify the model performance, model predictions, however, can be compared (Fig.3A) to a classical pairwise Joint Peristimulus Time Histogram[33] (JPSTH) that represents the joint correlations of spiking between two neurons and their variation across time. Specifically, given trial-aligned data with a trial length of T bins, the JPSTH is a $T \times T$ matrix where each entry (a, b) represents the percent of trials where neuron i spiked at time a and neuron j spiked at time b. Averaging over the columns of the JPSTH recovers the peristimulus time histogram (PSTH) of neuron i, while averaging over the rows of the JPSTH recovers the PSTH for neuron j (Fig.3A). Since DyNetCP learns the conditional probability of the spiking of one neuron conditioned on others, we cannot directly compare dynamic weights to a standard JPSTH, which models joint correlations. Instead, for a proper comparison, we use a conditional joint peristimulus time histogram (cJPSTH), where we divide the columns of the JPSTH by the PSTH of neuron i (Fig.3B). This changes the meaning of each entry (a, b) in the cJPSTH that represents the conditional probability that neuron j spikes at time b, conditioned on neuron i having spiked at time a (Fig.3C).

Comparison of the dynamic weights $\mathbf{W_{dyn}}$ matrix inferred by DyNetCP (Fig.3D) with the cJPSTH matrix (Fig.3E) for a given set of thresholds α_w, α_s, and α_p, requires setting up an optimal *L2* regularization coefficient for the model training. A squared *L2* penalty is introduced into the model loss function to compensate the sparseness and irregularity of spiking often observed in cortical recordings (Methods). Scanning of *L2* from 0.01 to 10 (SM, Fig.S4A) demonstrates statistically significant correlation (r_p>0.77 and P_p<0.001) of the dynamic weights $\mathbf{W_{dyn}}$ matrices and cJPSTH matrices observed for all *L2* values with the best results obtained for *L2* between 0.1 and 1 (SM, Fig.S4B). The two-sided paired equivalence test (TOST) (SM, Fig.S4C) confirms that the average difference between normalized weights inferred from both models is smaller than 0.09. Therefore, the DyNetCP reliably recovers the time-dependent dynamic weights $\boldsymbol{W_{dyn}}$ even in the presence of strong nonstationary spiking irregularities and sparce spiking.

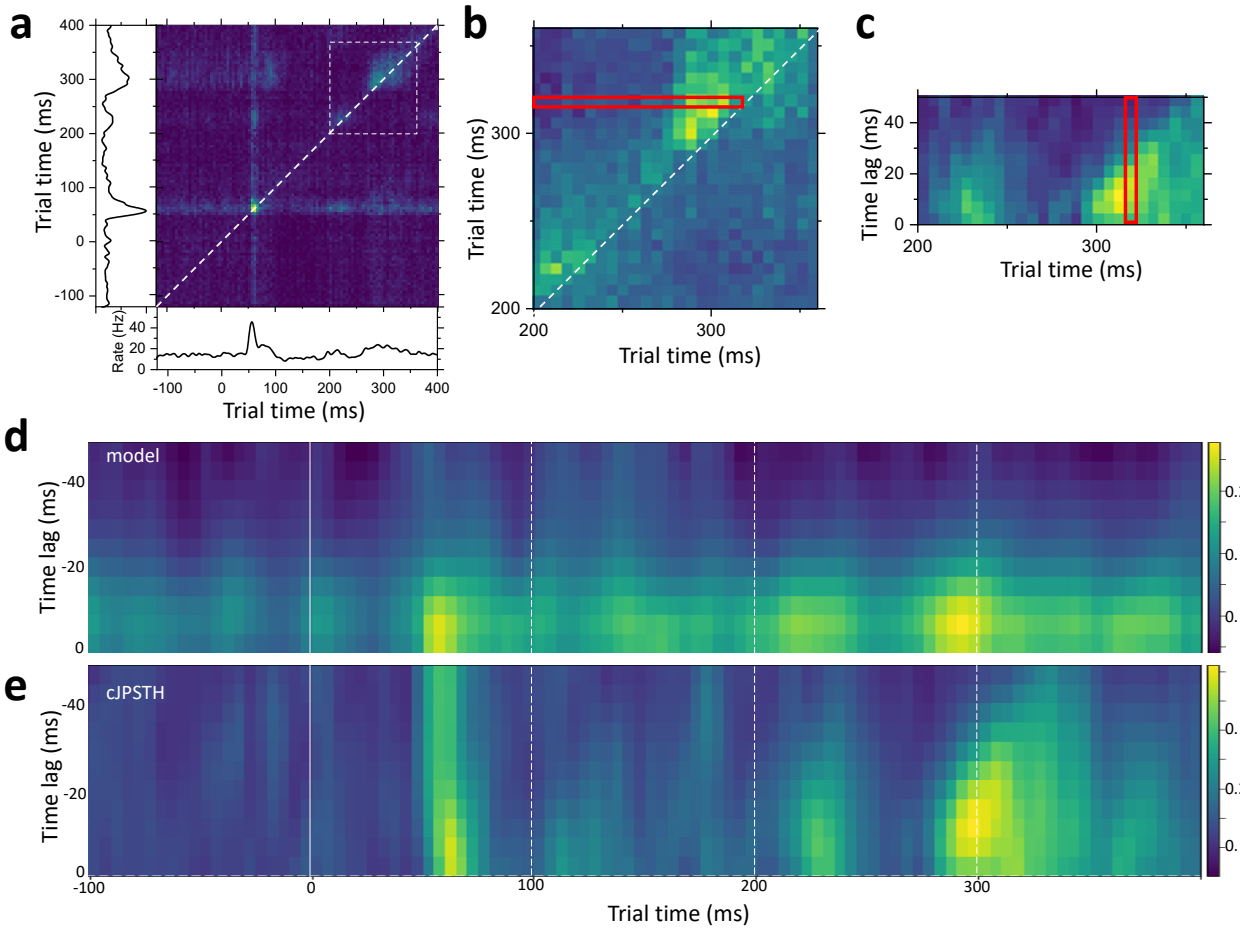

Figure 3. Performance benchmarking of dynamic connectivity inference relative to alternative methods

A) An example of JPSTH for a local pair of units (session 766640955 of the VCN dataset, spatially close units from Layer 5 of the VISp area). Panels on the left and at the bottom show corresponding spike rates for receive and send units, correspondingly. White dotted square corresponds to the area of interest. **B)** Construction of the conditional cJPSTH. Pixels from the white dotted square in A) are normalized by spiking rate of the send neuron. Row of pixels marked by red rectangle is used in C). **C)** cJPSTH corresponding to the white dotted square in A). Red rectangle corresponds to red rectangle pixels in B). **D)** Dynamic weight $\mathbf{W_{dyn}}$ for a local pair of excitatory units (Layer 5 VISp area, session 766640955) inferred for *L2* of 1. **E)** cJPSTH for the same pair of neurons.

Model enables discovery of cellular-level dynamic connectivity patterns in visual cortex.
The model architecture (Fig.1A) designed with two interacting static and dynamic parts enables justification of the choice of model parameters and verification of model inference results by benchmarking to the results of alternative methods. Therefore, even in the absence of experimental or synthetic datasets with known ground truth (GT) of cellular-level dynamic connectivity, the model can provide an otherwise unattainable insights into dynamic flows of information in cortical networks. To demonstrate the ability of the DyNetCP model to discover dynamic cortical circuits, three filters α_w, α_s, and α_p were applied to all 26 sessions of the VCN dataset (SM, Fig.S8) that produces 808 units forming 1020 pairs across all 6 cortical areas. In addition, to aid identification of confounding FP connections (Methods), these pairs were checked for the ratio of $\mathbf{W_{dyn}}$ to $\mathbf{W_{st}}$ (SM, Fig.S5).

Dynamic interaction in local circuit. An example of $\mathbf{W_{dyn}}$ and $\mathbf{W_{st}}$ recovered for a local circuit consisting of 6 interconnected units is shown in Fig.4A (SM, Movie 2). In this case recording from a single animal is used (session 819701982) from a single VISam area. Units produce 6 pairs with significant low-latency peak (α_w>7SD) in static weights $\mathbf{W_{st}}$ (Fig.4A, right panel) indicating strong putative connections. Dynamic $\mathbf{W_{dyn}}$ matrices (Fig.4A, left panel) demonstrate strong temporal modulation. Prior to presentation of a stimulus (t<0ms) the inhibitory drives (negative values of $\mathbf{W_{dyn}}$ marked by deep blue color in Fig.4A) prevail. The first positive peak of $\mathbf{W_{dyn}}$ at 70ms (positive values of $\mathbf{W_{dyn}}$ marked by bright yellow color in Fig.4A) is shared by all but one pair and is coinciding with almost synchronous firing shared by all population that might be an indication on synchronous arrival of afferent signals. However, at later times, additional strong peaks appear for some of the pairs (3→2 and 2→1) that are not accompanied by corresponding increase of the firing rates indicating dynamic reconfiguration of the information flow.

Since DyNetCP, as opposed to population dynamic models[27-30], learns latent variables assigned to individual units, the anatomical and cell-type specific information is preserved. For example, units in the circuit of Fig.4A can be ordered with respect to their cortical depth, assigned to specific cortical layers, classified as inhibitory (excitatory) based on their waveform duration, and, further, can even be assigned to a specific cell type (e.g., Pvalb, SST, and VIP used in VCN dataset) if cells are genetically engineered to provide a distinct response to optogenetic tagging. Schematic representation of this local circuit consisting of 2 inhibitory and 4 excitatory units distributed across cortical layers (Fig.4B) illustrates the temporal dynamics of interlayer inhibitory and excitatory drives (SM Movie 2). Therefore, not only DyNetCP can provide static connections in this local circuit, but, more importantly, can also track the time epochs when individual connections are activated or inhibited that are time-aligned to the stimulus presentation and behavior.

Dynamic connectivity in VISp primary visual area. Going beyond local circuits, the dynamic analysis of information flows during stimulus presentation can be extended to area-wide dynamic maps. An example of an area-wide cellular-level dynamic interactions in primary visual area VISp (Fig.5A) learned from all 26 sessions reveals complex dynamic pattern (SM, Movie 3) both within each cortical layer (along the anti-diagonal), as well as between layers (outside of the anti-diagonal). Extra-laminar interactions reveal formation of neuronal ensembles with both feedforward (e.g., layer 4 to layer 5), and feedback (e.g., layer 5 to layer 4) drives.

Dynamic connectivity along the hierarchy axis of all visual cortices.
Similarly, at the cortex-wide level (Fig.5B), long range interactions across various visual cortices (off-diagonal terms in Fig.5B) exhibit complex temporal evolution with rich feedforward (along the anatomical hierarchical score difference[5]) and feedback interactions (SM, Movie 4). Therefore, DyNetCP can uncover the dynamics of feedforward- and feedback-dominated epochs during sensory stimulation, as well as behavioral states (e.g., epochs in the VCN dataset when animals are running or sitting), however, as opposed to population decoding models[27-30], produce cellular-level cell-type specific connectivity patterns that are otherwise hidden from analysis.

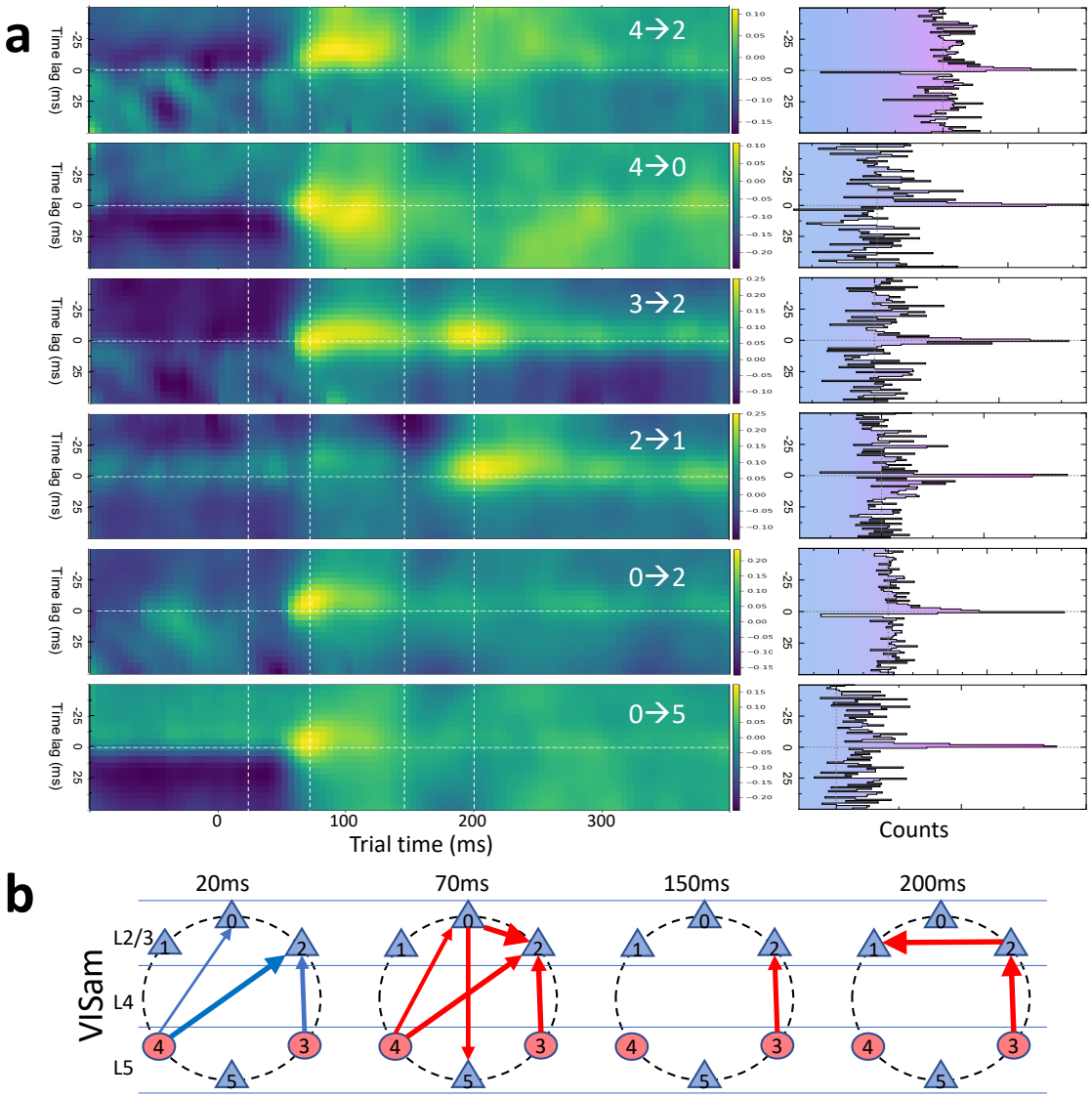

Figure 4. Model enables discovery of cellular-level dynamic connectivity patterns in visual cortex.

A) Left panel: Dynamic weights $\mathbf{W_{dyn}}$ for an example local circuit (session # 819701982, VISam area). Units are numbered by local indices. Right panel shows corresponding jitter-corrected static weights $\mathbf{W_{st}}$. **B)** Schematic diagram of dynamic connectivity in a local circuit in A) for different trial times. Circles and triangles correspond to excitatory and inhibitory units, respectively. The size of blue (red) arrows reflects the dynamic weight of the inhibitory (excitatory) connection at a given time.

DISCUSSION

DyNetCP can reveal cellular-level dynamic interactions within local circuits, within a single brain area, as well as across global hierarchically organized information pathways. Such detailed information, although present in the original datasets, is otherwise hidden from usual analysis that typically relies on time-averaged spike rate coding or population-averaged coding. It is instructional to assess whether the temporal cellular-level interactions uncovered by DyNetCP are bringing new latent dimensions to the analysis of neural code. Dimensionality reduction methods[18,34,35] are often used to estimate the number of independent dimensions of the code that can better explain the variability of spike trains. When principal component (PC) dimensionality reduction[30] is applied to the dynamic weights $\mathbf{W_{dyn}}$ of all valid pairs (i.e., passed through all 3 thresholds, Fig.S8) in a single animal (65 units, 105 pairs, session 831882777), up to 33 components are required to account for 95% of the variance (Fig.5C, black). In contrast, only 5 PC are sufficient to explain 95% variance of spike rates for the same units (Fig.5C, red). If all clean units in all visual cortices are taken (264 VIS units) the dimensionality increases, but only slightly to 8 PC (Fig.5C, blue). The normalized intrinsic dimensionality (NID) estimated as a number of major PC components divided by the number of units is between 0.03 and 0.08 for spike rates exhibiting striking simplicity consistent with an often observed trend[36]. However, in striking contrast, the NID for dynamic weights is as large as 0.5 showing dramatic increase of dimensionality.
This result holds for each of the 26 sessions with the NID in the spiking rate space for valid pairs (Fig.5D, green, mean:0.20±0.018 SEM) and for all VIS units (Fig.5D, violet, mean:0.08±0.01 SEM). In contrast, much larger NID is observed in the phase space of dynamic weights (Fig.5D, orange, mean:0.55±0.02 SEM) indicating that the dimensionality of a dynamic network manifold is becoming comparable to the number of recorded units. Hence the observed complexity stems from a relatively small subpopulation (valid units in pairs mean: 42.7±3.3 SEM) comprising just 20% of the total (all clean VIS units mean: 194.9±11.9 SEM) and at relatively short time scales below 30ms when it survives temporal Gaussian kernel smoothing (inset in Fig.5D). DyNetCP, therefore, reveals the dynamically reconfigurable functional architecture of cortical networks that is otherwise hidden from analysis.

In summary, DyNetCP provides a fully reproducible and generalizable processing framework that allows investigators to explore often overlooked dimensions of the neural code that are potentially rich for novel biological insights. We believe that our approach can help to provide a conceptual link between brain-wide network dynamics studied with neuroimaging methods and modern electrophysiology approaches resolving such dynamics at a cellular level.

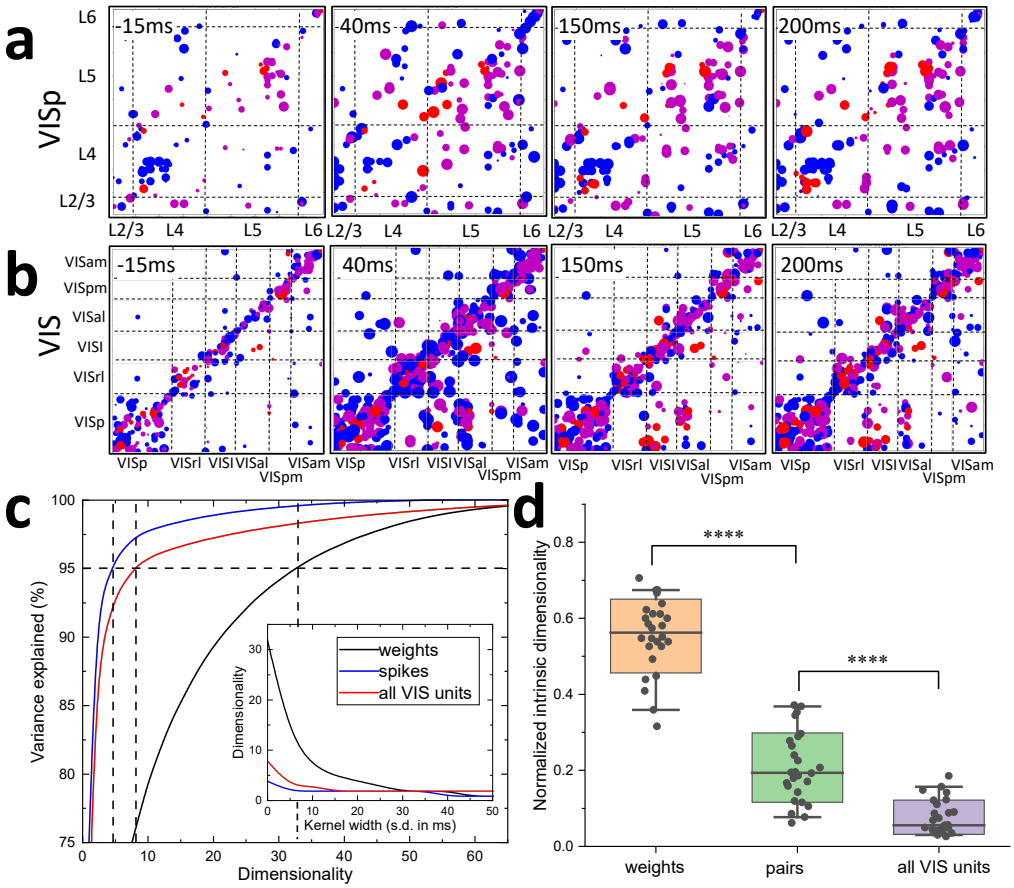

Figure 5. Dynamic functional connectivity prediction along the hierarchy axis of visual cortices.

A) $\mathbf{W_{off}}$ at different trial times (VISp area, n=26 animals). Units ordered by cortical depth and assigned to layers. The circles diameter is proportional to the dynamic offset. Red, blue, and magenta circles correspond to excitatory-excitatory, inhibitory-inhibitory, and mixed connections, respectively. **B)** $\mathbf{W_{off}}$ matrices for all visual areas (n=26 animals) ordered by their hierarchical score. **C)** Intrinsic dimensionality of neural activity manifold (session 831882777, no temporal smoothing) using spiking data for all VIS cortical units (red), units in selected pairs (blue), and for the same unit pairs using dynamic weights (black). **Inset**: Intrinsic dimensionality as a function of temporal gaussian kernel width. **D)** Intrinsic dimensionality (n=26 animals) in spike rate phase space normalized by the number of all VIS units (violet) and units in selected pairs (green). Intrinsic dimensionality in a weight phase space for units in selected pairs (orange). Box: SD, whiskers: 5%-95% range, horizontal line: median, **** is p-value<0.0001.

METHODS

The DyNetCP source code, Jupyter Notebook for analysis, and supporting documentation are available in the GitHub repository (https://github.com/NeuroTechnologies/DyNetCP)

1. DyNetCP TRAINING AND IMPLEMENTATION

1.1 Loss function

The loss used to train the model consists of two terms. The first is a negative log likelihood over the predicted spike probabilities, which encourages the weights to accurately encode the influence of spiking from other neurons on the spiking of the neuron in question. The entire loss is written as

$$L(x;w) = \sum_{t=1}^{T}\sum_{j=1}^{N} x_j(t) log P\big(x_j(t) = 1 | x_j(t-M:t-1)\big) + \Big(1 - x_j(t)\Big) log\Big(1 - P\big(x_j(t) = 1 | x_j(t-M:t-1)\big)\Big) + \lambda ||\mathrm{w}||_2^2, \quad \text{Eq.4}$$

where w represents all the predicted static and dynamic weights, and λ is a coefficient used to balance the magnitudes of the losses. Loss optimization during training results in predicted spike rate (PSTH) approaching the actual spike rate (SM, Fig.S1A). We introduce a squared *L2* penalty on all the produced static and dynamic weights as the second term to discourage the network from overpredicting activity for times when no spikes are present ($x_j^{t-d} = 0$) and the weight multiplied by zero is unconstrained. In these cases, adding the penalty provides a training target. For all experiments we used an *L2* weight between 0.1 and 1 that produced the best fit to the descriptive statistics results (cJPSTH) discussed in detail below (SM, Fig.S4).

1.2. Training

The DyNetCP model is designed to be trained in a single step to produce both, static and dynamic weight matrices for the whole dataset. However, for the purpose of this work, we are interested in verification and detailed comparative analysis of the model performance that enables clear justification for the choice of model parameters. Therefore, here, training of the model to analyze a new dataset is implemented in two separate stages. In the first stage, only the static weights are trained for all the valid neurons while the dynamic weights are all set to zero. In the second stage, the static model parameters and static weights are fixed, and we train only the dynamic component of the model. Dividing training into two parts is also more efficient computationally. Prior to implementing the dynamic part of DyNetCP, the pairs are classified as putative connections based on a statistical analysis (see below) of the static weights, and the dynamic component is trained only on these pairs.

Computation time and memory consumption can also be optimized by the choice of the bin size d at the cost of temporal precision of the weight prediction. To better identify putative connections and to ease comparison with descriptive CCG models, we use a bin size of 1ms for training of static weights. For training the dynamic part, we use spiking data binned at a 5ms resolution. Evaluation of statistical significance of the model predictions (see below) indicates that a 5ms bin size strikes a good balance between computational efficiency, temporal resolution, and data sparsity.

All models are trained using the ADAM optimizer[37], a batch size of 16, and a learning rate of 0.0001 for 2000 epochs, where the learning rate is reduced by a factor of 10 after 1000 epochs. For each dataset, we set aside some of the data for validation. We use the validation data for early stopping: after every epoch of training, we compute the loss on the validation data, and terminate training early if the validation loss has not improved for a specific number of epochs (100 when training the static portion and 50 when training the dynamic portion). Note, to properly assess generalization, all plots in this work show DyNetCP static and dynamic weights outputs from the validation data.

When training the static part of the model on the synthetic HH dataset[26], we use λ = 1. For training the static part on the VCN dataset[15] we use λ = 100, which we found to lead to a lower residual when comparing to CCG values. For training the dynamic weights for all models we use λ = 10.

1.3 Averaging Dynamic Weights

To extract a strong signal from the DyNetCP dynamic weights, we need to aggregate information over experimental trials. However, we do not want to simply average the weights over trials, as all weights which are not paired with an incoming spike (i.e., all weights $w^{d}_{j\to i}$ such that $x_j^{t-d} = 0$) do not contribute to the spike rate prediction and therefore are not constrained to capture the spiking correlations. As a result, when computing trial-aggregated DyNetCP weights, we average over weights that are time-aligned with spike times of corresponding unit (SM, Fig.S2A) as follows:

$$w\sim^{d,t}_{j\to i} = \frac{1}{\sum_{m=1}^{M} \mathbf{1}[X(m,j,t)=1]} \sum_{m=1}^{M} \mathbf{1}[X(m,j,t) = 1] w^{d,t}_{j\to i} \qquad \text{Eq.5}$$

Additionally, to compensate for the sparsity of spiking, we average these aggregated dynamic weights over the 10 most recent bins (SM, Fig.S2B).

1.4 Jitter correction

Jittering method [15,19,31,34,38] is often used in analysis of pairwise spiking correlations to minimize the influence of a potential stimulus-locked joint variation in population spiking that often occurs due to common input from many shared presynaptic neurons. To lessen the impact of such false positive (FP) connections in DyNetCP results and to ease the comparison with classical jitter-corrected CCG, we train a second static model on a jitter-corrected version of the data generated using a pattern jitter algorithm[31] with a jitter window of 25ms. When the dataset is trial-aligned (e.g. VCN dataset), we use the correction procedure[31] which determines the probability of a spike being present in each bin for all possible random shuffles of spikes among trials. For data which is not trial-aligned (e.g. synthetic dataset of HH neurons[26]), we randomly permute the spike times within the interval [-5ms, +5ms] before every weight update. New spike resampling is performed during every epoch of training. To assess putative connectivity, the jitter-corrected static weights $w'_{j\to i}$ produced by a jitter-corrected model are subtracted from the weights $w_{j\to i}$ trained on the original data to obtain $w^*_{j\to i} = w_{j\to i} - w'_{j\to i}$ and $w^*_{i\to j} = w_{i\to j} - w'_{i\to j}$.

2. Datasets

2.1 Synthetic network of HH neurons

We use a synthetic dataset consisting of Hodgkin-Huxley (HH) 800 excitatory and 200 inhibitory neurons with known ground truth (GT) synaptic connections[26]. The excitatory neurons influence 12.5% and the inhibitory neurons influence 25% of other neurons. We use the first 4320s of the 5400s-long data for training and the remaining 1080s for validation. Since DyNetCP requires training with trial-aligned data, we split each of these datasets into 1s "trials" consisting of 1000 bins each. For training and evaluation we use spikes from the same subset of 20 excitatory neurons as was used for GLMCC validation[26].

2.2 Synthetic dataset with FP connections

Synchronous spiking at short time lags does not necessarily indicate a direct connection but can also be induced by a shared common input (SM, Fig.S5A) or an indirect serial chain connection (SM, Fig.S5B) among others. While it is notoriously difficult to distinguish these confounding correlations using descriptive statistical models[25], the DyNetCP being a probabilistic model might lessen their impact by abstracting out such co-variates that do not contribute significantly to a prediction. To test the ability of DyNetCP to identify such confounds, we generate a synthetic dataset with known GT static and dynamic connectivity. The dataset consists of 100 excitatory neurons with their spikes generated by independent sampling from a Bernoulli distribution with spike rate between 0.002 and 0.01 per bin. The GT connection is active when spikes in neuron n_1 at time t are followed by spikes in neuron n_2 at a time $t + d$ with a probability of 0.6. Randomly generated 100 "triplets" emulating common input and serial chain connections are added to the pool. The "triplets" are active either during the first and last 125 bin period or only during the middle 375 bin period.

DyNetCP trained on this dataset (400 train and 200 validation trials, each 500 bins long) enables comparison of static and dynamic weights (SM, Fig.S5) that indicate that when the connection is present the $\mathbf{W_{dyn}}$ tends to be larger than $\mathbf{W_{st}}$, which enables classification of connections as TP and FP for both common input (SM, Fig.S5A) and serial chain (SM, Fig.S5B) connections for this synthetic dataset.

2.3 Experimental dataset recorded in visual cortex.

To demonstrate DyNetCP performance with in-vivo high-density electrophysiological recordings, we used the publicly available Allen Brain Observatory-Visual Coding Neuropixels (VCN) database[15] that contains spiking activity collected across 99,180 units from 6 different visual cortical areas in 58 awake mice viewing diverse visual stimuli. We use a "functional connectivity" subset of these recordings corresponding to the "drifting grating 75 repeats" setting recorded for 26 animals (SM, Table S1). Full-field drifting grating stimuli was passively viewed by a head-fixed animal freely running on a treadmill[15]. Stimuli consists of 2s presentation of drifting diffraction grating (temporal frequency 2 cycles/s, spatial frequency = 0.04 cycles per degree) that is interleaved with a 1s grey period (top left inset in Fig.1A). Presentation of gratings were repeated 75 times per orientation (0, 45, 90, and 135 degrees) and per contrast (0.8 and 0.4). To maximize the number of spikes available for training we use all angles and all contrast trials.

We split the 600 total experimental trials for each session into 480 training and 120 validation trials by selecting 60 training trials from each configuration of contrast or grating angle and 15 for validation. To further investigate the influence of brain state on connectivity dynamics we identify in each session trials with the average running speed above 5cm/s that are marked as "running". The rest of the trials are marked as "not running". When trained and validated, the model results can then be analyzed and compared for "running" vs "non-running" conditions separately.

3. Comparison with alternative methods

3.1 Jitter-corrected Cross-Correlogram

The cross-correlogram (CCG) between a pair of neurons n_1 and n_2 is defined as:

$$\mathrm{CCG}(\tau) = \frac{1}{M}\sum_{i=1}^{M}\frac{\sum_{t=1}^{T} x_1^t(i)x_2^{t+\tau}(i)}{\theta(\tau)\sqrt{\lambda_1\lambda_2}}, \qquad \text{Eq.6}$$

where τ represents the time lag between spikes from n_1 and n_2, λ_j is the spike rate of neuron j, and $\theta(\tau)$ is a triangular function which corrects for the varying number of overlapping bins per delay.

To minimize the influence of a potential stimulus-locked joint variation in population spiking that often occurs due to common input from many shared presynaptic neurons, we apply a jitter correction[15,19,31,34,38] to the CCG using a pattern jitter algorithm[31] with a jitter window of 25ms.

3.2 GLMCC model.

Python code for GLMCC method is taken from the author's version[39]. For these experiments, we use the synthetic dataset of interconnected HH neurons[26]. We focus specifically on recovering ground-truth (GT) excitatory connections. To facilitate a comparison with GLMCC model[26], we here choose thresholds α_w, α_s, and α_p to maximize the Matthews Correlation Coefficient (MCC), which is defined as

$$\mathrm{MCC} = \frac{TP\times TN - FP\times FN}{\sqrt{(TP+FP)(TP+FN)(TN+FP)(TN+FN)}}, \qquad \text{Eq.7}$$

where TP, TN, FP, and FN are true positive, true negative, false positive, and false negative pair predictions, respectively. MCC optimization balances between maximizing the number of TP pairs recovered while minimizing the number of FP pairs which are predicted.

Since a predicted connection is counted as a TP only once (i.e., $i \rightarrow j$ and j$\rightarrow i$ do not count as two negatives if i is not connected to j) and the number of GT connections decreases when α_p increases, the MCC exhibits an increase beyond α_p=100. A more detailed analysis of TP and FP rates as a function of pair spike threshold is presented in SM, Fig.S3.

Though GLMCC performs well in recovering static network structure, we emphasize that GLMCC is not compatible with modeling network dynamics and thus cannot be integrated into DyNetCP. Specifically, our goal is to model the correlations of spiking of a network of neurons and track the changes of these correlations across time. GLMCC learns correlations as a function of the time lag relative to the spiking time of a reference neuron. It is hence unable to link correlations to specific moments in a trial time. Therefore, it cannot represent the dynamics of correlations, preventing its use in analysis of network activity relative to subject behavior.

3.3 Conditional Joint Peristimulus Time Histogram (cJPSTH)

The Joint Peristimulus Time Histogram (JPSTH) is a classical tool[33] used to analyze the joint correlations of spiking behavior between two neurons and their variation across time. For a proper comparison with conditional DyNetCP results, we use a conditional joint peristimulus time histogram (cJPSTH), where we divide the columns of the JPSTH by the PSTH of neuron i (Fig.2B,C). Due to the sparsity of spiking in the data we use, it is beneficial to average the entries of the cJPSTH over short windows in time to more clearly extract the dynamics of the correlations between neurons. Specifically, we replace each entry (a, b) in the cJPSTH by the average of the *T* most recent bins having the same delay $a - b$, that is,

$$cJPSTH_{Avg}(a, b) = \frac{1}{T}\sum_{i=0}^{T-1} cJPSTH(a - i, b - i) \quad \text{Eq.8}$$

For most of the comparisons we use *T*=10 bins. Note that for most cJPSTH plots (e.g., Fig.2E), to directly compare to DyNetCP plots (e.g., Fig.2D), we only show data representing the "upper diagonal" of the full plot which represents data where neuron i spikes at the same time or before neuron j spikes (SM, Fig.S4A). Specific implementation and comparisons of both models can be found in the accompanying Jupyter Notebook.

3.4. Dimensionality reduction

Dimensionality reduction[18,34,35] is based on calculating principal components (PC) on the dataset and estimating the data variance that can be explained by a minimal number of PC. The dimensionality reduction code following a standard PCA reduction method[35] is rewritten in Python and is used for analysis in Fig. 5C,D.

4. STATISTICAL ANALYSIS OF FILTERING AND CLASSIFICATION OF UNITS AND PAIRS

The total number of units (raw units) recorded from visual cortices in 26 sessions of the VCN dataset #3.2 is 18168. Units and pairs are filtered and classified by the following procedure.

4.1 Unit quality metrics

First, we apply standard unit quality metrics[15] including amplitude cutoff < 0.1; violations of inter-spike interval (ISI) < 0.1; presence ratio > 0.95; isolation distance > 30; and signal to noise ratio (snr) > 1. This results in 5067 units (clean units).

4.2 Static weight peak threshold

Second, short-latency peaks within the first 10ms in the $w^*{}_{j\to i}$ and $w^*{}_{i\to j}$ of static weights are examined (example analysis for session 771160300 is shown Fig.2A,B). Following the accepted approach[15,19,20,22,26] a putative connection is considered statistically significant when the magnitude of the peak exceeds a certain peak weight threshold α_w measured in units of standard deviations (SD) of the noise in the flanks, calculated within [51ms, 100ms] from both directions $w^*{}_{j\to i}$ and $w^*{}_{i\to j}$. When pairs are filtered with increasing peak weight threshold α_w (SM, Fig.S6A), the number of corresponding valid units is fast decreasing (black curve). For all 26 sessions 5067 clean units participate in formation of 5203 pairs with noticeable weight peaks. Filtering them using α_w=7SD results in 1680 pairs corresponding to 1102 units. Close examination of these pairs (example analysis for session 771160300 is shown in SM, Fig.S6A) reveals that units not only form pairs (violet curve), but also form triplets (green), quintuplets (blue), and even participate in connections above 10-tuples (red). High radix hubs of this type are most likely FP artefacts imposed by sparse spiking (see below) and need to be filtered out. Indeed, electrophysiology spiking datasets are typically very sparse, with many interesting units often generating spikes at rates below 1Hz. Increasing the threshold α_w does help to filter out high radix connections, but still even for α_w as large as 8 there is a substantial number of units participating in connections larger than 3.

4.3 Unit spike rate

Therefore, as a third filtering step, we apply a unit spike rate threshold α_s to limit the minimal spike rate to 1Hz.

4.4 Pair spike rate threshold

It has been argued[26] that, to reliably infer that a connection is present (i.e. to disprove the null hypothesis that a connection is absent), each binned time interval in the CCG histogram d should contain a sufficiently large number of spikes from both participating units. This implies that the spike rate of each neuron in a pair λ_i and λ_j should exceed the threshold α_s, and the joint number of spikes in each time bin should exceed the pair spike threshold, defined as

$$\alpha_p = \lambda_i \lambda_j T M d. \qquad \text{Eq.9}$$

The confidence interval for a null hypothesis that two spike trains are independent stationary Poisson processes[26] is then defined as

$$J_{\mp} = \sqrt{\alpha_p}. \qquad \text{Eq.10}$$

To disprove the null hypothesis and infer that a connection is statistically significant, α_p should exceed[26] 10. To train the dynamic DyNetCP we use recordings binned at d of 5ms repeated over M of 480 randomized trials and the dynamic weights are influenced by T=10 most recent bins (SM Fig.S2B). This corresponds to the TMd product of 24 that implies the minimum joint pair spike rate $\lambda_i\lambda_j$ of 0.41s^{-2}. This threshold, however, might be insufficient for inference of the dynamic weight since only spikes within a short trial time interval are being used for learning. Indeed, analysis of an example pair (SM Fig.S7A) that passed the α_w=7SD threshold and has $\lambda_i\lambda_j$ = 0.73s^{-2}, reveals that it exhibits on average just 2 spikes per trial or a total of 272 spikes for all 480 trials in a 500ms trial time window of interest. Corresponding jitter-corrected static weight matrix (left) and cJPSTH (right bottom) are very sparsely populated. The dynamic weight matrix (right top), although it is reproducing this sparseness, is not statistically convincing. Moreover, such pairs contribute significantly to high radix tuples.

By increasing the $\lambda_i\lambda_j$ pair spike rate threshold, the number of high radix tuples is decreasing (example analysis for session 771160300 is shown in SM, Fig.S6B), however the α_p threshold alone is not sufficient to eliminate them. Hence, for a given pair to be classified as a putative connection, the classification procedure requires the use of all three thresholds: α_w, α_s, and α_p (see Jupyter Notebook for specific implementation).

4.5 Choice of thresholds

When all three thresholds α_s , α_w and α_p are applied simultaneously (SM, Fig.S6C) the number of valid units is decreasing rapidly with the increase of α_w to 7SD and $\lambda_i\lambda_j$ beyond 10 with slower decrease at higher thresholds. Examination of an example pair with joint pair spiking rate $\lambda_i\lambda_j$ of 50 s^{-2} (SM, Fig.S7B) indicates that while the static weight matrix shows a prominent (α_w >7SD) small latency peak, the cJPSTH is still populated relatively sparsely and the dynamic weight matrix resembles it much less (r_p=0.27). In contrast, for an example pair with joint pair spiking rate $\lambda_i\lambda_j$ of 130 s^{-2} (SM, Fig.S7C) the resemblance between cJPSTH and the dynamic weight matrix is striking (r_p=0.82, P_p<0.001).

For a fixed α_s of 1Hz and α_w of 7SD the distribution of all valid pairs with respect to their joint spike rates (SM, Fig.S8A) shows a maximum around $\lambda_i\lambda_j$=200 s^{-2} with a long tail to higher rates. To be conservative, for all the analysis of the inferred connectivity patterns in this work, we used $\lambda_i\lambda_j$ of 200 s^{-2} (α_p=4800, red arrow in SM, Fig.S8A).

Application of all 3 filters to all 26 sessions produces 808 units forming 1020 pairs with distribution of inferred static and dynamic weights shown in SM, Fig.S8B.

4.6 Units classification

Once all pairs are filtered, the directionality is assigned to each putative connection, either $j \rightarrow i$ or $i \rightarrow j$, that is identified by the functional delay of the static weight peak binned at 1ms. Cortical depth perpendicular to cortical surface is calculated from unit coordinates in ccfv3 format (Allen Mouse Brain Common Coordinate Framework [40]). Layer assignment is performed following method[15] using units coordinates in the ccfv3 framework and the annotation matrix with reference space key

‘annotation/ccf_2017’. All units are classified as excitatory if their waveform duration is longer than 0.4ms and the rest as inhibitory (SM, Fig.S8D). Since transgenic mice were used for some of the sessions in the VCN dataset, optical activation of light-gated ion channel (in this case, ChR2) in Cre+ neurons with light pulses delivered to the cortical surface generate precisely time-aligned spikes that enable to link spike trains to genetically defined cell classes. Optical tagging was used to further classify inhibitory units[41].

4.7 Potential biases

The statistical analysis and filtering procedure described above is biased towards strongly spiking units (SM, Fig.S8C) and as such can generate certain biases in connectivity patterns. For example, inhibitory units constitute about 18% of all 5067 clean units that pass unit quality metrics (SM, Fig.S8D). However, after filtering down to 808 valid units, they constitute over 50% of the population (SM, Fig.S8D). In general, inhibitory units have a higher spiking rate (for all clean units mean: 15.4Hz±0.29 SEM) than excitatory (mean: 6.3Hz±0.08 SEM). This might explain, at least partially, the over-representation of connections involving inhibitory units in the dynamic connectivity plots.

Data Availability

All of the datasets used in this article are publicly available online under the Creative Commons Attribution 4.0 International license. Synthetic data of interconnected HH neurons[26] is available at figshare[42] (https://doi.org/10.6084/m9.figshare.9637904). The Allen Brain Observatory-Visual Coding Neuropixels (VCN) database[15] is available for download in Neurodata Without Borders (NWB) format via the AllenSDK. The NWB files are available as an AWS public dataset (https://registry.opendata.aws/allen-brain-observatory/). Synthetic dataset with artifactual FP connections is available on GitHub.

Code Availability

DyNetCP introduced and used in this article is open-source software (GNU General Public License v3.0). The source code is available in a GitHub repository (https://github.com/NeuroTechnologies/DyNetCP) that contains codes for model training as well as a Jupyter notebook for generating the results used in the paper and in the SM.

SUPPLEMENTARY MATERIALS

SM Movie 1: Dynamic weight for an exemplary pair

Dynamic weight $\mathbf{W_{dyn}}$ for a local pair of excitatory units from Layer 5 VISp area, session 766640955 (same pair as in Fig.2D, E). Static weight is shown on the background. Dashed horizontal line is a maximum static weight. Static and dynamic weights are binned at 5ms.

SM Movie 2: Dynamic weights for an exemplary local circuit

Top row: Dynamic connectivity for an example local circuit (same as in Fig.4) from VISam area, session 819701982 for different trial times. Circles and triangles correspond to excitatory and inhibitory units, respectively. Units are numbered by local indices and ordered with respect to cortical layers. The size of blue (red) arrows reflects the dynamic weight of the corresponding connection at a given time. Bottom two rows: Dynamic weight $\mathbf{W_{dyn}}$ for each pair in the circuit. Dashed horizontal line is a maximum static weight. Static and dynamic weights are binned at 5ms.

SM Movie 3: Dynamic weights for VISp area

$\mathbf{W_{off}}$ for a VISp area for all n=26 animals (same as in Fig.5A) for different trial times. Units ordered by cortical depth and assigned to cortical layers. The circles diameter is proportional to the dynamic offset. Red, blue, and magenta circles correspond to excitatory-excitatory, inhibitory-inhibitory, and mixed connections, respectively.

SM Movie 4: Dynamic weights for all VIS areas

$\mathbf{W_{off}}$ for all VIS areas for all n=26 animals (same as in Fig.5B). Units ordered by cortical depth and assigned to cortical layers. The circles diameter is proportional to the dynamic offset. Red, blue, and magenta circles correspond to excitatory-excitatory, inhibitory-inhibitory, and mixed connections, respectively.

Session	Units	Clean units	Valid Units	Valid Units %	Valid Pairs	Run	Run %
766640955	842	145	25	17%	24	50	10%
767871931	713	185	53	29%	49	146	30%
768515987	802	198	41	21%	43	4	1%
771160300	930	223	35	16%	35	115	24%
771990200	546	108	42	39%	41	43	9%
774875821	649	172	43	25%	12	126	26%
778240327	784	275	78	28%	56	413	86%
778998620	793	233	44	19%	15	240	50%
779839471	863	203	29	14%	17	4	1%
781842082	833	229	36	16%	38	66	14%
786091066	700	306	17	6%	13	408	85%
787025148	696	134	18	13%	21	110	23%
789848216	415	81	31	38%	26	183	38%
793224716	781	198	82	41%	77	171	36%
794812542	1005	348	38	11%	30	54	11%
816200189	634	161	46	29%	75	11	2%
819186360	531	166	26	16%	13	13	3%
819701982	585	163	38	23%	29	440	92%
821695405	474	148	38	26%	28	40	8%
829720705	529	232	54	23%	43	88	18%
831882777	657	264	65	25%	62	391	81%
835479236	582	199	36	18%	38	70	15%
839068429	742	150	49	33%	57	401	84%
839557629	450	136	26	19%	11	307	64%
840012044	758	179	67	37%	97	135	28%
847657808	874	231	53	23%	70	72	15%
Total	18168	5067	1110	23%	1020	4101	33%

Table.S1. Experimental dataset recorded in-vivo in 6 visual cortices.

Sessions used for model training and analysis taken from the publicly available Allen Brain Observatory-Visual Coding Neuropixels (VCN) database. We use a "functional connectivity" subset of these recordings corresponding to the "drifting grating 75 repeats" setting recorded for 26 animals. Filtering of recorded units (see statistical analysis criteria below) and classification of valid pairs results in a significant reduction of units (5.6% of raw units or 23% of clean units) used for dynamic connectivity inference. The last two columns represent the number and percentage of trials when the animal was running with average speed over 5cm/sec.

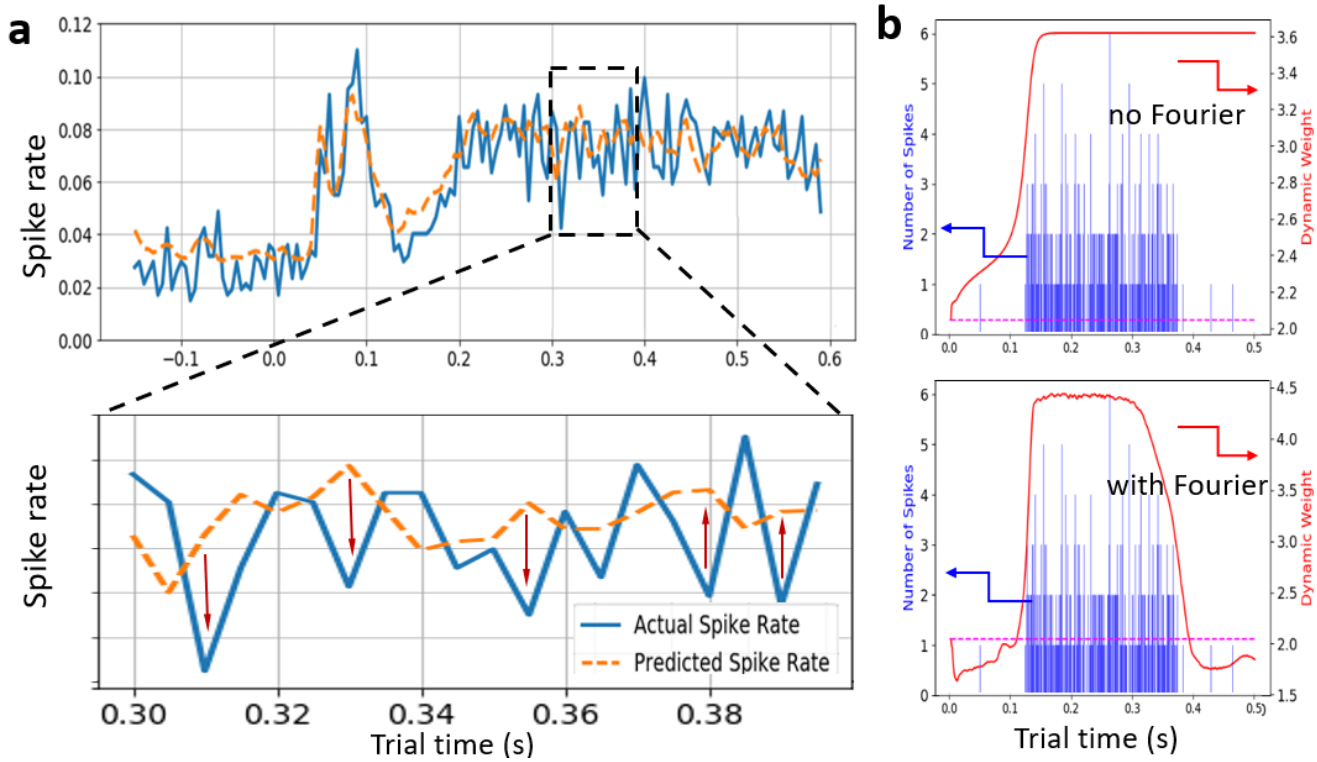

Fig.S1. Model training and implementation

A) Loss optimization. Blue curve is actual spike rate for a representative unit taken from the VCN dataset (see below) as a function of trial time. The dotted yellow curve is a spike rate predicted by DyNetCP model during training. **Inset:** Loss function is designed to push the predicted spike rate to approach the actual spike rate during training.

B) Model performance with and without Fourier features. Blue bars (left y-axis) represent a histogram of joint spiking probability (JPSTH anti-diagonal) for an example neuron pair with direct connection taken from the synthetic dataset (see below). Red curves (right y-axis) correspond to trial-averaged learned dynamic weights, while dotted magenta line represents static weight value. DyNetCP model without Fourier features (top plot) failed to properly localize the period where induced spiking is occurring, while use of Fourier features (bottom plot) enables to do so correctly.

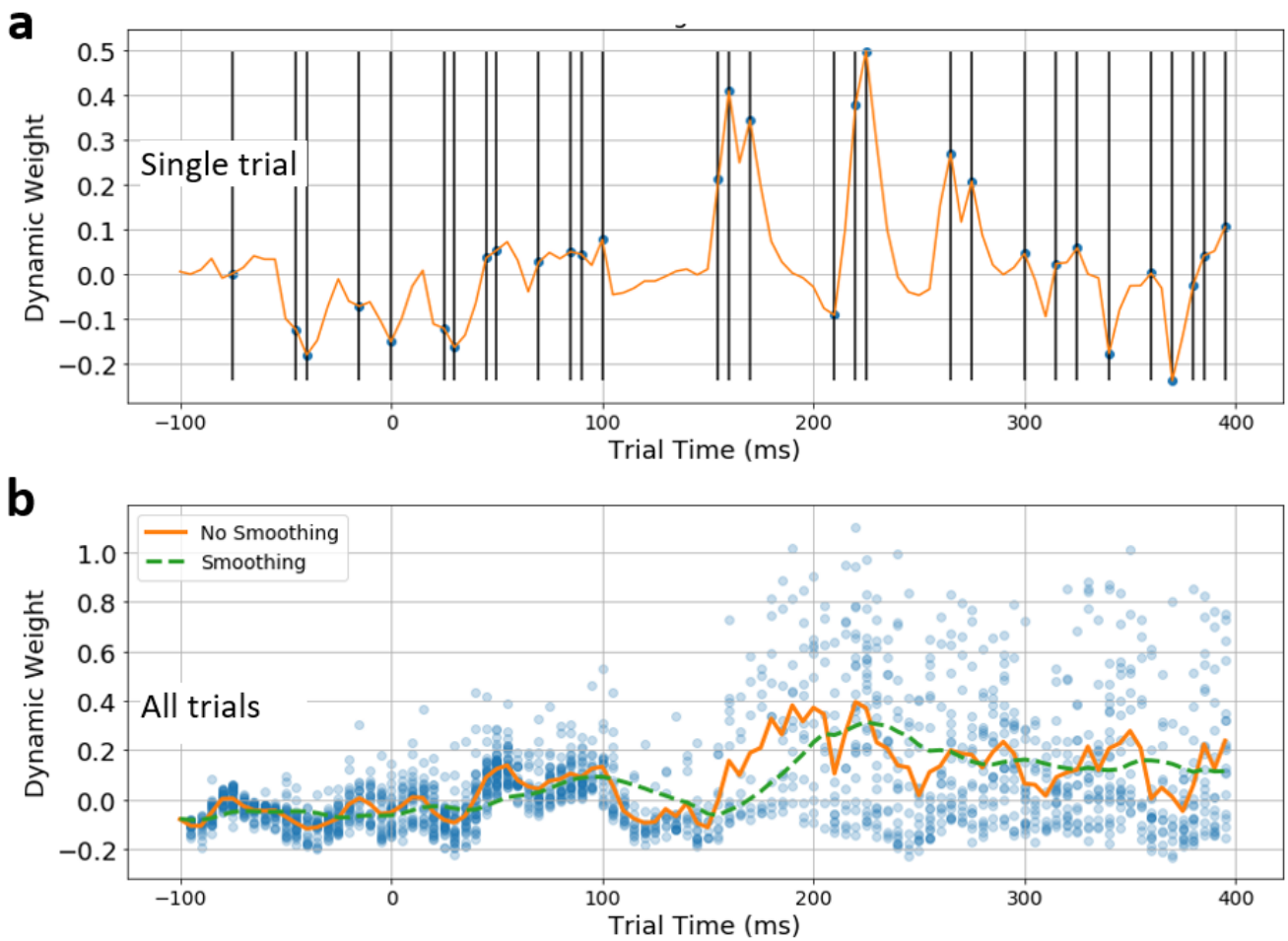

Fig.S2. Selection of dynamic weight values and weights averaging

A) Selection of weights which contribute to averaging. Single trial spiking times for a given unit (black bars). Inferred dynamic weight values (orange curve) are selected at times when associated unit spikes (black dots), as the remaining weights do not contribute to the predicted spiking probability and therefore are not supervised to represent a meaningful value.

B) Averaging of weights. Each blue point corresponds to a dynamic weight from a single trial. The orange curve represents a trial-average of every weight time-aligned with spikes. Green curve represents the Gaussian smoothing with a kernel including the 10 most recent bins.

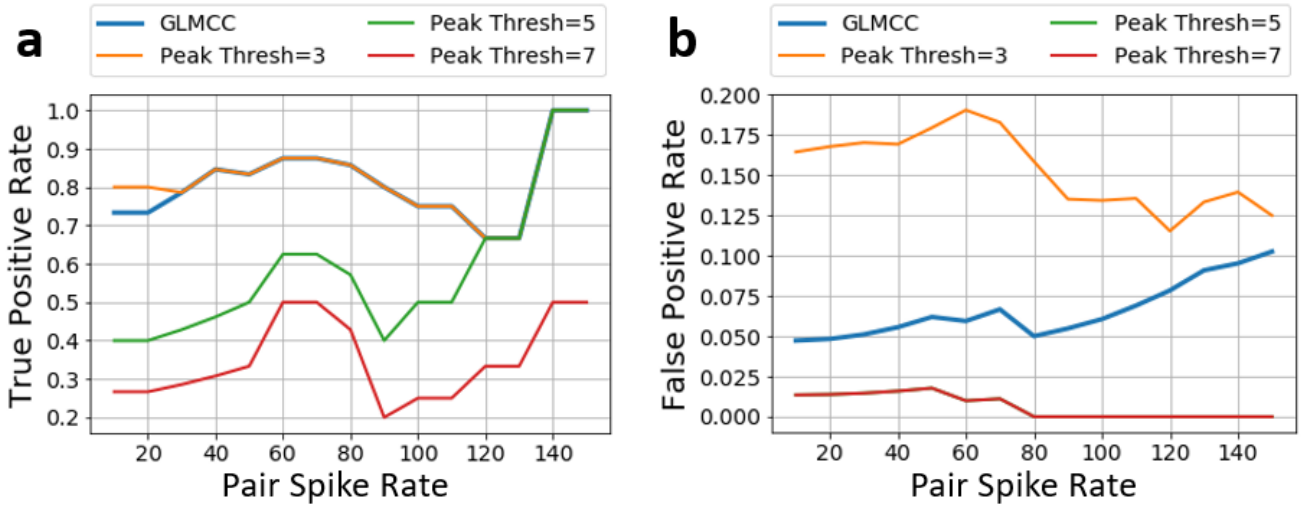

Fig.S3. TP and FP rates as a function of pair spike threshold

A) Recovery of True Positive (TP) connections in HH synthetic dataset. TP connections recovered by DyNetCP model at different pair spike thresholds. Yellow, green, and red curves correspond to peak threshold taken as 3SD, 5SD, and 7SD, respectively. TP connections recovered by GLMCC model are shown by blue curve.

B) Generation of False Positive (TP) connections in HH synthetic dataset. FP connections generated by the DyNetCP model at different pair spike rates. Yellow, green, and red curves correspond to peak threshold taken as 3SD, 5SD, and 7SD, respectively. FP connections recovered by GLMCC model are shown by blue curve.

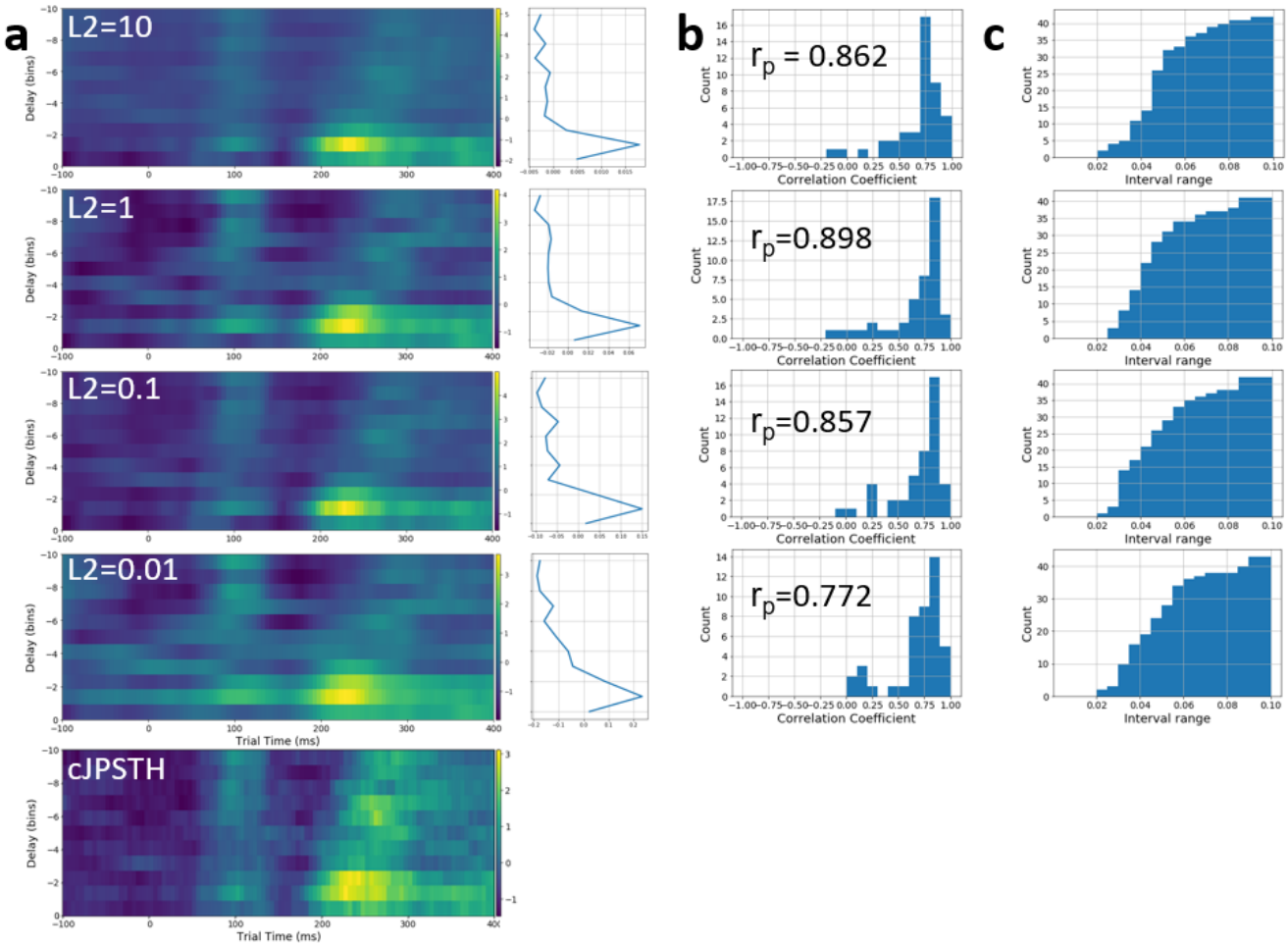

Fig.S4. **Comparison of dynamic weights and model loss parameters**

A) Set of dynamic weights $\mathbf{W_{dyn}}$ for a local pair of excitatory VISp neurons (session 771160300, same as in Fig.3D,E) learnt with different *L2* values. The corresponding cJPSTH is shown on the bottom. Left column shows a set of corresponding static weights $\mathbf{W_{st}}$.

B) A histogram of Pearson correlation coefficients between the dynamic weights and cJPSTH for each pair (comparing each pixel of the weight/cJPSTH matrix) calculated for all 41 pairs found to be significant for this session.

C) The two-sided paired equivalence tests (TOST) for all 41 pairs indicate that the average difference between normalized weights inferred from both models is smaller than 0.09.

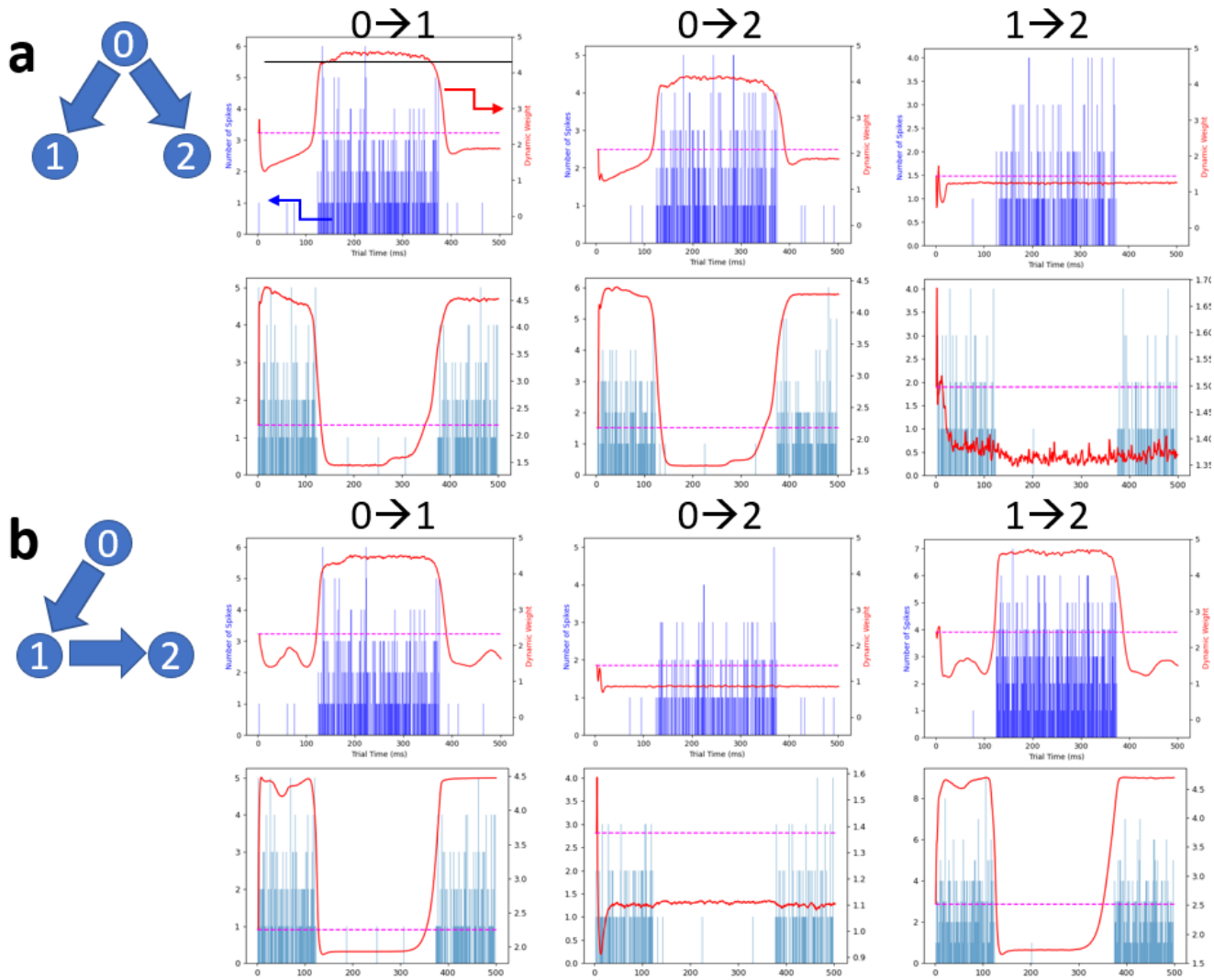

Fig.S5. Performance of the model on synthetic dataset with FP connections

A) Identification of FP connections for a "common input" triplet. **Inset:** schematics of a triplet with common input from the unit 0 to both units 1 and 2. **Top row:** connection is active during the first and last 125 bin period of the trial. **Bottom row:** Connection is active only during the middle 375 bin period. Blue bars (left y-axis) represent a histogram of joint spiking probability (JPSTH anti-diagonal). Red curves correspond to trail-averaged inferred dynamic weights (right y-axis), while dotted magenta line represents static weight value. Comparison of dynamic and static weights might help to distinguish TP connections 0→1 and 0→2 from an artifactual FP connection 1→2.

B) Identification of FP connections for a "serial input" triplet. **Inset:** schematics of a triplet with serial input from the unit 0 to 1 followed by 1 to 2. **Top row:** connection is active during the first and last 125 bin period of the trial. **Bottom row:** Blue bars (left y-axis) represent a histogram of joint spiking probability (JPSTH anti-diagonal). Red curves correspond to inferred dynamic weights (right y-axis), while dotted magenta line represents static weight value. Comparison of dynamic and static weights might help to distinguish TP connections 0→1 and 1→2 from an artifactual FP connection 0→2.

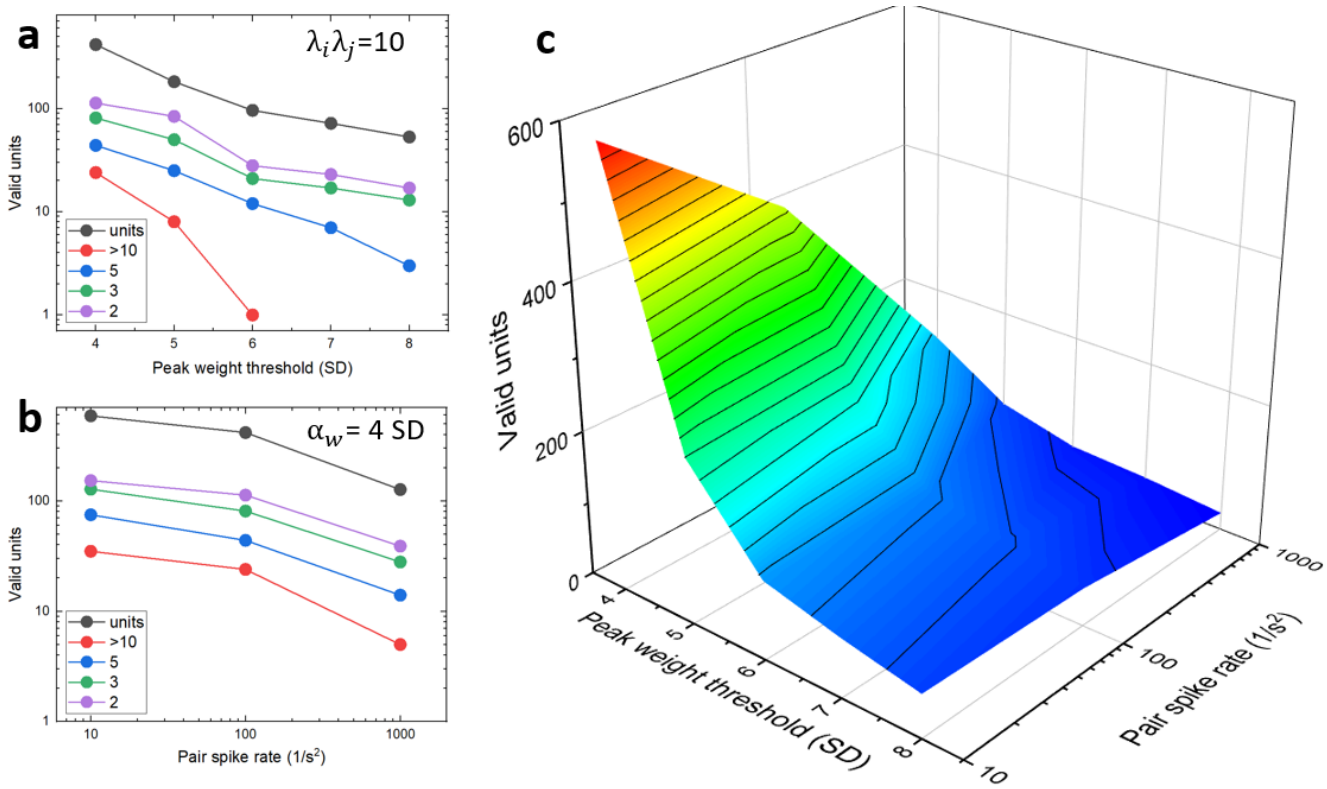

Fig.S6. Thresholds for units and pairs filtering

A) Number of valid units that form pairs (session #771160300) with distinct static peak (black curve) for different peak weight thresholds. Violet, green, blue, and red curves correspond to units that participate in formation of pairs, triplets, quintuplets, and connections above 10-tuples, correspondingly.

B) Number of valid units that form pairs with static peak above 4SD (black curve) for different pair spike rate. Violet, green, blue, and red curves correspond to units that participate in formation of pairs, triplets, quintuplets, and connections above 10-tuples, correspondingly.

C) 3D plot of a number of valid units that form pairs for different peak thresholds and pair spike rates.

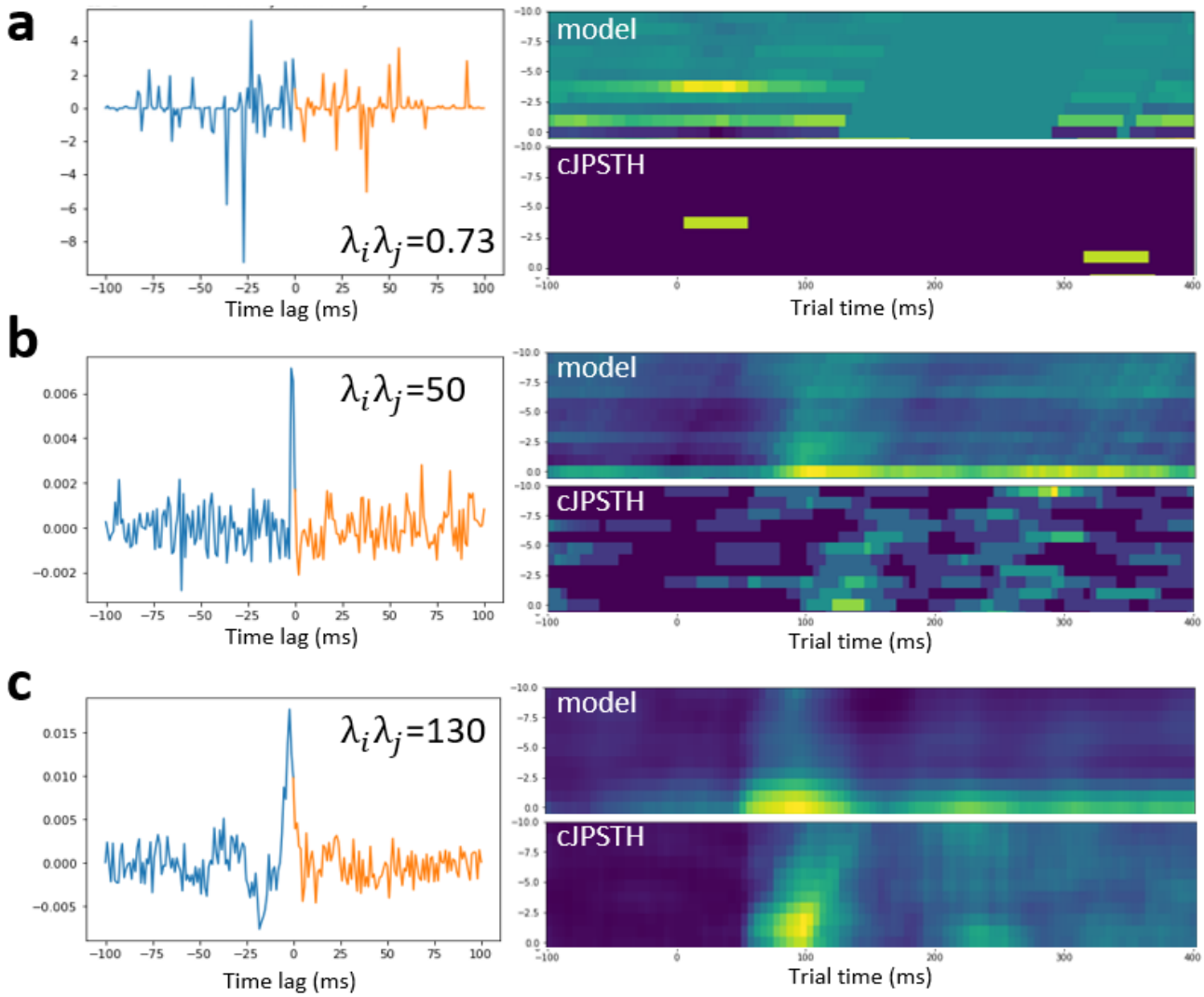

Fig.S7. Example of pairs and dynamic model performance

A) Example of a pair of units (session #771160300, excitatory units from VISam and VISpm areas with spike rates 1.92Hz and 0.35Hz) that pass a peak weight threshold of 7SD (left static weight matrix plot), however, has pair spike rate as small as 0.73 s^{-2}. Corresponding cJPSTH (bottom right) and dynamic weight plots (top right) are sparse.

B) Example of a pair of units (session #771160300, excitatory VISp unit with 7.2Hz spike rate and inhibitory VISp unit with 6.8Hz rate) that pass a peak weight threshold of 7SD (left static weight plot), however, has moderate pair spike rate of 50 s^{-2}. Corresponding cJPSTH and dynamic weight plots are shown on the right.

C) Example of a pair of units that pass peak weight threshold of 7SD (left static weight plot), that has a relatively high pair spike rate of 130 s^{-2}. Corresponding cJPSTH and dynamic weight plots are shown on the right.

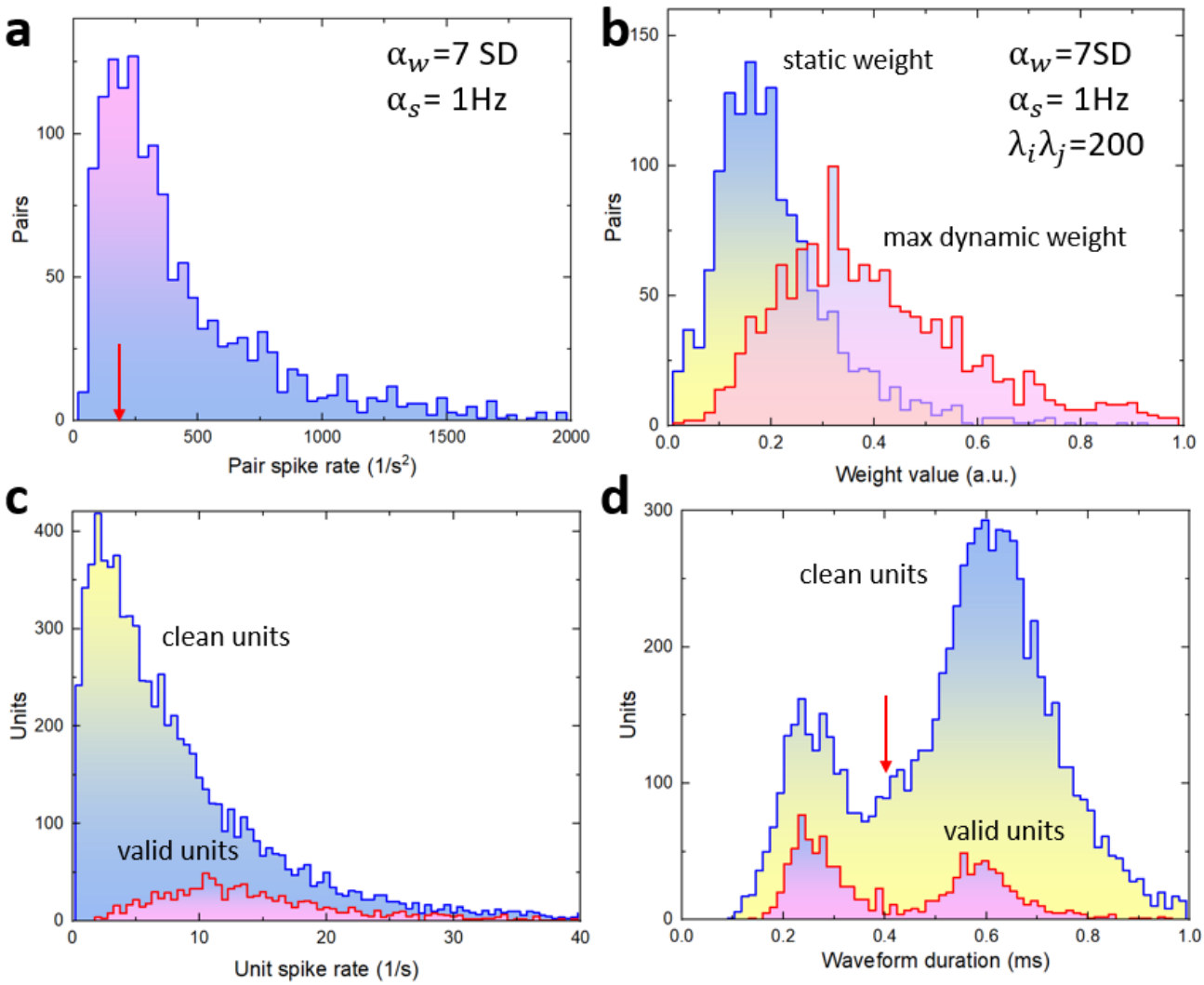

Fig.S8. Filtered pairs and potential biases

A) Histogram of pairs recorded in all VIS cortices for all 26 animals that pass 7SD peak weight threshold and are formed from units with spike rate exceeding 1Hz. Red arrow shows the pair spike threshold of 200 s^{-2}.

B) Histograms of inferred static and maximum dynamic weights for filtered pairs.

C) Histograms of unit spike rates for clean units and for valid units belonging to filtered pairs.

D) Histograms of waveform duration for clean units and valid units. Red arrow indicates a threshold to classify units as inhibitory or excitatory.

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