1 # QInfoMating: Sexual Selection and Assortative Mating
2 # Estimation Software
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Running headline: QInfomating

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Abstract

Background: Sexual selection theory is a multifaceted area of evolutionary research that has profound implications across various disciplines, including population genetics, evolutionary ecology, animal behavior, sociology, and psychology. It explores the mechanisms by which certain traits and behaviors evolve due to mate choice and competition within a species. In the context of this theory, the Jeffreys divergence measure, also known as population stability index, plays a key role in quantifying the information obtained when a deviation from random mating occurs for both discrete and continuous data.

Despite the critical importance of understanding mating patterns in the context of sexual selection, there is currently no software available that can perform model selection and multimodel inference with quantitative mating data. Recognizing this gap, I have developed QInfoMating which provides a comprehensive solution for analyzing and interpreting mating data within the framework of sexual selection theory.

Results: The program QInfoMating incorporates a user-friendly interface for performing statistical tests, best-fit model selection, and parameter estimation using multimodel inference for both discrete and continuous data. A use case is presented with real data of the species Echinolittorina malaccana.

Conclusions:

The application of information theory, model selection, and parameter estimation using multimodel inference are presented as powerful tools for the analysis of mating data, whether quantitative or categorical. The QInfoMating program is one of the few (if not the only) tools designed to perform this type of analysis.

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Introduction

By this point, there is no doubt about the importance of sexual selection theory and its impact in areas such as population genetics, evolutionary ecology, animal behavior, and even sociology and psychology. There are several strategies for measuring the impact of sexual selection, depending on the field of study and whether the available data pertain to discrete or continuous traits [1–3]. In previous works [2–4], it has been demonstrated

that the symmetric Kullback-Leibler divergence (also Jeffreys divergence or population

stability index), noted as J_{PTI} in [3] corresponds to the increase in information when

mating is not random. This divergence can be broken down additively into one

component that measures sexual selection and another that measures assortative mating,

and these statistics can be applied both to discrete and continuous data. Therefore, J_{PTI}

unifies the measure of sexual selection for both discrete and continuous traits [2].

The program QInfoMating is a major update (see below) to the Infomating program [3,

4] and incorporates the new quantitative methods developed in [2]. The previous

version (Infomating version $\leq$ 0.4) have already been utilized in empirical studies [5, 6].

While there are other software options available for computing sexual selection and

assortative mating from mating tables, such as JMating [7], to the best of my

knowledge, QInfoMating is the only software for applying model selection theory to

mating data, enabling the estimation of sexual selection and assortative mating for both

discrete and quantitative data.

Implementation

The backend of the program is implemented in C++11, while the interface is Python 3.

Therefore, QInfomating can be run via the user interface (Figure 1-A) or directly from

the console under Windows, Linux and macOS. Detailed instructions for use are

provided in the program manual

(https://acraaj.webs.uvigo.es/InfoMating/QInfoMating_v1.0_Manual.pdf), specifying

input formats, the meaning of parameters, models, and result files. In summary,

QInfoMating offers the capability to analyze both continuous and discrete data for

sexual selection and assortative mating. It begins by performing relevant statistical tests

to detect sexual selection and assortative mating and then identifies the best-fitting

68   model. The program employs multi-model inference techniques to estimate parameter

69   values.

Difference of QInfoMating with the previous version (Infomating)

71   Unlike the previous version (Infomating), which lacked a user-friendly interface and

72   only analyzed discrete data, QInfomating can be run via the user interface (Figure 1-A)

73   and now accepts continuous data as input (see the format specification in the program

74   manual). When continuous data is provided, the new statistical tests for sexual selection

75   and assortative mating detection, as developed in [2], are performed.

Sexual selection tests

77   Briefly (see ref. [2] for a more detailed explanation), we assume that traits *X* and *Y* are

78   normally distributed and the marginal density function for the trait in females within

79   matings is $f_1(x) \sim N(\mu_1, \sigma_1^2)$, and in the population is $f(x) \sim N(\mu_x, \sigma_x^2)$ then, the test for

80   sexual selection in females is

$$J_{S1} = \frac{1}{2} \left(\frac{\Phi_1^2 + 1}{\Phi_1} + \frac{\Phi_1 + 1}{\Phi_1} \frac{(\mu_1 - \mu_x)^2}{\sigma_x^2} - 2 \right)$$

82   where $\Phi_1 = \sigma_1^2 / \sigma_x^2$.

83   and similarly, the marginal density function for the trait in males within matings is $f_2(y)$

84   $\sim N(\mu_2, \sigma_2^2)$ and in the population is $g(y) \sim N(\mu_y, \sigma_y^2)$ then, the test for sexual selection in

85   males is

$$J_{S2} = \frac{1}{2} \left(\frac{\Phi_2^2 + 1}{\Phi_2} + \frac{\Phi_2 + 1}{\Phi_2} \frac{(\mu_2 - \mu_y)^2}{\sigma_y^2} - 2 \right)$$

where $\Phi_2 = \sigma_2^2 / \sigma_y^2$

and $J_{PSS} = J_{S1} + J_{S2}$.

For a random sample of n matings, nJ_{S1} and nJ_{S2} are asymptotically χ^2 distributed with 2

degrees of freedom [8, 9] under the null hypothesis that the females (males) within

matings are distributed with mean μ_x (μ_y) and variance σ_x^2 (σ_y^2) i.e. absence of sexual

selection.

If we want to test only the mean value of the female trait X in the mating sample, we set

$\Phi_1=1$ so that

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$$J_{S1\Phi_1=1}=\frac{(\mu_1-\mu_x)^2}{\sigma_1^2}=SSI_1^2$$

96   where SSI_1 is the standardized sexual selection intensity index [10–12].

97   And similarly for males

98
$$J_{S2\Phi_2=1}=\frac{(\mu_2-\mu_y)^2}{\sigma_2^2}=SSI_2^2.$$

Then with a sample size of n matings we have $(nJ_{S1\Phi=1})^{0.5} \sim t_{n-1}$ and $(nJ_{S2\Phi=1})^{0.5} \sim t_{n-1}$.

For large sample sizes both types of tests (χ^2 or t) work similarly, for a smaller sample

size the χ^2 test might be slightly liberal. More generally, the χ^2 test should also detect

differences in the variances, i.e., stabilizing (variance reduction) or diversifying

(variance increasing) selection, or combinations of these forms of selection with

directional selection (differences in means).

Assortative mating test

For assortative mating, assuming the quantitative traits we are measuring are normally

distributed and jointly normally distributed within mating pairs, the information

measure of assortative mating is a function of the square of correlation coefficient that

takes values within the set of non-negative real numbers $[0, +\infty)$, specifically (see ref [2]

for a more detailed explanation):

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$$J_{PSI} = \int\limits_{-a}^{+a} \int\limits_{-a}^{+a} (q'(x,y) - f_1(x)f_2(y)) \log \frac{q'(x,y)}{f_1(x)f_2(y)} \, dx \, dy = \frac{\rho^2}{1-\rho^2}$$

where $q'(x, y)$ is the mating probability density for pairs with values in the infinitesimal

interval ([$x, x + dx$], [$y, y + dy$]) and $f_1(x)$ and $f_2(y)$ are the marginal density functions for

the trait within matings in females and males, respectively [2].

For a random sample of n matings, nJ_{PSI} is asymptotically χ^2 distributed with 1 degree of

freedom under the null hypothesis that the mating probability distribution is equal to the

product of the female and male marginal distributions within matings [9].

Class frequency distribution

Once the statistical tests have been carried out, model selection is only executed if any

of the statistical tests yield a significant result. Following this, the program

automatically calculates the frequency distribution (classes) for the continuous data and

proceeds with multi-model estimation. The algorithm to obtain the frequency

distribution is detailed in the program manual. But it consists essentially of:

1- The range of the data set is calculated (maximum value *Max* - minimum value *Min*).

2- The formula that relates number of classes K and sample size n is [13]

126
$$K[\ln(K) + 0.5777] + \frac{1}{2} \leq \frac{n}{20 \ln(K)}$$

where we conservatively assume a sample size more than one order of magnitude larger

than that required for the uniform frequency case (details in the program manual).

3- The width w of each class is computed as w = (range / K).

4- Make the classes. The first class is always [*Min*, *Min* + w) and the last class is [x,

Max + w) where x is the maximum of the range of the previous class.

5- Compute the frequency for each class. Check that it is represented in each sex, if not,

decrease *K* and repeat from 3.

Set of models

There are also differences in the set of models considered for discrete and continuous

cases. In the discrete case, there is a default set of models that can be modified by the

user. Conversely, for the continuous case, the program, rather than the user, selects

models based on the statistical significance of various tests. Specifically, if there is a

statistically significant pattern of assortative mating but no sexual selection, the program

uses a set of models that incorporate mate choice and bias in conjunction with random

mating and the saturated model, but it does not include competition models. On the

other hand, if there is a statistically significant pattern of both assortative mating and

sexual selection in both sexes, QInfoMating includes double-effect models among the

models to be tested. These models are not included by default when the data is discrete.

In any case, QInfoMating still allows us to generate a mating table from the quantitative

data, enabling us to create an input file for analysis in discrete mode, employing the

default set of models or those selected by the user.

Results

Real data use case

Echinolittorina malaccana, a marine intertidal snail commonly found on rocky shores in

the Indo-West Pacific region [14], exhibits mate selection behaviors. Males have shown

a clear preference for females slightly larger than themselves [11]. In a subsequent study

conducted by [6], the continuous trait of size (specifically, shell length) was transformed

into categorical variables by creating four distinct size classes. This transformation

allowed for the creation of a mating table (see Table 1), which enabled the utilization of

the multimodel inference techniques available in the previous version of the program

(Infomating). This approach provided a more profound insight into the intricate

dynamics of mate choice. The analysis ultimately confirmed that the most suitable

model for mate choice in Echinolittorina malaccana involves a size bias, resulting in

both assortative mating and the presence of sexual selection favoring larger individuals.

In a recent study [2], the same onshore data, originally presented in [6], and accessible

via [15], was directly used without converting the continuous shell length trait into

discrete classes. This approach aimed to demonstrate the computation of Jeffreys

divergence indices [3] for quantitative traits. The research revealed that the statistical

tests for the quantitative data yielded similar conclusions as the previous analysis using

the statistical tests for discrete data. However, the quantitative data lacked the necessary

structure for applying the model selection methodology.

In this current study, we will leverage QInfoMating to conduct a quantitative analysis of

the same data set. The program will apply the quantitative statistical tests and

automatically transform data into classes to facilitate model selection and multi-model

inference. This analysis aims to compare the results with those obtained in [6]. For

consistency, we will employ the Akaike Information Criterion (AIC), the same criterion

used in [6], and additionally, the more conservative Bayesian Information Criterion

(BIC) to showcase the software's versatility and utility.

A CSV file containing shell length data for individual snails and their mate pairs served

as the input for QInfoMating. Although the original study by Lau et al. in [6], used four

classes, QInfoMating segmented the data into three classes (Table 2), before proceeding

with the model selection process.

If Figure 1-B the best-fit model from Lau et al. (B-7P, bias with 7 parameters model)

and the two best obtained by QInfoMating (D-3P, double 3 parameters, and B-5P, bias 5

parameters models) are presented. The D-3P model is a model with double effect i.e.,

generates sexual selection and assortative mating patterns. From Figure 1-B in the D-3P

model we appreciate that the choice parameters (main diagonal) are c_1 and c_3. The

parameter c_1 can also be considered a male sexual selection parameter jointly with c_2

since they change the marginal propensity for the second class males (second column).

However, from the point of view of biased choice, the parameter c_2 can be seen as a bias

(subdiagonal) in a model in which individuals in the shorter class have more difficulty

mating. In fact, the second best model was B-5P, which is the equivalent model to B-7P

when there are three classes instead of four.

 Figure 1. A: QInfomating user-friendly interface. B: Best-fitting models in the current

 analysis and previous work (see text).

 The best model by Lau et al. had a weight of 99%, so it is almost exact to the multi-

 model inference parameter matrix. In the case of QInfoMating, the best model (D-3P)

 had only 28% of the weight and other models such as B-5P (21%), D-5P (21%), D-4P

 (18%) and D-6P (8%), are necessary to capture more than 95% of the weight. The

 pattern obtained using the Bayesian Information Criterion (BIC) was similar to that

 obtained using the AIC criterion but with greater weight concentrated in the D-3P

 model (Table 3).

However, the structure of all these models is very similar: large males (rightmost

columns) choose females larger (closest to the bottom rows) than themselves, especially

for the largest classes (B_2 and B_3 parameters in the bias models, or c_2, c_3 in the D-3P

model) .

The pattern behind the QInfoMating models aligns with the findings reported by Lau et

al. [6] for the Multiple-design and Wild data, as depicted in their Figure 4. However,

there is a notable distinction: Lau et al. observed that the shorter class exhibited

considerably lower mating ability. This difference may be attributed to the presence of

their first class with a minimal number of individuals for both females and males, as

documented in Table 1.

However, one might wonder why QInfoMating did not clearly favor the B-5P model,

which is most akin to the B-7P model chosen in the original analysis by Lau et al [6].

The explanation lies in how QInfoMating operates when handling quantitative data. As

explained before, the program selects models based on the statistical significance of

various tests and have included double-effect models (as D-3P, D-4P and D-6P) among

the set of models to be tested. These particular models were not considered in the

original Lau et al. study.

To further elucidate, I excluded the double-effect models and repeated the analysis

using exactly the same set of models as in Lau et al. Upon conducting this analysis, the

best-fitting model becomes the B-5P, with a weight of 94%. The program's preference

for the D-3P model, when included, stems from its ability to explain the data with two

fewer parameters, thus aligning with the principle of parsimony. In cases where both

models are closely weighted, the choice between them is influenced by the researcher's

experience and the biological plausibility of the results. Nonetheless, it's worth noting

that the fundamental structure of these models remains quite similar: larger males tend

to prefer females larger than themselves, whenever such a pairing is possible.

Consistent with the result of models, the statistical tests performed by QInfoMating

detect assortative mating and sexual selection both in females and males (Table 4).

Discussion

Assortative mating based on size and other quantitative traits is common in many

species, from gastropods [11] to humans [16]. The processes leading to assortative

mating may not solely rely on similarity-based mechanisms and may not affect different

phenotypic classes equally. This is where the power of model selection methodology

becomes evident, as it doesn't require proposing a single ad hoc model. Instead, it

allows best fit of data for a wide range of models, enabling researchers to study non-

trivial mating patterns, some of which may not have been obvious before the

experiment.

Conclusion

239   In conclusion, the application of information theory, model selection, and parameter

240   estimation using multimodel inference are presented as powerful tools for the analysis

241   of mating data, whether quantitative or categorical. QInfoMating is software designed to

242   perform this type of analysis.

Availability and requirements

244   **Project name:** QInfomating

245   **Project home page:** https://acraaj.webs.uvigo.es/InfoMating/QInfomating.htm

246   **Operating system(s):** Windows, Linux, macOS

247   **Programming language:** C++, Python.

248   **License:** GNU GPL.

249   Declarations

• Data availability

The datasets generated and/or analysed during the current study are available in

the DRYAD repository, http://doi.org/10.5061/dryad.h214h8t

• Competing interests

The authors declare that they have no competing interests

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• Authors' contributions

ACR is the sole author of this work.

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267 **Tables**

269 **Table 1.** Mating table for the Wild data used in Lau et al [6]. The data is classified in
270 four classes.

Premating males numbers (421)			
23	181	167	50
Premating female numbers (455)			
23	146	190	96
Matings (228, rows are females)			
0	2	0	0
3	30	14	1
2	42	45	9
1	8	43	28

274   **Table 2.** Mating table generated by QInfoMating for the Wild data in Lau et al (2021).
275   The data is classified in three classes.

Premating males numbers (421)		
76	333	12
Premating female numbers (455)		
57	370	28
Matings (228, rows are females)		
4	6	0
18	163	2
1	30	4

Table 3. Models that accumulate up to 95% of the weight. The parameter notation corresponds to the B-7P model in Figure 1B where C_i represent the ith cell on main diagonal and B_i on the subdiagonal.

Analysis	Models (>95%)	Weight	Parameter estimation						
			C_1	C_2	C_3	C_4	B_1	B_2	B_3
Lau et al 2021	B-7P	99%	0	2	3	12	2	2	5
QInfoMating-AIC	D-3P	28%	1	3	22	-	1	6	-
QInfoMating-AIC	B-5P	21%	3	4	35	-	2	9	-
QInfoMating-AIC	D-5P	21%	3	4	35	-	2	9	-
QInfoMating-AIC	D-4P	18%	2	3	24	-	1	6	-
QInfoMating-AIC	D-6P	8%	3	4	36	-	2	10	-
QInfoMating-BIC	D-3P	85%	1	3	23	-	1	6	-
QInfoMating-BIC	D-4P	10%	2	3	24	-	1	6	-
QInfoMating-BIC	B-5P	2%	3	4	35	-	2	9	-
QInfoMating-BIC	D-5P	2%	3	4	35	-	2	9	-

284 **Table 4.** QInfoMating tests.

Test type	Statistic	H_0	p-value
Quantitative	$QJ_{PSI} = 0.49$	no assortative mating	$<10^{-6}$
Quantitative	$QJ_{PS1} = 0.24$	no female sexual selection	$<10^{-6}$
Quantitative	$QJ_{PS2} = 0.07$	no male sexual selection	0.0004
Discrete	$J_{PSI} = 0.08$	no assortative mating	0.0009
Discrete	$J_{PS1} = 0.17$	no female sexual selection	$<10^{-6}$
Discrete	$J_{PS2} = 0.06$	no male sexual selection	0.002