A novel interpretable deep transfer learning combining diverse learnable parameters for improved prediction of single-cell gene regulatory networks

Sumaya Alghamdi and Turki Turki *

Department of Computer Science, King Abdulaziz University, Jeddah 21589, Saudi Arabia

* Correspondence: tturki@kau.edu.sa

Abstract: Rapid progress in single-cell technologies has contributed to the availability of biological experiments pertaining to gene regulatory networks (GRNs). Although inferring GRNs can unveil insights about cellular mechanisms and functions to understand disease pathogenesis, existing deep learning tools are far from perfect and not providing appropriate interpretation as a guideline to explain the superior performance in the target task. Therefore, we provide an interpretation approach for our presented deep transfer learning (DTL) models to overcome such drawbacks, working as follows. We utilize several pre-trained models including SEResNet152, and SEResNeXt101. Then, we transfer knowledge from pre-trained models via keeping the weights in the convolutional base (i.e., feature extraction part) while modifying the classification part with the use of Adam optimizer to deal with classifying healthy controls and type 2 diabetes single-cell gene regulatory network (SCGRN) images. Another DTL models work in a similar manner but just with keeping weights of the bottom layers in the feature extraction unaltered while updating weights of consecutive layers through training from scratch. Experimental results on the whole 224 SCGRN images using 5-fold cross-validation show that our model (TFeSEResNeXT101) achieving the highest average balanced accuracy (BAC) of 0.97 and thereby significantly outperforming the baseline that resulted in an average BAC of 0.86. Moreover, the simulation study demonstrated that the superiority is attributed to the distributional conformance of model weight parameters obtained with Adam optimizer when coupled with weights from a pre-trained model.

Keywords: deep transfer learning; optimizers; explainable AI; classification; single-cell gene regulatory network

1. Introduction

Rapid advancement in single-cell technologies has played a key role in biological analysis and the existence of biological experiments related to gene regulatory networks [1-3]. By analyzing single-cell gene regulatory networks (SCGRNs), biologists can understand disease pathogenesis and treatment by unmasking various cellular mechanisms and functions pertaining to cellular heterogeneity presented at the tissue level [4, 5].

Xu et al. [6] proposed a supervised learning method based on transformer, STGRNS, to infer single-cell gene regulatory networks. First, the input data composed of the concatenation of expression values for transcription factors (TFs) and target gene (TGs). Then, providing the input data to transformer encoder, followed by classification layer determining if TF regulating a target gene or not for the reconstruction of single-cell gene regulatory networks. To interpret the supervised method, they provided a visualization of the classification and encoder layers. Experimental results demonstrate the good performance of their proposed method. Keyl et al. [7] proposed a supervised deep learning approach using layer-wise relevance propagation (LRP) [8, 9], to predict and explain the prediction of single-cell gene regulatory networks. Their proposed approach depends on scoring all pairwise of genes provided via LRP. The strengths of the scoring guide the

process of inferring the single-cell gene regulatory networks. Experimental results using single cell data pertaining to normal cells and tumor lung cancer cells demonstrate the feasibility of the proposed approach in inferring single-cell gene regulatory networks.

Turki et al. [10] presented a deep learning approach to discriminate between heathy controls and T2D SCGRN images as follows. First, single-cell gene expression data from the ArrayExpress repository was processed with the use of bigSCale and NetBioV packages, generating 224 SCGRN images. The class distribution was distributed evenly in terms of healthy controls and T2D images. Then, utilizing RMSprop optimizer with the following deep learning models: VGG16, VGG19, Xception, ResNet50, ResNet101, DenseNet121, and DenseNet169 to classify the SCGRNs. Experimental results demonstrated the VGG19 performed better than studied deep learning models. However, no interpretation was provided to back the prediction performance.

Although these recently developed methods aimed to address the task of prediction single-cell gene regulatory networks as well as justifying the superiority via interpreting models, these methods are still far from perfect and do not provide adequate interpretation for practical deep transfer learning models aiding in the explanation of the performance superiority. Therefore, this study is unique in the following aspects: (1) we present highly accurate deep transfer learning models working by combining weight parameters from pre-trained models and weights obtained with the use of Adam optimizer; (2) we provide, to the best of our knowledge, the first interpretation behind deep transfer learning models inspecting and quantifying that conformance of pre-trained model weight parameters with weight parameters obtained with the incorporation of Adam and RMSprop Optimizers. This interpretation framework can guide in the process of designing highly efficient deep transfer learning models applicable to wide range of problems; and (3) we conduct experimental study to report the prediction performance and computational running time for the task of predicting single-cell gene regulatory network images pertaining to healthy controls and type 2 diabetes. Experimental results demonstrate the superiority of our deep transfer learning model, TFeSEResNeXT101, performing better than the baseline with 11% improvements. In terms of the running time, our deep learning models exhibited a significant reduction in training time attributed to transfer learning, which reduced the number of trainable weight parameters. In addition, simulation study unveiled the conformance of parameter weights of both transfer weights from pre-trained models with weights obtained from Adam optimizer as compared to RMSprop that was used by the baseline and resulted in inferior prediction performance, attributed to the divergence of its weight parameters from the weight parameters of pre-trained models.

2. Materials and Methods

2.1. Biological Networks

We provide an illustration in Figure 1 for the biological networks used in this study, which were downloaded from [10] and consisted of 224 SCGRN images pertaining to healthy and type 2 diabetes. The class distribution for these biological network images is balanced (i.e., 224 divided evenly into the two classes). These biological network images were produced with the help of bigSCale package [11, 12] to process the single-cell gene expression data and build regulatory networks, then visualizing networks via the NetBioV package [13]. *In terms of the single-cell gene expression data pertaining to healthy controls and T2D patients, it was obtained from ArrayExpress repository under accession numbers E-MTAB-5061 [14].*

2.2. Deep Transfer Learning

Figure 1 demonstrates how our deep transfer learning approach is performed. First, we adapt the following pre-trained models: VGG19 [15], DenseNet201 [16], InceptionV3 [17], ResNet50V2, ResNet101V2 [18], SEResNet152, and SEResNeXt101 [19]. Each pre-trained model has a feature extraction part (i.e., series of convolutional and pooling layers) for feature extraction and a densely connected classifier for classification. Then, we keep the weights unchanged for the feature extraction part of a pre-trained model and change the densely connected classifier to deal with binary classification instead of 1000 classes. Therefore, when feeding the SCGRN image dataset, we extract features using weights of pre-trained models while training the densely connected classifier from scratch and performing prediction. We refer to models using this type of deep transfer learning computations as TFeVGG19, TFeDenseNet201, TFeInceptionV3, TFeResNet50V2, TFeResNet101V2, TFeSEResNet152, and TFeSEResNeXT101 (see Figure 2). For the other deep transfer learning computations, we keep weights of the bottom layers unchanged in the feature extraction part while performing training from scratch to change weights of top layers in feature extraction part and densely connected layers. As in TFe-based models, we modify the densely connected classifier dealing with binary classification problem before performing the training phase. As seen in Figure 3, we refer to models employing this type of deep transfer learning as TFtVGG19, TFtDenseNet201, TFtInceptionV3, TFtResNet50V2, TFtResNet101V2, TFtSEResNet152, and TFtSEResNeXT101.

Figure 1: Flowchart of the deep transfer learning-based approach for the inference of SCGRNs.

Figure 2: Transfer learning applying feature extraction with new classifier (TFe) for the inference of SCGRNs.   119

Figure 3: Transfer learning applying fine tuning with new classifier (TFt) for the inference of SCGRNs.   121

When changing weights during training, we employed three optimizers: Adam [20] , RMSprop [21], and SGD [22]. When weights are kept unchanged referring to the transfer of knowledge from pre-trained models using SGD optimizer. In terms of predictions of unseen SCGRN images, predictions are mapped to healthy control subjects if the predicted values are greater than 0.5. Otherwise, predictions are mapped to T2D.

3. Results

3.1. Classification Methodology

In this study, we considered seven pre-trained models, namely VGG19, DenseNet201, InceptionV3, ResNet50V2, ResNet101V2, SEResNet152, and SEResNeXt10. Each of the pre-trained models was trained on 1.28 million images from ImageNet database to classify images into 1000 different categories. In terms of TFe-based models, we used the feature extraction part of pre-trained models in which weights were kept unchanged and were used to extract feature from SCGRN images. Moreover, the densely connected classifier was trained from scratch to handle the binary class classification problem. Regarding the TFt-based models, we trained the top layers and densely connected classifier from scratch while retaining the weights of bottom layers unchanged in the feature extraction part. For both TFt- and TFe-based models, we employed Adam optimizer when updating weights of layers. Moreover, we compared the performance of our deep transfer learning approaches using different optimizers including the baseline (i.e., RMSprop optimizer) as well as against training models from scratch. We set optimization parameters as follows: 0.00001 for the learning rate, and 10 for the number of epochs. In terms of the loss function, we utilized categorical cross-entropy [23].

To assess the performance of studied models, we employed Balanced Accuracy (BAC), Accuracy (ACC), Precision (PRE), Recall (REC), and F1 computed as follows:

$$\text{BAC} = \frac{1}{2}\left(\frac{TP}{TP + FN} + \frac{TN}{TN + FP}\right) \tag{1}$$

$$\text{ACC} = \frac{TP + TN}{TP + TN + FP + FN} \tag{2}$$

$$\text{PRE} = \frac{TP}{TP + FP} \tag{3}$$

$$\text{REC} = \frac{TP}{TP + FN} \tag{4}$$

$$\text{F1} = \frac{2 * PRE * REC}{PRE + REC} \tag{5}$$

where *TN* designates true negative, corresponding to the number of T2D images that were correctly predicted as T2D. *FP* designates false positive, corresponding to the number of T2D images that were incorrectly predicted as healthy controls. *TP* designates true positive, corresponding to the number of healthy control images that were correctly predicted as healthy controls. *FN* designates false negative, corresponding to the number of healthy control images that were incorrectly predicted as T2D.

To evaluate the results on the whole SCGRN images dataset, we employed 5-fold cross-validation as follows. We partitioned the SCGRN images datasets and randomly assigned images into 5 folds. During the first run of 5-fold cross-validation, we used 4 of the folds to train our deep learning models and perform predictions to the remaining fold for testing and record the performance results. Such a process was repeated for an

additional 4 runs in which performance results were recorded. Finally, we report the average performance results corresponding to the results obtained from 5-fold cross-validation.

3.2. Implementation Details

All experiments were run on a machine equipped on central processing unit (CPU) of Google Colab. The specifications of CPU runtime offered by Google Colab were Intel Xeon Processor with two cores with 2.30 GHz and 13 GB RAM where the installed version of Python is 3.10.11. For the analysis of models, we used R statistical software [24] to run the experiments and utilized the optimg package in R to run Adam optimizer [25]. All plots were performed using Matplotlib package in python [26].

3.3. Classification Results

3.3.1. Training Results

In Figure 4, we illustrate the training accuracy performance results when running 5-fold cross-validation. It can be seen that our models outperformed all other models trained from scratch. Specifically, TFeVGG19 and TFtVGG19 achieved average accuracies of 0.976 and 0.962, respectively, while VGG19 achieved an average accuracy of 0.530. TFeDenseNet201 outperformed DensNet201 via achieving an average accuracy of 0.988 while DenseNet201 performed better than TFtDenseNet201 via achieving an average accuracy of 0.982 compared to 0.946. For TFe- and TFt-based models when coupled with ResNet101V2, SEResNet152 and SEResNetXT101, they outperformed their counterparts when not applying deep transfer learning models. These superior performance results are attributed to the learned representation using transfer learning.

Figure 4: The boxplots presenting the average 5-fold cross-validation results using the ACC measure for the training folds. (a) Deep transfer learning models using feature extraction (referred with the prefix TFe). (b) Deep transfer learning models using fine tuning (referred with the prefix TFt). (c) Deep learning models trained from scratch. ACC is accuracy.

3.3.2. Testing Results

Figures 5 and 6 report the generalization (i.e., test) accuracy performance results and combined confusion matrices, respectively, when 5-fold cross-validation is utilized. TFeSeResNeXT101 achieved the highest average accuracy of 0.968.

Figure 5: The boxplots presenting the average 5-fold cross-validation results using the ACC measure for the testing folds. (a) Deep transfer learning models using feature extraction (referred with the prefix TFe). (b) Deep transfer learning models using fine tuning (referred with the prefix TFt). (c) Deep learning models trained from scratch. Acc is accuracy.

Figure 6: Combined confusion matrices for all methods during the running of 5-fold cross-validation.

The second-best model is TFeDenseNet201, achieving an average accuracy of 0.958, followed by TFeVGG19, TFeResNet50V2, TFeSEResNet152, TFeInceptionV3, and TFeResNet101V2 (generating average accuracies of 0.946, 0.940, 0.936, 0.930, and 0.918, respectively). TFt-based models also outperformed all models trained from scratch (See Figure 5(b and c)). Particularly, TFt-based models generated average accuracies lower and upper bounded by 0.864 and 0.916, respectively, while models trained from scratch were lower and upper bounded by average accuracies of 0.468 and 0.590. These results demonstrate the superior performance of models employing our deep transfer learning computations.

In terms of reporting testing performance results using different metrics, our model TFeSeResneXT101 outperforms all other models (See Table 1) via achieving an average BAC of 0.97, average PRE of 0.97 (tie with our model TFeSEResNet152), and average F1 of 0.97. Moreover, TFeVGG19 and TFtVGG19 perform better than VGG19. Similarly, TFeDenseNet201, TFeInceptionV3, TFeResNet50V2, TFeResNet101V2, and TFeSEResNet152 performed better than DenseNet201, InceptionV3, ResNet50V2, ResNet101V2, and SEResNet152, respectively. Th same holds true for TFt-based models outperforming their counterparts (i.e., VGG19, DenseNet201, InceptionV3, ResNet50V2, ResNet101V2, SEResNet152, and SEResNetXT101)

Table 1: Reported average performance results during the running of 5-fold cross-validation on testing using studied models. BAC is balanced accuracy. PRE is precision. REC is recall. The best overall result is underlined and is shown in bold. The method outperforming its counterparts is just underlined.

Model	Optimizer	BAC	PRE	REC	F1
TFeVGG19	Adam	<u>0.94</u>	<u>0.95</u>	0.94	<u>0.94</u>
TFtVGG19	Adam	0.90	0.82	<u>**0.97**</u>	0.89
VGG19	Adam	0.50	0.37	0.46	0.41
TFeDenseNet201	Adam	<u>0.96</u>	<u>0.95</u>	<u>0.95</u>	<u>0.96</u>
TFtDenseNet201	Adam	0.90	0.91	0.90	0.90
DenseNet201	Adam	0.50	0.20	0.51	0.29
TFeInceptionV3	Adam	<u>0.93</u>	<u>0.95</u>	0.91	<u>0.92</u>
TFtInceptionV3	Adam	0.87	0.76	<u>0.92</u>	0.83
InceptionV3	Adam	0.50	0.91	0.50	0.64
TFeResNet50V2	Adam	<u>0.93</u>	0.93	<u>0.92</u>	<u>0.93</u>
TFtResNet50V2	Adam	0.87	<u>0.95</u>	0.81	0.87
ResNet50V2	Adam	0.50	-	-	-
TFeResNet101V2	Adam	<u>0.92</u>	<u>0.92</u>	<u>0.91</u>	<u>0.92</u>
TFtResNet101V2	Adam	0.89	0.90	0.86	0.88
ResNet101V2	Adam	0.52	0.75	0.49	0.59
TFeSEResNet152	Adam	<u>0.94</u>	<u>**0.97**</u>	<u>0.90</u>	<u>0.93</u>
TFtSEResNet152	Adam	0.88	0.96	0.81	0.88
SEResNet152	Adam	0.55	0.67	0.50	0.57
TFeSEResNeXT101	Adam	<u>**0.97**</u>	<u>**0.97**</u>	<u>0.96</u>	<u>**0.97**</u>
TFtSEResNeXT101	Adam	0.90	0.96	0.90	0.91
SEResNeXT101	Adam	0.60	0.56	0.60	0.58

Table 2 reports our best deep transfer learning models with different optimizers. It can be shown that TFeSeResNeXT101 and TFtSeResNeXT101 generate the highest performance results when coupled with Adam optimizer method. Specifically, TFeSEResNeXT101 with Adam optimizer generates the highest average BAC (and F1) of 0.97 (and 0.97). TFtSEResNeXT101 with Adam optimizer archives the highest average

BAC of 0.91, highest average F1 of 0.90 (tie with SGD optimizer). When 248
TFeSEResNeXT101 and TFtSEResNeXT101 are coupled with SGD optimizer, they gener- 249
ate inferior performance results. 250

Table 2: Performance comparison of our best deep transfer learning model under differ- 251
ent optimizers during the 5-fold cross-validation. BAC is balanced accuracy. Best perfor- 252
mance result is shown in bold. 253

Model	Optimizer	BAC	F1
	Adam	**0.97**	**0.97**
TFeSEResNeXT101	RMSprop	0.92	0.92
	SGD	0.77	0.77
	Adam	**0.91**	**0.90**
TFtSEResNeXT101	RMSprop	0.90	0.89
	SGD	0.90	**0.90**

In Table 3, we compare our model TFeVGG19 with Adam optimizer against the best 255
performing baseline TFeVGG19 with RMSprop optimizer, named VGG19 in [10]. It is ev- 256
ident that our model TFeVGG19 with Adam optimizer achieves the highest average BAC 257
of 0.94 while the baseline obtained an average BAC of 0.86. Moreover, when F1 perfor- 258
mance measure is considered, TFeVGG19 with Adam optimizer attains the highest aver- 259
age F1 of 0.94 while the baseline achieved an average F1 of 0.88. The same holds true for 260
TFtVGG19, which achieved the highest average BAC of 0.91, highest average F1 of 0.90 261

Table 3: Performance comparison of our deep transfer learning model against recent 263
baseline methods when 5-fold cross-validation is employed. BAC is balanced accuracy. 264
Best performance result is shown in bold. 265

Model	Optimizer	BAC	F1
	Adam (Ours)	**0.94**	**0.94**
TFeVGG19	RMSprop (Baseline)	0.86	0.88
	Adam (Ours)	**0.91**	**0.90**
TFtVGG19	RMSprop (Baseline)	0.89	0.89

Figure 7: Running time comparisons in seconds for selected models when running 5-fold 267
cross-validation. 268

In Figure 7, we report the running time in seconds for the process of running 5-fold cross-validation when utilizing our best model TFeSEResNeXT101 and TFeSEResNeXT101 compared to their peer SeResneXT101. Our model TFeSEResNeXT101 is 208.45x faster than SEResNeXT101. Also, our model TFtSEResNeXT101 is 3.82x faster than SEResNeXT101. Moreover, TFeVGG19 and TFtVGG19 are 802.67x and 2.53x, respectively, faster than VGG19. These results demonstrate the computational efficiency of the deep transfer learning models, in addition to the highly achieved performance results.

3.4. Models Introspection

3.4.1. Stochastic Gradient Descent (SGD)

To minimize the objective function $Q(\theta_0, \theta_1)$ for parameters θ_0 and θ_1 of model $H(x_i)$, we employ gradient descent optimization algorithms to find θ_0 and θ_1 minimizing the objective function. The optimization problem can be formulated as follows:

$$
\begin{aligned}
\min_{\theta_0,\theta_1} Q(\theta_0, \theta_1) &= \frac{1}{m} \sum_{i=1}^{m} Q_i(\theta_0, \theta_1) \\
&= \frac{1}{m} \sum_{i=1}^{m} (H(x_i) - y_i)^2 \\
&= \frac{1}{m} \sum_{i=1}^{m} (\theta_0 + \theta_1 x_i - y_i)^2
\end{aligned}
\tag{6}
$$

We utilize SGD, RMSprop, and Adam optimization algorithm to minimize the objective function and estimate the model parameters. For SGD, we initialize the parameters θ_0 and θ_1 according to the uniform distribution $U(0,1)$ and setting the learning rate $\eta = 0.001$, maximum number of iterations to 3000. Then, in each time, shuffling the data of m examples followed by looping m times over the following to update model parameters After the end of looping, the algorithm stops if the maximum number of iterations is reached or $\|\nabla Q(\theta_0, \theta_1)\| \leq 0.001$:

$$
\begin{aligned}
\theta_0 &:= \theta_0 - \eta \cdot \frac{\partial Q_i}{\partial \theta_0} \\
&:= \theta_0 - \eta.2(\theta_0 + \theta_1 x_i - y_i) \\
\theta_1 &:= \theta_1 - \eta \cdot \frac{\partial Q_i}{\partial \theta_1} \\
&:= \theta_1 - \eta.2x_i(\theta_0 + \theta_1 x_i - y_i)
\end{aligned}
\tag{7}
$$

3.4.2. Root Mean Square Propagation (RMSprop)

For RMSprop, we initialize model parameters according to uniform distribution $U(0,1)$, set the learning rate $\eta = 0.001$, maximum number of iterations to 3000, $\beta = 0.9$, $\epsilon = 10^{-6}$, BatchSize = 16, referred in the following as $|S|$. Then, looping to update model parameters according to each selected batch. After ending of looping over all selected batches, the algorithm terminates when $\|\nabla Q(\theta_0, \theta_1)\| \leq 0.001$ or the maximum number of iterations is reached:

$$v_{\theta_0} := \beta.v_{\theta_0} + (1 - \beta)(\frac{\partial Q}{\partial \theta_0})^2 \qquad (8)$$

$$:= \beta.v_{\theta_0} + (1 - \beta)(\frac{2}{|S|} \sum_i (\theta_0 + \theta_1 x_i - y_i))^2$$

$$v_{\theta_1} := \beta.v_{\theta_1} + (1 - \beta)(\frac{\partial Q}{\partial \theta_1})^2$$

$$:= \beta.v_{\theta_1} + (1 - \beta)(\frac{2}{|S|} \sum_i (\theta_0 + \theta_1 x_i - y_i).x_i)^2$$

$$\theta_0 := \theta_0 - \frac{\eta}{\sqrt{v_{\theta_0 + \epsilon}}} \frac{\partial Q}{\partial \theta_0}$$

$$:= \theta_0 - \frac{\eta}{\sqrt{v_{\theta_0 + \epsilon}}} (\frac{2}{|S|} \sum_i (\theta_0 + \theta_1 x_i - y_i))$$

$$\theta_1 := \theta_1 - \frac{\eta}{\sqrt{v_{\theta_1 + \epsilon}}} \frac{\partial Q}{\partial \theta_1}$$

$$:= \theta_1 - \frac{\eta}{\sqrt{v_{\theta_1 + \epsilon}}} (\frac{2}{|S|} \sum_i (\theta_0 + \theta_1 x_i - y_i)x_i)$$

<div style="text-align:right">304</div>

3.4.3. Adaptive Moment Estimation (Adam)

<div style="text-align:right">305</div>

  In terms of Adam, $m_{\theta_0}, m_{\theta_1}, v_{\theta_0}, v_{\theta_1}, \beta_1, \beta_2, \epsilon, and \eta$ are initialized as in [27]. Then, looping to update model parameters according to all selected batches of examples. After ending of looping over all selected batches, the algorithm stops if the maximum number of iterations (i.e., 3000) is reached or $\|\nabla Q(\theta_0, \theta_1)\| \leq 0.001$: 306
307
308
309

<div style="text-align:right">310</div>

$$m_{\theta_0} := \beta_1.m_{\theta_0} + (1 - \beta_1)(\frac{\partial Q}{\partial \theta_0}) \qquad (9)$$

$$:= \beta_1.m_{\theta_0} + (1 - \beta_1)(\frac{2}{|S|} \sum_i (\theta_0 + \theta_1 x_i - y_i))$$

$$m_{\theta_1} := \beta_1.m_{\theta_1} + (1 - \beta_1)(\frac{\partial Q}{\partial \theta_1})$$

$$:= \beta_1.m_{\theta_1} + (1 - \beta_1)(\frac{2}{|S|} \sum_i (\theta_0 + \theta_1 x_i - y_i)x_i)$$

$$v_{\theta_0} := \beta_2.v_{\theta_0} + (1 - \beta_2)(\frac{\partial Q}{\partial \theta_0})^2$$

$$:= \beta_2.v_{\theta_0} + (1 - \beta_2)(\frac{2}{|S|} \sum_i (\theta_0 + \theta_1 x_i - y_i))^2$$

$$v_{\theta_1} := \beta_2.v_{\theta_1} + (1 - \beta_2)(\frac{\partial Q}{\partial \theta_1})^2$$

$$:= \beta_2.v_{\theta_1} + (1 - \beta_2)(\frac{2}{|S|} \sum_i (\theta_0 + \theta_1 x_i - y_i).x_i)^2$$

$$\widehat{m}_{\theta_0} := \frac{m_{\theta_0}}{(1-\beta_1)}$$

$$\widehat{m}_{\theta_1} := \frac{m_{\theta_1}}{(1-\beta_1)}$$

$$\widehat{v}_{\theta_0} := \frac{v_{\theta_0}}{(1-\beta_2)}$$

$$\widehat{v}_{\theta_1} := \frac{v_{\theta_1}}{(1-\beta_2)}$$

$$\theta_0 := \theta_0 - \frac{\eta}{\sqrt{\widehat{v}_{\theta_0}} + \epsilon} \widehat{m}_{\theta_0}$$

$$\theta_1 := \theta_1 - \frac{\eta}{\sqrt{\widehat{v}_{\theta_1}} + \epsilon} \widehat{m}_{\theta_1}$$

3.4.4. Simulated Data

<div style="text-align: right">311</div>

To demonstrate the efficiency of the proposed deep transfer learning models incorporation mixed parameters derived from both SGD and Adam, we conducted simulation studies to explain the superiority behind the proposed models as well as imitate the numerical behavior. Particularly, we consider the following four predictive models:

$$F_1(x) = 0.5 + 0.79x + \epsilon \tag{10}$$

$$F_2(x) = 1 - \exp\left(\frac{-1}{2x}\right) \tag{11}$$

$$F_3(x) = 0.7 + 3x^2 + \epsilon \tag{12}$$

$$F_4(x) = (6x - 2)^2 + \sin(12x - 4) \tag{13}$$

where $X \sim U(0,1)$ and $\epsilon \sim N(0,0.2)$, where $U()$ and $N()$ are uniform and normal distributions, respectively. For F_1, when we have X and $Y=F_1(X)$, we perform the following steps. Let $H_{SGD}(x_i) = \theta_0 + \theta_1 x_i$ (for i =1..m) be the model in which we want to estimate parameters using (X,Y) data from F_1 coupled with Equation 7. Similarly, let $H_{RMSprop}(x_i)$ and $H_{Adam}(x_i)$ be models in which we want to estimate their parameters using Equations 8 and 9, respectively, coupled with (X,Y) data from F_1. Then, we provide each $x_i \in X$ to perform predictions corresponding to y_i'. In Figure 8, we report 2D plots for X and predicted $Y' = \{y_1', ..., y_m'\}$ via each model using data generated according to Equation 10, where Adam refers to plotting $(x_i, H_{SGD}(x_i))$ while Adam and RMSprop refers to plotting results obtained via $(x_i, H_{Adam}(x_i))$ and $(x_i, H_{RMSprop}(x_i))$, respectively, and i=1..m. We then repeat this process for an additional 8 runs. Therefore, we have 9 runs in total

Figure 8: Plots for the three models as $(x_i, H_{SGD}(x_i))$, $(x_i, H_{Adam}(x_i))$, and $(x_i, H_{RMSprop}(x_i))$ for i=1..m according to x_i generated using F_1.

It can be seen from Figure 8 that model induced via RMSprop has more distributional differences compared to those obtained via SGD and Adam. To quantify distributional differences between SGD and Adam against SGD and RMSprop, we perform the following computations:

$$d_{SA} = \sqrt{\sum_i \left(\left(x_i^{SGD} - x_i^{Adam} \right)^2 + \left(z_i^{SGD} - z_i^{Adam} \right)^2 \right)} \tag{14}$$

$$d_{SR} = \sqrt{\sum_i \left(\left(x_i^{SGD} - x_i^{RMSprop} \right)^2 + \left(z_i^{SGD} - z_i^{RMSprop} \right)^2 \right)} \tag{15}$$

where d_{SA} measuring the distance between data associated with SGD and Adam. Similarly, d_{SR} measures the distance between data associated with SGD and RMSprop. The lower the distance value, the less the distribution difference is. Figure 12(a) plots d_{SA} and d_{SR} for the 9 runs. It can be seen that $H_{Adam}(x_i)$ is closer to $H_{SGD}(x_i)$ than $H_{RMSprop}(x_i)$ to $H_{SGD}(x_i)$ in most runs. Moreover, the distributional differences are statistically significant (P-value = 7.28×10^{-14} from t-test).

Figure 9: Plots for the three models as $(x_i, H_{\text{SGD}}(x_i))$, $(x_i, H_{\text{Adam}}(x_i))$, and $(x_i, H_{\text{RMSprop}}(x_i))$ for i=1..m according to x_i generated using F2

These results demonstrate conformance of the weight parameters of models utilizing Adam and SGD optimizers. Figure 9 reports the 2D plots of three induced models as $(x_i, H_{SGD}(x_i))$, $(x_i, H_{Adam}(x_i))$, and $(x_i, H_{RMSprop}(x_i))$ for i=1..m using data generated according to Equation 11 (i.e., F2) [28]. It can be clearly seen that the data distributional difference of results via SGD is closer to that of Adam when compared to results obtained with the help of RMSprop. In Figure 12(b), we quantify distributional differences using Equations 14 and 15. It can be shown that Adam is closer to SGD as shown from AdamSGD when compared to that of RMSprop to SGD (i.e., RMSpropSGD) over the 9 runs.

The quantification of AdamSGD is attributed to d_{SA} while RMSpropSGD is attributed to d_{SR}. In addition, the distributional differences between AdamSGD and RMSpropSGD are statistically significant (P-value = 7.01×10^{-7} from t-test).

Figure 10: Plots for the three models as $(x_i, H_{\text{SGD}}(x_i))$, $(x_i, H_{\text{Adam}}(x_i))$, and $(x_i, H_{\text{RMSprop}}(x_i))$ for i=1..m according to x_i generated using F$_3$.

Figure 11: Plots for the three models as $(x_i, H_{\text{SGD}}(x_i))$, $(x_i, H_{\text{Adam}}(x_i))$, and $(x_i, H_{\text{RMSprop}}(x_i))$ for i=1..m according to x_i generated using F$_4$.

Figures 10 and 11 report 2D plots of $(x_i, H_{SGD}(x_i))$, $(x_i, H_{Adam}(x_i))$, and $(x_i, H_{RMSprop}(x_i))$ for i=1..m using generated data of Equations 12 (F₃) and 13 (F₄) [29], where models were induced with SGD, Adam, and RMSprop optimizers. It can be seen from the alignment of Adam with SGD that Adam has a closer data representation to SGD compared to RMSprop to SGD. When quantifying the data distributional differences in Figure 12 (c and d), it can be clearly shown that the distributional differences of SGD and Adam (referred to AdamSGD) are closer than SGD to RMSprop over the 9 runs.

Figure 12: Boxplots of the four studied models, F₁-F₄, showing the distance distribution over nine runs for AdamSGD and RMSpropSGD. a) results for F₁. B) results for F₂. c) results for F₃. d) results for F₄.

These quantified results for AdamSGD and RMSprop are attributed to d_{SA} and d_{SR}, respectively. Additionally, the distributional differences of between AdamSGD and RMSprop were statistically significant (P-value = 3.48×10^{-12} from t-test when F3 is used while P-value = 1.49×10^{-3} from t-test when F4 is used). These results demonstrate the stable performance when SGD is coupled with Adam.

4. Discussion

Our deep transfer learning models work as follows. In the TFe-based models, the convolutional base (also called the feature extraction part) in the pre-trained model is left unchanged while the densely connected classifier is modified to deal with the binary class classification at hand. Therefore, we applied the features extraction part of pre-trained models to the SCGRN images to extract features followed by a flattening step to train densely connected classifier from scratch. It can be noted that only weights of densely connected classifier are changed according to Adam optimizer while we transferred knowledge (i.e., weights) of the feature extraction part from pre-trained models. In terms of the TFt-based models, we keep weights of the bottom layers in the feature extraction part of pre-trained models unchanged while modifying weights in the proceeding layers including the densely connected classifier according to the Adam optimizer. Moreover, the densely connected classifier was altered to deal with the binary class classification problem pertaining to distinguishing between healthy controls and T2D SCGRN images. It can be seen that updating model weight parameters is done through the training with the use of Adam optimizer.

When conducting experimental study to assess deep transfer learning models, we used different optimizers, including SGD, RMSprop, and Adam. For SGD optimizer used in our deep transfer learning models, the model weight parameters were different than deep transfer models coupled with RMSprop and Adam optimizers. Therefore, we induced three sets of different models attributed to the three optimizers. Experimental results demonstrate the superiority of deep transfer learning models utilizing SGD and Adam optimizers when compared to that using SGD and RMSprop optimizers.

In our deep transfer learning models, we have transferred weights from pre-trained models coupled with weights obtained with the help of Adam optimizer. If weight parameters obtained using two optimizers are close, then the two models almost behave the same. On the other hand, when the weight parameters resulted from two optimizers are not close, then the two models behave differently. To mimic the real scenario and investigate the effects of coupling different model weight parameters, we performed a simulated study. In Figures 8-12, we showed that a model induced with the help of SGD optimizer is closer to a model induced with Adam optimizer when compared to a model induced with the help of RMSprop optimizer. It can be evident from visualized results in our study that SGD and Adam had less distributional differences than that of SGD and RMSprop. That resembles the case of having two related datasets for SGD and Adam against unrelated datasets for SGD and RMSprop. As a result, inferior performance results for models utilizing RMSprop are attributed to the high distributional differences in model weight parameters.

It is worth nothing that our deep transfer learning models keep weights of many layers unchanged. Therefore, when we trained our models, we had fewer number of updated weights compared to updated weights in models trained from scratch. It can be seen from Figure 7 that our deep transfer learning models are fast and can be adopted into mobile applications.

5. Conclusions and Future Work

In this paper, we present and analyze deep transfer learning models for the task of classifying 224 SCGRN images pertaining to healthy controls and T2D patients. First, we utilized seven pre-trained models (including SEResNet152 and SEResNeXt101) already trained on more than million images from the ImageNet dataset. Then, we left weights in the convolutional base (i.e., feature extraction part) unchanged and thereby transferring knowledge from pre-trained models while modifying the densely connected classifier with the use of Adam optimizer to discriminate heathy and T2D SCGRN images. Another presented deep transfer learning models work as follows. We kept weights of bottom

layers in the feature extraction part of pre-trained model unchanged while modifying consequent layers including the densely connected classifier with the use of Adam optimizer. Experimental results on the whole 224 SCGRN image dataset using 5-fold cross-validation demonstrate the superiority of TFeSEResNeXT101, achieving the highest average BAC of 0.97 and therefore significantly surpassing the performance of the baseline resulted in an average BAC of 0.86. Furthermore, our simulation study showed that the highly accurate performance in our models is attributed to the distributional conformance of weights obtained with the use of Adam optimizer when coupled with weights of pre-trained models.

Future work includes (1) adopting our computational framework to analyze deep transfer learning models with different network topologies and thereby identifying the best practice for deep transfer learning; (2) incorporating multi-omics datasets with images to improve the prediction performance using deep transfer learning; (3) developing a boosting mechanism to improve the performance of deep transfer learning in different biological problems [30, 31]; and (4) utilizing our framework to speed up the learning process, e.g., TFeVGG19 was 802.67x faster than VGG19, trained from scratch.

Author Contributions: T.T. conceived and designed the study. S.A. performed the deep learning experiments and the visualization of results. T.T. performed the analysis. T.T. and S.A. wrote the manuscript. T.T. supervised the study. All authors have read and agreed to the revised version of the manuscript.

Funding: This research received no funding.

Institutional Review Board Statement: Not applicable.

Informed Consent Statement: Not applicable.

Data Availability Statement: The dataset in this study is available at https://doi.org/10.1016/j.compbiomed.2021.104257.

Conflicts of Interest: The authors declare no conflicts of interest.

References

1. Zhang, S., et al., *Inference of cell type-specific gene regulatory networks on cell lineages from single cell omic datasets.* Nature Communications, 2023. **14**(1): p. 3064.

2. Lin, Z. and L. Ou-Yang, *Inferring gene regulatory networks from single-cell gene expression data via deep multi-view contrastive learning.* Briefings in Bioinformatics, 2023. **24**(1): p. bbac586.

3. Ma, A., et al., *Single-cell biological network inference using a heterogeneous graph transformer.* Nature Communications, 2023. **14**(1): p. 964.

4. Badia-i-Mompel, P., et al., *Gene regulatory network inference in the era of single-cell multi-omics.* Nature Reviews Genetics, 2023: p. 1-16.

5. Xue, L., Y. Wu, and Y. Lin, *Dissecting and improving gene regulatory network inference using single-cell transcriptome data.* Genome Research, 2023: p. gr. 277488.122.

6. Xu, J., et al., *STGRNS: an interpretable transformer-based method for inferring gene regulatory networks from single-cell transcriptomic data.* Bioinformatics, 2023. **39**(4): p. btad165.

7. Keyl, P., et al., *Single-cell gene regulatory network prediction by explainable AI.* Nucleic Acids Research, 2023. **51**(4): p. e20-e20.

8. Bach, S., et al., *On pixel-wise explanations for non-linear classifier decisions by layer-wise relevance propagation.* PloS one, 2015. **10**(7): p. e0130140.

9. Montavon, G., et al., *Layer-wise relevance propagation: an overview*. Explainable AI: interpreting, explaining and visualizing deep learning, 2019: p. 193-209.

10. Turki, T. and Y.h. Taguchi, *Discriminating the single-cell gene regulatory networks of human pancreatic islets: A novel deep learning application.* Computers in Biology and Medicine, 2021. **132**: p. 104257.

11. Iacono, G., et al., *bigSCale: an analytical framework for big-scale single-cell data.* Genome research, 2018. **28**(6): p. 878-890.

12. Iacono, G., R. Massoni-Badosa, and H. Heyn, *Single-cell transcriptomics unveils gene regulatory network plasticity.* Genome biology, 2019. **20**(1): p. 110.

13. Tripathi, S., M. Dehmer, and F. Emmert-Streib, *NetBioV: an R package for visualizing large network data in biology and medicine.* Bioinformatics, 2014. **30**(19): p. 2834-2836.

14. Segerstolpe, Å., et al., *Single-cell transcriptome profiling of human pancreatic islets in health and type 2 diabetes.* Cell metabolism, 2016. **24**(4): p. 593-607.

15. Simonyan, K. and A. Zisserman, *Very Deep Convolutional Networks for Large-Scale Image Recognition*, in *3rd International Conference on Learning Representations (ICLR)*. 2015: San Diego, CA, USA.

16. Huang, G., et al. *Densely connected convolutional networks*. in *Proceedings of the IEEE conference on computer vision and pattern recognition*. 2017.

17. Szegedy, C., et al. *Rethinking the inception architecture for computer vision*. in *Proceedings of the IEEE conference on computer vision and pattern recognition*. 2016.

18. He, K., et al. *Identity mappings in deep residual networks*. in *Computer Vision–ECCV 2016: 14th European Conference, Amsterdam, The Netherlands, October 11–14, 2016, Proceedings, Part IV 14*. 2016. Springer.

19. Hu, J., L. Shen, and G. Sun. *Squeeze-and-excitation networks*. in *Proceedings of the IEEE conference on computer vision and pattern recognition*. 2018.

20. Kingma, D.P. and J. Ba, *Adam: A Method for Stochastic Optimization*, in *3rd International Conference on Learning Representations*. 2015: San Diego, CA, USA.

21. Bengio, Y., I. Goodfellow, and A. Courville, *Deep learning*. Vol. 1. 2017: MIT press Cambridge, MA, USA.

22. Bottou, L., *Stochastic gradient descent tricks*, in *Neural Networks: Tricks of the Trade: Second Edition*. 2012, Springer. p. 421-436.

23. Chollet, F., *Deep Learning with Python*. 2017, Manning Publications Co.

24. Team, R.C., *R: A Language and Environment for Statistical Computing.* Journal of Statistical Software, 2008. **25**(1).

25. Franco, V.R., *optimg: General-Purpose Gradient-Based Optimization*.

26. Hunter, J.D., *Matplotlib: A 2D graphics environment.* Computing in science & engineering, 2007. **9**(03): p. 90-95.

27. Ruder, S., *An overview of gradient descent optimization algorithms.* arXiv preprint arXiv:1609.04747, 2016.

28. Currin, C., et al., *A Bayesian approach to the design and analysis of computer experiments*. 1988, Oak Ridge National Lab., TN (USA).

29. Forrester, A., A. Sobester, and A. Keane, *Engineering design via surrogate modelling: a practical guide*. 2008: John Wiley & Sons.

30. Turki, T. and Z. Wei, *Boosting support vector machines for cancer discrimination tasks.* Computers in biology and medicine, 2018. **101**: p. 236-249.

31. Turki, T. and Z. Wei, *Improved Deep Convolutional Neural Networks via Boosting for Predicting the Quality of In Vitro Bovine Embryos.* Electronics, 2022. **11**(9): p. 1363.