

# 1 Independent Influences of Movement Distance and Visual 2 Distance on Fitts' Law

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## 38 **Abstract**

39 Fitts' Law is among a handful of psychophysical laws. However, one of the fundamental  
40 variables of Fitts' Law – the movement distance,  $D$  – confounds two variables: the physical  
41 distance the effector has to move to reach a goal, and the visually perceived distance to that  
42 goal. While these two quantities are functionally equivalent in typical motor behaviors,  
43 decoupling them might improve our understanding of Fitts' Law. Here we leveraged the  
44 phenomenon of visuomotor gain adaptation to de-confound movement and visual distance  
45 during goal-directed upper-limb movements. We found that movement distance and visual  
46 distance can influence movement times, supporting a variant of Fitts' Law that considers both.  
47 The weighting of movement versus visual distance was modified by restricting movement range  
48 (emphasizing vision) or degrading visual feedback (emphasizing proprioception). These results  
49 reflect a multisensory integration process in the computation of expected movement difficulty,  
50 perhaps during early stages of motor planning.

51 *Keywords: adaptation; Fitts' Law; speed-accuracy tradeoff; motor behavior; skill; skill learning*

## 52 **Public Significance**

53 You will automatically slow your movement when picking up a needle five inches away versus a  
54 handkerchief three inches away. This fact is elegantly formalized by Fitts' Law, which  
55 mathematically relates movement duration to movement difficulty. However, one of the  
56 fundamental variables in the law – the distance of a planned movement – is ambiguous: Is it the  
57 actual distance the hand has to move that shapes planning and biases movement duration, or is  
58 it the visually perceived distance? We decoupled these variables, finding that Fitts' Law is  
59 shaped by both quantities, and that the influence of one versus the other is related to the  
60 relevance of proprioceptive versus visual information. We believe our “addendum” to Fitts' Law  
61 is timely, as everyday motor behavior has become increasingly enmeshed with virtual  
62 environments that abstract our movements into digital realities.

## 63 Introduction

64 Motor behavior is limited by a speed-accuracy trade-off: whenever an action must be  
65 executed quickly, its accuracy diminishes. Such a trade-off has been observed in saccadic eye  
66 movements (Gopal et al., 2017; Wu et al., 2010), goal-directed reaches (Goldberg et al., 2015),  
67 pointing movements (van Donkelaar, 1999), and even video game performance (Listman et al.,  
68 2021; Warburton et al., 2023). Fitts (1954) famously formalized the relationship between  
69 movement speed and accuracy constraints. This relationship, known as Fitts' Law, is one of the  
70 few so-called "laws" of psychophysics and has been replicated (and occasionally caveated)  
71 extensively over decades of behavioral research in humans and other animals (Adam, 1992; de  
72 Grosbois et al., 2015; Goldberg et al., 2015; Gopal et al., 2017; MacKenzie, 1992; MacKenzie &  
73 Buxton, 1992; Sambrooks & Wilkinson, 2013; Van Gisbergen et al., 1981; Wu et al., 2010).

74 The common form of Fitts' Law states that movement duration (MT) is logarithmically  
75 related to the width of a movement target ( $W$ ) and the movement's amplitude ( $D$ ):

$$MT = a + b * \log_2(2D/W)$$

76 where  $a$  and  $b$  are empirically-determined free parameters. The quantity  $\log_2(2D/W)$  is typically  
77 referred to as the Index of Difficulty (ID), reflecting a task's accuracy constraints (other accuracy  
78 constraints, such as the weight of a held tool, can be incorporated as well).

79 Fitts' Law has been of particular interest in applications involving human-computer  
80 interactions (MacKenzie, 1992), such as controlling a cursor on a computer screen with a  
81 mouse (Sambrooks & Wilkinson, 2013; Thompson et al., 2004; Whisenand & Emurian, 1996),  
82 making movements in virtual or augmented reality (Rohs et al., 2011; Rohs & Oulasvirta, 2008),  
83 or performing actions in a video game (Listman et al., 2021; Warburton et al., 2023). In these  
84 virtual arenas, the inherent ambiguity of the movement amplitude ( $D$ ) term of Fitts' Law is laid  
85 bare: Does  $D$  reflect the physical distance traversed by the limb, or the perceptual distance over

86 which one intends to move a proxy of their action (e.g., a cursor or avatar)? For example, a  
87 hand-held computer mouse only needs to move a few centimeters for its visual proxy to traverse  
88 a large computer monitor. It has been observed that as visual distance on a screen becomes  
89 increasingly decoupled from physical movement distance, predictions using Fitts' Law tend to  
90 be degraded (Thompson et al., 2004).

91 Popular explanations for Fitts' Law suggest that it is an outgrowth of basic facets of the  
92 motor system. For instance, it has been argued that Fitts' Law emerges from the size of the  
93 command signal used to produce a movement – a smaller command signal may achieve  
94 greater accuracy but result in a slower movement, while a larger command signal may generate  
95 a faster but less accurate movement. This “signal-dependent noise” model (Harris & Wolpert,  
96 1998) suggests that movement times (MTs) primarily reflect the physical distance traversed by  
97 the limb executing the movement.

98 It has also been argued that Fitts' Law emerges in the absence of such variability. Al  
99 Borno and colleagues (2020) position Fitts' Law at a more abstract level of planning: When a  
100 task is challenging, action selection is more likely to land upon an inefficient solution in the  
101 repertoire of potential reaches of varying movement durations that land within the target region,  
102 resulting in accurate but slower movements; however, when accuracy constraints are relaxed,  
103 more potential movement policies are readily selected with shorter movement durations, but  
104 more variable endpoints. If Fitts' Law emerges at this more abstract level (action selection),  
105 rather than as a direct consequence of the command signal itself, movement durations could be  
106 affected by multiple factors that influence planning. To this effect, some have observed  
107 violations of Fitts' Law when visual illusions alter the perception of movement amplitude ( $D$ ) and/  
108 or the width of a goal target ( $W$ ), suggesting that perceptual representations alone can shape  
109 speed-accuracy tradeoffs during movement planning (van Donkelaar, 1999, but see also  
110 Alphonsa et al., 2016).

111           Here we hypothesized that Fitts' Law is influenced by both visual and physical  
112 movement distances. To test this, we leveraged the phenomenon of visuomotor gain adaptation  
113 (Krakauer et al., 2004) to decouple movement and visual distance. We found support for our  
114 predictions in a standard reaching task with continuous visual feedback: MTs were influenced  
115 by both movement and visual distance even when no visual feedback was provided (Exp. 1).  
116 Moreover, the relative weighting of these quantities was flexible: Visual distance dominated  
117 when the range of physical movements was restricted (Exp. 2). In contrast, when continuous  
118 visual feedback was removed during adaptation, enhancing the role of proprioceptive input,  
119 movement distance alone could explain MTs (Exp. 3). These latter effects persisted when we  
120 accounted for difficulty differences between conditions attributable to latent task geometry (Exp.  
121 4). Taken together, our results suggest that Fitts' Law may reflect an integration of multiple  
122 sensory inputs, namely vision and proprioception. We speculate that this process may occur  
123 during an early planning stage of goal-directed movement.

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125

## 126 **Methods**

### 127 *Participants*

128 Experiments 1 & 4a were conducted in-lab. A total of N = 20 subjects (19 right-handed,  
129 age:  $28.9 \pm 9.1$ , 55% female) participated in these experiments at an honorarium of \$10/hr (Exp.  
130 1: N=10, age:  $29.8 \pm 10.9$ , 50% female; Exp. 4a: N=10, age:  $27.9 \pm 7.5$ , 60% female). (Sample  
131 sizes for Experiments 1 and 4a were not determined using *a priori* power analysis, though are  
132 consistent with similar investigations of the basic psychophysics of Fitts' Law; Alphonsa et al.,  
133 2016; Rohs et al., 2011; Rohs & Oulasvirta, 2008; van Donkelaar, 1999; Wu et al., 2010). All  
134 participants provided informed, written consent in accordance with procedures approved by the  
135 Yale University Institutional Review Board, and reported their handedness using the Edinburgh  
136 Handedness Inventory, with a score of >40 indicating right-handedness (Oldfield, 1971).

137 Experiments 2, 3, and 4b were crowd-sourced, where data from N = 84 subjects (77  
138 right-handed, 7 ambidextrous, age:  $28.3 \pm 4.6$ , 54% female) was collected online via Prolific  
139 (Exp. 2: N=27, age:  $27.1 \pm 5.0$ , 56% female; Exp. 3: N=27, age:  $29.2 \pm 4.7$ , 52% female; Exp.  
140 4b: N=30, age:  $28.5 \pm 4.1$ , 53% female). Recruitment was restricted to right-handed or  
141 ambidextrous individuals in the United States between the ages of 18 and 35, who had at least  
142 40 prior Prolific submissions, and a sample size of 30 was targeted for each experiment. While  
143 not based on *a priori* power analysis, this sample size vastly exceeds typical psychophysics  
144 sample sizes.

145

### 146 *Apparatus*

147 In-lab participants sat on a height-adjustable chair facing a 24.5-in. LCD monitor (Asus  
148 VG259QM; display size: 543.74 mm x 302.62 mm; resolution: 1920 x 1080 pixels; frame rate  
149 set to 240Hz; 1 ms response time), positioned horizontally ~30 cm in front of the participant  
150 above the table platform, thus preventing vision of the hand. In their dominant hand they held a

151 stylus embedded within a custom-modified paddle which they could slide across a digitizing  
152 tablet (Wacom PTH860; active area: 311 mm x 216 mm). Hand position was recorded from the  
153 tip of the stylus sampled by the tablet at 200 Hz. Stimulus presentation and movement recording  
154 were controlled by a custom-built Octave script (GNU Octave v5.2.0; Psychtoolbox-3 v3.0.18;  
155 Ubuntu 20.04.4 LTS).

156

### 157 *General Task Protocol*

158         Across all experiments, participants completed center-out reaching movements and  
159 were instructed to move their hand (in-lab, **Figure 1a**) or computer mouse (online) to land a  
160 displayed cursor within a visually indicated target. Participants were instructed to always move  
161 as quickly and accurately as possible. A trial would start when participants brought their cursor  
162 to the central starting location (in-lab: 7mm diameter starting circle; online: 6mm diameter). To  
163 assist with re-centering, the cursor (in-lab: 3mm diameter cursor; online: 4mm diameter) was  
164 visually displayed when it was within 1cm of the start location. After waiting in the center for  
165 500ms, a circular target would appear at one of three possible angular locations (straight ahead,  
166 or  $\pm 45^\circ$  from straight ahead) and two possible distances (in-lab: 5.3cm or 10.6cm away from the  
167 start location; online: 4cm or 8cm away). For online studies, mouse acceleration was inhibited  
168 by our task code.

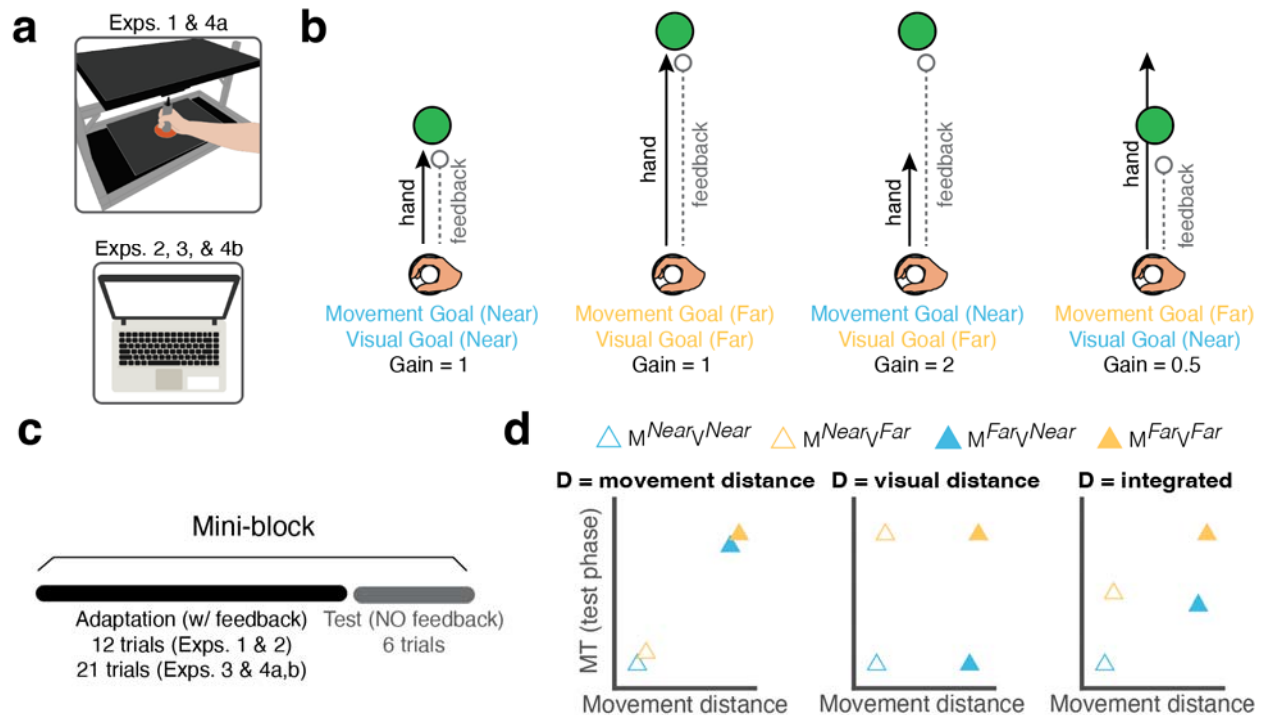
169         We leveraged gain perturbations (Krakauer et al., 2004) – alterations in the relationship  
170 between movement distance and the visual consequences of those movements – to decouple  
171 physical and visual distance in “mini-blocks” of trials. We used a 2 X 2 design that yielded 4  
172 possible conditions (**Figure 1b**): 1) the target was displayed at the shorter distance, and the  
173 required movement was similarly short (gain = 1; no perturbation), 2) the target was displayed at  
174 the farther distance, and the required movement was similarly long (gain = 1), 3) the target was  
175 displayed at the shorter distance but the required movement displacement was the same as the  
176 longer distance (gain = 0.5), 4) the target was displayed at the farther distance, but the required

177 movement displacement was the same as the shorter distance (gain = 2). In-lab participants  
178 would have to physically move either 5.3cm or 10.6cm for all respective trials, whereas online  
179 participants executed dramatically shorter movement amplitudes due to their use of a computer  
180 mouse or trackpad. Trials ended when participants stopped moving (velocity criterion: <5mm/s  
181 for greater than 200ms) or after a maximum time elapsed from the start of their reach. In  
182 Experiments 1 and 2, this maximum time was 1s. In Experiments 3 and 4, this maximum time  
183 was 2s.

184 In each mini-block (**Figure 1c**), participants first completed an “adaptation phase” (Exps.  
185 1 & 2: 12 trials; Exps. 3 & 4: 21 trials), in which visual feedback was provided. If the visual  
186 cursor successfully landed within the target region, participants received 10 points, which was  
187 displayed adjacent to the target in green text and added to a point total displayed on the screen.  
188 Endpoint cursor feedback and points were displayed for 500ms. This adaptation phase allowed  
189 participants to learn the appropriate distances required to hit the target for each condition (i.e.,  
190 to undergo gain adaptation). After adaptation, participants completed a “test phase” (all Exps.: 6  
191 trials), in which, critically, no visual feedback nor points were provided. All key movement time  
192 (MT) analyses were performed on these testing phases to preclude effects of feedback  
193 corrections. During the testing phases, participants were instructed to try to recreate the  
194 movements that were successful in the previous trials, and were informed that they would not  
195 receive any feedback about their performance.

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**Figure 1.** *Task design and theoretical predictions.* **a)** *Top:* In-lab experimental apparatus in Exps. 1 and 4A. Participants made center-out reaching movements on a digitizing tablet and viewed visual feedback on a monitor that occluded the arm. *Bottom:* Exps. 2, 3, and 4B were conducted online. **b)** Illustration of the four conditions used across all experiments – a 2x2 design crossing two levels of movement goal distances and visual goal distances by using feedback gain perturbations. **c)** Participants completed multiple mini-blocks for each of the four conditions. These mini-blocks consisted of a short adaptation phase with feedback, followed by a no-feedback test phase. Analyses were conducted on movement time (MT) in the test phase. **d)** Idealized predicted movement times given different (log) movement distances across the four conditions, for three different models. The models differ in their definition of the D term of Fitts' Law.

211 *Left:* movement distance (MD model); *Center:* visual distance (VD model); *Right:*  
212 multi-sensory integration of both movement and visual distance (MSI model).

213

#### 214 *Experiment 1*

215 Participants (N=10) were provided continuous (“online”) cursor feedback during the  
216 adaptation phase of each mini-block. For trials where the visual distance and the movement  
217 distance were identical (gain = 1), the cursor veridically tracked the position of the hand. For  
218 trials where the visual distance and the movement distance were de-confounded (**Figure 1b**),  
219 the cursor was perturbed (i.e., for the condition in which the visual distance was twice as long as  
220 the movement distance, a hand displacement of 1 cm resulted in a cursor displacement of 2  
221 cm). This manipulation is typically referred to as a gain perturbation (Krakauer et al., 2004), and  
222 the ratio between the visual distance and the movement distance is referred to as the gain (i.e.,  
223 the previous example has gain = 2). Training mini-blocks were 12 trials in length, followed by a  
224 6-trial test phase. Participants completed 24 training-test mini-block pairs, with 6 pairs for each  
225 condition. Conditions were pseudo-randomized such that all 4 conditions appeared in a shuffled  
226 order before repeating in a new shuffled order. The target diameter was 1.4cm and reach  
227 distances were 5.3cm or 10.6 cm.

228

#### 229 *Experiment 2*

230 Participants (N=27) completed a task that was largely identical to Exp. 1. The task was  
231 slightly shorter in length (16 training-test mini-block pairs; 4 per condition) to accommodate the  
232 crowd-sourced format. The target diameter was 1.6cm and visual distances were 4cm or 8cm  
233 (assuming a standard of 72 pixels per inch). Crucially, given the online format, the task now  
234 required only small, restricted mouse movements.

235

#### 236 *Experiment 3*

237           Participants (N=27) completed a similar task to Exp. 2, with some modifications. Instead  
238 of providing online feedback during the adaptation phase, feedback was degraded such that it  
239 was only provided when participants stopped moving (i.e., endpoint-only feedback). Since  
240 adaptation to endpoint feedback is slower (Taylor et al., 2014), adaptation phases were  
241 lengthened to 21 trials. Participants completed 16 training-test mini-block pairs (4 per condition).  
242 The endpoint cursor seen during adaptation followed the 2 X 2 gain perturbation design  
243 employed in Exps. 1 and 2 (**Figure 1b**). Additionally, to facilitate learning in this more difficult  
244 context, the targets were slightly larger (2cm diameter) and color-coded: blue targets indicated  
245 no gain manipulation, green targets indicated that participants needed to “go farther” than  
246 expected in order for the cursor to hit the target, and red targets indicated that participants  
247 needed to “stop shorter” than expected in order to hit the target. This instruction was repeated  
248 throughout the task at the start of each training mini-block and there was an additional 3-trial  
249 tutorial used to explain the nature of the perturbations. The target diameter was 2cm and reach  
250 distances were 4cm or 8cm.

251

#### 252 *Experiments 4a and 4b*

253           Experiments 4a (in-lab, N=10) and 4b (online, N=30) were largely identical to Exp. 3,  
254 including the 3-trial tutorial, color-coded targets, and endpoint-only feedback. Participants  
255 completed 16 training-test mini-block pairs (4 per condition) and adaptation phases were again  
256 21 trials long. The target diameter was 2cm and reach distances were 4cm or 8cm. However, in  
257 Exp. 4, the cursor was not manipulated using a “gain” manipulation. Instead, Exp. 4 aimed to  
258 preserve the “effective width” of the target across all 4 conditions. By effective width, we refer to  
259 the fact that gain manipulations will alter the area that constitutes successful reaches which  
260 would cause the cursor to land in the target. In other words, if the gain is 2 and a far target  
261 distance is displayed, any initial small deviation from the correct amplitude or angle of the reach,  
262 relative to the goal, will be magnified two-fold by the visually displayed cursor. Thus, in effect,

263 the region which allows successful reaches to land within the targets has effectively half the  
264 radius as the equivalent (in movement distance) no-gain condition.

265 To control for this geometric difficulty difference, Exp. 4 employed a slightly modified  
266 perturbation: In conditions where the visual and movement distance were matched, no change  
267 occurred, as in earlier experiments. However, in conditions where the movement distance was  
268 decoupled from visual distance, endpoint feedback was calculated using a novel translation that  
269 accounted for effective width (a “difficulty clamp”). That is, if the movement distance exceeded  
270 the visual distance of the target, the endpoint feedback displayed was calculated as if the target  
271 were at the larger distance, but was displayed at the shorter distance translated exactly along  
272 the direction of the target. (E.g., if the participant reached such that they would have hit the  
273 bottom-left side of the target at the farther distance, the endpoint feedback would be displayed  
274 in the bottom-left side of the target displayed at the shorter visual distance.). This design  
275 maintained the basic procedures of Experiment 3, but ensured that effective goal width was  
276 identical within each movement distance condition.

277

### 278 *Statistical Analysis*

279 The primary dependent measure was movement duration (MT). Linear mixed-effect  
280 models were run using R’s *lmerTest* package. These models were designed to fit MTs during  
281 the test phases using fixed effects of both the physical movement extent and the visual distance  
282 of the target, with subject ID as a random effect. ANOVA analysis was done using R’s *anova*  
283 command on the results of the LMER regression, with automatic sphericity corrections applied.  
284 It should be noted that this analysis was only on MTs during the no-feedback test phases, and  
285 thus these MTs were not contaminated by corrective movements. We additionally computed the  
286 physical error between the movement executed and the ideal movement. This was done by  
287 computing the difference between the movement vector that would bring the cursor to the exact  
288 center of the target and the vector from the center to where the participant stopped their

289 movement. The error was quantified as the magnitude of this vector. Learning curves were  
290 computed using this metric, averaging across trials within each adaptation phase. Lastly,  
291 percent error during the adaptation phase indexed the proportion of trials in which participants  
292 did not land within the target in the allotted maximum movement time for a given cycle of  
293 adaptation trials. All analyses were conducted in R (version 4.2.1).

294

### 295 *Modeling*

296 Individual participant MT data were fit using various models all employing the basic Fitts'  
297 Law formulation,  $MT = a + b * \log(2D/W)$ . The basic predicted patterns of data generated by  
298 these models are plotted in **Figure 1d**. The movement-distance-only (MD) model predicts MTs  
299 solely using the extent of the participants' hand displacement to set the D term. The visual-  
300 distance-only (VD) model predicts MTs solely using the visually displayed distance of the target  
301 to set the D term. The multisensory integration (MSI) model employs a weighted average  
302 between the movement distance and the visual distance to set the D term on each trial:

$$MT = a + b * \log(\lambda * MD + [1 - \lambda] * VD)$$

303 where the weighting parameter  $\lambda$  constitutes a third free-parameter in addition to the standard  $a$   
304 and  $b$  offset and scaling parameters from Fitts' Law; this additional weighting parameter varied  
305 from 0 (only visual distance matters) to 1 (only movement distance matters).

306 All models assumed the target width was constant, as its visual width was identical  
307 across all conditions and experiments. As a control, we also included a fourth model that  
308 accounts for differences in "effective goal width" are caused by gain manipulations (see  
309 descriptions for Experiment 4a and 4b above for details). This effective width (EW) model  
310 performed a weighted average between the visual width (a constant) and the effective width (the  
311 inverse of the gain applied on a particular trial):

$$MT = a + b * \log \left( \frac{MD}{W_{eff}} \right)$$

$$W_{eff} = \eta / gain + (1 - \eta)$$

312 where, if the free parameter  $\eta$  is 1, the width term of Fitts' law is entirely about the effective  
313 width of the target, and if  $\eta$  is 0, the width term is completely unaffected by the gain  
314 manipulation, reflecting the constant width of the visual target across all conditions.

315 Model fitting was performed using R's *optim* function, employing the L-BFGS-B  
316 optimization method. Model comparison was conducted with the Bayesian information criterion  
317 (BIC) computed on the average of model-predicted MTs for each condition and subject.  
318 Reported "summed  $\Delta$ BICs" were computed relative to the mean BIC for each subject across the  
319 three main models (MSI, MD, VD). When comparing any two models, mean  $\Delta$ BICs represent  
320 across-subject averages of the difference in BICs for the two models compared. Pseudo- $R^2$  was  
321 computed per subject as  $1 - \frac{Model\ SSE}{Null\ SSE}$  where the Model SSE was the sum of squared errors  
322 between the model-predicted average MT for each condition and the true average MT for each  
323 condition, and the Null SSE was the sum of squared errors between the true average MT for  
324 each condition and the average MT for all conditions.

325

326 *Author's Note*

327 Data and analysis scripts are available at <https://zenodo.org/record/8287803>. The  
328 experiments reported here were not preregistered. Ideas and data presented here were not  
329 previously disseminated.

## 330 **Results**

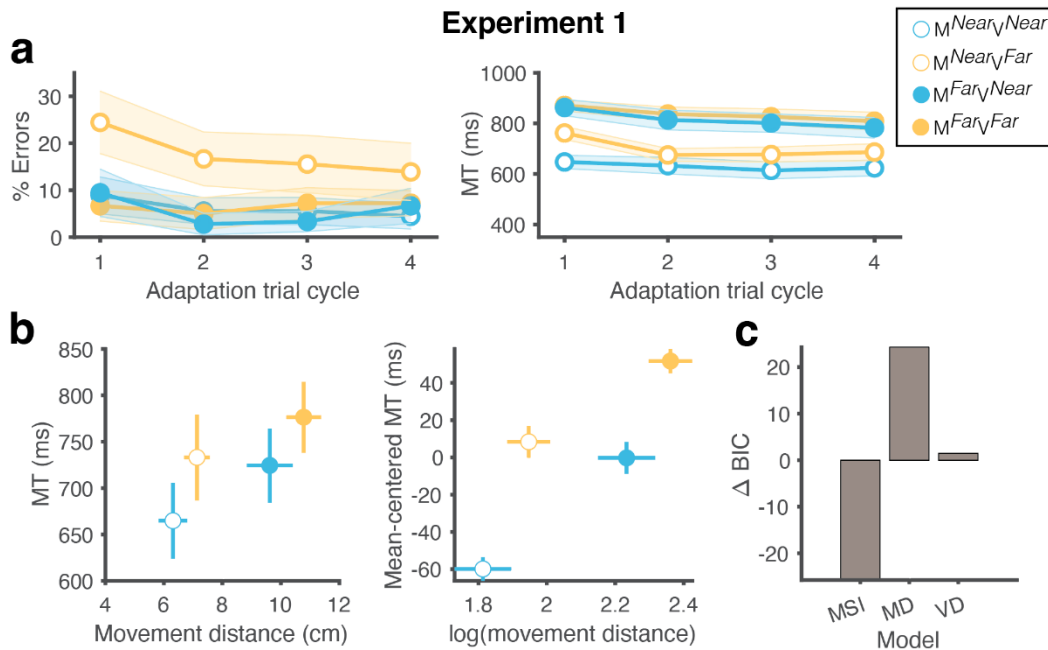
331 *Experiment 1*

332 In this study we aimed to clarify which distance cues determine movement duration in a  
333 reaching task. Online feedback was provided and the gain on the cursor was manipulated in  
334 order to dissociate the visual distance of the target and the physical movement distance  
335 required to hit the target (**Figure 1b**). During the 12-trial adaptation phases, participants largely  
336 successfully adapted to the perturbation, achieving reach errors averaging 4.3 mm (95% CI [3.3,  
337 5.3]) from the optimal solution (i.e. the movement need in order for the cursor to land in the  
338 center of the target) by the last trial within each adaptation phase. Errors on the last trial were  
339 not significantly different between the un-manipulated (gain = 1) and manipulated (gain = 2 or  
340 0.5) conditions (paired t-test,  $t(9)=-0.41$ ,  $p=0.67$ ,  $d_z=-0.18$ ). On average, participants  
341 successfully landed within the target on 91.0 % of training trials (95% CI [88%, 94%]; **Figure**  
342 **2a**). Success rates subtly but significantly differed between conditions (paired t-test,  $t(9)=3.59$ ,  
343  $p=0.005$ ,  $d_z=0.72$ ), with manipulated trials resulting in 5.3% less success on average (88.4% vs  
344 93.7%). While statistically significant, this difference amounts to an average of one additional  
345 failed trial per 20 trials.

346 Movement times during the critical test phase were fit using a linear mixed-effect model.  
347 MTs were predicted using fixed effects of true hand displacement and the visual distance of the  
348 target, and a random effect of subject ID. True hand displacement was used instead of ideal  
349 displacement to better capture the true data, and because participants did not always reach  
350 100% adaptation (**Figure 2b**). Crucially, an ANOVA indicated main effects of both hand  
351 displacement ( $F(1, 28.35)=36.58$ ,  $p=1.5 \times 10^{-6}$ ) and the visual distance of the target ( $F(1,$   
352  $28.03)=26.88$ ,  $p=1.7 \times 10^{-5}$ ) on MTs, suggesting that both factors may influence Fitts' Law  
353 (**Figure 2b**).

354 These results were echoed by our computational modeling (**Figure 2c**): The MSI model  
355 (summed  $\Delta\text{BIC}=-26$ ) outperformed both the MD (summed  $\Delta\text{BIC} =24$ , mean  $\Delta\text{BIC}=-5.00$ , 7/10  
356 better fit by MSI) and VD models (summed  $\Delta\text{BIC}=1.5$ , mean  $\Delta\text{BIC}=-2.72$ , 6/10 better fit by  
357 MSI). The MSI model fit participant trial-type average MTs with a strong pseudo- $R^2$  of 0.83 (MD:

358 0.40, VD: 0.54), again supporting the idea that physical distance and visual distance both  
 359 contributed to MTs.



360

361 **Figure 2. Experiment 1 results. a)** Percent error (*Left*) and MT (*Right*) during the  
 362 adaptation phase, averaged across mini-blocks for each condition. Adaptation  
 363 trial cycle reflects the average of 3 reaches, one to each target location. Shaded  
 364 error bars reflect standard error of the mean (SEM). Percent error reflects binary  
 365 target-hitting success by the maximum movement time, averaged across mini-  
 366 blocks for each cycle. **b)** Test phase MTs (*Left: raw, Right: mean-centered*)  
 367 plotted against the distance moved by the participant (*Left: raw, Right: log-*  
 368 *scaled*), averaged for each of the four conditions. Error bars reflect SEM for both  
 369 the movement distance data (horizontal error bars) and MT data (vertical error  
 370 bars). **c)** Summed  $\Delta BIC$  for the three main models (MSI: Multi-Sensory  
 371 Integration; MD: Movement Distance; VD: Visual Distance), computed relative to  
 372 the average BIC for all three models in order to visualize differences. Lower  
 373 values translate to stronger model fits.

374



375 As an additional control, participant MTs were fit using the EW model, which controls for  
376 the gain perturbation's tendency to modify error tolerances (see *Methods*). Critically, this model  
377 failed to beat the MSI model (mean  $\Delta\text{BIC}=4.65$ , 8/10 better fit by MSI). Lastly, the key free  
378 parameter in the MSI model ( $\lambda$ ), which lineary averages the visual and movement distances,  
379 had a mean value of 0.53 (95% CI [0.28, 0.78]), indicating that roughly 53% of the D term in  
380 Fitts' Law was reflective of the movement distance and 47% was reflective of the perceived  
381 visual distance of the target. Having demonstrated effects of both movement and visual distance  
382 on MT, we next asked if we could alter the relative weighting of both variables.

383

#### 384 *Experiment 2*

385 Experiment 2 was identical to Experiment 1 but was conducted online. The online format  
386 was chosen so that actions would be restricted to small mouse movements, significantly  
387 decreasing the difference between the physical movements required by each condition but  
388 maintaining large visual differences. It was hypothesized that this restriction would reduce the  
389 effect of the hand displacement on the index of difficulty (ID), and thus emphasize the effect of  
390 the visual distance of the target.

391 During the 12-trial adaptation phases, participants adapted to gain perturbations when  
392 they were present: By the last trial of the adaptation phase, errors from the optimal movement  
393 averaged 15 pixels (25% of the target diameter; 95% CI [13, 16] px). Since Exp. 2 was  
394 conducted online, these errors reflect the error of the mouse displacement in the absence of any  
395 gain manipulation from the mouse displacement that would have been necessary to hit the  
396 center of the target. (These errors cannot be cleanly translated into physical distances since  
397 computer mice and trackpads do not report their sensitivities for security reasons, but it should  
398 be noted that 15px is roughly 4mm on a screen.) Unlike in Experiment 1, errors differed subtly  
399 between manipulated and un-manipulated trials: Errors on the last training trial within a block  
400 were significantly larger when the cursor gain was manipulated (paired t-test,  $t(26)=-4.3$ ,

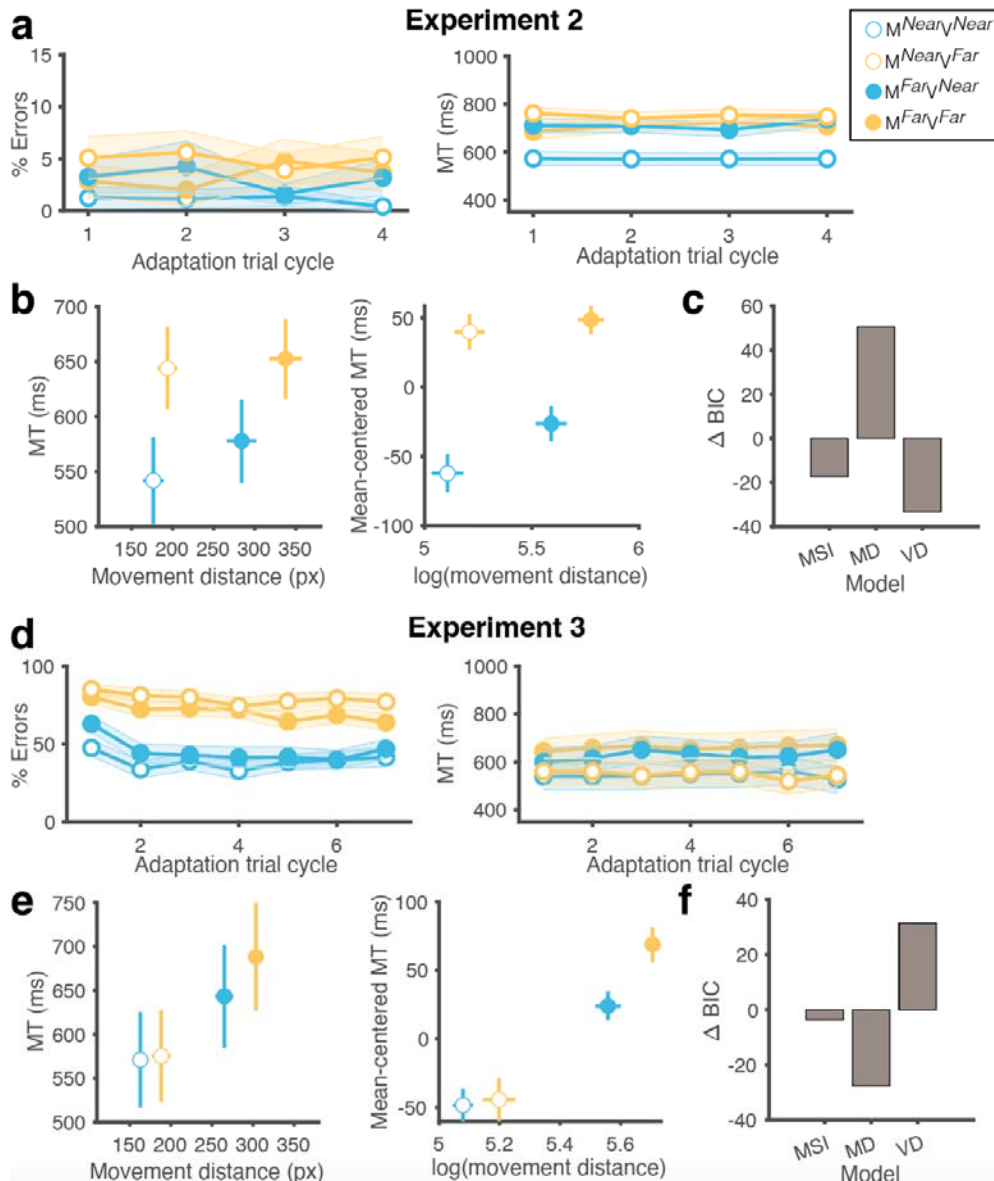
401  $p=2.4 \times 10^{-4}$ ,  $d_z=-0.92$ ) by an average of 4.4px (95% CI [2.3, 6.6] px). This also corresponded to  
402 differences in success rates (**Figure 3a**): Across all training trials, manipulated trials had  
403 significantly lower success rates (paired t-test,  $t(26)=2.69$ ,  $p=0.01$ ,  $d_z=0.54$ ) by an average of  
404 2.1% (95% CI [0.5%, 3.6%]). Nonetheless, participants averaged 96.8% (95% CI [95.5%, 98.0])  
405 success across all adaptation trials, indicating a high degree of success and rather small  
406 accuracy differences between conditions.

407 Test phase MTs were once again well predicted by both movement distance and visual  
408 distance, but primarily the latter (**Figure 3b**). An ANOVA analysis over the linear mixed-effect  
409 regression on MTs showed a significant main effect of both movement ( $F(1, 86.38)=4.35$ ,  
410  $p=0.04$ ) and visual distance ( $F(1, 79.25)=30.9$ ,  $p=3.5 \times 10^{-7}$ ). As hypothesized, the role of  
411 movement distance was substantially diminished relative to the veridical context of Exp. 1, likely  
412 due to the fact that in Exp. 2 the required kinematic displacements were dwarfed by their  
413 corresponding visual displacements. Instead, MTs were largely modulated by the visual  
414 distance of the target (**Figure 3b**).

415 This result was further supported by modeling (**Figure 3c**): while the MSI model  
416 (summed  $\Delta\text{BIC}=-17$ ) beat the MD model (summed  $\Delta\text{BIC}=50$ , mean  $\Delta\text{BIC}=-2.51$ , 15/27 better fit  
417 by MSI), it did not beat the VD model (summed  $\Delta\text{BIC}=-33$ , mean  $\Delta\text{BIC}=0.59$ , 9/27 better fit by  
418 MSI). We note that the VD model performs well here because it has fewer parameters than the  
419 MSI model, and the data indicates almost a near-complete dominance of visual distance, as  
420 hypothesized. The MSI model fit participants' trial-type MTs with a pseudo- $R^2$  of 0.53 (MD: 0.19,  
421 VD: 0.46). As a further control, the EW model, which controls for task geometry-induced  
422 differences in difficulty, did not win by BIC (mean  $\Delta\text{BIC}=-0.85$ , 13/27 better fit by MSI, pseudo-  
423  $R^2=0.53$ ). Having shown that we can downweight the role of movement distance and upweight  
424 the role of visual distance in Fitts' Law, we next tried to do the opposite.

425

426



427

428 **Figure 3.** *Experiment 2 and Experiment 3 results. a, d* Percent error (*Left*) and

429 MT (*Right*) during the adaptation phase averaged across mini-blocks for each

430 condition for Exps. 2 and 3, respectively. Shaded error bars reflect standard error

431 of the mean (SEM). **b, e** Test phase MTs (*Left: raw, Right: mean-centered*)

432 plotted against the distance moved by the participant (*Left: raw, Right: log-*

433 scaled), averaged across all four conditions for Exps. 2 and 3, respectively. Error

434 bars reflect SEM for both the movement distance data (horizontal error bars) and

435 MT data (vertical error bars). **c, f** Summed  $\Delta BIC$  for the three main models (MSI,

436 MD, VD) for Exps. 2 and 3, respectively. Lower values translate to stronger  
437 model fits.

### 438 *Experiment 3*

439 The results of Experiments 1 and 2 suggest that both movement and visual distances  
440 can influence Fitts' Law, and that the role of visual distance can be amplified by restricting the  
441 range of movement distances relative to visual distances. In Experiment 3, we asked if the  
442 opposite effect could be elicited, such that movement distance alone could be made to shape  
443 MTs even under the restricted movement range conditions of Exp. 2. Thus, in Experiment 3 we  
444 provided only endpoint feedback during the adaptation phase. This degraded visual feedback  
445 should, we reasoned, lessen the salience of the visual aspects of the task and increase the  
446 salience of the kinesthetic aspects, and consequently boost the effect of movement distance on  
447 MTs while attenuating the effect of visual distance.

448 Due to the degraded feedback, participant errors were predictably larger in Exp. 3  
449 compared to Exp. 2. Movement errors on the last trial of the adaptation phase were on average  
450 67.6px (89% of the diameter of the target or roughly 1.8cm on the screen, 95% CI [54, 81] px).  
451 Errors were predictably larger for conditions where the required movement distance was longer  
452 (paired t-test,  $t(26)=2.83$ ,  $p=0.009$ ,  $d=0.54$ ) by an average of 44px (95% CI [12, 76]).  
453 Additionally, errors on perturbation trials were significantly larger compared to un-manipulated  
454 trials (paired t-test,  $t(26)=-2.51$ ,  $p=0.02$ ,  $d=-0.38$ ) by an average of 14.7px (95% CI [3, 27] px).  
455 Success rates (**Figure 3d**) were higher for shorter visual distance trials (paired t-test,  
456  $t(26)=17.1$ ,  $p=1.2 \times 10^{-15}$ ,  $d=1.65$ ), by an average of 32.6% (95% CI [29%, 37%]). Manipulated  
457 trials also had lower success rates (paired t-test,  $t(26)=4.72$ ,  $p=7.0 \times 10^{-5}$ ,  $d=0.46$ ), by an average  
458 of 7.7% (95% CI [4%, 11%]). Overall, success rates were vastly lower in Exp. 3 (as was  
459 expected, given the lack of online feedback), with average success across all training trials at  
460 41.4% (95% CI [35%, 48%]) despite the lengthened adaptation phase (21 trials).

461 Participant MTs were well predicted by movement extent, but, critically, not by visual  
462 distance (**Figure 3e**): An ANOVA analysis revealed a main effect of movement distance on MTs  
463 ( $F(1, 79.66)=42.58, p=5.8 \times 10^{-9}$ ) but no significant effect of visual distance ( $F(1, 79.04)=0.03,$   
464  $p=0.87$ ). Model comparison (**Figure 3f**) using BIC indicated that the MD model (summed  
465  $\Delta\text{BIC}=-28$ ) was the best-fitting model (compared to MSI [summed  $\Delta\text{BIC}=-3$ ]: mean  $\Delta\text{BIC}=-0.88,$   
466 24/27 better fit by MD; compared to VD [summed  $\Delta\text{BIC}=31$ ]: mean  $\Delta\text{BIC}=-2.18, 20/27$  better fit  
467 by MD). However, the MSI model had the highest pseudo  $R^2$  at 0.46 (MD: 0.41, VD: 0.12). The  
468 control EW model was largely equivalent to the MSI model (mean  $\Delta\text{BIC}=-0.16$  in favor of EW,  
469 13/27 better fit by EW).

470 These observations support the conclusion that MTs in Exp. 3 were primarily determined  
471 by movement distances as opposed to visual distances, in stark contrast to Exp. 2. Given that  
472 the underlying gain manipulation in Exp. 3 was identical to Exps. 1 and 2 and that the  
473 movement demands fully matched Exp. 2, the complete flip in the factor shaping MTs from  
474 visual to movement distance appeared to be driven solely by the change in visual feedback.  
475 Taken as a whole, the results of Exps. 1-3 point to both movement and visual distance  
476 independently influencing the D term in Fitts' Law.

477

#### 478 *Experiment 4a*

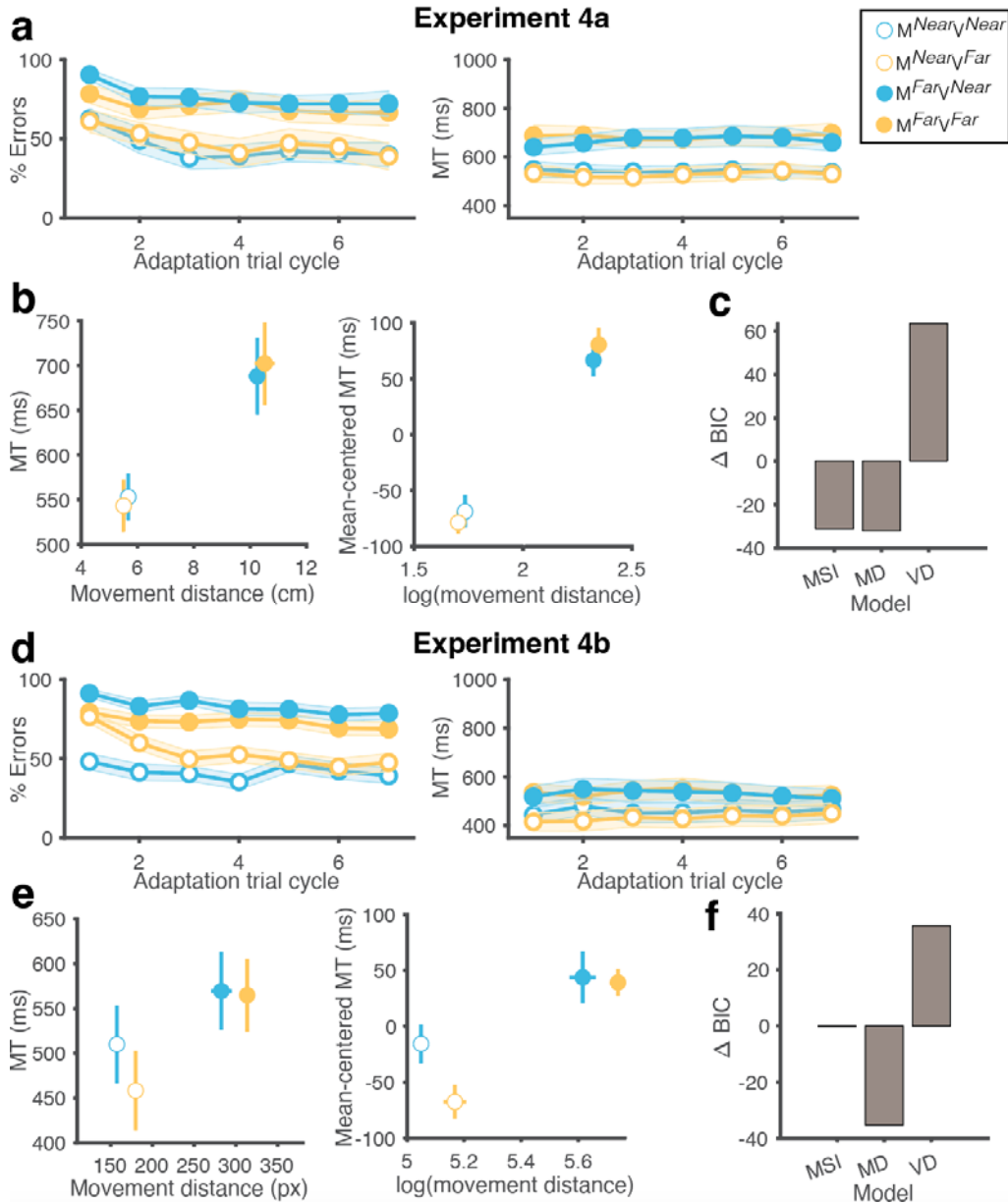
479 Experiments 1-3 employed conventional gain perturbations in which small  
480 displacements,  $\Delta x$ , are displayed as  $\Delta x * gain$ . As a result of this, the “effective width” (that is,  
481 differences in error tolerance in gain versus non-gain contexts; see *Methods*) of the movement  
482 targets varies across conditions with different gains, in that gain can inflate or deflate errors in  
483 initial movement direction and extent. (For example, when gain = 2, any slight deviation from the  
484 correct movement amplitude would be magnified two-fold in the observed visual error.) To  
485 control for this geometric difference, which is inherent to gain perturbations, Experiments 4a and  
486 4b employed a novel translational perturbation where the visual feedback was “teleported” along

487 the straight-line path to the target to either a greater or shorter amplitude, depending on the  
488 gain. The size of the effective area of successful reach vectors was thus standardized for all  
489 conditions.

490 Due to the discrete nature of this perturbation, only endpoint feedback could be  
491 provided. Despite this degraded feedback, participants learned to adequately adapt to the  
492 perturbation during gain trials, achieving average errors of 13.3mm (67% of target diameter;  
493 95% CI [11, 16] px) on the last trial of the adaptation phase. Errors were significantly larger for  
494 the larger movement distance trials (paired t-test,  $t(9)=-6.10$ ,  $p=1.8 \times 10^{-4}$ ,  $d=-1.82$ ) by an  
495 average of 7.9 mm (95% CI [5, 11] mm). However, errors were not significantly different  
496 between manipulated and un-manipulated trials (paired t-test,  $t(9)=-0.86$ ,  $p=0.41$ ,  $d=-0.33$ ).  
497 Consistent with the larger errors, conditions with greater movement distances also had lower  
498 success rates (**Figure 4a**; paired t-test,  $t(9)=9.43$ ,  $p=5.8 \times 10^{-6}$ ,  $d=2.11$ ), by an average of 27%  
499 (95% CI [21%, 34%]), broadly consistent with Fitts' Law. Notably, the pattern of difficulty  
500 differences between conditions in Exp. 4a, as reflected in success rates (**Figure 4a**), deviated  
501 from the pattern seen in Exp. 3 (**Figure 3d**), signaling the success of our novel "difficulty clamp"  
502 perturbation method.

503 Even with a rather different perturbation applied, the test phase results of Experiment 4a  
504 largely replicated the results of Experiment 3 (**Figure 4b**). Specifically, the ANOVA analysis  
505 revealed a main effect of movement distance ( $F(1, 28.04) = 144.4$ ,  $p=1.4 \times 10^{-12}$ ) but not visual  
506 distance ( $F(1, 28.00) = 0.06$ ,  $p=0.81$ ) on MT. Modeling further corroborated these results  
507 (**Figure 4c**): By BIC comparison, the MSI (summed  $\Delta\text{BIC}=31$ ) and MD (summed  $\Delta\text{BIC}=32$ )  
508 models were largely identical in fit quality (mean  $\Delta\text{BIC}=-0.08$  in favor of MD, 6/10 better fit by  
509 MD). However, the MSI model had a pseudo- $R^2$  of 0.89, as opposed to the MD model at 0.79.  
510 The average value of the fitted  $\lambda$  parameter was 0.91 (SD: 0.11), indicating that movement  
511 distance contributed ~91% of the  $D$  term in Fitts' Law. Thus, even after accounting for the effect

512 of varying effective target widths and altering the pattern of adaptation phase errors across  
 513 conditions relative to Exp. 3, the key results of Exp. 3 were replicated in Exp. 4a.  
 514



515  
 516 **Figure 4.** Experiment 4 results. **a, d)** Percent error (Left) and MT (Right) during  
 517 the adaptation phase averaged across mini-blocks for each condition for Exps.  
 518 4a and 4b, respectively. Shaded error bars reflect standard error of the mean  
 519 (SEM). **b, e)** Test phase MTs (Left: raw, Right: mean-centered) plotted against

520 the distance moved by the participant (*Left: raw, Right: log-scaled*) averaged  
521 across all four conditions for Exps. 4a and 4b, respectively. Error bars reflect  
522 SEM for both the movement distance data (horizontal error bars) and MT data  
523 (vertical error bars). **c, f**) Summed  $\Delta$ BIC for the three main models (MSI, MD,  
524 VD) for Exps. 4a and 4b, respectively. Lower values translate to stronger model  
525 fits.

#### 526 *Experiment 4b*

527 Here, we replicated Exp. 4a in an online sample. As with Exp. 3, the degraded visual  
528 feedback led to relatively large errors on the last trial of the adaptation phase, averaging 67.7px  
529 (1.8cm or 89% of the diameter of the target; 95% CI [58, 78] p). Errors were significantly larger  
530 on trials where the movement amplitude was greater (paired t-test,  $t(29)=-5.10$ ,  $p=1.9 \times 10^{-5}$ ) by  
531 an average of 35.3px (95% CI [21, 49] px). Errors were marginally different between  
532 manipulated and un-manipulated trials (paired t-test,  $t(29)=-2.00$ ,  $p=0.054$ ,  $d=-0.33$ ), with errors  
533 10.5px (~2.8mm; 95% CI [0, 21] px) larger for manipulated trials. Shorter movements had  
534 significantly higher success rates (**Figure 4d**) throughout training (paired t-test,  $t(29)=21.2$ ,  
535  $p=2.2 \times 10^{-16}$ ,  $d=2.26$ ), by an average of 30% (95% CI [27%, 33%]); un-manipulated trials also  
536 had significantly higher success rates (paired t-test,  $t(29)=9.32$ ,  $p=3.2 \times 10^{-10}$ ,  $d=0.96$ ), by an  
537 average of 11% (95% CI [9%, 13%]).

538 Test phase movement durations in Exp. 4b were again only weakly predicted by visual  
539 distance, consistent with degraded feedback downweighting vision's role (**Figure 4e**): The  
540 ANOVA revealed a main effect of movement distance, as expected ( $F(1, 90.19)=22.86$ ,  
541  $p=6.7 \times 10^{-6}$ ), and, a small but significant main effect of visual distance ( $F(1, 87.98)=5.30$ ,  
542  $p=0.02$ ). However, the longer visual distances actually predicted lower MTs, an effect that was  
543 largely driven by faster MTs on the condition where the movement goal was near but the visual  
544 target was far. Interestingly, for this condition, when compared to the un-manipulated near-  
545 movement condition, participants had marginally larger errors ( $t(29)=1.77$ ,  $p=0.09$ ,  $d=0.38$ ;



546 13.8px, 95% CI [-2, 30] px) and significantly lower success rates ( $t(29)=6.76$ ,  $p=2.04 \times 10^{-7}$ ,  
547  $d=0.86$ ; 12%, 95% CI [9%, 16%]) during adaptation phases, yet had faster MTs during the test  
548 phase ( $t(29)=-2.40$ ,  $p=0.02$ ,  $d=-0.22$ ; 52ms, 95% CI [8, 96] ms).

549 Modeling supported the conclusion that MTs were predominantly driven by movement  
550 distance (**Figure 4f**): The MD model (summed  $\Delta\text{BIC}=-35$ ) won model comparison by BIC,  
551 beating the MSI model (summed  $\Delta\text{BIC}=0$ , mean  $\Delta\text{BIC}=-1.17$ , 27/30 better fit by MD) and the VD  
552 model (summed  $\Delta\text{BIC}=36$ , mean  $\Delta\text{BIC}=-2.37$ , 22/30 better fit by MD). The MSI model had a  
553 slightly higher pseudo- $R^2$  compared to the MD model (MSI: 0.38, MD: 0.36, VD: 0.05). We note  
554 that the lower pseudo- $R^2$  values in general arise from the models' inability to account for the  
555 aforementioned violation of Fitts' Law in one of the conditions.

556 Overall, the key test phase findings of both Exps. 4a and 4b did not differ from the  
557 results of Experiment 3 – this echoes the poor fit of the EW model in the previous studies, and  
558 further suggests that the key results of our study were likely not driven by differences in target  
559 effective widths or other difficulty considerations. Instead, the four experiments suggest that  
560 both movement distance and visual distance can influence Fitts' Law.

## 561 Discussion

562           What information does the brain use to predict the difficulty of a movement? Across four  
563 experiments we sought to clarify the nature of the movement distance (D) term of Fitts' Law  
564 (**Figure 1d**). We leveraged gain adaptation (**Figure 1b**) to create conditions where both visual  
565 and kinesthetic aspects of a reaching task could independently influence movement times  
566 (MTs). Our results showed that when continuous visual feedback is provided during adaptation  
567 (Exps. 1 & 2), the visually perceived distance of a goal and the reach amplitude needed to reach  
568 that goal both contributed to MT (**Figures 2 and 3**). The role of vision was especially  
569 pronounced when movement amplitudes were restricted relative to visual distances (Exp. 2;  
570 **Figure 3**). However, when visual feedback was degraded to only appear at the endpoint of a  
571 movement, visual goal distance no longer predicted MT even within the same restricted  
572 movement context (Exp. 3; **Figure 3**). When potential condition difficulty differences due to the  
573 geometry of the task were accounted for (Exp. 4a & b; **Figure 4**), these latter results remained  
574 largely unchanged. Crucially, all of our key results were quantified in a test phase where visual  
575 feedback was withheld. Thus, differences in MTs could not be explained by online, corrective  
576 movements or similar reactive strategies.

577           What is the underlying process that explains our findings? We speculate that visual  
578 distance may exert an effect during an early motor planning stage (Al Borno et al., 2020). The  
579 visual distance to the goal, even when decoupled from the required movement distance, may  
580 act as a “prior” on the expected difficulty of a movement. The results of Exps. 1-2 demonstrate  
581 that visual distance independently affects MT, and Exps. 3 and 4 show that the removal of  
582 continuous visual feedback during adaptation decreased the influence of visual distance; this is  
583 likely because subjects had to rely heavily on proprioception in these conditions. The distinct  
584 behavioral effects of online versus endpoint feedback we observed are consistent with findings  
585 in motor adaptation that show similar tradeoffs between vision and proprioception in online

586 versus endpoint feedback conditions (Hayashi et al., 2020; Izawa & Shadmehr, 2011). Taken  
587 together, our results may reflect an integration of visual and proprioceptive information in the  
588 computation of the D term in Fitts' Law.

589 Another consideration here is the role of attention: It may be that continuous visual  
590 feedback (Exps. 1-2) biased people's attention to visual cues during online control of the cursor;  
591 in contrast, endpoint feedback (Exps. 3-4) may have biased attention to proprioceptive cues (the  
592 felt distance of the hand) to facilitate estimation of the correct reach stopping point. Put another  
593 way, putative multisensory integration in our task may occur at the level of conscious attention  
594 to vision versus proprioception. This attentional account could help explain our results and is an  
595 interesting theoretical direction. However, the attentional account is somewhat undermined by  
596 the fact that all of our key results were observed in a testing phase where feedback was  
597 removed and was thus identical between conditions. It is worth considering that our gain  
598 perturbation may be compensated for by a combination of explicit and implicit motor learning  
599 processes (Krakauer et al., 2004; McDougle et al., 2016; Taylor et al., 2014). Future work could  
600 target the role of explicit cognitive processes versus implicit motor planning processes in our  
601 task, and in Fitts' Law more generally.

602 It is unlikely that test phase MTs were significantly impacted by the latent changes in  
603 task geometry due to gain perturbations: When we directly controlled for these intrinsic condition  
604 difficulty differences in Exp. 4, the results of Exp. 3 largely replicated. Furthermore, the  
605 integrative MSI model was able to explain MT results across multiple experiments and only  
606 failed when it was overfit because a single factor explained the data. While this does not fully  
607 rule out a potential role of the 'effective width' (see *Methods*) of reach targets in our task, in  
608 Exps. 1-3, vastly different visual and movement distance effects were observed even when  
609 effective widths did not differ across the experiments.

610 In general, when performance during adaptation was relatively weak, test phase MTs  
611 were slower. This was predictable (Adam, 1992; de Grosbois et al., 2015; Fitts, 1954; Fitts &

612 Peterson, 1964; van Donkelaar, 1999) – Fitts' Law relates the difficulty of a movement to its  
613 duration. However, we did not always see a 1-1 relationship between success during the  
614 adaptation phase and the key MT results in the testing phase (**Figure 4**). While it is difficult to  
615 fully separate effects of accuracy and movement time (their close relationship is the point of  
616 Fitts' Law), one limitation of our study is that it targeted MT effects following gain adaptation  
617 which may account for additional difficulty variables not accounted for in our models. In  
618 Experiments 1 and 2, participants may have learned to associate particular visual distances with  
619 the ease of cursor control and the cursor speed. However, these associations persisted into the  
620 probe phase where no feedback was provided, suggesting still that visual cues of difficulty  
621 (namely visual target distance) were integrated into movement durations under Fitts' Law. This  
622 is parsimoniously explained by our model of the D term of Fitts' Law. Future studies could  
623 further explore these additional aspects of difficulty.

624 More broadly, we think our results could contribute to a synthesis of documented  
625 amendments to Fitts' Law (Crossman & Goodeve, 1983; de Grosbois et al., 2015; Heath et al.,  
626 2011). First, our findings are consistent with literature suggesting that strategic attention to a  
627 range of task dimensions shape Fitts' Law (Adam, 1992). Our results also echo and extend  
628 findings that Fitts' Law can emerge at perceptual or mental “simulation” stages of motor  
629 planning (Decety & Jeannerod, 1995; Grosjean et al., 2007), are consistent with findings that  
630 visual illusions can bias Fitts' Law (van Donkelaar, 1999), and comport with studies relating the  
631 law to more abstract features of motor preparation and planning (Augustyn & Rosenbaum,  
632 2005; Jax et al., 2007). Incentives also modulate movement durations (Ashworth-Beaumont &  
633 Nowicky, 2013; Bogacz et al., 2010; Du et al., 2022; Listman et al., 2021; Thura et al., 2014),  
634 further supporting flexibility in the strategies the brain employs when selecting movement  
635 parameters. Future investigations can address other non-motor indicators of difficulty, such as  
636 the visually inferred weight of a tool (Ellis & Lederman, 1993).

637           As interest in the applicability of Fitts' Law to virtual and augmented reality grows (Rohs  
638 et al., 2011; Rohs & Oulasvirta, 2008; Sambrooks & Wilkinson, 2013), it is important to  
639 understand the law's underlying mechanisms. We demonstrated here that under certain  
640 conditions, fundamental variables in Fitts' Law are responsive both to perceptual (visual goal  
641 distance) and physical (movement distance) cues. Developers of AR/VR applications could  
642 leverage this observation in optimizing or calibrating the feedback they provide to users. Our  
643 results may also inform investigations into the neural correlates of action selection and the  
644 speed-accuracy trade-off (Al Borno et al., 2020; Harris & Wolpert, 1998) perhaps serving to  
645 illuminate distinct factors that the motor system represents as it prepares fast and accurate  
646 actions.

## 647 **Constraints on Generality**

648 Fitt's Law is a surprisingly robust psychophysical law with broad applicability. Samples reported  
649 here may not be generally representative of the global population as participants were recruited  
650 from the US. Nonetheless, we believe these results should broadly apply to all neurotypical  
651 adults, as they relate to the typical performance of goal-directed movements.

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