A Mechanistically Integrated Model of Exploitative and Interference Competition over a Single Resource Produces Widespread Coexistence

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ABSTRACT

Many ecological models treat exploitative competition in isolation from interference competition. Corresponding theory centers around the R^* rule, according to which consumers who share a single limiting resource cannot coexist. Here we model motile consumers that directly interfere while handling resources, mechanistically capturing both exploitative and interference competition. Our analytical coexistence conditions show that interference competition readily promotes coexistence. In contrast to previous theory, coexistence does not require intra-specific interference propensities to exceed inter-specific interference propensities, nor for interference behaviors to carry a direct (rather than merely an opportunity) cost. The underlying mechanism of coexistence can resemble the hawk-dove game, the dominance-discovery trade-off (akin to the competition-colonization trade-off), or a novel trade-off we call the "dove-discovery trade-off", depending on parameter values. Competitive exclusion via the R^* rule occurs only when differences in exploitative abilities swamp other differences between species, and more easily when differences in R^* reflect different search speeds than when they reflect different handling times. Our model provides a mathematically tractable framework that integrates exploitative and interference competition, and synthesizes previous disparate models.

Keywords: coexistence theory, consumer-resource model, game theory, evolution of aggression, Grime's triangle, R* theory

INTRODUCTION

The R^* rule (Armstrong and McGehee 1980; Tilman 1981; Tilman 1982) is a

fundamental building block of theoretical ecology. Briefly, R^* theory equates the competitive

ability of a focal species or genotype with its ability to deplete a limiting resource. Consider

one species consuming a single limiting resource. The consumer's population grows until it

depletes the resource concentration (R) down to the level (R^*) at which its growth stops. A

species or genotype is predicted to exclude any competitors with higher R^*, because it drives

the resource level too low for others to persist – this is referred to as the R^* rule.

R^* theory and the R^* rule thus focus on *exploitative competition*, in which consumers

compete indirectly through shared use of a depletable resource (either biotic or abiotic). This

emphasis on exploitation has often neglected *interference competition*, i.e. direct interactions

between individuals at the same trophic level, via behavioral contests or chemical inhibition.

Interference competition is common in natural communities (Boynton 2019; DeLong and

Vasseur 2011; Drury et al. 2020; García-Bayona and Comstock 2018; Grether et al. 2017;

Inderjit et al. 2011; Leighton et al. 2024; Schoener 1983; Ziv et al. 1993; Ziv and Kotler

2003) but is rarely emphasized in coexistence theory. Indeed, many otherwise wide-ranging

reviews of coexistence theory, replete with discussions of resource exploitation/partitioning

and predation, lack a single direct mention of interference competition (e.g. Adler et al. 2013;

Barabás et al. 2018; Chesson 2018; Ellner et al. 2019; Letten et al. 2017).

Several previous models that do highlight interference competition use

phenomenological terms to summarize the strengths of intra-specific (or intra-type) and inter-

specific (or inter-type) interference. These Lotka-Volterra type equations model resources

implicitly or non-dynamically (Case and Gilpin 1974; Hsu 1982; Kishi and Nakazawa 2013;

Schoener 1976; Schoener 1978; Vance 1984), making them incommensurable with R^*

theory. These studies broadly conclude that interference can promote coexistence if intra-

specific interference exceeds inter-specific interference, but further insight is limited by the

phenomenological nature of both terms.

Amarasekare (2002) incorporates both resource dynamics and interference

competition to produce an R^*-related analysis of species coexistence. Amarasekare (2002)

concludes that interference competition can only maintain coexistence when one consumer

species engages in a "beneficial" interference mechanism such as intraguild predation or

parasitism, while the second consumer is superior at exploitation. Amarasekare (2002)

explicitly argues that "costly" contests over resources (for which she explicitly lists food

items or territories as examples) cannot promote coexistence. Interpreting what is a

"beneficial" vs. a "costly" interference mechanism is made more difficult by the fact that

Amarasekare (2002) continues the phenomenological tradition for modeling interference

competition via Lotka-Volterra-like competition coefficients, on top of a typical consumer-

resource model. We do, however, note that she models only inter-specific interference.

In contrast, in the hawk-dove game (Maynard Smith 1974; Maynard Smith 1982;

Maynard Smith and Price 1973), interference does promote coexistence. "Doves" abstain

from, while "hawks" participate in, contests (i.e., interference competition) for access to a

shared, implicitly modeled resource. Obtaining a resource yields benefit b, and losing a

contest yields cost c. When a hawk within a hawk-only population incurs more cost than

benefit from interference ($c/b > 1$), a dove that forgoes interference can invade, enabling

coexistence. This does not occur in the model of Amarasekare (2002), which corresponds to

modeling hawk-dove interactions but not hawk-hawk nor dove-dove interactions. We also

note that hawk-dove coexistence does not require co-evolution as in Grether and Okamoto

(2022) (i.e., hawks and doves can coexist when each of the two strategies is unchanging over

time).

Surprisingly, the insights of the hawk-dove game have not been incorporated into ecological theory. Some models have generalized and added realism to the hawk-dove game by incorporating explicit consumer-resource dynamics (Auger et al. 2006; Galanthay et al. 2023; Kooi 2015; Křivan et al. 2018). However, differences in exploitative abilities were neglected (e.g., search rates, handling times, and, consequently, R^*s), and results were not contextualized within coexistence theory nor R^* theory.

Within ecological theory, the dominance-discovery trade-off enables coexistence. The theory, describing a trade-off between colonizing resource-rich patches (exploitation), and displacing heterospecifics from patches (interference), was developed for ants, and seems to be used only in that context (Adler et al. 2007; Davidson 1998; Fellers 1987; Holway 1999). The better known competition-colonization trade-off (Hastings 1980; Horn and MacArthur 1972; Skellam 1951; Tilman 1994) is formally similar, but inferior competitors are interpreted as being displaced via locally superior exploitation (i.e. a per-patch version of the R^* rule), rather than by interference competition. Key results on the competition-colonization trade-off also apply to the dominance-discovery trade-off, because of the formal similarity between the models.

While both the dominance-discovery trade-off and the hawk-dove game describe interference over a shared resource, they achieve coexistence in qualitatively different ways. In the hawk-dove game, interference bears a direct fitness cost (c) that trades off with the benefits of interference (b); hawks and doves have identical exploitative ability (e.g. Galanthay et al. 2023; Maynard Smith 1982). In contrast, dominance-discovery has interference ability trade off with exploitative ability (Adler et al. 2007).

Here we develop a model of motile consumers that mechanistically treats both exploitative and interference competition for an explicitly modeled resource. This unifies a

continuum of mechanisms that, depending on parameter values, may resemble the R^* rule,

the hawk-dove game, the dominance-discovery trade-off, or a novel coexistence mechanism

that we call the "dove-discovery" trade-off. We explore which parameter values lead to

which regime, when interference-exploitation trade-offs enable coexistence, and whether the

R^* ratio for competing species (or genotypes) is a reliable metric of competitive success

given the possibility of interference.

METHODS

Model

113   We extend a typical consumer-resource model to incorporate consumer-consumer

114   interference competition over a single shared resource. We consider the following set of

115   differential equations:

$$\frac{dS_i}{dt} = \underbrace{\frac{1}{\tau_i}(1+e)H_i}_{\substack{\text{Handler } i \text{ grows / reproduces} \\ \text{and reinstates search} \\ \text{after consuming resource}}} + \underbrace{2\beta_i C_{ii}}_{\substack{\text{One of two} \\ i \text{ Contestants} \\ \text{gives up}}} + \underbrace{\beta_i\left(C_{ij} + C_{ji}\right)}_{\substack{\text{Contestant } i \text{ gives} \\ \text{up against } j}} \underbrace{-m_i S_i}_{\substack{\text{Base} \\ \text{Mortality}}} - \underbrace{a_i S_i \sum_{j=1}^{2} H_j}_{\substack{\text{Searcher } i \\ \text{initiates contest}}}$$

$$- \underbrace{a_i S_i R}_{\substack{\text{Searcher } i \\ \text{finds unconstested} \\ \text{Resource}}}$$

$$\frac{dH_i}{dt} = \underbrace{a_i S_i R}_{\substack{\text{Searcher } i \\ \text{finds unconstested} \\ \text{Resource}}} + \underbrace{(2\beta_i + 2m_i + 2m_{Ci})C_{ii}}_{\substack{\text{One of two} \\ i \text{ Contestants} \\ \text{wins}}} + \underbrace{(\beta_j + m_j + m_{Cj})\left(C_{ij} + C_{ji}\right)}_{\text{Contestant } i \text{ wins against } j} - \underbrace{m_i H_i}_{\substack{\text{Base} \\ \text{Mortality}}}$$

$$- \underbrace{H_i/\tau_i}_{\text{Consumption}} - \underbrace{H_i \sum_{j=1}^{2} a_j S_j}_{\substack{\text{New Contest} \\ \text{interrupts Handling}}}$$

$$\frac{dC_{ii}}{dt} = \underbrace{a_i S_i H_i}_{\substack{\text{Begin} \\ \text{Contest}}} - \underbrace{(2\beta_i + 2m_i + 2m_{Ci})C_{ii}}_{\text{End contest}} \tag{1}$$

$$\frac{dC_{\{ij\}}}{dt} = \underbrace{a_j S_j H_i + a_i S_i H_j}_{\substack{\text{Begin} \\ \text{Contest}}} - \underbrace{C_{ij}\left(\beta_i + \beta_j + m_i + m_j + m_{Ci} + m_{Cj}\right)}_{\text{End Contest}}$$

$$\frac{dR}{dt} = \underbrace{f(R)}_{\substack{\text{Resource} \\ \text{growth}}} - \underbrace{R \sum_{j=1}^{2} a_j S_j}_{\substack{\text{Consumer} \\ \text{acquires} \\ \text{Resource}}} + \underbrace{\sum_{j=1}^{2} m_j H_j}_{\substack{\text{Resource released when} \\ \text{Handling consume dies}}}$$

While seemingly complex, the system of equations in (1) straightforwardly describes mass

action kinetics (i.e. approximating exponential distributions of waiting times by using

continuous, additive rates) that are most easily understood through inspection of Fig. 1.

Consumer types i and j could either be different species, or different variants of a single

polymorphic species.

Exploitation is shown in the green/left oval of Figure 1. Searching consumers S_i of

type i find Resources R at rate a_i and begin to handle them once encountered. Handlers H_i

consume resources at rate $1/\tau_i$ (Figure 1, right). We refer to τ as "handling time," although

we note that it differs from the transformed handling time (h) traditionally used in ecological

models (Real 1977). Reproduction is proportional to resource consumption $e_i H_i / \tau_i$, with e_i

as a conversion factor.

Consumers die at base rate m_i, elevated by m_{Ci} during contests (see below). We treat

resources as discrete, such that τ specifies the probability that a resource is 0% vs 100%

consumed, rather than the degree to which a resource is consumed. When a consumer dies

while handling a resource, the resource returns to the resource pool (i.e., at rate $m_i H_i$; Fig. 1,

curved arrow below green/left oval).

Interference is shown in the blue and peach ovals of Figure 1. Contests begin when a

Searcher encounters a Handler. C_{ii} represents the number of within-type contests of type i

(Fig. 1, blue), and $C_{\{ij\}} = C_{ij} + C_{ji}$ ($j \neq i$) represents the number of between-type contests

(Fig. 1, peach). Future extensions might distinguish C_{ij}, in which type i found the resource

first, from C_{ji}, but we assume they are equivalent. Conflicts resolve either when a consumer

gives up at rate β_i, or dies at rate $m_i + m_{Ci}$. Because each unit of C_{ii} contains two individuals

of type i, victors re-enter the handling state at rate $(2\beta_i + 2m_i + 2m_{Ci})C_{ii}$. The losers

similarly re-enter the handling state at rate $2\beta_i C_{ii}$. $C_{\{ij\}}$ resolves into a type i victory at rate

$(\beta_j + m_j + m_{Cj})C_{\{ij\}}$, with losers of type i re-entering the handling state at rate $\beta_i C_{\{ij\}}$.

Fig. 1: Model schema. Variables are in upper case, parameters in lower. Full dynamics of
consumer i are shown; those of consumer j are symmetric and truncated from the lower
portion of the figure for simplicity. In green, <u>R</u>esources and type i <u>S</u>earchers ($R + S_i$)
combine to form a <u>H</u>andler (H_i). <u>H</u>andlers of type i combine with <u>S</u>earchers (S_i or S_j) to form
C_{ii} (blue) or $C_{\{ij\}} = C_{ij} + C_{ji}$ (peach) <u>C</u>ontesting pairs, respectively. Search rate is denoted a,
base mortality m, additional mortality from contests m_c, giving up on contests β, and
handling $1/\tau$.

Intra-type interference propensity would exceed inter-type interference if type i gave

up more slowly against i than against j. We avoid this assumption, which is known to easily

produce coexistence (Vance 1984), by making giving up rates β_i depend only on the focal

type i and not on the opponent type j. Similarly, contest initiation occurs whenever a

Searcher encounters a Handler, regardless of their type.

Resource R grows according to a saturating function $f(R)$. We assume $f(R) =$

$r(K - R)$, representing a spontaneously regenerating consumable resource. We consider this

functional form because it avoids limit cycles in the 1-consumer-1-resource case

(Supplementary Materials A), which is not the case for a biological resource exhibiting

logistic growth (i.e. $f(R) = rR(1 - R/K)$) (Johnson and Amarasekare 2015; Rosenzweig

1971). The lack of oscillations simplifies our coexistence analyses, because oscillations

driven by nonlinear functional responses (i.e., handling time) can affect species coexistence

(Armstrong and McGehee 1980). However, numerical simulations suggest that results are not

qualitatively different with logistic resource growth (Supplement Materials B).

Our model (1) has similarities to several previous works. Kooi (2015) and Galanthay

et al. (2023) use a similar set of equations to model hawk-dove-like dynamics, in the special

case where types i and j have identical exploitative ability (a, τ, etc.). Adler et al. (2007)'s

model of the dominance-discovery trade-off corresponds to the limit of fast contests in our

model, which are not explicitly modeled in theirs, with outcomes instead resolved as soon as

one consumer encounters another.

Analysis

In the Supplementary Materials Sections D, F, and G, we solve for invasion criteria

(Turelli 1978) for the two-consumer one-resource system described by equations in (1). To

do so, we first solve the non-trivial equilibrium for each one-consumer one-resource system,

yielding $S_i^*, H_i^*, C_{ii}^*,$ and R_i^*. We derive the 4×4 Jacobian matrix for the variables

$S_j, H_j, C_{jj},$ and $C_{\{ij\}}$ where $j \neq i$. We then compute the eigenvalues of the Jacobian matrix at

consumer i's non-trivial equilibrium when consumer j is a rare invader: $[S_i = S_i^*, H_i =$

$H_i^*, C_{ii} = C_{ii}^*, R_i^*, S_j = 0, H_j = 0, C_{jj} = 0, C_{\{ij\}} = 0]$. We derive the conditions for invasion

and coexistence both analytically and numerically using Mathematica version 13.2.

Consumer j will increase in abundance (invade) when rare if and only if at least one

eigenvalue is positive. Coexistence is inferred from mutual invasibility, which we validate

using numerical simulations of the system of differential equations in (1) (Supplementary

Materials Section C).

RESULTS

R^* rule in the absence of interference competition

191   The R^* rule is a limiting case of our model, which occurs when we remove

192   interference entirely. When a Searcher who encounters a Handler does not contest the

193   resource, the system of equations reduces to

194
$$\frac{dS_i}{dt} = \underbrace{\frac{1}{\tau_i}(1+e)H_i}_{\substack{\text{Handler } i \text{ grows/reproduces} \\ \text{and reinstates search} \\ \text{after consuming resource}}} - \underbrace{m_i S_i}_{\text{Mortality}} - \underbrace{a_i S_i R}_{\substack{\text{Searcher } i \\ \text{finds unconstested} \\ \text{Resource}}}$$

195
$$\frac{dH_i}{dt} = \underbrace{a_i S_i R}_{\substack{\text{Searcher } i \\ \text{finds Resource}}} - \underbrace{m_i H_i}_{\text{Mortality}} - \underbrace{H_i/\tau_i}_{\text{Consumption}}$$

196
$$\frac{dR}{dt} = \underbrace{f(R)}_{\substack{\text{Resource} \\ \text{growth}}} - R\underbrace{\sum_{j=1}^{2} a_j S_j}_{\substack{\text{Consumer} \\ \text{acquires} \\ \text{Resource}}} + \underbrace{\sum_{j=1}^{2} m_j H_j}_{\substack{\text{Resource released when} \\ \text{Handling consume dies}}}$$

197   Let $R^*_{i,E}$ denote the corresponding equilibrium resource abundance set by type i in

198   isolation, in this scenario when only _Exploitative_ competition occurs. Assuming population

199   viability ($R^*_{i,E} > 0$):

$$R^*_{i,E} = \frac{m_i(m_i\tau_i + 1)}{a_i(e_i - m_i\tau_i)} \tag{2}$$

(Supplementary Materials Section D.3) which is feasible when $e_i > \tau_i m_i$ and $R^*_{i,E} < K$. We

refer to $R^*_{i,E}$ as the _exploitative ability_ of consumer i, and to $R^*_{i,E}/R^*_{j,E}$ as the _relative_

exploitative ability of i and j. $R^*_{i,E}$ also represents the minimum resource requirement for

consumer i.

Type i can invade a population of type j if and only if $R^*_{i,E}/R^*_{j,E} < 1$ (Supplementary

Materials Section D.4), and so mutual invasibility requires the unfulfillable condition:

$$1 < \frac{R^*_{i,E}}{R^*_{j,E}} < 1 \tag{3}$$

208   This is the R^* rule of Tilman (1982). Neutral coexistence is possible in the knife edge case of

209    $R^*_{i,E}/R^*_{j,E} = 1$. Equation (3) can be compared to our more general Equation (11).

Interference increases equilibrium resource density

211   Interference competition increases the equilibrium resource density set by a

212   consumer, setting the stage for deviations from the R^* rule. We denote the equilibrium

213   resource density set by consumer i in the 1-consumer-1-resource system when _Interference_

214   occurs as (Supplementary Materials Section E):

$$R^*_{i,I} = R^*_{i,E} \frac{1 + K \frac{r\, a_i\tau_i}{\beta_i + m_i + m_{Ci}}\left(1 + \frac{m_{Ci}}{m_i}\right)}{1 + R^*_{i,E} \frac{r\, a_i\tau_i}{\beta_i + m_i + m_{Ci}}\left(1 + \frac{m_{Ci}}{m_i}\right)}. \tag{4}$$

Because $K > R_{i,E}^*$, Equation (4) implies $R_{i,I}^* > R_{i,E}^*$, with $R_{i,I}^* \to R_{i,E}^*$ as $\beta_i \to \infty$ or as $\tau_i \to 0$.

$R_{i,E}^*$ continues to describe the minimum resource requirement for i: interference thus

decouples a consumer's resource requirement from the resource abundance it sets at

equilibrium.

There are two reasons why interference increases equilibrium resource density. First,

conflict-induced mortality m_{Ci} directly removes consumers, allowing the resource to grow.

The direct cost of contests c in the classic hawk-dove game can readily be interpreted in

terms of a probability of death per contest $c_i = \frac{m_{Ci}}{\beta_i + m_{Ci}}$ as $m_{Ci}, \beta_i \to \infty$ (contests are very fast

and lethal). In this limit, equation (4) becomes:

225
$$R_{i,I}^* = R_{i,E}^* \frac{1 + K c_i \dfrac{r a_i \tau_i}{m_i}}{1 + R_{i,E}^* c_i \dfrac{r a_i \tau_i}{m_i}}.$$

$R_{i,I}^*$ increases as the probability of contest mortality c_i increases.

Second, engaging in conflicts incurs an opportunity cost, because time spent in a

conflict is not available for searching or handling resources, allowing the resource to grow.

Consequently, $R_{i,I}^* \geq R_{i,E}^*$ even if contests do not increase death rates (substitute $m_{Ci} = 0$ into

Equation (4)). The extent to which opportunity costs increase resource density depends on

how the time spent in contests compares to the rate at which new resources appear.

Opportunity costs are large when contests begin frequently (large $a_i \tau_i$), when contests are

long (small β_i) and when resources renew rapidly (large r; see Equation (4)). Below, we

emphasize opportunity costs only (by assuming $m_{Ci} = 0$), but the same qualitative results

apply for direct costs.

Classifying outcomes when only one type interferes

Our main goal is to unify previously disparate mechanisms of interference and

exploitative competition over resources. To this end, we first consider a simplified version of

the set of equations in (1), with limiting cases that resemble the hawk-dove game and the

dominance-discovery trade-off. We consider two types of consumers: (1) a "hawk" h that

contests resources ($\beta_h < \infty$) and (2) a "dove" d that does not ($\beta_d = \infty$), replacing our

previous, more general notation of i and j. In later sections, we will consider the more

general asymmetric case of $\beta_h < \beta_d < \infty$. Note that the h indicating a "hawk" should not be

confused with the H indicating "Handlers".

Doves can invade a community of hawks if:

246
$$R_{d,E}^* < R_{h,I}^* P_d' \tag{5}$$

247   where

248
$$P_d' = \frac{1}{1 + \dfrac{a_h S_h^*}{1/\tau_d + m_d}}$$

is the probability that a dove does not experience hawk interference during handling

(Supplementary Materials Sections F.4.1 and F.5). Equation (5) represents the fact that doves

must be able to persist at a resource density ($R_{d,E}^*$) not just below the equilibrium set by the

hawks ($R_{h,I}^*$), but below a lower level that takes into account doves' inability to benefit from

resources that they relinquish to hawks ($P_d' R_{h,I}^*$). Note that from $\beta_d = \infty$, we have $R_{d,I}^* =$

$R_{d,E}^*$, in contrast to $R_{h,I}^* > R_{h,E}^*$. Hawk interference generates both a benefit ($R_{h,I}^* > R_{h,E}^*$) and

a cost ($P_d' < 1$) to dove invasion.

Hawks can invade a resident dove population if:

257
$$R^*_{h,E} < R^*_{d,E} + H^*_d \qquad (6)$$

258   (Supplementary Materials Section F.4.2). Equation (6) represents the fact that hawks must be

259   able to persist on resources that include both those currently unclaimed by doves ($R^*_{d,E}$), and

260   those currently held by doves that hawks can readily steal (H^*_d).

261   The two invasion criteria can be rearranged to form the mutual invasion criterion

262
$$\frac{1}{1 + H^*_d / R^*_{d,E}} < \frac{R^*_{d,E}}{R^*_{h,E}} < \frac{R^*_{h,I}}{R^*_{h,E}} P'_d \qquad (7)$$

(Supplementary Materials Section F.4.3), which implies coexistence when fulfilled. Equation

(7) can be compared to Equation (3) describing exploitation alone.

Connection to the Classic Hawk-Dove Game

The traditional hawk-dove game is akin to a special case of our model, when hawks

and doves have identical exploitative ability ($R^*_{d,E} / R^*_{h,E} = 1$). In this scenario, the hawk can

always invade a dove population (from Equations (6) and (7)). The dove can also invade a

pure hawk population, implying coexistence, when:

270
$$1 < \frac{R^*_{h,I}}{R^*_{h,E}} P'_d \qquad (8)$$

Akin to the classic hawk-dove game, the dove invades if the cost associated with hawk-hawk

interference ($R^*_{h,I} / R^*_{h,E} > 1$) more than compensates for hawk-dove resource theft ($P'_d < 1$).

Hawk-dove coexistence, if it occurs, thus stems from an "intra-type interference – inter-type

interference trade-off". Hawks benefit from stealing from doves (inter-type interference).

Doves invade due to the increase in resource density caused by hawk-hawk (intra-type)

interference.

Connection to the Dominance-Discovery Trade-off

In dominance-discovery models, contests resolve instantaneously and are not directly

costly. Our model can capture this by letting hawks finish contests arbitrarily fast ($\beta_h \to \infty$),

while always defeating doves ($\beta_h/\beta_d = 0$). This yields $R^*_{h,I} \to R^*_{h,E}$. The coexistence criteria

then become

282
$$\frac{1}{1 + H^*_d/R^*_{d,E}} < \frac{R^*_{d,E}}{R^*_{h,E}} < P'_d. \tag{9}$$

The dove then needs to be superior at exploitation ($R^*_{d,E}/R^*_{h,E} < 1$) to invade (because

$P'_d \leq 1$), offsetting the disadvantage of losing contests. The resemblance of this model limit

to the dominance-discovery trade-off is most intuitive when the dove's superior exploitation

comes from a higher search rate (a). The condition for dove invasion is then $a_d P'_d > a_h$, i.e.

faster resource discovery of doves must more than compensate for theft by hawks. Hawks can

invade if there are enough doves handling resources (H^*_d) that can be stolen, to compensate

for hawks' inferior exploitative ability. Coexistence, if it occurs, thus stems from an

"exploitation – inter-type-interference trade-off".

The dominance-discovery trade-off and hawk-dove coexistence differ with respect to

how doves invade. With hawk-dove coexistence, doves invade by taking advantage of

increased resource density due to hawk-hawk interference ($R^*_{h,I}/R^*_{h,E} > 1$). With the

dominance-discovery trade-off, doves invade because of superior exploitative ability

($R^*_{d,E}/R^*_{h,E} < 1$). Note each dove invasion criterion depends on the ratio of different R^*s.

Classifying outcomes when both types interfere

We generalize our above results by analyzing our model when both consumer types

interfere.

General Invasion Criteria

When both β_i and $\beta_j < \infty$, we refer to the consumer with the smaller β as the hawk

and that with the larger β as the dove based on their propensities to engage in interference

contests, although both are on a spectrum of hawkishness and dovishness. Generalizing

equations (5) and (6), j can invade i if and only if:

304
$$R_{j,E}^* < P_j\left(R_{i,I}^* + \omega_{ji}H_i^*\right). \tag{10}$$

305   (see Supplementary Materials Section G.3 for derivation; note that for simplicity, we assume

306    $e_i = e_j = e$ and $m_i = m_j = m$). As before, $R_{i,I}^*$ is the resource availability set by consumer i,

307   including intra-type-i interference effects. The new term ω_{ji} is the probability that invader

308   j wins a contest against resident i:

309
$$\omega_{ji} = \frac{\beta_i + m}{\beta_i + \beta_j + 2m}.$$

310   (see Supplementary Section Materials G.5). $\omega_{ji}H_i^*$ represents resources that invader j steals

311   from handling residents of type i, i.e. type j's benefit from inter-type interference. $R_{i,I}^* +$

312    $\omega_j H_i^*$ is the total resource available to j.

313   P_j is a generalization of P_d' from equation (5). P_j quantifies the negative impact that

314   inter-type interference has on the invasion of type j ($0 \leq P_j \leq 1$) where

315
$$P_j = \cfrac{1}{1 + \underbrace{\frac{a_j H_i^*}{\beta_i + \beta_j + 2m}}_{\substack{\text{time spent in} \\ \text{contests started by } j}} + \underbrace{\frac{a_i S_i^*}{1/\tau_j + m}}_{\substack{i \text{ initates} \\ \text{contests}}}\left(\underbrace{\omega_{ij}}_{\substack{\text{theft} \\ \text{probability}}} + \underbrace{a_j \frac{H_i^* + R_{i,I}^*}{\beta_i + \beta_j + 2m}}_{\text{opportunity cost}}\right)}$$

See Supplementary Materials Section G.3 for a derivation.

The first non-unity term in the denominator of P_j captures the opportunity cost from

contests initiated by type j. The second term reflects costs from contests initiated by type i

against j. Costs are larger when resource theft by i is more likely (larger ω_{ij}) and when

opportunity costs of participation are greater. Opportunity costs increase with the resource

encounter rate, $a_j(H_i^* + R_{i,I}^*)$. This illustrates the key tension of hawkish behavior: giving up

slower (smaller β_j) decreases the probability of losing contests but increases opportunity

costs. Short handling time reduces the cost of interference; if type j rapidly handles resources

($\tau_j \rightarrow \infty$), i cannot initiate contests with j and the second term in P_j disappears ($\frac{a_i S_i^*}{1/\tau_j + m} \rightarrow 0$).

Classifying coexistence and exclusion outcomes

Rearranging Equation (10) for each type (i and j) in Supplementary Material G.4, we

derive criteria for coexistence in terms of interference competition I_j and I_i, and relative

exploitative competition ability E_{ji}:

$$
\underbrace{\frac{1}{P_i\left(\frac{H_j^*}{R_{j,E}^*}\omega_{ij} + \frac{R_{j,I}^*}{R_{j,E}^*}\right)}}_{\substack{\text{Net impact of} \\ \text{interference on the} \\ \text{invasion of type } i \\ (I_i)}} \;<\; \underbrace{\frac{R_{j,E}^*}{R_{i,E}^*}}_{\substack{\text{Relative} \\ \text{exploitative} \\ \text{ability} \\ (E_{ji})}} \;<\; \underbrace{P_j\left(\frac{H_i^*}{R_{i,E}^*}\omega_{ji} + \frac{R_{i,I}^*}{R_{i,E}^*}\right)}_{\substack{\text{Net impact of} \\ \text{interference on the} \\ \text{invasion of type } j \\ (I_j)}} \tag{11}
$$

i invades if the left-hand side inequality is fulfilled; j invades if the right-hand side inequality

is fulfilled. Equation (11) reduces to Equation (7) if j does not interfere ($\beta_j \rightarrow \infty$) and further

reduces to the R^* rule (equation (3)) in the absence of interference (for which $I_i = I_j = 1$).

The interference terms (I_i, I_j) permit deviations from the R^* rule and quantify the

impacts of interference relative to exploitative competition (E_{ji}) in determining outcomes.

How far the logarithm of each term deviates from 0 quantifies its impact on invasion. For

example, type j invades if $E_{ji}/I_j < 1$; the magnitude of departure from equality is $\log E_{ji} -$

$\log I_j$. Whether the difference in exploitation vs. in interference quantitatively contributes the

most to the outcome depends on whether $\left|\log E_{ji}\right| > \left|\log I_j\right|$. Signs of the log-terms indicate

whether exploitation and interference favor i vs. j, while magnitudes indicate the relative

importance of the terms, regardless of sign. We therefore use the absolute value of the logs

when we wish to focus on magnitude (e.g. $E_{ji} = 1/2$ and $E_{ji} = 2$ describe exploitative

differences equal in magnitude; $\left|\log E_{ji}\right|$ preserves this equality).

344   We again substitute h (hawk) and d (dove) for the more general i and j, on the basis

345   of $\beta_h < \beta_d$. We compare the magnitudes of $|\log I_d|$, $|\log E_{dh}|$, and $|\log I_d|$ to distinguish six

346   possible scenarios in Table 1 and Fig. 2. Firstly, differences in exploitative ability may be

347   predominantly responsible for competitive exclusion. This scenario resembles the R^* rule

348   because the exploitative R_E^* ratio, $|\log E_{dh}|$, underlies exclusion (Fig. 2, top portion of blue

349   area).

350   Secondly, interference competition can cause competitive exclusion (Fig. 2, left

portion of blue area). This can occur via two mechanisms. (1) "Hawk victory" in which

hawks exclude doves via inter-type interference when $|\log E_{dh}| < |\log I_d|$. (2) "Dove

victory" in which doves exclude hawks when the opportunity costs from interference are too

large, when $|\log E_{dh}| < |\log I_h|$. Unlike the simplified case of $\beta_h = \infty$, the hawk may be

excluded even if the dove is not superior at exploitation. It is therefore possible for a

consumer who is both superior at exploitation and more likely to win contests to be

competitively excluded.

Fig. 2: Interference I_j and exploitative E_{ji} combine to shape outcomes (here $I_i = 2$). Whether i vs. j is the dove depends on which has larger β, information not given by I_j, I_i, and E_{ji}. Colors indicate outcomes: i excludes j (blue) or coexistence (purple). Lines delineate mechanisms by which outcomes are achieved, as summarized in Table 1. Coexistence comes from either an interference vs. exploitation trade-off (dominance-discovery and dove-discovery), or an inter-type interference vs. intra-species interference trade-off (hawk-dove coexistence). Competitive exclusion is driven by either exploitative competition (R^* rule), or interference competition (hawk and dove victories).

Coexistence can occur via three mechanisms. Firstly, "hawk-dove coexistence" describes when interference considerations enable invasion of both types: $|\log E_{dh}| < |\log I_d|$, and $|\log E_{dh}| < |\log I_h|$. Those considerations are the hawk's gain from stealing (intra-type interference), and the dove's gain from hawk-hawk contests (intra-type interference). This generalizes the inter-type vs intra-type interference trade-off beyond the previous section's treatment of $\beta_d = \infty$.

Coexistence can also occur via a trade-off between exploitative and interference

abilities (Fig. 2, top and bottom portions of purple area). This trade-off occurs via two distinct

mechanisms. First, doves invade primarily due to superior exploitative ability ($|\log E_{dh}| >$

$|\log I_d|$) while hawks invade predominantly due to interference effects, meaning stealing

resources from doves ($|\log E_{dh}| < |\log I_h|$). This scenario resembles the dominance-

discovery trade-off, generalizing our treatment above of the $\beta_d = \infty$ case. This scenario can

also be thought of as a "hawk-discovery" trade-off.

The direction of the exploitative vs. interference trade-off is reversed in the second

mechanism: doves primarily invade due to the increase in resource density caused by hawk-

hawk interference ($|\log E_{dh}| < |\log I_d|$), while hawks invade primarily due to superior

exploitative ability ($|\log E_{dh}| > |\log I_h|$). This constitutes a novel intra-type-interference vs.

exploitation trade-off, which we call the "dove-discovery trade-off".

Scenario	Description	Invasion Criteria	Condition(s)
R^* Rule	Either type is excluded due to inferior exploitative ability.	$1/I_h > E_{dh} < I_d$ OR $1/I_h < E_{dh} > I_d$	$\|\log E_{dh}\| > \|\log I_h\|$ OR $\|\log E_{dh}\| > \|\log I_d\|$
Hawk victory	Dove is excluded due to inter-type interference	$1/I_h < E_{dh} > I_d$	$\|\log E_{dh}\| < \|\log I_d\|$
Dove victory	Hawk is excluded due to opportunity cost	$1/I_h > E_{dh} < I_d$	$\|\log E_{dh}\| < \|\log I_h\|$
Hawk-dove coexistence	Hawk invades due to inter-type interference, dove due to intra-hawk interference.	$1/I_h < E_{dh} < I_d$	$\|\log E_{dh}\| < \|\log I_d\|$, $\|\log E_{dh}\| < \|\log I_h\|$,
Dominance-Discovery trade-off	Dove invades due to superior exploitation, hawk invades due to inter-type interference.	$1/I_h < E_{dh} < I_d$	$\|\log E_{dh}\| > \|\log I_d\|$, $\|\log E_{dh}\| < \|\log I_h\|$,
Dove-Discovery trade-off	Hawk invades due to superior exploitation, dove invades due to intra-hawk interference.	$1/I_h < E_{dh} < I_d$	$\|\log E_{dh}\| < \|\log I_d\|$, $\|\log E_{dh}\| > \|\log I_h\|$,

Table 1: Summary of the different scenarios, associated criteria for invasion or lack of
invasion, and the conditions that further distinguish scenarios beyond their invasion criteria.
h indexes the "hawk" and d the "dove" on the basis of $\beta_d > \beta_h$. Each scenario refers to the
predominant mechanism underlying the outcome. Expressions come from Equation (11).

Finally, a priority effect (founder control) occurs when $1/I_h > E_{dh} > I_d$. However,

we do not discuss this scenario in detail, nor include it in Table 1 or Fig. 2 because priority

effects require unlikely parameter value choices in our model (Supplementary Materials

Section H).

I_j and E_{ji} are not independent, despite being shown on orthogonal axes in Fig. 2.

Instead, changes to a single model parameter alter multiple key properties ($R_E^*, R_I^*, \omega H^*, P$).

We next dig deeper into the causal effects of mechanistic parameters on competitive

outcomes and which scenario causes them.

Fig. 3: The hawk-dove game for types that vary only in giving up rate β. A) Coexistence
requires $\beta_h < \beta_0 < \beta_d$, where β_0 is shown as a yellow star. B) β_h and β_d strongly modify the
ratio of resources set by each type at equilibrium, $R_{h,I}^*/R_{d,I}^*$. Coexistence occurs in the upper-
left, where $R_{h,I}^*/R_{d,I}^*$ is the farthest from unity. Note the log scale for color in Panel B.
Throughout, parameters are: $\tau = 1, a = 0.1, m = 0.015, e = 0.035, m_C = 0, r = 0.26, K = 250$.

Outcome classification based on mechanistic parameters

First, consider the relatively simple case of hawk and dove equal in all parameters

except giving up rate, β, resulting in equal exploitative abilities. Hawk-dove coexistence

(Table 1) occurs if and only if β_h and β_d are on either side of a central value (henceforth β_0;

Fig. 3A, yellow star). β_0 is a complicated (though mathematically tractable) expression that

depends on every parameter of the model (Supplementary Materials Section G.6).

R^* theory predicts the exclusion of the consumer that sets a higher equilibrium

resource abundance. However, coexistence predominantly occurs when the equilibrium

resources abundances differ by a large factor (Fig. 3B, top-left corner), while small

differences are associated with competitive exclusion. Coexistence corresponds to a greater

R^* ratio ($R_{h,I}^*/R_{d,I}^*$) because dove invasion requires intra-hawk interference to increase the

equilibrium resource density set by the hawk. The ratio of equilibrium resources abundances

$R_{h,I}^*/R_{d,I}^*$ should not be confused with the exploitative R^* ratio; $E_{dh} = 1$ in Fig. 3.

We now consider types that also differ in exploitative ability. Instead of denoting

types by their giving up rates as hawk h and dove d, we distinguish types by their relative

exploitative ability. We denote type 2 as better at exploitation than type 1 ($R_{1,E}^*/R_{2,E}^* > 1$);

this implies nothing about which type is the hawk vs. dove with respect to β. The sometimes

dramatic extent to which exploitative differences change the region of coexistence (Figs. 4-

5), depends on the relative importance of interference vs. exploitative differences, which is

mediated by the mechanistic parameters.

For example, exploitative competition is relatively important for a rapidly handled

resource because small τ decreases the frequency of contests. Correspondingly, the region of

coexistence declines with decreasing τ (Fig. 4, left to right) given a constant difference in

exploitative ability (Fig. 4 bottom row, $R_{1,E}^*/R_{2,E}^* = 1.2$ via $a_2 > a_1$), but not when

exploitative ability is identical (Fig. 4 top row).

Fig. 4: Short handling time erodes coexistence when types differ in exploitative ability. Consumers 1 and 2 differ in search rate (a) and giving up rate (β)**.** Below the dashed diagonal line, $\beta_1 > \beta_2$ makes type 1 the dove, while type 1 is the hawk above the line. Columns vary the handling time. Panels A-C depict identical exploitative abilities; gold stars are as defined in Fig. 3. In panels D-F, type 2 is better at exploitation ($a_2 = 0.12 > a_2 = 0.10$). Other parameters are: $m = 0.015, e = 0.035, m_{C1} = m_{C2} = 0, r = 0.26, K = 250$.

Differences in exploitative ability have different effects on interference competition

when mediated by a rather than τ. Faster search a slightly increases opportunities to interfere

with others, while shorter handling time τ dramatically decreases vulnerability to

interference. When different search rates are responsible for a moderate difference in

exploitative ability (e.g., $R^*_{1,E}/R^*_{2,E} = 1.2$ because $a_2 > a_1$; Fig 5B, 5H), outcomes are little

impacted (compare Figs. 5A and 5B), at least when τ is not very small (Fig. 4). However, the

mechanism behind the same outcome (coexistence or competitive exclusion) may be different

(compare Figs. 5G and 5H). When giving up rates (β) are similar, the R^* rule operates. When

coexistence occurs, it can now stem from exploitation-interference trade-off scenarios (the

dominance-discovery and dove-discovery trade-offs) rather than from an inter-type vs. intra-

type interference trade-off (hawk-dove coexistence). Even with larger differences in

exploitative ability (e.g., $R^*_{1,E}/R^*_{2,E} = 1.75$ because $a_2 > a_1$; Fig 5C, 5I), coexistence remains

possible for a wide region of parameter space, largely via exploitation-interference trade-offs.

When differences in handling time τ drive the same advantage in exploitative ability

(e.g. $R^*_{1,E}/R^*_{2,E} = 1.2$ because $\tau_2 < \tau_1$), coexistence becomes less likely than when driven by

differences in search rate a (compare Figs. 5B with 5D and Figs. 5C with 5E). Coexistence

largely evaporates when large exploitative differences are caused by τ ($R^*_{1,E}/R^*_{2,E} = 1.75$ in

Fig. 5E). Hawk or dove victories dominate the parameter space in which competitive

exclusion occurs, rather than the R^* rule (Fig. 5K).

The difference in exploitative ability ($R^*_{1,E}/R^*_{2,E}$) does not reliably explain outcomes.

Fig. 5F shows an example where type 1 is superior at exploitation ($R^*_{1,E}/R^*_{2,E} = 0.5$) yet is

excluded via interference by type 2, which searches more slowly ($a_1 > a_2$) but uses

resources faster ($\tau_2 < \tau_1$). Type 1 is excluded in this scenario irrespective of whether it

utilizes a hawk or dove strategy (Fig. 5L) and even though both $R^*_{1,E}/R^*_{2,E} < 1$ and

$R^*_{1,I}/R^*_{2,I} < 1$ for much of the parameter space. The disconnect between $R^*_{1,E}/R^*_{2,E}$ and

outcomes reflects in how R^*_E effected by a vs. τ also impact interference.

Fig. 5: Differences in exploitative ability effected by search speed a permit more coexistence than those effected by handling time τ, due to impacts also on interference competition. Row 1 (A-F) depicts outcomes and row 2 (G-H) depicts the corresponding dominant mechanism as defined by Table 1. The dashed diagonal line delineates when type 1 is the Dove (below) or the hawk (above). The first column shows consumers that are identical in every exploitative parameter. The second and third columns show differences in search rate ($a_2 = 0.12$ or $a_2 = 0.175 > a_1 = 0.1$). The fourth and fifth columns show differences in resource use rate ($\tau_2 = 1/1.35$ or $\tau_2 = 1/30 < \tau_1 = 1$), and the rightmost column shows differences in both ($0.35 = a_1 > a_2 = 0.1$; $1/5.19 = \tau_2 < \tau_1 = 1$). When not specified above, $a_i = 0.1, \tau_i = 1, m = 0.015, e = 0.035, m_C = 0, r = 0.26, K = 250$.

DISCUSSION

Exploitative resource competition is the foundation of much ecological theory, often in the form of R^* theory (Tilman 1982), but its co-occurrence with interference competition has received less focus. Here, we analyze a mechanistic framework in which consumers can be interrupted by interference from competitors while handling a resource, and time invested in contesting a resource incurs an opportunity cost of not searching for uncontested resources. Outcomes rarely follow R^* theory, whether R^* is interpreted as the equilibrium resource level (R_I^*) or as the hypothetical equilibrium resource level in the absence of interference (the minimum resource level required for persistence R_E^*). Coexistence can stem from a trade-off between inter-type interference and intra-type interference (hawk-dove coexistence), from a trade-off between exploitation and inter-type interference (dominance-discovery), or from a novel trade-off between exploitation and intra-type interference that we call dove-discovery. Which outcome occurs via which form(s) of competition is a complex outcome of parameter value combinations, with search rate and handling time simultaneously affecting both exploitation and interference.

Interference competition and R^* Theory

A key result of R^* theory – the R^* rule – breaks down with interference competition for two basic reasons. Firstly, interference allows the equilibrium resource density to rise, making the minimum tolerated resource density less important. Within R^* theory, the minimum tolerated resource density R_E^* is equal to the equilibrium resource density R_I^*. With interference, this is no longer true. Secondly, when invading consumers steal resources, their growth rate is higher than expected from the equilibrium density of free resources.

Our mechanistic terms for search rate and resource handling rate affect not just exploitative ability, but also interference competition. Genotypes or species that achieve low

R_E^* by handling resources more rapidly also gain substantial protection from interference.

Genotypes or species that achieve the same low R_E^* through faster search benefit more

modestly from an increased ability to interfere with others. Previous models used handling

time to describe relative non-linearity in consumers' functional responses (Armstrong and

McGehee 1980), and explored its effects on intrinsically driven consumer-resource

oscillations (Johnson and Amarasekare 2015; Rosenzweig 1971). We emphasize for the first

time the effect of handling time on interference rather than exploitation.

R^* theory and the R^* rule hold within some regions of parameter space (Fig. 5); how

common these are is an empirical question. While R^* theory has experimental support

(Wilson et al. 2007), this generally comes from well-mixed chemostats. Interference invokes

co-localization of at least two individuals and a resource; well-mixed chemostats minimize

the duration of co-localization in which a contest can occur. Outside the laboratory, spatial

structure is ubiquitous and interference competition is widespread; perhaps most obviously in

animals, often over territories (Drury et al. 2020; Schoener 1983), but also among plants via

soil interactions and allelopathy (Inderjit et al. 2011; Meiners et al. 2012; Rice 2012), and

among microbes through mechanisms such as stabbing and toxin-antitoxin systems (Böck et

al. 2017; Boynton 2019; García-Bayona and Comstock 2018; Ghoul and Mitri 2016).

Measuring outcomes plus exploitative ability provides insufficient evidence in favor

of the R^* rule, because the same consumer can also be favored by interference competition.

Ideally, experiments and models should be tailored to the mechanistic biology of the

organisms in question. Comparing R_E^* (e.g. as implied by measured trait values a, m, e, and

τ) to R_I^* (as measured by the equilibrium resource abundance) could quantify the strength of

negative intra-specific density-dependence driven by interference.

Comparison with Past Coexistence Models

Density-dependence in our model emerges not just from resource depletion via

exploitation, but also from more frequent interference with higher consumer density. In

contrast, every round of the classic hawk-dove game (Maynard Smith 1974) involves a

contest, and the payoff matrix does not depend on density. Our approach, in which the

absolute density of consumers regulates interference dynamics, also differs from models in

which payoff matrices of interacting competitors depend on environmental variables such as

resource density (Tilman et al. 2020). Our underlying model is more similar to work

incorporating density-dependence into game theory models, to position hawk-dove dynamics

within more ecologically realistic scenarios (Auger et al. 2006; Galanthay et al. 2023; Kooi

2015; Křivan and Cressman 2022; Křivan et al. 2018). Our work formally connects this class

of models to ecological coexistence and R^* theory for the first time.

We distinguish between two different exploitation-interference trade-offs. One

resembles the dominance-discovery trade-off described by Adler et al. (2007), in which inter-

type interference enables hawk invasion, and superior exploitation enables "dove" invasion

(typically via faster resource discovery/search rate). In contrast, it is intra-hawk interference

that enables dove invasion under hawk-dove coexistence. The dominance-discovery trade-off

can alternatively be thought of as a "hawk-discovery" trade-off in our model.

Competition-colonization trade-off models (Hastings 1980; Horn and MacArthur

1972; Tilman 1994) are formally similar. Our model has two key differences. Firstly, as in

Adler et al. (2007), we consider consumption of an exhaustible resource instead of durable

territories. Secondly, "competition" in our model is interpreted as interference, rather than as

local superiority in exploitation (e.g., a plant species with a lower R^* for nitrogen that locally

excludes its competitor on a patch of a metacommunity; Tilman 1994). Classically,

coexistence requires the inferior exploiter (with higher local R^* for nitrogen) to colonize

patches more rapidly. This can be interpreted as having a lower "global" R^*, despite higher

local R^*, where global R^* represents the equilibrium proportion of unoccupied patches set by

a species in monoculture. Coexistence in these classic models thus requires a trade-off

between local and global exploitation competition with corresponding R^*s. These local and

global R^*s should not be confused with R_E^* and R_I^* introduced in our model.

We discovered a second and perhaps counterintuitive exploitation-interference trade-

off: "dove-discovery". Here the hawk invades due to its superior exploitative abilities, in

addition to its (by definition) superiority at inter-type interference. The dove can nevertheless

invade because intra-hawk interference frees up resources. Hawk invasion can require an

exploitative advantage because winning inter-type contests might not be enough to counter

the high opportunity costs of those inter-type contests. This emphasizes that relatively

doveish behavior can yield a competitive advantage.

Dove-discovery complicates empirical efforts to detect and interpret trade-offs in

interference and exploitative abilities, e.g. in ants suspected to be subject to the discovery-

dominance trade-off (Davidson 1998; Fellers 1987; Holway 1999). Under dove-discovery,

coexisting types who are better at obtaining resources are expected to be less likely to win

contests, at least in the absence of additional trade-offs (e.g., vulnerability to parasitoids

Adler et al. 2007; LeBrun 2005). However, under dove-discovery, species or genotypes that

are more likely to win contests are also better at obtaining resources – the exact opposite

pattern. Similarly, under hawk-dove coexistence, either the hawk or dove may be superior at

exploitation. Empirical investigations looking for trends consistent with dominance-discovery

and competition-colonization trade-offs (often yielding mixed support; for a recent review,

see Ferzoco and McCauley 2023) may therefore overlook key interference-related

coexistence mechanisms. Hawk-dove coexistence and the dove-discovery trade-off have not

received similar levels of attention in this context, perhaps because previous theory had not

outlined the conditions under which they occur. Hawk-dove and dove-discovery make up a

large region of coexistence space (Fig. 5) and may turn out to be as or more important than

dominance-discovery for maintaining coexistence in empirical communities.

Interference-exploitation trade-offs (dominance-discovery and dove-discovery) and

inter-type vs intra-type interference trade-offs (hawk-dove) are not mutually exclusive. While

our Fig. 5 classifications are based on which has the larger effect on invasion, a second,

weaker trade-off might either reinforce or weaken coexistence.

Previous Models of Interference Competition

Most previous models of interference competition use Lotka-Volterra-like terms in

phenomenological models to summarize the strengths of intra- and inter-specific interference

(Case and Gilpin 1974; Hsu 1982; Schoener 1976; Schoener 1978; Vance 1984). Papers such

as Vance (1984) suggest that coexistence requires intra-specific interference to exceed inter-

specific interference. Our model shows this is not necessary: we find coexistence occurs even

if genotypes/species are equally likely to interfere with themselves or the other

genotype/species.

McPeek (2012) incorporated a phenomenological intra-specific density-dependent

term for consumers into a consumer-resource model, which increases the resource level set

by a resident (mathematically similar to our distinction between R_E^* and R_I^*). Adding this term

allows multi-consumer coexistence on a single resource. Our model provides a mechanistic

basis by which this might occur within a model of resource consumption; intra-type

interference competition interrupts consumption and thus increases resource density.

Amarasekare (2002), analyzing a model similar to ours, assumed no intra-specific

interference (implying $R_E = R_I^*$), and concluded that (1) mutually costly forms of

interference (e.g., aggression, territoriality) cannot maintain coexistence, and (2) interference-

exploitation trade-offs can facilitate coexistence when interference is beneficial to the inferior

exploiter. Amarasekare (2002) then interprets "beneficial" interference as intraguild predation

or parasitism, to argue that the restricted nature of these scenarios limits the role of

interference in promoting coexistence. An alternative interpretation is that aggression,

territoriality, and interference over resources within dominance-discovery also qualify as

"beneficial" because the aggressor can profit from acquiring stolen resources. Interference

also promotes coexistence via hawk-dove dynamics and the dove-discovery trade-off, which

make up a large portion of potential coexistence space, and are not examined in Amarasekare

(2002). This suggests that the breadth of conditions under which costly interference

competition maintains coexistence is much larger than previously recognized.

Interference, Character Displacement, and the Evolution of Niche Differences

Our theory provides foundations with which one might understand how interference

competition modifies character displacement and the evolution of niche differences (Brown

and Wilson 1956; Grant and Grant 2006). Classic work on character displacement focuses on

exploitative competition, an emphasis perhaps stemming from the remarkable associations of

beak size/shape and seed diet observed in Darwin's finches (Grant 1999; Grant and Grant

2006). However, several recent studies highlight so-called Agonistic Character Displacement

(ACD), broadly defined as phenotypic evolution due to interference competition among

sympatric species (Grether et al. 2013; Grether et al. 2009; Grether et al. 2017). ACD enjoys

growing empirical support (Anderson and Grether 2010; McEachin et al. 2024; Moran and

Fuller 2018). Our model provides a basis with which to contextualize the role of interference

competition, especially ACD, in niche evolution.

The fact that handling time modifies both exploitation and interference has

implications for niche evolution as depicted in classic ecological models that only consider

exploitative competition. For example, MacArthur's consumer–resource model (Chesson

1990; MacArthur 1970) describes a 2-consumer-multiple-resource exploitative competition

model in which niche differences are defined in terms of a trait (e.g., beak shape) that

determines its search rate for each resource (e.g., different seeds sizes/shapes). The evolution

of niche differences is construed as the selective pressure driven by inter-specific overlap in

resource exploitation (Pastore et al. 2021; Song et al. 2019). MacArthur's consumer–resource

model ignores handling time, which does not matter for exploitation-only models. However,

shorter handling times decrease vulnerability to interference. Many specialized

morphological features (e.g. bird beak morphology and its compatibility with seed

shape/size) do more to decrease handling time than to make search more rapid. Selection for

trait specialization might be driven in part by escaping interference.

Caveats, Future Directions, and Conclusion

We analyzed a simple ecological scenario – two consumers competing for a single

limiting resource – to describe conditions and mechanisms of coexistence. It remains an open

question precisely how much diversity can be maintained when interfering consumers

compete for multiple resources.

Our model considers a spontaneously generated, consumable resource, rather than a

biotic resource that undergoes a replicative form of growth from a starting population. The

same general principles likely apply for other resource types, with an interesting caveat.

Because our model introduces resource handling, consumers have non-linear functional

responses (Holling 1965). For a replicating resource, this allows the possibility of stable limit

cycles. When different non-linear functional responses result in a trade-off between fitness in

low-resource environments (gleaners) and high-resource environments (opportunists),

resource oscillations may contribute to coexistence (Armstrong and McGehee 1980;

Yamamichi and Letten 2022). The interplay of this effect with interference competition is

beyond the scope of our study.

Our modeling of interference as a delay before a motile organism "gives up" is not an

obvious fit to sessile plants, although it is, following precedent in classic game theory

(Maynard Smith and Price 1973), a good fit for motile animals (Ferzoco and McCauley 2023;

Rodríguez et al. 2007; Stanton et al. 2002). Specifically, temporal investment in interference

incurs an opportunity cost to foraging, facilitating coexistence. Plants also invest in local

interference strategies, e.g., root competition, overgrowth, undercutting, and allelopathy,

likely incurring an opportunity cost to reproduction and resource acquisition, rather than to

foraging. Such trade-offs are likely ubiquitous, and process-based models of interference

tailored to plant biology may yield results similar to our study.

Our model considers a consumable resource. Bertram and Masel (2019) considered

competition for a durable resource such as territory, via three traits within a variable-density

lottery model: the rate b that adults give birth to and disperse juveniles, juveniles' ability c to

contest each other to take possession of an unoccupied territory and thus become adults, and

adult survival $1/d$. Our searching term a is somewhat analogous to b, our persistence in

interference competition $1/\beta$ is somewhat analogous to c, and our mortality m is directly

analogous to d.

These similarities perhaps reveal profound patterns. (Grime 1977; Grime 1988; Grime

2006) hypothesized that trade-offs shaped species into three types of specialization:

"ruderals" tolerate low resource levels, "competitors" excel at interference competition, and

"colonizers" rapidly disperse to ephemeral resources. Grime's three-dimensional scheme is

often contrasted with R^* models of exploitative competition (the "Grime-Tilman debate";

(Aerts 1999; Craine 2005; Jabot and Pottier 2012). A major obstacle to synthesis has been the

lack of explicit mathematical models of Grime's scheme (Jabot and Pottier 2012; Tilman

2007). Our framework mathematically unites ideas of Grime with ideas of Tilman. Grime

imagined low density environments in which intraspecific competition (both interference and

exploitation) was weak and ruderals would prevail, whereas Tilman's view was that

organisms in apparently low density environments simply had larger territories, with resource

levels still set by consumption down to the lowest tolerated level. Our work provides loose

support for Grime's view, by highlighting that resource levels need not be set by exploitation

alone.

In the ant literature, Grime's colonizers are called discoverers, Grime's competitors

are called dominators, and a slightly different take on Grime's ruderals is known as the

insinuator foraging strategy (Hölldobler and Wilson 1990; LeBrun 2005). Insinuators adopt

non-aggressive strategies to capitalize on a small portion of resources. In our model,

discoverers are characterized by a high search rate, and dominators by a low giving up rate.

To incorporate insinuators, we could expand our model to include multiple resources of

differing quality. Discoverers are more likely to discover high-value resources, dominators to

steal them, while insinuators rely on low-quality resources that are not worth the handling

time of dominators and are therefore uncontested. Insinuators are thus characterized by both

non-aggressive behavior, and better yield from low value resources.

The aggressive behavior that we capture as lower β is likely to co-evolve with other

critical parameters (e.g. m, a, τ). Concerted trait combinations seem likely, including traits

not considered by our model. E.g., types may differ in intrinsic fighting abilities, as reflecting

in the death rate of their opponent. Physiological constraints might impose trade-offs, e.g.,

between fighting, reducing vulnerability to interference τ, dispersing a, and persisting at low

resource levels m and e. Incorporating these into adaptive dynamic models (Dieckmann et al.

2006; Leimar 2009) may help understand the evolution of aggression in motile organisms,

and which trade-offs promote or inhibit species coexistence.

CODE AVAILABILITY

Code is available on GitHub:

https://github.com/DanielSmithEcology/R_Star_Interference_Competition

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