Research Article

Inversions Can Accumulate Balanced Sexual Antagonism: Evidence from Simulations and Drosophila *Experiments*

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Abstract

Chromosomal inversion polymorphisms can be common, but the causes of their persistence are often unclear. We

propose a model for the maintenance of inversion polymorphism, which requires that some variants contribute

antagonistically to two phenotypes, one of which has negative frequency-dependent fitness. These conditions

yield a form of frequency-dependent disruptive selection, favoring two predominant haplotypes segregating alleles

that favor opposing antagonistic phenotypes. An inversion associated with one haplotype can reduce the fitness

load incurred by generating recombinant offspring, reinforcing its linkage to the haplotype and enabling both

haplotypes to accumulate more antagonistic variants than expected otherwise. We develop and apply a forward

simulator to examine these dynamics under a tradeoff between survival and male display. These simulations

indeed generate inversion-associated haplotypes with opposing sex-specific fitness effects. Antagonism

strengthens with time, and can ultimately yield karyotypes at surprisingly predictable frequencies, with striking

genotype frequency differences between sexes and between developmental stages. To test whether this model

may contribute to well-studied yet enigmatic inversion polymorphisms in *Drosophila melanogaster*, we track

inversion frequencies in laboratory crosses to test whether they influence male reproductive success or survival.

We find that two of the four tested inversions show significant evidence for the tradeoff examined, with *In(3R)K*

favoring survival and *In(3L)Ok* favoring male reproduction. In line with the apparent sex-specific fitness effects

implied for both of those inversions, *In(3L)Ok* was also found to be less costly to the viability and/or longevity of

males than females, whereas *In(3R)K* was more beneficial to female survival. Based on this work, we expect that

balancing selection on antagonistically pleiotropic traits may provide a significant and underappreciated

contribution to the maintenance of natural inversion polymorphism.

1 Introduction

1.1 The Enigmatic Prevalence of Inversion Polymorphism

Inversions, DNA segments in reversed sequence order relative to the ancestor, have been a focus of population genetic study for their direct or indirect effects on recombination in natural populations for more than a century. In their most dramatic effect on meiosis, inversions generate aneuploid gametes when a crossover occurs between the interior of an inverted region and its non-inverted homolog (White 1973). As aneuploidy is often fatal in embryos or severely deleterious, this may translate to a fecundity cost for a heterokaryotypic parent: a parent heterozygous for an inversion arrangement. However, depending on a species' reproductive biology, such reproductive fitness effects may be mitigated if the zygotes terminate early or before significant parental resource investment (Charlesworth 1994, Munasinghe and Brandvain 2023). Alternatively, crossovers may be inhibited directly in heterokaryotypes around the inversion by mechanisms similar to crossover interference (Koury 2023), avoided by achiasmy in one sex or all, or aneuploid gametes may be segregated to polar bodies in female meiosis (Sturtevant 1921; Sturtevant and Beadle 1936; Krimbas and Powell 1992; Coyne et al. 1993; Gong et al. 2005). Regardless of the differences between these scenarios, effectively fewer recombinant offspring are produced in heterokaryotypes.

Inversions may also have direct effects on fitness when disrupting a gene, a regulatory element, or other genomic structure like a topologically associated domain (Lupiáñez et al. 2015; McBroome et al. 2020). Given that another potential effect of inversions in heterokaryotypic individuals is the deleterious generation of aneuploid gametes, it seems reasonable to expect inversion rearrangements to confer either deleterious or neutral fitness consequences in the absence of association with other variants. However, when a new inversion mutates, it samples a single haplotype from a population, which is likely to have some non-neutral fitness effect, even if mild. Greater natural variation in fitness within a population increases the likelihood of sampling haplotypes with exceptionally deleterious or beneficial associations of alleles, even when there are no other effects on fitness (Berdan et al. 2023).

In contrast to the above predictions, a considerable number of well-studied inversion variants are maintained at an

intermediate frequency within a population, presumably due to the indirect effect inversions have on reducing

recombination and maintaining fit haplotypes that are themselves under selection (reviewed in Berdan et al.

2023). The evolutionary forces maintaining both haplotypes are thought to be quite varied between populations

and arrangements, but a common first hypothesis for a frequently sampled inversion is that local adaptation in one

region or environment is balanced with migration from another (Kirkpatrick and Barton 2006; Charlesworth and

Barton 2018). This association may be maintained more strongly when the alleles have beneficial epistatic

interactions, and assumed beneficial epistasis between loci is often paired with another mechanism of balancing

selection operating at a locus to explain inversion (Dobzhansky 1949, 1950, 1970; Schaeffer et al. 2003; Hoffmann

and Rieseberg 2008). However, unless migration rates are very high, local adaptation models predict inversions to

be at high frequency in their favored geographic range but at low frequency elsewhere, and many inversions do

not have sampled locations at which they reach very high frequency.

Alternately, chance associations of both an inversion and its standard arrangement counterpart with different

recessive deleterious alleles may mimic the fitness profile of a single overdominant locus (sometimes termed

associative overdominance), where heterozygotes carrying both main haplotypes experience none of the

deleterious effects of a homozygous recessive across the region (Sturtevant and Mather 1938; Frydenberg 1963;

Zhao and Charlesworth 2016; Gilbert et al. 2020). However, recent theory and simulation suggests that this

dynamic is uncommon unless an arrangement polymorphism is maintained at intermediate frequency under some

other selective force, and the population scaled recombination rate between arrangements is low (Charlesworth

2024).

Balanced polymorphic loci may be maintained in other ways, under various models and selective pressures. For

example, multiple overdominant loci that are each most beneficial as heterozygotes may benefit from linkage

maintaining complementary haplotypes (Sved 1968; Charlesworth and Charlesworth 1973; Charlesworth 1974).

Several recent studies have proposed that functionally overdominant loci may be more common than previously

considered. Specifically, the dominance relation between alleles at a locus may change between different sexes,

seasons, life history stages, or other trait or fitness challenge contexts, generally termed 'reversal of dominance',

which in some cases can lead heterozygotes to have greatest average fitness (Rose 1982; Wittman et al. 2017;

Grieshop and Arnqvist 2018; Connallon and Chenoweth 2019). Other specific biological dynamics may predict the

maintenance of inversion polymorphism in particular ways. For example, inversions may also link drivers and

enhancers in meiotic drive systems (Babcock and Anderson 1996; Mroczek et al. 2006; Courret et al. 2019), and

these drive-associated inversions may persist at equilibrium frequencies in the presence of repressors (*e.g.* Bastide

et al. 2022).

In natural populations, it can be difficult to distinguish among these alternate hypotheses. They are not always

mutually exclusive, and the selective pressures acting upon an inversion may vary across space and time. The

frequency patterns of many inversions, including a number in *Drosophila melanogaster*, remain poorly explained.

88   1.2 Inversions in *Drosophila melanogaster*

D. melanogaster is a widely studied organism in many fields of biology, including evolutionary and population

genetics. Multiple polymorphic inversions segregate at meaningful frequencies in natural populations of *D.*

melanogaster (Lemeunier and Aulard 1992; Aulard et al. 2002; Kapun et al. 2016; Kapun and Flatt 2019), but even

in this model system, it is not entirely clear which population genetic processes are most responsible for shaping

their frequencies. In this species, achiasmy in males (Morgan 1910; John et al. 2016) and a lack of evidence for

female fecundity costs for most inversions (Sturtevant 1921; Sturtevant and Beadle 1936; Coyne et al. 1993; Gong

et al. 2005) suggest that most paracentric inversions in D. melanogaster do not generate aneuploid gametes at any

appreciable frequency. Further, genome editing tools have allowed for the creation of synthetic inversions,

revealing that the tested structural rearrangements are not themselves responsible for the gene regulatory

changes that are associated with natural inversions in *D. melanogaster* (Said et al. 2018). Instead, given that

breakpoints of common *D. melanogaster* inversions occur disproportionately in regions that confer greater

recombination suppression (Corbett-Detig 2016), *D. melanogaster* inversions would appear to be maintained

primarily for the sake of maintaining linkage associations between distant variants.

D. melanogaster originated in southern-central Africa, in seasonally dry Miombo and Mopane woodlands, and

(potentially after adapting to a human commensal niche) expanded out across much of Africa and into the Middle

East around 13,000 years ago, and into Europe around 1,800 years ago (Sprengelmeyer et al. 2020). With an

ancestral N_e of around 2 million (Sprengelmeyer et al. 2020), *D. melanogaster* populations have high levels of

standing diversity and high population recombination rates. Many *D. melanogaster* inversions have geographic

clines repeated between several colonized regions (Mettler et al. 1977; Reinhardt et al. 2014; Kapun et al. 2016),

and inversions often show geographic differences in frequency that exceed genome-wide average differentiation

between the same populations (*e.g.* Pool et al. 2017). It has therefore been suggested that local ecological

adaptation may shape the distribution of *D. melanogaster* inversions (Kapun et al. 2016; Kapun and Flatt 2019).

Indeed, it is difficult to explain their geographic differentiation without some type of spatially-varying selective

pressures.

Yet, it is unclear whether ecological adaptation is a sufficient explanation for *D. melanogaster* inversion frequency

patterns, for two reasons. First, most of the common inversions become less frequent as one samples populations

farther from the sub-Saharan ancestral range (or similar warm environments) into potentially more challenging,

colder high latitude and altitude environments (Aulard et al. 2002; Kapun et al. 2016; Lack et al. 2016a; Pool et al.

2017; Kapun and Flatt 2019) with *In(3R)Mo* representing an exception to this pattern (Kapun et al. 2014; Kapun et

al. 2016). As these inversions are all derived (being absent from closely related species), local adaptation theory

would predict that they arose to protect local adaptation against ongoing migration, more likely in the novel

environment if it is experiencing high levels of immigration (Kirkpatrick and Barton 2006). It is unclear why

inversions would be needed to adapt to the species' ancestral environments, or why ancestral "standard"

arrangements would have an ecological advantage in derived environments that are very different from the

ancestral range.

Second, even in the locations where inversions would hypothetically be ecologically advantageous, they rarely

surpass intermediate frequencies (Lemeunier and Aulard 1992; Pool et al. 2017; Kapun and Flatt 2019;

Sprengelmeyer et al. 2020). Under a local adaptation model, that observation would require a secondary

explanation that resists fixation, such as very high levels of long distance gene flow or the fixation of recessive

deleterious variants on inverted haplotypes (Ohta and Kimura 1970; Zhao and Charlesworth 2016; Gilbert et al.

2020). While migration may well limit inversion frequencies in some populations, we note that some putatively

adaptive Single Nucleotide Polymorphism (SNP) variants do achieve much greater frequency differentials between

populations (da Silva Ribeiro et al. 2022), and thus we would have to suppose that inversions are under relatively

weaker selection to explain their lesser differentiation. Regarding the hypothesis of high recessive load, we note

that *D. melanogaster* populations do generally contain substantial recessive genetic load (Greenberg and Crow

1960), and it has been speculated that associative overdominance between sampled backgrounds might boost

inversion frequencies in *D. melanogaster* populations during founder events (Pool et al. 2012) or in isolated

wilderness environments (Sprengelmeyer et al. 2020). However, it seems likely that in large human-commensal

populations, *D. melanogaster* inversions would escape from linked deleterious variants through gene conversion or

double crossover events with standard chromosomes, in light of both the age of most of these inversions (Corbett-

Detig and Hartl 2012) and the very high population recombination rates of *D. melanogaster*. Homozygous lines for

each common inversion also appear at appreciable frequency in inbred lab strains, demonstrating a lack of perfect

linkage of the inversions with recessive lethal or infertile variants (*e.g.* Lack et al. 2016a).

While local adaptation, gene flow, and associative overdominance may all contribute to geographic variation in

inversion frequency among *D. melanogaster* populations, it is not clear that these processes are collectively

sufficient to explain observed patterns. Alternatively, the allele frequencies and diversity patterns of at least some

of these inversions might be primarily shaped by some form of balancing selection acting on inversion-linked

variation, in which the balanced frequency is dependent on the environment (Kapun et al. 2023). Balancing

selection on inversions has received increasing attention in recent literature (Wellenreuther and Bernatchez 2018;

Faria et al. 2019). In *Drosophila*, inversions have been associated with balancing selection due to seasonal,

temporally fluctuating selection (Machado et al. 2021). However, the potential for temporally varying selection to

maintain stable balanced polymorphisms on its own is somewhat limited (Gillespie 1988). Further, most common

inversions maintain relatively high polymorphic frequencies across broad geographic ranges without obvious

shared seasonal selective pressures, from tropical and subtropical dry forests to temperate locations with harsh

winter conditions (Lemeunier and Aulard 1992). Therefore, we predict that the frequencies of some of these

inversions could be in part explained by a mechanism of balancing selection that would operate even within a

temporally and spatially homogenous population. Below, we propose such a model in which alleles that contribute

to competitive mating display simultaneously contribute antagonistically to survival to reproductive maturity, a

tradeoff that offers a mechanism by which the life-history characteristics of a population could generate epistatic

balancing selection.

1.3 Sexually Antagonistic Polymorphism in *D. melanogaster*

Among mechanisms of selection, sexual selection is both prevalent, and provides a simple mechanism for

frequency dependence (O'Donald et al. 1997). Alleles that benefit an individual in competitive mate choice

systems often decrease in fitness as the beneficial allele increases in frequency, as display success depends on the

relative quality of a male among local competitors, and the more common a display-enhancing allele is, the fewer

competitors it succeeds over. Albeit, the direction and magnitude of the frequency dependent effect can depend

on the way mate choice is parameterized even among "best of n" models, as well as the strength of selective

versus stochastic effects (O'Donald 1973; O'Donald et al. 1997). Combinations of display-enhancing alleles at

multiple loci may similarly gain a disproportionate benefit together, as male mating success in competitive display

systems can be skewed towards a few successful individuals (Bateman 1948; Jones et al. 2002; Tatarenkov et al.

2008, though see Gowaty et al. 2012; Hoquet et al. 2020). In a mate choice system such as a best of n model in

which a female chooses the highest quality male encountered, a marginally higher quality male similarly

outcompetes either a marginally lower or an exceptionally worse male. So, the last few alleles to push display into

the top quantile should contribute a significantly greater fitness increase to the genotype than the first few display

alleles. This interaction of alleles is a form of epistasis - a non-independent fitness interaction between loci - that is

emergent and non-specific to the genetic identity of the variants. In other words, the alleles contribute

independently to the generation of a trait, and the fitness of the individual is a nonlinear function of that trait

(Blows and Brooks 2003; Rest et al. 2013; Otwinowski et al. 2018). This epistatic interaction suggests a potential for

indirect selection on the recombination-suppressing effects of inversions, in order to maintain combinations of

sexually antagonistic variants that have the greatest fitness when carried together. This tendency of selection to

favor the reduction of recombination when the haplotypes present are at a fitness optimum is well studied for

recombination modifiers including inversions, and has been termed the 'reduction principle' (Feldman 1972;

Feldman and Balkau 1973; Feldman et al. 1980; Altenberg and Feldman 1987; Altenberg et al. 2017; see Altenberg

and Feldman 1987 for a direct treatment of inversions).

While the emergent epistasis generated by a mate choice system may favor linkage of variants, alleles that

contribute only to a sexually selected display are not expected to remain as balanced polymorphisms, rather they

are expected to fix, albeit perhaps slowly as their fitness benefits diminish at high frequencies (Hazel 1943;

Dickerson 1955; Charlesworth and Hughes 2000). However, if these alleles simultaneously contribute deleteriously

to other components of fitness, they are pleiotropic (Stearns 2010), and given the sex-limited benefits of the

display they would likely also be sexually antagonistic (Rowe et al. 2018), whereby traits increase the fitness of one

sex but decrease fitness if found in the other. Pleiotropy can result from traits that are inherently physiologically

coupled, from resource allocation restraints, or from the specific role or behavior of genes. Pleiotropy can further

be sexually antagonistic when the traits in the tradeoff are differentially important to different sexes, which may

be common given the differing fitness requirements of the sexes in a population (Cox and Calsbeek 2009;

Connallon and Clark 2014; Connallon and Chenoweth 2019). It should be noted that a model of two pleiotropically

determined traits each with potentially sex-specific fitness can be treated separately from a model where one trait

has sexually antagonistic fitness effects.

D. melanogaster mating involves a male display performance and female acceptance or rejection. A number of

experimental evolution studies (Rice 1992; Rice 1996; Audet et al. 2024) and genetic studies (Innocenti and

Morrow 2010; Cheng and Kirkpatrick 2016; Glaser-Schmitt et al. 2023) have confirmed the prevalence of sexually

antagonistic loci in *D. melanogaster*. Pleiotropic alleles that trade off between survival and male display quality

represent one clear potential case of antagonism to consider for a model of balancing selection, and one highly

relevant to the biology of *D. melanogaster*. Many such antagonistically pleiotropic scenarios are possible under

different selective tradeoffs, and indeed some have been proposed for other model inversions with varying

mechanisms of maintenance (Betrán et al. 1998; Pearse et al. 2019; Mérot et al. 2020; Pei et al. 2023; see

Discussion), but we focus on a specific scenario of sexual antagonism here.

Given the relevance of sexual selection and sexual antagonism to *Drosophila* evolution, we propose that

polymorphic *D. melanogaster* inversion and standard arrangements may help maintain haplotypes of alleles that

specify opposite ends of a sexually antagonistic tradeoff that is subject to balancing selection and for which

intermediate states are inherently disfavored. We first explore this model through forward simulation, to establish

that it may in theory arise in a population and maintain inversion polymorphism over a significant number of

generations. Then we examine the results of an experiment with an outbred laboratory population of *D.*

melanogaster, to test whether common inversions show changes in frequency over the course of a generation in a

manner consistent with a trade-off between survival and male reproductive success.

2 Results

2.1 A Model of Sexually Antagonistic Inversions

Here, we consider a population featuring a competitive mate choice system that results in a skewed distribution of

reproductive success among males. Within this population, we model a genomic region containing a number of

linked loci, each with alternate antagonistic, pleiotropic alleles that trade off between male display success and

survival likelihood (of either or both sexes). Critically, we do not directly model any epistatic interactions among

loci affecting survival or display traits, nor do we invoke dominance in our diploid model, so any such fitness

dynamics emerge from the modeled population processes.

If mate choice is highly competitive, such that each female can choose amongst several or many males, the

variance of offspring number among males (Figure 1A) may be much higher than for females - yielding a

distribution of male reproductive output that follows a relatively convex trend, in which most males produce few

offspring. Conversely, superior display quality can enable males to mate successfully much more often than other

display phenotypes they compete against (Figure 1A). An increase in the display of a male with low quality results

in a smaller change in number of offspring than an increase in display of a male with high quality (change ii in

Figure 1A), due to the reproductive skew towards highly competitive individuals. So, there is an emergent non-

additive fitness effect, where multiple variants increasing the reproductive rank of an individual together have a

larger fitness benefit than the combined effects of each substitution separately - a positive, synergistic epistatic

effect. This effect occurs whether the difference is from substituting alleles at two loci, or from substituting two

homologous alleles at a single locus in a diploid or polyploid organism, which would give an emergent dominance

effect. Additionally, fitness conveyed by an allele favoring display quality is also frequency-dependent: since

mating success depends on the frequency of comparable display qualities of other males in a best of n model, the

relative advantage of a display trait can diminish as more males carry it, for both haploid and diploid populations

(Figure 1B, male fitnesses; O'Donald 1973; O'Donald et al. 1997). If a variant only conveys benefit to mate

competition success, it is expected to fix given enough time, as even if its evolution is nearly neutral at high

population frequency, selection will push the frequency back up if it drifts down. Whereas, if the variant is

antagonistically pleiotropic for a trait not involved in competition between males, such as survival in the face of

climate, pathogens, or predators, these fitness costs may typically not be frequency dependent. If the benefit of an

antagonistic display-favoring allele overcomes the pleiotropic cost when the variant is rare, its diminished benefit

when at higher frequency may reverse its net benefit, while at some intermediate frequency, we predict that these

fitness effects should be equal and an equilibrium frequency should be reached and maintained (Figure 1B). In the

absence of other forces, this dynamic is expected to maintain the allele under balancing selection indefinitely. We

note that this dynamic can be described as a "negative frequency dependence" of the fitness component for mate

choice alone, as the selection coefficient of the favored allele may decrease towards zero while remaining positive,

though some authors instead use negative frequency dependence to specifically describe fitness functions in which

all alternate alleles are of selective benefit when rare (*e.g.* Charlesworth and Charlesworth 2010). In addition to

the relationship between sex averaged fitness and frequency, the contrasting sex-specific fitnesses of antagonistic

alleles under this model could further enhance the potential for balanced polymorphism.

We further predict that multiple such balanced pleiotropic loci should generate interesting emergent behavior.

Because of the emergent synergistic epistasis from mate competition (see discussion of Figure 1A above), the

haplotype with the greatest male display benefit should increase in frequency relative to other haplotypes until

reaching an equilibrium at which its relative advantage in mate choice is reduced enough to be balanced by the

pleiotropic, frequency-independent, non-epistatic survival cost (Figure 1B). The haplotypes and their linked alleles

conveying intermediate phenotypes will have less than proportional benefits during mate choice due to the convex

relationship between quality and success described above (Figure 1A), but a larger, proportional cost to survival

against non-intraspecific survival challenges, giving them lower average fitness in the equilibrium state than either

of the extreme haplotypes (Figure 1C). Therefore, recombination between the two extreme haplotypes will

generate less fit haplotypes in the gametes, and a local modifier of recombination that reduces recombination and

its associated costs (such as an inversion) will be favored by indirect selection (Altenberg and Feldman 1987; Otto

and Lenormand 2002). And so, selection will favor the association of these haplotypes with the alternate standard

and inverted karyotypes, which generate fewer recombinant gametes from a heterokaryotypic parent. We further

predict that in a population that is close to the balanced equilibrium state for such a pleiotropic trade-off, the

population of adults will contain a higher frequency of survival-focused haplotypes than the population of zygotes,

but the display-focused haplotypes will increase in frequency in zygotes relative to adults, in line with the life

stage-specific fitness differences between these haplotypes.

[Figure 1: Conceptual representations of the proposed model of inversion-associated balanced sexual antagonism.

(A) Hypothetical skewed distribution of male mating success, yielding a greater variance in reproductive success for

males than for females, such as expected under a "best of n" mate choice model. (B) Fitnesses of display-favoring

alleles under sexually antagonistic balancing selection, illustrating a pleiotropic variant that should rise in

frequency when rare, but decline if frequency exceeds the balanced equilibrium value. (C) Fitnesses of display-

favoring alleles at two haploid loci under the same model, illustrating synergistic epistasis between displaying-

favoring alleles. (D) A hypothetical trajectory of four such mutations, in which B outcompetes A, an inversion links

B and C to create a more strongly display-favoring haplotype, and then the addition of D to that haplotype furthers

the accumulation of antagonistic variants, reaching an equilibrium frequency while displacing less extreme display-

favoring haplotypes.]

While Figure 1 illustrates a haploid scenario for the sake of simplicity, this model extends naturally to a diploid

case. The main difference is that heterokaryotypic diploids – those heterozygous for the arrangement – would

have intermediate trait values and be less fit than either homokaryotype, for the same selective reasons that an

intermediate haplotype with two alleles of opposing effects at different loci is least fit in a haploid context. This is

therefore, interestingly, an example of a scenario in which the two most common haplotypes in the population can

exhibit underdominant fitness, and yet may still be maintained at a stable balanced equilibrium. By comparison,

the simplest models of underdominant fitness predict an unstable equilibrium that disfavors polymorphism

(Gillespie 2004, Charlesworth and Charlesworth 2010), a characteristic shared with non-frequency-dependent

models of disruptive selection. The cost of generating underdominant offspring might be compensated for by a

strong co-directional dominance of the variants involved, such that heterokaryotypic individuals exhibit a

phenotype similar to one of the homokaryotypes. However, dominance is not a necessary feature of our model,

and it is not invoked in our simulations. Whereas, investigating a wider range of genetic architectures would be a

potential direction for future study.

2.2 Simulation Results

[**Figure 2:** The layout of a single simulated generation. Simulated individuals each reach the reproductive stage

with probability in proportion to the product of the survival effects of their alleles. To generate each offspring in

the next generation, a surviving female is first randomly sampled (with replacement) to be the mother. Then a

specified number of surviving males are randomly sampled to generate the pool of males encountered by the

sampled female for the best of n mate choice - without replacement for each pool and with replacement between

pools. Unless otherwise noted, we defaulted to 100 encountered males in simulations presented here. For each

encounter pool, each male is assigned an observed display quality as the sum of the display effects of its alleles,

plus a normally distributed noise effect for each encounter. The highest quality male in the encounter pool is

selected as the father, and the offspring genome is generated. The female gamete is generated with crossover and

gene conversion events. Odd numbers of crossovers in the interior of an inversion are resampled from the same

parent, to model the biology of an organism that eliminates aneuploid gametes during oogenesis or exhibits

reproductive compensation. *D. melanogaster* males do not cross-over, and so males do not recombine in the

simulations presented.]

[**Figure 3**: Simulations show that a balanced equilibrium frequency exists for certain sexually antagonistic variants.

The proportion of simulations retaining polymorphism (top) and the average final frequency (bottom) are plotted

for a single locus at which there is one antagonistic allele with the indicated effects reducing survival proportion (of

both sexes) and increasing male reproductive quality score, initiated at equal frequency with an alternative allele

that has no such effects. Larger values of both effect sizes are plotted in the left panels, with values incrementing

by 0.025, and smaller effect sizes (a subset of the larger) are plotted in greater detail in the right panels, with

values incrementing by 0.005. Reproductive quality contributes to male success in a best of 100 mate competition

with an added normally distributed noise effect of standard deviation 1 (Figure 2; Materials and Methods). See

Figure S1 for plots with sex-specific costs and differing encounter numbers in the best of n mate competition. Most

parameters result in either all simulations retaining polymorphism (purple), or else all simulations losing

polymorphism (white). However, simulations retaining polymorphism have a broad range of equilibrium

frequencies (shades of green). For each parameter combination, 500 replicates were simulated for a diploid

population of 1,000 individuals evolving for 20,000 generations, with further details as indicated in the Materials

and Methods.]

We investigated the predictions of the above model of inversion-associated balanced sexual antagonism using a

purpose-built forward simulation program, "Sexually Antagonistic Inversion simulator" (SAIsim; see Materials and

Methods). This simulation program incorporates the generation of new nucleotide and inversion polymorphisms

by mutation, where each nucleotide mutation independently draws a positive or negative effect on survival and on

male display. It also simulates crossing over and gene conversion, and inherently the effects of drift (Materials and

Methods). SAIsim includes gene conversion between all homologous sites regardless of karyotype, and models

crossing over in heterokaryotypic individuals from even numbers of crossover events within the inverted region. It

explicitly models mate selection, in that for each female selected to reproduce, a set number of 'encountered'

males are randomly selected, and the observed display value of each male for this competitive event is assigned

based on the sum of the male's genetic effects and a noise effect resampled at every encounter. The male with the

highest observed display value then succeeds in this mating (Figure 2).

With this simulator, we first confirmed that some individual variants with an antagonistic pleiotropy between

survival (initially of both sexes) and male reproduction can generate stable selectively balanced polymorphisms *in*

silico. We simulated a single locus in diploid populations of N = 1000, polymorphic for an allele of a specified

survival cost and display benefit at an initial frequency of 0.5, with the alternate allele having no trait effect. For

each female's mating competition, 100 males were sampled, though see Figure S1 for plots with varying encounter

number. After 20N generations, we calculated the proportion of simulations retaining polymorphism and the

average final frequency of the variant across all simulations, revealing that there is a range of paired trait effects

for which the mutation consistently remained polymorphic, with intermediate mean frequency, after 20N

generations (Figure 3) – implying the action of balancing selection. Alleles with small effect sizes had only a narrow

band of selective maintenance, outside of which they were either fixed or lost, while large-effect alleles remained

balanced across a larger area of simulated parameter space. While the overall balanced range is somewhat

narrow, such variants may persist under balancing selection indefinitely in the absence of other forces, and many

small-effect alleles in linkage blocks may confer larger effects in synergy. In a scenario where only females pay the

survival cost, the balanced parameter space of antagonistic trait effects is broader and shifted somewhat (Figure

S1). In a scenario where only males pay the survival cost, and variants are neutral in females, essentially no

simulations retain polymorphism (Figure S1). The number of males sampled to assess mate competition for each

offspring also has a significant effect, with larger values giving broader polymorphic ranges, though simulations

with costs only in females show robust polymorphism even when only sampling two males for each competition

(Figure S1).

We then tested the behavior of two linked loci, both polymorphic for an antagonistic and non-antagonistic allele.

We identified two antagonistic variants previously found to undergo balancing selection separately, and performed

simulations with varying genetic distances between them (Figure 4). Crossing over and gene conversion were

simulated, with gene conversion occurring for each heterozygous variant at a probability of 10^{-2} per female meiosis

per site, with random direction. This behavior was intended to be a conservative approximation of the number of

gene conversion events affecting a given site in *D. melanogaster*, scaled to simulations of N=1000 (Comeron et al.

2012). The stronger antagonistic variant (modelled at fixed position 0.225M) persisted in all simulations, in line

with expectations, and so we focus on whether the weaker variant (at varying positions) also persisted with it. As

seen in the upper panel of Figure 4, the weaker variant (pale red line) was retained at close linkage, as the

haplotype containing both antagonistic variants acts as a single larger effect supergene. The haplotypes with

intermediate trait values were less fit, leaving less offspring per haplotype across simulations (Figure S2A), whereas

the extreme haplotypes were maintained at much higher frequency (Figure S2B), generating linkage disequilibrium

between display-favoring variants (r^2=0.2139 across simulations in which the smaller effect variant was positioned

at 0.250M). This demonstrates the synergistic epistasis proposed in our verbal model. The maintenance of

haplotypes AB and ab under selection while Ab and aB are selectively removed relies on the lesser relative fitness

of Ab and aB. And since survival values are multiplicative, this additional contribution must come from the mate

success of AB being disproportionately larger than Ab or aB. As the weaker variant was then moved farther from

the stronger variant, recombination increasingly generated unfit intermediate genotypes compared to the

extremes of the reproduction-survival tradeoff, and the stronger variant outcompeted the weaker variant among

these haplotypes despite the epistatic benefit from associating the two variants together, leading to the loss of the

weaker variant. In the scenario examined by Figure S2, the differences among haplotypes in sex-averaged fitness

are modest, whereas the sex-specific fitness effects are more dramatic. These results could indicate that in

addition to the frequency-dependent dynamics proposed above, the contrasting fitness effects in females and

males may also play an important role in maintaining balanced polymorphism, particularly when near frequency-

dependent balance (Connallon and Clark 2014; Kaufmann et al. 2023).

We then examined the same spacings between antagonistic variants across a region containing a polymorphic

inversion, with its left breakpoint close to the stronger variant, and the right breakpoint within the range of the

positions in which the weaker variant was simulated (Figure 4, lower panel). When the inversion was added, the

weaker variant was then retained when the two antagonistic variants were relatively more distant, due to

association of the weaker variant with the right-hand inversion breakpoint (pale red line), at which point this

association also preserved the inversion itself in a polymorphic state (light blue line). While less predictable, a

weaker antagonistic variant near the middle of the inversion also appeared to maintain polymorphism more

frequently in systems starting with an inversion than without, i.e. across approximate positions 0.30-0.45M in

Figure 4, in spite of its weaker linkage with the inversion itself due to double cross-over events. The inversion was

not maintained when the weaker antagonistic variant was within the inversion but tightly linked to the stronger

variant (see positions 0.22-0.25M); here there is little crossing-over for an inversion to suppress, and so the effect

of the inversion approaches neutrality. Interestingly, there was a small window of weaker variant position in which

the inversion remained polymorphic despite the already tight linkage between SA variants, where the inversion

seemingly does not modify recombination much (see positions 0.2-0.22M). Here, the weaker antagonistic variant is

more tightly linked to the breakpoint than to the stronger variant in this range, and presumably benefits more

consistently from the crossover reduction. The maintenance of the weaker variant drops more rapidly outside of

the inversion than over similar distances in the simulation without inversions (positions 0-0.2M, bottom versus top

panel). This seemingly counter-intuitive result may stem from crossover events that result in aneuploid gametes

being resampled in our simulations, which effectively increases the crossover rate outside the inversion

breakpoints, a behavior which should be biologically reasonable in taxa with aneuploid chromosome elimination or

reproductive compensation. So, for a weaker variant outside the left inversion breakpoint, the presence of the

inversion can increase the crossover rate between the two antagonistic variants, and thus reduce the probability of

the weaker variant surviving by retaining linkage to the stronger one.

[Figure 4: Simulated inversions may persist as polymorphisms when linked to sexually antagonistic, pleiotropic

variants. In turn, the presence of inversions facilitates the accumulation of antagonistic variation, demonstrating

synergistic epistasis. Rates of long-term persistence are shown for simulations with two defined antagonistic

variants alone (left panels) and with the additional presence of a defined inversion (right panels). To focus the

potential addition of a second linked variant to an antagonistic haplotype, we begin with the stronger variant

already at an intermediate frequency in the population (0.5). The weaker antagonistic variant and the inversion

either both start at 0.5 frequency as well (upper row) or both start at a lower frequency of 0.05 (lower row), with

all variants initially in linkage equilibrium. The 1 Morgan chromosomal segment is diagrammed above the plots,

with the inversion breakpoints marked (0.21M, 0.55M), chosen to include space across and beyond the inverted

region. The proportion of simulations in which the second, variably positioned weaker antagonistic variant

(survival and reproductive values 0.86, 0.12) maintains polymorphism is shown (light red line), dependent on the

recombination distance from a stronger allele (0.75, 0.3) at fixed position 0.225M, which always persists (dark red

line at 1 across the top of each plot). In the right panels, the proportion of replicates in which the inversion is

retained is also plotted (blue line). Values for each parameter combination were averaged over 1000 replicate

simulations, for populations of 1000 diploid individuals run for 20N generations. Gene conversion occurs for each

heterozygous variant at a probability of 10^{-2} per female meiosis with random direction. Crossover arrangements

generating aneuploidy, where there are an odd number of crossovers within the inverted region of a

heterokaryotypic parent, are resampled from the same parent to represent removal to polar bodies or

reproductive compensation.]

[**Figure 5**: Simulated populations with stochastic mutation of new inversions and sexually antagonistic variants

generate persistent inversion polymorphisms and accumulate linked sexually antagonistic variants. (A) In simulated

populations with stochastic mutation of new variants having pleiotropic effects on survival and male display, levels

of antagonism increased with time before stabilizing at an intermediate value (left panel). Whereas, simulations

which also allowed the mutation of new inversions continued accumulating stronger antagonism throughout the

simulated time interval (right panel). (B) In simulations which allowed the mutation of new inversions, a low

crossover rate (left panel, 43.6 cM in females after scaling) allowed populations to accumulate larger differences

between the most common karyotype and all others than when the rate of crossover was particularly high (right

panel, 43.6 M in females after scaling). Gene conversion occurs at each heterozygous variant with a scaled

probability of 0.1295 per heterozygous variant in both scenarios. Values given are the mean of 1000 replicate

simulations of 1000 diploid individuals run for 20N generations.]

In further simulations, we began with a population initially free of variation, in which sexually antagonistic

mutations arise stochastically. To assess differences between longer or shorter antagonistic regions, or higher or

lower crossover rates, we modeled populations with parameters scaled to either 1 Mb or 10 kb, using estimates

from Comeron et al. (2012) and Huang et al. (2016). The mutations had pleiotropic effects increasing reproductive

quality score and decreasing survival proportion, each drawn sampled independently (Materials and Methods).

Depending on the effect scores drawn, a mutation could be broadly advantageous (potentially leading to a

selective sweep), broadly deleterious, or potentially subject to balancing selection (Figure 3, Figure S1). These

mutations arose at a rate equal to one thousandth of the scaled single nucleotide mutation rate given in Huang et

al. (2016). Inversions (of random lengths and positions) also arose stochastically, at a hundredth of the rate of

antagonistic variants. The frequency trajectories of antagonistic variants and inversions were tracked, and the

simulation was run for 20N generations to allow near-equilibrium patterns to be established. These simulations

demonstrated the potential of a population without initial genetic variation to establish alternate karyotypes

which link sexually antagonistic, pleiotropic alleles and an inversion, to maintain polymorphism in a balanced

manner, and then to subsequently accumulate significant antagonistic character (Figure 5A), although the degree

of antagonism accumulated depends strongly on the rate of crossing over (relative to the occurrence of

antagonistic mutations; Figure 5B).

The simulations that successfully maintained balanced antagonistic chromosomes also had an interesting

distribution of allele and genotype frequencies of the balanced haplotypes at equilibrium. Without any selection,

the inversion frequencies followed a pattern characteristic of the expected neutral site frequency spectrum (Figure

S3). But strikingly, in parameter spaces where simulations with shared survival costs between sexes maintained

polymorphism under balancing selection, inversion frequency distributions were tightly clustered around 0.25 and

0.75 among the zygote population (Figure S3, 6A). We found that this outcome was related to the genotype

frequencies of reproducing adults. These simulations evolve toward strong antagonism, and it is predominantly

males homozygous for the display-favoring haplotype (whether that is inverted or standard) who succeed in

reproducing, and these males therefore contribute one copy of the display-favoring haplotype to each of their

male and female offspring. However, this haplotype's significant cost to viability and longevity would select for the

heterokaryotypic females over the display-favoring homokaryotypes. Given that successful parents would

predominantly be heterokaryotypic females and display-favoring homokaryotypic males, around three quarters of

transmitted chromosomes have the display-favoring arrangement and one quarter does not, yielding the 0.25 and

0.75 zygote inversion frequencies seen in simulations. Although these are autosomal simulations, selection yields

an inheritance pattern similar to that of a ZW sex chromosome system, where the Z chromosome is

homokaryotypic in the fathers, and heterokaryotypic with the W chromosome in the mothers.

The sex-specific fitness dynamics present at equilibrium under this model also resulted in population-wide

genotype frequencies that depart from standard Hardy-Weinberg expectations. If the preponderance of matings

are between heterokaryotypic females and homokaryotypic display-favoring males, then homokaryotypes for the

survival-focused haplotype will rarely be produced (as confirmed in Figure 6B). We note that in cases where the

standard arrangement favors male display, then especially if antagonism is strong, this model could explain an

observed deficiency or absence of inversion homokaryotypes, even if the inverted arrangement was not associated

with any recessive deleterious load. Further, heterokaryotypes may become disproportionately frequent after

viability selection (Figure 6B). And still, this enrichment for heterokaryotypes reflects neither the existence of

recessive deleterious load associated with each arrangement, nor overdominance with respect to viability. Hence,

our model may offer an alternative explanation for deviations from Hardy-Weinberg genotype frequencies

observed for polymorphic inversions in natural populations.

[**Figure 6:** Antagonism-associated karyotypes reach predictable equilibrium frequencies in simulations with

antagonistic and inversion mutations, when survival costs are shared between sexes. (A) Histograms of the number

of karyotypic arrangements at a specified frequency across all simulation replicates in females (left) and males

(right), colored by how the average survival effect of that arrangement ranks compared to the others in its

population. Ranks are normalized to be relative to the median arrangement value, to better account for rare

arrangements and ties. These simulations reach an equilibrium with two predominant arrangements, with the

more survival-focused arrangement around an overall frequency of 0.25 and more common in females, and the

more male-competition-focused arrangement around a frequency of 0.75 and more common in males. (B) Because

successful males tend to be homozygotes and successful females heterozygotes, the less frequent of the two

major arrangements (which tends to favor survival) has homokaryotype frequencies far below the Hardy-Weinberg

expectation, and there is an excess of heterokaryotypes. These genotype frequencies shift between zygote (left

panel) and adult (right panel) populations as the genotype affects survival.]

We further ran simulations in which the survival costs were not shared, but instead specific to females,

representing a distinct, stronger form of sexual antagonism. In these simulations, we surprisingly recovered three

different equilibrium arrangement states (Figure 7). In 20.0% of simulations, we observed a state similar to the

shared costs simulations presented in Figure 6, where we infer that fathers were homokaryotypic for a display-

favoring arrangement, and mothers were heterokaryotypic and carried survival-focused arrangement that is

observed in surviving but not reproducing males. For 37.0% of simulations, there were again two predominant

arrangements, but with transmission patterns similar to an XY sex chromosome system rather than a ZW sex

chromosome system. In these cases, we infer that the mothers were homokaryotypic for an X-like survival-focused

arrangement, but the fathers were heterokaryotypic and carried a Y-like display-focused arrangement that was

apparently lethal in females. In 40.6% of simulations, we instead detected three intermediate frequency

haplotypes: with both Y-like and W-like arrangements restricted to reproducing fathers and mothers respectively,

and a third shared arrangement with intermediate phenotypic effects (Figure 7).

Specific properties of our simulations may have influenced the occurrence of these three stable states under the

female-limited cost model. To reduce the computational complexity of both crossovers and arrangement-specific

trait values, the simulations do not allow two inversions on the same individual chromosome, whether overlapping

or not, though two chromosomes sampled from the population may have distinct inversions with overlapping

breakpoints. This means that if two arrangements, each with an inversion, become the prevalent haplotypes and

thereby remove all standard arrangement chromosomes from the population, there is no mutational path to

generate a third arrangement. However, a portion of the two-state simulations still had the ancestral, non-inverted

arrangement as one of the two haplotypes present, which could have been mutated to a third arrangement to

establish the three-arrangement pattern. We are not sure which selective or mutational barriers may prevent

transitioning between each state once established. One clear barrier is that it is difficult to generate a less extreme

arrangement from a Y-like arrangement, as these can accumulate an indefinite number of mutations since males

experience no costs in this set of simulations.

[**Figure 7:** In simulations with female-limited survival costs, three distinct outcomes are observed involving either

two or three balanced haplotypes. From simulations with randomly occurring antagonistic and inversion

mutations, histograms of inversion frequencies across simulations for surviving females (left) and males (right) are

partitioned into three categories based on sex-specific haplotype frequency outcomes. The "Favors Female"

category (top) includes simulations in which there are exactly two arrangements with frequencies between 0.1 and

0.9 in both sexes (20.0% of replicates). The "Male-Specific" category (middle) includes simulations in which there

are two arrangements with whole-population frequencies between 0.1 and 0.9, but one arrangement is absent in

adult females (37.0% of replicates). The "Three Arrangement" category (bottom) includes simulations in which

there are exactly three arrangements with whole-population frequencies between 0.1 and 0.9 frequency (40.6% of

replicates). 2.3% of simulations did not fit in these categories and had only one predominant arrangement. As in

Figure 6, inversions are colored by how the average survival effect of that arrangement ranks compared to the

others in its population, and ranks are normalized to be relative to the median arrangement value, to better

account for rare arrangements and ties.]

534 2.3 Empirical tests for inversion-associated tradeoffs

A specific motivation for developing and evaluating the model of inversion-associated, balanced sexual antagonism

was to potentially better explain the pattern of inversion frequencies observed in *D. melanogaster*, in which

multiple inversions reach some of their highest frequencies in populations from the ancestral range or with

similarly tropical/subtropical climates. We therefore set out to test experimentally whether any of four inversions

common in a Zambia population of this species show evidence for tradeoffs between male reproductive success

and survival (in terms of viability and/or longevity).

[**Figure 8:** The layout and potential expectations of the laboratory evolution experiment. We cross outbred males

from a high-inversion population to inbred, non-inverted females from a specific inbred line, and collect DNA

samples from the fathers, embryo offspring, and aged adult offspring for inversion frequency estimation via

sequencing (left). We hypothesize from our antagonistic pleiotropy model that one or more of the four inversions

present on separate chromosome arms in our experimental populations may experience opposing selection

between fathers and embryos versus between embryos and aged adults (middle). To test the significance of

observed frequency changes, we designed a resampling model to represent the sources of neutral variation

expected in the experiment (right).]

We assembled an outbred population with moderate frequencies of each inversion to obtain karyotypically diverse

males. We set up four crosses using these males along with females from one of four different inversion-free

inbred Zambia lines (Figure 8). Each of these parental crosses occurred in a single large population cage, with

populations of at least 600 and equal numbers of each sex (Table S1). We developed a PCR and next-generation

sequencing-based assay to estimate inversion-associated SNP frequencies in each pool of males and in each

corresponding pool of embryos. These SNPs (given in Table S2) were based on our own analysis of variants that

showed perfect association with inversions among 197 Zambia genomes (Table S3; see Materials and Methods).

We then implemented a resampling method to test for significant inversion frequency changes between parents

and offspring (while accounting for the variance observed in technical replicates; see Materials and Methods), in

order to determine whether males carrying each inversion were more or less successful in reproducing than the

average male. We also compared frequencies between embryos and aged adults collected 10 weeks after eclosion,

to investigate the relationship between inversions and viability/longevity. These aged adults eclosed either in the

first or second half of the collection period from the same batch of eggs, thus allowing us to test for inversion

associations with development time. We calculated p-values from the resampling tests to assess the significance of

each individual change in inversion frequency between relevant samples (Table S4). However, in accord with our

primary question regarding fitness tradeoffs, we primarily focus here on joint tests of two opposing frequency

changes, as further described below. We could therefore test the hypothesis that a given inversion had opposing

influences on survival and male reproduction, which would provide evidence consistent with our model of

balanced sexual antagonism, while also examining whether any such tradeoffs depend on maternal genetic

background.

When we initially examined the joint effects of male reproduction and survival, we found that in a majority of

cases (in 13 out of 16 inversion-line trials; binomial P = 0.02; Figure 9), a given inversion increased in frequency in

aged adult offspring compared to the null expectation based on the frequency in fathers. The remaining three

cases were all for *In(3L)Ok*. Ten of the 13 increases were primarily due to increase in frequency between embryo

and aged adult samples, suggesting that in terms of viability and/or longevity, inversion heterokaryotypes often

had higher fitness than standard homokaryotypes (no offspring were homokaryotypic for an inversion under our

crossing design). We note that even standard homokaryotypes among the fathers and offspring should not have

broad-scale homozygosity within the inverted region, but should instead be heterozygous for unique standard-

arrangement haplotypes from two independent Zambia strains, and that long genomic tracts of identity-by-

descent between Zambia strains are quite rare in this large, ancestral-range population (Lack et al. 2016a). Hence,

we do not expect that inversion heterokaryotypy is buffering against deleterious effects of inbreeding. Instead, this

fitness advantage suggests either an advantage for heterokaryotypy in particular, or perhaps more likely, that

multiple inversions harbor alleles that benefit survival or longevity under our experimental conditions (see

Discussion).

A Testing for tradeoffs between male reproduction and survival

B Inversions convey some sex-specific survival effects

[**Figure 9**: Some *Drosophila* inversions show evidence for antagonistic tradeoffs and sex-specific survival. (A)

Testing for antagonistic fitness effects on reproduction and survival (encompassing viability and longevity). Each

inversion's frequency in parents after collection (2 to 3 weeks from eclosion), embryo offspring, and aged adult

offspring (10 weeks from eclosion) are shown for each maternal inbred line. Parental frequency is represented

instead of paternal frequency for easier visual comparison, and is taken as the paternal frequency divided by two

to account for the inversion-free inbred mothers. Adult offspring frequencies are taken from the sum of estimated

allele counts across all adult offspring cohorts. * indicates p-value < 0.05 for evidence of significant reversed

frequency change from parental to embryo and from embryo to offspring, combined across all four maternal line

crosses and corrected for multiple tests, when compared to neutral simulated experiments (details in Materials

and Methods). (B) Testing for evidence of sex-specific survival effects. The changes in inversion frequencies

between embryos and the aged adult offspring are again illustrated, now separated by their sex. * indicates p-

value < 0.05 for significant differences in female versus male inversion frequency among adult offspring, combined

across all four maternal crosses and corrected for multiple tests.]

When we separated the effects of male reproduction (based on father to embryo changes) and survival (embryos

versus adults), we found that the effects of inversions on survival were generally consistent across maternal

genotypes. Three inversions were associated with increased survival to 10 weeks: *In(3R)K* was in all four crosses,

while *In(2L)t* and *In(2R)NS* each showed elevated survival with all maternal strains except ZI418N (Figure 9A). In

contrast, *In(3L)Ok* was associated with lower survival in each cross (Figure 9A). With regard to male reproduction,

the trajectory of inversion frequencies from fathers to embryos to offspring was less consistent between different

crosses (Figure 9A), implying that differences in male reproductive success may be dependent on the maternal

genotype, which is consistent with past findings in *D. melanogaster* (Reinhart et al. 2015). Despite such variability,

each of the four inversions had multiple frequency changes that departed strongly from null expectations (Figure

9A; Table S4), as might be expected if selection was present but varied in strength and direction between crosses

and life stages.

To test our central hypothesis of a tradeoff between male reproductive success and cumulative survival during

development and adult aging, we used neutral resampling to test the likelihood of observing the magnitudes of

opposing inversion frequency changes (between fathers and embryos, and between embryos and aged adult

offspring) under the null hypothesis, integrating across the four maternal crosses and accounting for multiple test

correction (Materials and Methods). For *In(3R)K*, which had particularly consistent changes in frequency across

replicate lines (decreasing between parents and embryos, and then increasing between embryos and aged

offspring; Figure 9A), this frequency reversal was significantly non-random ($p = 2.70 \times 10^{-3}$; Table S5). In contrast to

In(3R)K, *In(3L)Ok* was associated with (variably) higher male reproductive success and (consistently) lower survival;

this reversal was also statistically significant ($p = 2.97 \times 10^{-7}$).

We also tested for frequency differences between aged adult offspring of different sexes and from early-eclosing

versus late-eclosing cohorts. All four inversions displayed differences in frequency between female versus male

offspring (Figure 9B), consistent with differential effects on sex-specific survival. Strikingly, *In(3L)Ok* and *In(3R)K*

each displayed sex survival differences in alignment with their antagonistic effects implied above: *In(3L)Ok* (which

favored male reproduction) reduced female survival more strongly than male survival ($p = 0.0450$), whereas

In(3R)K (associated with lower male reproduction) favored the survival of females more than it did males ($p = 4.61$

$\times 10^{-3}$; Table S5; see Materials and Methods). The other two inversions, *In(2L)t* and *In(2R)NS*, each consistently

favored female over male survival in all four maternal crosses, although their raw unidirectional cross-combined *p*

values (0.0260 and 0.0126) were not significant after multiple test correction ($p = 0.282$ and 0.137). In contrast, we

found no consistent differences in inversion frequency between early- and late-eclosing offspring (Figure S4).

Estimated selection coefficients for each tested change based on a Wright-Fisher population approximation are

available in Table S6; however these may overestimate inversion fitness effects since the survival terms reflect the

probability of reaching advanced age. Further, there may be an influence of differential sex-specific mortality

during aging leading to greater frequency shifts in females. We collected a total of 1960 females and 3156 males,

and if the survivors represent 20% of an original population with an equal sex ratio, then there was 84.7% female

mortality and 75.3% male mortality. Additionally, there was some mortality among the parents over the laying

period, so some of the frequency change observed in embryos may be attributable to paternal mortality. Paternal

mortality was at most 15% among the crosses (Table S1), and the fathers were at most three weeks old, suggesting

mild effects on inversion frequency estimation. Further, any positive correlation between the paternal and

offspring survival effects of an inversion would bias against detecting the tradeoffs implied above. Overall, we

conclude that *D. melanogaster* inversions have distinct and often context-dependent influences on male

reproduction and on survival, with some evidence for antagonistic tradeoffs of the sort proposed in our model.

3 Discussion

Here, we have introduced a new conceptual model in which (1) sexually antagonistic variation is present and

subject to balancing selection that maintains extreme genotypes favoring either male reproduction or survival, and

(2) inversions are predicted to facilitate the aggregation of progressively more antagonistically differentiated

haplotypes. We have tested this model using simulations, confirming the predicted efficacy of balancing selection

and demonstrating that inversions indeed facilitate the construction of haplotypes containing multiple antagonistic

variants. Finally, we have deployed *Drosophila* lab experiments to uncover some evidence for inversion-associated

tradeoffs between reproduction and survival, depending on the specific inversion and strains tested.

3.1 Inversions in *D. melanogaster*

We have presented results from a single generation laboratory evolution experiment, in which we crossed outbred

male *D. melanogaster* carrying inversions *In(2L)t*, *In(2R)NS*, *In(3L)Ok*, and *In(3R)K* to four separate inbred female

lines and tracked the frequency of the inversions in the initial males, embryonic offspring, and aged adults. For

most inversions, the strength and direction of the tradeoff varied notably between crosses. This might suggest high

variance in their phenotypic effects or potentially maternally-dependent variation in male reproductive-success,

but is not distinguishable from experimental noise with only one replicate per maternal line. However, greater

consistency was observed for *In(3R)K*, which was associated with lesser male reproductive success but greater

survival. A significant tradeoff was also inferred for *In(3L)Ok*, which favored male reproduction (albeit variably)

over survival. These results provide significant but measured evidence for the presence of sexually antagonistic

autosomal inversions in this model species, while emphasizing the importance of genetic background.

As indicated in the Introduction, models like ours in which inversion frequencies are influenced by balancing

selection on pleiotropic tradeoffs may help explain multiple aspects of observed *D. melanogaster* inversion

frequencies. This class of models inherently accounts for the intermediate maximal frequency of most *D.*

melanogaster inversions in natural populations. To the extent that inversions favor male reproduction, the sexually

antagonistic model we propose here could also help account for the predominantly autosomal locations of

common inversions in this species, given that male-specific fitness effects have a weaker influence on the

frequencies of X-linked variants since the X chromosome spends only one third of its time in males.

This model could also help explain the observed geographic variability of inversion frequencies, as a change in

environment may change the fitness value of either pleiotropic effect of the alleles. If a population experiences a

novel harsh environment with low survivability, then the population density may decrease, and the number of

encountered competing males may decrease as well, reducing the relative fitness advantage of enhanced male

display. If there is a genetic tradeoff between mating display and viability, the equilibrium frequency of an

antagonistic inversion that favors the genetic extreme of display should be lower. Additionally, in hostile

environments, the survival cost of display-favoring variants could be increased, which could further shift their

equilibrium frequencies downward or render them not worth carrying at any frequency. These predictions could

contribute to the observed negative relationships between some inversion frequencies and latitude or altitude

(Kapun et al. 2016; Pool et al. 2017). As a specific example, it is notable that in a high altitude Ethiopian

environment with year-round cool weather, which hosts some of this species' most pronounced phenotypic

evolution (Bastide et al. 2014; Lack et al. 2016b), inversions are virtually absent - occurring at the lowest

frequencies of any analyzed population (Sprengelmeyer et al. 2020). Concordantly, geographically marginal

populations of other *Drosophila* species are often found to host less inversion polymorphism than more central

populations (Krimbas and Powell 1992). Also consistent with tradeoffs involving inversion-associated survival costs,

a disadvantage of some *D. melanogaster* inversions in challenging thermal environments (both cold and hot) was

supported by a previous experimental evolution analysis that included *In(2L)t*, *In(2R)NS*, and *In(3R)K* (Kapun et al.

2014), though they did find that *In(3R)C* consistently increased in frequency in hot conditions and *In(3R)Mo* in cold.

In contrast, our experiments yielded evidence that *In(3R)K* may have a tradeoff opposite from our prediction - with

the inverted arrangement associated with greater survival but lower male reproductive success. In line with our

findings, Said et al. (2018) found that among Zambia strains, *In(3R)K* was associated with strongly reduced

expression of *desat2*, involved in pheromone production. Whereas, higher *desat2* expression – as reported by Said

et al. (2018) for standard Zambia karyotypes – has been linked to the "Z-type" males preferred by females of some

strains from this region (*e.g.* Fang et al. 2002; but see Grillet et al. 2012). Conversely, a recent genome-wide

association study found *In(3R)K* heterokaryotypes to be associated with elevated male reproductive success

compared to standard homokaryotypes, when males from various North Carolina strains were paired with a Z-type

Zimbabwe strain known to exhibit preference for southern African male phenotypes (Yamamoto et al. 2024),

underscoring that inversion-related tradeoffs may depend on genetic background and/or experimental context.

Given that our model relies on the ability of either an inverted or a standard karyotype to place males carrying it

among the top reproductive competitors, it may seem surprising that we found two different inversions associated

with a tradeoff between survival and male reproduction – in that an individual's karyotype at one inversion could

undercut the advantage of their karyotype the other. In our case, it might seem unfavorable for a male carrying

In(3L)Ok (associated with increased male reproductive performance but lower survival) to also carry In(3R)K (which

showed the opposite patterns). Strikingly then, among 197 sequenced haploid embryo genomes from this Zambia

population (each reflecting one female gamete from independent isofemale lines; Lack et al. 2016a), not a single

genome carried both of these inversions (even though *In(3L)Ok* and *In(3R)K* were carried individually by 36 and 35

of these genomes respectively), representing a significant lack of this hypothetically disadvantageous doubly-

inverted karyotype (p = 0.0031, two-tailed Fisher's Exact Test). These inversions are 20.4 cM apart in terms of

meiosis in standard karyotype females (Comeron et al. 2012), but the contributions of natural selection versus

potentially altered meiotic dynamics in individuals heterozygous for two inversions in generating this pattern will

require further investigation.

More broadly, we observed a trend toward increased inversion frequencies across our full experimental

generation. A general benefit for inversions would mirror previous findings in which inversions found at

intermediate frequencies in natural *D. melanogaster* populations (Inoue 1979), as well as inversions from seaweed

flies known to be under balancing selection in the wild (Mérot et al. 2020), were both inferred to be under

directional selection in the lab. However, one laboratory study did report evidence that a *D. melanogaster*

inversion not tested here, *In(3R)P*, had frequency-dependent fitness under crowded conditions (Nassar et al.

1973). Furthermore, even an inversion found to be under directional selection in the lab might still be subject to a

balanced tradeoff under a more challenging or complex natural environment. Other studies in *D. melanogaster*,

including those on focused seasonal evolution, have found evidence for important tradeoffs between reproduction

and robustness to environmental challenges (*e.g.* Behrman et al. 2015). Hence, it would clearly be desirable to

study the effects of inversions on a wider range of potential tradeoffs. For example, Said et al. (2018) suggested

that inversions *In(2L)t* and *In(3R)K* might be maintained by immunity-related tradeoffs, in light of an over-

representation of immune-related genes among differentially expressed transcripts between inverted and

standard karyotypes.

In addition to a broader array of balanced tradeoffs that could modulate *D. melanogaster* inversion frequencies,

drift and other forms of selection may contribute as well. Although we emphasize above the potential interplay

between ecological adaptation and balanced tradeoffs, some inversions could be impacted by simpler forms of

directional selection. However, we must then invoke secondary explanations to account for their limited maximal

frequencies (see Introduction). Other forms of balancing selection may also come into play as well. It is clear that

some variation in this species is subject to temporally-varying selection, and some inversions have displayed

seasonal frequency differences (Dobzhansky 1943; Kapun et al. 2016; Machado et al. 2021; Lange et al. 2022). As

with spatial clines, temporal shifts could reflect either simple directional selection or else environmentally-

modulated tradeoffs in a model such as ours. Spatial selective pressures may vary both between populations and

within population scales.

As indicated in the Introduction, balancing selection on inversions could also be achieved by linkage to recessive

deleterious variants, which may be observed as an antagonistic pleiotropic phenotype despite potentially involving

strictly deleterious variants in linkage (Pei et al. 2023). In extreme form inversions might be under associative

overdominance (Zhao and Charlesworth 2016; Gilbert et al. 2020), where two haplotypes are balanced by

recessive cost to both homozygotes. Inversions may be particularly susceptible to carrying recessive deleterious

alleles if population size and/or inversion frequency are low, since under these circumstances inversion

homozygotes are rarely generated and hence the crossover rate among inverted chromosomes is low, plus there

are fewer inverted chromosomes to facilitate rare double recombination events with standard chromosomes.

However, this dynamic is not expected to establish new inversions easily (Charlesworth 2024) and is expected to

decay with increased age and population size of the inversion, as mutation, gene conversion, or double crossover

resolve the negative linkage between recessive deleterious alleles. Most common inversions in *D. melanogaster*

are both relatively old and have large effective population sizes. Inversions including *In(2L)t*, *In(2R)NS*, and *In(3R)K*

have breakpoints estimated to be several times older than the expansion of the species out of southern-central

Africa (Corbett-Detig and Hartl 2012; Sprengelmeyer et al. 2020). Those three inversions, plus *In(3L)Ok*, for which

inversion age has not been estimated, all maintain frequencies greater than 0.15 within very large populations

(Kapun and Flatt 2019; Sprengelmeyer et al. 2020), and so it is not clear that the persistence of recessive

deleterious or lethal alleles in the inverted regions is expected to be high enough that inversions would be

maintained by a shared recessive lethal variant preventing fixation. However, sampling of natural populations has

demonstrated a somewhat higher frequency of recessive lethal variants in inverted haplotypes, but these are

largely unique and heterokaryotypic individuals remain robust, giving low costs to a heavily outbred population

(Mukai and Yamaguchi 1974). Many wild-derived inbred strains of *D. melanogaster* are homokaryotypic for

inversions (Lack et al. 2016a). Furthermore, as noted in the Results, an observed lack of inversion homozygotes

could reflect strong sexual antagonism as opposed to recessive deleterious variation. Nevertheless, further

simulation and experimental testing regarding the potential influence of associative overdominance and other

processes on inversion frequencies in *D. melanogaster* and other species would be desirable.

3.2 Generality of Balanced Pleiotropic Inversions

We have proposed that some polymorphic inversions in *D. melanogaster*, and in other species with analogous

mating dynamics, may be maintained in part through balancing selection acting on a frequency-dependent

tradeoff. While we explored the tradeoff between male reproduction and viability, we emphasize that any

antagonistic pleiotropy involving at least one frequency-dependent trait has the potential to generate similar

inversion polymorphism. Such antagonistic pleiotropy may be common in evolution, and might be useful in

explaining the many examples of inversions associated with distinct phenotypes.

For the specific model explored here, of antagonistic pleiotropy between survival and display in a mate choice

system, the prevalence of the dynamic across species and populations is unclear. It seems plausible that a similar

model of antagonistic pleiotropy and balancing selection under mate choice underlies other systems, such as the

balanced inversion system in the European ruff *Calidris pugnax* (formerly *Philomachus pugnax*), where three

inverted haplotypes on an autosome determine aggressive, cooperative, and female-mimic male lekking morphs,

albeit with a dominance relationship and homozygous inviability for an inverted haplotype (Küpper et al. 2016). A

recent study on the female-mimic Faeder morph suggests that it may be maintained in part by a balance between

its effects lowering female reproductive output while increasing male mating success, and the system is likely more

complex as a whole due to the three interacting morphs (Giraldo-Deck et al. 2022). More generally, a number of

factors contribute to the potential prevalence of this dynamic. Mate competition and choice during reproduction is

rather common among animals, and this may mean sexually antagonistic inversions are plausibly also common.

The model depends on the distribution of fitness effects of new mutations and the availability of sexually

antagonistic variation, but such variation does seem prevalent (Zajitschek and Connallon 2018; Ruzicka et al. 2019).

More likely to limit the prevalence of such inversions are the meiotic costs experienced by inversion

heterokaryotypes in some systems (White 1973), whether sexually antagonistic variants are clustered in a region

that would allow inversions to increase linkage, and whether other mechanisms like sex-biased expression (Ingleby

et al. 2015), gene duplication (Connallon and Clark 2011), and linkage to the sex chromosome or sex-determining

locus would resolve the antagonism more frequently (though see following subsection on sex chromosome

evolution).

Perhaps more importantly, there are a number of well-studied cases of inversion polymorphism that might

potentially follow this dynamic of balancing selection between haplotypes simultaneously demonstrating

antagonistic pleiotropy and trait-specific frequency dependence, but which do not involve sexual antagonism. An

inversion polymorphism in the seaweed fly *Coelopa frigida* has been found to trade off between larval survival and

adult reproduction (Mérot et al. 2020). *Papilio* butterfly populations harbor well-studied mimicry polymorphisms

that segregate between inverted segments and may often experience frequency-dependent selection (Clarke and

Sheppard 1960; Kunte et al. 2014; Poul et al. 2014). The snail *Cepaea nemoralis* harbors diverse and distinct shell

patterning haplotypes associated with inversions that remain balanced within single sampling locations (Cook

2013; Surmacki et al. 2013). Several inversions in different ant species segregate a single-queen colony strategy

from a cooperative multi-queen strategy within the same range (Wang et al. 2013; Libbrecht and Kronauer 2014).

Some vertebrates found to harbor antagonistically pleiotropic inversions include the rainbow trout (Pearse et al.

2019) and the zebra finch (Pei et al. 2023). These balanced polymorphisms are variously hypothesized to involve

maintenance by overdominance (Mérot et al. 2020), linked deleterious recessives (Pei et al. 2023), or reversals of

dominance (Pearse et al. 2019), but these mechanisms are not mutually exclusive with each other, or with the

model presented here.

Essentially, any population with antagonistic pleiotropy involving some form of negative frequency-dependent

balancing selection on one of the phenotypes might exhibit the same dynamic. The population would experience

similar divergent selection towards alternate phenotypic extremes, with the frequency-dependence maintaining

the presence of two genotypes. Importantly, this model involves a different mechanism for the maintenance of

antagonistically pleiotropic variation than models based on reversals in dominance, where dominance effects

generate a net heterozygote advantage at a locus (Connallon and Chenoweth 2019). The model proposed here

integrates well with existing thought on the evolution of divergent selection on balanced systems. For example,

Kopp and Hermisson (2006) have proposed a specific form of frequency dependent divergent selection (FDDS),

involving competitive exclusion between similar genotypes for a trait otherwise under stabilizing selection, and this

model was expected to result in single or few loci of large effect. Their model did not consider pleiotropy or linkage

modifiers, but still had comparable dynamics in that selection in the FDDS regime favored small numbers of large

effect loci, while the inversion haplotypes in the model presented here simplify the recombination architecture to

approximate a single locus. This simplification of the genetic architecture follows the reduction principle in

recombination modifier theory (Feldman 1972; Feldman and Balkau 1973; Feldman et al. 1980; Altenberg and

Feldman 1987; Altenberg et al. 2017). When a population experiences selection towards two (or more) divergent

optima, under a selection regime that provides a balancing mechanism to maintain both, indirect selection will

favor a reduction of the genetic architectures to prevent the generation of intermediate phenotypes. The

likelihood of either model likely rests in part upon the inherent polygenicity of the trait under selection, with

simpler traits being more likely to resolve by single locus FDDS dynamics than by inversion association (*e.g.* Yassin

et al. 2016).

Notably, our simulations tended to result in strong sexual antagonism, such that it leads to a substantial fraction of

the population failing to survive to reproductive age. It is unclear how common such extreme antagonism may be

in natural populations. If it is uncommon in nature, even in taxa that experience high levels of mate competition as

modeled here, then it is unclear what prevents our simulation predictions from being realized. It may be that

genetic constraints prevent the occurrence of highly antagonistic genotypes, or that the relationship between

survival-altering mutations and fitness is different than we have modeled. Or, populations may steadily evolve to

mitigate antagonistic effects that arise and persist through processes such as those we modeled. Alternatively,

some highly antagonistic haplotypes may become associated with sex determination, as suggested below.

3.3 Antagonistic autosomal inversions may precede novel sex chromosomes

If balanced, sexually antagonistic, autosomal inversions occur frequently enough, they may also contribute to the

evolution of sex chromosomes. Given an established inversion with significant sexual antagonism, the inverted

haplotype that favors one sex still experiences an antagonistic cost of transmission to offspring of the opposite sex.

Mutations that link the haplotype with the sex it benefits are therefore favored under selection, and this can occur

either by fusing to an existing sex chromosome (Charlesworth and Charlesworth 1980), though this only fully

resolves the antagonism for linkage to Y and W chromosomes, or by linkage to a new sex determining mutation

(van Doorn and Kirkpatrick 2007).

Here, we discovered that strong inversion-linked antagonism could yield a scenario where essentially all highly-

successful males were homokaryotypic for a display-favoring karyotype, whereas reproducing females were

overwhelmingly heterokaryotypic (Figure 5). This situation is similar to the ZW sex chromosome system, suggesting

that this particular pleiotropic trade-off may favor resolution by linkage to a female sex determination factor.

Further, simulations in which only females experienced antagonistic survival cost usually generated populations

with a chromosome essentially lethal in females, thus exclusively transmitted in males similar to a Y chromosome

(Figure 7). These simulations sometimes had three states that appeared stable at 20N generations, including Y

chromosome-like, W chromosome-like, and shared intermediate arrangements. This three-arrangement stable

polymorphism seems unusual for a natural population, but might be interesting to explore in populations with

polymorphic sex determination.

There are often deleterious effects of chromosome fusion or novel sex determination (Pennell et al. 2015;

Saunders et al. 2019), which may represent a general obstacle to sex chromosome evolution. However, balanced

sexually antagonistic inversions may concentrate enough antagonism that the built-in benefit of resolving it may

sometimes overcome the fitness costs of evolving new sex chromosomes (Blackmon and Brandvain 2017). Hence,

antagonistic inversions might be more likely than other loci to be involved in the evolution of new sex

chromosomes.

A basic prediction of the above hypothesis is that at least one inversion difference between sex chromosomes

should already exist at the time of new sex chromosome formation, and genomic differentiation therefore begins

between inversion karyotypes on an autosome even before sex-specific transmission of the region. This scenario

contrasts with current models of sex chromosome evolution in which inversion accumulation and genomic

differentiation accrue only after sex chromosome formation, due to advantages in suppressing recombination

involving sexual antagonistic variants already associated with a sex-determining locus (Wright et al. 2016). In this

context, we note that the neo-X and neo-Y homologs of Muller element C in *Drosophila miranda*, which became

sex-linked only about 1.5 million years ago, already appear to have inversion differences between them (Chen et

al. 2024 – Figure 5A). Further, a recent study in *Littorina saxatalis* snails has discovered an ecotype-specific sex

determination system that may be founded on such tradeoffs, though selection across ecotypes involves discrete

geographic boundaries and is only partly comparable (Hearn et al. 2022). Still, additional genomic studies of new

sex chromosomes are needed to assess the potential role of sexually antagonistic inversions in sex chromosome

evolution.

Summary and Future Prospects

We have advanced a model in which inversion polymorphism is maintained by the frequency-dependent fitness

effects of a pleiotropic tradeoff associated with inversion-linked genetic variation. We have used sexual

antagonism associated with increased male reproduction versus survival as a specific motivating case, and we

explore the predictions of this model using a novel simulation algorithm. In our simulations, antagonistic variants

could be maintained at an equilibrium frequency, and inversions enabled multiple antagonistic variants to persist

and form more strongly antagonistic haplotypes. We complemented our conceptual and computational modeling

with laboratory experiments designed to detect fitness effects of four inversions common in an ancestral range

population of *D. melanogaster*. We indeed found some evidence of tradeoffs between male reproduction and

survival for these inversions, with two out of four inversions showing significant evidence for such a tradeoff,

although we also observed a strong dependence of male reproductive success on female genetic background.

In light of the persistent mystery of how *D. melanogaster* inversion frequencies are determined, and how readily

we detected tradeoffs involving male reproduction and survival, we suggest that further studies investigating the

potential fitness tradeoffs of inversions in this model system are strongly warranted. While some such studies have

previously been conducted, the applicability of our amplicon sequencing approach to estimate inversion

frequencies in large pools of flies may improve the sensitivity of such experiments. Our understanding of the

phenotypic impacts of *D. melanogaster* inversions would benefit from investigations of a wider range of fitness-

related traits that might be involved in balanced tradeoffs, including female fecundity and immunity. It will also be

important to verify the potential frequency dependence and phenotypic consequences of *D. melanogaster*

inversions under a wider range of conditions, including challenging environments such as cool temperatures and

high population densities. While inherently challenging, a further goal would be to identify loci within an inversion

such as *In(3L)Ok* or *In(3R)P* that contribute to observed tradeoffs, and in the case of an arrangement favoring male

reproduction, to test for the predicted synergistic epistasis (for male reproductive fitness) among linked variants.

Clearly, it will also be important to test the generality of our model by estimating the fitness associations of

inversions in a wider range of species. And particularly in the case of species with very recent changes sex

chromosomes, it will be of great interest to test whether one or more inversions are already present between

these new sex chromosomes, as predicted a model in which sex chromosome evolution involves the resolution of

inversion-associated sexual antagonism. Further analytic and simulation work will also be important in clarifying

the range of potential scenarios in which balancing selection and antagonistic pleiotropy may lead to the

maintenance of polymorphic haplotypes involving inversions (or parts of the genome that rarely recombine),

including studies that consider the effects of dominance and that consider tradeoffs other than the one examined

here. Collectively, such studies will advance our broader understanding of the roles of balancing selection,

pleiotropic tradeoffs, and genome structure in shaping genetic variation and genomic evolution.

899 4 Materials and Methods

900 4.1 Simulations

We developed a new individual-level forward simulator ('SAIsim' for Sexually Antagonistic Inversion simulator)

written in python 3.7 for the simulation of inversions and sexually antagonistic alleles at infinite loci, with uniform

rates of mutation, crossing over, and gene conversion (per bp, per generation) over a number of independent

chromosome arms. The dynamic we were interested in modeling requires direct accounting of pleiotropy between

different components of fitness, crossing over and gene conversion within inversions (as well as the possibility of

inversion fixation), and directly modeling male display and female choice, and no existing simulator provided this

functionality. These simulations were used to establish the potential for the model to occur in a population

generally, and not to compare against specific empirical observations. We have used literature estimates of

mutation rate and conversion rate of Zambian *D. melanogaster* for these simulations (Comeron et al. 2012; Huang

et al. 2016) but have no information on the joint distribution of effects of mutations on our model of survival and

display in *D. melanogaster*. So, we sampled from relatively broad but arbitrary combinations of mutation effects,

only assuming that there is likely some degree of antagonistic pleiotropy naturally present in genomic variation.

In SAIsim, a population is instantiated as a python object, and populated with individuals which are also

represented by python objects. These individuals may be instantiated using genomes specified by the user, or by

default carry no genomic variation. In each generation, as diagrammed in Figure 2, the simulator calculates a

survival probability for each individual as the product of the survival values of each variant they carry, which range

[0,1]. Here, multiplicative selection for survival prevents biologically unreasonable negative survival probabilities

from occurring. Male and female survival costs can each be included in a sex-specific manner, but only globally in

the simulation, not per mutation. For each offspring in the next generation, a mother is selected randomly,

weighted by individual survival probabilities, with replacement. To model the encountered males that might

become the father of an offspring individual from this female, a set number of males (*i.e.* the uniformly specified

encounter number, here 100 males unless otherwise specified) is randomly sampled from the full population of

males, weighted by their survival probabilities. The males each have a genetic display quality given as the sum of

the reproductive values of their alleles, each of which range [0,1]. A noise parameter, normally distributed around

zero with a standard deviation of one, is added to each male display value during each encounter. The male with

the highest noise-adjusted display quality among the encountered males is chosen to be the father. As offspring

are generated, crossover locations are sampled, and resampled in cases where the resultant gamete would be

aneuploid. While the simulator can allow recombination in both sexes, all simulations presented only generate

crossovers and gene conversion events for female gametes, in accordance with the biology of *D. melanogaster*.

Resampling aneuploids removes the fecundity cost that may exist in some taxa, but was chosen to reflect the lack

of observed fecundity effects for most paracentric inversions of *D. melanogaster*. Gene conversion is modeled as a

constant probability per heterozygous variant, with each event independently affecting just one locus, rather than

explicitly modeling a per-bp conversion rate and tract length (given that gene conversion tracts are generally short

and each would typically contain only a single modeled variant in our simulations). The dynamics of gene

conversion are expected to have separate effects on the assembly and the maintenance of arrangements. The

assembly of an arrangement is positively dependent on the population-scaled rate of recombination of alleles as

new polymorphisms start at low frequency and often not on their optimal haplotype. However, the indirect fitness

effect of the inversion is dependent on its effect on recombinant offspring, and therefore negatively depends on

the per-individual rate of conversion. Finally, inversions and new mutations are potentially added to the resultant

gamete, with inversions resampled when overlapping the coordinates of an inversion already present on the same

individual chromosome. SAIsim also allows the specification of mutation rates and the distribution of effect sizes of

new mutations.

The simulations presented in Figures 5, 6, and 7 rescale parameter values by a factor of 2,000 to emulate an

estimated ancestral N_e of roughly 2×10^6 (Sprengelmeyer et al. 2020) while using a smaller simulated population of

1,000 individuals. The low crossover rate simulations model a 0.0218 cM region and the high crossover rate

simulations model 2.18 cM, which scale to 43.6 cM and 43.6 M female meiotic maps in the simulated populations.

Based on an average autosomal recombination rate in females of 2.18×10^{-8} for *D. melanogaster* (Comeron et al.

2012), these represent 10kb and 1Mb regions. Gene conversion occurs at each heterozygous variant with a

probability of 0.1295, based on scaling $\gamma=1.25 \times 10^{-7}$ events/bp/female meiosis with a conversion track length of

518 bp (Comeron et al. 2012) to a per-single-nucleotide-variant estimate of 6.475×10^{-5} conversions/bp/female

meiosis.

Rates of sexually antagonistic mutations and inversion mutations are empirically undetermined. Here, sexually

antagonistic mutations were modeled at a rate corresponding to one per thousand mutations, and so based on an

estimate of 5.21×10^{-9} mutations/bp/gen on autosomes (Huang et al. 2016), and modeling 10kb and 1Mb regions,

these were scaled to 1.042×10^{-4} and 1.042×10^{-2} events per gamete respectively. Inversions were approximated

as arising once per hundred sexually antagonistic mutations, *i.e.* 1.042×10^{-6} and 1.042×10^{-4} events per gamete.

The simulations use mutations with uniformly distributed quality values in the range [0,1]; although distributions

skewed toward small effects may be more realistic, our uniform approach avoids the need to invoke a specific but

empirically unknown distribution.

SAIsim's object-oriented design allows specification of a population model by a new user familiar with the basics of

python scripting. A population object can be parameterized and populated in a few lines of python script, and then

parameters can be changed between periods of simulation, allowing bottlenecks and demographic changes as well

as changes in mutational parameters between generations. Replicate SAIsim simulations were performed via the

UW-Madison Center For High Throughput Computing (CHTC), which manages cycle servers using the HTCondor

distributed computing project (Thain et al. 2005; Erlandson and Theisen 2018).

966   4.2 Experimental Populations and Sequencing

To act as a high-inversion source population for the potential fathers in our experiment, we combined 15 males

and 15 females from each of 10 inbred strains derived from wild flies collected in Zambia, and allowed the

population to breed for two generations. These 10 strains were chosen to collectively carry the following common

inversions: *In(2L)t*, *In(2R)NS*, *In(3L)Ok, In(3R)K*. This high-inversion population may not and need not have been at

an equilibrium frequency for any particular inversion; instead it was simply designed to transmit each inversion to

offspring at meaningful frequency. We collected males from this second generation to use as the paternal pool in

each of our independent maternal line experiments, and these males were expected to carry a wide range of

inversion genotypes. Each batch of high-inversion males was crossed to an equal number of virgin females from a

single inbred Zambian strain (Figure 8; Table S1). Four such experiments were performed, each using one

inversion-free maternal strain, in clear plexiglass cages (19.3 by 19.3 by 30.0 cm) with a loose mesh covering on

one end for access by hand.

Embryos were collected by placing four 7.9 cM petri dishes of grape agar in a population cage for one day, then

counting and freezing the collected eggs. To obtain adult offspring, six bottles of standard *Drosophila* medium (see

below) were placed in a population cage for one day. Egg-laying for embryo and adult collections occurred on

alternating days over two weeks, after which all surviving parents were counted and frozen. From the first day in

which flies eclosed in a bottle, adults were collected at the end of each period of a day to two days and were

separated by sex. These cohorts were aged by weekly transfer to new bottles. The adult offspring were therefore

initially separated by sex and by the time after laying at which they eclosed, as well as the time in which they were

laid, with different early- or late-eclosing batches from a given cross later pooled before DNA extraction. In our

husbandry conditions, the earliest eclosion was 11 days after laying, but this was rare and a first eclosion at 12

days was more common among the bottles. Most flies took several days longer to develop, and we considered flies

collected in the first 6 days of a 10 day collection window to be the early-eclosing pool, in order to split the pool

sample sizes closer to evenly. The collected adult flies were then aged by sequentially transferring them between

bottles weekly for approximately 2.5 months, and then the adult offspring were sexed, counted, and collected. A

10-week aging window was chosen based on the time taken for a control set of four bottles of flies from the

paternal outbred population to reach 80% mortality, to reflect the survival and longevity stressors of the

laboratory bottle environment. All adult and embryo samples were frozen at -80°C before DNA extraction.

Since no inversions could be inherited through the mothers, inversion frequencies among successful male gametes

could be inferred from their pooled offspring. Therefore, the above sampling scheme allowed us to identify

inversion frequencies in the set of potential parents, in embryonic offspring, and in older adults, and so to assess

potentially selected changes in inversion frequency across male reproduction or between eggs and aged adults

(encompassing viability plus longevity). We chose to age the populations to include longevity as long term survival,

which both encompasses fitness challenges that generate mortality at earlier time points, and is relevant to the

need to survive during periods of unsuitable environments. Although a natural population from North Carolina was

estimated to have an average generation time of about 24 days (including developmental time; Pool 2015), in

many climates fly populations cycle seasonally between periods of rapid reproduction and survival for months as

adults under reproductive diapause (Saunders et al. 1990; Ragland et al. 2019). While longevity is a key selective

pressure underlying overwintering, the relationship between longevity in permissive lab conditions without

diapause and in natural conditions under diapause is unclear (Schmidt et al. 2005; Flatt 2020), and our experiment

represents just one of many possible ways to examine tradeoffs involving survival.

Unless otherwise noted, all flies in the above experiments were kept in a lab space of 23°C with around a degree of

temperature fluctuation and without an artificially controlled day/night cycle. Light exposure was dependent on

the varying use of the space by laboratory workers but amounted to near constant exposure to at least a minimal

level of lighting, with some variable light due to indirect lighting from adjacent rooms with exterior windows. All fly

food used was prepared in batches of 4.5 L water, 500 mL cornmeal, 500 mL molasses, 200 mL yeast, 54 g agar, 20

mL propionic acid, and 45 mL tegosept 10% (in 95% ethanol). The grape agar was prepared in batches of 500 mL

from FlyStuff.com grape agar powder, and wet Red Star yeast was brushed over the agar plates before use to

encourage laying.

1015   4.3 Sequencing and Data Preparation

DNA for each replicate age group was extracted by a phenol-chloroform extraction protocol used previously in

preparing DNA for the Drosophila Genome Nexus and *Drosophila* Population Genomics Project. We followed

protocol 'BPC' used in DPGP phase 1 (presented in Langley et al. 2012), except with the addition of proteinase-K

during homogenization of adult flies. These protocols are ultimately based on the common quick preparation

protocol presented in *Drosophila Protocols* (Huang et al. 2009). Inversion genotyping was performed by amplicon

sequencing, where amplicons associated with each inversion were designed to contain at least one single

nucleotide polymorphism in the inversion interior that is fixed for alternate alleles between the inversion

karyotypes, while still sharing conserved primer regions across karyotypes to prevent primer bias. Genetic

variation in these inversions was assessed using 197 previously sequenced and inversion-called haploid genomes

from the same Zambian *D. melanogaster* population studied here, available from the *Drosophila* Genome Nexus

(Lack et al. 2016a). The amplicon region identification and primer selection was performed with a custom script,

which calls Primer3 version 2.4.0 for primer candidate generation (Koressaar and Remm 2007; Untergasser et al.

2012; Koressaar et al. 2018). Primers thus selected were ordered from IDT as oligos ligated to Illumina stubby

adaptors (Table S2). Illumina sequencing libraries were then prepared for each sample following the Illumina

metagenomic amplicon sequencing protocol (Illumina 2013), with 50 ng/uL diluted DNA samples. and sequenced

using 150bp paired end reads on an Illumina NovaSeq to at least a depth of 20,000 reads. Depth was selected to

ensure high likelihood of detecting a 0.025 change in inversion frequency from an initial frequency of 0.10, based

on simulated resampling of the collected flies, DNA extraction, and sequencing.

Sequence preparation and analysis were performed using custom pipeline scripts. Read trimming, alignment, and

QC were performed using bwa version 0.7.17-r1188 (Li 2013), GATK version 3.4-46 (Van der Auwera and O'Connor

2020), and Picard version 1.79 (Broad Institute 2019). Reads were trimmed at the ends to remove segments with

base quality less than 20, and read pairs were filtered to retain only those pairs where both reads aligned with

mapping quality >20. SNP identity at the sites of interest was called from those remaining reads with base

quality >20 at the SNP of interest. Due to the presence of chimeric reads in the amplicon library sequencing, we

chose to use a single discriminant SNP to determine each inversion's frequency in the read pool, instead of

incorporating haplotype or additional SNP information.

4.4 Statistical Analysis of Inversion Frequencies

Before analyzing the significance of frequency change reversals across three cohorts (which is described below),

we assessed the significance of the difference in inversion frequency between just two sampled life stages in the

same experiment. For each such comparison, we first calculated a chi-square test statistic (as a convenient metric

to use when comparing empirical data with simulated experimental replicates, rather than as a formal test) from

the two-by-two table of inverted and non-inverted allele counts at two life stages. Allele counts were estimated by

multiplying the inversion-specific SNP allele frequency in the sequencing reads by the allelic sample size based on

the number of flies present in the sample. We then generated an approximate distribution of the chi-square

statistic when selection is absent (our null hypothesis), using a resampling approach (Figure 8), as described in the

following paragraph. Comparing the observed statistic to our modeled neutral distribution of test-statistic values

allowed us to calculate a p-value for this inversion's frequency change between these two life stages.

To generate the neutral distribution of the chi-square statistic, we took the observed paternal inversion

frequencies and then sampled from them to obtain new paternal and offspring read counts to represent a single

neutral data set as follows. First, we resampled the collected allelic counts (given in Tables S7 and S8) to account

for sampling variance between replicates. For the paternal samples, we needed to account for pre-sequencing

mortality as up to 15% of males died before collection (Table S1). So, in generating a new paternal read set, we

first modeled down-sampling of the paternal allele sample from the initial census allelic count to the collected

allelic count as a hypergeometric sampling. For all other cohorts we used a binomial resampling from the collected

allelic count. Second, we used a binomial sampling step to account for the experimental variance introduced by the

extraction and library preparation. The extraction and library preparation appeared to introduce variation

independent of allele sample size, possibly due to variation introduced during PCR or sample homogenization. This

inference was based on analysis of data from control library preparations (Table S9) and from sequencing done in

parallel with our experiment from sample fly pools with known inversion frequencies. These control samples

included an average of 6 technical replicates (separate library prep and sequencing replicates from the same flies)

from four different expected frequencies for *In(2L)t,* as well as one expected frequency for each of *In(2R)NS* and

In(3R)K. Due to genotyping and husbandry difficulties we did not have a control set for *In(3L)Ok*. Based on the

inversion frequency differences observed among these technical replicates, we estimated that taking a binomial

sampling of size 316 from the sample allele frequency reflected a maximum likelihood model for the sample-size-

independent variation introduced by the library prep and sequencing process. Third, from the preliminary

resampled paternal inversion frequency, we then took a binomial sample of size equal to the read count to

account for the random sample of sequencing reads, thus yielding resampled paternal read counts (given in Tables

S7 and S8) that accounted for the number of sampled and non-sampled individuals, experimental variance, and

depth of coverage. Fourth, to generate resampled offspring read sets, we instead used a binomial sampling of half

the offspring alleles from the fully resampled paternal allele frequency for each separate offspring cohort, since

the homozygous mothers all contributed non-inverted alleles. Finally, each offspring allele sample was resampled

using the same size 316 binomial sampling to account for the variation introduced during this library's preparation,

and binomial sampled again with the read count size to account for sampling reads from the library, thus yielding

resampled offspring read counts that accounted for the same three factors as for paternal counts.

For a pairwise comparison of inversion frequency between two samples, we calculated the same allele count chi-

square statistic as described above for the empirical data for each resampled set of allele counts, generating the

full distribution of neutral chi-square test statistics from which we could identify extreme value cutoffs. We then

obtained a p-value from the proportion of resampled replicates in which the chi-square statistic was greater than

or equal to the empirical value. If the test was directional, we took the proportion of resampled replicates with

both a chi-square statistic greater than or equal to the empirical value and a frequency difference in the expected

direction.

In order to identify a frequency change reversal between life history stages that could reflect a fitness tradeoff, we

tested for the joint significance of two opposing frequency changes using three cohorts: specifically a frequency

change in one direction between paternal and embryo samples, followed by a frequency change in the opposite

direction between embryo and adult offspring samples. These changes both depend on the shared embryonic

cohort in the test, and so are not independent. Therefore, we evaluated the two inversion frequency changes

jointly from a set of resampled neutral data sets in which the three cohorts arose from the same resampling

process. Here we considered how likely it was that a sample of the three cohorts from the associated estimated

neutral model had chi-square values for both the comparison of the fathers to embryos and the embryos to adult

offspring that were each equivalent or more extreme in the test direction than the observed data. For example,

when testing the significance of an observed paternal-embryo increase and then embryo-adult decrease in

frequency, our p-value would be defined by the proportion of resampled replicates in which the frequency

changes were in the tested directions of increase then decrease, and their chi-square values were both more

extreme than the empirical values. The potential for empirical frequency change reversals to occur in either

direction was accounted for at the multiple test correction step as indicated below.

To assess the significance of inversion frequency changes considered across all four maternal line crosses at once,

we used Fisher's combined probability test. We applied this to both particular three-cohort frequency change

reversals and to the set of two-cohort frequency changes. The inversion trajectory is independent between

maternal crosses, but the differences between each cross in maternal line and initial paternal genetic variation

make the replicates difficult to compare in a more structured way, so we felt this was an appropriate test for

combined significance. In assessing our tradeoff hypothesis, we applied this test only for inversions where it was

well-motivated; *i.e.* where the averaged frequency change across maternal crosses was in opposite directions

between paternal/embryo and embryo/adult comparisons.

To account for multiple hypothesis testing in our cohort comparisons, we used a Benjamini-Yekutieli false

discovery rate correction for significance. We applied this correction across the set of Fisher's method combined p-

values we generated to assess the relevant frequency change reversal hypotheses. So, this corrected for the

multiple hypotheses of two potential tradeoff directions and the four inversions studied, from p-values that

already combined evidence from different maternal line crosses. Benjamini-Yekutieli was chosen due to its

robustness to the unclear dependence relationships between some of the tests involved. For example, multiple

tests of frequency changes from a single cohort (*e.g.* an embryo sample compared against both paternal and aged

adult samples) are likely to be positively correlated.

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Data Availability

1119   Sequencing reads have been uploaded to the NIH Short Read Archive under project XXXXXX. The simulation

1120   program and other analysis scripts can be found at https://github.com/csmcal/.

1121

Acknowledgements

Particular thanks to Shimeng Gao, who assisted with *Drosophila* husbandry and collection of adult flies during the

within-generation experiment. We also thank members of the Pool lab and three anonymous reviewers for helpful

comments on earlier versions of this manuscript.

This research was supported by National Science Foundation Graduate Research Fellowship (DGE-1747503 to

CSM), and by the National Institutes of Health (grants R35 GM136306 to JEP, T32 GM007133, and T32 HG002760).

This research was performed using the compute resources and assistance of the UW-Madison Center for High

Throughput Computing (CHTC) in the Department of Computer Sciences. The CHTC is supported by UW-Madison,

the Advanced Computing Initiative, the Wisconsin Alumni Research Foundation, the Wisconsin Institutes for

Discovery, and the National Science Foundation, and is an active member of the Open Science Grid, which is

supported by the National Science Foundation and the U.S. Department of Energy's Office of Science.

1133

Works Cited

Altenberg L, Feldman MW. 1987. Selection, generalized transmission and the evolution of modifier genes. I. The reduction principle. *Genetics* 117:559–572.

Altenberg L, Liberman U, Feldman MW. 2017. Unified reduction principle for the evolution of mutation, migration, and recombination. *Proc. Natl. Acad. Sci. U.S.A.* 114:E2392–E2400.

Audet T, Krol J, Pelletier K, Stewart AD, Dworkin I. 2024. Sexually discordant selection is associated with trait specific morphological changes and a complex genomic response. *Evolution* 78:1426–1440.

Aulard S, David JR, Lemeunier F. 2002. Chromosomal inversion polymorphism in Afrotropical populations of *Drosophila melanogaster*. *Genet. Res.* 79:49–63.

Babcock CS, Anderson WW. 1996. Molecular evolution of the Sex-Ratio inversion complex in *Drosophila pseudoobscura*: analysis of the Esterase-5 gene region. *Mol. Biol. Evol.* 13:297–308.

Bastide H, Ogereau D, Montchamp-Moreau C, Gérard PR. 2022. The fate of a suppressed X-linked meiotic driver: experimental evolution in *Drosophila simulans*. *Chromosome Res.* 30:141–150.

Bastide H, Yassin A, Johanning EJ, Pool JE. 2014. Pigmentation in *Drosophila melanogaster* reaches its maximum in Ethiopia and correlates most strongly with ultra-violet radiation in sub-Saharan Africa. *BMC Evol. Biol.* 14:179.

Bateman AJ. 1948. Intra-sexual selection in *Drosophila*. *Heredity* 2:349–368.

Behrman EL, Watson SS, O'Brien KR, Heschel MS, Schmidt PS. 2015. Seasonal variation in life history traits in two *Drosophila* species. *J. Evol. Biol.* 28:1691–1704.

Berdan EL, Barton NH, Butlin R, Charlesworth B, Faria R, Fragata I, Gilbert KJ, Jay P, Kapun M, Lotterhos KE, et al. 2023. How chromosomal inversions reorient the evolutionary process. J. Evol. Biol. 36:1761–1782.

Betrán E, Santos M, Ruiz A. 1998. Antagonistic Pleiotropic Effect of Second-Chromosome Inversions on Body Size and Early Life-History Traits in *Drosophila buzzatii*. *Evolution* 52:144–154.

Blackmon H, Brandvain Y. 2017. Long-Term Fragility of Y Chromosomes Is Dominated by Short-Term Resolution of Sexual Antagonism. *Genetics* 207:1621–1629.

Blows MW, Brooks R. 2003. Measuring Nonlinear Selection. *Am. Nat.* 162:815–820.

Broad Institute. 2019. Picard Toolkit. Available from: http://broadinstitute.github.io/picard/

Charlesworth B. 1974. Inversion polymorphism in a two-locus genetic system. *Genet. Res.* 23:259–280.

Charlesworth B. 1997. The evolution of lethals in the t-haplotype system of the mouse. *Proc. Royal Soc. B* 258:101–107.

Charlesworth B. 2024. The fitness consequences of genetic divergence between polymorphic gene arrangements. Genetics 226:iyad218.

1166   Charlesworth B, Barton NH. 2018. The Spread of an Inversion with Migration and Selection. *Genetics* 208:377–382.

1167   Charlesworth B, Charlesworth D. 1973. Selection of new inversions in multi-locus genetic systems. *Genet. Res.*
1168   21:167–183.

1169   Charlesworth B, Charlesworth D. 2010. Elements of Evolutionary Genetics. W. H. Freeman

1170   Charlesworth B, Hughes KA. 2000. The maintenance of genetic variation in life-history traits. In: Singh RS, Krimbas
1171   CB, editors. Evolutionary Genetics: from Molecules to Morphology. Cambridge, U.K.; New York, NY, USA:
1172   Cambridge University Press. p. 369–392.

1173   Charlesworth D, Charlesworth B. 1980. Sex differences in fitness and selection for centric fusions between sex-
1174   chromosomes and autosomes. *Genet. Res.* 35:205–214.

1175   Chen KH-C, Chatla K, Bachtrog D. 2024. Single-cell RNA-seq of *Drosophila miranda* testis reveals the evolution and
1176   trajectory of germline sex chromosome regulation. *PLOS Genet.* 22(4): e3002605.

1177   Cheng C, Kirkpatrick M. 2016. Sex-Specific Selection and Sex-Biased Gene Expression in Humans and Flies. *PLOS*
1178   *Genet.* 12:e1006170.

1179   Clarke CA, Sheppard PM. 1960. Super-genes and mimicry. *Heredity* 14:175–185.

1180   Comeron JM, Ratnappan R, Bailin S. 2012. The Many Landscapes of Recombination in *Drosophila melanogaster*.
1181   *PLOS Genet.* 8:e1002905.

1182   Connallon T, Chenoweth SF. 2019. Dominance reversals and the maintenance of genetic variation for fitness. *PLOS*
1183   *Biol.* 17:e3000118.

1184   Connallon T, Clark AG. 2011. The resolution of sexual antagonism by gene duplication. *Genetics* 187:919–937.

1185   Connallon T, Clark AG. 2014. Balancing Selection in Species with Separate Sexes: Insights from Fisher's Geometric
1186   Model. *Genetics* 197:991–1006.

1187   Cook LM. 2013. Selection and disequilibrium in Cepaea nemoralis. *Biol. J. Linn. Soc.* 108:484–493.

1188   Corbett-Detig RB. 2016. Selection on Inversion Breakpoints Favors Proximity to Pairing Sensitive Sites in Drosophila
1189   melanogaster. *Genetics* 204:259–265.

1190   Corbett-Detig RB, Hartl DL. 2012. Population Genomics of Inversion Polymorphisms in *Drosophila melanogaster*.
1191   *PLOS Genet.* 8:e1003056.

1192   Courret C, Chang C-H, Wei KH-C, Montchamp-Moreau C, Larracuente AM. 2019. Meiotic drive mechanisms: lessons
1193   from Drosophila. *Proc. Royal Soc. B* 286:20191430.

1194   Coyne JA, Meyers W, Crittenden AP, Sniegowski P. 1993. The Fertility Effects of Pericentric Inversions in *Drosophila*
1195   *melanogaster*. *Genetics* 134:487–496.

1196   Cox RM, Calsbeek R. 2009. Sexually Antagonistic Selection, Sexual Dimorphism, and the Resolution of Intralocus
1197   Sexual Conflict. *Am. Nat.* 173:176–187.

1198   da Silva Ribeiro T, Galván JA, Pool JE. 2022. Maximum SNP FST Outperforms Full-Window Statistics for Detecting
1199   Soft Sweeps in Local Adaptation. *Genome Biol. Evol.* 14:evac143.

Dickerson GE. 1955. Genetic slippage in response to selection for multiple objectives. *Cold Spring Harbor Symposia*
on Quantitative Biology 20:213–224.

Dobzhansky TG. 1943. Genetics of Natural Populations IX. Temporal Changes in the Composition of Populations of
Drosophila pseudoobscura. *Genetics* 28:162–186.

Dobzhansky TG. 1949. Observations and Experiments on Natural Selection in *Drosophila*. *Hereditas* 35:210–224.

Dobzhansky TG. 1950. Genetics of natural populations. XIX. Origin of heterosis through natural selection in
populations of *Drosophila pseudoobscura*. *Genetics* 35:288–302.

Dobzhansky TG. 1970. Genetics of the Evolutionary Process. Columbia University Press

van Doorn GS, Kirkpatrick M. 2007. Turnover of sex chromosomes induced by sexual conflict. *Nature* 449:909–912.

Erlandson E, Theisen T. 2018. htcondor: HTCondor source repository, formerly the Condor Project. Available from:
https://github.com/htcondor/htcondor

Fang S, Takahashi A, Wu C-I. 2002. A Mutation in the Promoter of *Desaturase 2* Is Correlated With Sexual Isolation
Between *Drosophila* Behavioral Races. *Genetics* 162:781-784.

Faria R, Johannesson K, Butlin RK, Westram AM. 2019. Evolving Inversions. *Trends Ecol. Evol.* 34:239–248.

Feldman MW. 1972. Selection for Linkage Modification: I. Random Mating Populations. *Theor. Pop. Biol.* 3:324–
346.

Feldman MW, Balkau B. 1973. Selection for Linkage Modification: II. A Recombination Balance for Neutral
Modifiers. *Genetics* 74:713–726.

Feldman MW, Christiansen FB, Brooks LD. 1980. Evolution of recombination in a constant environment. *Proc. Natl.*
Acad. Sci. U.S.A. 77:4838–4841.

Flatt T. 2020. Life-History Evolution and the Genetics of Fitness Components in *Drosophila melanogaster*. *Genetics*
214:3–48.

Frydenberg O. 1963. Population Studies of a Lethal Mutant in *Drosophila melanogaster*. *Hereditas* 50:89–116.

Gilbert KJ, Pouyet F, Excoffier L, Peischl S. 2020. Transition from Background Selection to Associative
Overdominance Promotes Diversity in Regions of Low Recombination. *Curr. Biol.* 30:101-107.e3.

Gillespie JH. 1998. Population Genetics: A Concise Guide. Johns Hopkins University Press

Giraldo-Deck LM, Loveland JL, Goymann W, Tschirren B, Burke T, Kempenaers B, Lank DB, Küpper C. 2022.
Intralocus conflicts associated with a supergene. *Nat. Commun.* 13:1384.

Glaser-Schmitt A, Ramnarine TJS, Parsch J. 2023. Rapid evolutionary change, constraints and the maintenance of
polymorphism in natural populations of *Drosophila melanogaster*. *Mol. Ecol.*

Gong WJ, McKim KS, Hawley RS. 2005. All Paired Up with No Place to Go: Pairing, Synapsis, and DSB Formation in a
Balancer Heterozygote. *PLOS Genet.* 1:e67.

Gowaty PA, Kim Y-K, Anderson WW. 2012. No evidence of sexual selection in a repetition of Bateman's classic
study of *Drosophila melanogaster*. *Proc. Natl. Acad. Sci. U. S. A.* 109:11740–11745.

Grieshop K, Arnqvist G. 2018. Sex-specific dominance reversal of genetic variation for fitness. *PLOS Biol.*
16:e2006810.

Grillet M, Everaerts C, Houot B, Ritchie MG, Cobb M, Ferveur J-F. 2012. Incipient speciation in *Drosophila*
melanogaster involves chemical signals. *Sci. Rep.* 2:224.

Hazel LN. 1943. The Genetic Basis for Constructing Selection Indexes. *Genetics* 28:476–490.

Hearn KE, Koch EL, Stankowski S, Butlin RK, Faria R, Johannesson K, Westram AM. 2022. Differing associations
between sex determination and sex-linked inversions in two ecotypes of Littorina saxatilis. *Evolution*
Letters 6:358–374.

Hoffmann AA, Rieseberg LH. 2008. Revisiting the Impact of Inversions in Evolution: From Population Genetic
Markers to Drivers of Adaptive Shifts and Speciation? *Annu. Rev. Ecol. Evol. Syst.* 39:21–42.

Hoquet T, Bridges WC, Gowaty PA. 2020. Bateman's Data: Inconsistent with "Bateman's Principles." *Ecol. Evol.*
10:10325–10342.

Huang AM, Rehm EJ, Rubin GM. 2009. Quick Preparation of Genomic DNA from Drosophila. *Cold Spring Harb.*
Protoc. 2009:pdb.prot5198.

Huang W, Lyman RF, Lyman RA, Carbone MA, Harbison ST, Magwire MM, Mackay TF. 2016. Spontaneous
mutations and the origin and maintenance of quantitative genetic variation. Przeworski M, editor. *eLife*
5:e14625.

Illumina. 2013. 16S metagenomic sequencing library preparation guide. Available from:
https://support.illumina.com/documents/documentation/chemistry_documentation/16s/16s-
metagenomic-library-prep-guide-15044223-b.pdf

Ingleby FC, Flis I, Morrow EH. 2015. Sex-Biased Gene Expression and Sexual Conflict throughout Development. *Cold*
Spring Harb. Perspect. Biol. 7:a017632.

Innocenti P, Morrow EH. 2010. The Sexually Antagonistic Genes of Drosophila melanogaster. *PLOS Biol.*
8:e1000335.

Inoue Y. 1979. The Fate Of Polymorphic Inversions Of *Drosophila melanogaster* Transferred To Laboratory
Conditions. *Jpn. J. Genet.* 54:83–96.

John A, Vinayan K, Varghese J. 2016. Achiasmy: Male Fruit Flies Are Not Ready to Mix. *Front. Cell Dev. Biol.* 4:75.

Jones AG, Arguello JR, Arnold SJ. 2002. Validation of Bateman's principles: a genetic study of sexual selection and
mating patterns in the rough-skinned newt. *Proc. R. Soc. B Biol. Sci.* 269:2533–2539.

Kapun M, Fabian DK, Goudet J, Flatt T. 2016. Genomic Evidence for Adaptive Inversion Clines in *Drosophila*
melanogaster. *Mol. Biol. Evol.* 33:1317–1336.

Kapun M, Flatt T. 2019. The adaptive significance of chromosomal inversion polymorphisms in *Drosophila*
melanogaster. *Mol. Ecol.* 28:1263–1282.

Kapun M, Mitchell ED, Kawecki TJ, Schmidt P, Flatt T. 2023. An Ancestral Balanced Inversion Polymorphism Confers
Global Adaptation. *Mol. Biol. Evol.* 40:msad118.

Kapun M, van Schalkwyk H, McAllister B, Flatt T, Schlötterer C. 2014. Inference of chromosomal inversion dynamics
from Pool-Seq data in natural and laboratory populations of *Drosophila melanogaster*. *Mol. Ecol.*
23:1813–1827.

Kaufmann P, Howie JM, Immonen E. 2023. Sexually antagonistic selection maintains genetic variance when sexual
dimorphism evolves. *Proc. Royal Soc. B* 290:20222484.

Kirkpatrick M, Barton N. 2006. Chromosome Inversions, Local Adaptation and Speciation. *Genetics* 173:419–434.

Kopp M, Hermisson J. 2006. The evolution of genetic architecture under frequency-dependent disruptive selection.
Evolution 60:1537–1550.

Koury SA. 2023. Predicting recombination suppression outside chromosomal inversions in *Drosophila
melanogaster* using crossover interference theory. *Heredity* 130:196–208.

Koressaar T, Lepamets M, Kaplinski L, Raime K, Andreson R, Remm M. 2018. Primer3_masker: integrating masking
of template sequence with primer design software. *Bioinforma. Oxf. Engl.* 34:1937–1938.

Koressaar T, Remm M. 2007. Enhancements and modifications of primer design program Primer3. *Bioinforma. Oxf.
Engl.* 23:1289–1291.

Krimbas CB, Powell JR. 1992. Introduction. In: Krimbas CB, Powell JR, editors. *Drosophila* Inversion Polymorphism.
Boca Raton, FL: CRC Press. p. 1–52.

Kunte K, Zhang W, Tenger-Trolander A, Palmer DH, Martin A, Reed RD, Mullen SP, Kronforst MR. 2014. doublesex
is a mimicry supergene. *Nature* 507:229–232.

Küpper C, Stocks M, Risse JE, Remedios N dos, Farrell LL, McRae SB, Morgan TC, Karlionova N, Pinchuk P, Verkuil YI,
et al. 2016. A supergene determines highly divergent male reproductive morphs in the ruff. *Nat. Genet.*
48:79–83.

Lack JB, Lange JD, Tang AD, Corbett-Detig RB, Pool JE. 2016. A Thousand Fly Genomes: An Expanded *Drosophila*
Genome Nexus. *Mol. Biol. Evol.* 33:3308–3313.

Lack JB, Yassin A, Sprengelmeyer QD, Johanning EJ, David JR, Pool JE. 2016. Life history evolution and cellular
mechanisms associated with increased size in high-altitude *Drosophila*. *Ecol. Evol.* 6:5893–5906.

Lange JD, Bastide H, Lack JB, Pool JE. 2022. A Population Genomic Assessment of Three Decades of Evolution in a
Natural *Drosophila* Population. *Mol. Biol. Evol.* 39:msab368.

Langley CH, Stevens K, Cardeno C, Lee YCG, Schrider DR, Pool JE, Langley SA, Suarez C, Corbett-Detig RB,
Kolaczkowski B, et al. 2012. Genomic Variation in Natural Populations of *Drosophila melanogaster*.
Genetics 192:533–598.

Lemeunier F, Aulard S (1992). Inversion polymorphism in *Drosophila melanogaster*. In: Krimbas CB, Powell JR
(eds) *Drosophila Inversion Polymorphism*. CRC Press: Boca Raton, FL pp 339–405.

Li H. 2013. Aligning sequence reads, clone sequences and assembly contigs with BWA-MEM. Available from:
http://arxiv.org/abs/1303.3997

Libbrecht R, Kronauer DJC. 2014. Convergent Evolution: The Genetics of Queen Number in Ants. *Curr. Biol.* 24:R1083–R1085.

Lupiáñez DG, Kraft K, Heinrich V, Krawitz P, Brancati F, Klopocki E, Horn D, Kayserili H, Opitz JM, Laxova R, et al. 2015. Disruptions of Topological Chromatin Domains Cause Pathogenic Rewiring of Gene-Enhancer Interactions. *Cell* 161:1012–1025.

Machado HE, Bergland AO, Taylor R, Tilk S, Behrman E, Dyer K, Fabian DK, Flatt T, González J, Karasov TL, et al. 2021. Broad geographic sampling reveals the shared basis and environmental correlates of seasonal adaptation in Drosophila. *eLife* 10:e67577.

McBroome J, Liang D, Corbett-Detig RB. 2020. Fine-Scale Position Effects Shape the Distribution of Inversion Breakpoints in *Drosophila melanogaster*. *Genome Biol. Evol.* 12:1378–1391.

Mérot C, Llaurens V, Normandeau E, Bernatchez L, Wellenreuther M. 2020. Balancing selection via life-history trade-offs maintains an inversion polymorphism in a seaweed fly. *Nat. Commun.* 11:670.

Mettler E, Voelker RA, Mukai T. 1977. Inversion Clines in Populations of *Drosophila melanogaster*. *Genetics* 87:8.

Morgan TH. 1910. Sex Limited Inheritance in *Drosophila*. *Science* 32:120–122.

Mroczek RJ, Melo JR, Luce AC, Hiatt EN, Dawe RK. 2006. The Maize Ab10 Meiotic Drive System Maps to Supernumerary Sequences in a Large Complex Haplotype. *Genetics* 174:145–154.

Mukai T, Yamaguchi O. 1974. The genetic structure of natural populations of *Drosophila melanogaster*. XI. Genetic variability in a local population. *Genetics* 76:339–366.

Munasinghe M, Brandvain Y. 2023. Together Inbreeding and Reproductive Compensation Favor Lethal t-Haplotypes. *J. Hered.*, Accepted.

Nassar R, Muhs HJ, Cook RD. 1973. Frequency-dependent selection at the Payne inversion in *Drosophila melanogaster. Evolution* 27:558-564.

O'Donald P. 1973. Frequency-dependent sexual selection as a result of variations in fitness at breeding time. *Heredity* 30:351–368.

O'Donald P, Majerus MEN, Clarke BC, Partridge L, Robertson A, Clarke BC, Partridge L. 1997. Frequency-dependent sexual selection. *Philos. Trans. R. Soc. Lond. B Biol. Sci.* 319:571–586.

Ohta T, Kimura M. 1970. Development of associative overdominance through linkage disequilibrium in finite populations. *Genet. Res.* 16:165–177.

Otto SP, Lenormand T. 2002. Resolving the paradox of sex and recombination: Evolution of sex. *Nat. Rev. Genet.* 3:252–261.

Otwinowski J, McCandlish DM, Plotkin JB. 2018. Inferring the shape of global epistasis. *Proc. Natl. Acad. Sci. U.S.A.* 115:E7550–E7558.

Pearse DE, Barson NJ, Nome T, Gao G, Campbell MA, Abadía-Cardoso A, Anderson EC, Rundio DE, Williams TH, Naish KA, et al. 2019. Sex-dependent dominance maintains migration supergene in rainbow trout. *Nat. Ecol. Evol.* 3:1731–1742.

Pei Y, Forstmeier W, Knief U, Kempenaers B. 2023. Weak antagonistic fitness effects can maintain an inversion
polymorphism. *Mol. Ecol.* 32:3575–3585.

Pennell MW, Kirkpatrick M, Otto SP, Vamosi JC, Peichel CL, Valenzuela N, Kitano J. 2015. Y Fuse? Sex Chromosome
Fusions in Fishes and Reptiles. *PLOS Genet.* 11:e1005237.

Pool JE. 2015. The Mosaic Ancestry of the *Drosophila* Genetic Reference Panel and the *D. melanogaster* Reference
Genome Reveals a Network of Epistatic Fitness Interactions. *Mol. Biol. Evol.* 32:3236–3251.

Pool JE, Braun DT, Lack JB. 2017. Parallel Evolution of Cold Tolerance within *Drosophila melanogaster*. *Mol. Biol.*
Evol. 34:349–360.

Poul YL, Whibley A, Chouteau M, Prunier F, Llaurens V, Joron M. 2014. Evolution of dominance mechanisms at a
butterfly mimicry supergene. *Nat. Commun.* 5:5644.

Ragland GJ, Armbruster PA, Meuti ME. 2019. Evolutionary and functional genetics of insect diapause: a call for
greater integration. *Curr. Op. Insect Sci.* 36:74–81.

Reinhardt JA, Kolaczkowski B, Jones CD, Begun DJ, Kern AD. 2014. Parallel Geographic Variation in *Drosophila*
melanogaster. *Genetics* 197:361–373.

Reinhart M, Carney T, Clark AG, Fiumera AC. 2015. Characterizing Male–Female Interactions Using Natural Genetic
Variation in Drosophila melanogaster. *J. Hered.* 106:67–79.

Rest JS, Morales CM, Waldron JB, Opulente DA, Fisher J, Moon S, Bullaughey K, Carey LB, Dedousis D. 2013.
Nonlinear Fitness Consequences of Variation in Expression Level of a Eukaryotic Gene. *Mol. Biol. Evol.*
30:448–456.

Rice WR. 1992. Sexually antagonistic genes: experimental evidence. *Science* 256:1436–1439.

Rice WR. 1996. Sexually antagonistic male adaptation triggered by experimental arrest of female evolution. *Nature*
381:232–234.

Rose MR. 1982. Antagonistic pleiotropy, dominance, and genetic variation. *Heredity* 48:63–78.

Rowe L, Chenoweth SF, Agrawal AF. 2018. The Genomics of Sexual Conflict. *Am. Nat.* 192:274–286.

Ruzicka F, Hill MS, Pennell TM, Flis I, Ingleby FC, Mott R, Fowler K, Morrow EH, Reuter M. 2019. Genome-wide
sexually antagonistic variants reveal long-standing constraints on sexual dimorphism in fruit flies. *PLOS*
Biol. 17:e3000244.

Said I, Byrne A, Serrano V, Cardeno C, Vollmers C, Corbett-Detig RB. 2018. Linked genetic variation and not genome
structure causes widespread differential expression associated with chromosomal inversions. *Proc. Natl.*
Acad. Sci. U.S.A. 115:5492–5497.

Saunders DS, Richard DS, Applebaum SW, Ma M, Gilbert LI. 1990. Photoperiodic diapause in *Drosophila*
melanogaster involves a block to the juvenile hormone regulation of ovarian maturation. *Gen. Comp.*
Endocrinol. 79:174–184.

Saunders PA, Neuenschwander S, Perrin N. 2019. Impact of deleterious mutations, sexually antagonistic selection,
and mode of recombination suppression on transitions between male and female heterogamety. *Heredity*
123:419–428.

Schaeffer SW, Goetting-Minesky MP, Kovacevic M, Peoples JR, Graybill JL, Miller JM, Kim K, Nelson JG, Anderson
WW. 2003. Evolutionary genomics of inversions in *Drosophila pseudoobscura*: Evidence for epistasis. *Proc.*
Natl. Acad. Sci. U.S.A. 100:8319–8324.

Schmidt PS, Paaby AB, Heschel MS. 2005. Genetic Variance For Diapause Expression And Associated Life Histories
In *Drosophila melanogaster*. *Evolution* 59:2616–2625.

Sprengelmeyer QD, Mansourian S, Lange JD, Matute DR, Cooper BS, Jirle EV, Stensmyr MC, Pool JE. 2020.
Recurrent Collection of *Drosophila melanogaster* from Wild African Environments and Genomic Insights
into Species History. *Mol. Biol. Evol.* 37:627–638.

Stearns FW. 2010. One Hundred Years of Pleiotropy: A Retrospective. *Genetics* 186:767–773.

Sturtevant AH. 1921. A Case of Rearrangement of Genes in *Drosophila*. *Proc. Natl. Acad. Sci. U.S.A.* 7:235–237.

Sturtevant AH, Beadle GW. 1936. The Relations of Inversions in the X Chromosome of *Drosophila melanogaster* to
Crossing Over and Disjunction. *Genetics* 21:51.

Sturtevant AH, Mather K. 1938. The Interrelations of Inversions, Heterosis and Recombination. *Am. Nat.* 72:447–
452.

Surmacki A, Ożarowska-Nowicka A, Rosin ZM. 2013. Color polymorphism in a land snail Cepaea nemoralis
(Pulmonata: Helicidae) as viewed by potential avian predators. *Naturwissenschaften* 100:533–540.

Sved JA. 1968. The Stability of Linked Systems of Loci with a Small Population Size. *Genetics* 59:543–563.

Tatarenkov A, Healey CIM, Grether GF, Avise JC. 2008. Pronounced reproductive skew in a natural population of
green swordtails, *Xiphophorus helleri*. *Mol. Ecol.* 17:4522–4534.

Thain D, Tannenbaum T, Livny M. 2005. Distributed computing in practice: the Condor experience. *Concurr.*
Comput. Pract. Exp. 17:323–356.

Untergasser A, Cutcutache I, Koressaar T, Ye J, Faircloth BC, Remm M, Rozen SG. 2012. Primer3—new capabilities
and interfaces. *Nucleic Acids Res.* 40:e115.

Van der Auwera GA, O'Connor BD. 2020. Genomics in the Cloud: Using Docker, GATK, and WDL in Terra. O'Reilly
Media, Incorporated.

Wang J, Wurm Y, Nipitwattanaphon M, Riba-Grognuz O, Huang Y-C, Shoemaker D, Keller L. 2013. A Y-like social
chromosome causes alternative colony organization in fire ants. *Nature* 493:664–668.

Wellenreuther M, Bernatchez L. 2018. Eco-Evolutionary Genomics of Chromosomal Inversions. *Trends Ecol. Evol.*
33:427–440.

White MJD. 1973. Animal Cytology and Evolution. 3rd ed. Cambridge University Press. Available from:
https://wellcomecollection.org/works/meqhhay5

Wittmann MJ, Bergland AO, Feldman MW, Schmidt PS, Petrov DA. 2017. Seasonally fluctuating selection can
maintain polymorphism at many loci via segregation lift. *Proc. Natl. Acad. Sci. U.S.A.* 114:E9932–E9941.

Wright AE, Dean R, Zimmer F, Mank JE. 2016. How to make a sex chromosome. *Nat. Commun.* 7:1–8.

Yamamoto A, Huang W, Carbone MA, Anholt RRH, Mackay TFC. The Genetic Basis of Incipient Sexual Isolation in
Drosophila melanogaster. *Proc. Royal Soc. B* 291:20240672.

Yassin A, Bastide H, Chung H, Veuille M, David JR, Pool JE. 2016. Ancient balancing selection at tan underlies female
colour dimorphism in Drosophila erecta. *Nat. Commun.* 7:10400.

Zajitschek F, Connallon T. 2018. Antagonistic pleiotropy in species with separate sexes, and the maintenance of
genetic variation in life-history traits and fitness. *Evolution* 72:1306–1316.

Zhao L, Charlesworth B. 2016. Resolving the Conflict Between Associative Overdominance and Background
Selection. *Genetics* 203:1315–1334.

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