Multiunit frontal eye field activity codes the visuomotor transformation, but not gaze prediction or target memory, in a delayed saccade task

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Number of Pages: 45
Number of main Figures: 10
Number of Supplementary Figures: 2
Number of Words (Significance Statement): 112
Number of Words (Abstract): 220
Number of Words (Introduction): 1198
Number of Words (Discussion): 1879
Number of words (all): 9434

Running title: FEF multi-unit activity codes visuomotor transformations for gaze

Conflict of Interest: The authors declare no conflicts of research.

Key Words: Eye movements, Frontal Cortex, Single-unit, Multi-unit, Macaques

ABSTRACT

Single-unit (SU) activity — action potentials isolated from one neuron — has traditionally been employed to relate neuronal activity to behavior. However, recent investigations have shown that multi-unit (MU) activity — ensemble neural activity recorded within the vicinity of one microelectrode — may also contain accurate estimations of task-related neural population dynamics. Here, using a well-established model-fitting approach, we compared the spatial codes of SU response fields with corresponding MU response fields recorded from the frontal eye fields (FEF) in head-unrestrained monkeys (*Macaca mulatta*) during a memory-guided saccade task. We focused on characterizing the visuomotor transformation from Target-in-Eye coordinates to future Gaze-in-Eye coordinates (Sajad et al., 2015). Most SU *visual* response fields coded targets (with some predicting Gaze), whereas the MU population only coded targets. Most SU *motor* responses coded Gaze, but many still retained a target code. In contrast, MU motor activity predominantly coded Gaze with very little target coding. Finally, both SU and MU populations showed a progressive transition through intermediate 'Target-to-Gaze' codes during the delay period, but the MU activity showed a 'smoother' transition. These results confirm the theoretical and practical potential of MU activity recordings as a biomarker for fundamental sensorimotor transformations (e.g., Target-to-Gaze coding in the oculomotor system), while also highlighting the importance of SU activity for coding more cognitive (e.g., predictive / memory) aspects of sensorimotor behavior.

SIGNIFICANCE STATEMENT

Multi-unit recordings (undifferentiated signals from several neurons) are relatively easy to record and provide a simplified estimate of neural dynamics, but it is not clear which single-unit signals are retained, amplified, or lost. Here, we compared single-/multi-unit activity from a well-defined structure (the frontal eye fields) and behavior (memory-delay saccade task), tracking their spatial codes through time. The progressive transformation from target to gaze coding observed in single-unit activity was retained in multi-unit activity, but gaze prediction (in the visual response) and target memory (in the motor response) were lost. This suggests that multi-unit activity provides an excellent biomarker for healthy sensorimotor transformations, at the cost of missing more subtle cognitive signals.

INTRODUCTION

In systems neuroscience, it is common to estimate neuronal population dynamics by relating recordings of neuronal activity to some concurrent task or behavior. Traditionally, neuroscientists have isolated single-unit (SU) action potentials of individual neurons from raw recorded background noise, based upon its unique spike shape; a process called spike-sorting. Recently, however, there has been increased interest in the use of multi-unit (MU) activity (i.e., unsorted signals recorded from the tip of an electrode, which may arise from several nearby neurons (Buzsáki, 2004; Panzeri et al., 2015; Quian Quiroga and Panzeri, 2009; Rossi-Pool and Romo, 2019). It has been suggested that MU activity

recordings have practical and theoretical implications for experimental and applied electrophysiology (Ahmadi et al., 2021; Choi et al., 2010; Fraser et al., 2009; Leuthardt et al., 2021; Mattia et al., 2010; Sharma et al., 2015; Smith et al., 2013; Trautmann et al., 2019; Zhang and Constandinou, 2021). However, it remains unclear what is highlighted, and what is obliterated, when one combines the activity of several neurons into one conglomerate signal. Our aim was to test this question in a well-defined sensorimotor system (the frontal eye fields, FEF), task (memory-delay saccades), and analytic technique, as described in detail below.

Although SU recordings remain important for many applications, they pose both practical and theoretical challenges. The detection and extraction of SU amongst a sea of extracellular signals is often hindered by variability in spike shape / amplitude, and extraneous background noise (Lewicki, 1994; Mtetwa and Smith, 2006). Isolation of single action potentials is further confounded by overlapping spikes, making it hard to identify and classify spikes (Mtetwa and Smith, 2006; Quiroga et al., 2004; Rossi-Pool and Romo, 2019). These are time-consuming procedures that normally can only be done after recordings are complete. Further, neurons do not work in isolation, but as ensembles forming functional networks (Buzsáki, 2010; Edelman, 1987; Hebb, 1949; Levy et al., 2020; Miller et al., 2014; Molotchnikoff et al., 2019; Singer, 2013).

MU activity analysis sidesteps these challenges by avoiding the need to identify unique spike waveforms. The process of extracting / sorting MU activity is more reproducible since it does not eliminate data or depend on specific sorting techniques / parameters. Some studies found that MU activity provided a more stable signal with higher spatial resolution than SU activity (Drebitz et al., 2019; Lewicki, 1998; Sharma et al., 2015; Xing

et al., 2009). Further, MU activity profiles are similar to local field potential (LFP) signals

but tend to show less correlation between nearby neurons (Ahmadi et al., 2021; Burns et

al., 2010; Drebitz et al., 2019; Telenczuk and Destexhe, 2020). Finally, MU analysis is

capable of decoding the task and behavior by reducing the dimensionality of neural states

(Quian Quiroga and Panzeri, 2009; Rossi-Pool and Romo, 2019; Smith et al., 2013;

Trautmann et al., 2019). Therefore, MU activity analysis has become popular for

applications such as brain-machine interfaces, recording paralytic motor activity (Gilja et

al., 2015; Pandarinath et al., 2017) and other clinical / preclinical trials (Christie et al.,

2015; Fraser et al., 2009; Kao et al., 2017; Todorova et al., 2014). Some research

suggests that MU activity sometimes contains more accurate estimates of neural

population dynamics (Sharma et al., 2015; Trautmann et al., 2019). However, it remains

unclear which signals are retained, and which are lost, when one switches from SU to MU

analysis.

The gaze control system provides an ideal model system to compare the SU *vs.* MU

codes, because spatiotemporal codes have already been described at the SU level.

Neurons in higher-level gaze structures [superior colliculus (SC), lateral intraparietal

cortex (LIP), frontal eye fields (FEF) and supplementary eye fields (SEF)] show separate

visual and motor responses when a memory delay separates visual target presentation

and saccade initiation (Gnadt et al., 1991; Heusser et al., 2022; Schall, 2015; Umeno and

Goldberg, 2001; White et al., 1994). Further, these responses are spatially organized into

visual and motor response fields (Andersen et al., 1992; Hafed et al., 2023; Schall, 2015;

Schlag and Schlag-Rey, 1987; Sommer and Wurtz, 2001). Finally, although results vary

with task, higher-level visuomotor structures primarily show eye-centered response fields

(Andersen et al., 1985; Caruso et al., 2018a, 2018b; Constantin et al., 2007; Keith et al.,

2009; Mullette-Gillman et al., 2005; Park et al., 2006; Snyder, 2005). For example, the

FEF and SEF, located in dorsolateral and medial frontal cortex, show predominantly eye-

centered sensory / motor response fields for visual targets / saccades respectively (Peck

et al., 1995; Caruso et al., 2021).

We have used a model-fitting approach (fitting various spatial models against response

field data) to track sensorimotor transformations in the gaze system through time (Keith

et al., 2009; Sadeh et al., 2020, 2015; Sajad et al., 2016, 2015). In contrast to decoding

techniques, which allow one to extract information from noisy neural populations (Fraser

et al., 2009; Meyers, 2013; Bremmer et al., 2016; Brandman et al., 2017; Dong et al.,

2023), this technique tests the original spatial code used by individual neurons or

populations (Ahmadi et al., 2021; Burns et al., 2010; Drebitz et al., 2019; Keith et al.,

2009). Initial investigations in SC and FEF confirmed a distributed, eye-centered

transformation from target (Te) coding in visual response fields to future gaze (Ge) coding

in the saccade motor response. When a spatial 'T-G' continuum between Te and Ge was

used to track these codes through time, they showed a progressive transition from target

to gaze coding at the population level (Sadeh et al., 2018, 2015; Sajad et al., 2016, 2015),

even without a memory delay (Sadeh et al., 2020). But not all cells showed this transition:

some visual response predicted Ge and some motor responses retained Te. Recently,

this technique was applied to FEF / SEF response fields in the presence of background

landmarks (**Fig. 1A).** Although background stimuli produced various modulations (Schütz

et al., 2023), the data still showed a strong T-G transformation (Bharmauria et al., 2021,

2020). Therefore, we deemed this might provide an ideal dataset to test the relative

robustness of sensorimotor codes derived from SU versus MU activity.

Here, we analyzed the spatial codes of SU and MU activity derived from the same FEF

recording sessions (Bharmauria et al., 2020). After isolating SU and MU activity (Drebitz

et al., 2019; Quiroga et al., 2004), we applied our model-fitting approach to test their visual

and motor response fields. After confirming that SU / MU visual and motor population

codes were best characterized overall by the Te and Ge models respectively, we used

the 'T-G' spatial continuum between these models to characterize, quantify and compare

the spatiotemporal progression of SU *vs.* MU activity coding schemes (DeSouza et al.,

2011; Keith et al., 2009; Sadeh et al., 2015; Sajad et al., 2015). We found that the MU

and SU response fields show similar spatial codes and spatiotemporal transformations,

but MU showed a 'smoother' sensorimotor transition and lacked certain nuances (i.e.*,*

gaze prediction in visual responses and residual target signals in motor responses),

resulting in a 'cleaner' sensorimotor transition. We conclude that MU activity could provide

a practical, quick, and reliable biomarker for basic sensorimotor transformations but may

lack certain nuances important for the more cognitive aspects of sensorimotor behavior.

MATERIALS AND METHODS

Most experimental and analytic details of this study were published previously in analysis

of SU response fields in the FEF (Bharmauria et al., 2020). These are summarized here

along with specific details related to the MU activity response field analysis.

Surgical Procedures

All experimental protocols were approved by the York University Animal Care Committee

and were in alignment with the guidelines of Canadian Council on Animal Care on the

use of laboratory animals. Neural data used in this study were gathered from two female

Macaca mulatta monkeys (Monkey V and Monkey L). Two 3D search coils, each with a

diameter of 5 mm, were implanted in the sclera of the left eye of the respective animal.

The recording chambers in the FEF of both animals were implanted and centered at 25

mm anterior and 19 mm lateral. Surgeries were performed as previously done (Crawford

et al., 1999; Klier et al., 2003). There was a craniotomy (19 mm diameter) beneath each

chamber that allowed access to the right FEF. During the experiment, animals were

placed in custom-designed chairs which allowed free head movements. To prevent

animals from rotating in the chair, they wore a vest fixed to the chair. Furthermore, animals

were placed in the setup with three orthogonal magnetic fields with two orthogonal cells

mounted on their heads (Crawford et al., 1999). These fields induced a current in each

coil. The amount of current induced by one of the fields is proportional to the area of the

coil parallel to this field. This allowed us to derive the orientation of each coil in relation to

the magnetic fields, as well as other variables including eye orientations, head velocities

and eye and head accelerations (Crawford et al., 1999)

Behavioral Paradigm

We chose the following paradigm for the current study because it provides a visually rich,

noisy dataset for extraction of spatial codes and has already been applied to an existing

dataset of FEF recordings. We employed head-unrestrained gaze shifts (i.e., including

coordinated eye saccades and head motion) to separate signals organized relative to eye,

head, or space coordinates. Visual stimuli were presented using laser projections on a

flat screen that was placed 80 cm away from the animal **(Fig. 1A).** The monkeys

performed a memory-guided gaze task in which animals were trained to remember a

target relative to a visual allocentric landmark (displayed using two intersecting lines).

This led to a temporal delay between the target presentation and eye movement initiation.

This allowed us to independently analyze visual (aligned to target) and eye-movement-

related (saccade onset) responses in the FEF. The experiments were conducted in a dark

room to prevent any extraneous allocentric cues. Each trial began with the animal fixating

on a red dot in the center of the screen for 500 ms in the presence of a landmark. A brief

flash of the visual target (T, white dot) followed for 100 ms, then a 300 ms delay, followed

by a grid-like mask for 200 ms (this concealed past visual traces, and current and future

landmarks) and a second memory delay (200-600 ms). The disappearance of the red

fixation dot signaled the animal to perform a head-unrestrained saccade (indicated by the

solid white arrow) toward the memorized location of the target either in the presence of a

shifted landmark (broken pink arrow, 90 % of trials shifted in one of the eight radial

directions by 8°) or a non-shifted landmark (10 %, zero-shift condition, i.e., landmark

position did not change as before mask). The saccade targets were flashed one-by-one

in a random manner throughout a neuron's response field. The details of the task are

outlined in **Figure B1-B2**. In the shift condition, where the shifted target (T') was fixed to

the landmark, the animal was rewarded with a water-drop when its gaze (G) landed within

8-12° radius of the original target (animals were rewarded if they looked at T, T', or

anywhere in between). This large reward window is what allowed variability in the

memory-guided gaze shifts and error accumulation (Gnadt et al., 1991; Sajad et al., 2015;

White et al., 1994), and thus formed the logical base of our analysis (see below).

A

500 ms Fixation

100 ms Target on

300 ms Delay

200 ms Mask

NO SHIFT

200-600 ms Delay

GO signal

SHIFT

200-600 ms Delay

GO signal

Time

T = original target location   T' = virtual target location (fixed to shifted landmark)

B1

Vertical (degree)

Fixation Point

Fixation Point Jitter

T' G T

Horizontal (degree)

B2

Vertical (degree)

8°shift

11°

Horizontal (degree)

✛ Original Landmark   ● Original Target   ✛ Shifted Landmark   ⬭ Virtual Target

Figure 1: Representation of the experimental task and behavior. A, Cue-conflict paradigm, and its time course. The monkey began the task by fixating on a red dot for 500 ms while a landmark (white, intersecting lines) was present on the screen. Next, a target (white dot) was flashed for 100 ms, followed by a 300 ms memory delay where the target disappeared from the screen. After a 200 ms grid-like mask and another memory delay (200-600 ms), the monkey was cued by the disappearance of the fixation dot (i.e., go signal) to saccade head-unrestrained toward the remembered target location either

*when the landmark was shifted (represented by the broken pink arrow) or when it was not shifted. The monkey was rewarded when they placed their gaze (G) within a radius of 8-12º around the original target [at T (original target), T' (virtually shifted target fixed to shifted landmark) or between T and T']. The reward window was centered on T so that behavior was not biased. Note that the actual landmark shift was 8º, but it has been exaggerated in the schematic figure for clarity. The pink-colored objects are only used in the schematic figure for purposes of representation. **B1**, Representation of a gaze shift (pink curve) from the initial fixation point (red dot) toward the virtual target (dotted pink circle) fixed to shifted landmark (pink cross). G represents the final gaze location, and the yellow square represents the area in B2. The dotted circle stands for the jitter of the initial fixation points on the screen from one trial to another. **B2**, Representation of all (four) possible landmark (black cross) locations and shifted landmark (pink cross, relative to the original landmark location) locations for an example target (black dot). The landmark was presented 11º around the original target in one of four oblique directions. The shifted landmark was presented 8º around the original landmark location in one of eight radial directions.*

The response fields were tested roughly across horizontal and vertical dimensions (rectangular range of 30-80°). For both animals, there was a high correlation between the direction of the target and the gaze in both dimensions. This implies that that their gaze was aimed toward the vicinity of the T.

Electrophysiological and Behavioral Recordings

We recorded acutely from the FEF, a gaze area associated with sensorimotor transformations (Caruso et al., 2018b; Siegel et al., 2015). Extracellular activity was recorded by lowering tungsten electrodes (0.2–2.0 mΩ impedance, FHC Inc.) into the FEF [using Narishige (MO-90) hydraulic micromanipulator] using the Plexon MAP System. The recorded activity was then digitized, amplified, filtered, and saved for offline spike sorting (using template matching). The recorded sites (in head-restrained conditions) were further confirmed using a low-threshold electrical microstimulation (50 µA) as used previously (Bruce et al., 1985)**.** A superimposed pictorial of the recorded sites from both

Figure 2: FEF recordings ***A,*** *Acute FEF recordings were done with a single tungsten electrode.* ***B,*** *Overlapped sites of neural recordings from two animals [Monkey V, MV and Monkey L, ML]. Curved lines denote the arcuate sulcus.* ***C,*** *Top 10 % (with 95 % confidence interval) spike density plots for SU (red) and MU (dark red) activity for visual neurons. Blue line indicates the target onset.* ***D,*** *Same as C but for motor neurons. Blue line stands for saccade onset. Note: the top 10 % activity from each neuron was taken and then pooled across all neurons.*

animals is presented in **Figure 2A**-**B** (Monkey L in Blue and Monkey V in red)**. Figure 2C-D** displays the overlapped and averaged spike density plots for top 10 % (for each neuron and MU site) trials for the SU and MU. An average of 331 ± 156 (mean ± SD) trials/neuron were recorded. Mostly, the monkeys were free to scan the environment (head-unrestrained) while neurons were searched for.

The experiment started once a neuron had reliable spiking activity. The visual or motor response field of a neuron was characterized while the animals performed memory-guided gaze shifts. These gaze shifts started from an initial fixation location to a target (which was randomly flashed one-by-one, generally contralateral to the recording site) within an array (that varied between 4 × 4 to 7 × 7 depending on the size and shape of the response field) of targets (5 –10° apart from each other). The initial fixation locations were jittered within a 7-12° window, which increased variability of 3D gaze, eye, head

distributions to initial fixation and the displacements. For our analysis, this variation

allowed for separation between effectors and the space-fixed and eye-centered frames

of reference for target and gaze (Keith et al., 2009; Sajad et al., 2020). It should be noted

that there was no correlation between the initial gaze location and final gaze errors.

The 3D coil signals were sampled at 1000 Hz to measure eye and head orientation in

space (Bharmauria et al., 2021, 2020). Gaze (the 2D pointing direction of the eye in space)

and eye-in-head positions were derived from these signals (Crawford et al., 1999). When

conducting eye movement analysis, the saccade onset (eye movement in space) was

marked as the point in time when the gaze velocity increased above 50°/s, while the gaze

offset was marked as the point in time when the velocity decreased below 30°/s. The

head movement was marked from the saccade onset up to the point in time when the

head velocity decreased below 15°/s.

Single- (SU) and Multi-unit (MU) activity sorting

We manually isolated the SU activity from the saved neural recordings using template

matching and further confirming it with principal component analysis (PCA). We only

carried forward those neurons that had a relatively constant template throughout

recording. As the MU cluster comprises different spikes, it generally has a lower amplitude

than the individual spikes sorted from it. We re-thresholded the high-pass filtered raw data

to isolate the MU activity from the 40 kHz signal with a spike detection threshold of 3.5

standard deviations (SDs). This procedure led us to spiking activity recorded from several

neurons recorded within a vicinity of ~100–200 μm around the electrode tip, thereby

allowing us to discriminate the spikes above the noise level (Bullock, 1997; Burns et al.,

2010; Buzsáki, 2004; Land et al., 2013; Mattia et al., 2010).

Data Inclusion Criteria and sampling window

Only neurons (or MU sites) that were clearly isolated and task-modulated were analyzed

i.e., SU / MU with clear visual activity and / or with perisaccadic movement **(Fig. 2C-D)**.

Neurons with only post-saccadic activity (activity after the saccade onset) or that lacked

significant spatial tuning (see 'testing for spatial tuning' below) were excluded from the

analysis. While trials where monkeys landed their gaze within the reward acceptance

window were included, we excluded trials when the gaze end points went beyond 2°

distance from the average gaze endpoint for a given target. In conducting neural activity

analysis, the "visual epoch" referred to a fixed 100 ms window of 80-180 ms aligned to

the target onset, and the "movement period" referred to a high-frequency perisaccadic

100-ms (-50 - +50 ms relative to saccade onset) window (Sajad et al., 2015). This allowed

us to have a good SNR ratio for neuronal activity analysis, and most likely corresponded

to the epoch during which gaze shifts influenced neural activity.

Fitting Neural Response Fields Against Spatial Models

In order to test between different spatial models, they must be experimentally separable

(Keith et al., 2009; Sajad et al., 2015). For instance, in our paradigm, the variability

induced by memory-guided gaze shift end-points allows one to discriminate target coding

from the gaze coding, natural variations in initial eye and head locations allow one to

distinguish between different egocentric reference frames, and variable eye and head

components for the same gaze shift permit the separation of different effectors (Crawford

et al., 1999; Keith et al., 2009). In our method, we use these experimentally derived

measures as coordinate systems to analyze neural response field data and then

discriminate which spatial model best describes the data.

The logic of our response field fitting in different reference frames is schematized in

Figure 3A. If the response field data is plotted in the correct / best coordinate system,

this should yield a uniform distribution of data with low residuals (i.e., errors between the

actual data and a mathematical fit made to these data) **(Fig. 3A**, left**)**. On the other hand,

if the coordinate system / fit does not match the data well, this will lead to higher residuals

(Fig. 3A, right**)**. For example, if an eye-fixed response field is computed in eye-

coordinates, this should yield lower residuals compared with head or space coordinates

(Sajad et al., 2015). **Figure 3B** represents one head-unrestrained trial (left).

*Figure 3: Schematic representation of spatial model fitting procedure. **A**, Illustration of the spatial model fitting technique. The X-axis is the coordinate frame, and the Y-axis is the associated activity to the target. If the activity (blue data points) related to a fixed target is plotted in the correct coordinate frame (left), it yields lower residuals. On the other hand, activity that is plotted in an incorrect coordinate frame, leads to higher residuals (right). **B**, Illustration of the task and gaze influence for a single trial. The black dot depicts the projection of an initial fixation point, and the pink dot represents the target position (T) in relation to the original landmark (L) position (dotted intersecting lines). The solid intersecting lines correspond to the*

shifted landmark (L') position and the purple dot depicts the final gaze endpoint (G). An
egocentric T-G continuum was plotted to compute the gaze influence by designating the
space between T and G into ten uniform steps.

For the actual analysis, we employed a non-parametric fitting method to characterize the

neural activity with reference to a specific spatial coordinate system and varied the spatial

bandwidth (kernel 2-25°) of the fit to plot any response field size, shape, or contour (Keith

et al., 2009). We tested between various spatial models using Predicted Residual Error

Some of Squares (PRESS) statistics. In this method, the residual for a trial is computed

by comparing the actual activity relative to fits computed from other trials (similar to cross-

validation). For a given neuron and temporal window (**Fig. 2**), this was done for all trials,

for each bandwidth of fit and for each spatial model tested (e.g., Te, Ge etc.). The model

and bandwidth that yields the lowest residuals was deemed 'best.' The PRESS residual

of this model was then compared with the PRESS residuals of the other models at the

same kernel bandwidth using a two-tailed Brown-Forsythe test to test for significant

differences in the goodness of fit (typically, a significantly superior fit is only found in a

fraction of individual neurons). Finally, we performed the same statistical analysis (Brown-

Forsythe) at the population level by comparing the means of PRESS residuals across

neurons (DeSouza et al., 2011; Keith et al., 2009). (Significance is more often reached at

this level.).

'Cardinal' Models Tested

We first repeated the model-fitting analysis of the previous study (Bharmauria et al., 2020)

on SU and MU activity populations to confirm if Te and Ge were the overall best 'canonical'

models to represent response field activity in this task. [Note that in the recent

investigation (Schütz et al., 2023) these models were called $T_{F(e)}$ / $G_{F(e)}$ to specify the

Foveal coordinate origin (0,0), but this can be assumed here]. Again, these are not

theoretical models, but rather models that were derived from the experimental measures

described above. Possible egocentric models included target position *vs.* effector (gaze,

eye, head) displacement or position in three egocentric frames (See **supplementary**

Figure 1 for schematic representations). Specifically, Target in space, eye or head

coordinates (Ts, Te, Th); future gaze in space, eye, and coordinates (Ge, Gh, Gs); eye

displacement (dE), i.e. the difference between initial and final eye orientation relative to

the head; and head displacement (dH), i.e., the difference between initial and final head

orientation relative to space; and finally, future orientation of the head in space

coordinates (Hs). (We removed dG because it was indistinguishable from Ge in this

dataset). We did not test allocentric models (e.g., Target relative to landmark, Landmark

relative to Eye) here because they were statistically eliminated at the population level in

previous studies (Bharmauria et al., 2021, 2020; Schütz et al., 2023) and our goal here

was to test the population egocentric visuomotor transformation.

Intermediate spatial models: the TG continuum

Previous studies suggested that FEF responses do not exactly fit against spatial models

like Te or Ge, but actually may fit best against intermediate models between the canonical

ones (DeSouza et al., 2011; Sadeh et al., 2015; Sajad et al., 2016, 2015). The spatial

continuum between Te and Ge ('T-G continuum') provided the best overall description of

the data and a signature for the sensorimotor transformation, where G includes variable

errors relative to T (Sajad et al., 2015). This continuum was created by taking ten (10%)

steps between and beyond Te and Ge (**Fig. 3B**). Here, these T-G fits were then done at

each of these steps, and where the fit yields the lowest PRESS residuals, was considered

'best', as described above.

Note that even the best model would not be expected to have zero residuals, because of

uncontrolled factors such as biological / measurement noise, non-spatial factors such as

arousal / motivation levels (Sajad et al., 2020), and in the case of the motor response,

dynamics of the movement (van Opstal, 2023).

Testing for Spatial Tuning

The method described above works under the assumption that neuronal activity is

structured as spatially tuned response fields. Other neurons might implicitly sub-serve the

overall population code (Bharmauria et al., 2016a, 2014; Chaplin et al., 2018; Goris et al.,

2014; Leavitt et al., 2017; Pruszynski and Zylberberg, 2019; Zylberberg, 2018), but here

we were testing for explicit codes. Therefore, we confirmed the spatial tuning of neurons

before including them in further analysis. We tested for spatial tuning by randomly (100

times to obtain random 100 response fields) shuffling the firing rate data points across

the position data that we obtained from the best model. The mean PRESS residual

distribution ($PRESS_{random}$) of the 100 randomly generated response fields was then

statistically compared with the mean PRESS residual ($PRESS_{best-fit}$) distribution of the

best-fit model (unshuffled, original data). If the best-fit mean PRESS fell outside of the 95%

confidence interval of the distribution of the shuffled mean PRESS, then the neuron's

activity was deemed spatially selective. At the population level, the percentage of neurons

showing significant spatial tuning varied through time. Thus, we removed the time steps

where the populational mean spatial coherence (goodness of fit) was statistically

indiscriminable from the baseline (before target onset). We then defined an index

(Coherence Index, CI) for spatial tuning. CI for an SU / MU site, which was calculated as

(Sajad et al., 2015):

$$Coherence\ index = 1 - \left(\frac{PRESS_{bestfit}}{PRES_{random}}\right) \qquad (i)$$

If the PRESS$_{best-fit}$ was similar to PRESS$_{random}$ then the CI would be roughly 0, whereas if

the best-fit model is a perfect fit (i.e., PRESS$_{best-fit}$ = 0), then the CI would be 1. We only

included those SUs / MU sites in our analysis that showed significant spatial tuning.

Time-normalization for spatiotemporal analysis

In this task, the time between the onset of the target and the gaze onset was not equal

across trials because of a variable delay period. To accommodate this variable trial-time

for transformations between these events, we time-normalized the duration of each trial

(Bharmauria et al., 2021; Sajad et al., 2016). Accordingly, the neural activity across

different trials (between the events that we were interested in — 80 ms after the target

onset until the onset of saccade for whole population in **Figure 9**) was divided into 14

equal half overlapping bins (with a range of 112.26 – 178.93 ms depending on the trial).

If we aligned the trials in a standard way (relative to visual stimulus onset or saccade

onset), this would lead to the loss and/or mixing of neural activities across trials. The

rationale behind the bin number choice was to make sure that the sampling time window

was wide enough, and therefore robust enough, to account for the stochastic nature of

spiking activity. During this normalization procedure, the duration of the mask was also

convolved in time (on average from step 4.69 to step 7.63). Therefore, the time-

normalization procedure was performed to account for the different delay period and the

details of this procedure are provided in the previous study (Sajad et al., 2016). For this

analysis, the neural firing rate (in spikes/second; the number of spikes divided by the

sampling interval for each trial) was sampled at 14 half overlapping time windows from

these time-normalized data. The choice for sampling window numbers was based on the

approximate ratio of the duration of the visual burst to delay period to movement burst

(Sajad et al., 2016). The final (14th) time step in **Figure 9** also contained some part of the

perisaccadic sampling window as mentioned above. This time-normalization procedure

allowed us to consider the entire time-period (across different trials) of visual–memory–

motor responses as an aligned spatiotemporal continuum**.**

RESULTS

In the current study, we compared sensorimotor codes by fitting spatial models against

SU and MU activity derived from anatomically matched FEF populations. In summary,

we recorded task-related neural activity from 257 FEF sites in both animals and isolated

a total of 312 FEF units. After applying our exclusion criteria, including tests for spatial

tuning, 147 SUs (including visual, V; visuomotor, VM; and motor, M neurons) and the

corresponding 101 MU sites, respectively, were taken forward for analysis. Of these, 91

SU sites were accompanied by MU data and 59 MU sites were accompanied by SU data

for motor responses (the difference is due to the exclusion criteria). 63 SU sites were

accompanied by MU data and 52 MU sites were accompanied by SU data for visual

responses. The anatomic distributions of the SU and MU sites were nearly identical in

both animals (**Fig. 2B**). Finally, of the 147 SU sites, we analyzed 102 visual and 109

motor responses; and of the 101 MU sites, we analyzed 88 visual and 90 motor responses.

Summary of Overall Statistical Analysis of Egocentric Models

As a preliminary step, we first tested the Te and Ge models (the overall preferred models for sensory and motor activity in our previous study) against other potential egocentric models (target, eye, head, and gaze displacement or position coding in various egocentric frames of reference). Again, these tests are based on finding the model that yields the overall lowest residuals between our non-parametric fits and actual response field data, and the testing for significance relative to other models.

Figure 4 summarizes this result for both our SU (**Fig 4 A-B)** and MU (**Fig. 4C-D**) populations (see **Figures 5 and 6** below for example response field fits). The overall patterns for the SU and MU populations were similar: the visual response best codes for Te and the motor response best codes for Ge, as found previously in the SU activity study (Bharmauria et al., 2020). Data points below the horizontal line ($P = 0.05$) indicate models with worse fits. In the case of the visual responses, all other models were significantly eliminated in both population datasets. In the case of the motor responses, all models were significantly eliminated except for gaze displacement (dG, which is very similar to Ge in this dataset). This does not mean that these populations do not code for other variables in individual cells or in more subtle ways (Schütz et al., 2023) but shows that Te and Ge provide the best overall measures of their explicit population coding scheme. These results confirm the previous SU analysis and tend to suggest that MU populations show similar results. To further investigate this, a more in-depth analysis was performed based on the T-G continuum between the two best models.

Figure 4: P-Value statistics performed on the residuals of different egocentric models (Brown-Forsythe test) in FEF SU (A) visual and (B) motor responses. Same analysis for MU (C) visual and (D) motor responses. Target in eye (Te) is the best model for the visual response and Ge is the best model for the motor response in both the SU and MU activities. Best model: p = 10^0 = 1; the best-fit spatial model that yielded the lowest residuals. The horizonal line indicates p = 0.05. Models tested: the difference between the initial and the final head orientation relative to space (dH); the difference between the initial and the final eye orientation relative to the head (dE); future orientation of the head in space coordinates (Hs); Eye in head (Eh); Future gaze in space (Gs); Future gaze in head (Gh) Future gaze in eye (Ge); Target in space (Ts): Target in head (Th); Target in eye (Te).

Example comparisons of SU and MU activity response fields along the T-G continuum

Previously, it was shown that the major egocentric transformation occurs between target-to-gaze (T-G) by plotting response fields at intermediate steps between a T-G continuum (Bharmauria et al., 2020). Here, a similar analysis on the MU activity was done to compare it with the SU activity. **Figure 5** shows a typical visual response field analysis along the T-G continuum for SU and MU activity recorded at the same site. **Figure 5A** and **B** show the raster and spike density (gray and black curves; representing top 10% of responses) of an SU and the corresponding MU visual response aligned to the target onset (blue line and arrow), respectively. The shaded gray region is the sampling window (80-180 ms) for

the response field analysis. The SU response (firing frequency along the y-axis) is

considerably lower than the MU response (because this combined several neurons).

Figure 5C shows the best SU fit for the response field along the T-G continuum. The

response field best fits at T as indicated by the converging broken lines. Each circle

represents the response to one trial, where the bigger the circle, the higher the response.

The heat map represents the non-parametric fit to the data. Note that the main cluster of

large circles (and the corresponding red 'hot-spot' of the fit) is located in the upper-left

quadrant relative to center (0,0, i.e., initial fixation). This localized peak denotes the typical

'closed' response field often seen in FEF visual data. The residuals (difference between

the fit and each datapoint) are shown below the response fields.

Figure 5. Examples of SU and MU visual response field analysis. A and B, Raster/spike density plot (with top 10% of responses) of an SU and MU visual response aligned to target onset (blue arrow), respectively. The shaded gray region represents the sampling window (80-180 ms) for the response field analysis. C and D, Representation of the response field of SU, and MU visual activity along the T-G continuum, respectively. The size of the circle corresponds to the magnitude of the response and the heat map represents the non-parametric fit to the data (red area is the response field hot spot). The converging dotted lines indicate that both SU and MU fit best at exactly at T. 0, 0

 indicates the center of the coordinate system which yielded the lowest residuals (best fit).

 The graph at the bottom of C and D represents the respective residuals for the response

 field plots.

 Figure 5D shows the response field map of the corresponding MU, again with the best fit

 at T. In this case, the response fields of SU and MU activity were very similar (both

 showing similar 'closed' organization at the same location), showed the same best fits (T),

 and their fit residuals were qualitatively similar. Overall, this suggests that SU and MU

 activity might carry similar spatial information, but we will document this more thoroughly

 below.

*Figure 6. Examples of SU and MU motor response field analysis. **A** and **B**, Raster/spike density plot (with top 10% of responses) of an SU and the corresponding MU motor response aligned to the saccade onset (blue arrow), respectively. The shaded gray region is the sampling window (-50-50ms) for the response field analysis. **C** and **D**, Representation of the response field of SU and MU for motor response along the T-G continuum, respectively. The SU response field fits best at the 9th step from T and MU response field fits best at the 8th step. The graph at the bottom of C and D represents the respective residuals for the response field plots.*

Figure 6 shows a typical example of an SU and MU motor response field analysis from

the same recording site. **Figure 6A-B** shows the raster and spike density (same

conventions as **Figure 5** for visual analysis) of an SU (**Fig. 6A**) and MU activity (**Fig. 6B**)

for a motor response aligned to the saccade onset (blue line and arrow).

Figure 6C shows the response field fit of an SU along the T-G continuum. In this case

both the SU and MU response fields showed the typical 'open' pattern, with activity

continuing to increase away from the center of the coordinates. But in this case, they

peaked in different quadrants (upper-left for SU activity, upper-right for MU activity). This

suggests that the response field of MU was strongly influenced by other nearby neurons

(the second neuron, not shown, isolated from the same site had a response field hot-spot

in the second quadrant). However, both the SU and MU activities showed a similar best

fit point along the T-G continuum: one step from G (for SU activity) and two steps from G

(for MU activity), i.e., close to Ge. In short, despite their differences, both the SU and MU

motor responses utilized a similar code (future gaze relative to initial gaze). Collectively,

the above examples suggest that MU and SU activities carry comparable information.

Population analysis along the T-G continuum

To quantify how representative the above examples were, we plotted the overall

distribution of best fits for the SU and MU populations. **Figure 7A1** shows the distribution

of best fits for the SU visual responses (n = 96) along the T-G continuum with a primary

peak around T and a secondary smaller peak near G. Overall, the distribution fit around

T, though significantly shifted toward G (mean = 0.13; median = 0.10; p = 0.03, one

sampled Wilcoxon signed rank test). This suggests that the SU visual responses mostly

encoded the target, but some already predicted the future gaze location. The MU visual

distribution (n = 88, **Fig. 7A2**) still showed a small but significant shift from T toward G

(mean = 0.13, median = 0; one sampled Wilcoxon signed rank test p = 0.013). However,

whereas the primary peak near T was retained, the prominent secondary 'G' peak in SU

disappeared. This indicates that the MU visual response, comprising several closely

connected neurons, simply encodes the target position.

Figure 7. *Frequency distribution of SU and MU along the T-G continuum at the population level.* ***A1,*** *Frequency distribution of all spatially tuned SU visual responses (n = 96) with the best fit closer to T (mean = 0.13; median = 0.1).* ***A2,*** *Frequency distribution of all spatially tuned MU visual responses (n = 88) with the best fit closer to T (mean = 0.13; median = 0).* ***B1,*** *Frequency distribution of all spatially tuned SU motor responses (n = 103) with a shifted distribution toward G (mean = 0.57; median = 0.7).* ***B2,*** *Frequency distribution of all spatially tuned MU motor responses (n = 90 with a significantly shifted distribution toward G (mean = 0.77; median = 0.8).* ***C1,*** *The sum of two*

655
Gaussian distributions of SU (two tuning curves) and MU (one tuning curve) visual
responses. ***C2,*** *The sum of two Gaussian distributions of SU (two tuning curves) and MU*
(one tuning curve) motor responses. In both cases, the smaller secondary peak
disappeared.

Figure 7B1-B2 show the similar distributions for motor responses. The SU motor (n =

103) distribution had a primary peak near G and a smaller peak around T (suggesting

some retention of target information). Overall, the SU motor distribution was significantly

shifted toward G from T (mean = 0.57; median = 0.7; p < 0.0001, one sampled Wilcoxon

signed rank test) and was significantly different from the SU visual distribution (p < 0.0001,

Mann-Whitney U-test). The SU and MU motor distributions (n = 88, **Fig. 8B2**) also showed

a significant shift toward G (p < 0.0001, one sampled Wilcoxon signed rank test). The

shift in MU (mean = 0.77; median = 0.8) was somewhat larger than the SU shift (mean =

0.57; median = 0.7), likely because this time the secondary 'T' peak was diminished in

the MU data.

Figure 7C1-C2 superimposes the SU and MU Gaussian distributions for the visual and

motor fit frequency distributions shown above. In both cases, the primary peak (T for

visual, G for motor) is similar for SU and MU, but the secondary peak (G for visual, T for

motor) is missing in the MU population. Overall, there was no significant difference

between the entire SU and MU distributions for either visual (p = 0.922, Mann-Whitney U

test) and motor responses (p = 0.063, Mann-Whitney U test). These data support the

notion that MU visual and motor activities encode much 'pure' representations of T and

G respectively, without the secondary codes in the SU (a predictive G in the visual

response, and a retained T in the motor response).

Figure 8: Visuomotor transformation at the single and multi-unit level for visuomotor responses along the T-G continuum. *Movement best fit (y-axis) as a function of the corresponding visual best fit (x-axis) for VM neurons (A) and corresponding MU activity (B) sites. Each dot*

represents one neuron/site. The pink intersecting lines indicate the median of the best-fit
for the movement against the median of the best-fit for visual responses. The distribution
was significantly shifted toward G in both cases (p < 0.0001, Wilcoxon matched-pairs
signed rank test) suggesting visual-to-motor transformation from the target (T) to gaze (G)
coding in both cases. However, their (A, B) slopes and elevations were not significantly
different from each other, implying a similar profile of visual-to-motor transformations.

It is possible that the overall population shift from target to gaze coding could occur only

due to transference of activity from visual to motor cells, in SU activity this also occurs

within cells as well (Sadeh et al., 2015; Sajad et al., 2015). To test if MU activity shows

the same behavior, we contrasted visual and motor codes for neurons/sites that have

both visual and the motor responses (**Fig. 8**). **Figure 8A** shows the motor best fits (y-axis)

as a function of the visual fits (x-axis) for individual neurons. **Figure 8** illustrates the motor

best fits (y-axis) as a function of the visual fits (x-axis) for the MU sites. An upward /

leftward shift in these data suggests a transformation from target to gaze coding *within*

visuomotor cells (Sadeh et al., 2015; Sajad et al., 2015). In both cases (SU and MU

activity), most of the points and the intersection of medians (pink lines) were above the

line of unity, and this was significant at the population level ($p < 0.0001$, Wilcoxon

matched-pairs signed rank test) suggesting a visual-to-motor transformation in both cases.

Further, the slopes ($F = 0.23$, $p = 0.88$) and elevations ($F = 0.70$, $p = 0.40$) for SU and MU

distributions were not significantly different from each other, suggesting that SU and MU

activities reveal similar within-cell/site visuomotor transformation.

Site-matched Anatomic Comparison: Multi-unit *vs.* Single-unit

We next tested if these fit distributions were comparable for anatomically matched

recording sites. Note that the anatomic variance could arise from both 2D distribution of

recordings as well as cortical layer depth, which we could not measure accurately. For

this analysis only specific sites that contained both SU and MU fits were obtained for

visual and / or motor responses, taking the values the SU fits against the MU fits. From

Figure 7 we hypothesized that SU and MU sites might show some anatomical relation,

since there was no significant difference in their overall distributions. We did not find

significant correlation (**Supplementary Fig. 2**) for MU vs. SU for visual responses for

anatomically matched sites (Spearman R = 0.05, Slope = - 0.04 ± 0.08, P = 0.66).

However, a modest (Spearman R = 0.20, Slope = 0.10 ± 0.06) but insignificant (P = 0.053)

correlation was observed for motor responses. Overall, this suggests that variations in

the SU and MU fits do not reflect any anatomical variance in spatial coding.

Spatiotemporal Analysis

Finally, we performed the 14-step time-normalized analysis (Bharmauria et al., 2020) from

visual response until the saccade onset (**Fig. 9**) for both SU and MU activity (see

methods). This procedure permitted us to track the progression of T-G along the

 spatiotemporal domain. The gray curve represents the SU transformation along time (Bharmauria et al., 2020), whereas the black curve corresponds to the visuomotor

Figure 9. Spatiotemporal analysis at the populational level. Progression of the spatial code (gaze influence, mean ± SEM) along the T-G continuum with time (at different time steps) from visual response onset until the saccade onset.

There was a gradual and significant progression toward G for both SU (gray) and MU (black) activity.

transformation in the MU activity. In both cases, there was a gradual transition from T-G, however, in the case of the MU activity, the transition seems much 'smoother than the SU,' without the dips and rises seen during and after visual mask presentation. Specifically, in the SU activity, the code moves back and forth several times after time-step 6, but in the MU activity, the code is mostly maintained from time-step 8 (post-landmark shift) until the 14th step when the gaze was just imminent. Although subtle differences between the SU and MU data are evident at certain steps between SU and MU, there was no significant difference between the curves ($p > 0.05$, Mann-Whitney U-test).

DISCUSSION:

The aim of this study was to compare sensorimotor transformations derived from single-unit (SU) activity vs. multi-unit (MU) activity from the same FEF recording sessions, using data from a signal-rich memory-delay gaze task. Our analysis of visual and motor response fields (**Figs. 4-6**) results indicated that both SU and MU activity show a fundamental progression from target coding in the visual response to gaze coding in the motor response, except that MU activity does not reveal secondary characteristics, i.e., motor prediction in the sensory response and target location retention in the motor response (**Fig. 7**). This basic transformation was also evident *within* single SU / MU recording sites that showed both visual and motor activity (**Fig. 8**). Finally, SU and MU activity showed a similar temporal target-to-gaze progression during the memory delay,

but the transition in MU activity was somewhat 'smoother' (**Fig. 9**). One might conclude

that MU activity provides an accurate measure of the overall sensorimotor transformation

in our dataset (in some ways more clearly than SU activity), whereas SU activity contains

additional information that might prove important for more cognitive aspects of the task.

Multi-unit *vs.* Single-unit Activity

Recently, there has been increased interest in comparing SU and MU activity in both

animals and humans (Ahmadi et al., 2021; Burns et al., 2010; Christie et al., 2015; Drebitz

et al., 2019; Gilja et al., 2015; Pandarinath et al., 2017; Trautmann et al., 2019). For

example, Trautmann and colleagues (Trautmann et al., 2019) suggested that MU

recordings provide both the practical benefit eliminating spike sorting (required for SU

analysis) and reducing the dimensionality of the signal without losing important

information content. They performed this analysis on three sets of monkey data from

different labs (Ames et al., 2014; Churchland et al., 2012; Kaufman et al., 2014) and

reached the same conclusion. This fits with the theory of random projections from high-

dimensional statistics (Dasgupta and Gupta, 2003; Ganguli and Sompolinsky, 2012; Indyk

and Motwani, 1998; Lahiri et al., 2016), i.e., to recover the geometrical properties of a

low-dimensional manifold embedded in a high-dimensional space, one can bypass the

coordinates of the high-dimensional space. The results of our study tend to agree with

this conclusion, with certain caveats that we will discuss in more detail below.

Implications for Sensorimotor Control

As noted in the introduction, oculomotor scientists have spent many years studying the

transformation from visual target coding to the coding of saccade metrics in saccades

and head-unrestrained gaze shifts (Bruce and Goldberg, 1985; Everling and Munoz, 2000;

Gandhi and Katnani, 2011; Hanes et al., 1995; Sadeh et al., 2015; Sajad et al., 2015;

Schall, 2015; Umeno and Goldberg, 2001). Visual and motor tuning have been

dissociated by introducing various position or memory-related errors (Gnadt et al., 1991;

Heusser et al., 2022; Mays and Sparks, 1980; Umeno and Goldberg, 2001; White et al.,

1994), training animals to make 'antisaccades' opposite to the stimulus (Everling and

Munoz, 2000) or introducing an intervening saccade (Baizer and Bender, 1989; Camalier

et al., 2007). Some of these approaches introduce 'top-down signals that might alter the

circuitry involved (Gaymard et al., 1998; Munoz, 2002; Munoz and Everling, 2004; Pierrot-

Deseilligny et al., 2002), but more recent model-fitting and decoding analyses confirm a

transition from target-to-saccade coding in SC (Sadeh et al., 2018, 2015), FEF

(Bharmauria et al., 2020; Sajad et al., 2016, 2015), and SEF (Bharmauria et al., 2021)

activity, even in reactive gaze shifts to visual targets (Sadeh et al., 2020).

The current study shows that both SU and MU activity retain this target-to-gaze

transformation, even in the presence of a relatively complex stimulus array. A previous

analysis of the same dataset showed that some visual responses also encoded landmark

locations (Schütz et al., 2023) and the motor response was modulated by landmark shifts

(Bharmauria et al., 2020) but overall, Te to Ge was retained (Bharmauria et al., 2020).

Here, we showed that MU activity shows the same sensorimotor transformation (in some

ways 'cleaner', providing a 'purer' measure of target and gaze coding at the population

levels). Further, whereas the spatiotemporal progression of the SU data showed various

dips and rises during the delay period, perhaps related to microsaccades (Heusser et al.,

2022), the MU data showed a 'smoother' transition, suggesting a more robust

sensorimotor signature. Considering the relative ease of recording online MU activity

(without the need for offline spike sorting), this suggests that MU activity could be

sufficient for certain practical applications requiring low-dimensional information. For

example, MU activity could be observed to rapidly assess the health of sensorimotor

transformations during presurgical recordings in patient populations.

Implications for the Cognitive Aspects of Movement Control

Higher dimensional neural data from single electrodes may require pooling across several

simultaneously recorded MU channels to confidently estimate the neuronal population

dynamics (Gao and Ganguli., 2015; Trautmann et al., 2019). Here, specifically, the

secondary Ge code that was observed in some SU visual responses and the secondary

Te code that was observed in some motor responses (Bharmauria et al., 2020). These

secondary codes are dominated by the primary codes in population statistics (**Fig. 4)** and

likewise, they appeared to be 'drowned out' by the primary codes of most neurons in the

MU activity. Ge activity in the visual response could reflect internal noise that ends up

influencing variable errors in final gaze position (Sajad et al., 2020, 2016), but it has been

suggested that the prefrontal cortex is involved in the intentional prediction of future gaze

errors (Fu et al., 2023). Conversely, the retention of Te in the motor response could be

used for motor learning, updating perception and/or corrective saccades (Dash et al.,

2015; Lundqvist et al., 2018; Mohsenzadeh et al., 2016; Sajad et al., 2020; Wagner et al.,

2021).

Figure 10 shows a schematic circuit that could explain how these signals arise during a

memory-delay gaze paradigm, simplifying the process into serial visual, memory, and

motor circuits (these signals are both mixed and distributed in the real brain). The sensory

input to the visual circuit leads to predominantly eye-centered spatial tuning (red circles)

(Sajad et al., 2020; Mullette-Gillman et al., 2005; Snyder, 2005). Some poorly connected

neurons (empty red circles) exhibit no tuning (Barth and Poulet, 2012) but may still

contribute to population dynamics   (Bharmauria et al., 2016a; Levy et al., 2020;

Pruszynski and Zylberberg, 2019; Zylberberg, 2018). Finally, motor-tuned neurons (Ge)

in the visual circuit presumably receive feedback input from upstream memory and motor

circuits, exhibiting a strong gaze prediction (Masselink and Lappe, 2021; Sajad et al.,

2020; Stavisky et al., 2017).

The visual circuit relays information to the memory circuit, which in turn continuously

retains multiplexed signals and provides feedback to the visual circuit (Chatham and

Badre, 2015; Sajad et al., 2020). This circuit involves a loop between the LIP, dorsolateral

prefrontal cortex (DLPFC), and FEF (Christophel et al., 2017; Lundqvist et al., 2018;

Pinotsis et al., 2019). Finally, the system may monitor this feedback loop by up /

downregulating feedback gains when feedforward mechanisms fail to provide accurate

motor predictions (Franklin et al., 2012; Mathew and Crevecoeur, 2021; Shadmehr and

Mussa-Ivaldi, 1994; Wolpert et al., 2011). As noted above, some of these signals are

likely obscured in the MU response, resulting in a smoother T-G transition.

Figure 10: A neural circuit model. Visual neurons mostly encode the Target-in-eye coordinates (solid red); however, some neurons (light solid) may predict Ge due to continuous feedback from memory (pink) and motor (blue) circuits. Some neurons may remain untuned, but their role in

population dynamics cannot be overruled. The visual neurons pass information to memory circuits where continuous updating of the target occurs in the eye coordinates while providing continuous feedback to visual neurons. Memory activity passes the most recent memory to motor neurons to execute the gaze command. Motor neurons also provide feedback to visual circuits for corrective measures.

Lastly, when a gaze shift is cued, activity from the memory circuit is transferred to the motor circuits (blue) in a memory-motor transformation (Bharmauria et al., 2020). This has been shown to involve an additional population shift toward Ge coding (Sajad et al., 2016). Differences of Ge from Te may result from internal noise, endogenous inputs (top-down, updating) or exogenous influences from the internal world (Abedi Khoozani et al., 2022; Bharmauria et al., 2020; Schütz et al., 2023). The solid blue neurons produce the most accurate Ge command and thus potentiate the gaze shift, whereas the light solid blue neurons remain untuned. Importantly, some Te signals (empty blue circles) have passed through relatively unaffected, providing the system with an untainted visual memory signal for learning or use in subsequent saccades (Pruszynski and Zylberberg, 2019; Zylberberg, 2018; Barth and Poulet, 2012; Bharmauria et al., 2016a). Overall, the ensemble code shows a progressive transition from Te to Ge across the visual-memory-motor circuitry (Sajad et al., 2020).

General Implications for Population Coding

Neural data is fundamentally noisy, arising both from endogenous biological noise (Faisal et al., 2008) and from methodological constraints. In the cortex, neurons fire sparsely and exhibit emergent properties in relation to a task/stimulus, but not all activated neurons are necessarily part of the emergent network (Barth and Poulet, 2012; Bharmauria et al., 2016b; Buzsáki, 2010; Molotchnikoff et al., 2019; Singer, 2013). However, if a neural

population has homogenous properties, i.e., similar tuning curves, averaging the

ensemble activity of several neurons might provide a better estimate of the network's goal

(Quian Quiroga and Panzeri, 2009; Trautmann et al., 2019). Thus, this level of analyses

may work best for brain areas with homogeneous populations (Panzeri et al., 2015). This

suggests some degree of fundamental homogeneity in the signals we recorded here,

despite the relative lack of topography in the recording sites. Moreover, it may also

provide information about network level changes after brain damage (Chaudhary et al.,

2016) or neuroplasticity (Bharmauria et al., 2022; Kohn, 2007).

Even in the presence of dissimilar tuning curves, or underlying decorrelation, one might

still accurately estimate neural manifold geometries using MU channels (Panzeri et al.,

2015; Quian Quiroga and Panzeri, 2009). For example, the response field of the motor

neuron in **Figure 7C** has a hot-spot in the third quadrant, but the second neuron (not

shown) recorded from the same site had a hot-spot in the second quadrant. Despite this,

when their MU activity was analyzed, it was possible to create a population hot-spot and

determine its motor code (Ge). Consistent with our findings, it has been suggested that

only extreme anticorrelations between neural tuning curves disrupt accurate estimation

of population manifolds (Trautmann et al., 2019).

Conclusions:

The aim of this study was to test what is retained and what is lost in the methodological

transition from SU to MU analysis. An advantage here is that we were able to combine a

well-defined sensorimotor system, task, and analytic technique to compare signal coding

across both situations. Overall, we find that FEF MU activity carries an excellent

representation of the overall sensorimotor transformation for memory-guided gaze shifts

but loses some nuances that may be important for the more cognitive aspects of the task.

We conclude that MU activity has advantages for applications that must prioritize time

over sophistication (potentially including presurgical recordings and some brain-machine

interfaces), whereas SU remains relevant for tasks and analyses where more subtle

secondary signals and modulations are important.

Acknowledgement: This project was supported by a Canadian Institutes for Health
Research (CIHR) Grant and the Vision: Science to Applications (VISTA) Program, which
is supported in part by the Canada first Research Excellence Fund. SS was supported by
a Natural Sciences and Engineering (NSERC) Undergraduate Student Award. VB and
AS were supported by the NSERC/DFG Brain in Action International Research Training
Group (IRTG).VB, XY, and HW were supported by CIHR and VISTA. JDC is supported
by the Canada Research Chair Program.
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Supplementary Figure 1: ***A***, *Basic egocentric reference frames: eye (e), head (h) and*
body / space (s). ***B***, *Different variables, and egocentric models for an example trial.*
Models tested: the difference between the initial and the final head orientation relative
to space (dH); the difference between the initial and the final eye orientation relative to
the head (dE); future orientation of the head in space coordinates (Hs); Eye in head (Eh);
Future gaze in space (Gs); Future gaze in head (Gh) Future gaze in eye (Ge); Target in
space (Ts): Target in head (Th); Target in eye (Te).

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Site-matched Analysis

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1239 ***Supplementary Figure 2: Site-matched analysis. A**, Visual MU sites as a function of*
1240 *the corresponding best fit score of visual SUs. No significant correlation was observed*
1241 *(Spearman R = 0.05, Slope = - 0.04 ± 0.08, P = 0.66). **B,** Motor MU sites as a function of*
1242 *the corresponding best fit score of motor SUs. A modest correlation (Spearman R = 0.20,*
1243 *Slope = 0.10 ± 0.06) but nearly reaching significance was observed (P = 0.053).*