Origin of Neural Frequency Responses: Intrinsic Sensory Coding vs. Structural Influences

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Abstract

Periodic changes in visual input can produce rhythmic patterns in EEG signals, which appear as narrowband frequency components. These components are commonly interpreted as reflecting the activity of neurons sensitive to the modulated stimulus features. Here, we present a scenario in which frequency components arise solely from retinotopic variations in signal strength, without reflecting any specific neural mechanism sensitive to the modulated feature. Using simulated and empirical data, we show that signal fluctuations based purely on retinotopic stimulus position can produce identifiable frequency components in response to position-modulated stimuli. These components likely reflect structural rather than functional cortical factors influencing signal strength across different retinotopic areas. Our results challenge the conventional assumption that frequency components necessarily indicate intrinsic neural signal processing, instead highlighting how interactions between stimuli and cortical architecture can give rise to such components.

Introduction

Rhythmic changes in visual stimuli can induce corresponding rhythmic patterns in brain activity, which appear in EEG recordings as narrowband frequency components. When a visual or semantic stimulus property (e.g., contrast, object identity) is modulated at a specific frequency, neurons sensitive to that property tend to oscillate at the same or related frequencies, resulting in periodic fluctuations in EEG amplitude. By presenting the stimulus for a sufficient duration (e.g., longer than one second; Norcia et al. (2015)) and applying frequency-domain analyses, these periodic fluctuations can be identified as precise, narrowband frequency components. This phenomenon, known as the steady-state visually evoked potential (SSVEP; Regan (1977)), allows researchers to extract stimulus-related brain activity with a high signal-to-noise ratio. As a result, SSVEPs have become a powerful tool for probing visual processing at multiple levels (Allen et al., 1996; Alp & Ozkan, 2022; Alp et al., 2016, 2018; Gundlach & Müller, 2013; Rossion et al., 2015), characterizing visual and neurological impairments (Sartucci et al., 2010; Silberstein et al., 2000), and developing brain-computer interface (BCI) technologies (see Liu et al. (2022) for a review).

The distinctive inferential power of SSVEPs is rooted in the presumption that the precise frequency components evident in the data can be attributed to modulations in neuronal activity, particularly of cells sensitive to the modulated stimulus property. In theory, any other factor capable of inducing fluctuations in EEG amplitude could also give rise to such frequency components. However, for these fluctuations to be practically relevant, they must withstand the standard practices in experimental design and data processing that are typically used to filter out extraneous signals.

Of particular significance of these practices are extended trial durations and the averaging of data across multiple trials, which serve to accentuate visually evoked potentials by removing transient fluctuations that are not time-locked across trials (Trimble, 1968). Consequently, induced fluctuations must exhibit consistency within trials

over time and synchronized phase across multiple trials to produce identifiable frequency components. Furthermore, given that SSVEP studies often focus exclusively on frequency components related to the modulation frequency of a periodically modulated stimulus property (Norcia et al., 2015), these fluctuations must also display periodic components that correspond to the stimulus modulation frequency and its harmonics.

Admittedly, it is challenging to envision any other factors capable of generating highly consistent signal fluctuations that are also sensitive to modulations in visual stimuli. Particularly, the latter condition suggests a level of computational capability to process the modulated aspects of stimuli. Given the extensive array of low (e.g., contrast, motion direction) and high-level (e.g., face identity, object category) stimulus properties that can produce frequency components when modulated, it is clear that neuronal responses tuned to specific stimulus properties are the primary driver of these signal fluctuations. Consequently, alternative sources for these fluctuations have traditionally been overlooked, as no compelling scenario has emerged in which any other factor could consistently introduce signal fluctuations that align with the modulations in visual stimuli.

Nonetheless, the magnitude of neuronal activity is not the only factor that determines the strength of measured EEG signals. Various other factors, such as the cortical volume (Schaul, 1998) and depth of the activated regions (Butler et al., 2019), the signal cancellation between simultaneously active brain areas (Ahlfors et al., 2010), and the thickness of the cerebrospinal fluid layer covering regions of interest (Rice et al., 2013), can impact the translation of cell activity into EEG signals. Under certain circumstances, such structural factors, as opposed to functional, can potentially interact with stimuli to introduce superficial influences into the data by modulating EEG amplitudes across conditions and/or time.

Particularly, position-dependent factors that introduce variances in the properties of different retinotopic populations can have a potentially large impact on recorded EEG signals by interacting with stimulus position. The visual field is not uniformly mapped

onto the visual cortex (Allman & Kaas, 1971; Daniel & Whitteridge, 1961; Talbot & Marshall, 1941; Wandell et al., 2007). Significant differences exist in cortical volume and depth across retinotopic areas, depending on eccentricity and polar angle (Daniel & Whitteridge, 1961; Horton & Hoyt, 1991; Schwartz, 1980). When a stimulus is located in the periphery, a given portion of the visual field engages smaller and deeper neural populations (Daniel & Whitteridge, 1961; Horton & Hoyt, 1991; Schwartz, 1980). Similarly, population receptive field sizes are much smaller in foveal areas compared to peripheral ones, meaning that a central stimulus would engage a greater volume of neural tissue (Dumoulin & Wandell, 2008). As a result, the same stimulus can evoke larger or smaller EEG responses depending on the size and depth of the activated brain areas based on its position in the visual field (Slotnick et al., 2001).

For SSVEP studies in general, the modulation of EEG signals by such position-dependent factors does not directly warrant identifiable frequency components in the signal. In order to yield frequency components, these position-dependent factors would somehow have to induce consistent and phase-locked signal fluctuations across many repetitions of a condition. When stimuli are static, or when they do not follow a consistent pattern of motion across trials, it is highly unlikely for position-dependent factors to induce signal fluctuations that survive trial-averaging. However, if the position of a stimulus is periodically modulated in a consistent manner across trials, as is often the case in SSVEP studies involving moving stimuli (e.g., Aissani et al., 2011; Nozaradan et al., 2012; Pitchaimuthu et al., 2021; Varlet et al., 2023), these position-dependent imbalances may introduce consistent time-locked fluctuations in the signal, potentially giving rise to narrowband frequency components even after averaging signals across trials (Figure 1).

In this context, we present a scenario in which stimulus-related frequency components emerge exclusively due to retinotopic variations in signal strength, rather than as a result of neural processing by specific feature-tuned neurons. First, we use simulations to demonstrate that any sort of position-dependent variance in measured EEG responses

Figure 1

Frequency components arising from position-dependent periodic fluctuations

This figure depicts a hypothetical situation based on the known eccentricity-related variations in cortical magnification (Daniel & Whitteridge, 1961; Horton & Hoyt, 1991; Schwartz, 1980). If the brain allocated equal-sized and equally-dense cortical regions to different parts of the visual field, a singleton moving stimulus would generate a uniform, consistent neural response across all positions, resulting in a stable, unvarying signal (gray line). On the other hand, if different areas in the visual field are represented disproportionately in the visual cortex, the same stimulus can lead to stronger or weaker signals depending on its position and the size of the corresponding brain regions (blue line). When the stimulus position is periodically modulated, this could lead to the emergence of periodic fluctuations in the EEG signal, which could yield identifiable frequency components.

⁸¹ can potentially introduce periodic signal fluctuations by interacting with

⁸² position-modulated stimuli even when the responses of local receptive units are driven

⁸³ equally. If these fluctuations are discernible in actual EEG signals, they should manifest

⁸⁴ even in the absence of modulations in other stimulus properties, and must be strictly

⁸⁵ phase-coupled to modulations in stimulus position. In two subsequent EEG experiments,

⁸⁶ we demonstrate that periodically modulating the polar angle and eccentricity of a singleton

⁸⁷ stimulus induces frequency components when all other stimulus properties remain constant

⁸⁸ over time. Critically, these frequency components are eliminated through phase-cancelation

⁸⁹ when the phases of the position modulations are varied across trials.

₉₀ If these frequency components were generated solely by the intrinsic neural

₉₁ processing of the stimulus, they would have persisted even in the phase-varied conditions.

₉₂ Phase-cancelation in the phase-varied conditions suggests that these frequency components

₉₃ are phase-coupled to the position modulation of the stimulus, and therefore must strictly

₉₄ be related to fluctuations produced by position-dependent factors. Taken together, these

₉₅ results indicate that inherent retinotopic differences in measured EEG amplitude can

₉₆ autonomously introduce consistent, time-locked signal fluctuations in response to

₉₇ position-modulated stimuli, offering a counterexample to the conventional approach of

₉₈ associating frequency components with intrinsic neural signal processing.

₉₉ **Simulation**

₁₀₀ It is conceivable to view the EEG signal as a comprehensive non-linear

₁₀₁ transformation on visual input. This transformation is the culmination of numerous layers

₁₀₂ of diverse non-linear processes introduced by the intricate machinery of neural processing,

₁₀₃ in addition to the physical factors that govern the translation of neuronal activity into

₁₀₄ EEG signals. For our purposes, we draw a clear distinction between two pivotal concepts:

₁₀₅ unit response and population-level response. Following this distinction, we will argue that

₁₀₆ while traditional explanations attribute stimulus-related frequency components to the

₁₀₇ responses of units tuned to the modulated stimulus properties, these components can also

₁₀₈ emerge at the level of population response. This emergence hinges on variances in the

₁₀₉ population response contingent upon the retinotopic stimulus position and the presence of

₁₁₀ a position-modulated stimulus.

₁₁₁ We start by conceptualizing the unit response as an abstract representation of

₁₁₂ neuronal responses triggered by visual stimuli. In this context, the unit response

₁₁₃ characterizes a transformation of visual input, which we define as an arbitrary nonlinear

₁₁₄ function, denoted as $y = f(xs(t), a(t))$. Here, y signifies the response amplitude of a unit

₁₁₅ responding to a stimulus whose position is xs and intensity a at time t. Our focus is not on

₁₁₆ modeling specific types of neurons, but rather on defining units that adjust their responses

based on varying intensities of the stimulus properties to which they are tuned. Therefore, a (i.e., stimulus intensity) can be associated with any stimulus property to which these hypothetical units are sensitive, and the function f can encompass various forms of neural computations.

The conventional interpretation of the frequency components observed in EEG signals in response to a periodically modulated stimulus assumes that these frequency components arise from the nonlinear relationship between a and y. As long as f includes a non-zero coefficient for a, indicating sensitivity to changes in stimulus intensity, periodic modulation of a will invariably result in a periodic modulation of y. Consequently, if the stimulus intensity undergoes sinusoidal modulation, for example, it will induce a non-sinusoidal modulation of the unit response that repeats at the same time intervals as the stimulus modulation. As a result, the EEG signal will contain frequency components that are harmonics (integer multiples) of the sinusoidal stimulus modulation frequency, provided that an adequate number of units synchronously respond to the stimulus.

Here, our aim is to investigate whether identifiable frequency components can be generated independently of the unit response, specifically due to position-dependent variances in the responses of different retinotopic populations. Therefore, we focus on the scenario in which the stimulus intensity α remains constant across time and the unit responses do not vary as a function of modulations in stimulus intensity. If a position-modulated stimulus, across its different positions, was processed by a perfectly homogenous ensemble of identical units without any position-dependent variability in the measured EEG strength, the resulting signal would not exhibit fluctuations and remain constant across time. This is because the stimulus would drive uniform responses from the same number of units with identical properties at each time point (Figure 1, gray line). Conversely, if there are position-dependent factors that influence how unit responses translate into measured EEG strength, such as the density of units or their distance from the electrodes, the signal would exhibit fluctuations across different positions of the

stimulus, even though individual local units receive the same information (i.e., stimulus

intensity) and produce the same response. Moreover, if there are consistent variations in

the receptive field properties of different retinotopic populations, these could also lead to

position-dependent variability in EEG signals by modulating unit responses based on the

pattern of overlap between the receptive fields and stimulus (Figure 1, blue line).

To capture the effect of such position-dependent factors, we conceptualize

population response as a representation of collective activity from many individual units

responding to the stimulus as measured by the EEG. At each position of the stimulus, a

number of units whose receptive fields overlap with the stimulus produce a response. The

population response is a sum of responses from each of these units with weights determined

as a function of the location of the unit's receptive field within the visual field:

$$Y(t) = \sum_{i=1}^{d(xs(t),a(t))} g(x_i) \cdot f_i(xs(t), a(t))$$

where d is a unit-density function that determines the number of units responding

to a stimulus presented at retinotopic position xs with intensity a at time t; f is the

magnitude of response for each unit responding to that stimulus; and g determines the

extent to which the response of each unit contributes to the measured population response

based on the location of its receptive field, x_i. Therefore, Y is the magnitude of the

measured population response evoked by a stimulus whose position is xs and intensity a.

As our focus is solely on signal variations arising from position-specific factors, we

assume that individual units produce identical responses when a stimulus with the same

intensity a falls within their receptive fields. Therefore, we factor out the variance

attributable to the correlation between individual unit responses and stimulus intensity

under the condition that the intensity a is constant. However, unit responses would still

vary depending on the extent of overlap between each unit's receptive field and the

stimulus. Consequently, unit responses would exhibit variability contingent upon the

positioning and dimensions of both their receptive fields and the stimulus. This inter-unit

variance alone would not lead to differences in population response if the spatial

distribution of units' receptive field sizes were identical for each population. Conversely, if

the receptive field sizes of individual units, or their spatial distribution within the

population receptive field, vary across populations, this could lead to differences in

population responses along with other position-dependent factors. We account for this by

keeping the $f_i(xs(t))$ term while excluding the variance attributable to a. Thus, we obtain:

$$Y(t) = \sum_{i=1}^{d(xs(t))} g(x_i) \cdot f_i(xs(t))$$

which denotes a stimulus-position-dependent coefficient for the magnitude of EEG

signals recorded from a population of stimulated units, whose responses do not vary as a

function of stimulus intensity but only as a function of the position of their receptive fields.

It is then possible to calculate these position-dependent coefficients for stimuli

encompassing arbitrary portions of the visual space (such as pixels on an image) at discrete

time points and map them across the visual field. This produces a two-dimensional

heatmap representing the variance in EEG amplitude caused by position-dependent factors

given otherwise uniform unit responses; which we refer to as Retinotopic Weight Function

(RWF):

$$RWF_{u,v} = \sum_{i=1}^{d(xs_{u,v})} g(x_i) \cdot f_i(xs_{u,v})$$

The actual nature of the Retinotopic Weight Function is not of critical importance

for our demonstration, and it can be substituted by any two-dimensional function that may

or may not approximate the influence of biologically-plausible position-dependent factors

on the EEG strength. The critical requirement for the Retinotopic Weight Function in this

context is that it consistently varies across the visual field and scales the contribution of

each unit (to the signal) based on the location of their receptive fields. We will

demonstrate that as long as this condition is fulfilled, position-dependent factors can

interact with position-modulated stimuli to generate periodic signal fluctuations and

therefore yield identifiable frequency components.

To this end, we simulate a hypothetical signal that contains only the fluctuations

caused by position-dependent variances in population responses and not by the oscillations

in unit responses induced by modulations in stimulus intensity. Therefore, we generate

signals by multiplying a constant average unit response C with the respective

position-dependent weight corresponding to the population response strength at each

position of a moving stimulus.

$$S(t) = RWF_{x(t),y(t)} * C$$

where x and y are the cartesian coordinates of the stimulus position.

Given this framework, we explore three different cases for the Retinotopic Weight

Function, as depicted in Figure 2a-c. Although these Retinotopic Weight Functions were

defined arbitrarily, some of them can be loosely associated with certain retinotopic

properties of the visual cortex. For instance, in Figure 2a, the Retinotopic Weight Function

is depicted as a function whose output diminishes linearly with distance from the center. It

could be argued that eccentricity-dependent differences in cortical magnification could give

rise to analogous variations in population response. In Figure 2b, the Retinotopic Weight

Function exhibits a linear decrease from left visual field to right visual field and

consequently introduces variations across polar angles, which could provide insights about

the effect of retinotopic anisotropies. Finally, in Figure 2c, the outputs of the Retinotopic

Weight Function are randomly determined from a uniform distribution in a fine grid to

represent a complex spatially-varying function without assuming any specific computation.

Although arbitrary, these Retinotopic Weight Functions all fulfill the essential condition of

exhibiting consistent variations in measured population responses across different stimulus

positions.

Finally, we examine various forms of position modulation applied to a singleton

stimulus (Figure 2, Position Modulation column). First, we consider the rotational motion

of a singleton object orbiting a central point (orbital). Second, we consider the repetitive

Figure 2

Simulated signals and their frequency domain representations.

Description on next page.

Description for Figure 2: The Retinotopic Weight Function (first column) interacts with the type of position modulation (second column: Orbital, Linear, Blinking) to shape the time domain response (third column) and resulting frequency content (last column). Frequency domain responses (last column) show harmonics of the position modulation frequency. **a)** Retinotopic Weight Function decreases linearly with eccentricity. **Orbital position modulation:** The singleton stimulus traverses along a circular path with constant eccentricity, which does not introduce fluctuations in the signal and does not lead to any frequency components. **Linear:** Stimulus eccentricity is linearly modulated along a horizontal line. The course of the eccentricity modulation is reversed sharply at the center and during motion-direction reversals (left-to-right, right-to-left). This is reflected in the signal as a triangular wave, which contains harmonics of double the position modulation frequency. **Blinking:** The singleton stimulus alternates between two locations that have identical weights in the Retinotopic Weight Function, therefore it also does not produce fluctuations and frequency components. **b)** Retinotopic Weight Function decreases linearly from left to right visual field. **Orbital:** The signal is the projection of a circular motion along a linear gradient, which by definition is sinusoidal. Therefore, only the fundamental position modulation frequency is represented in the frequency domain. **Linear:** Stimulus seesaws along the axis of linear Retinotopic Weight Function gradient. The signal exhibits sharp reversals when the stimulus changes direction. This triangular signal contains the odd harmonics of the position modulation frequency. **Blinking:** Stimulus alternates between two locations with different weights, leading to a square wave signal and harmonics of the position modulation frequency. **c)** Retinotopic Weight Function is randomly determined. **Orbital and linear position modulation:** The stimulus traverses through areas with randomly determined weights for the Retinotopic Weight Function. The consequent signals are highly complex, but since they have the same period as the position modulation cycle, they contain harmonics of the position modulation frequency in their frequency domain representations. **Blinking:** Stimulus alternates between two locations with different weights similarly to b). The square wave signal contains the harmonics of the position modulation frequency.

translational motion of an object with a constant speed, which moves back and forth along a horizontal axis (linear). Third, we consider the position modulation of an object that blinks between two positions, akin to traditional long-range motion paradigms (blinking).

Figure 2 (Signal column) illustrates the simulated signals generated for all combinations of three distinct Retinotopic Weight Functions and three types of position modulation (i.e., orbital, linear, and blinking). Signals were generated for 4-second time windows with all three types of position modulation being repeated four times with a cycling frequency of 1 Hz. The simulated signals were then Fourier transformed to the frequency domain with a $1/4 = 0.25$ Hz frequency resolution. All visible frequency components in the Frequency Domain column in Figure 2 correspond to the harmonics of the position modulation frequency (i.e., 1 Hz).

Experiment 1: Polar angle modulation

Materials and Methods

In Experiment 1, we investigated whether the modulated polar angle of a singleton stimulus could interact with position-dependent factors to produce distinct frequency components when other stimulus properties are kept constant.

Participants

14 Sabancı University students (8 female, 6 male; mean age = 21.1 years, SD = 2.02) with normal or corrected-to-normal vision participated in Experiment 1 for course credit. One participant's data was excluded from all analyses due to software errors during the recording session, reducing our sample size to 13. The sample size was based on previous studies with similar methods (e.g., Nozaradan et al., 2012; Pitchaimuthu et al., 2021; Varlet et al., 2023). A sensitivity analysis conducted using GPower software (Faul et al., 2007) revealed that this sample size was sufficiently powered (power = .80) to detect large effect sizes (Cohen's f > .42) for our within-subjects factors (see, Frequency domain analysis). All procedures in this study were reviewed and approved by the Sabancı University Research Ethics Council. Participants gave informed consent prior to the experiment session.

Apparatus and Stimuli

Stimuli were generated using Psychopy (Peirce et al., 2019) and presented on an ASUS XG248Q monitor (23.8", resolution=1920x1080) with a refresh rate of 60 Hz. Participants viewed the stimuli from a 76.5 cm distance in a dark and quiet room. The stimuli consisted of a single light gray (contrast = 75%) dot rotating around a fixation cross on a dark gray (contrast = 25%) background. The dot had a radius of 1 dva and an eccentricity of 5 dva from the fixation cross. The dot always completed one full rotation in exactly 1 second and had a constant movement speed with a 6° polar angle shift per motion frame. Trials lasted 11 seconds, during which the dot completed 11 full rotations.

The rotational motion of the dot meant that its polar angle was modulated as a function of time. The phase of this polar angle modulation depended on the position from which the dot started its rotation. In one condition, the dot's rotation always started from the same predetermined polar angle chosen randomly for each participant from a range of 0° to 350° in steps of 10° (e.g., 50° for one participant, 130° for another). The constant starting polar angle led to a phase-locked manipulation of the dot's polar angle across trials (Figure 3a). We will hereafter refer to this condition as the phase-locked (PL) condition. In the second condition, the starting polar angle was randomly selected for each trial from the same range (0° to 350° in steps of 10°) without replacement (i.e., each step was used only once). Since the dot started its rotation from a different polar angle on each trial, the polar angle modulation was not phase-locked in this condition (Figure 3b). Therefore, we will refer to this condition as the phase-varied (PV) condition. There were 72 trials for each phase condition (PL and PV).

The only difference between the two phase conditions was the locked vs. varied phase of the polar angle modulation. All other stimulus properties, including motion speed, direction-switch rate, rotational frequency, and eccentricity were identical between the two conditions. Moreover, these properties were either not expected to induce periodical signal fluctuations as they were not periodically modulated (e.g., motion speed) or were expected

to yield identical frequency components in both conditions as their modulations were

phase-locked in all trials (e.g., direction-switch rate, rotational frequency). For example,

even when the dot started its rotation from different angles, it repeated its rotation cycle

at exactly 1-second intervals (i.e., rotational frequency). Likewise, the dot's movement

direction was shifted by the same amount at each frame regardless of its starting polar

angle (i.e., direction-switch rate). Therefore, we expected that any differences between the

frequency components extracted from the two phase conditions would primarily stem from

the phase manipulation applied to the polar angle modulation.

Since we were interested in EEG activity sensitive to polar angle modulation, we

expected rotation direction to be a defining factor in the profile of the modulated EEG

signal. Therefore, we also manipulated the rotation direction of the dot. In both phase

conditions, the dot rotated either clockwise (CW) or counterclockwise (CCW),

counterbalanced within each condition. Hence, we had 36 CW and 36 CCW trials for each

phase condition.

Procedure

Each trial started with a fixation cross displayed on a gray background for 1 second,

followed by an 11-second presentation of the rotating dot stimulus. After each trial, there

was a self-paced break in which the participants pressed a keyboard key to proceed with

the next trial. In approximately 14% of the trials (12 trials per block), the rotating dot

briefly changed its color for 250 milliseconds at a random time (except during the first and

last seconds of the trial). Participants were instructed to fixate on a red cross at the center

of the screen, and press keys on the keyboard whenever they noticed a change in the dot's

color (F key if the dot turned red, J if it turned green). The trial was terminated upon

response or after the 1-second response window, with a feedback (i.e., correct/incorrect)

text displayed for 1 second. These trials acted as catch trials to motivate participants to

pay attention to the stimulus.

Trials from PL and PV conditions were presented in two separate blocks, the order

Figure 3

Phase manipulation of the polar angle modulation

a) In the phase-locked condition, the dot consistently initiated its rotation from the same polar angle across trials, resulting in a consistent phase for the polar angle modulation. The sine functions (green lines) in the second row are provided for illustrative purposes, demonstrating how the dot's starting angle influences the phase of the polar angle modulation. Although the actual signal evoked by the polar angle modulation may not be sinusoidal, its phase is expected to align with the phase of this modulation. **b)** In the phase-varied condition, the dot's starting angle was randomly chosen on each trial from the 36 predefined polar angles. Consequently, the polar angle modulation was not phase-locked across trials in the phase-varied condition, which would result in non-phase-locked signals canceling out each other when averaged in the time domain (the straight green line).

₂₉₉ of which was counterbalanced between participants. Each block consisted of 72

₃₀₀ experimental and 12 catch trials, with an equal number of CW and CCW trials, in random

₃₀₁ order. Participants took a 3-5 minute break between the two blocks. Prior to the

₃₀₂ experiment, participants completed a short practice block (2-3 minutes) of 12 catch trials

₃₀₃ to get accustomed to the task.

EEG acquisition

₃₀₅ EEG was recorded using 64 Ag/AgCl active electrodes placed on the scalp according

₃₀₆ to the international 10-10 system (ActiCAP, Brain Products GmbH, Gilching, Germany)

₃₀₇ with the following modifications: The channels TP10 and FT10 were placed above and

₃₀₈ below the participants' right eye to be used as vertical electrooculogram (VEOG) channels,

₃₀₉ and TP9 was used to replace the otherwise absent Iz channel. BrainVision Recorder

₃₁₀ software (Brain Products GmbH, Gilching, Germany) was used to record the EEG data at

₃₁₁ a 1000 Hz sampling rate with channel impedances kept below 20 kΩ.

EEG preprocessing

₃₁₃ Fieldtrip Toolbox (Oostenveld et al., 2010) and custom scripts were used to

₃₁₄ preprocess the data. A fourth-order Butterworth bandpass filter (0.5 - 100 Hz) was applied

₃₁₅ to the continuous data. Power line noise was removed by a multi-notch filter at frequencies

₃₁₆ 50, 100, and 150 Hz with bandwidths of 1, 2, and 3 Hz respectively. The online reference

₃₁₇ channel (FCz) was re-added to the data and channels were re-referenced to the average of

₃₁₈ all channels. Blink artifacts were removed by implementing an Independent Component

₃₁₉ Analysis (ICA) in Fieldtrip, using EEGLAB's runica algorithm (Delorme & Makeig, 2004).

₃₂₀ Bad channels were determined by visual inspection and interpolated (0.37% per participant

₃₂₁ on average) using neighboring channels. Data were then segmented into 11-second trial

₃₂₂ epochs and downsampled by a quarter to 250 Hz for computational efficiency. A small

₃₂₃ number of trials were rejected (M = 1.38%, SD = 2.38) due to hardware-related artifacts

₃₂₄ (peak amplitude > 500 µV). Data from the catch trials were excluded from all analyses.

Frequency domain analysis

We expected position-dependent discrepancies in EEG strength to induce periodic fluctuations in the signal by enhancing or attenuating the strength of the population response at different polar angles of the rotating dot stimulus. Therefore, we expected the phases of these periodic fluctuations to align with the phase of our polar angle modulation. Consequently, we anticipated these fluctuations to exhibit phase-locking across the trials of our PL condition, but not across the trials of the PV condition.

To extract the periodic fluctuations induced by the polar angle modulation, we utilized time-domain averaging and averaged the trials from each of our conditions in the time domain (Trial N ≈ 36). Time-domain averaging eliminates noise while keeping phase-locked signals intact (Trimble, 1968). As a consequence, we expected time-domain averaging to preserve the polar angle modulation frequencies in the phase-locked condition, but eliminate the same frequencies in the phase-varied condition through phase-cancellation. As previously discussed (see, Apparatus and stimuli), other stimulus properties were either not expected to induce periodic fluctuations or were expected to induce the same periodic fluctuations in both conditions. Therefore, any frequency components with amplitudes significantly higher in the PL than the PV condition should belong to fluctuations induced by the polar angle modulation alone.

We applied a Fourier transform on the time-averaged data (frequency resolution: $1/11 = 0.09$ Hz), and calculated the baseline-subtracted amplitudes by subtracting from the amplitude of each frequency bin the average amplitude of 16 neighboring bins (8 from both sides), with the exclusion of two immediately adjacent bins (one on each side). Since the dot's polar angle was modulated at 1 Hz, we expected to observe frequency components at 1 Hz and its harmonics. We also compared the overall amplitude of activity distributed across these fundamental and harmonic frequencies. To this end, we summed the baseline-subtracted amplitudes of all harmonic frequencies which were significantly above the noise level (Retter & Rossion, 2016; Retter et al., 2021). Significant harmonics

were determined by first grand-averaging the FFT spectra across participants, channels, and conditions, and then calculating Z-scores for each frequency bin with a similar procedure to the baseline-subtracted amplitude calculation (i.e., 16 neighboring bins were used as the baseline for each frequency bin). Only the frequency components up to the sixth harmonic (including the fundamental frequency) passed the threshold of significance ($Z > 1.64$, $p < 0.05$, one-tailed, signal > noise), and thus were included when calculating the summed baseline-subtracted amplitudes for each condition.

We identified two separate ROIs for our analyses. The first included only the Oz channel, which largely covers V1 where the position-dependent discrepancies across different retinotopic areas, such as cortical magnification, are most well-known (Dahlem & Tusch, 2012; Daniel & Whitteridge, 1961; Dow et al., 1981; Gattass et al., 1987; Palmer et al., 2012; Van Essen et al., 1984). The second ROI consisted of 8 posterior channels (Oz, O1, O2, POz, PO3, PO4, PO7, PO8) which roughly encompasses the occipital-parietal areas in which previous studies consistently found frequency components induced by position-modulated stimuli (Aissani et al., 2011; Alp et al., 2017; Nozaradan et al., 2012; Palomares et al., 2012; Pitchaimuthu et al., 2021; Varlet et al., 2023). Separately for each ROI, We ran a 2-by-2 repeated-measures ANOVA (rm-ANOVA) on participants' summed baseline-subtracted amplitudes with phase (PV vs. PL) and rotation direction (CW vs. CCW) as within-subject factors. For the first ROI, the summed baseline-subtracted amplitudes from the Oz channel were used in the rm-ANOVA. For the second ROI, we averaged the summed baseline-subtracted amplitudes from the 8 channels to quantify and compare the overall response in these posterior channels. All reported p-values for both tests were Bonferroni-corrected for multiple comparisons (i.e., one for each ROI; Keil et al., 2022). Lastly, we calculated the signal-to-noise ratio (SNR = signal/baseline) for all frequency bins using the same baseline as described above, to better illustrate the pattern of harmonic frequencies contained in the evoked signal. SNR is preferred for this purpose as higher frequencies can have a low amplitude (and therefore a low baseline-subtracted

amplitude) but still have a high SNR.

Results

Behavioral results

The behavioral task in the catch trials served the sole purpose of encouraging

participants to pay attention to the stimulus. Therefore, we only required participants to

have accuracy above 50% on the catch trials. Overall, participants' accuracy was high (M

= 88.14%, SD = 8.31), and no participant had below-chance accuracy in either of the two

experimental blocks (Min. = 58.33%).

Frequency domain results

Z-scores calculated on the grand-averaged amplitude spectra indicated that

harmonics of the polar angle modulation frequency were significant up to the sixth

harmonic (see Frequency domain analysis), thereby constituting our frequencies-of-interest

for the following analyses. Figure 4 illustrates that these six frequencies are clearly

distinguishable from noise in the two PL conditions (CW and CCW) whereas they are at

noise levels (SNR $\approx$ 1) in the PV conditions. A visual inspection of the topographical maps

(Figure 5) displaying the summed baseline-subtracted amplitudes for each condition across

EEG channels suggests a clear posterior activity in the PL, but not in the PV, conditions.

A rm-ANOVA on the summed baseline-subtracted amplitudes from the Oz channel

(i.e., the first ROI) revealed a significant main effect of phase ($F(1, 12) = 86.74$, $p_{\mathrm{bonf}} <$

10^{-5}, $\eta^2_{\mathrm{p}} = 0.878$). The main effect of rotation direction ($F(1, 12) = 0.59$, $p_{\mathrm{bonf}} = 0.91$, η^2_{p}

$= 0.047$) and the interaction term ($F(1, 12) = 5.86*10^{-5}$, $p_{\mathrm{bonf}} = 1$, $\eta^2_{\mathrm{p}} = 4.88*10^{-6}$) were

not significant. Figure 5b depicts the distinction among each condition.

Bonferroni-corrected post hoc tests revealed that the summed baseline-subtracted

amplitudes from the PL condition were significantly larger than those from the PV

condition, within both CW ($M_{\mathrm{diff}} = 1.516$, $p_{\mathrm{bonf}} < 10^{-5}$) and CCW ($M_{\mathrm{diff}} = 1.517$, $p_{\mathrm{bonf}} <$

10^{-5}) conditions. CW and CCW conditions did not differ significantly within PV ($M_{\mathrm{diff}} =$

0.048, $p_{\mathrm{bonf}} = 1$) or PL ($M_{\mathrm{diff}} = 0.047$, $p_{\mathrm{bonf}} = 1$) conditions.

A separate rm-ANOVA on the summed baseline-subtracted amplitudes averaged

from the eight posterior channels (i.e., the second ROI) also revealed similar results: The

main effect of phase ($F(1,\ 12) = 75.77$, $p_{\mathrm{bonf}} < 10^{-5}$, $\eta^2{}_{\mathrm{p}} = 0.863$) was significant, but the

main effect of rotation direction ($F(1,\ 12) = 0.48$, $p_{\mathrm{bonf}} = 1$, $\eta^2{}_{\mathrm{p}} = 0.039$) and the

interaction term ($F(1,\ 12) = 0.064$, $p_{\mathrm{bonf}} = 1$, $\eta^2{}_{\mathrm{p}} = 0.005$) were not. The PL condition

had larger summed baseline-subtracted amplitudes than the PV condition in both CW

($M_{diff} = 1.67$, $p_{\mathrm{bonf}} < 10^{-5}$) and CCW ($M_{diff} = 1.69$, $p_{\mathrm{bonf}} < 10^{-5}$) conditions (see Figure

5b). There was no significant difference between the CW and CCW conditions within PV

($M_{diff} = 0.05$, $p_{\mathrm{bonf}} = 1$) or PL ($M_{diff} = 0.023$, $p_{\mathrm{bonf}} = 1$) conditions.

Figure 4

FFT signal-to-noise ratio (SNR) spectra

SNR calculated on the FFT amplitude spectra obtained from time-domain averaged trials for each condition. The figures here reflect the SNR values extracted from the Oz channel, averaged across participants. The first six harmonics of the modulation frequency ($1f$, $2f$, $3f$, $4f$, $5f$, and $6f$) exhibit high SNR (> 2) in the phase-locked conditions, but are at noise levels (≈ 1) in the phase-varied conditions.

Figure 5

Summed baseline-subtracted amplitudes

a) Topographical plots of grand-averaged summed baseline-subtracted amplitudes of the first six harmonics of the modulation frequency (1f, 2f, . . . , 6f) across all channels. **b)** The summed baseline-subtracted amplitudes of the first six harmonics of the modulation frequency (1f, 2f, ..., 6f) are depicted for the two regions-of-interest. Left: Summed baseline-subtracted amplitudes obtained from the Oz channel. Right: Average of the summed baseline-subtracted amplitudes obtained from the eight posterior EEG channels. Error bars indicate the standard error of the mean. Statistical significance is denoted as *** (p < 10^{-5}).

Experiment 2: Eccentricity modulation

Results from Experiment 1 revealed frequency components that are contingent on the phase of the polar angle modulation, and therefore originate from a position-dependent modulation of the EEG signal. These results are in line with our hypothesis that systematic position-dependent discrepancies in the EEG strength can yield frequency components by interacting with a position-modulated stimulus. In Experiment 2, we investigated whether a modulation of stimulus eccentricity can drive similar results.

Materials and Methods

Materials and methods were identical to Experiment 1, with the exceptions outlined below.

Participants

13 Sabancı University students (8 female, 5 male; mean age = 21.38 years, SD = 0.5) with normal or corrected-to-normal vision were recruited in exchange for course credit. The sample size was based on previous studies as in Experiment 1. A sensitivity analysis revealed that this sample size was sufficiently powered (power = .80) to detect effect sizes larger than 0.73 (Cohen's d, one-tailed paired-samples t-test; see, Frequency domain analysis).

Apparatus and Stimuli

In Experiment 2, we employed the same rotating dot stimulus but adjusted the position of the rotation trajectory by shifting it in eight different directions (shift direction angles: 0°to 315°in increments of 45°). As a consequence, the center of the rotation trajectory was always positioned 2 dva away from the fixation cross, which allowed the dot's eccentricity to be modulated between 3 and 7 dva during its rotation. The phase of this eccentricity modulation depended on the position from which the dot started its rotation. More specifically, the phase of the eccentricity modulation was determined by the relative angle between the dot's initial position and the axis of the trajectory shift (Figure

6). Using this property, we kept the phase of the eccentricity modulation constant across

trials in the phase-locked (PL) eccentricity modulation condition and varied it in the

phase-varied (PV) condition (range: 0°to 315°in steps of 45°). The constant phase used for

the eccentricity modulation in the PL condition was randomized between participants by

randomly assigning each participant a predetermined relative starting angle. This meant

that the relative starting angle of the dot in the PL condition, and therefore the phase of

the eccentricity modulation, was different for each participant (but still constant across the

PL trials within participants).

Shifting the rotation trajectory in eight different directions allowed for varying the

phase of the polar angle modulation in both phase conditions, while still enabling a

phase-locked eccentricity modulation in the PL condition. Therefore, we expected to

observe only the frequency components introduced by the eccentricity modulation, as those

introduced by the polar angle modulation would be eliminated through phase-cancelation.

As a consequence of the cancellation of polar angle-dependent signals, any influence of the

dot's rotation direction (CW and CCW) was also expected to be eliminated. Therefore, to

increase the number of trials for our phase conditions, we omitted the rotation direction

conditions in Experiment 2. Instead, we maintained a constant rotation direction (either

clockwise or counterclockwise) across all trials, with the specific direction randomly

predetermined for each participant.

Each trial lasted 10 seconds and contained 10 full rotations of the dot. Phase-locked

and phase-varied conditions were presented in two different blocks similar to Experiment 1.

Each block had 76 trials, 12 of which were catch trials. The task in the catch trials was

identical to Experiment 1.

Frequency domain analysis

465 Bad channels were interpolated (0.5% per subject on average) using neighboring

466 channels, and a small number of trials (M = 0.96%, SD = 1.15) with hardware-related

467 artifacts were excluded from the analyses. Later, trials from the PL and PV conditions

Figure 6

Rotation trajectory shift and the phase of the eccentricity modulation

a) Left: The circular rotation trajectory was shifted by 2 dva. As a result, the dot's eccentricity changed from 3 to 7 dva during its rotation. Right: Relative starting angle of the dot defined as the angle between the vector of the rotation trajectory shift and the dot's initial position (shift angle - dot's polar angle). This relative starting angle determined the phase of the eccentricity modulation. **b)** The phase of the eccentricity modulation was determined by the relative starting angle of the dot, even when different shift angles were applied to the rotation trajectories. The left and right columns represent conditions where the rotation trajectories were shifted in different directions, yet the phases of the eccentricity modulation remained the same. This consistency was achieved by maintaining the same relative starting angle across different shift directions.

were averaged separately in the time domain (Trial N ≈ 64). Following the same Z-score

calculation procedure and significance criterion as in Experiment 1 (baseline: 14

neighboring bins for each frequency), only the fundamental frequency component (1 Hz)

was found significant. Therefore, we used the baseline-subtracted amplitudes of the

fundamental frequency to compare the two conditions in two paired-samples t-tests for the

two ROIs. Since we expected the PL condition to produce large baseline-subtracted

amplitudes and the PV condition around the noise level (baseline-subtracted amplitude ≈

0), we ran one-tailed tests.

Results

Behavioral results

Participants' accuracy on the behavioral task was similar to Experiment 1 (M =

84.62%, SD = 9.22, Min. = 58.33%).

Frequency domain results

Z-scores calculated on the grand-averaged amplitude spectra revealed that only the

fundamental frequency was significantly larger than the noise ($Z = 2.75$, $p = .003$,

one-tailed, signal > noise). Figure 7 shows that the fundamental frequency had a large

SNR in the PL condition, but was at noise levels in the PV condition (SNR ≈ 1).

Topographical maps of the baseline-subtracted amplitudes (Figure 8b) suggest that

phase-locked eccentricity modulation elicited activity in the posterior channels, whereas no

particular activity was observed in the PV condition.

We ran two separate one-tailed (i.e., PL > PV) paired-samples t-tests on the two

ROIs. The fundamental frequency had a significantly larger baseline-subtracted amplitude

in the PL condition for both the Oz channel ($t(12) = 5.17$, $p_{\text{bonf}} < .001$, $d= 1.43$), and the

average of the eight posterior channels ($t(12) = 5.12$, $p_{\text{bonf}} < .001$, $d= 1.42$), compared to

the PV condition (Figure 8a).

Figure 7

FFT signal-to-noise ratio (SNR) spectra

SNR calculated on the FFT amplitude spectra obtained from time-domain averaged trials for each condition, from the Oz channel. The fundamental modulation frequency (1f) exhibits a high SNR in the phase-locked condition, whereas its SNR is at noise levels in the phase-varied condition.

Discussion

We hypothesized that position-dependent factors that influence the strength of signals measured from different retinotopic populations, such as their volume and depth, could introduce consistent fluctuations in EEG signals under certain circumstances. We investigated whether the signal fluctuations driven purely by such position-dependent factors could yield frequency components when no other stimulus property was periodically modulated. Our simulations revealed that position-dependent factors could interact with a position-modulated stimulus, generating signal fluctuations that produce distinct frequency components. These signal fluctuations are strictly phase-coupled to the stimulus's position modulation. Furthermore, the frequency components they produce depend on both the trajectory of the position modulation and the way position-dependent factors influence signals measured from different retinotopic populations (i.e., Retinotopic Weight Function).

In two subsequent experiments, we modulated the position of a singleton shape by separately modulating its polar angle (Experiment 1) and eccentricity (Experiment 2). For

Figure 8

Baseline-subtracted amplitudes

a) The baseline-subtracted amplitudes of the modulation frequency ($1f$) are depicted for the two regions-of-interest: Baseline-subtracted amplitudes obtained from the Oz channel, and average of the baseline-subtracted amplitudes obtained from the eight posterior EEG channels. Error bars indicate the standard error of the mean. Statistical significance is denoted as *** ($p <$ .001). **b)** Topographical maps of grand-averaged baseline-subtracted amplitudes of the fundamental modulation frequency ($1f$) across all channels.

both types of position modulation, we had a phase-locked condition in which the phase of the modulation was synchronized across trials, and a phase-varied condition where the phase of the modulation was randomized across trials. Moreover, we kept all other stimulus properties constant between the two conditions so that these properties would either yield no frequency components, or would yield identical frequency components in both conditions. Our goal was to selectively eliminate signal fluctuations produced by position-dependent factors through phase-cancellation in the phase-varied conditions. This way, the frequency components that differ between the phase-locked and phase-varied conditions would indicate the existence of position-dependent factors that can produce consistent periodic signal fluctuations by interacting with a position-modulated stimulus.

In line with our hypothesis, we observed clear frequency components at the position

modulation frequencies in both experiments when the phases of the polar angle and

eccentricity modulations were synchronized across trials. However, when the phases of

these modulations were randomized, the same frequency components were indistinguishable

from noise.

Frequency components in SSVEP studies typically exhibit narrowband

characteristics, as they arise from periodic fluctuations in neural activity in response to

stimulus properties modulated at specific frequencies. In our study, the only stimulus

property that was periodically modulated was its position. Consequently, the observed

frequency components are best explained by variations in the structural properties of

different retinotopic populations captured in EEG signals, rather than by the activity of

feature-tuned neurons.

This position-dependent modulation of the EEG signal can be readily explained by

the retinotopic discrepancies in cortical properties that influence the strength of the

measured EEG signals (e.g., cortical volume: Schaul, 1998; cortical depth: Butler et al.,

2019; cancellation between simultaneously active sources: Ahlfors et al., 2010). Simple

amplification or attenuation of signals across different retinotopic areas—for instance, due

to variations in the size or depth of the activated regions—can produce signal fluctuations

based on stimulus position. Therefore, any set of structural factors that systematically

influences EEG amplitude could potentially generate distinguishable frequency components

by introducing position-dependent signal fluctuations.

For instance, due to the non-uniform mapping of the visual field to the visual

cortex, parts of the visual field are processed by disproportionately larger brain areas, a

property known as cortical magnification (Daniel & Whitteridge, 1961; Horton & Hoyt,

1991; Schwartz, 1980). In our study, the position-modulated stimulus may have activated

brain areas of varying sizes depending on the stimulus position, leading to differences in

EEG amplitudes as a result of cortical magnification. In this case, the observed frequency

components would reflect the differences in the size of the activated brain regions and the

total number of neurons within them, rather than fluctuations in the responses of neurons

tuned to the stimulus.

The key point here is not that any one structural factor solely explains these results,

but that such structural factors—either collectively or independently—can generate

frequency components unrelated to the functional sources of EEG fluctuations. This

finding challenges a core assumption of SSVEP methodology, which posits that the

frequency components observed in response to a periodically modulated stimulus are a

direct reflection of evoked neuronal activity processing the specific stimulus property that

is modulated (Norcia et al., 2015). In contrast, the frequency components we report do not

arise from any specific neural processing mechanism. Instead, structural factors

superimpose on signals originating from intrinsic neural processing and modify those

signals as an independent source of amplitude modulation. As a result, while these

frequency components may resemble typical SSVEP components, they do not provide

insights into the brain's processing of visual information. Rather, they emerge as a

byproduct of the brain's structural organization.

The frequency components generated by position-dependent factors present a

particular challenge when they closely resemble those expected to result from specific

neural mechanisms or feature-tuned populations. For instance, in SSVEP studies focusing

on visual motion processing, researchers often employ stimuli composed of moving visual

elements whose positions undergo repetitive modulation along a fixed path of motion (e.g.,

Aissani et al., 2011; Nozaradan et al., 2012; Pitchaimuthu et al., 2021; Varlet et al., 2023).

Some of these studies have argued that the frequency components elicited in response to

such stimuli reflect the modulation in the activity of motion-sensitive neural populations,

including those sensitive to motion direction (e.g., Aissani et al., 2011; although their

results based on intermodulation components cannot be readily explained by structural

factors) or repetitive motion patterns (e.g., Aissani et al., 2011; Pitchaimuthu et al., 2021).

However, with such motion stimuli, the motion-related characteristics are inherently linked

to position modulation. Consequently, position-dependent periodic fluctuations could lead

to similar frequency components either independently or in conjunction with the signal

fluctuations introduced by the modulated activity of motion-sensitive populations. This

complicates the interpretation of results from these studies, making it challenging to

attribute the observed frequency components solely to specific neural mechanisms or

populations.

Interestingly, our results do not implicate specific neural responses sensitive to

repeating motion patterns, or "visual beats", that previous studies have reported

(Nozaradan et al., 2012; Pitchaimuthu et al., 2021). In our experiments, the singleton dot

stimulus always completed a full cycle every 1 second in both phase-locked and

phase-varied conditions. If there were neural responses specific to the periodicity of motion,

we would have observed them in both of our phase conditions. Instead, we only observed

significant frequency components when the modulations of stimulus position were

phase-locked across trials. This suggests that these frequency components were not driven

by neural mechanisms sensitive to the periodicities in motion, but rather by

position-dependent modulation of the EEG signal.

Another interesting aspect of our data is the differing patterns of frequency

components resulting from our polar angle and eccentricity modulations. The polar angle

modulation in Experiment 1 generated complex periodic waveforms that included the first

six harmonics of the modulation frequency ($1f$, $2f$, $3f$, $4f$, $5f$, and $6f$). In contrast, the

eccentricity modulation in Experiment 2 produced simpler, sinusoidal waveforms,

containing only the modulation frequency ($1f$). This difference is intriguing because it

likely reflects how the position-dependent factors influencing EEG strength vary as a

function of polar angle compared to eccentricity.

The frequency components we observed in our simulations always depended on an

interaction between the type of the position modulation and the Retinotopic Weight

Function. As such, different types of position modulation led to different frequency

components even for the same Retinotopic Weight Function. In the experimental data, the

actual Retinotopic Weight Function of the visual system is assumed to be consistent across

the two experiments. Therefore, the difference in the observed frequency components must

be due to the different types of position modulation.

In Experiment 1, the stimulus rotated steadily along an imaginary circle, allowing

variations in the Retinotopic Weight Function across polar angles to be directly captured

in the signal. A constant population response across polar angles would yield a flat signal

with no frequency components, while variations across polar angles would result in

observable frequency components that reflect the specific pattern of the variation. In

Experiment 2, both polar angle and eccentricity were modulated, but only the eccentricity

modulation was phase-locked across trials, which followed a sinusoidal pattern. Thus, if the

Retinotopic Weight Function varied linearly with eccentricity, the resulting signal would

reflect the sinusoidal pattern of the eccentricity modulation. In contrast, a non-linear

variation across eccentricity would produce a more complex, non-sinusoidal signal

containing harmonics of the modulation frequency.

In this regard, our results suggest that the actual Retinotopic Weight Function of

the visual system is one that varies linearly across eccentricity—at least within the range of

our eccentricity modulation (3-7 dva)—and non-linearly across polar angles. This

observation aligns with previous findings indicating that cortical magnification factors and

population receptive field sizes decrease roughly linearly within this eccentricity range (i.e.,

3-7 dva; Daniel and Whitteridge, 1961; Dumoulin and Wandell, 2008) while they vary

non-linearly with polar angle (Silva et al., 2018). However, it remains to be elucidated how

other structural factors, aside from cortical magnification, may contribute to the differences

in results between the two experiments.

We have proposed that the frequency components observed in our results reflect the

brain's structure rather than its function. However, could these position-dependent

frequencies arise from functional rather than structural sources? Specifically, might these frequency components be driven by neural mechanisms that produce stronger or weaker responses based on stimulus position?

The observed frequency components were most prominent in posterior visual areas, where neurons possess small, highly overlapping receptive fields. For example, a neuron in the striate cortex typically has a receptive field spanning less than 1 degree of visual angle (Dow et al., 1981; Schiller et al., 1976). With our position-modulated stimulus, the entire receptive field of such a neuron would be traversed in less than ~30 milliseconds. This suggests that the full range of response variations for this neuron would occur within a time window far shorter than the periods of the frequency components in our data (~160–1000 ms). Furthermore, the overlapping receptive fields of neighboring neurons would generate out-of-phase responses, effectively canceling out these functional variations as the degree of overlap increases. Therefore, large-scale position-dependent signal variations observed in our results cannot originate from fluctuations in individual neuron responses in these early visual areas.

An alternative explanation is that these position-dependent signal variations are mediated by feedback from higher visual areas, where neurons have larger receptive fields. For instance, object-selective neurons in the monkey IT cortex (analogous to the LOC in humans) have receptive fields spanning ~50 dva and exhibit enhanced responses to foveal stimuli (Rolls et al., 2003). Feedback from such neurons to lower-level visual areas could partially explain our findings, particularly regarding eccentricity modulation. However, it remains unclear whether the foveal bias observed in IT neurons originates independently or arises from increased feedforward input from lower-level areas driven by the aforementioned structural factors such as cortical magnification. Consequently, it is still uncertain whether position-dependent responses can emerge in high-level visual areas independently of structural influences.

One of the key advantages of SSVEPs is the ability to isolate and track the activity

of specific neural populations tuned to specific properties of sensory inputs. However, achieving this requires careful consideration of the targeted neural populations that will be influenced by experimental manipulations, as well as the structural and physical factors governing the translation of neural activity into EEG signals. Our study highlights a scenario in which the observed frequency components do not reflect the tuned activity of a selective neural population of interest, but instead capture the inherent discrepancies in EEG strength that vary systematically across different retinotopic areas due to position-dependent factors. If not adequately addressed in the experimental design, these discrepancies could introduce confounding influences into the data, and lead to the misinterpretation of observed frequency components, particularly in the context of position-modulated stimuli. Furthermore, they could also cause variations in response amplitudes across different stimuli if those stimuli are consistently positioned at different positions on the retina.

To mitigate these issues, we propose that researchers should give due consideration to these position-dependent factors when designing SSVEP studies. It is crucial to ensure that the stimuli being compared do not have consistent differences in retinotopic position. Furthermore, in experiments involving moving stimuli, it is essential to clearly distinguish between frequency components arising from the visual processes of interest from those generated by position-dependent factors. In our phase-varied conditions, we randomized the phase of our position modulations while keeping the modulations in other motion-related stimulus properties synchronized across trials. This enabled us to eliminate the frequency components arising from position modulation through phase-cancellation. Future studies can employ similar approaches to effectively isolate the main activity of interest from the influence of position-dependent effects.

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Declaration of interests

The authors declare no competing interests.

Ethics approval

All experimental procedures were reviewed and approved by the Sabancı University Research Ethics Council.

Consent to participate

All participants signed informed consent prior to the experiment session.

Consent for publication

All participants signed informed consent for their anonymized data to be published.

Availability of data and materials

The experiment was not preregistered. All data and materials can be found at the following OSF repository:

https://osf.io/mqb49/?view_only=43e71e2549d8485baa73f1ebc82f230a

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