Break-up and Recovery of Harmony between Direct and Indirect Pathways in The Basal Ganglia; Huntington's Disease and Treatment

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The basal ganglia (BG) in the brain exhibit diverse functions for motor, cognition, and emotion. Such BG functions could be made via competitive harmony between the two competing pathways, direct pathway (DP) (facilitating movement) and indirect pathway (IP) (suppressing movement). As a result of break-up of harmony between DP and IP, there appear pathological states with disorder for movement, cognition, and psychiatry. In this paper, we are concerned about the Huntington's disease (HD), which is a genetic neurodegenerative disorder causing involuntary movement and severe cognitive and psychiatric symptoms. For the HD, the number of D2 SPNs ($N_{\rm D2}$) is decreased due to degenerative loss, and hence, by decreasing $x_{\rm D2}$ (fraction of $N_{\rm D2}$), we investigate break-up of harmony between DP and IP in terms of their competition degree $\mathcal{C}_d$, given by the ratio of strength of DP ($\mathcal{S}_{DP}$) to strength of IP ($\mathcal{S}_{IP}$) (i.e., $\mathcal{C}_d = \mathcal{S}_{DP}/\mathcal{S}_{IP}$). In the case of HD, the IP is under-active, in contrast to the case of Parkinson's disease with over-active IP, which results in increase in $\mathcal{C}_d$ (from the normal value). Thus, hyperkinetic dyskinesia such as chorea (involuntary jerky movement) occurs. Treatment of HD, based on optogenetics, is also investigated through recovery of harmony between DP and IP. Finally, we study effect of loss of healthy synapses of all the BG cells on HD.

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I. INTRODUCTION

The basal ganglia (BG) (called the dark basement of the brain) are a group of subcortical deep-lying nuclei, receiving excitatory cortical input from most areas of cortex, and they provide inhibitory output to the thalamus and brainstem [1–4]. The BG exhibit a variety of functions for motor control and regulation of cognitive and emotional processes [1–10]. Dysfunction in the BG is related to movement disorder [e.g., Parkinson's disease (PD) and Huntington's disease (HD)] and cognitive and psychiatric disorders [1–4].

In this paper, we are concerned about the HD. It is a rare hereditary neurodegenerative disease with severe symptoms for motor, cognition, and emotion [11–17]. As is well known, patients with HD show hyperkinetic dyskinesia such as chorea (involuntary jerky dance-like movement) as well as cognitive (e.g., dementia) and psychiatric (e.g,, depression and anxiety) disorders. In contrast, patients with PD show hypokinetic disorder such as slowed movement (bradykinesia) [18–23]. Thus, if PD lies at one end of the spectrum of movement disorders in the BG, HD lies at the other end. We note that HD is caused by a mutated huntingtin (HTT) gene on chromosome 4 [24, 25]. As a result of mutation in HTT gene, the defective HTT gene has abnormal excessive repeats of a three-base (CAG) DNA sequence; in the mutant gene, the repeat occurs over and over again, from 40 times

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to more than 80. The greater the number of CAG repeats, the earlier the onset and severity of HD. This kind of trinucleotide repeat expansion results in production of abnormal HTT protein that accumulates, resulting in creation of toxic HTT protein aggregates damaging neurons (e.g., death of striatal cells in the BG). Thus, the primary pathological feature of HD is appearance of toxic HTT protein aggregates, causing the characteristic neurodegeneration seen in HD, in contrast to the case of PD where DA deficiency is a major cause.

In our previous work for the PD in the BG [26], we developed a spiking neural network (SNN) for the BG, based on anatomical and physiological data derived from rat-based studies [27–50]. Here, we use rat-brain terminology throughout. The BG receive excitatory cortical input from most regions of cortex via the input nuclei [striatum and subthalamic nucleus (STN)] and project inhibitory output via the output nucleus [substantia nigra pars reticulata (SNr)], through the thalamus to the motor area of the cortex [7, 10]. We also note that, the principal input nucleus, striatum, is the primary recipient of dopamine (DA), arising from the substantia nigra pars compacta (SNc). Within the striatum, spine projection neurons (SPNs), comprising up to 95 % of the whole striatal population, are the only primary output neurons [51, 52]. There are two types of SPNs with D1 and D2 receptors for the DA. The DA modulates firing activity of the D1 and D2 SPNs in a different way [53–55]. In the early stage of HD, degenerative loss of D2 SPNs occurs due to mutation in the HTT gene, while DA level in the striatum is nearly normal [56–59].

There are two competing pathways, direct pathway (DP) and indirect pathway (IP), in the BG [60–63]. D1

SPNs in the striatum make direct inhibitory projection to the output nucleus, SNr, through DP, and then the thalamus becomes disinhibited. Consequently, movement facilitation occurs. In contrast, D2 SPNs are connected to the SNr through IP, crossing the intermediate control nucleus, GP (globus pallidus), and the STN. In the case of IP, the firing activity of the SNr becomes enhanced mainly because of excitatory input from the STN. As a result, firing activity of the thalamus becomes decreased, resulting in movement suppression.

Diverse functions of the BG could be made via "balance" of DP and IP. So far, a variety of subjects for the BG have been investigated in many computational works [5–10, 52–55, 64–89]. But, no quantitative analysis for balance between DP and IP was made. As a first time, in our recent work [26], we made quantitative analysis for competitive harmony (i.e., competition and cooperative interplay) between DP and IP by introducing their competition degree $\mathcal{C}_d$, given by the ratio of strength of DP ($\mathcal{S}_{DP}$) to strength of IP ($\mathcal{S}_{IP}$) (i.e., $\mathcal{C}_d = \mathcal{S}_{DP}/\mathcal{S}_{IP}$); $\mathcal{S}_{DP}$ ($\mathcal{S}_{IP}$) is given by the magnitude of the total time-averaged synaptic current into the output nucleus, SNr, through DP (IP).

In this paper, we take into consideration of degenerative loss of D2 SPNs for the HD; N_{D2} (number of D2 SPNs) $= N_{D2}^*$ (normal value) x_{D2} [$1 > x_{D2}$ (fraction of number of D2 SPNs) ≥ 0] [56–59, 90, 91]. By decreasing x_{D2} from 1, we investigate break-up of harmony between DP and IP for the HD by employing the competition degree $\mathcal{C}_d$ in the case of normal DA level ($\phi = 0.3$). Due to degenerative loss of D2 SPNs, IP becomes under-active (i.e., weakened), leading to increase in $\mathcal{C}_d$ from normal value. Thus, hyperkinetic dyskinesia such as chorea occurs, which is in contrast to the case of PD with reduced $\mathcal{C}_d$, causing hypokinetic disorder. Next, based on optogenetics [92, 93], treatment of HD is also studied via recovery of harmony between DP and IP. Through activation of D2 SPN (STN) and deactivation of GP, IP becomes strengthened and thus harmony between DP and IP may be recovered. Finally, we investigate effect of loss of healthy synapses of all the BG cells on HD [94–99].

This paper is organized as follows. In Sec. II, we describe our SNN for the BG. Then, in the main Sec. III, we make quantitative analysis of break-up and recovery of harmony between DP and IP for the HD. Finally, we give summary and discussion in Sec. IV.

II. BG SPIKING NEURAL NETWORK

In this section, we describe our SNN for the BG. In our recent work [26], we developed our BG SNN, composed of D1/D2 SPNs, STN neurons, GP neurons, and SNr neurons, based on the anatomical and the physiological properties of the BG [27–50]. In our BG SNN, we also consider the modulation effect of DA on D1/D2 SPN and afferent synapses into the D1/D2 SPNs, the STN, and the GP [53–55]. Here, for the sake of completeness and

FIG. 1: Box diagram of our spiking neural network for the basal ganglia (BG). Excitatory and inhibitory connections are denoted by lines with triangles and circles, respectively, and dopamine-modulated cells and connections are represented in blue color. Striatum and STN (subthalamic nucleus), receiving the excitatory cortical input, are two input nuclei to the BG. In the striatum, there are two kinds of inhibitory spine projection neurons (SPNs); SPNs with the D1 receptors (D1 SPNs) and SPNs with D2 receptors (D2 SPNs). The D1 SPNs make direct inhibitory projection to the output nuclei SNr (substantia nigra pars reticulate) through the direct pathway (DP; green color). In contrast, the D2 SPNs are connected to the SNr through the indirect pathway (IP; red color) crossing the GP (globus pallidus) and the STN. The inhibitory output from the SNr to the thalamus/brainstem is controlled through competition between the DP and IP.

understanding of readers, we provide description of our BG SNN; for more details, refer to Sec. II in Ref. [26].

A. Framework of Our SNN of The BG

Figure 1 shows a box diagram of major neurons and synaptic connections in our BG SNN. Our BG SNN consists of striatum and STN (input nuclei), SNr (output nucleus), and GP (intermediate controller). Here, all the BG neurons except the excitatory STN neuron are inhibitory ones.

Both striatum and STN receive cortical inputs from most regions of the cortex. Here, we model cortical inputs in terms of 1,000 independent Poisson spike trains with firing rate f_i ($i = 1, \cdots, 1000$). Tonic cortical input in the resting state has $f = 3$ Hz. On the other hand, the phasic cortical input in the phasically-active state has $f = 10$ Hz, independently of i [7, 52, 55, 78, 100–104]. The striatum is also the primary recipient of the DA (arising from the SNc). Two kinds of SPNs with D1 and D2 receptors for the DA exist within the striatum. They comprise up to 95 % of the whole striatal population [51, 52]. We note that these D1 and D2 SPNs show different firing behaviors because of DA modulation [53–55].

TABLE I: Intrinsic parameter values for each BG cell in the X [= D1 (SPN), D2 (SPN), STN, GP, SNr] population.

Parmeters	D1/D2 SPN	STN	GP	SNr
C_X	16.1	23.0	68.0	172.1
$v_r^{(X)}$	-80.0	-56.2	-53.0	-64.58
$v_t^{(X)}$	-29.3	-41.4	-44.0	-51.8
k_X	1	0.439	0.943	0.7836
a_X	0.01	0.021	0.0045	0.113
b_X	-20	4	3.895	11.057
c_X	-55	-47.7	-58.36	-62.7
d_X	84.2	17.1	0.353	138.4
$v_{peak}^{(X)}$	40	15.4	25	9.8

There are two competing pathways, DP and IP, in the BG [60–63]. The D1 SPNs make direct inhibitory projection to the output nucleus, SNr, via DP (green color in Fig. 1). Then, the thalamus is disinhibited, resulting in movement facilitation. On the other hand, the D2 SPNs are connected to the SNr via IP (red color in Fig. 1), crossing the GP and the STN. Here, the GP plays a role of intermediate controller to control the firing behavior of the STN. In the case of IP, the firing activity of the SNr becomes increased mainly due to excitatory input from the STN. Consequently, firing activity of the thalamus becomes decreased, leading to movement suppression. Thus, the firing activity of the output nucleus, SNr, is controlled through competition between DP (green) and IP (red).

We choose the numbers of the striatal neurons, the STN neurons, the GP neurons, and the SNr neurons in the BG, based on the anatomical information [29]. A scaled-down SNN where the total number of striatal neurons is 2,791, corresponding to $\frac{1}{1000}$ of the $2,791 \cdot 10^3$ striatal cells found in the rat BG, is developed. In this way, we scale down with ratio 10^{-3} for all the BG neurons [75, 81]; $N_{D1} = N_{D2} = 1325$, $N_{STN} = 14$, $N_{GP} = 46$, and $N_{SNr} = 26$ (N_X is the number of neurons in the X population). 90-97 % of the whole striatal population corresponds to the major subpopulation of D1/D2 SPNs [75]; in our BG SNN, we choose 95 %. The remaining 5 % subpopulation of fast spiking interneurons are not considered in our SNN.

The cortex (Ctx) provides the external excitatory inputs randomly to the D1/D2 SPNs and the STN neurons with the connection probabilities, $p_c^{(SPN,Ctx)} = 0.084$ (8.4 %) and $p_c^{(STN,Ctx)} = 0.03$ (3 %), respectively [55]. Here, we consider random synaptic connections between BG cells in Fig. 1. The synaptic connection probabilities $p_c^{(T,S)}$ from a presynaptic neuron in the source population (S) to a postsynaptic neuron in the target population (T) in the BG are as follows [78]: $p_c^{(SNr,D1)} = 0.033$ (3.3 %), $p_c^{(GP,D2)} = 0.033$ (3.3 %), $p_c^{(GP,STN)} = 0.3$ (30 %), $p_c^{(GP,GP)} = 0.1$ (10 %), $p_c^{(STN,GP)} = 0.1$ (10 %), $p_c^{(SNr,STN)} = 0.3$ (30 %), and $p_c^{(SNr,GP)} = 0.1066$ (10.66 %).

B. Izhikevich Spiking Neuron Models and DA Effects in Our BG SNN

The Izhikevich spiking neuron model (which is not only biologically plausible, but also computationally efficient) is used as elements of our BG SNN [105–108]. Unlike the Hodgkin-Huxley-type conductance-based models, the Izhikevich model matches neuronal dynamics by tuning its parameters.

Our BG SNN consists of 5 populations of D1 SPNs, D2 SPNs, STN neurons, GP neurons, and SNr neurons. The following equations govern evolution of dynamical states of individual neurons in the X population [$X =$ D1 (SPN), D2 (SPN), STN, GP, and SNr]:

$$C_X \frac{dv_i^{(X)}}{dt} = k_X(v_i^{(X)} - v_r^{(X)})(v_i^{(X)} - v_t^{(X)})$$
$$-u_i^{(X)} + I_i^{(X)}, \quad (1)$$
$$\frac{du_i^{(X)}}{dt} = a_X \left\{ b_X(v_i^{(X)} - v_r^{(X)}) - u_i^{(X)} \right\};$$
$$i = 1, ..., N_X, \quad (2)$$

with the auxiliary after-spike resetting:

if $v_i^{(X)} \geq v_{peak}^{(X)}$, then $v_i^{(X)} \leftarrow c_X$ and $u_i^{(X)} \leftarrow u_i^{(X)} + d_X$. (3)

Here, N_X and $I_i^{(X)}(t)$ are the total number of neurons and the current into the ith neuron in the X population, respectively. The dynamical state of the ith neuron in the X population at a time t (msec) is given by its membrane potential $v_i^{(X)}(t)$ (mV) and the slow recovery variable $u_i^{(X)}(t)$ (pA). As the membrane potential $v_i^{(X)}(t)$ arrives at its apex $v_{peak}^{(X)}$, the neuron fires, and then both the membrane potential $v_i^{(X)}$ and the recovery variable $u_i^{(X)}$ are reset according to the rules of Eq. (3).

The Izhikevich neuron model has 9 intrinsic parameters in each X population; C_X (membrane capacitance,

pF), $v_r^{(X)}$ (resting membrane potential, mV), $v_t^{(X)}$ (instantaneous threshold potential, mV), k_X (parameter associated with the neuron's rheobase, nS/mV), a_X (recovery time constant, msec^{-1}), b_X (parameter associated with the input resistance, nS), c_X (after-spike reset value of $v_i^{(X)}$, mV), d_X (after-spike jump value of $u_i^{(X)}$, pA), and $v_{peak}^{(X)}$ (spike cutoff value, mV). The 9 intrinsic parameter values of D1 SPN, D2 SPN, STN, GP, and SNr are shown in Table I. We obtain the parameter values of the STN neuron, GP neuron, and SNr neuron, based on the work in [55], in addition to the parameter values of the D1/D2 SPNs given in [53, 54]. These parameter values are based on physiological properties of the D1/D2 SPNs, the STN neurons, the GP neurons, and the SNr neurons [31–41].

Time-evolution of the dynamical state $[v_i^{(X)}(t), u_i^{(X)}(t)]$ is governed by the current $I_i^{(X)}(t)$ into the ith neuron in the X population in Eq. (1), given by:

$$I_i^{(X)}(t) = I_{ext,i}^{(X)}(t) - I_{syn,i}^{(X)}(t) + I_{stim}^{(X)}(t), \qquad (4)$$

where $I_{ext,i}^{(X)}$, $I_{syn,i}^{(X)}(t)$, and $I_{stim}^{(X)}(t)$ represent the external current from the external background region (not considered in the modeling), the synaptic current, and the injected stimulation current, respectively. Here, we consider the case of no injected stimulation DC current (i.e., $I_{stim} = 0$).

We model the external current $I_{ext,i}^{(X)}(t)$ in terms of its time average, $I_{spon,i}^{(X)}$ (spontaneous current for spontaneous firing activity), and fluctuation from the time average, $I_{back,i}^{(X)}(t)$ (random background input). Here, $I_{spon}^{(X)}$ (independent of i) is just the spontaneous in-vivo current, $I_{vivo}^{(X)}$, to obtain the spontaneous in-vivo firing rate $f_{vivo}^{(X)}$ in the presence of synaptic inputs in the tonic cortical resting state. We also model the random background current $I_{back,i}^{(X)}(t)$ as follows:

$$I_{back,i}^{(X)}(t) = D_X \cdot \xi_i^{(X)}(t). \qquad (5)$$

Here, D_X is the noise intensity parameter and $\xi_i^{(X)}$ is the Gaussian white noise, which satisfies the zero mean and the unit variance [109–111]:

$$\langle \xi_i^{(X)}(t) \rangle = 0 \text{ and } \langle \xi_i^{(X)}(t)\xi_j^{(X)}(t') \rangle = \delta_{ij}\delta(t-t'). \quad (6)$$

Finally, we consider the effects of DA modulation on the D1 and D2 SPNs [53–55]. As a result of D1 receptors activation, there occur two opposing effects on intrinsic ion channels. Enhancement of the inward-rectifying potassium current (KIR) results in hyperpolarization of the D1 SPN. On the other hand, decrease in the activation threshold of the L type Ca^{2+} current leads to depolarization of the D1 SPN. These two competing hyperpolarization and depolarization effects may be modeled through changes in intrinsic parameters of the D1 SPN:

$$v_r(1 + \beta_1^{(D1)}\phi_1) \quad \text{and} \quad d(1 - \beta_2^{(D1)}\phi_1), \qquad (7)$$

TABLE II: Spontaneous in-vivo current $I_{vivo}^{(X)}$, in-vivo firing rates $f_{vivo}^{(X)}$, and random background input D_X^* for in-vivo firing activities of BG cells in awake resting state with tonic cortical input (3 Hz) for the normal DA level of $\phi = 0.3$; $X =$ D1 (SPN), D2 (SPN), STN, GP, and SNr

Parmeters	D1/D2 SPN	STN	GP	SNr
$I_{vivo}^{(X)}$	0	56.5	84.0	292.0
$f_{vivo}^{(X)}$	1	9.9	29.9	25.5
D_X^*	246	11.9	274	942

where $\beta_1^{(D1)} = 0.0289$, $\beta_2^{(D1)} = 0.331$, and ϕ_1 is the DA level (i.e., fraction of active DA receptors) for the D1 SPNs. Here, the hyperpolarizing effect of the increasing KIR is modeled by upscaling v_r in Eq. (7). On the other hand, enhanced depolarizing effect of the L type Ca^{2+} current is modelled by downscaling d in Eq. (7). The parameters $\beta_1^{(D1)}$ and $\beta_2^{(D1)}$ denote the amplitudes of their respective effects.

In contrast, small inhibitory effect on the slow A-type potassium current through D2 receptors activation results in decrease in the neuron's rheobase current. We model the depolarizing effect by downscaling the parameter, k:

$$k(1 - \beta^{(D2)}\phi_2), \qquad (8)$$

where ϕ_2 is the DA level for the D2 SPNs, and the parameter $\beta^{(D2)}$ ($= 0.032$) denotes the downscaling degree in k.

In this paper, we consider the case of normal DA level throughout; $\phi_1 = \phi_2 = \phi = 0.3$. In-vivo firing activities of BG neurons in awake resting state with tonic cortical input (3 Hz) are shown in Table II; spontaneous in-vivo currents $I_{vivo}^{(X)}$, in-vivo firing rates $f_{vivo}^{(X)}$, and random background inputs D_X^* in each X population [$X =$ D1 (SPN), D2 (SPN), STN, GP, and SNr] are given.

C. Synaptic Currents and DA Effects in Our BG SNN

We consider the synaptic current $I_{syn,i}^{(X)}(t)$ into the ith neuron in the X population in Eq. (4). As in our previous works [112–117], we follow the "canonical" formalism for the synaptic currents. There are 3 kinds of synaptic currents, $I_{AMPA,i}^{(X,Y)}(t)$, $I_{NMDA,i}^{(X,Y)}(t)$, and $I_{GABA,i}^{(X,Z)}(t)$. Here, $I_{AMPA,i}^{(X,Y)}(t)$ and $I_{NMDA,i}^{(X,Y)}(t)$ are the excitatory AMPA (α-amino-3-hydroxy-5-methyl-4-isoxazolepropionic acid) receptor-mediated and NMDA (N-methyl-D-aspartate) receptor-mediated currents from the presynaptic source Y population to the postsynaptic ith neuron in the target X population. In contrast, $I_{GABA,i}^{(X,Z)}(t)$ is the inhibitory GABA$_A$ (γ-aminobutyric acid type A) receptor-mediated current from the presynaptic source Z population to the postsynaptic ith neuron in the target X population.

The R (= AMPA, NMDA, or GABA) receptor-mediated synaptic current $I_{R,i}^{(T,S)}(t)$ from the presynaptic source S population to the ith postsynaptic neuron in the target T population is given by:

$$I_{R,i}^{(T,S)}(t) = g_{R,i}^{(T,S)}(t)\,(v_i^{(T)}(t) - V_R^{(S)}). \qquad (9)$$

Here, $g_{(R,i)}^{(T,S)}(t)$ and $V_R^{(S)}$ are synaptic conductance and synaptic reversal potential, respectively.

We get the synaptic conductance $g_{R,i}^{(T,S)}(t)$ from:

$$g_{R,i}^{(T,S)}(t) = \tilde{g}_{max,R}^{(T,S)} \sum_{j=1}^{N_S} w_{ij}^{(T,S)}\, s_j^{(T,S)}(t). \qquad (10)$$

Here, $\tilde{g}_{max,R}^{(T,S)}$ is the maximum synaptic conductance and N_S is the number of neurons in the source population. The interpopulation synaptic connection from the source S population to the target T population is given by the connection weight matrix $W^{(T,S)}$ $(= \{w_{ij}^{(T,S)}\})$ where $w_{ij}^{(T,S)} = 1$ in the presence of synaptic connection from the jth neuron in the source S population to the ith neuron in the target T population; otherwise, in the absence of synaptic connection, $w_{ij}^{(T,S)} = 0$.

Fraction of open postsynaptic ion channels (opened via binding of neurotransmitters emitted from the source S population) is represented by $s^{(T,S)}(t)$ in Eq. (10). Time evolution of $s^{(T,S)}(t)$ is given by a sum of exponential-decay functions $E_R^{(T,S)}(t - t_f^{(j)} - \tau_{R,l}^{(T,S)})$:

$$s_j^{(T,S)}(t) = \sum_{f=1}^{F_j^{(S)}} E_R^{(T,S)}(t - t_f^{(j)} - \tau_{R,l}^{(T,S)}). \qquad (11)$$

Here, $t_f^{(j)}$ and $F_j^{(S)}$ are the fth spike time and the total number of spikes of the jth cell in the source S population, respectively, and $\tau_{R,l}^{(T,S)}$ is the synaptic latency time constant for R-mediated synaptic current.

As in our previous works in the cerebellum [112, 113], the exponential-decay function $E_R^{(T,S)}(t)$ (corresponding to contribution of a presynaptic spike occurring at $t = 0$ in the absence of synaptic latency) is given by:

$$E_R^{(T,S)}(t) = e^{-t/\tau_{R,d}^{(T,S)}} \cdot \Theta(t). \qquad (12)$$

Here, $\tau_{R,d}^{(T,S)}$ is the synaptic decay time constant, and $\Theta(t)$ is the Heaviside step function: $\Theta(t) = 1$ for $t \geq 0$ and 0 for $t < 0$.

In the NMDA-receptor case, some of the postsynaptic NMDA channels are known to be blocked by the positive magnesium ion Mg^{2+}. In this case, fraction of NMDA channels that are not blocked by the Mg^{2+} ion is given by a sigmoidal function $f(v^{(T)})$ [53, 55, 118],

$$f(v^{(T)}(t)) = \frac{1}{1 + 0.28 \cdot [Mg^{2+}] \cdot e^{-0.062 v^{(T)}(t)}}. \qquad (13)$$

TABLE III: Parameters for the synaptic currents from the source population (S) to the target population (T): Maximum synaptic conductances $\tilde{g}_{max,R}^{(T,S)}$, synaptic decay times $\tau_{R,d}^{(T,S)}$, synaptic delay times $\tau_{R,l}^{(T,S)}$, and synaptic reversal potential $V_R^{(S)}$.

$S \to T$	R	$\tilde{g}_{max,R}^{(T,S)}$	$\tau_{R,d}^{(T,S)}$	$\tau_{R,l}^{(T,S)}$	$V_R^{(S)}$
Ctx $\to$ D1/D2 SPN	AMPA	0.6	6	10	0
	NMDA	0.3	160	10	0
Ctx $\to$ STN	AMPA	0.388	2	2.5	0
	NMDA	0.233	100	2.5	0
D1 SPN $\to$ SNr	GABA	4.5	5.2	4	-80
D2 SPN $\to$ GP	GABA	3.0	6	5	-65
STN $\to$ GP	AMPA	1.29	2	2	0
	NMDA	0.4644	100	2	0
GP $\leftrightarrow$ GP	GABA	0.765	5	1	-65
GP $\to$ STN	GABA	0.518	8	4	-84
STN $\to$ SNr	AMPA	12	2	1.5	0
	NMDA	5.04	100	1.5	0
GP $\to$ SNr	GABA	73	2.1	3	-80

Here, $v^{(T)}$ is the membrane potential of a neuron in the target population T and $[Mg^{2+}]$ is the equilibrium concentration of magnesium ions $([Mg^{2+}] = 1$ mM).

Thus, the synaptic current into the ith neuron in the target X population becomes

$$I_{syn,i}^{(X)}(t) = I_{AMPA,i}^{(X,Y)}(t) + f(v_i^{(X)}(t)) \cdot I_{NMDA,i}^{(X,Y)}(t) + I_{GABA,i}^{(X,Z)}(t). \qquad (14)$$

Synaptic parameters of the synaptic currents from the source population S to the target population T: maximum synaptic conductance $\tilde{g}_{max,R}^{(T,S)}$, synaptic decay time $\tau_{R,d}^{(T,S)}$, synaptic delay time $\tau_{R,l}^{(T,S)}$, and synaptic reversal potential $V_R^{(S)}$ are shown in Table III. These parameter values are also based on the physiological properties of the relevant neurons [32, 42–50, 54, 55, 78].

Finally, we consider the effect of DA modulation on the synaptic currents into D1 SPN, D2 SPN, STN, and GP neurons in Fig. 1 [53–55]. In the case of synaptic currents into the D1 SPNs, DA modulation effect is modeled by up-scaling the NMDA receptor-mediated current I_{NMDA} with the factor $\beta^{(D1)}$:

$$I_{NMDA}(1 + \beta^{(D1)}\phi_1), \qquad (15)$$

where $\beta^{(D1)} = 0.5$ and ϕ_1 is the DA level for the D1 SPNs. (In the case of D1 SPNs, there is no effect of DA modulation on the AMPA receptor-mediated current I_{AMPA}.) On the other hand, in the case of synaptic currents into the D2 SPNs, DA modulation effect is modeled by down-scaling the AMPA receptor-mediated current I_{AMPA} with the factor $\beta^{(D2)}$:

$$I_{AMPA}(1 - \beta^{(D2)}\phi_2), \qquad (16)$$

FIG. 2: Involuntary jerky movement due to degenerative loss of D2 SPNs in the tonic pathological state for the tonic cortical input (3 Hz) in the resting state. Colors: parts, related to DP (green), while parts, associated with IP (red). (a) Raster plot of spikes and IPSR (instantaneous population spike rate) $R_{D1}(t)$ of D1 SPNs. Raster plots of spikes and IPSRs $R_{D2}(t)$ of D2 SPNs for (b1) $x_{D2} = 1.0$, (b2) 0.8, (b3) 0.5, and (b4) 0.2. (c) Plot of population-averaged MFR (mean firing rate) $\langle f_i^{(D2)} \rangle$ of D2 SPNs versus x_{D2}. Raster plots of spikes and IPSRs $R_{STN}(t)$ of STN neurons for (d1) $x_{D2} = 1.0$, (d2) 0.8, (d3) 0.5, and (d4) 0.2. Raster plots of spikes and IPSRs $R_{GP}(t)$ of GP neurons for (e1) $x_{D2} = 1.0$, (e2) 0.8, (e3) 0.5, and (e4) 0.2. Plots of population-averaged MFRs of (f) STN neurons $\langle f_i^{(STN)} \rangle$ and (g) GP neurons $\langle f_i^{(GP)} \rangle$ versus x_{D2}. (h) Plots of strengths of DP $\mathcal{S}_{DP}$ and IP $\mathcal{S}_{IP}$ versus x_{D2}. (i) Plot of the competition degree $\mathcal{C}_d$ versus x_{D2}. Raster plot of spikes and IPSR $R_{SNr}(t)$ of SNr neurons for (j1) $x_{D2} = 1$, (j2) 0.8, (j3) 0.5, and (j4) 0.2. (k) Plot of population-averaged MFR $\langle f_i^{(SNr)} \rangle$ of SNr neurons versus x_{D2}.

where $\beta^{(D2)} = 0.3$ and ϕ_2 is the DA level for the D2 SPNs. (There is no DA effect on I_{NMDA} for the D2 SPNs.)

Unlike the above cases of D1 and D2 SPNs, there are DA effects on all the synaptic currents, I_{AMPA}, I_{NMDA}, and I_{GABA} into the STN neurons and GP neurons. In these cases, all excitatory and inhibitory synaptic currents, I_{AMPA}, I_{NMDA}, and I_{GABA}, are down-scaled with their scaling factors, depending on ϕ_2 (DA level for the D2 SPNs):

$$(I_{AMPA} + f(v) \cdot I_{NMDA})(1 - \beta_1^{(STN)}\phi_2)$$
$$+ I_{GABA}(1 - \beta_2^{(STN)}\phi_2), \tag{17}$$
$$(I_{AMPA} + f(v) \cdot I_{NMDA})(1 - \beta_1^{(GP)}\phi_2)$$
$$+ I_{GABA}(1 - \beta_2^{(GP)}\phi_2). \tag{18}$$

Here, the scaling factors $\beta_1^{(STN)} = \beta_2^{(STN)} = 0.5$ and $\beta_1^{(GP)} = \beta_2^{(GP)} = 0.5$.

III. QUANTITATIVE ANALYSIS OF BREAK-UP AND RECOVERY OF HARMONY BETWEEN DP AND IP FOR THE HD

In this section, we quantitatively analyze competitive harmony (i.e., competition and cooperative interplay) between DP and IP for the HD in terms of the competition degree $\mathcal{C}_d$ between them, introduced in our previous work [26]. $\mathcal{C}_d$ is given by the ratio of strength of DP ($\mathcal{S}_{DP}$) to strength of IP ($\mathcal{S}_{IP}$) (i.e., $\mathcal{C}_d = \mathcal{S}_{DP}/\mathcal{S}_{IP}$).

We consider the early stage of HD where neurodegerative loss of D2 SPNs occurs; N_{D2} (number of D2 SPNs) $= N_{D2}^*$ (=1325; normal value) x_{D2} [$1 > x_{D2}$ (fraction of number of D2 SPNs) ≥ 0] [56–59, 90, 91]. By decreasing x_{D2} from 1, we investigate break-up of harmony between DP and IP in both cases of tonic cortical input (3 Hz) in the resting state and phasic cortical input (10 Hz) in the phasically active state. In these cases, the IP becomes weakened, and thus $\mathcal{C}_d$ becomes larger than normal ones. Consequently, involuntary jerky movement and abnormal hyperkinetic movement occur in the tonic and phasic cases, respectively. Next, we study treatment

of HD through recovery of harmony between DP and IP. We strengthen the IP via activation of D2 SPNs and STN neurons and deactivation of GP neurons, based on optogenetics [92, 93]. Consequently, harmony between DP and IP becomes recovered, leading to normal movement. Finally, we also investigate the effect of loss of healthy synapses in the BG neurons on the HD.

A. Break-up of Harmony between DP and IP for the HD

In the early stage of HD, we consider the case of normal DA level of $\phi_1 = \phi_2 = \phi = 0.3$ for the D1 and D2 SPNs. As explained in Sec. II A, cortical inputs are modeled in terms of 1,000 independent Poisson spike trains with firing rate f. We first consider the case of tonic cortical input with $f = 3$ Hz in the resting state [7, 52, 55, 78, 100–104].

Population firing behavior of BG neurons could be well visualized in the raster plot of spikes, corresponding to a collection of spike trains of individual BG neurons. Figure 2(a) shows the raster plot of spikes for D1 SPNs, associated with DP (green color). In contrast to the case of D1 SPNs, degenerative loss of D2 SPNs occurs. With decreasing x_{D2} (i.e., fraction of number of D2 SPNs) from 1, we also get the raster plots of spikes of D2 SPNs [Figs. 2(b1)-2(b4)], the STN neurons [Figs. 2(d1)-2(d4)], and the GP neurons [Figs. 2(e1)-2(e4)], related to the IP (red color) for $x_{D2} = 1.0, 0.8, 0.5$, and 0.2.

As a collective quantity showing population behaviors, we employ an IPSR (instantaneous population spike rate) which may be obtained from the raster plot of spikes [119–123]. Each spike in the raster plot is convoluted with a kernel function $K_h(t)$ to get a smooth estimate of IPSR $R_X(t)$ [124]:

$$R_X(t) = \frac{1}{N_X} \sum_{i=1}^{N_X} \sum_{s=1}^{n_i^{(X)}} K_h(t - t_{s,i}^{(X)}). \qquad (19)$$

Here, N_X is the number of the neurons in the X population, and $t_{s,i}^{(X)}$ and $n_i^{(X)}$ are the sth spiking time and the total number of spikes for the ith neuron, respectively. We use a Gaussian kernel function of band width h:

$$K_h(t) = \frac{1}{\sqrt{2\pi}h} e^{-t^2/2h^2}, \qquad -\infty < t < \infty, \qquad (20)$$

where the band width h of $K_h(t)$ is 20 msec. The IPSRs $R_X(t)$ for $X =$ D1 (SPN), D2 (SPN), STN, GP, and SNr are also shown below their respective raster plots of spikes. Here, the case of $x_{D2} = 1$ corresponds to the normal one without degenerative loss of D2 SPNs. With decreasing x_{D2} from 1, the population firing activities of the D2 SPNs, the STN neurons, and the GP neurons, associated with IP (red), are changed, while that of the D1 SPN, related to DP (green), is unchanged.

We also study the population-averaged mean firing rate (MFR) of the neurons $\langle f_i^{(X)} \rangle$ in the X population [$X =$ D1 (SPN), D2 (SPN), STN, and GP]; $f_i^{(X)}$ is the MFR of the ith neuron in the X population, and $\langle \cdots \rangle$ represents a population average over all the neurons. For the D1 and D2 SPNs, $\langle f_i^{(D1)} \rangle = 1.03$ Hz and $\langle f_i^{(D2)} \rangle = 0.97$ Hz, independently of x_{D2}, because there is no change in cortical inputs to the D1/D2 SPNs; see Fig. 2(c) for the D2 SPNs. As x_{D2} is decreased from 1, $\langle f_i^{(GP)} \rangle$ of the GP neurons is increased from 29.9 to 38.8 Hz, due to decrease in inhibitory projection from the D2 SPNs, as shown in Fig. 2(g). In contrast, because of increased inhibitory projection from the GP, $\langle f_i^{(STN)} \rangle$ of the STN neurons is decreased from 9.9 to 6.5 Hz [see Fig. 2(f)].

We note that, there are two types of synaptic currents into the (output) SNr neurons, I_{DP} and I_{IP}, via DP (green) and IP (red) in Fig. 1, respectively. The DP current, $I_{DP}(t)$, is just the (inhibitory) synaptic current from the D1 SPNs to the SNr neurons:

$$I_{DP}(t) = -I_{syn}^{(SNr,D1)}(t). \qquad (21)$$

There is no change in $I_{DP}(t)$, independently of x_{D2}.

The IP current, $I_{IP}(t)$, is composed of the excitatory component, $I_{IP}^{(E)}(t)$, and the inhibitory component, $I_{IP}^{(I)}(t)$:

$$I_{IP}(t) = I_{IP}^{(E)}(t) + I_{IP}^{(I)}(t). \qquad (22)$$

Here, $I_{IP}^{(E)}(t)$ [$I_{IP}^{(I)}(t)$] is just the synaptic current from the STN (GP) to the SNr:

$$I_{IP}^{(E)}(t) = -I_{syn}^{(SNr,STN)}(t) \quad \text{and} \quad I_{IP}^{(I)}(t) = -I_{syn}^{(SNr,GP)}(t). \qquad (23)$$

Unlike the case of $I_{DP}(t)$, with decreasing x_{D2} from 1, $I_{IP}(t)$ becomes decreased due to decrease in $I_{IP}^{(E)}(t)$ and increase in $|I_{IP}^{(I)}(t)|$ ($|\cdots|$: absolute magnitude).

Firing activity of the (output) SNr neurons is determined through competition between $I_{DP}(t)$ (DP current) and $I_{IP}(t)$ (IP current) into the SNr. The strengths of DP and IP, $\mathcal{S}_{DP}$ and $\mathcal{S}_{IP}$, are given by the magnitudes of their respective time-averaged synaptic currents:

$$\mathcal{S}_{DP} = |\overline{I_{DP}(t)}| \quad \text{and} \quad \mathcal{S}_{IP} = |\overline{I_{IP}(t)}|, \qquad (24)$$

where the overline denotes the time averaging and $|\cdots|$ represents the absolute magnitude. Then, the competition degree $\mathcal{C}_d$ between DP and IP (given by the ratio of $\mathcal{S}_{DP}$ to $\mathcal{S}_{IP}$) was introduced in [26]:

$$\mathcal{C}_d = \frac{\mathcal{S}_{DP}}{\mathcal{S}_{IP}}. \qquad (25)$$

For $x_{D2} = 1$ (without degenerative loss of D2 SPNs), $\mathcal{S}_{DP} = 23.1$ and $\mathcal{S}_{IP} = 23.4$, and hence DP and IP become nearly balanced (i.e., $\mathcal{C}_d = 0.99$). In this non-degenerative case, the SNr neurons fire very actively with $\langle f_i^{(SNr)} \rangle = 25.5$ Hz. Due to strong inhibitory projection

FIG. 3: Abnormal hyperkinetic movement due to degenerative loss of D2 SPNs in the phasic pathological state for the phasic cortical input (10 Hz) in the phasically-active state. Colors: parts, related to DP (green), while parts, associated with IP (red). (a) Raster plot of spikes and IPSR (instantaneous population spike rate) $R_{D1}(t)$ of D1 SPNs. Raster plots of spikes and IPSRs $R_{D2}(t)$ of D2 SPNs for (b1) $x_{D2} = 1.0$, (b2) 0.8, (b3) 0.5, and (b4) 0.2. (c) Plot of population-averaged MFR (mean firing rate) $\langle f_i^{(D2)} \rangle$ of D2 SPNs versus x_{D2}. Raster plots of spikes and IPSRs $R_{STN}(t)$ of STN neurons for (d1) $x_{D2} = 1.0$, (d2) 0.8, (d3) 0.5, and (d4) 0.2. Raster plots of spikes and IPSRs $R_{GP}(t)$ of GP neurons for (e1) $x_{D2} = 1.0$, (e2) 0.8, (e3) 0.5, and (e4) 0.2. Plots of population-averaged MFRs of (f) STN neurons $\langle f_i^{(STN)} \rangle$ and (g) GP neurons $\langle f_i^{(GP)} \rangle$ versus x_{D2}. (h) Plots of strengths of DP $\mathcal{S}_{DP}$ and IP $\mathcal{S}_{IP}$ versus x_{D2}. (i) Plot of the competition degree $\mathcal{C}_d$ versus x_{D2}. Raster plot of spikes and IPSR $R_{SNr}(t)$ of SNr neurons for (j1) $x_{D2} =1$, (j2) 0.8, (j3) 0.5, and (j4) 0.2. (k) Plot of population-averaged MFR $\langle f_i^{(SNr)} \rangle$ of SNr neurons versus x_{D2}.

from the SNr, the thalamic cells become silent, resulting in no movement (i.e., the BG door to the thalamus is locked in the normal tonic default state).

But, with decreasing x_{D2} from 1 (degenerative case), as shown in Fig. 2(h), $\mathcal{S}_{IP}$ is rapidly decreased from 23.4 to 1.4 , while there is no change in $\mathcal{S}_{DP}$ ($= 23.1$). In this way, IP for the HD becomes weakened. Thus, as x_{D2} is decreased from 1, the competition degree $\mathcal{C}_d$ between DP and IP is found to increase from 0.99 to 16.5 [see Fig. 2(i)]. Thus, balance between DP and IP becomes broken up in the degenerative tonic case.

Figures 2(j1)-2(j4) show raster plots of spikes and IP-SRs $R_{SNr}(t)$ of the (output) SNr neurons for $x_{D2} = 1.0$, 0.8, 0.5, and 0.2, respectively. We note that, firing activity of the SNr neurons becomes reduced with decreasing x_{D2} because of weakened IP. As a result of decrease in $\mathcal{S}_{IP}$ (strength of IP), the population-averaged MFR $\langle f_i^{(SNr)} \rangle$ is found to decrease from 25.5 to 6.9 Hz with decreasing x_{D2} from 1, as shown in Fig. 2(k). Thus, the BG gate to the thalamus becomes opened even in the case of tonic cortical input (3 Hz) in the resting state via break-up of balance between DP and IP. Consequently,

a tonic pathological state with involuntary jerky movement occurs, in contrast to the tonic default state without movement.

Next, we consider the case of phasic cortical input (10 Hz) in the phasically active state [7, 52, 55, 78, 100–104], which is shown in Fig. 3. Population firing behavior of D1 SPNs, associated with DP (green color), is shown in their raster plot of spikes and the IPSR $R_{D1}(t)$ in Fig. 3(a). In comparison to the tonic case with the population-averaged MFR $\langle f_i^{(D1)} \rangle = 1.03$ Hz in Fig. 2(a), firing activity of the D1 SPNs become very active with $\langle f_i^{(D1)} \rangle = 30.7$ Hz, independently of x_{D2}.

But, due to degenerative loss of D2 SPNs, population firing activities of the D2 SPNs, the STN neurons, and the GP neurons [related to the IP (red color)] are changed with decreasing x_{D2}, as shown in their raster plots of spikes and IPSRs in Fig. 3. The population-averaged MFRs of the D2 SPNs, the STN neurons, and the GP neurons are also shown in Figs. 3(c), 3(f), and 3(g), respectively. For the D2 SPNs, $\langle f_i^{(D2)} \rangle = 24.1$ Hz [much larger than that (0.97 Hz) in the tonic case], indepen-

FIG. 4: Treatment of tonic pathological state by strengthening IP for the tonic cortical input (3 Hz). Colors: parts, related to DP (green), while parts, associated with IP (red). (1) Activation of D2 SPN: Plots of (a1) $\mathcal{S}_{DP}$ (green circles) and $\mathcal{S}_{IP}$ (red crosses), (a2) $\mathcal{C}_d$, and (a3) $\langle f_i^{(SNr)} \rangle$ versus $\Delta I_{ion}^{(D2)}$ for $x_{D2} = 0.5$. (b) Plot of threshold $\Delta I_{ion}^{(D2)*}$ versus x_{D2}. (2) Activation of STN: Plots of (c1) $\mathcal{S}_{DP}$ and $\mathcal{S}_{IP}$, (c2) $\mathcal{C}_d$, and (c3) $\langle f_i^{(SNr)} \rangle$ versus $\Delta I_{ion}^{(STN)}$ for $x_{D2} = 0.5$. (d) Plot of threshold $\Delta I_{ion}^{(STN)*}$ versus x_{D2}. (3) Deactivation of GP: Plots of (e1) $\mathcal{S}_{DP}$ and $\mathcal{S}_{IP}$, (e2) $\mathcal{C}_d$, and (e3) $\langle f_i^{(SNr)} \rangle$ versus $\Delta I_{ion}^{(GP)}$ for $x_{D2} = 0.5$. (f) Plot of threshold $\Delta I_{ion}^{(GP)*}$ versus x_{D2}. (4) Ablation of GP: Plots of (g1) $\mathcal{S}_{DP}$ and $\mathcal{S}_{IP}$, (g2) $\mathcal{C}_d$, and (g3) $\langle f_i^{(SNr)} \rangle$ versus x_{GP} for $x_{D2} = 0.5$. (h) Plot of threshold x_{GP}^* versus x_{D2}. Horizontal dashed lines in (a2), (c2), (e2), and (g2) represent $\mathcal{C}_d^*$ $(= 1.0)$ for the default healthy tonic state when $x_{D2} = 1$. Horizontal dashed lines in (a3), (c3), (e3), and (g3) represent $\langle f_i^{(SNr)} \rangle$ $(=25.5$ Hz) for the default healthy tonic state when $x_{D2} = 1$.

dently of x_{D2}, because there is no change in cortical input to the D2 SPNs. As a result of decreased inhibitory projection from the D2 SPNs, $\langle f_i^{(GP)} \rangle$ of the GP neurons is rapidly increased from 7.3 to 66.1 Hz with decreasing x_{D2} from 1; the increasing rate is higher than the tonic case. On the other hand, due to increase in inhibitory projection from the GP, $\langle f_i^{(STN)} \rangle$ of the STN neurons decreases from 39.8 to 17.6 Hz; the decreasing rate is also larger than that in the tonic case.

We consider the case of $x_{D2} = 1$ without degeneration. In this non-degenerative case, $\mathcal{S}_{DP} = 2309.7$ and $\mathcal{S}_{IP} = 815.6$. Thus, the competition degree becomes $\mathcal{C}_d = 2.82$ [i.e., $\mathcal{S}_{DP}$ (strength of DP) is 2.82 times larger than $\mathcal{S}_{IP}$ (strength of IP)]. In this case, $\langle f_i^{(SNr)} \rangle$ of the (output) SNr neurons are decreased to 5.5 Hz (cf., in the tonic case, 25.5 Hz). Consequently, the BG door to the thalamus becomes opened, leading to normal movement. This phasic healthy state with $\mathcal{C}_d = 2.82$ is in contrast to the tonic healthy state with $\mathcal{C}_d \simeq 1.0$ resulting in no movement.

However, as x_{D2} is decreased from 1 (degenerative case), $\mathcal{S}_{IP}$ is rapidly decreased from 815.6 to 92.3 , while there is no change in $\mathcal{S}_{DP}$ ($= 2309.7$) [see Fig. 3(h)].

Thus, IP becomes rapidly weakened. Due to such underactivity of IP, the competition degree $\mathcal{C}_d$ increases from 2.82 (healthy state) to 25.0, as shown in Fig. 3(i). Consequently, harmony between DP and IP becomes broken up in the degenerative case with $x_{D2} < 1$, and then a phasic pathological state with abnormal hyperkinetic movement appears, in contrast to the phasic healthy state with normal movement.

Raster plots of spikes and IPSRs $R_{SNr}(t)$ of the (output) SNr neurons for $x_{D2} = 1.0, 0.8, 0.5,$ and 0.2 are shown in Figs. 3(j1)-3(j4), respectively. Due to underactivity of IP, firing activity of the SNr neurons becomes decreased with decreasing x_{D2} from 1. Due to decreased $\mathcal{S}_{IP}$ (strength of IP), the population-averaged MFR $\langle f_i^{(SNr)} \rangle$ decreases from 5.5 (healthy state) to 0.7 Hz with decreasing x_{D2} from 1 [see Fig. 3(k)]. In this phasic pathological state with $\mathcal{C}_d > 2.82$ (where harmony between DP and IP is broken up), abnormal hyperkinetic movement disorder occurs, in contrast to the normal movement for the phasic healthy state with $\mathcal{C}_d = 2.82$ (where there is harmony between DP and IP).

To sum up the above results briefly, it is shown that, for the HD, pathological states (where harmony between

DP and IP is broken up) appear due to degenerative loss of D2 SPNs in the cases of both tonic and phasic cortical inputs. On the other hand, for the PD, pathological states appear because of DA deficiency [18–23, 26]. In the case of HD, IP is under-active, in contrast to the case of PD with over-active IP. Thus, patients with HD exhibit abnormal hyperkinetic movement disorder, while patients with PD show abnormal hypokinetic movement disorder. Consequently, HD lies at one end of the spectrum of movement disorders in the BG, while PD lies at the other end.

B. Treatment of HD via Recovery of Harmony between DP and IP

For the pathological state in the HD, IP is under-active due to degenerative loss of D2 SPNs, in comparison to the healthy state. Thus, harmony between DP and IP is broken up (i.e. occurrence of disharmony between DP and IP), leading to abnormal hyperkinetic movement disorder. Here, we investigate treatment of the pathological state with enhanced competition degree $\mathcal{C}_d$ (than the normal one for the healthy state) in both cases of tonic and phasic cortical inputs via recovery of harmony between DP and IP.

Activation and deactivation of the target neurons via optogenetics are studied in [26]. When light-sensitive proteins (called the opsins) are activated through light stimulation, variation in the intrinsic ionic currents of the neurons in the target population X, $\Delta I_{ion}^{(X)}$, takes place. If $\Delta I_{ion}^{(X)}$ is positive (negative), firing activity of the target neurons is increased (decreased), leading to their activation (deactivation) [92, 93]. As discussed in [26], we simulate the effects of optogenetics by adding $\Delta I_{ion}^{(X)}$ in Eq. (1), in addition to the current, $I_i^{(X)}$, into the target X population. With increasing the intensity of light stimulation, the magnitude of $\Delta I_{ion}^{(X)}$ also increases.

We first consider tonic pathological states with enhanced competition degree $\mathcal{C}_d$ [larger than that (1) for the tonic healthy state (with balanced DP and IP)], occurring due to degenerative loss of D2 SPNs, in the case of tonic cortical input (3 Hz) (see Fig. 2). As an example, we consider the tonic pathological case of $x_{\rm D2} = 0.5$ with $\mathcal{C}_d = 1.53$. In this pathological case, IP is under-active in comparison to the tonic healthy case (with balanced DP and IP); firing activity of D2 SPNs is under-active, leading to over-activity of GP neurons, which then results in under-activity of the STN neurons. Hence, for recovery of balance between DP and IP, we try to strengthen the IP via activation of D2 SPNs and STN neurons and deactivation of GP neurons.

We first strengthen the IP through activation of the target (under-active) D2 SPNs. Figure 4(a1) shows plots of $\mathcal{S}_{IP}$ (strength of IP) and $\mathcal{S}_{DP}$ (strength of DP) versus $\Delta I_{ion}^{(\rm D2)}$. As $\Delta I_{ion}^{(\rm D2)}$ is increased from 0, $\mathcal{S}_{IP}$ (red) increases from 15.1, while $\mathcal{S}_{DP}$ (green) remains unchanged

(i.e., 23.1). As a result of increase in $\mathcal{S}_{IP}$, the competition degree $\mathcal{C}_d$ between DP and IP is found to decrease from 1.53 [Fig. 4(a2)]. Also, the population-averaged MFR of the output SNr neurons, $\langle f_i^{(\rm SNr)} \rangle$, is found to increase from 16.1 Hz [Fig. 4(a3)].

We note that, as $\Delta I_{ion}^{(\rm D2)}$ passes a threshold $\Delta I_{ion}^{(\rm D2)*}$ (= 262 pA), $\mathcal{C}_d = \mathcal{C}_d^*$ (= 1.0) and $\langle f_i^{(\rm SNr)} \rangle = \langle f_i^{(\rm SNr)*} \rangle$ (= 25.5 Hz); $\mathcal{C}_d^*$ and $\langle f_i^{(\rm SNr)*} \rangle$ are those for the tonic healthy state, and they are represented by the horizontal dashed lines in Figs. 4(a2) and 4(a3). Thus, for $x_{\rm D2} = 0.5$, the pathological state with $\mathcal{C}_d = 1.53$ may have $\mathcal{C}_d$ (= 1.0) via activation of D2 SPNs for the threshold, $\Delta I_{ion}^{(\rm D2)*}$ (= 262 pA); DP and IP becomes balanced, as in the case of tonic healthy state. In this way, balance between DP and IP is recovered for $\Delta I_{ion}^{(\rm D1)*} = 262$ pA. Figure 4(b) shows the plot of $\Delta I_{ion}^{(\rm D2)*}$ versus $x_{\rm D2}$. As $x_{\rm D2}$ is decreased from 1, the threshold $\Delta I_{ion}^{(\rm D2)*}$ is increased; with decreasing $x_{\rm D2}$, more $\Delta I_{ion}^{(\rm D2)*}$ is necessary for recovery of balance between DP and IP.

We also strengthen the IP via activation of the target (under-active) STN neurons, which is shown in Figs. 4(c1)-4(c3) for $x_{\rm D2} = 0.5$. All the behaviors are qualitatively the same as those in the case of activation of D2 SPNs. With increasing $\Delta I_{ion}^{(\rm STN)}$ from 0, $\mathcal{S}_{IP}$ (strength of IP) increases, leading to decrease in the competition degree $\mathcal{C}_d$, and the population-averaged MFR of the output SNr neurons, $\langle f_i^{(\rm SNr)} \rangle$, also increases. But, the threshold $\Delta I_{ion}^{(\rm STN)*}$ (= 14 pA), where balance between DP and IP is recovered (i.e., $\mathcal{C}_d = 1$ and $\langle f_i^{(\rm SNr)} \rangle = 25.5$ Hz, as in the case of tonic healthy state), is smaller than that (262 pA) in the case of activation of D2 SPNs. The mono-synaptic effect of STN neurons on the output SNr neurons is more direct than the bi- or tri-synaptic effect of D2 SPNs, which could result in the smaller threshold $\Delta I_{ion}^{(\rm STN)*}$ in the case of STN neurons. Figure 4(d) shows the plot of $\Delta I_{ion}^{(\rm STN)*}$ versus $x_{\rm D2}$. With decreasing $x_{\rm D2}$ from 1, the threshold $\Delta I_{ion}^{(\rm STN)*}$ increases, as shown in Fig. 4(d); As $x_{\rm D2}$ is decreased, more $\Delta I_{ion}^{(\rm STN)*}$ is necessary for recovery of balance between DP and IP.

Unlike the cases of activation of (under-active) D2 SPNs and STN neurons, IP may be strengthened via deactivation of (over-active) GP neurons; in the case of deactivation, $\Delta I_{ion}^{(\rm GP)}$ is negative, in contrast to the case of activation with $\Delta I_{ion}^{(X)} > 0$ [$X =$ D2 (SPN) and STN]. Figures 4(e1)- 4(e3) and 4(f) show the case of deactivation of GP neurons. As the magnitude of $\Delta I_{ion}^{(\rm GP)}$ is increased (i.e., more negative), strength of IP, $\mathcal{S}_{IP}$ (red), is found to increase from 15.1, while $\mathcal{S}_{DP}$ (green) remains constant (= 23.1). Thus, when passing a threshold $\Delta I_{ion}^{(\rm GP)*} = -28$ pA, balance between DP and IP becomes recovered (i.e., the competition degree $\mathcal{C}_d$ becomes 1 and the population-averaged MFR of output SNr neurons $\langle f_i^{(\rm SNr)} \rangle$ becomes 25.5 Hz) [see Figs. 4(e2)-

FIG. 5: Treatment of phasic pathological state by strengthening IP for the phasic cortical input (10 Hz). Colors: parts, related to DP (green), while parts, associated with IP (red). (1) Activation of D2 SPN: Plots of (a1) $\mathcal{S}_{DP}$ and $\mathcal{S}_{IP}$, (a2) $\mathcal{C}_d$, and (a3) $\langle f_i^{(\mathrm{SNr})} \rangle$ versus $\Delta I_{ion}^{(\mathrm{D2})}$ for $x_{\mathrm{D2}} = 0.5$. (b) Plot of threshold $\Delta I_{ion}^{(\mathrm{D2})*}$ versus x_{D2}. (2) Activation of STN: Plots of (c1) $\mathcal{S}_{DP}$ and $\mathcal{S}_{IP}$, (c2) $\mathcal{C}_d$, and (c3) $\langle f_i^{(\mathrm{SNr})} \rangle$ versus $\Delta I_{ion}^{(\mathrm{STN})}$ for $x_{\mathrm{D2}} = 0.5$. (d) Plot of threshold $\Delta I_{ion}^{(\mathrm{STN})*}$ versus x_{D2}. (3) Deactivation of GP: Plots of (e1) $\mathcal{S}_{DP}$ and $\mathcal{S}_{IP}$, (e2) $\mathcal{C}_d$, and (e3) $\langle f_i^{(\mathrm{SNr})} \rangle$ versus $\Delta I_{ion}^{(\mathrm{GP})}$ for $x_{\mathrm{D2}} = 0.5$. (f) Plot of threshold $\Delta I_{ion}^{(\mathrm{GP})*}$ versus x_{D2}. (4) Ablation of GP: Plots of (g1) $\mathcal{S}_{DP}$ and $\mathcal{S}_{IP}$, (g2) $\mathcal{C}_d$, and (g3) $\langle f_i^{(\mathrm{SNr})} \rangle$ versus x_{GP} for $x_{\mathrm{D2}} = 0.5$. (h) Plot of threshold x_{GP}^* versus x_{D2}. Horizontal dashed lines in (a2), (c2), (e2), and (g2) represent $\mathcal{C}_d^*$ (= 2.82) for the healthy phasic state when $x_{\mathrm{D2}} = 1$. Horizontal dashed lines in (a3), (c3), (e3), and (g3) represent $\langle f_i^{(\mathrm{SNr})} \rangle$ (= 5.5 Hz) for the healthy phasic state when $x_{\mathrm{D2}} = 1$.

4(e3)]. As shown in Fig. 4(f), with decreasing x_{D2} from 1, the threshold $\Delta I_{ion}^{(\mathrm{GP})*}$ is decreased (i.e., its magnitude increases); as x_{D2} is decreased from 1, more negative $\Delta I_{ion}^{(\mathrm{GP})*}$ is required for recovery of balance between DP and IP.

Instead of the above deactivation of GP neurons via optogenetics, we also consider ablation of (over-active) GP neurons in the pathological state for $x_{\mathrm{D2}} = 0.5$ to reduce the over-activity of GP neurons. In the case of ablation, the number of GP neurons, N_{GP}, is reduced to $N_{\mathrm{GP}}^{(n)} x_{\mathrm{GP}}$ $(1 > x_{\mathrm{GP}} > 0)$, where $N_{\mathrm{GP}}^{(n)}$ (= 46) is the normal number of GP neurons and x_{GP} is the fraction of number of GP neurons. As shown in Figs. 4(g1)- 4(g3) and 4(h), the effect of decreasing x_{GP} via ablation is similar to that of deactivation of GP neurons via optogenetics. As x_{GP} is decreased from 1, strength of IP, $\mathcal{S}_{IP}$ (red), is found to increase from 15.1 (i.e., IP becomes strengthened) [see Fig. 4(g1)]. When passing a threshold, x_{GP}^* ($\simeq 0.78$), balance between DP and IP becomes recovered (i.e., $\mathcal{C}_d$ = 1.0 and $\langle f_i^{(\mathrm{SNr})} \rangle$ = 25.5 Hz), as shown in Figs. 4(g2)- 4(g3). Figure 4(h) shows the plot of x_{GP}^* versus x_{D2}. With decreasing x_{D2} from 1, x_{GP}^* decreases; more ablation (i.e., smaller x_{GP}) is necessary for balance between

DP and IP.

Next, we consider phasic pathological states with enhanced competition degree $\mathcal{C}_d$ [larger than that (2.82) for the phasic healthy state (with harmony between DP and IP)], occurring due to degenerative loss of D2 SPNs, in the case of phasic cortical input (10 Hz) (see Fig. 3). As an example, we consider the pathological case of $x_{\mathrm{D2}} = 0.5$ with $\mathcal{C}_d = 7.19$. In this phasic pathological case, IP is under-active in comparison to the case of phasic healthy state. For the phasic healthy state with $\mathcal{C}_d^* = 2.82$ (i.e., harmony between DP and IP), the population-averaged MFR of output STr neurons, $\langle f_i^{(\mathrm{SNr})*} \rangle$, is much reduced to 5.5 Hz, leading to normal movement, in contrast to the case of tonic healthy state with $\mathcal{C}_d \simeq 1.0$ and $\langle f_i^{(\mathrm{SNr})} \rangle$ = 25.5 Hz without movement. As in the above tonic pathological state, firing activity of D2 SPNs is under-active, resulting in over-activity of GP neurons, which then leads to under-activity of the STN neurons. Hence, for recovery of harmony between DP and IP, we strengthen the IP through activation of D2 SPNs and STN neurons and deactivation of GP neurons by employing optogenetic technique and via ablation of GP neurons.

(1) Tonic Pathological State

(2) Phasic Pathological State

FIG. 6: Effect of loss of healthy synapses in all the BG neurons on the HD for $x_{D2} = 0.5$. Colors: parts, related to DP (green), while parts, associated with IP (red). (1) Tonic pathological state: Plots of (a) $\mathcal{S}_{DP}$ and $\mathcal{S}_{IP}$, (b) $\mathcal{C}_d$, and (c) $\langle f_i^{(SNr)} \rangle$ versus x_c. (2) Phasic pathological state: Plots of (d) $\mathcal{S}_{DP}$ and $\mathcal{S}_{IP}$, (e) $\mathcal{C}_d$, and (f) $\langle f_i^{(SNr)} \rangle$ versus x_c.

Figure 5 shows treatment of phasic pathological state for $x_{D2} = 0.5$ with $\mathcal{C}_d = 7.19$; (1) activation of D2 SPNs, (2) activation of STN neurons, (3) deactivation of GP neurons, and (4) ablation of GP neurons. The overall results of these treatments are qualitatively the same as those in the above case of tonic pathological state in Fig. 4. Only the corresponding thresholds are quantitatively different; (1) $\Delta I_{ion}^{(D2)*} = 1{,}636$ pA, (2) $\Delta I_{ion}^{(STN)*} = 405$ pA, (3) $\Delta I_{ion}^{(GP)*} = -540$ pA, and (4) x_{GP}^{*} ($\simeq 0.52$). When passing a threshold for each treatment, harmony between DP and IP becomes recovered (i.e., $\mathcal{C}_d = 2.82$ and $\langle f_i^{(SNr)} \rangle = 5.5$ Hz), resulting in normal movement. Finally, we note that, with decreasing x_{D2}, the thresholds, $\Delta I_{ion}^{(D2)*}$ and $\Delta I_{ion}^{(STN)*}$, for activations of D2 SPNs and STN neurons are increased (i.e., more positive), and the threshold, $\Delta I_{ion}^{(GP)*}$ for deactivation of GP neurons becomes more negative, as shown in Figs. 5(b), 5(d), and 5(f). Thus, as x_{D2} is decreased, more light stimulation for activation and deactivation is necessary for recovery of harmony between DP and IP. Also, in the case of ablation of GP neurons, with decreasing x_{D2}, more ablation is required to get harmony between DP and IP.

C. Effect of Loss of Healthy Synapses on The HD

In the HD, loss of healthy synapses occurs not only in the striatum, but also in other regions of the BG, including STN, GP, and SNr [94–99]. Such loss of synapses in the BG neurons is an important feature of HD, and it is thought to contribute to the motor and cognitive symptoms of the disease. Here, we study effect of loss of healthy synapses of all the BG neurons on HD.

As examples, we consider pathological states for $x_{D2} = 0.5$ in both cases of tonic (3 Hz) and phasic (10 Hz) cortical inputs. Loss of synapses in the BG neurons is

modeled in terms of decreased synaptic connection probability, $p_c = p_c^{(n)} x_c$; $p_c^{(n)}$ is the normal synaptic connection probability (depending on the type of BG neurons and given in the subsection II A) and x_c represents the fraction in p_c ($1 > x_c > 0$).

We first consider a tonic pathological state in Figs. 6(a)-6(c). As a result of loss of synapses, decreased cortical inputs into D1 SPNs leads to reduction in their firing activity $\langle f_i^{(D1)} \rangle$. Then, strength of DP, $\mathcal{S}_{DP}$, becomes decreased. As shown in Fig. 6(a), $\mathcal{S}_{DP}$ (green color) is found to monotonically decrease from 23.1 with decreasing x_c from 1. Also, due to reduced cortical synaptic inputs into D2 SPNs, firing activity of D2 SPNs, $\langle f_i^{(D2)} \rangle$, becomes decreased, leading to increased firing activity of GP neurons ($\langle f_i^{(GP)} \rangle$), which then results in decrease in the firing activity of STN neurons ($\langle f_i^{(STN)} \rangle$). Consequently, strength of IP, $\mathcal{S}_{IP}$, becomes decreased. In this case of IP, with decreasing x_c from 1, $\mathcal{S}_{IP}$ (red color) is found to more rapidly decrease from 15.1 than the case of DP. Then, the competition $\mathcal{C}_d$ between DP and IP increases rapidly from 1.53 with decreasing x_c from 1 [see Fig. 6(b)]. Thus, as x_c is decreased from 1, population-averaged MFR of the output SNr neurons ($\langle f_i^{(SNr)} \rangle$) decreases from 16.1 Hz. In this way, with decreasing x_c, the degree of disharmony between DP and IP becomes increased, resulting in more severe involuntary jerky movement in the tonic pathological case.

Next, we consider a phasic pathological state in Figs. 6(d)-6(f). With decreasing x_c, tendency in the phasic pathological case is qualitatively the same as that in the above tonic pathological case. Based on the same reasoning given in the tonic pathological case, as x_c is decreased from 1, strength of IP ($\mathcal{S}_{IP}$; red color) is found to decreases much more rapidly than strength of DP ($\mathcal{S}_{DP}$; green color), as shown in Fig. 5(d). Then, the competition degree $\mathcal{C}_d$ increases from 7.19 with decreasing x_c from 1 [see Fig. 5(e)]. Consequently, firing activity of the output SNr neurons ($\langle f_i^{(SNr)} \rangle$) decreases from 2.7 Hz with x_c, as shown in Fig. 5(f). In this way, as x_c is decreased from 1, the broken-up degree of harmony between DP and IP becomes increased, leading to more severe abnormal hyperkinetic movement disorder in the phasic pathological case.

Overall, in both tonic and phasic pathological cases, as a result of loss of healthy synapses in the BG neurons, symptoms of the HD become more severe with decreasing x_c, because the disharmony degree between DP and IP becomes increased.

IV. SUMMARY AND DISCUSSION

The BG exhibit a variety of functions for motor, cognition, and emotion. Dysfunction in the BG is associated with movement disorder (e.g., HD and PD) and cognitive and psychiatric disorders. There are two competing pathways in the BG, DP (facilitating movement) and

IP (suppressing movement) [60–63]. In our recent work [26], as a first time, we made quantitative analysis of competitive harmony between DP and IP in the default tonic state and the phasic healthy and pathological states by introducing their competition degree, $\mathcal{C}_d$, between DP and IP, given by the ratio of strength of DP ($\mathcal{S}_{DP}$) to strength of IP ($\mathcal{S}_{IP}$) (i.e., $\mathcal{C}_d = \mathcal{S}_{DP}/\mathcal{S}_{IP}$).

In the case of normal DA level. a healthy state with normal movement was found to appear, while in the case of lower DA level, a pathological state (PD) with reduced competition degree was found to occur. In PD, DP is under-active, while IP is over-active, resulting in abnormal hypokinetic movement.

In this paper, we are concerned in the HD which is a genetic neurodegenerative disease. As a result of mutant HTT gene, toxic HTT protein aggregates appear, causing the characteristic neurodegeneration seen in HD. We considered degenerative loss of D2 SPNs in the case of normal DA level. By decreasing x_{D2} (i.e. fraction of number of D2 SPNs) from 1, we quantitatively analyzed break-up of harmony between DP and IP. IP was found to be under-active (i.e., weakened), in contrast to the case of PD with over-active IP. Thus, the competition degree $\mathcal{C}_d$ becomes increased than normal one. Consequently, abnormal hyperkinetic movement such as chorea occurs, in contrast to the case of PD with hypokinetic disorder.

Unfortunately, at present there is no cure for HD. The available treatments for HD primarily aim to control and alleviate its symptoms, resulting from weakened IP: medication treatment [125–128], reducing symptoms, deep brain stimulation in research and clinical trials [129–131], and experimental surgery [132]. We studied treatment of HD via recovery of harmony between DP and IP by activating D2 SPNs and STN neurons and deactivating GP neurons, based on optogenetics [92, 93]. Through the treatment process, the IP becomes strengthened, and thus harmony between DP and IP may be regained. We also studied effects of loss of healthy synapses of the BG cells on the HD. As a result of such synaptic loss, the HD status was found to become more severe.

Finally, we discuss limitations of our present work and future works. In the present work, we considered early stage of HD where degenerative loss of D2 SPNs occurs in the nearly normal DA level. But, in the late stage of HD, degenerative loss of D1 SPN also occurs along with decrease in DA level, leading to hypokinetic disorder (e.g., rigidity and bradykinesia) due to weakened DP, as in the case of PD [133]. Moreover, in addition to deaths of D1/D2 SPNs, degeneration of cortical pyramidal cells occurs [134, 135]. Hence, as a future work, it would be interesting to investigate consequences of degeneration of D1 SPNs and cortical pyramidal cells, in addition to degenerative loss of D2 SPNs.

Next, we would like to consider more realistic striatal circuit in the BG. In our present striatal circuit, we considered only the D1/D2 SPNs (95 % major population). But, the minor population of fast interneurons (FSIs) in the striatum are known to exert strong effects on firing activities of the D1/D2 SPNs [52, 136]. Hence, in future, it would be worth while to contain the FSIs in our BG SNN. In our present BG SNN, cortical inputs were modelled by Poisson spike trains. Such SNN could be extended to the cortico-BG-thalamo-cortical (CBGTC) loop by including the cortical and the thalamic neurons for more complete computational work [66, 137].

We also make discussion on application of the optogenetics to human patients for treatment of a pathological state [138, 139]. In the case of HD, harmony between DP and IP is broken up due to under-active IP. As shown in Sec. III B, harmony between DP and IP could be recovered by strengthening IP. To this end, optogenetic techniques may be employed. Activation of D2 SPNs and STN neurons via optogenetics results in strengthening IP. We hope that, in near future, safe clinical applications of optogenetics to human patients with HD could be successfully available via collaboration of researchers and clinicians. Then, it would take a substantial step forward for treatment of HD.

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