Presaccadic attention enhances and reshapes the Contrast Sensitivity Function around the visual field

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Abstract

The visual world is processed with a great degree of non-uniformity across eccentricity and around polar angle locations. Contrast sensitivity, a fundamental visual dimension constraining our vision, drops drastically from foveal to peripheral locations. It also decreases from the horizontal to the vertical meridian, and from the lower vertical to the upper vertical meridian (i.e., polar angle asymmetries). Moreover, contrast sensitivity is a function of spatial frequency, and the general relation between the two dimensions is referred to as the Contrast Sensitivity Function (CSF). To overcome constraints of the visual system throughout the visual field, we constantly make rapid saccadic eye movements to foveate on relevant objects in the visual scene. Already before saccade onset, attention shifts to the saccade target location (upcoming fovea) and enhances visual processing at that location. This *presaccadic shift of attention* typically benefits contrast sensitivity, but it is unknown whether and how it modulates the CSF and if this effect varies around polar angle locations. Contrast sensitivity enhancement may result from a horizontal or vertical shift of the CSF, increase in bandwidth, or any of their combinations, and the magnitude may differ around the visual field. In the current study, we investigated these possibilities by extracting key attributes of the CSF using Hierarchical Bayesian Modeling. First, we characterized how the CSF varies around polar angle. Then we compared the CSF attributes during fixation and saccade preparation (presaccadic attention). The results reveal that presaccadic attention (1) enhances contrast sensitivity across a wide range of spatial frequencies, (2) increases both the most preferred and the highest discernable spatial frequency, and (3) narrows the bandwidth. Importantly, the presaccadic enhancement in contrast sensitivity was more pronounced along the horizontal than the vertical meridian, exacerbating the polar angle asymmetries present during fixation. In conclusion, presaccadic attention bridges the gap between presaccadic peripheral and post-saccadic foveal input by rendering more of the world visible at the saccade target, and more so at the horizontal than the vertical meridian.

Introduction

Visual processing is heterogeneous — it varies across eccentricity and around polar angle locations. Our visual ability to process fine details at the center of gaze declines rapidly with eccentricity, and peripheral acuity is about 50 times lower than that in the fovea (Frisén & Glansholm, 1975). Moreover, at iso-eccentric locations, visual performance changes as a function of polar angle (**Figure 1a,** see Himmelberg, Winawer, & Carrasco, 2023 for review): it is better along the horizontal than vertical meridian (HVA: Horizontal-Vertical Anisotropy) and along the lower than the upper vertical meridian (VMA: Vertical Meridian Asymmetry).

These constraints of the visual system can be mitigated by deployment of spatial attention. *Covert* spatial attention selectively enhances visual processing voluntarily (endogenously) or involuntarily (exogenously) at a visual location in the absence of eye movements (Carrasco, 2011). Moreover, we often compensate for these

constraints by making rapid saccadic eye movements to actively explore the visual world and place relevant objects in the fovea where visual perception is most sensitive (Eckstein, 2017). Already before our eyes move (i.e., during saccade preparation), *presaccadic attention* shifts to the saccade target location and prioritizes visual processing (Deubel & Schneider, 1996; Kowler, Anderson, Dosher, & Blaser, 1995; Montagnini & Castet, 2007). It is well established that presaccadic attention boosts accuracy (e.g., Hanning, Deubel, & Szinte, 2019; Hoffman & Subramaniam, 1995) and reduces reaction times (e.g., Shepherd, Findlay, & Hockey, 1986), but there are relatively few studies on whether and how it modulates perception of basic visual dimensions. Presaccadic attention enhances contrast sensitivity (Hanning, Fernández, & Carrasco, 2023; Hanning, Himmelberg, & Carrasco, 2022b, 2022a; Li, Pan, & Carrasco, 2021) and spatial acuity (Kwak, Hanning, & Carrasco, 2023), sharpens orientation tuning and orientation acuity (Castet, Jeanjean, Montagnini, Laugier, & Masson, 2006; Li, Barbot, & Carrasco, 2016; Ohl, Kuper, & Rolfs, 2017), and shifts spatial frequency tuning, enhancing sensitivity for spatial frequencies higher than that of the stimulus (Li et al., 2016), even if detrimental to the task (Li, Pan, & Carrasco, 2019). The effect of presaccadic attention on visual sensitivity increases as saccade onset approaches (Hanning et al., 2019; Kroell & Rolfs, 2021; Li et al., 2016; Ohl et al., 2017; Rolfs & Carrasco, 2012). Such modulations suggest a functional role of presaccadic attention in rendering visual information at the peripheral saccade target more "fovea-like". Across every saccade, our visual system needs to seamlessly integrate two very dissimilar percepts: a blurry presaccadic input from the peripheral saccade target and a high-resolution post-saccadic input from the same location once the saccade target has been foveated. Presaccadic attention eases the integration of pre- and post-saccadic visual information, facilitating perceptual continuity (Herwig, 2015; Herwig & Schneider, 2014; Kroell & Rolfs, 2022; Li, Hanning, & Carrasco, 2021; Stewart, Valsecchi, & Schütz, 2020).

Contrast sensitivity is a fundamental visual dimension that constrains our vision. It drops markedly with eccentricity (Rovamo, Virsu, & Näsänen, 1978; Virsu & Rovamo, 1979) and exhibits pronounced polar angle asymmetries (Abrams, Nizam, & Carrasco, 2012; Baldwin, Meese, & Baker, 2012; Jigo, Tavdy, Himmelberg, & Carrasco, 2023; Rijsdijk, Kroon, & van der Wildt, 1980). Moreover, contrast sensitivity depends heavily on spatial frequency and is typically bandpass (**Figure 1b**). At the fovea, for example, it peaks at a spatial frequency range of 2 to 6cpd (cycles per degree of visual angle) and declines rapidly for lower and higher spatial frequencies (Campbell & Robson, 1968; Kelly, 1977). This general relation between contrast sensitivity and spatial frequency, referred to as the Contrast Sensitivity Function (CSF), defines our "window of visibility" (Ginsburg, 1978; Watson, Ahumada, & Farrell, 1986), and holds across eccentricities and around polar angle locations.

Given the limits in contrast sensitivity across eccentricity and around polar angle locations, and the prevalence of presaccadic attention in compensating for the constraints in our visual system, the purpose of this study was twofold.

(1) We investigated whether and how presaccadic attention bridges the gap in contrast sensitivity between foveal and peripheral locations around the visual field. Presaccadic attention increases contrast sensitivity across the contrast response function at a constant spatial frequency (Hanning et al., 2022b; Li, Pan,

et al., 2021; Zhao, Gersch, Schnitzer, Dosher, & Kowler, 2012). One study has assessed the accuracy benefit of presaccadic attention at a range of spatial frequencies at a constant contrast (Kroell & Rolfs, 2021). But how presaccadic attention modulates the CSF is unknown. For example, an increase in contrast sensitivity at a given spatial frequency may result from an upward shift of the CSF, a horizontal shift, increased bandwidth, or any of their combinations (**Figure 1b**).

(2) We assessed whether the effect of presaccadic attention on the CSF varies around polar angle locations. The effect of presaccadic attention around the visual field varies for different visual dimensions. During saccade preparation, polar angle asymmetries established during fixation are exacerbated for contrast sensitivity (Hanning et al., 2022b, 2022a) but are preserved for acuity (Kwak et al., 2023). Here, we examined presaccadic modulations of contrast sensitivity and acuity jointly by measuring the CSF around the visual field.

To investigate whether and how presaccadic attention shapes our window of visibility, we characterized the CSFs and compared the key CSF attributes **(Figure 1b)** during fixation and saccade preparation for the upper vertical, lower vertical, and horizontal meridian. We fit a Hierarchical Bayesian Model (HBM) that has been recently applied to analyze CSFs (Zhao, Lesmes, Dorr, & Lu, 2021; Zhao, Lesmes, Hou, & Lu, 2021). The HBM enables precise estimates of the peak contrast sensitivity (peak-CS), peak spatial frequency (peak-SF, the preferred spatial frequency, at the peak-CS), bandwidth (full width at half maximum), cutoff spatial frequency (cutoff-SF, the highest discernable spatial frequency), and area under the log CSF (AULCSF).

We found polar angle asymmetries in peak-CS, cutoff-SF, and AULCSF during fixation, consistent with recent studies (Hanning et al., 2022b; Jigo et al., 2023; Kwak et al., 2023). Importantly, presaccadic attention 1) shifted the CSF upward, increasing the peak-CS; 2) shifted the CSF rightward to higher spatial frequencies, increasing the peak-SF and cutoff-SF; 3) narrowed the CSF, decreasing the bandwidth; and 4) increased the AULCSF. These presaccadic modulations were present at all polar angle locations, but there was a larger

Figure 1. Background. **(a)** Polar angle asymmetries around the visual field. Visual performance is better along the horizontal than the vertical meridian, and along the lower than the upper vertical meridian. **(b)** Key attributes of the CSF. We derived peak-CS (peak contrast sensitivity), peak-SF (peak spatial frequency), bandwidth (full width at half maximum; half width shown for illustration purposes), cutoff-SF (cutoff spatial frequency), and AULCSF (area under the log CSF). Key CSF attributes were measured during fixation and saccade preparation to quantify presaccadic attention modulation on the CSFs.

presaccadic enhancement in the horizontal than the vertical meridian, specifically for the peak-CS as well as for contrast sensitivity across a wide range of spatial frequencies. These findings reveal that presaccadic attention increases our window of visibility, reducing the gap between visual representations at the peripheral saccade target and the future fovea, and more so along the horizontal meridian.

Methods

Participants

Twelve observers (4 males and 8 females, including authors YK and NH; ages 20–34) with normal or corrected-to-normal vision participated in the experiment. All participants (except for the two authors) were naïve to the experimental hypothesis and were paid $12 per hour. The experimental procedures were approved by the Institutional Review Board at New York University, and all participants (except for the two authors) provided informed consent. All procedures were in agreement with the Declaration of Helsinki.

Setup

Participants sat in a dark room with their head stabilized by a chin and forehead rest. All stimuli were generated and presented using MATLAB (MathWorks, Natick, MA, USA) and the Psychophysics Toolbox (Brainard, 1997; Pelli, 1997) on a gamma-linearized 20-inch ViewSonic G220fb CRT screen (Brea, CA, USA) at a viewing distance of 79 cm. The CRT screen had a resolution of 1,280 by 960 pixels and a refresh rate of 100 Hz. Gaze position was recorded using an EyeLink 1000 Desktop Mount eye tracker (SR Research, Osgoode, Ontario, Canada) at a sampling rate of 1 kHz. The Eyelink Toolbox was used for eyetracking with MATLAB and Psychophysics Toolbox (Cornelissen, Peters, & Palmer, 2002).

Experimental Procedure

Participants performed an orientation discrimination task for stimuli varying in contrast and spatial frequency, during *fixation* and *saccade preparation (presaccadic attention)* **(Figure 2)**. To place trials efficiently in the dynamic range of the CSF, we leveraged the qCSF (quick Contrast Sensitivity Function) method for data collection (Lesmes, Lu, Baek, & Albright, 2010). Given participants' performance in previous trials, this procedure selects stimulus contrast and spatial frequency to be tested on each trial, based on the maximum expected information gain, to further refine the CSF parameter estimates. The possible stimulus space was composed of 60 contrast levels from 0.001 to 1, and 12 spatial frequency levels from 0.5 to 16cpd, evenly spaced in log units.

We manipulated eye movement instruction (*fixation* and *saccade preparation,* from now on "instruction") between experimental blocks. **Figure 2a** shows the trial sequence under the saccade instruction. Each trial started with a fixation circle (0.175° radius) on a gray background (~26 cd/m^2) with a duration randomly jittered between 400ms and 600ms. Four placeholders indicated the locations of the upcoming stimuli, 6° left, right, above, and below fixation. Measurements at the left and right locations were combined for analysis, as it is well established that contrast sensitivity does not differ between these locations (e.g., Cameron, Tai, & Carrasco, 2002; Himmelberg, Winawer, & Carrasco, 2020). Each placeholder was composed of four corners (black lines, 0.2° length). The trial began once a 300-ms stable fixation (eye coordinates within a 1.75° radius virtual circle centered on fixation) was detected.

Figure 2. Experimental procedure. **(a)** Trial sequence. In saccade blocks (*presaccadic attention*), a central saccade cue indicated the saccade target after a fixation period. Participants were instructed to make a saccade precisely to the center of the corresponding placeholder as soon as the cue appeared. Just before saccade onset, a test Gabor stimulus was presented briefly at the cued location, and participants judged its orientation (CW or CCW) after response cue onset (i.e., after the saccade). The spatial frequency and the contrast of the Gabor on each trial was varied based on the qCSF (quick Contrast Sensitivity Function) procedure. The eye icons are for illustration only and were not shown during the experiment. In the fixation blocks (not illustrated here), the trial sequence was identical except that the cue pointed to all four locations, and participants were instructed to fixate at the center throughout the entire block. **(b)** Trial-by-trial data points for an example participant and location. Blue and red dots indicate trials with correct and incorrect responses respectively. The qCSF procedure efficiently samples stimuli in spatial frequency and contrast space based on responses on previous trials.

In blocks with the saccade instruction (*saccade preparation*), after the fixation period, a central cue (black line, 0.35° length) pointed to one of the four cardinal placeholders, indicating the saccade target. Participants were instructed to move their eyes to the center of the cued location as fast and precisely as possible. 140ms after cue onset (i.e., before saccade onset), a test Gabor grating (tilted ±45 relative to vertical, random phase, delimited by a raised cosine envelope with 2° radius) appeared for 30ms at the cued saccade target location. The spatial frequency and the contrast of the Gabor stimulus were determined by the qCSF procedure on each trial (Lesmes et al., 2010), based on the maximum expected information gain (reduction in entropy). 450ms after stimulus offset (and after saccade offset), the cued location was highlighted by increasing the width and length of the corresponding placeholders. Participants performed an un-speeded, orientation discrimination task for the Gabor grating at the cued location (by pressing left arrow key for -45°, right arrow key for +45°).

Stimulus parameters and timing for the blocks with the fixation instruction were identical to the saccade blocks with one exception: instead of one saccade target cue, four black direction cue lines pointed to all locations. Participants maintained fixation throughout the entire trial sequence.

Gaze position was monitored online to ensure fixation within a 1.75° radius virtual circle from the central fixation until the response phase (fixation blocks) or until cue onset (saccade blocks). Trials in which gaze deviated from fixation were aborted and repeated at the end of each block. In addition, in the saccade blocks, we repeated trials in which saccade latency was too short (< 150ms) or too long (> 350ms), or in which saccades landed outside of a 2.25° radius virtual circle around the saccade target center. Moreover, because we are interested in the presaccadic interval, we only included trials in which saccades were initiated after stimulus offset.

CSF analysis

Bayesian Inference

To characterize the CSFs during *fixation* and *saccade preparation* for each of the four locations, we used the Bayesian Inference Procedure (BIP, **Figure 3a**) and the Hierarchical Bayesian Model (HBM, **Figure 3b**) to fit the three-parameter CSF model to trial-by-trial data points (**Figure 2b**) (Zhao, Lesmes, Dorr, et al., 2021; Zhao, Lesmes, Hou, et al., 2021). For both the BIP and the HBM, Bayesian inference was used to estimate the posterior distribution of the three CSF parameters —peak contrast sensitivity (peak-CS), peak spatial frequency (peak-

Figure 3. CSF model fitting. **(a)** Schematic representation of the BIP (Bayesian Inference Procedure). The first stage of the data analysis consists of fitting trial-by-trial data points with the BIP to estimate the CSF parameters —peak contrast sensitivity (peak-CS), peak spatial frequency (peak-SF), and bandwidth. The BIP computes the posterior distribution of the parameters for each test independently. **(b)** Schematic representation of the HBM (Hierarchical Bayesian Model). In the second stage of the data analysis, the BIP outputs are used as the mean and covariance of the prior distributions of the CSF hyperparameters in the HBM. We used a three-level hierarchical model to incorporate potential relations in the CSF parameters across individuals and tests. For details on the BIP and the HBM, see section on **CSF analysis** and **Supplementary Materials**.

SF), and bandwidth. Other key attributes, such as the cutoff spatial frequency (cutoff-SF) and area under the log CSF (AULCSF), were computed from the final estimate of the CSF.

Contrast sensitivity S at spatial frequency sf is modeled as a log-parabola function with parameters $\theta = (peakCS, peakSF, bandwidth)$ (Lesmes et al., 2010; Watson & Ahumada, 2005):

$$log_{10}(S(sf,\theta)) = log_{10}(peakCS) - \frac{4}{log_{10}(2)}(\frac{log_{10}(sf)-log_{10}(peakSF)}{bandwidth})^2 . \quad Eq(1)$$

The probability of a correct response ($r = 1$) on a trial given the stimulus —spatial frequency sf and contrast c — is described as a psychometric function:

$$p(r = 1 | \theta, sf, c) = g + (1 - g - \lambda/2)(1 - \exp(-(cS(sf,\theta))^\beta)), \quad Eq(2)$$

where g is the guessing rate (g = 0.5), λ is the lapse rate (λ = 0.04; Wichmann & Hill, 2001; Zhao, Lesmes, Hou, et al., 2021), and β determines the slope of the psychometric function (β = 2). The probability of making an incorrect response ($r = 0$) is:

$$p(r = 0 | \theta, sf, c) = 1 - p(r = 1 | \theta, sf, c). \quad Eq(3)$$

Equations 2 and 3 define the likelihood function, or the probability of a correct/incorrect response in a trial given the stimulus and the CSF parameters. To infer the CSF parameters given the experimental data, Bayes' Rule is used to estimate the posterior distribution of the CSF parameters (θ) based on the likelihood and the prior (*Eq(7)*) in the BIP procedure. Details on modeling the prior distributions can be found in the **Supplementary Materials**.

HBM: Three-level hierarchy

We used a simple three-level HBM without considering any structure related to the experimental conditions, as reported in Zhao, Lesmes, Dorr, et al. (2021) (**Figure 3b**). In the current study, an individual refers to a combination of a participant, location (upper, lower, horizontal), and instruction (*fixation*, *saccade preparation*) condition (I=72). In addition, all trials that each participant completed were combined into one test (J=1).

The BIP fits these parameters independently for each individual and test (**Figure 3a**). Although the BIP has been proven to be a good estimate of the CSF, it may have overestimated the variance of each test because it scores each test independently with a uniform prior without considering potential relations of the parameters (Zhao, Lesmes, Dorr, et al., 2021). Therefore, we used a hierarchical model which recently has been shown to reduce the uncertainties of the parameter estimates when fitting the CSF (Zhao, Lesmes, Dorr, et al., 2021; Zhao, Lesmes, Hou, et al., 2021). The HBM considers potential relations of the CSF parameters and hyperparameters

within and across individuals **(Figure 3b).** More specifically, it quantifies the joint distribution of the CSF parameters and hyperparameters at three hierarchies in a single model: test- (J), individual- (I), and population-level. The within-individual and cross-individual regularities are modeled as the covariance of the CSF parameters at the individual level (φ) and covariance at the population level (Σ), respectively. Incorporating this knowledge into the model and decomposing the variability of the entire dataset into distributions at multiple hierarchies enabled us to reduce the variance of the test-level estimates and to obtain more precise estimates of the CSF parameters.

We fit the BIP and the HBM sequentially. As a first step, the BIP was fit to obtain the mean and standard deviation of each of the three CSF parameters across all participants and conditions, using a uniform prior distribution. Next, these values were fed into the HBM and set the mean and covariance of the prior distributions of the CSF hyperparameters (**Supplementary Materials** *Eq(S1)*).

At the population level of the HBM, the joint distribution of hyperparameter η was modeled as a mixture of three-dimensional Gaussian distributions N with mean μ and covariance Σ, which have distributions $p(\mu)$ and $p(\Sigma)$:

$$p(\eta) = N(\eta, \mu, \Sigma)\, p(\mu)p(\Sigma). \quad Eq(4)$$

At the individual level (I), the joint distribution of hyperparameter τ_i of individual i was modeled as a mixture of three-dimensional Gaussian distributions N with mean ρ_i and covariance φ, which have distributions $p(\rho_i|\eta)$ and $p(\varphi)$; where $p(\rho_i|\eta)$ denotes that the mean ρ_i was conditioned on the population-level hyperparameter η:

$$p(\tau_i|\eta) = N(\tau_i, \rho_i, \varphi)p(\rho_i|\eta)p(\varphi). \quad Eq(5)$$

At the test level (J), $p(\theta_{ij}|\tau_i)$, the joint distribution of parameter θ_{ij} of individual i and test j was conditioned on hyperparameter τ_i at the individual level.

The probability of obtaining the entire dataset was computed by probability multiplication:

$$p(r_{1:I,1:J,1:K}|X) = \prod_{i=1}^{I} \prod_{j=1}^{J} p(r_{ij,1:K}|\theta_{ij})\, p(\theta_{ij}|\tau_i)\, p(\tau_i|\eta)\, p(\eta)$$
$$= \prod_{i=1}^{I} \prod_{j=1}^{J} p(r_{ij,1:K}|\theta_{ij})\, p(\theta_{ij}|\tau_i)\, N(\tau_i, \rho_i, \varphi)\, p(\rho_i|\eta)\, p(\varphi)\, N(\eta, \mu, \Sigma)\, p(\mu)\, p(\Sigma), \quad Eq(6)$$

where $X = (\theta_{1:I,1:J}, \rho_{1:i}, \varphi, \mu, \Sigma)$ are all parameters and hyperparameters in the HBM, I is the total number of individuals, and J is the total number of tests on each individual.

HBM: Computing the joint posterior distribution

Bayes' rule ($posterior\ probability\ p(A|B) = \frac{likelihood\ p(B|A)\ \times\ prior\ probability\ p(A)}{marginal\ probability\ p(B)}$) was used to compute the joint posterior distribution of all the parameters and hyperparameters in the HBM:

$$p(X|r_{1:I,1:J,1:K}) = \frac{\prod_{i=1}^{I}\prod_{j=1}^{J} p(r_{ij,1:K}|\theta_{ij})\, p(\theta_{ij}|\tau_i)\, N(\tau_i,\rho_i,\varphi)\, p(\rho_i|\eta)\, p_0(\varphi)\, N(\eta,\mu,\Sigma)\, p_0(\mu)\, p_0(\Sigma)}{\int \prod_{i=1}^{I}\prod_{j=1}^{J} p(r_{ij,1:K}|\theta_{ij})\, p(\theta_{ij}|\tau_i)\, N(\tau_i,\rho_i,\varphi)\, p(\rho_i|\eta)\, p_0(\varphi)\, N(\eta,\mu,\Sigma)\, p_0(\mu)\, p_0(\Sigma)\, dX}, \quad Eq(7)$$

where the denominator is the probability of obtaining the entire dataset (*Eq(6)*).

We used the JAGS package (Plummer, 2003) in R (R Core Team, 2020) to evaluate the joint posterior distribution. JAGS generates representative samples of the joint posterior distribution of all the parameters and hyperparameters in the HBM via Markov Chain Monte Carlo (MCMC). We ran three parallel MCMC chains, each generating 2000 samples, resulting in a total of 6000 samples. Steps in the burn-in and adaptation phases — 20000 and 500000 steps respectively— were discarded and excluded from the analysis because the initial part of the random walk process is largely determined by random starting values.

Eye movement analysis

In addition to the gaze monitoring and detection of saccades online (see **Experimental Procedure**), we also performed an offline eye movement analysis using an established algorithm for saccade detection (Engbert & Mergenthaler, 2006). Saccades were detected based on their velocity distribution using a moving average over 20 subsequent eye position samples. Saccade onsets and offsets were detected based on when the velocity exceeded or fell below the median of the moving average by 3 standard deviations for at least 20ms. This offline analysis takes into account the entire distribution of eye position samples and velocity and allows for a more detailed evaluation of both fixation and saccadic eye movements. In total, we included 22,527 trials in the analysis —on average 1877 ± 55 (mean ± 1 SEM) trials per observer.

Statistical analysis

Convergence of the HBM parameters was determined based on the Gelman and Rubin's diagnostic rule (Gelman & Rubin, 1992). Each parameter and hyperparameter was considered to have "converged" when the variance of the samples across the MCMC chains divided by the variance of the samples within each chain was smaller than 1.05. In the current study, all parameters of the HBM converged.

To obtain final estimates of the CSF parameters in the HBM —peak-CS, peak-SF, and bandwidth—, parameter estimates of the 6000 samples were averaged for each participant and location-instruction

combination. The final CSFs for each participant and location-instruction combination were obtained by inputting the final parameter estimates to *Eq (1)*. From these final CSFs, cutoff-SF and AULCSF were computed. These key CSF attribute values were used for statistical testing.

All *p* values reported are based on permutation testing over 1000 iterations with shuffled data. *P* value is the proportion of a metric (*F* score or *t* score) in the permuted null distribution greater than or equal to the metric computed using intact data. Note that the minimum *p* value achievable with this procedure is 0.001. *P* values were FDR corrected for multiple comparisons, when applicable (Benjamini & Hochberg, 1995).

We also performed Bayesian statistics using the "BayesFactor" package in R (version 0.9.12–4.4). We report BF_{10} only for null results from permutation testing. The Bayes factors (BF_{10}) for main effects and interaction effects in the repeated measures ANOVA design were computed by comparing the full model (H1) against the restricted model (H0) in which the effect of interest was excluded from the full model (Rouder, Morey, Verhagen, Swagman, & Wagenmakers, 2017). BF_{10} smaller than 1 is in support for the absence of an effect; values 1–3, 3–10, 10–30, 30–100, and > 100 indicate anecdotal, moderate, strong, very strong, and extreme evidence for the presence of an effect (Kass & Raftery, 1995; Lee & Wagenmakers, 2014).

Results

Figure 4 shows the CSFs averaged across participants, during *fixation* and *saccade preparation* (presaccadic attention) for each location. To preview the results, *saccade preparation* shifted and reshaped the CSFs during *fixation* for all locations, increasing overall contrast sensitivity (**Figure 4a**). Second, during *fixation* (**Figure 4b**), contrast sensitivity was better in the horizontal than the vertical meridian, and in the lower vertical than the upper

Figure 4. Group average CSFs. **(a)** CSFs for the *fixation* and *saccade preparation* instruction, collapsed across locations. *Saccade preparation* modulates contrast sensitivity across spatial frequencies. **(b)** CSFs during *fixation* for each location, exhibiting polar angle asymmetries. **(c)** CSFs during *saccade preparation*, separately for each location. Polar angle asymmetries in the CSFs during *fixation* were also present during *saccade preparation*. **(a-c)** The CSF parameters were fitted with the HBM (Hierarchical Bayesian Model). Shaded regions denote ±1 standard error of the mean (SEM).

vertical meridian, consistent with HVA and VMA effects. Third, this pattern was overall maintained during *saccade preparation* (**Figure 4c)**, but the presaccadic benefit on contrast sensitivity was more pronounced at the horizontal than at the vertical meridian across a wide spatial frequency range.

We conducted a two-way repeated measures ANOVA for each of the key CSF attributes, with location (upper, lower, horizontal) and eye movement instruction (*fixation*, *saccade preparation*) as within-subject factors (**Figure 5**).

Peak-CS: peak contrast sensitivity

We observed main effects of location ($F(2,22) = 18.266$, $p < 0.001$, $\eta^2 = 0.624$) and instruction ($F(1,11) = 26.311$, $p < 0.001$, $\eta^2 = 0.705$), and an interaction effect ($F(2,22) = 18.266$, $p = 0.014$, $\eta^2 = 0.322$) on peak-CS (**Figures 5a, 6a**). As can be seen in **Figure 6a**, there were significant location effects during *fixation* ($F(2,22) = 9.356$, $p = 0.003$, $\eta^2 = 0.460$), as well as *saccade preparation* ($F(2,22) = 18.266$, $p < 0.001$, $\eta^2 = 0.704$). During *fixation*, peak-CS was significantly higher for the horizontal ($t(11) = 6.137$, $p < 0.001$, $d = 0.903$) and for the lower vertical meridian ($t(11) = 2.655$, $p = 0.025$, $d = 0.678$) than the upper vertical meridian. With *saccade* preparation, peak-CS was still higher for the horizontal ($t(11) = 8.486$, $p < 0.001$, $d = 2.118$) and the lower vertical ($t(11) = 3.797$, $p = 0.005$, $d = 1.089$) than the upper vertical meridian, similar to during *fixation*. In addition, peak-CS became higher for the horizontal than the lower vertical meridian ($t(11) = 3.096$, $p = 0.013$, $d = 1.034$), unlike during *fixation*.

Saccade preparation increased peak-CS compared to *fixation* for all locations (**Figure 6a**) — upper vertical ($t(11) = 3.159$, $p = 0.013$, $d = 0.711$), lower vertical ($t(11) = 4.534$, $p = 0.002$, $d = 0.844$), and horizontal ($t(11) = 5.824$, $p < 0.001$, $d = 1.245$) meridian, but the effect was larger for the horizontal meridian than the upper ($t(11) = 2.833$, $p = 0.049$, $d = 0.158$) and lower ($t(11) = 2.370$, $p = 0.056$, $d = 0.151$, $BF_{10} = 2.083$) vertical meridian. In summary, when compared to *fixation*, *saccade preparation* shifts the CSF upward and increases contrast sensitivity, for all locations, but more so for the horizontal meridian.

Peak-SF: spatial frequency leading to the peak-CS

There was a main effect of instruction ($F(1,11) = 16.355$, $p = 0.001$, $\eta^2 = 0.598$), but not a main effect of location ($F(2,22) = 1.756$, $p = 0.196$, $\eta^2 = 0.138$, $BF_{10} = 1.454$) on peak-SF (**Figure 5b**). The location-instruction interaction was marginally significant ($F(2,22) = 3.303$, $p = 0.057$, $\eta^2 = 0.231$, $BF_{10} = 0.335$), resulting from presaccadic enhancement (increased peak-SF during *saccade preparation* relative to *fixation*) surviving FDR correction only for the horizontal ($t = 3.082$, $p = 0.031$, $d = 0.728$) and the upper vertical ($t = 3.082$, $p = 0.031$, $d = 0.728$) meridian (**Figure 6b**). Taken together, (1) peak-SF during *fixation* did not differ across locations; (2) *saccade preparation* increased the peak-SF compared to *fixation*, resulting in a rightward shift of the CSF; (3) the effect of *saccade preparation* on peak-SF was present at all locations. These results show that during *saccade preparation*

contrast sensitivity is enhanced around the visual field particularly for spatial frequencies above the *fixation* peak-SF.

Figure 5. Main effects of location (averaged across *fixation* and *saccade preparation* instruction) and eye movement instruction (averaged across locations). **(a)** peak-CS; **(b)** peak-SF; **(c)** bandwidth; **(d)** cutoff-SF; **(e)** AULCSF. Errorbars indicate ±1 standard error of the mean (SEM), and vertical bars depict ±1 standard error of the difference (SED). Main effects of location and instruction are shown above the thick gray horizontal bars on the top. Significant post-hoc pairwise comparisons of location effects are denoted by asterisks above thin gray bars. ***p < 0.001, **p < 0.01, *p < 0.05, †*p* < 0.1, *n.s.* not significant; FDR corrected.

Bandwidth: full width at half maximum

There were main effects of location ($F(2,22)$ = 7.137, p < 0.001, η^2 = 0.396) and instruction ($F(1,11)$ = 10.258, p = 0.005, η^2 = 0.483, BF_{10} = 2.648), and no significant interaction ($F(2,22)$ = 0.289, p = 0.752, η^2 = 0.026, BF_{10} = 0.220) on bandwidth (**Figures 5c, 6c**). To further examine the main effect of location, bandwidth values were averaged across *fixation* and *saccade preparation* within each location for comparison across location pairs (**Figure 5c**). Only the difference between the lower vertical and the horizontal meridian survived FDR-correction: The bandwidth at the lower vertical meridian was narrower than at the horizontal meridian ($t(11)$ = 4.142, p = 0.005, d = 1.134). The main effect of instruction reflects the bandwidth narrowing with *saccade preparation* (**Figure 5c**), and the lack of location-instruction interaction indicates that this effect is similar around the visual field (**Figure 5c**).

Cutoff-SF: highest perceivable spatial frequency at which contrast sensitivity is 1.0

We observed main effects of location ($F(2,22) = 22.232$, $p < 0.001$, $\eta^2 = 0.669$) and instruction ($F(1,11) = 18.250$, $p = 0.002$, $\eta^2 = 0.624$), and no significant location-instruction interaction ($F(2,22) = 2.285$, $p = 0.125$, $\eta^2 = 0.172$, $BF_{10} = 0.860$) on cutoff-SF (**Figures 5d, 6d**). To follow up the location effect, we conducted post-hoc comparisons for location pairs on cutoff-SF values averaged across *fixation* and *saccade preparation* for each location (**Figure 5d**). The cutoff-SF at the horizontal meridian was significantly higher than that at the upper ($t(11) = 7.787$, $p < 0.001$, $d = 1.324$) and the lower vertical meridian ($t(11) = 4.181$, $p = 0.002$, $d = 0.902$). The main effect of instruction was caused by *saccade preparation* increasing the cutoff-SF (**Figure 5d**). This presaccadic enhancement on cutoff-SF was similar around the visual field (**Figure 6d**). These results, together with the increase in peak-SF, indicate that *saccade preparation* shifts the CSF rightward and enhances contrast sensitivity more for spatial frequencies higher than peak-SF during *fixation*.

Figure 6. Group average key CSF attributes for each location and eye movement instruction. **(a)** peak-CS; **(b)** peak-SF; **(c)** bandwidth; **(d)** cutoff-SF; **(e)** AULCSF. Errorbars indicate ±1 standard error of the mean (SEM), and vertical bars depict ±1 standard error of the difference (SED). Location-instruction interaction effects are shown at the top of each figure with dark gray horizontal bars. Significant post-hoc pairwise comparisons of location and instruction effects are denoted by asterisks above black crosses and horizontal lines, respectively. ***$p < 0.001$, **$p < 0.01$, *$p < 0.05$, †$p < 0.1$, *n.s.* not significant, FDR corrected.

AULCSF: area under the log CSF

We observed main effects of location ($F(2,22) = 21.626$, $p < 0.001$, $\eta^2 = 0.663$) and instruction ($F(1,11) = 26.642$, $p < 0.001$, $\eta^2 = 0.708$) on AULCSF (**Figure 5e**). The location-instruction interaction was marginally significant ($F(2,22) = 3.109$, $p = 0.070$, $\eta^2 = 0.220$, $BF_{10} = 0.207$), from presaccadic enhancements in AULCSF surviving FDR correction only at the horizontal ($t = 4.365$, $p = 0.003$, $d = 0.961$) and the upper vertical ($t = 2.602$, $p = 0.040$, $d = 0.500$) meridian (**Figure 6e**). Post-hoc analyses of location effects were conducted on AULCSF values averaged across *fixation* and *saccade preparation* for each location (**Figure 5e**): AULCSF was significantly larger for the horizontal than the upper ($t(11) = 8.725$, $p < 0.001$, $d = 1.486$) and lower ($t(11) = 3.900$, $p = 0.003$, $d = 0.957$) vertical meridian. Thus, *saccade preparation* increases AULCSF at all locations, widening the window of visibility and rendering more of the world perceivable at the saccade target around the visual field.

Presaccadic benefit on contrast sensitivity across spatial frequencies

Saccade preparation improved performance across a wide range of spatial frequencies. There were main effects of location ($F(2,22) = 7.162$, $p = 0.003$ $\eta^2 = 0.394$) and spatial frequency ($F(50,550) = 9.957$, $p < 0.001$, $\eta^2 = 0.143$), and a significant interaction effect ($F(100,1100) = 1.841$, $p < 0.001$, $\eta^2 = 0.672$) on the magnitude of the presaccadic benefit. To better understand the interaction effect, we conducted a one-way repeated measures ANOVA with location as a factor for each spatial frequency and observed a significant location effect in a wide

Figure 7. Presaccadic benefit, quantified as the ratio of contrast sensitivity during *saccade preparation* and *fixation*. Group average presaccadic benefit on the CSF, separately for each location. The yellow and blue horizontal bars at the top mark the spatial frequencies at which horizontal enhancement was larger than at the upper and lower vertical meridian, respectively. The vertical dashed arrows denote group peak-SF during *fixation* separately for each location. The vertical solid arrows indicate the spatial frequency resulting in the peak of the presaccadic benefit for each location. Note that the vertical solid lines do not necessarily correspond to the spatial frequency resulting in the maximum value of the group averaged curve shown in the figure. Shaded regions represent $\pm$1 standard error of the mean (SEM).

spatial frequency range (**Figure 7**, between 0.616 and 11.314cpd, $p < 0.05$). The presaccadic benefit at the horizontal meridian was greater than at the upper vertical meridian (between 0.536 and 12.126cpd, $p < 0.05$) and the lower vertical meridian (between 0.758 and 11.314cpd, $p < 0.05$). The presaccadic benefit did not differ between the upper and lower vertical meridian for any of the spatial frequencies tested. Moreover, there was a maximum benefit of *saccade preparation* (relative to *fixation*) on contrast sensitivity for spatial frequencies higher than the *fixation* peak-SF (**Figure 7**), which is consistent with presaccadic attention shifting the peak-SF to higher spatial frequencies (**Figures 5b, 6b**).

Eye movement parameters

We evaluated eye movement parameters as a function of saccade direction, to determine whether these parameters influence presaccadic attention effects at different locations (**Figure 8**). A one-way repeated measures ANOVA yielded a main effect of saccade direction on latency, i.e., saccade onset relative to cue onset ($F(1,11) = 22.459$, $p < 0.001$, $\eta^2 = 0.672$). Downward saccades were the slowest (mean = 228.015ms; **Figure 8a**), followed by horizontal (mean = 217.178ms) than upward (mean = 209.159ms) saccades (upward-downward: $t(11) = 5.902$, $p < 0.001$, $d = 0.909$; horizontal-downward: $t(11) = 3.709$, $p = 0.002$, $d = 0.490$; upward-horizontal $t(11) = 3.524$, $p = 0.006$, $d = 0.419$). There was neither a main effect of saccade direction on saccade amplitude (**Figure 8b**; $BF_{10} = 1.126$) nor on precision — mean of the Euclidean distance between saccade endpoints and saccade target center (**Figure 8c**; $BF_{10} = 0.458$). Note that a minor difference in saccade latencies around the visual field has been reported previously (Honda & Findlay, 1992; Kwak et al., 2023; Schlykowa, Hoffmann, Bremmer, Thiele, & Ehrenstein, 1996; Tzelepi, Laskaris, Amditis, & Kapoula, 2010).

Figure 8. Group average saccade parameters as a function of saccade direction. **(a)** Saccade latencies (ms); **(b)** Saccade amplitudes (°). Shaded error areas indicate ±1 standard error of the mean (SEM). **(c)** Normalized saccade endpoint frequency maps averaged across participants as a function of saccade direction. Dashed gray circles indicate the 2.25° radius saccade target region. The central black circle indicates the fixation location (not on scale).

Discussion

The current study reveals that presaccadic attention enhances and reshapes the CSF and the magnitude of these effects varies around the visual field. We compared key attributes of the contrast sensitivity function (CSF), estimated through Hierarchical Bayesian Modeling (HBM), during fixation and saccade preparation for different polar angle locations. Deployment of presaccadic attention increased the peak contrast sensitivity (peak-CS), shifted the peak (peak-SF) and cutoff spatial frequency (cutoff-SF) to higher spatial frequencies, and sharpened the bandwidth (**Figure 9**). These presaccadic modulations resulted in a larger area under the log CSF (AULCSF) compared to fixation, indicating that during saccade preparation we can discriminate orientation with lower contrast at the saccade target. The presaccadic benefits of for these key attributes were present at all tested locations. Moreover, the increase in contrast sensitivity across a wide range of spatial frequencies, including the peak-CS, was more pronounced at the horizontal than the vertical meridian. Thus, during saccade preparation, the polar angle asymmetries in contrast sensitivity — specifically, the HVA (Horizontal-Vertical Anisotropy) — was exacerbated.

Figure 9. Summary schematic. **(a)** Key CSF attributes during fixation and saccade preparation. Presaccadic attention modulates peak contrast sensitivity (peak-CS), peak spatial frequency (peak-SF), cutoff spatial frequency (cutoff-SF), and bandwidth, which result in widening the window of visibility at the saccade target. Purple arrows demonstrate the direction of change. **(b)** Presaccadic benefit on contrast sensitivity across spatial frequencies. The benefit peaks at a spatial frequency (vertical solid arrow) higher than peak-SF during *fixation* (vertical dashed arrow). Shaded regions represent ±1 standard error of the mean (SEM).

The present results indicate that presaccadic attention renders the peripheral representation at the saccade target more fovea-like, in anticipation of the corresponding post-saccadic (foveal) input. Increases in peak-CS, peak-SF, and cutoff-SF during saccade preparation resemble the way the CSFs change from peripheral to foveal locations. Previous studies have shown that peak-CS and peak-SF gradually increase from the periphery to the fovea (Hilz & Cavonius, 1974; Jigo & Carrasco, 2020; Rovamo & Virsu, 1979; Rovamo et

al., 1978). Moreover, cutoff-SF (i.e., acuity or spatial resolution) is directly proportional to the cortical magnification factor, indicating that cutoff-SF increases from peripheral to foveal locations (Cowey & Rolls, 1974; Rovamo & Virsu, 1979; Rovamo et al., 1978; Virsu & Rovamo, 1979). Thus, our findings illustrate that presaccadic attention helps to bridge the perceptual gap between current peripheral and future foveal representations, which may facilitate a smooth transition in retinal images across saccadic eye movements (Herwig, 2015; Herwig & Schneider, 2014; Kroell & Rolfs, 2022; Li, Hanning, & Carrasco, 2021; Stewart, Valsecchi, & Schütz, 2020).

In fact, there is neurophysiological evidence that around the time of saccades, receptive fields of neurons shrink and shift toward the saccade target location (Neupane, Guitton, & Pack, 2016; Tolias et al., 2001). Moreover, neuronal receptive fields predictively shift to their post-saccadic retinal positions (Duhamel, Colby, & Goldberg, 1992; Neupane et al., 2016; Umeno & Goldberg, 1997). According to these accounts, the peripheral test stimulus in our study would have been processed by neurons more selective for foveal locations during saccade preparation. During fixation, however, the same stimulus would have been processed only by neurons tuned to the periphery. This receptive field shift during saccade preparation might underlie the behavioral effects observed in the present study — higher peak-CS, peak-SF, and cutoff-SF. This mechanism may also explain the decrease in bandwidth during saccade preparation. Contrast sensitivity peaks between 2 and 6cpd in the fovea (Campbell & Robson, 1968). If during saccade preparation the saccade target is represented by foveal neurons tuned to these spatial frequencies instead of peripheral neurons tuned to lower spatial frequencies (Rovamo et al., 1978), the benefit would peak between 2 to 6cpd and decrease at other ranges, resulting in a narrower bandwidth.

In this study, we have *jointly* examined key attributes of the CSF in a systematic manner, across the whole contrast range, a wide range of spatial frequencies, and critically at different polar angle locations. The current findings conceptually correspond to presaccadic attention effects on *individual* attributes of the CSF tested *separately* in various visual tasks and dimensions. Presaccadic attention enhances contrast sensitivity at the saccade target when measured at a fixed spatial frequency (Hanning et al., 2022b; Li, Pan, et al., 2021). It also enhances sensitivity to spatial frequencies higher than the stimulus spatial frequency (Li et al., 2016, 2019), but this was tested only for a narrow frequency range (e.g., 1-2cpd at 10° eccentricity) at the horizontal meridian. These results are in line with the rightward shift of peak-SF and cutoff-SF reported in the present study. Moreover, the increased cutoff-SF (i.e., the highest spatial frequency one can perceive at 100% contrast) is consistent with presaccadic attention enhancing visual acuity (Kwak et al., 2023). Lastly, for a constant contrast level, saccade preparation benefits orientation discrimination at horizontal saccade targets primarily at mid spatial frequencies, and this benefit becomes more pronounced as saccade onset approaches (Kroell & Rolfs, 2021). Here, measuring the CSF, we show that presaccadic benefit on contrast sensitivity peaks at spatial frequencies higher than the peak-SF during fixation around the visual field.

Deploying covert attention without concurrent eye movements also modulates the CSF (Jigo & Carrasco, 2020). Endogenous attention, a voluntary and flexible mechanism, enhances contrast sensitivity across a broad

range of spatial frequencies. Exogenous attention, an involuntary and inflexible mechanism, enhances contrast sensitivity primarily for spatial frequencies higher than the peak-SF at each eccentricity. The presaccadic attention benefits in the current study are reminiscent of both types of covert attention. As for endogenous attention, contrast sensitivity benefits are present across a wide range of spatial frequencies; at the peak spatial frequency during fixation, as well as below and above it. As for exogenous attention, contrast sensitivity benefits are more pronounced for higher spatial frequency ranges during saccade preparation, with peak-SF and cutoff-SF shifting to higher frequencies.

This study reveals that the benefit of presaccadic attention on the CSF changes as a function of polar angle. During fixation, there were robust HVA and VMA effects in peak-CS, cutoff-SF, and AULCSF, but not in peak-SF, in line with previous reports (Barbot, Xue, & Carrasco, 2021; Jigo et al., 2023). With covert spatial attention (Cameron et al., 2002; Purokayastha, Roberts, & Carrasco, 2021; Roberts, Cymerman, Smith, Kiorpes, & Carrasco, 2016) and temporal attention (Fernández, Denison, & Carrasco, 2019), polar angle asymmetries are preserved. During saccade preparation, the extent of the asymmetries for some of the CSF parameters was preserved; but for peak-CS as well as for a wide spatial frequency range, contrast sensitivity benefited more from saccade preparation at the horizontal than the vertical meridian, resulting in an even more pronounced HVA. Recent studies examining the interaction between presaccadic attention and polar angle asymmetries have yielded different results for contrast sensitivity and acuity. Specifically, presaccadic attention intensified location differences in contrast sensitivity, due to a lack of or a smaller benefit preceding upward saccades (Hanning et al., 2022a; Hanning, Himmelberg, & Carrasco, 2023). However, presaccadic attention enhanced acuity (spatial resolution) similarly around the visual field, thus preserving the polar angle asymmetries in acuity (Kwak et al., 2023). The results of the current study also reveal a dissociation between location-instruction interactions in cutoff-SF and peak-CS, which relate to acuity and contrast sensitivity measurements respectively: Asymmetries in cutoff-SF remained, whereas those in peak-CS as well as contrast sensitivity at a wide spatial frequency range were exacerbated with presaccadic attention, expanding contrast sensitivity more across the horizontal than the vertical meridian. Hence, the interaction between presaccadic benefits and polar angle asymmetries may depend on the visual dimension. Importantly, what is consistent across presaccadic attention effects for both contrast sensitivity and acuity is that polar angle asymmetries cannot be alleviated even with the deployment of presaccadic attention: They are either intensified (Hanning et al., 2022b, 2022a) or preserved (Kwak et al., 2023).

The findings that both the CSF and the benefit of presaccadic attention vary as a function of polar angle call into question the generalizability of behavioral and neurophysiological measurements obtained along the horizontal meridian, the most frequently assessed to characterize the effects of target eccentricity as well as saccadic eye movements. Future studies should test whether oculomotor feedback signals (between eye movement and visual areas), which are thought to underlie presaccadic modulations of visual perception, differ between horizontal and vertical saccades, and whether other perceptual correlates of presaccadic attention —

such as the sensitivity shift to higher spatial frequencies (Kroell & Rolfs, 2021; Li et al., 2016, 2019) or orientation tuning (Li et al., 2016; Ohl et al., 2017)— are more pronounced for horizontal than vertical saccades.

In conclusion, the benefits of presaccadic attention on the CSF can facilitate the integration of pre- and post-saccadic visual representations around the visual field. This study compares the effects of fixation and saccade preparation on a wide range of contrast and spatial frequency. The results reveal that presaccadic attention enhances the portion of the world that becomes visible at the saccade target, anticipating foveal vision. Moreover, the degree of such enhancement varies with polar angle, thereby reshaping the window of visibility.

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Supplementary Materials

Modeling prior distributions for HBM

For fitting the HBM, we start with the prior distributions of μ (population mean), Σ^{-1} (inverse of population level covariance matrix), and φ^{-1} (inverse of individual level covariance matrix), which are $p_0(\mu)$, $p_0(\Sigma^{-1})$, and $p_0(\varphi^{-1})$ respectively.

For each of the CSF parameter, the prior distribution of μ is a truncated normal distribution: $N(\text{mean}, \text{standard deviation})\text{T}(\text{lower bound}, \text{upper bound})$. The mean and standard deviation of the truncated normal distribution is set to the average of the mean ($\mu_{peakCS,0}$, $\mu_{peakSF,0}$, $\mu_{bandwidth,0}$) and standard deviation ($\sigma_{peakCS,0}$, $\sigma_{peakSF,0}$, $\sigma_{bandwidth,0}$) of the corresponding parameters obtained from the BIP across individuals (I=72; combination of a participant, location, and instruction):

$p_0(\mu_{peakCS}) = N(\mu_{peakCS,0}, \sigma_{peakCS,0})\text{T}(\log_{10}(1.05), \log_{10}(1050))$. *Eq(S1a)*

$p_0(\mu_{peakSF}) = N(\mu_{peakSF,0}, \sigma_{peakSF,0})\text{T}(\log_{10}(0.1), \log_{10}(5))$. *Eq(S1b)*

$p_0(\mu_{bandwidth}) = N(\mu_{bandwidth,0}, \sigma_{bandwidth,0})\text{T}(\log_{10}(1), \log_{10}(9))$. *Eq(S1c)*

The prior distributions of the precision matrices (the inverse of covariance matrices Σ^{-1} and φ^{-1}) are modeled as Wishart distributions. $W(Y, v)$ denotes a Wishart distribution with expected precision matrix Y and degrees of freedom v ($v = 4$). Σ_{BIP} and φ_{BIP} are population-level and individual-level covariance matrices obtained from the BIP:

$p_0(\Sigma^{-1}) = W\left(\frac{\Sigma_{BIP}^{-1}}{v}, v\right)$. *Eq(S2)*

$p_0(\varphi^{-1}) = W\left(\frac{\varphi_{BIP}^{-1}}{v}, v\right)$. *Eq(S3)*