High-fidelity, generalizable light-field reconstruction of biological dynamics with physics-informed meta neural representation

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Abstract:

Light field microscopy (LFM) offers rapid volumetric imaging of dynamic biological processes via 2D light field snapshots. However, LFM's 2D-to-3D inversion with limited spatial-angular tomography leads to artifacts and poor axial resolution. Here, we introduce light-field meta neural representation (LFMNR), a new LFM reconstruction paradigm based on physics-informed implicit neural representation and meta learning, to address these issues for LFM. Leveraging INR's continuity, LFMNR achieves self-supervised, artifact-free 3D reconstruction with enhanced structural fidelity (~2.2-fold improvement), spatial resolution (~4.4-fold enhancement) and data compression (~10-fold), when compared to classical model-based light-field deconvolution. In addition, our meta-learning and progressive sampling strategies also mitigate INR's intrinsic limitations in weak generalization and low representation speed scene by scene, thereby resulting in rapid representation (~100-fold acceleration) of hundreds of consecutive volumes capturing sustained biological dynamics in three dimensions. LFMNR demonstrates superior performance across diverse biological samples without any prior spatial structure knowledge. We showcase LFMNR's

40 capability in observing cell apoptosis in several hours and capturing instantaneous
41 organelle interactions at millisecond timescale. LFMNR approach readily delivers
42 high-fidelity, high-speed 3D imaging with vast potential applications in biological
43 research and provides a paradigm shift with extensive value for computational imaging
44 reconstruction.
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Introduction
Understanding the spatial dynamics and interactions within microenvironments
necessitates high spatiotemporal resolution across three dimensions. This imperative
drives the advancement of volumetric imaging technologies to probe rapid biological
processes, such as cardiac hemodynamics[1, 2] and intracellular interactions[3-5]. While
scanning-based microscopy compromises volumetric imaging speed and can induce
additional phototoxicity due to its sequential scanning approach, light field microscopy[6]
(LFM) enables one-shot volumetric imaging by capturing all fluorescence signals from
an excited volume in a single 2D image through multi-view captures. Though LFM is
ideal for imaging dynamic biological processes[7], the non-uniform spatial resolution
resulting from frequency aliasing limits its broader application. Fourier light field
microscopy[8-10] employs a microlens array at the Fourier plane to mitigate spatial
sampling aliasing in standard LFM and better leverage the optical aperture, thereby
achieving improved spatial resolution with fewer views. Since these methods
commonly employ Richard-Lucy (RL) deconvolution for iterative 3D volume
reconstruction using the point spread function, challenges arise under the lower angular
sampling rate and limited angle-range of FLFM. This alternate projection algorithm,
applied in a tomography reconstruction manner, may introduce artifacts and impact
structure fidelity, especially when the signals are dense[11, 12].
To address limitations in multi-view 3D reconstruction, data-driven algorithms are
proposed, leveraging deep learning models to convert 2D LF captures into high-
resolution 3D stacks with improved reconstruction quality[13-17]. However, end-to-end
supervised approaches require large-scale volumetric data and well-aligned "2D-3D"
training pairs, which are not readily accessible and prone to introducing artifacts due to
mismatch between training and experimental data[18]. Self-supervised learning-based
algorithms, which do not require volumetric data, offer a promising alternative for
advanced light-field reconstruction. Current self-supervised methods in microscopy
tasks often integrate physical priors into models through well-designed loss functions
derived from analytical models to ensure physical consistency[19-21]. However, building
self-supervised models for 3D reconstruction encounters challenges primarily due to
the dimensionality reduction, which adds complexity to finding viable solutions within
physical consistency constraints. This complexity often leads to significant artifacts,
hallucinations, and discontinuities in the reconstructed output (Supplementary Figure
1, Supplementary Note 1).
Recently, Neural Radiance Field[22] (NeRF) has been known for its ability to
generate novel views with geometry consistency, and applied in various vision tasks[23-
26]. NeRF employs an MLP (Multi-Layer Perceptron) to represent 3D scenes from 2D
multi-view input, known as implicit neural representation (INR), capturing the latent

continuous function of signal distribution. While NeRF's volumetric representation correlates with the 3D reconstruction inverse problem in FLFM, differences in forward models between macrophotography and diffraction theory in microscopy imaging pose big challenges for realization of INR-based light-field reconstruction. Moreover, NeRF's grid-based training strategy is highly computationally intensive, limiting its further application in processing dynamic data.

Here, we introduce a physically informed, meta-learning based self-supervised approach, termed light-field meta neural representation (LFMNR), for efficient light-field 3D reconstruction with high fidelity. By integrating light field forward model into implicit neural representation for the first time, light-field INR (LFINR) achieves 3D reconstruction through self-supervised learning from 2D views. Leveraging the continuity of the INR function and the geometry consistency of synthesized views, LFINR effectively reduces artifacts and axial elongation even with extremely-limited views input of just 3, far surpassing classical model based deconvolution approaches. In addition, we employ a progressive sampling strategy with structural error maps to significantly reduce computational time compared to conventional INR methods. Furthermore, based on the intrinsic continuity of dynamic LF time-sequences, we utilize meta-learning to transfer optimized weights to adjacent time points, achieving accelerated (~100-fold faster) light-field meta neural representation (LFMNR) for high-throughput reconstruction of sustained light-field videos. Several experiments have validated LFMNR's minimized artifacts and improved reconstruction fidelity across diverse biological samples. It achieves approximately 2.2-fold improvement in structural fidelity and a 4.4-fold enhancement in resolution compared to conventional LFM deconvolution. Long-term cell apoptosis and several intracellular dynamic events such as mitochondrial fission and mitochondria-lysosome interaction cell apoptosis, have been identified and quantitatively analyzed to demonstrate the capability of LFMNR.

Results
The principle of LFINR
The framework of LFINR includes 3 steps: spatial coordinates sampling, scene-representation network constructing, and physics-model consistency evaluation, as illustrated in Fig. 1. Unlike conventional convolution neural networks (CNN) in image enhancement or reconstruction, LFINR requires spatial coordinates $\{x_i, y_i, z_i\}_{i=1}^{N}$ as network input, which means a 3D spatial grid covering the reconstructed signals needed to be defined before network inference ("*Objective space*" in Fig. 1a). However, due to the discrete grid form of image data, the quantity of spatial coordinates will increase multiplicatively with the enlargement of image size, which burden the computation cost and reduce network convergence speed. Here, we introduced a progressive sampling strategy, which first used down-sampled mesh grid to pre-train network and next fed all grids for details fitting, to make network fast convergence. Initially, a sparse-sampled mesh grid was employed to pre-train the network, providing a preliminary approximation of the overall distribution ("*i. Sparse sampling*" in Fig. 1b). Subsequently, during the fine-tuning phase, the full-size grids were firstly fed into the

network for details recovery ("*ii. Full sampling*" in Fig. 1b). Then, during the later stages of training, a focal sampling approach was implemented to prioritize the training on regions exhibiting higher distortion, in which, we leveraged local structural similarity to compute the error map ("*iii. Focal sampling*" in Fig. 1b, Methods). With this spatially aware optimization strategy, LFINR could achieve ~2-fold acceleration and outperform in weak-signal reconstruction compared with random-sampling based approach[22] (Supplementary Figure 3).

After coordinates sampling, a fully-connected network ("MLP network" in Fig. 1b) was constructed to serve as the underlying continuous volumetric scene function. By querying the 3D spatial coordinates, the network could recover the volumetric intensity information.

Finally, the produced volume was utilized to generate projections with forward rendering model for physical consistency evaluation. However, during this process, the difference between forward rendering model and real-world model degraded the 3D reconstruction. For example, the photography model utilized in conventional NeRF[22] relies on ray-casting model to form the volumetric density and color of opaque 3D scene. While FLFM imaging model is based on wave-optics theory and aims to accurately describe the intensity distribution of semi-/transparent sample. The ignoration of diffraction effect in wave-optics model will blur the represented 3D volume with increased errors (Supplementary Figure 4).

Taking this into account, we developed a hybrid physics model following the principle of wave-optics model and tomographic projection geometry to obtain dual-channel forward projections in rendering process and compute the hybrid loss function for evaluating physics consistency (Fig1b, Methods). For the wave-optics rendering branch, the FLFM Point Spread Function (PSF) was employed to convolve with the predicted volume to generate wave-optics rendering results, which simulated the light-field propagation determined by the hardware settings ("*Light-field propagation*", Fig. 1a). For the geometry rendering branch, we derived the projection matrix through parallax extraction and obtained the geometry rendering results (Methods). During the model optimization phase, we adopted weighted hybrid function based on the dual rendering results. The first term of loss function was pixel-wise errors (L_2 loss) between the extracted views and wave-optics rendering results. The second one was structure discrepancy to capture the skeleton information of input views. Before this loss computation, we employed a self-supervised view-enhancement network, termed as VE module in Fig. 1b, to remove the depth-correlated blur in extracted LF views, which matched the geometry rendering model (Supplementary Note 2). Then, the structure discrepancy could be derived from Structure Similarity Index Measurement (SSIM) between enhanced views and geometry rendering results. By continuously minimizing the hybrid loss, LFINR gradually learned to produce the 3D volume only with input coordinates, in a form of scene representation. Our hybrid physics projection model, compared to utilizing only one rendering strategy, exhibited accelerated network convergence, and maintained high structural fidelity (Supplementary Figure 5). Further details about the network implementations can be found in the Methods section.

Fig1. The overview of LFINR framework. a, The schematic diagram of the Fourier light-field microscopy. **b.** Workflow of LFINR, which contains 3 steps: Sampling coordinates from 3D spatial grid with progressive strategy; Constructing MLP (Multi-Layer Perceptron) based scene-representation network; Computing the hybrid physics model consistency. With constant network optimization in a self-supervised manner, LFINR could learn to represent the 3D scene within the MLP, referred to implicit neural representation. During the optimization process, progressive sampling strategy was adopted to accelerate network convergence under the guidance of structural error map. The hybrid physics model contains wave-optics model for evaluating pixel errors between the extracted views and wave-optics rendering results, and tomographic projection geometry for evaluating structure discrepancy between geometry rendering results and enhanced views obtained by VE (view-enhancement) module.

LFINR enables high-fidelity 3D reconstruction by its continuous representation.

For the inverse problem of 3D reconstruction from encoded multi-view light-field images, the quality of reconstructed results is highly depended on the performance of decoded algorithm. The 3D supervised DL algorithms[13, 15, 17] solve such problem in an unexplainable way by building CNN network mapping from 2D capture to 3D volume, which suffers the generalization errors due to the data bias[18]. The classical model based method, such as RL-deconvolution[8], is still the most widely-used approach especially when the volumetric data guidance is not available. However, the inherent constraints within inverse problems, characterized by limited angle range and sparse sampling of captured views[11], often lead to poor reconstruction quality, particularly evident along the axial dimension and for densely packed signals.

We compare the reconstruction between FLFM deconvolution and our LFINR on different biological samples as shown in Fig 2. In Fig. 2a, LFINR preserved obviously more structure details and higher contrast compared with deconvolution approach when decoding the 3D microtubule signals in an *U2OS* cells (labeled with 3mEmerald-Ensconsin) from 7 simulated FLFM views (Methods). The deconvolution approach exhibited noticeable blurs in lateral/axial projection and significant view-related stripe artifacts, which have been validated by the frequency analysis and high structure errors. Such deficiencies came from the depth-wise blurry modulation and signal cross-talk in Fourier light-field imaging process. For suppressing the blur effect, we first used the self-supervised VE network to remove the resolution degradation in FLFM views (Methods). The blur occurred in traditional deconvolution results decreased remarkably but the stripe artifacts still existed, as shown in "*View-enhanced Deconv.*", Fig 2b. In sharp contrast, LFINR produced artifacts-free 3D reconstruction with higher SSIM of ~0.96 and lower NRMSE (Normalize Root Mean Square Error) of ~0.058, and recovered much more high-frequency details validated through the spectrum analysis (insets in Fig. 2b). These notable enhancements in quality stemmed from the intrinsic continuity of implicit representation and physics-based hybrid rendering model in LFINR (Supplementary Figure 6).

In addition to the improvements in structural fidelity and spatial resolution, LFINR, with its ability for arbitrary view synthesis facilitated by the continuity of representation, also demonstrate significant superiority in 3D reconstruction of ER (labeled with EGFP-Sec61β) with extremely low number of light-field views, such as just 3, achieving ~2.3-fold higher SSIM, ~1.3-fold improvement in xy planes and ~1.76-fold improvement in xz planes (Fig. 2c, Supplementary Figure 7). The deconvolution-based results exhibited severe striped artifacts in axial plane (white arrowheads), when only 3 views were used. Such undesirable hallucinations across different depth further deteriorated the lateral structural fidelity denoted by the lower SSIM (Fig. 2c, d). Besides the evaluation in space domain, we also conducted geometry consistency comparison among different results (Fig 2e, Method, Supplementary Figure 8). The EPIs (epi-polar plane images)[27] used here described the distribution of both angle and space, and the slopes of lines in EPIs denoted the parallax across different views. When angular sampling was reduced, deconvolution-based methods exhibited artificial stripes in EPIs. In contrast, LFINR's outputs maintained a seamless transition across various views, as evidenced by the consistent alignment of signals and a higher SSIM of 0.908. This indicates LFINR's capability to generate arbitrary views with strong geometric consistency, even when operating under constraints of limited supervision

We noted that, with the image quality enhancement, LFINR also achieves higher accuracy in downstream analysis (Fig. 2f, g). The segmentation results of cardiomyocyte nuclei (labeled with *Tg(myl7:nls-gfp)*) showed higher intersection over union (IOU) scores of LFINR, while deconvolution ones showed obvious errors in the boundary of single cell (red area in "*Deconv*" results, Fig. 2g). Additionally, with the alternative projection process in RL-deconvolution, structural errors tended to gradually accumulate, as evidenced by the over-refined details. (Supplementary Figure 9).

Fig.2 Light-field reconstruction with improve quality by LFINR. a, The depth-encoded
projections of microtubules by LFINR reconstruction, FLFM deconvolution and ground truth (GT).
The number of FLFM views used was 7. Scale bar: 50 μm. **b,** magnified horizontal and vertical
sectional views of white rectangular boxes marked in **a**, denoting the higher structure fidelity of
LFINR results compared to deconvolution and VE-Deconv (view-enhanced deconvolution) ones.
Scale bar: 2 μm. **c,** The comparison between deconvolution, VE-Deconv and LFINR results
reconstructed from three FLFM views of ER (endoplasmic reticulum). Scale bar: 5 μm. **d,** Structure
similarity comparison of three approaches. The numbers above the "VE-Deconv" and "LFINR"
boxes represent the structure similarity enhancement ratio compared to the deconvolution approach.
e, Angular consistency evaluation through computed EPIs (epi-polar plane image) comparison of
different approaches. Top to bottom: deconvolution, VE-Deconv, LFINR and GT. **f,** LFINR
reconstruction from 19 FLFM views of cardiomyocyte nuclei**. g,** The
segmentation results of reconstructed volume in **(f)**, along with the comparison of IOU scores
between deconvolution and LFINR. Scale bar:10 μm.TP: True Positive. FP: False Positive. FN:
False Negative.

Fig.3 Comparative performance of deconvolution and LFINR reconstruction on diverse organelles. a, Captured views (7-view FLFM) of the mito Ma (tagged with Cox4-EGFP) in a whole live U2OS cell (left) and corresponding reconstruction results by deconvolution and LFINR (right). Scale bar: 10 μm. **b,** The comparison between deconvolution results (top row) and LFINR reconstruction (bottom row) in lateral and axial plane when the number of views becomes fewer. Full-aperture reconstruction referred to the reconstruction derived from 7 input views and tri-views reconstruction means using only 3 views (higher spatial resolution in each view) for the reconstruction. Insets denote the magnified view of *xy/xz* sections by each approach under each FLFM configuration. The linecuts through the resolved single mitochondria indicate the improved lateral and axial resolutions in LFINR reconstructions. Scale bar: 2 μm. **c,** Comparative results offered by deconvolution and LFINR along lateral and axial planes on microtubule (tagged with 3mEmerald-Ensconsin). Scale bar: 10 μm. **d,** The higher-magnification views of microtubule (marked by white rectangular regions in **c**). The plots denote the intensity profiles of the lines shown in the *xy* MIPs. Scale bar: 5 μm. **e,** The box plots show the statistical contrast ratio[28] of raw FLFM views, deconvolution results and LFINR results under various signal densities. The numbers denote the enhancement ratio compared with deconvolution approach. **f,** Comparison of the lateral planes at various axial position reconstructed by deconvolution (top row) and LFINR (bottom row). The dotted white line denoted the signal boundary at each depth, showing notably stronger optical sectioning capability by LFINR reconstruction. Scale bar: 10 μm. **g,** The captured 3 FLFM views of ER (tagged with EGFP-Sec61β) in a live U2OS cell. Scale bar: 10 μm**. g,** Depth-encoded *xy*

MIPS of 3D reconstructions by deconvolution, VE-Deconv and LFINR. Scale bar: 10 μm. **i**, The

higher-magnification views of white rectangular regions in **g,** showing notably less hallucinations

and axial aliasing, as indicated by the white arrows. The three insets shown in the right are *x-z*

sectional planes along the white dash line in **i**. Scale bar: 2 μm.

Spatial- angular bandwidth enlargement offered by LFINR

The hardware design of Fourier light-field microscopy (FLFM) is an art of balance on

angular and spatial information in a limited bandwidth determined by objective lens. In

the image domain, such trade-off usually reflected as the form of spatial resolution

degradation and axial artifacts. Here, in a complete self-supervised way eliminating

concerns regarding generalization, LFINR showcased its strong reconstruction

capability across diverse FLFM imaging configurations. The superior results were

quantitatively verified through various metrics (Fig. 3).

As shown in Fig 3a, LFINR reconstruction revealed the detailed structure of

mitochondria Ma (mitochondrial matrix) while deconvolution results exhibited blurry

(denoted by white arrowheads) under 7 views FLFM settings. The line width

measurement on resolved mitochondrial, in 'Full-aperture Reconstruction' of Fig 3b,

denoted that our 7-view LFINR has surpassed the FLFM system's theoretical resolution

limits, which shows ~1.68× and ~2.63× lateral and axial resolution enhancement

compared to model-based deconvolution results. Besides, with the robustness in 3D

reconstruction with few views, LFINR persevered the structural details while

deconvolution yielded noticeable artifacts in axial plane (denoted by red arrowheads in

'*Tri-views Reconstruction*', Fig 3b). Furthermore, with the increment of signals'

complexity, the model-based deconvolution approach suffered the cross-talk from

different slices. As depicted in Fig 3c, 3d, the microtube reconstructions by

deconvolution suffered from the blur and axial elongation, thereby showing lower

contrast and couldn't resolve the hollow structure in cell's axial slice. In contrast,

LFINR recovered the sharp contrast of microtubules and enabled the 3D visualization

of whole cell. The statistics results (Methods) in Fig 3e and different *xy*-planes in Fig

3f revealed the 3.7~4.1-folds contrast improvement under different signal's densities

and the superior optical sectioning ability of LFINR.

Besides, LFINR significantly reduced the artifacts when reconstructing volume

from merely three light-field views, under which though the views show higher spatial

resolution (Fig 3g), excessive high-frequency hallucinations and cross-talk of depth

information also arise (Fig 3h). These undesirable artifacts shown in deconvolution-

based results (denoted by white arrowheads in Fig 3i) have led to inadequate RSP[29]

metrics and low spatial resolution. In contrast, our LFINR removed the stripe artifacts

brought by lower angular sampling rate and achieved enhanced fidelity indicated by

higher RSP[29] values (0.886 vs 0.751, Fig 3i) and ~1.78-fold lateral resolution

enhancement (450 nm vs 800 nm on dense Endoplasmic Reticulum signals , Fig 3i).

High-quality 3D reconstruction with extremely few light-field views verified the

powerful arbitrary view-synthesis ability of LFINR.

Fig.4 Visualizations and quantifications of intracellular dynamics in live cells by LFMNR. a,
The scheme of light-field meta neural representation in solving multi-scenes generalization and
accelerating optimization. **b,** The rendering process of 3D volume derived from LFMNR weights.
c, *Left***:** The data size of 4D data (3D videos), LF videos (raw LF sequences) and LFMNR weights
(network parameters), denoting the strong data-compression ability of LFMNR. *Right*: The time-
consumption comparison of deconvolution and LFMNR for 3D reconstruct of light-field vieos. **d,**
Dual-color imaging of mitochondria (Green, tagged with Cox 4-EGFP) and lysosome (magenta,
tagged with EGFP-rab7) in live U2OS cells. Insets show the comparison of axial section between
deconvolution and LFINR. Scale bar: 5 μm. **e,** The volume rendering of the interaction process
between mitochondria and lysosome occurring in 100 seconds. Scale bar: 1 μm. **f,** The lateral
projection of dual-color LFMNR results illustrating the fast "kiss" (top panel) and "run" (bottom
panel) process. Scale bar: 1 μm. **g,** The velocity changes of lysosome during the whole process
visualized in **f**, quantifying the phenomenon of accelerated running away of lysosomes after
detaching with mitochondria. **h,** LFINR reconstruction of the first frame of the long-term
mitochondria evolution during cell mitosis. Scale bar, 50 μm. **i,** The dynamic process of
mitochondria over an observation period of 3.3 hours. The orange-yellow arrowheads denote the
spatial location of dynamics events. Scale bar: 2 μm. **j,** The segmentation result of LFMNR

reconstruction shown in (**h**). Scale bar: 20 μm. Insets show the fragmentation of mitochondria during
observation. Scale bar: 5 μm. **k,** The statistical results of the total length and quantity of
mitochondria during the whole observation based on the segmentation approach in (**j**).
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Light-field meta neural representation (LFMNR) boosts the 4D visualization of intracellular dynamics.

Dynamic biological processes, such intracellular interactions, often occur across three-
dimensional space for a long time. High-resolution extraction of the spatiotemporal
patterns of these dynamics requires consecutive volumetric reconstruction of light field
videos at high throughput, thereby posing big challenge to native LFINR which relies
on the scene-wise representation. To make LFINR practical to continuous 4D
visualization of biological dynamics, we proposed a weights-transfer strategy based on
meta-leaning to enhance the efficiency of sequential 3D reconstruction by inheriting
optimized parameters from prior implicit representation network, which was termed as
LFMNR (Fig. 4a, Methods). Initially, the first frame (LFINR T_0) was served as the key-
point to perform self-supervised 3D reconstruction with the progressive sampling
strategy. Subsequently, the optimized parameters were employed to initialize the
network of subsequent LF frame (LFINR T_1). Owing to the inherent motion continuity
of biological dynamics, the convergence can be reached with merely 100 fine-tuning
iterations with hybrid rendering model. As a result, an acceleration of ~100 folds was
achieved as compared to the time consumption on native INR optimization, leading to
an ~20 s quick reconstruction for each volume (Fig. 4c, Supplementary Figure 10).
When sequential optimization finished, LFMNR could "memorize" the 4D information
in a form of saved network weights. Users could input arbitrary 4D coordinates to index
corresponding voxels (Fig. 4b) instead of storage of grid-based 4D images. With the
unique feature of representation network and meta-learning strategy, our LFINR
overcame the deficiency on reconstruction speed, meanwhile it achieved data
compression (~10 folds reduction than the data size of LF views) and computation-cost
reduction (~2 folds) compared with current deconvolution approach (Fig. 4c).
To demonstrate the utility of LFINR, we conducted dual-color live-cell imaging to
capture the locomotion and interaction of mitochondria (tagged with Cox4-EGFP) and
lysosome (EGFP-rab7) in three dimensions, as shown in Fig. 4d. We visualized the
instantaneous 3D interactions between two types of organelles (Fig. 4e, f) at 10 Hz
volume rate. We tracked the velocity of lysosome during the period of "approaching-
contacting-separating", and identified the dramatic speed increase of lysosomes when
they were running away (Fig. 4f, g). Besides the fast interaction between organelles,
we also conducted long-term observation (~3.3 hours) of mitochondria evolution (Fig.
4 h, i). LFINR enabled capturing the multiple division events of mitochondria and
completely tracking the daughter mitochondria. In addition, leveraging the high
contrast of LFINR results, we segmented and identified each mitochondrion, revealing
the smaller and rounder mitochondria resulted from extensive fragmentation of
mitochondria shape (Fig. 4j). The statistical variation of mitochondria length and
quantity in Fig. 4k also demonstrated the mitochondrial fragmentation process,
indicating the potential apoptosis phase of the cells[30, 31].

Conclusion and Discussion

Achieving high-structural-fidelity 3D reconstruction in light-field microscopy, especially when the angular captures are limited and sparse, is essential for accurately capturing dynamic biological processes at high spatiotemporal resolution. Classical model-based approaches are inefficient in this regard due to the absence of prior knowledge. While supervised-learning methods offer a solution by constructing a "2D-to-3D" mapping function guided by volumetric data, they are laborious and costly in preparing labeled datasets and often suffer from poor generalization. Furthermore, the recovery of dense signals remains a challenge to all current light-field reconstruction approaches.

LFINR we propose in this work can achieve high-throughput and high-quality 3D reconstruction from a single 2D FLFM capture in a completely self-supervised manner, with the combination of inductive continuity bias of INR model and physics-based hybrid-rendering model.

Compared to conventional deconvolution approach, LFINR eliminates axial artifacts for dense signal reconstruction, maintaining high structural fidelity (Structural Similarity Index, SSIM: ~0.96) with low errors (Root Mean Square Error, RMSE: ~0.06). Notably, even in scenarios involving few-views reconstruction, LFINR maintains high structural fidelity due to its inherent geometric consistency across predicted views. INR's view-synthesis ability also mitigates axial elongation induced by missing cone problem, enabling artifact-free 3D reconstruction and spatial resolution enhancement by approximately ~4.4-fold in the imaging of diverse organelles. Furthermore, based on the correlation between FLFM and tomography, we extend the LFINR framework to tomography reconstruction, demonstrating its robustness and universality in solving a broad range of inversion problems in 3D image reconstruction (Supplementary Figure 11).

In addition to the improvement of reconstruction quality, to mitigate the computational cost in conventional uniform-random sampling strategy, we propose the progressive sampling with the aid of structural error map to accelerate convergence speed and prevent the signal loss. Further, to make LFINR practical in visualizing sustained biological dynamics, we develop a Meta-learning approach to expedite network convergence through temporal correlations, achieving ~two-order-of-magnitude significant acceleration with averaged inference time of merely 20 seconds for one volume.

In summary, our LFINR utilizes neural networks to smoothly represent high-dimensional scenes (3D volumes) with low-dimensional observations (2D FLFM views). This new "scene representation" paradigm solves the issue of inadequate quality in classical model-based light-field reconstruction approaches while completely eliminates the dependence on data priors. Meanwhile, it not only enhances the image quality for light-field 3D reconstruction but also exhibits capability in data compression. We envision that LFINR can be further optimized through the future efforts on training acceleration for real-time reconstruction[32], combination with high-quality optical setups for higher resolution beyond diffraction limit of the views[33], and robust

restoration under diverse degradation models[34, 35]. Besides the light-field microscopy, we anticipate that this self-supervised concept will also facilitate solutions in various other computational 3D bioimaging techniques, such as x-ray tomography[36, 37], cryo-electron tomography[38], Fourier ptychographic microscopy[39, 40], MRI[41, 42] etc.

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Declaration of Interests

The authors declare no competing interests.

Methods

FLFM optical setup

The FLFM system was built on a commercial inverted microscope (IX73, Olympus). To demonstrate the versatility of LFINR under various hardware settings, we conducted experiments with both 7-view and 3-view configurations.

For the 7-view setting, we utilized an objective lens (M60/NA1.5, Olympus UPLXAPO60XO) to collect fluorescent emission, which was controlled by an objective scanner. To prevent the overlap between captured views, an iris (SM1D12, Thorlabs) was positioned as the native image plane. The focal length of Fourier lens was set to 250 mm. A microlens array (*pitch* = 3.25 mm, *f-number* = 37, f_{ML} = 120 mm) was placed at the back foci plane of Fourier lens, producing 7 FLFM views. The whole schematic of the optical path is shown in Fig 1a.

For the 3-view setting, the objective (Olympus UPLSAPO100XO/1.4) was set to 100×/1.4 and the focal length of Fourier length was 300 mm. The optical parameters of microlens array were the same with 7-view settings.

The simulation parameters for the 3-view & 7-view system in Fig 2 were the same with above experimental settings, except for the 19-views one. For obtaining the projections of cardiomyocyte nuclei, we used 20×/0.5 objective and Fourier lens with 250 mm focal length. The focal length and pitch of MLA were 150 mm and 2 mm, which produced 19 views.

Progressive sampling strategy

INR-based approach[22] adopted random sampling strategy to constant optimize the scene-representation network. The number of coordinates depended the speed of network convergence, which was multiplicatively increased with the size of 3D scene. Further, when applied such random sampling strategy to represent the 3D biological scene, the uneven distribution of grayscale intensity and structural complexity in fluorescent images made this representation difficult, denoted by the weak-signal loss

and slow convergence (Supplementary Figure 3). We attributed this deficiency to the
ignoration of each voxel's contribution when conducting loss summation and averaging,
implying that the network tended to repeatedly optimize the "easy" area with low-
frequency and high intensity[43]. Inspired by the hard example mining in object
detection[44], we developed a progressive sampling strategy to focus on the positions
where contains structural distortion and signal loss.

The sampling strategy contains 3 steps: sparse sampling, full-sampling and focal
sampling as shown in Fig 1b.

Firstly, for the optimization process of one scene, the captured FLFM views were
down-sampled to half the size of original ones. Accordingly, the spatial meshgrid and
the projection matrixes (FLFM PSF and geometry projection matrix) in hybrid physics
model were also re-sampled to match the location and sampling rate of the resized
views. Based on the low-frequency implicit bias[43] in neural network, this sparse
sampling strategy simplified the fitting task on complex 3D signal and reduced the
number of query voxels, thereby promoting the convergence at the initial stage.

Secondly, the neural network was optimized under the supervision of multi-views
with the original sampling rate to recover the high-frequency details of the 3D scene,
which would exist signal loss like random sampling strategy. Therefore, during the
optimization process, an error map was simultaneously calculated and saved for the
following step as the sampling probability map. Denoting $y' \subseteq \mathbb{R}^{N \times N}$ as the center-
view projection from LFINR 3D prediction with geometry-model, and $y \subseteq \mathbb{R}^{N \times N}$ as
the target enhanced center view. The error map can be formulated as:

$$ErrorMap(y', y) = \hat{1} - SSIMMap(y', y) - \frac{1}{N^2} \sum_{i=1}^{N^2} SSIMMap(y', y)$$

$$SSIMMap(y', y) = \frac{(2\mu_y\mu_{y'} + c_1)(2\sigma_{yy'} + c_2)}{(\mu_y^2 + \mu_{y'}^2 + c_1)(\sigma_y^2 + \sigma_{y'}^2 + c_2)}$$

where $\hat{1}$ means an all-ones matrix with the size of center view and N means the lateral
size of the center view. μ_y and $\mu_{y'}$ are the mean of y and y', respectively. σ_y^2 and
$\sigma_{y'}^2$ stand for the variance of y and y'. $c_1 = 0.01^2$ and $c_2 = 0.03^2$ are constants
for 32-bit data (normalized to (0,1)). The kernel size used in SSIM calculation was set
to 7. Then, we converted this map into a sampling probability map via dividing each
pixel value by the summation of error map.

Thirdly, based on the calculated dynamic probability map, we conducted selective
optimization on different regions of scene to recover the structural details. The time
consumptions of various samples were listed in Supplementary Table 1.

Hybrid model rendering.
During the view rendering phase, LFINR adopted hybrid physics model to generate
dual forward projection. The first term in the hybrid model was described by the FLFM
PSF based on the wave-optics theory. In this paper, we modified the source code of
oLaF[45] to generate PSF matrix, which was then convolved with represented 3D scene
to produce wave-optics projection. The second term involved a geometric-optical
model to describe the propagation process of ideal rays. Similar to the convolution

process in first part, this rendering process can be also described as the convolution
between 3D volume and geometry projection matrix. To obtain this matrix, the 3D
positions of maximum value of FLFM PSF at different depth were extracted first. Then,
conducting linear fitting on these coordinates to obtain the depth-wise shift functions
of different views:

$$x^i(z) = f_x^i(z)$$

$$y^i(z) = f_y^i(z)$$

515 where i is the view index and $x \& y \& z$ are the 3D spatial coordinates. f_x^i and f_y^i are
516 the fitted parallax function, which revealed the projective geometry relation. Then,
517 input all z-coordinates into these two functions to obtain the 3D positions of chief rays.
518 Finally, an all-zero matrix with the size of the FLFM PSF was created, and voxels at
519 the obtained 3D positions were assigned a value of 1.
520
521 **Geometry consistency.**
522 To assess the fidelity of 3D reconstructions and underscore the view-synthesis ability
523 of LFINR, we employed geometry-consistency, computed from the structural similarity
524 of Epi-polar Plane Images (EPIs)[27] generated from 3D reconstructions and ground truth,
525 which can be formulated as:

$$Geometry consistency = SSIM\big(EPI(y'), EPI(y)\big)$$

$$EPI(\cdot) = Reslice(Proj_{geometry}(\cdot))$$

where y' is the reconstruction result from deconvolution-based methods or LFINR

and y is the ground truth. $Proj_{geometry}$ refers to the generation of views with
horizontal arrangement by a tomography projection model. The number of generated
views was set to 19 to ensure angular continuity. The angle range of this model was set
to $(-\theta_{obj}, \theta_{obj})$ where θ_{obj} is the maximum acquisition angle decided by
objective's NA. The operation of *Reslice* involves two steps: *a*. Concatenate the
generated 2D projections along z-axis to obtain "view-stack"; *b*. "Top-reslice" the
"view-stack" in Fiji to obtain axial section. This section plane is the EPI, containing
both spatial information and angular information. The whole process is illustrated in
Supplementary Figure 8.
538
Network implementation of LFINR
During one network optimization process, the input coordinates would follow 3 steps
to obtain the computed loss: 1) Position encoding 2) MLP inference 3) Loss
computation (Supplementary Figure 2).
Position encoding. The coordinates' low-frequency variation among 3D space would
degrade the rendering quality of structural details or color variation[22]. Therefore, in
LFINR, we adopt the Fourier positional encoding to convert such variation to the
encoded high-frequency information:

$\gamma(p_{xy}) = \{(sin2^0\pi p_{xy}, cos2^0\pi p_{xy}), (sin2^1\pi p_{xy}, cos2^1\pi p_{xy}), ..., (sin2^{L_{xy}-1}\pi p_{xy}, cos2^{L_{xy}-1}\pi p_{xy})\}$
$\gamma(p_z) = \{(sin2^0\pi p_z, cos2^0\pi p_z p_z), (sin2^1\pi p_z, cos2^1\pi p_z), ..., (sin2^{L_z-1}\pi p_z, cos2^{L_z-1}\pi p_z)\}$

where p_{xy} is the lateral coordinate (x, y) while p_z is the axial coordinate (z). L_{xy} and
L_z are lateral and axial encoding order, respectively. The detailed settings of L_{xy} and
L_z in various sample are listed in Supplementary Table 1. After position encoding, a
high-dimensional feature vector would be obtained, denoting as $v \subseteq \mathbb{R}^{N \times L}$, where N is
the number of input coordinates and L is the channel of encoded feature deiced by L_{xy}
and L_z. Each element v_i in v can be expressed as:

555
$$v_i = [\gamma(p_{xy}), \gamma(p_z), x, y, z]$$

556   ***MLP inference.*** We utilized a Multi-layer Perceptron (MLP) to represent the 3D scene
557   with querying spatial coordinates. MLP consists of input layer, hidden layers and output
558   layers. The detailed parameters are seen in Supplementary Table 1. This process can be
559   formulated as:

560
$$I_i = Relu(MLP(v_i))$$
561
$$Vol_{pred} = Reshape(\{I_i\}_{i=1}^N)$$

where i is the index of some voxel and $I(i)$ is corresponding grayscale. $Relu$ is
used to truncate the predicted values smaller than zero. After network inference, the
collection of predicted voxels would be reshaped to the 3D-grid image (Vol_{pred}).
Loss computation. In LFINR, the loss function consisted two parts: L_2 loss function in
wave-optics projection process and structural loss function in geometry projection
process (Fig 1b). Specifically, the represented volume was convolved with FLFM PSF
to fit the captured LF views and also with geometry projection matrix to fit enhanced
views. The objective function of network optimization based on these views can be
expressed as:

571
$$Loss = L_2(Vol_{pred} * PSF_o, y) + \lambda_1 \left(1 - SSIM(Vol_{pred} * PSF_g, \hat{y})\right) + \lambda_2 \nabla_{zz}(Vol_{pred})$$

572
$$+ \lambda_3 L_1(Vol_{pred})$$

where PSF_o and PSF_g are wave-optics PSF and geometry PSF, respectively. $\hat{y}$ and
y are enhanced views and raw views. ∇_{zz} and $L_1(\cdot)$ are the regularization term to
avoid model overfitting. λ_1, λ_2, λ_3 are weighting coefficients (Supplementary Table
1).

Data pre-processing
For static scene, the raw LF images underwent background subtraction by rolling-ball
subtraction in Fiji. Subsequently, the mean intensity of each view was rescaled to be
the same. Additionally, the PSF of each view was divided by the corresponding
summation to conduct normalization. For dynamic scenes, in addition to background
subtraction, the mean intensity of each frame was rescaled to be uniform. Due to the
noise inherent in living cell imaging, a lightweight self-supervised denoising network
(Supplementary Note 3) was constructed to enhance the signal-to-noise ratio (SNR)
based on the captured LF videos. During the training stage, all input LF images were
normalized to the range (0, 1).

Dynamic-scene representation by LFMNR

The essence of implicit neural representation (INR) is to represent complex high-
dimensional signal smoothly with neuron network. For living biological imaging, the
signal varies along 3D spatial coordinates and a 1D time axis, presenting challenges for
network representation. One plausible approach is to add the 't-variable' directly into
INR optimization to learn the 4D function $f(x, y, z, t)$. However, this approach
significantly increases the computational burden due to the massive inputs of four-
dimensional coordinates, especially for long-term imaging. Moreover, sudden
grayscale changes caused by fast motion further complicate the four-dimensional
function. Another approach involves employing an additional network to predict the
motion modality of 3D signal[46], but constructing such motion model requires
sophisticated handcrafting, making it challenging to accurately model irregular motion
patterns and local morphologies of biological samples. Inspired by redundancy
elimination techniques in data compression[47], we proposed a meta-learning-based
approach to represent dynamic 3D scenes encoded in light field sequence, termed light-
field meta neural representation (LFMNR), enabling the acceleration of network
convergence based on high inter-frame correlation. Meta-learning, often referred to as
"learning to learn", is a broad concept in metacognition that involves understanding and
improving one's own learning processes. In this context, meta-learning refers to using
optimization results from one scenario as the starting point for the next scenario's
optimization, aiming to accelerate the learning process of neural networks. Specifically,
during training phase, we first optimized network to represent the first volume with the

guidance of input T_1 views, which produced network weights θ_1' and optimizer Opt_1.
The learning rate was 5×10^{-4} and the number of total iterations were 12000. For the

second volume, the network and optimizer were initialized with parameters θ_1' and
with Opt_1, respectively. Then, the network was updated under the supervision of T_2
views. For remained volumes, according to consecutively transferring the previous
parameters, the network convergence time was dramatically. During transfer-learning
stage, the number of iterations was 100 for each time-point, which cost ~20 s.
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