Semantical and Geometrical Protein Encoding Toward Enhanced Bioactivity and Thermostability

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Abstract Protein engineering is a pivotal aspect of synthetic biology, involving the modification of amino acids within existing protein sequences to achieve novel or enhanced functionalities and physical properties. Accurate prediction of protein variant effects requires a thorough understanding of protein sequence, structure, and function. Deep learning methods have demonstrated remarkable performance in guiding protein modification for improved functionality. However, existing approaches predominantly rely on protein sequences, which face challenges in efficiently encoding the geometric aspects of amino acids' local environment and often fall short in capturing crucial details related to protein folding stability, internal molecular interactions, and bio-functions. Furthermore, there lacks a fundamental evaluation for developed methods in predicting protein thermostability, although it is a key physical property that is frequently investigated in practice. To address these challenges, this paper introduces a novel pre-training framework that integrates sequential and geometric encoders for protein primary and tertiary structures. This framework guides mutation directions toward desired traits by simulating natural selection on wild-type proteins and evaluates variant effects based on their fitness to perform specific functions. We assess the proposed approach using three benchmarks comprising over 300 deep mutational scanning assays. The prediction results showcase exceptional performance across extensive experiments when compared to other zero-shot learning methods, all while maintaining a minimal cost in terms of trainable parameters. This study not only proposes an effective framework for more accurate and comprehensive predictions to facilitate efficient protein engineering, but also enhances the *in silico* assessment system for future deep learning models to better align with empirical requirements. The PyTorch implementation are available at https://github.com/tyang816/ProtSSN.

Introduction

The diverse roles proteins play in nature necessitate their involvement in varied bio-functions, such as catalysis, binding, scaffolding, and transport. Advances in science and technology have posi-

Figure 1. An illustration of ProtSSN that extracts the semantical and geometrical characteristics of a protein from its sequentially-ordered global construction and spatially-gathered local contacts with protein language models and equivariant graph neural networks. The encoded hidden representation can be used for downstream tasks such as variants effect prediction that recognizes the impact of mutating a few sites of a protein on its functionality.

tioned proteins, particularly those with desired catalytic and binding properties, to pivotal positions in medicine, biology, and scientific research (*Zhou et al., 2024a*). While wild-type proteins exhibit optimal bio-functionality in their native environments, industrial applications often demand adaptation to conditions such as high temperature, high pressure, strong acidity, and strong alkalinity. The constrained efficacy of proteins in meeting the stringent requirements of industrial functioning environments hinders their widespread applications (*Woodley, 2013*; *Ismail et al., 2021*; *Jiang et al., 2023*). Consequently, there arises a need to engineer these natural proteins to enhance their functionalities, aligning them with the demands of both industrial and scientific applications.

Analyzing the relationship between protein sequence and function yields valuable insights for engineering proteins with new or enhanced functions in synthetic biology. The intrinsic goal of protein engineering is to unveil highly functional sequences by navigating the intricate, high-dimensional surface of the fitness landscape (*Yang et al., 2019*), which delineates the relationship between amino acid (AA) sequences and the desired functional state. Predicting the effects of AA substitutions, insertions, and deletions (*Riesselman et al., 2018*; *Gray et al., 2018*; *Notin et al., 2022a*) in proteins, *i.e.*, mutation, thus allows researchers to dissect how changes in the AA sequence can impact the protein's catalytic efficiency, stability, and binding affinity (*Shin et al., 2021*). However, the extensive, non-contiguous search space of AA combinations poses challenges for conventional methods, such as rational design (*Aprile et al., 2020*) or directed evolution (*Wang et al., 2021*), in efficiently and effectively identifying protein variants with desired properties. In response, deep learning has emerged as a promising solution that proposes favorable protein variants with high fitness.

Deep learning approaches have been instrumental in advancing scientific insights into proteins, predominantly categorized into sequence-based and structure-based methods. Autoregressive protein language models (*Notin et al., 2022a*; *Madani et al., 2023*) interpret AA sequences as raw text to generate with self-attention mechanisms (*Vaswani et al., 2017*). Alternatively, masked language modeling objectives develop attention patterns that correspond to the residue-residue contact map of the protein (*Meier et al., 2021*; *Rao et al., 2021a*; *Rives et al., 2021*; *Vig et al., 2021*; *Brandes et al., 2022*; *Lin et al., 2023*). Other methods start from a multiple sequence alignment, summarizing the evolutionary patterns in target proteins (*Riesselman et al., 2018*; *Frazer et al., 2021*; *Rao et al., 2021b*). These methods result in a strong capacity for discovering the hidden protein space. However, the many-to-one relationship of both sequence-to-structure and structure-to-function projections requires excessive training input or substantial learning resources, which raises concerns regarding the efficiency of these pathways when navigating the complexities of the vast sequence space associated with a target function. Moreover, the overlooked local environment of proteins hinders the model's ability to capture structure-sensitive properties that impact protein's thermostability, interaction with substrates, and catalytic process (*Zhao et al., 2022*;

₇₇ *Koehler Leman et al., 2023*). Alternatively, structure-based modeling methods serve as an effective
₇₈ enhancement to complement sequence-oriented inferences for proteins with their local environ-
₇₉ ment (*Tan et al., 2024e*; *Zhou et al., 2024c*; *Yi et al., 2024*; *Zhou et al., 2024b*; *Tan et al., 2024c*).
₈₀ Given that core mutations often induce functional defects through subtle disruptions to structure
₈₁ or dynamics (*Roscoe et al., 2013*), incorporating protein geometry into the learning process can
₈₂ offer valuable insights into stabilizing protein functioning. Recent efforts have been made to en-
₈₃ code geometric information of proteins for topology-sensitive tasks such as molecule binding (*Jin
₈₄ et al., 2021*; *Myung et al., 2022*; *Kong et al., 2023*) and protein properties prediction (*Zhang et al.,
₈₅ 2022*; *Tan et al., 2024d*,a). Nevertheless, structure encoders fall short in capturing non-local con-
₈₆ nections for AAs beyond their contact region and overlook correlations that do not conform to the
₈₇ 'structure-function determination' heuristic.

₈₈ There is a pressing need to develop a novel framework that overcomes limitations inherent
₈₉ in individual implementations of sequence or structure-based investigations. To this end, we in-
₉₀ troduce ProtSSN to assimilate the semantics and topology of **Prot**eins from their **S**equence and
₉₁ **S**tructure with deep neural **N**etworks. ProtSSN incorporates the intermediate state of protein struc-
₉₂ tures and facilitates the discovery of an efficient and effective trajectory for mapping protein se-
₉₃ quences to functionalities. The developed model extends the generalization and robustness of
₉₄ self-supervised protein language models while maintaining low computational costs, thereby facil-
₉₅ itating self-supervised training and task-specific customization. A funnel-shaped learning pipeline,
₉₆ as depicted in Fig. 1, is designed due to the limited availability of protein crystal structures com-
₉₇ pared to observed protein sequences. Initially, the linguistic embedding establishes the semantic
₉₈ and grammatical rules in AA chains by inspecting millions of protein sequences. The topological
₉₉ embedding then enhances the interactions among locally connected AAs. Since a geometry can
₁₀₀ be placed or observed by different angles and positions in space, we represent proteins' topol-
₁₀₁ ogy by graphs and enhance the model's robustness and efficiency with a rotation and translation
₁₀₂ equivariant graph representation learning scheme.

₁₀₃ The pre-trained ProtSSN demonstrates its feasibility across a broad range of mutation effect
₁₀₄ prediction benchmarks covering catalysis, interaction, and thermostability. Mutation effects pre-
₁₀₅ diction serves as a common *in silico* assessment for evaluating the capability of an established
₁₀₆ deep learning framework in identifying favorable protein variants. With the continuous evolution of
₁₀₇ deep mutation scanning techniques and other high-throughput technologies, benchmark datasets
₁₀₈ have been curated to document fitness changes in mutants across diverse proteins with varying de-
₁₀₉ grees of combinatorial and random modifications (*Moal and Fernández-Recio, 2012*; *Nikam et al.,
₁₁₀ 2021*; *Veleckỳ et al., 2022*). **ProteinGym v1** (*Notin et al., 2024*) comprehends fitness scoring of mu-
₁₁₁ tants to catalytic activity and binding affinity across over 200 well-studied proteins of varying deep
₁₁₂ mutational scanning (DMS) assays and taxa. Each protein includes tens of thousands of mutants
₁₁₃ documented from high-throughput screening techniques. While **ProteinGym v1** initiates the most
₁₁₄ comprehensive benchmark dataset for mutants toward different properties enhancement, these
₁₁₅ fitness scores are normalized and simplified into several classes without further specifications. For
₁₁₆ instance, a good portion of protein assays is scored by their stability, which, in practice, is further
₁₁₇ categorized into thermostability, photostability, pH-stability, *etc*. Moreover, these stability prop-
₁₁₈ erties should be discussed under certain environmental conditions, such as pH and temperature.
₁₁₉ Unfortunately, these detailed attributes are excluded in **ProteinGym v1**. Since a trade-off rela-
₁₂₀ tionship emerges between activity and thermostability (*Zheng et al., 2022*), protein engineering in
₁₂₁ practice extends beyond enhancing catalytic activities to maintaining or increasing thermostabil-
₁₂₂ ity for prolonged functional lifetimes and applications under elevated temperatures and chemical
₁₂₃ conditions (*Liu et al., 2019*). Consequently, there is a need to enrich mutation effect prediction
₁₂₄ benchmarks that evaluate the model's efficacy in capturing variant effects concerning thermosta-
₁₂₅ bility under distinct experimental conditions. In this study, we address the mutation effect predic-
₁₂₆ tion tasks on thermostability with **DTm** and **DDG**, two new single-site mutation benchmarks that
₁₂₇ measure thermostability using ΔTm and $\Delta\Delta$G values, respectively. Both benchmarks group exper-

Figure 2. An example source record of the mutation assay. The record is derived from DDG for the A chain of protein 1A7V, experimented at pH=6.5 and degree at 25°C.

Table 1. Statistical summary of **DTm** and **DDG**.

pH Range	DTm			DDG		
	# Assays	avg. # mut	avg. AA	# Assays	avg. # mut	avg.AA
Acid (pH < 7)	29	29.1	272.8	21	22.6	125.3
Neutral (pH = 7)	14	37.4	221.2	10	23.1	78.3
Alkaline (pH > 7)	23	50.1	233.3	5	24.6	101.4
sum	66	38.2	221.2	36	23.0	108.8

imental assays based on the protein-condition combinations. These two datasets supplement the publicly available DMS assay benchmarks and facilitate ready-to-use assessment for future deep learning methods toward protein thermostability enhancement.

This work fulfills practical necessities in the development of deep learning methods for protein engineering from three distinct perspectives. Firstly, the developed ProtSSN employs self-supervised learning during training to obviate the necessity for additional supervision in downstream tasks. This zero-shot scenario is desirable due to the scarcity of experimental results, as well as the 'cold-start' situation common in many wet lab experiments. Secondly, the trained model furnishes robust and meaningful approximations to the joint distribution of the entire amino acid chain, thereby augmenting the *epistatic effect* (*Sarkisyan et al., 2016*; *Khersonsky et al., 2018*) in deep mutations. This augmentation stems from the model's consideration of the nonlinear combinatorial effects of amino acid sites. Additionally, we complement the existing dataset of DMS assay with additional benchmark assays related to protein-environment interactions, specifically focusing on thermostability–an integral objective in numerous protein engineering projects.

Materials and Methods

This section starts by introducing the three mutational scanning benchmark datasets used in this study, including an open benchmark dataset **ProteinGym v1** and two new datasets on protein thermostability, *i.e.*, **DTm** and **DDG**. We establish the proposed ProtSSN for protein sequences and structures encoding in Section Proposed Method. The overall pipeline of model training and inference is presented in Section Model Pipeline. The experimental setup for model evaluation is provided in Section Experimental Protocol.

Dataset

To evaluate model performance in predicting mutation effects, we compare ProtSSN with SOTA baselines on **ProteinGym-v1**, the largest open benchmark for DMS assays. We also introduce two novel benchmarks, **DTm** and **DDG**, for assessing protein thermostability under consistent control

Table 2. Details of Zero-shot Baseline Models.

Model	Type		Description	Source Code
	seq	struct		
RITA (*Hesslow et al., 2022*)	✓		a generative protein language model with billion-level parameters	github.com/lightonai/RITA
ProGen2 (*Nijkamp et al., 2023*)	✓		a generative protein language model with billion-level parameters	github.com/salesforce/progen
ProtTrans (*Elnaggar et al., 2021*)	✓		Transformer-based models trained on large protein sequence corpus	github.com/agemagician/ProtTrans
Tranception (*Notin et al., 2022a*)	✓		an autoregressive model for variant effect prediction with retrieve machine	github.com/OATML-Markslab/Tranception
CARP (*Yang et al., 2024*)	✓		pretrained CNN protein sequence masked language models of various sizes	github.com/microsoft/protein-sequence-models
ESM-1b (*Rives et al., 2021*) ESM-1v (*Meier et al., 2021*) ESM2 (*Lin et al., 2023*)	✓ ✓ ✓		a masked language model-based pre-train method with various pre-training dataset and positional embedding strategies	github.com/facebookresearch/esm
ESM-if1 (*Hsu et al., 2022*)		✓	an inverse folding method with mask language modeling and geometric vector perception (*Jing et al., 2020*).	
MIF-ST (*Yang et al., 2023*)	✓	✓	pretrained masked inverse folding models with sequence pretraining transfer	github.com/microsoft/protein-sequence-models
SaProt (*Su et al., 2023*)	✓	✓	structure-aware vocabulary for protein language modeling with FoldSeek	github.com/westlake-repl/SaProt

153 environments. Details of the new datasets are provided in Table 1. Considering the significant in-
154 fluence of experimental conditions on protein temperature, we explicitly note the pH environment
155 in each assay. Refer to the following paragraphs for more details.

ProteinGym

The assessment of ProtSSN for deep mutation effects prediction is conducted on **ProteinGym v1**
(**Notin et al., 2024**). It is the most extensive protein substitution benchmark comprising 217 assays
and more than $2.5M$ mutants. These DMS assays cover a broad spectrum of functional properties
(*e.g.*, ligand binding, aggregation, viral replication, and drug resistance) and span various protein
families (*e.g.*, kinases, ion channel proteins, transcription factors, and tumor suppressors) across
different taxa (*e.g.*, humans, other eukaryotes, prokaryotes, and viruses).

DTm

The assays in the first novel thermostability benchmark are sourced from single-site mutations
in **ProThermDB** (**Nikam et al., 2021**). Each assay is named in the format '*UniProt_ID-pH*'. For in-
stance, '*O00095-8.0*' signifies mutations conducted and evaluated under pH 8.0 for protein 000095.
The attributes include 'mutant', 'score', and 'UniProt_ID', with at least 10 mutants to ensure a mean-
ingful evaluation. To concentrate on single-site mutations compared to wild-type proteins, we
exclude records with continuous mutations. To avoid dealing with partial or misaligned protein
structures resulting from incomplete wet experimental procedures, we employ UniProt ID to pair
protein sequences with folded structures predicted by AlphaFold2 (**Jumper et al., 2021**) from https:
//alphafold.ebi.ac.uk. In total, **DTm** consists of 66 such protein-environment pairs and $2,520$ muta-
tions.

DDG

The second novel thermostability benchmark is sourced from **DDMut** (**Zhou et al., 2023**), where
mutants are paired with their PDB documents. We thus employ crystal structures for proteins
in **DDG** and conduct additional preprocessing steps for environmental consistency. In particular,
we group mutants of the same protein under identical experimental conditions and examine the
alignment between mutation sites and sequences extracted from crystal structures. We discard
mutant records that cannot be aligned with the sequence loaded from the associated PDB docu-
ment. After removing data points with fewer than 10 mutations, **DDG** comprises 36 data points and
829 mutations. As before, assays are named in the format '*PDB_ID-pH-temperature*' to indicate the
chemical condition (pH) and temperature (in Celsius) of the experiment on the protein. An example
assay content is provided in Fig. 2.

Proposed Method

Labeled data are usually scarce in biomolecule research, which demands designing a general self-supervised model for predicting variant effects on unknown proteins and protein functions. We propose ProtSSN with a pre-training scheme that recovers residues from a given protein backbone structure with noisy local environment observations.

Multi-level Protein Representation

Protein Primary Structure (Noisy)

Denote a given observation with resiude $\tilde{v}$. We assume this arbitrary observation is undergoing random mutation toward a stable state. The training objective is to learn a revised state v that is less likely to be eliminated by natural selection due to unfavorable properties such as instability or inability to fold. The perturbed observation is defined by a multinomial distribution.

$$\pi(\tilde{v} \mid v) = p\Theta(\pi_1, \pi_2, \ldots, \pi_{20}) + (1 - p)\delta(\tilde{v} - v), \tag{1}$$

where an AA in a protein chain has a chance of p to mutate to one of 20 AAs (including itself) following a *replacement distribution* $\Theta(\cdot)$ and $(1 - p)$ of remaining unchanged. We consider p as a tunable parameter and define $\Theta(\cdot)$ by the frequency of residues observed in wild-type proteins.

Protein Tertiary Structure

The geometry of a protein is described by $\mathcal{G} = (\mathcal{V}, \mathcal{E}, \boldsymbol{W}_V, \boldsymbol{W}_E, \boldsymbol{X}_V)$, which is a residue graph based on the k-nearest neighbor algorithm (kNN). Each node $v_i \in \mathcal{V}$ represents an AA in the protein connected to up to k closest nodes within 30Å. Node attributes $\boldsymbol{W}_V$ are hidden semantic embeddings of residues extracted by the semantic encoder (see Section Semantic Encoding of Global AA Contacts), and edge attributes $\boldsymbol{W}_E \in \mathbb{R}^{93}$ feature relationships of connected nodes based on inter-atomic distances, local N-C positions, and sequential position encoding (*Zhou et al., 2024b*). Additionally, $\boldsymbol{X}_V$ records 3D coordinates of AAs in the Euclidean space, which plays a crucial role in the subsequent geometric embedding stage to preserve roto-translation equivariance.

Semantic Encoding of Global AA Contacts

Although it is generally believed by the community that a protein's sequence determines its biological function via the folded structure, following strictly to this singular pathway risks overlooking other unobserved yet potentially influential inter-atomic communications impacting protein fitness. Our proposed ProtSSN thus includes pairwise relationships for residues through an analysis of proteins' primary structure from $\tilde{V}$ and embeds them into hidden representations $\boldsymbol{W}_V$ for residues. At each iteration, the input sequences are modified randomly by (3) and then embedded via an *Evolutionary Scale Modeling* method, ESM-2 (*Lin et al., 2023*), which employs a BERT-style masked language modeling objective. This objective predicts the identity of randomly selected AAs in a protein sequence by observing their context within the remainder of the sequence. Alternative semantic encoding strategies are discussed in Section AA Perturbation Strategies.

Geometrical Encoding of Local AA Contacts

Proteins are structured in 3D space, which requires the geometric encoder to possess roto-translation equivariance to node positions as well as permutation invariant to node attributes. This design is vital to avoid the implementation of costly data augmentation strategies. We practice *Equivariant Graph Neural Networks* (EGNN) (*Satorras et al., 2021*) to acquire the hidden node representation $\boldsymbol{W}_V^{l+1} = \left\{ \boldsymbol{w}_{v_1}^{l+1}, \ldots, \boldsymbol{w}_{v_n}^{l+1} \right\}$ and node coordinates $\boldsymbol{X}_{\text{pos}}^{l+1} = \left\{ \boldsymbol{x}_{v_1}^{l+1}, \ldots, \boldsymbol{x}_{v_n}^{l+1} \right\}$ at the $l + 1$th layer

$$\boldsymbol{m}_{ij} = \phi_e \left(\boldsymbol{w}_{v_i}^l, \boldsymbol{w}_{v_j}^l, \left\| \boldsymbol{x}_{v_i}^l - \boldsymbol{x}_{v_j}^l \right\|^2, \boldsymbol{w}_{e_{ij}} \right),$$

$$\boldsymbol{x}_{v_i}^{l+1} = \mathbf{x}_{v_i}^l + \frac{1}{n} \sum_{j \neq i} \left(\mathbf{x}_{v_i}^l - \mathbf{x}_{v_j}^l \right) \phi_x \left(\mathbf{m}_{ij} \right), \tag{2}$$

$$\boldsymbol{w}_{v_i}^{l+1} = \phi_v \big(\boldsymbol{w}_i^l, \sum_{j \neq i} \boldsymbol{m}_{ij} \big).$$

In these equations, $\boldsymbol{w}_{e_{ij}}$ represents the input edge attribute on $\mathcal{V}_{ij}$, which is not updated by the network. The propagation rules ϕ_e, ϕ_x and ϕ_v are defined by differentiable functions, *e.g.*multi-layer perceptrons (MLPs). The final hidden representation on nodes $\boldsymbol{W}_V^L$ embeds the microenvironment and local topology of AAs, and it will be carried on by readout layers for label predictions.

Model Pipeline

ProtSSN is designed for protein engineering with a self-supervised learning scheme. The model is capable of conducting zero-shot variant effect prediction on an unknown protein, and it can generate the joint distribution for the residue of all AAs along the protein sequence of interest. This process accounts for the epistatic effect and concurrently returns all AA sites in a sequence. Below, we detail the workflow for training the zero-shot model and scoring the effect of a specific mutant.

Training

The fundamental model architecture cascades a frozen sequence encoding module and a trainable tertiary structure encoder. The protein is represented by its sequence and structure characteristics, where the former is treated as plain text and the latter is formalized as a kNN graph with model-encoded node attributes, handcrafted edge attributes, and 3D positions of the corresponding AAs. Each input sequence $\boldsymbol{V}$ are first one-hot encoded by 33 tokens, comprising both AA residues and special tokens *Lin et al.* (*2023*). The ground truth sequences, during training, will be permuted into

$$\tilde{\boldsymbol{V}} = \text{Permute}(\boldsymbol{V}). \tag{3}$$

Here $\tilde{\boldsymbol{V}}$ is the perturbed AA to be encoded by a protein language model, which analyses pairwise hidden relationships among AAs from the input protein sequence and produces a vector representation $\boldsymbol{w}_{v_i} \in \boldsymbol{W}_V$ for each AA, *i.e.*,

$$\boldsymbol{W}_V = \text{LM}_{\text{frozen}}(\tilde{\boldsymbol{V}}) \tag{4}$$

The language model $\text{LM}_{\text{frozen}}(\cdot)$, ESM-2 (*Lin et al., 2023*) for instance, has been pre-trained on a massive protein sequence database (*e.g.*, **UniRef50 (*Suzek et al., 2015*)**) to understand the semantic and grammatical rules of wild-type proteins with high-dimensional AA-level long-short-range interactions. The independent perturbation on AA residues follows (1) operates in every epoch, which requires constant updates on the sequence embedding. To further enhance the interaction of locally connected AAs in the node representation, a stack of L EGNN layers is implemented on the input graph $\mathcal{G}$ to yield

$$\boldsymbol{W}_V^L = \text{EGNN}(\mathcal{G}). \tag{5}$$

During the pre-training phase for protein sequence recovery, the output layer $\phi(\cdot)$ provides the probability of tokens in one of 33 types, *i.e.*,

$$\boldsymbol{Y} = \phi(\boldsymbol{W}_V^L) \in \mathbb{R}^{n \times 33} \tag{6}$$

for a protein of n AAs. The model's learnable parameters are refined by minimizing the cross-entropy of the recovered AAs with respect to the ground-truth AAs in wild-type proteins:

$$\text{loss} = -\sum_{n=1}^{L} \sum_{c=1}^{33} V_{n,c} \log\left(\text{softmax}(Y_{n,c})\right), \tag{7}$$

where L is the length of the sequence, n represents the position index within the sequence and each c corresponds to a potential type of token.

Inferencing

For a given wild-type protein and a set of mutants, the fitness scores of the mutants are derived from the joint distribution of the altered residues relative to the wild-type template. First, the wild-type protein sequence and structure are encoded into hidden representations following (4)-(5). Unlike the pre-training process, here the residue in the wild-type protein is considered as a

Table 3. Spearman's ρ correlation of variant effect prediction by with zero-shot methods on **DTm**, **DDG**, and **ProteinGym v1**.

Model	Version	# Params (million)	DTm	DDG	ProteinGym v1					
					Activity	Binding	Expression	Organismal	Stability	Overall Fitness
Sequence Encoder										
RITA	small	30	0.122	0.143	0.294	0.275	0.337	0.327	0.289	0.304
	medium	300	0.131	0.188	0.352	0.274	0.406	0.371	0.348	0.350
	large	680	0.213	0.236	0.359	0.291	0.422	0.374	0.383	0.366
	xlarge	1,200	0.221	0.264	0.402	0.302	0.423	0.387	0.445	0.373
ProGen2	small	151	0.135	0.194	0.333	0.275	0.384	0.337	0.349	0.336
	medium	764	0.226	0.214	0.393	0.296	0.436	0.381	0.396	0.380
	base	764	0.197	0.253	0.396	0.294	0.444	0.379	0.383	0.379
	large	2,700	0.181	0.226	0.406	0.294	0.429	0.379	0.396	0.381
	xlarge	6,400	0.232	0.270	0.402	0.302	0.423	0.387	0.445	0.392
PortTrans	bert	420	0.268	0.313	-	-	-	-	-	-
	bert_bfd	420	0.217	0.293	-	-	-	-	-	-
	t5_xl_uniref50	3,000	0.310	0.365	-	-	-	-	-	-
	t5_xl_bfd	3,000	0.239	0.334	-	-	-	-	-	-
Tranception	small	85	0.119	0.169	0.287	0.349	0.319	0.270	0.258	0.288
	medium	300	0.189	0.256	0.349	0.285	0.409	0.362	0.342	0.349
	large	700	0.197	0.284	0.401	0.289	0.415	**0.389**	0.381	0.375
ESM-1v	-	650	0.279	0.266	0.390	0.268	0.431	0.362	0.476	0.385
ESM-1b	-	650	0.271	0.343	0.428	0.289	0.427	0.351	0.500	0.399
ESM-2	t12	35	0.214	0.216	0.314	0.292	0.364	0.218	0.439	0.325
	t30	150	0.288	0.317	0.391	0.328	0.425	0.305	0.510	0.392
	t33	650	0.330	0.392	0.391	0.328	0.425	0.305	0.510	0.419
	t36	3,000	0.327	0.351	0.417	0.322	0.425	0.379	0.509	0.410
	t48	15,000	0.311	0.252	0.405	0.318	0.425	0.388	0.488	0.405
CARP	-	640	0.288	0.333	0.395	0.274	0.419	0.364	0.414	0.373
Structure Encoder										
ESM-if1	-	142	0.395	**0.409**	0.368	**0.392**	0.403	0.324	**0.624**	0.422
Sequence + Structure Encoder										
MIF-ST	-	643	**0.400**	0.406	0.390	0.323	0.432	0.373	0.486	0.401
SaProt	masked	650	0.382	-	**0.459**	**0.382**	**0.485**	0.371	**0.583**	**0.456**
	unmasked	650	0.376	0.359	0.450	**0.376**	**0.460**	0.372	**0.577**	**0.447**
ProtSSN (ours)	k20_h512	148	**0.419**	**0.442**	**0.458**	0.371	0.436	**0.387**	0.566	0.444
	ensemble	1,467	**0.425**	**0.440**	**0.466**	0.371	**0.451**	**0.398**	0.568	**0.451**

† The top three are highlighted by **First**, **Second**, **Third**.

reference state and is compared with the predicted probability of AAs at the mutated site. Next, for a mutant with mutated sites $\mathcal{T}$ ($|\mathcal{T}| \geq 1$), we define its fitness score F_x using the corresponding *log-odds-ratio*, *i.e.*,

$$F_x = \sum_{t \in \mathcal{T}} \log p(\mathbf{y}_t) - \log p(\mathbf{v}_t), \tag{8}$$

where $\mathbf{y}_t$ and $\mathbf{v}_t$ denote the mutated and wild-type residue of the tth AA.

Experimental Protocol

We validate the efficacy of ProtSSN on zero-shot mutation effect prediction tasks. The performance is compared with other SOTA models of varying numbers of trainable parameters. The implementations are programmed with `PyTorch-Geometric` (ver 2.2.0) and `PyTorch` (ver 1.12.1) and executed on an NVIDIA® Tesla A100 GPU with $6,912$ CUDA cores and 80GB HBM2 installed on an HPC cluster.

Training Setup

ProtSSN is pre-trained on a non-redundant subset of **CATH v4.3.0** (*Orengo et al., 1997*) domains, which contains $30,948$ experimental protein structures with less than 40% sequence identity. We remove proteins that exceed $2,000$ AAs in length for efficiency. For each kNN protein graph, node

features are extracted and updated by a frozen ESM2-t33 prefix model (*Lin et al., 2023*). Protein topology is inferred by a 6-layer EGNN (*Satorras et al., 2021*) with the hidden dimension tuned from $\{512, 768, 1280\}$. Adam (*Kingma and Ba, 2015*) is used for backpropagation with the learning rate set to 0.0001. To avoid training instability or CUDA out-of-memory, we limit the maximum input to $8,192$ AA tokens per batch, constituting approximately 32 graphs.

Baseline Methods

We undertake an extensive comparison with baseline methods of self-supervised sequence or structure-based models on the fitness of mutation effects prediction (Table 2). Sequence models employ position embedding strategies such as autoregression (RITA (*Hesslow et al., 2022*), Tranception (*Notin et al., 2022a*), and ProGen2 (*Nijkamp et al., 2023*)), masked language modeling (ESM-1b (*Rives et al., 2021*), ESM-1v (*Meier et al., 2021*), and ESM2 (*Lin et al., 2023*)), a combination of the both (ProtTrans (*Elnaggar et al., 2021*)), and convolutional modeling (CARP (*Yang et al., 2024*)). Additionally, we also compare with ESM-if1 (*Hsu et al., 2022*) which incorporates masked language modeling objectives with GVP (*Jing et al., 2020*), as well as MIF-ST (*Yang et al., 2023*) and SaProt *Su et al.* (*2023*) with both sequence and structure encoding.

The majority of the performance comparison was conducted on zero-shot deep learning methods. However, for completeness, we also report a comparison with popular MSA-based methods, such as GEMME (*Laine et al., 2019*), Site-Independent (*Hopf et al., 2017*), EVmutation (*Hopf et al., 2017*), Wavenet (*Shin et al., 2021*), DeepSequence (*Riesselman et al., 2018*), and EVE (*Frazer et al., 2021*). Other deep learning methods use MSA for training or retrieval, including MSA-Transformer (*Rao et al., 2021b*), Tranception (*Notin et al., 2022a*) and TranceptEVE (*Notin et al., 2022b*).

Scoring Function

Following the convention, the fitness scores of the zero-shot models are calculated by the log-odds ratio in (8) for encoder methods, such as the proposed ProtSSN and the ProtTrans series models. For autoregressive and inverse folding models (*e.g.*, Tranception and ProGen2) that predict the next token x_i based on the context of previous $x_{1:i-1}$ tokens, the fitness score F_x of a mutated sequence $\boldsymbol{y}$ is computed via the log-likelihood ratio with the wild-type sequence $\boldsymbol{v}$, *i.e.*,

$$F_x = \log \frac{P(\boldsymbol{y})}{P(\boldsymbol{v})}. \tag{9}$$

Benchmark Datasets

We conduct a comprehensive comparison of deep learning predictions on hundreds of DMS assays concerning different protein types and biochemical assays. We prioritize experimentally measured properties that possess a monotonic relationship with protein fitness, such as catalytic activity, binding affinity, expression, and thermostability. In particular, **ProteinGym v1** (*Notin et al., 2024*) groups 5 sets of protein properties from 217 assays. Two new datasets named **DTm** and **DDG** examine 102 environment-specific assays with thermostability scores. In total, 319 assays with around 2.5 million mutants are scored. To better understand the novelty of the proposed ProtSSN, we designed additional investigations on **ProteinGym v0** (*Notin et al., 2022a*), an early-release version of **ProteinGym** with $1.5M$ missense variants across 86 assays (excluding one assay that failed to be folded by both AlphaFold2 and ESMFold, *i.e.*, `A0A140D2T1_ZIKV_Sourisseau_growth_2019`).

Evaluation Metric

We evaluate the performance of pre-trained models on a diverse set of proteins and protein functions using Spearman's ρ correlation that measures the strength and direction of the monotonic relationship between two ranked sequences, *i.e.*, experimentally evaluated mutants and model-inferred mutants (*Meier et al., 2021*; *Notin et al., 2022a*; *Frazer et al., 2021*; *Zhou et al., 2024b*). This non-parametric rank measure is robust to outliers and asymmetry in mutation scores, and it does not assume any specific distribution of mutation fitness scores. The scale of ρ ranges from -1

Figure 3. Number of trainable parameters and Spearman's ρ correlation on **DTm**, **DDG**, and **ProteinGym v1**, with the medium value located by the dashed lines. Dot, cross, and diamond markers represent sequence-based, structure-based, and sequence-structure models, respectively.

to 1, indicating the negative or positive correlation of the predicted sequence to the ground truth. The prediction is preferred if its ρ to the experimentally examined ground truth is close to 1.

Results

Variant Effect Prediction

We commence our investigation by assessing the predictive performance of ProtSSN on four benchmark datasets using state-of-the-art (SOTA) protein learning models. We deploy different versions of ProtSSN that learns kNN graphs with $k \in \{10, 20, 30\}$ and $h \in \{512, 768, 1, 280\}$ hidden neurons in each of the 6 EGNN layers. For all baselines, their performance on **DTm** and **DDG** are reproduced with the official implementation listed in Table 2, and the scores on **ProteinGym v1** are retrieved from https://proteingym.org/benchmarks by *Notin et al.* (*2024*). As visualized in Fig. 3 and reported in Table 3, ProtSSN demonstrated exceptional predictive performance with a significantly smaller number of trainable parameters when predicting the function and thermostability of mutants.

Compared to protein language models (Fig. 3, colored circles), ProtSSN benefits from abundant structure information to more accurately capture the overall protein characteristics, resulting in enhanced thermostability and thus achieving higher correlation scores on **DTm** and **DDG**. This is attributed to the compactness of the overall architecture as well as the presence of stable local structures such as alpha helices and beta sheets, both of which are crucial to protein thermostability by providing a framework that resists unfolding at elevated temperatures (*Robinson-Rechavi et al., 2006*). Consequently, the other two structures-involved models, *i.e.*, ESM-if1 and MIF-ST, also exhibit higher performance on the two thermostability benchmarks.

On the other hand, although protein language models can typically increase their scale, *i.e.*, the number of trainable parameters, to capture more information from sequences, they cannot fully replace the role of the structure-based analysis. This observation aligns with the mechanism of protein functionality, where local structures (such as binding pockets and catalytic pockets) and the overall structure (such as conformational changes and allosteric effect) are both crucial for binding and catalysis (*Sheng et al., 2014*). Unlike the thermostability benchmarks, the discrepancies between structure-involved models and protein language models are mitigated in **ProteinGym v1** by increasing the model scale. In summary, structure-based and sequence-based methods are suitable for different types of assays, but a comprehensive framework (such as ProtSSN) demonstrates superior overall performance compared to large-scale language models. Moreover, ProtSSN demonstrates consistency in providing high-quality fitness predictions of thermostability. We randomly bootstrap 50% of the samples from **DTm** and **DDG** for ten independent runs, the results are reported In Table 6 for both the average performance and the standard deviation. ProtSSN achieves top performance with minimal variance.

Ablation Study

The effectiveness of ProtSSN with different modular designs is examined by its performance on the early released version **ProteinGym v0** (*Notin et al., 2022a*) with 86 DMS assays. The complete comparison of baseline comparison on **ProteinGym v0** is detailed in Table S1 in SI. For the ablation

Figure 4. Ablation Study on **ProteinGym v0** with different modular settings of ProtSSN. Each record represents the average Spearman's correlation of all assays. (a) Performance using different structure encoders: EGNN (orange) versus GCN/GAT (purple); (b) Performance using different node attributes: ESM2-embedded hidden representation (orange) versus one-hot encoding (purple); (c) Performance with varying numbers of EGNN layers; (d) Performance with different versions of ESM2 for sequence encoding; (e) Performance using different amino acid perturbation strategies during pre-training.

study, the results are summarized in Fig. 4(a)-(d) and detailed in Table S2, where each record is subject to a combination of key arguments under investigation. For instance, in the top orange box of Fig. 4(a), we report all ablation results that utilize 6 EGNN layers for graph convolution, regardless of the different scales of ESM-2 or the definitions of node attributes. For all modules investigated in this section, we separately discuss their influence on predicting mutation effects when modifying a single site or an arbitrary number of sites. The two cases are marked on the y-axis by single' and 'all', respectively.

Inclusion of Roto-Translation Equivariance

We assess the effect of incorporating rotation and translation equivariance for protein geometric and topological encoding. Three types of graph convolutions are compared, including GCN (*Kipf and Welling, 2017*), GAT (*Veličković et al., 2018*), and EGNN (*Satorras et al., 2021*). The first two are classic non-equivariant graph convolutional methods, and the last one, which we apply in the main algorithm, preserves roto-translation equivariance. We fix the number of EGNN layers to 6 and examine the performance of the other two methods with either 4 or 6 layers. We find that integrating equivariance when embedding protein geometry would significantly improve prediction performance.

Sequence Encoding

We next investigate the benefits of defining data-driven node attributes for protein representation learning. We compare the performance of models trained on two sets of graph inputs: the first set defines its AA node attributes through trained ESM2 (*Lin et al., 2023*), while the second set uses one-hot encoded AAs for each node. A clear advantage of using hidden representations by prefix models over hardcoded attributes is evident from the results presented in Fig. 4(b).

Depth of EGNN

Although graph neural networks can extract topological information from geometric inputs, it is vital to select an appropriate number of layers for the module to deliver the most expressive node representation without encountering the oversmoothing problem. We investigate a wide range of choices for the number of EGNN layers among $\{6, 12, 18\}$. As reported in Fig. 4(c), embedding graph topology with deeper networks does not lead to performance improvements. A moderate choice of 6 EGNN layers is sufficient for our learning task.

Scale of ESM

We also evaluate ProtSSN on different choices of language embedding dimensions to study the trade-off between computational cost and input richness. Various scales of prefix models, including $\{8, 150, 650, 3000\}$ millions of parameters, have been applied to produce different sequential embeddings with $\{320, 640, 1280, 2560\}$ dimensions, respectively. Fig. 4(d) reveals a clear preference for ESM2-t33, which employs 650 million parameters to achieve optimal model performance with

Table 4. Influence of folding strategies (AlphaFold2 and ESMFold) on prediction performance for structure-involved models.

	DTm			DDG			ProteinGym-interaction			ProteinGym-catalysis		
	AlphaFold2	ESMFold	diff ↓	AlphaFold2	ESMFold	diff ↓	AlphaFold2	ESMFold	diff ↓	AlphaFold2	ESMFold	diff ↓
avg. pLDDT	90.86	83.22	-	95.19	86.03	-	82.86	65.69	-	85.80	73.45	-
ESM-if1	0.395	0.371	0.024	0.457	0.488	-0.031	0.351	0.259	0.092	0.386	0.368	0.018
MIF-ST	0.400	0.378	0.022	0.438	0.423	-0.015	0.390	0.327	0.063	0.408	0.388	0.020
k30_h1280	0.384	0.370	0.014	0.396	0.390	**0.006**	0.398	0.373	**0.025**	0.443	0.439	**0.004**
k30_h768	0.359	0.356	**0.003**	0.378	0.366	0.012	0.400	0.374	**0.026**	0.442	0.436	**0.006**
k30_h512	0.413	0.399	0.014	0.408	0.394	0.014	0.400	0.372	**0.028**	0.447	0.442	**0.005**
k20_h1280	0.415	0.391	0.024	0.429	0.410	0.019	0.399	0.365	0.034	0.446	0.441	**0.005**
k20_h768	0.415	0.403	**0.012**	0.419	0.397	0.022	0.401	0.370	0.031	0.449	0.442	0.007
k20_h512	0.419	0.395	0.024	0.441	0.432	**0.009**	0.406	0.371	0.035	0.449	0.439	0.010
k10_h1280	0.406	0.391	0.015	0.426	0.411	0.015	0.396	0.365	0.031	0.440	0.434	**0.006**
k10_h768	0.400	0.391	**0.009**	0.414	0.400	0.014	0.379	0.349	0.030	0.431	0.421	0.010
k10_h512	0.383	0.364	0.019	0.424	0.414	**0.010**	0.389	0.364	**0.025**	0.440	0.432	0.008

† The top three are highlighted by **First**, **Second**, **Third**.

396 the best stability. Notably, a higher dimension and richer semantic expression do not always yield
397 better performance. A performance degradation is observed at ESM2 with 3 billion parameters.

AA Perturbation Strategies

ProtSSN utilizes noise sampling at each epoch on the node attributes to emulate random muta-
tions in nature. This introduction of noise directly affects the node attribute input to the graphs.
Alongside the 'mutate-then-recode' method we implemented in the main algorithm, we examined
four additional strategies to perturb the input data during training. The construction of these ad-
ditional strategies is detailed below, and their corresponding Spearman's ρ on **ProteinGym v0** is
in Fig. 4(e).

Global Average

Suppose the encoded sequential representation of a node is predominantly determined by its
residue. In essence, the protein sequence encoder will return similar embeddings for nodes of the
same residue, albeit at different positions within a protein. With this premise, the first strategy
replaces the node embedding for perturbed nodes with the average representations of the same
residues. For example, when perturbing an AA to glycine, an overall representation of glycine is
assigned by extracting and average-pooling all glycine representations from the input sequence.

Sliding Window

The presumption in the previous method neither aligns with the algorithmic design nor biological
heuristics. Self-attention discerns the interaction of the central token with its neighbors across
the entire document (protein). The representation of a residue is influenced by both its neighbors'
residues and locations. Thus, averaging embeddings of residues from varying positions is likely
to forfeit positional information of the modified residue. For this purpose, we consider a sliding
window of size 3 along the protein sequence.

Gaussian Noise

420 The third option regards node embeddings of AA as hidden vectors and imposes white noise on
421 the vector values. We define the mean= 0 and variance= 0.5 on the noise, making the revised node
422 representation $\tilde{v} = v + \mathcal{N}(0, 0.5)$.

Mask

424 Finally, we employ the masking technique prevalent in masked language modeling and substitute
425 the perturbed residue token with a special `<mask>` token. The prefix language model will interpret
426 it as a novel token and employ self-attention mechanisms to assign a new representation to it.

Table 5. Variant Effect Prediction on **ProteinGym v0** with both zero-shot and few-shot methods. Results are retrieved from (*Notin et al., 2022a*).

Model	Type	# Params (million)	ρ (by mutation depth) ↑			ρ (by MSA depth) ↑			ρ (by taxon) ↑			
			Single	Double	All	Low	Medium	High	Prokaryote	Human	Eukaryote	Virus
few-shot methods												
SiteIndep	single	-	0.378	0.322	0.378	0.431	0.375	0.342	0.343	0.375	0.401	0.406
EVmutation	single	-	0.423	0.401	0.423	0.406	0.403	0.484	0.499	0.396	0.429	0.381
Wavenet	single	-	0.399	0.344	0.400	0.286	0.404	0.489	0.492	0.373	0.442	0.321
GEMME	single	-	0.460	0.397	0.463	0.444	0.446	0.520	0.505	0.436	0.479	0.451
DeepSequence	single	-	0.411	0.358	0.416	0.386	0.391	0.505	0.497	0.396	0.461	0.332
	ensemble	-	0.433	0.394	0.435	0.386	0.411	0.534	0.522	0.405	0.480	0.361
EVE	single	-	0.451	0.406	0.452	0.417	0.434	0.525	0.518	0.411	0.469	0.436
	ensemble	-	0.459	0.409	0.459	0.424	0.441	0.532	0.526	0.419	0.481	0.437
MSA-Transfomer	single	100	0.405	0.358	0.426	0.372	0.415	0.500	0.506	0.387	0.468	0.379
	ensemble	500	0.440	0.374	0.440	0.387	0.428	0.513	0.517	0.398	0.467	0.406
Tranception-R	single	700	0.450	0.427	0.453	0.442	0.438	0.500	0.495	0.424	0.485	0.434
TranceptEVE	single	700	0.481	0.445	0.481	0.454	0.465	0.542	0.539	0.447	0.498	0.461
zero-shot methods												
RITA	ensemble	2,210	0.393	0.236	0.399	0.350	0.414	0.407	0.391	0.391	0.405	0.417
ESM-1v	ensemble	3,250	0.416	0.309	0.417	0.390	0.378	0.536	0.521	0.439	0.423	0.268
ProGen2	ensemble	10,779	0.421	0.312	0.423	0.384	0.421	0.467	0.497	0.412	0.459	0.373
ProtTrans	ensemble	6,840	0.417	0.360	0.413	0.372	0.395	0.492	0.498	0.419	0.400	0.322
ESM2	ensemble	18,843	0.415	0.316	0.413	0.391	0.381	0.509	0.508	0.456	0.461	0.213
SaProt	ensemble	1,285	0.447	0.368	0.450	0.456	0.410	0.544	0.534	0.464	0.460	0.334
ProtSSN	ensemble	1,476	0.433	0.381	0.433	0.406	0.402	0.532	0.530	0.436	0.491	0.290

† The top three are highlighted by **First**, **Second**, **Third**.

We utilize the same hyperparameter settings as that of BERT (*Devlin et al., 2018*) and choose 15% of tokens per iteration as potentially influenced subjects. Specifically, 80% of these subjects are replaced with `<mask>`, 10% of them are replaced randomly (to other residues), and the remaining 10% stay unchanged.

Folding Methods

The analysis of protein structure through topological embeddings poses challenges due to the inherent difficulty in obtaining accurate structural observations through experimental techniques such as NMR (*Wüthrich, 1990*) and Cryo-EM (*Elmlund et al., 2017*). As a substitution, we use *in silico* folding models such as AlphaFold2 (*Jumper et al., 2021*) and ESMFold (*Lin et al., 2023*). Although these folding methods may introduce additional errors due to the inherent uncertainty or inaccuracy in structural predictions, we investigate the robustness of our model in the face of potential inaccuracies introduced by these folding strategies.

Table 4 examines the impact of different folding strategies on the performance of DMS predictions for ESM-if1, MIF-ST, and ProtSSN. Although the performance based on ESMFold-derived protein structures generally lags behind structures folded by AlphaFold2, the minimal difference between the two strategies across all four benchmarks validates the robustness of our ProtSSN in response to variations in input protein structures. We deliberately divide the assays in **ProteinGym v0** (*Notin et al., 2022a*) into two groups of interaction (*e.g.*, binding and stability) and catalysis (*e.g.*, activity), as the former is believed more sensitive to the structure of the protein (*Robertson and Murphy, 1997*).

ProtSSN emerges as the most robust method, maintaining consistent performance across different folding strategies, which underscores the importance of our model's resilience to variations in input protein structures. The reported performance difference for both ESM-if1 and MIF-ST is 3 − 5 times higher than that of ProtSSN. The inconsistency between the optimal results for **DDG** and the scores reported in Table 3 comes from the utilization of crystal structures in the main results. Another noteworthy observation pertains to the performance of ESM-if1 and MIF-ST on **DDG**. In this case, predictions based on ESMFold surpass those based on AlphaFold2, even outperforming

Table 6. Average Spearman's ρ correlation of variant effect prediction on **DTm** and **DDG** for zero-shot methods with model ensemble. The values within () indicate the standard deviation of bootstrapping.

Model	# Params (million)	DTm	DDG
RITA	2,210	$0.195_{(0.045)}$	$0.255_{(0.061)}$
ESM-1v	3,250	$0.300_{(0.036)}$	$0.310_{(0.054)}$
Tranception	1,085	$0.202_{(0.039)}$	$0.277_{(0.062)}$
ProGen2	10,779	$0.293_{(0.042)}$	$0.282_{(0.063)}$
ProtTrans	6,840	$0.323_{(0.039)}$	$0.389_{(0.059)}$
ESM2	18,843	$0.346_{(0.035)}$	$0.383_{(0.055)}$
SaProt	1,285	$0.392_{(0.040)}$	$0.415_{(0.061)}$
ProtSSN	1,476	$\mathbf{0.425}_{(0.033)}$	$\mathbf{0.440}_{(0.057)}$

predictions derived from crystal structures. However, the superior performance of these methods with ESMFold hinges on inaccurate protein structures, rendering them less reliable.

Performance Enhancement with MSA and Ensemble

We extend the evaluation on **ProteinGym v0** to include a comparison of our zero-shot ProtSSN with few-shot learning methods that leverage MSA information of proteins (*Meier et al., 2021*). The details are reported in Table 5, where the performance of baseline methods are retrieved from https://github.com/OATML-Markslab/ProteinGym. For ProtSSN, we employ an ensemble of nine models with varying sizes of kNN graphs ($k \in \{10, 20, 30\}$) and EGNN hidden neurons ($\{512, 768, 1280\}$), as discussed previously. The MSA depth reflects the number of MSA sequences that can be found for the protein, which influences the quality of MSA-based methods.

ProtSSN demonstrates superior performance among non-MSA zero-shot methods in predicting both single-site and multi-site mutants, underscoring its pivotal role in guiding protein engineering towards deep mutation. Furthermore, ProtSSN outperforms MSA-based methods across taxa, except for viruses, where precise identification of conserved sites is crucial for positive mutations, especially in spike proteins (*Katoh and Standley, 2021*; *Mercurio et al., 2021*). In essence, ProtSSN provides an efficient and effective solution for variant effects prediction when compared to both non-MSA and MSA-based methods. Note that although MSA-based methods generally consume fewer trainable parameters than non-MSA methods, they incur significantly higher costs in terms of search time and memory usage. Moreover, the inference performance of MSA-based methods relies heavily on the quality of the input MSA, where the additionally involved variance makes impacts the stability of the model performance.

Discussion and Conclusion

The development of modern computational methodologies for protein engineering is a crucial facet of *in silico* protein design. Effectively assessing the fitness of protein mutants not only supports cost-efficient experimental validations but also guides the modification of proteins toward enhanced or novel functions. Traditionally, computational methods rely on analyzing small sets of labeled data for specific protein assays, such as FLIP (*Dallago et al., 2021*), PEER (*Xu et al., 2022*), and PETA (*Tan et al., 2024b*). More recent work has also focused on examining the relationship between models and supervised fitness prediction (*Li et al., 2024*). However, obtaining experimental data is often infeasible in real-world scenarios, particularly for positive mutants, due to the cost and complexity of protein engineering. This limitation renders supervised learning methods impractical for many applications. As a result, it is crucial to develop solutions that can efficiently suggest site mutations for wet experiments, even when starting from scratch without prior knowl-

edge. Recent deep learning solutions employ a common strategy that involves establishing a hidden protein representation and masking potential mutation sites to recommend plausible amino acids. Previous research has primarily focused on extracting protein representations from either their sequential or structural modalities, with many treating the prediction of mutational effects merely as a secondary task following inverse folding or *de novo* protein design. These approaches often overlook the importance of comprehensive investigation on both global and local perspectives of amino acid interaction that are critical for featuring protein functions. Furthermore, these methods hardly tailored model designs for suggesting mutations, despite the significance of this type of task. In this work, we introduce ProtSSN, a denoising framework that effectively cascades protein sequence and structure embedding for predicting mutational effects. Both the protein language model and equivariant graph neural network are employed to encode the global interaction of amino acids with geometry-aware local enhancements.

On the other hand, existing benchmarks for evaluating computational solutions mostly focus on assessing model generalization on large-scale datasets (e.g., over 2 million mutants in **ProteinGym v1**). However, such high-throughput datasets often lack accurate experimental measurements (*Frazer et al., 2021*), leading to significant noise in the labels. Furthermore, the larger data volumes typically do not include environmental labels for mutants (e.g., temperature, pH), despite the critical importance of these conditions for biologists. In response, we propose **DTm** and **DDG**. These low-throughput datasets, which we have collected, emphasize the consistency of experimental conditions and data accuracy. They are traceable and serve as valuable complements to ProteinGym, providing a more detailed and reliable evaluation of computational models. We have extensively validated the efficacy of ProtSSN across various protein function assays and taxa, including two thermostability datasets prepared by ourselves. Our approach consistently demonstrates substantial promise for protein engineering applications, such as facilitating the design of mutation sequences with enhanced interaction and enzymatic activity.

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