Title: **Evolutionary change is remarkably time-independent across scales**

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Abstract Apparent time-scaling of evolutionary rates presents a potential dilemma. Rates of molecular, phenotypic, and lineage diversification typically scale negatively with time interval, raising questions about the ecological and evolutionary processes driving this pattern. Here we explore the fact that much apparent temporal scaling is an inevitable outcome of plotting a ratio against its denominator. We show that this effect readily explains the qualitative existence of a negative scaling relationship across different types of evolutionary rates. Highly unlikely relationships between timescale and accumulated evolutionary change are required to produce anything other than negative rate-time relationships. Empirical rate-time scaling relationships reflect unscaled magnitudes of evolution that are either unrelated to time and/or vary in their relationship with time. Over 99% of variation in rate-time relationships across five datasets can be explained by time interval alone, and simulations suggest a range of rate-time scaling exponents can be generated by similar evolutionary processes. These results raise challenges in the interpretation of evolutionary rate-time relationships, and highlight segmented regression as one useful approach to understanding temporal variation in evolution. Time-independence of evolutionary change raises new questions about the factors that generate temporal consistency in evolution.

Main Text: Evolutionary rates vary with the time interval over which they are measured. A seemingly general pattern with faster evolutionary rate over short timescales, and slower rates over longer timescales has been recognized for decades (Gingerich 1983, 1993; Hendry & Kinnison 1999; Gingerich 2001; Harmon *et al.* 2021). Such apparent time-dependence has subsequently been documented consistently for nearly every possible measure of evolutionary rate (Rolland *et al.* 2023), including rates of morphological and molecular evolution (Ho *et al.* 2011), and rates of lineage formation on phylogenies and in the fossil record (Figure 1). Negative rate-time scaling relationships were initially proposed as an artifact that needed to be taken into account, because evolutionary rates over different time intervals were not directly comparable (Gingerich 1983). Yet these negative relationships between evolutionary rate and time continue to generate discussions and stimulate new hypotheses about the possible shared features of the underlying evolutionary processes and ecological environment that could explain such general time-scaling (Henao Diaz *et al.* 2019; Rolland *et al.* 2023). Recent technical and statistical explanations to these apparent negative rate-time scaling relationships focus on sampling biases (Louca *et al.* 2022), such as a the "push of the past" (Rolland *et al.* 2023) model mis-specification (Harmon *et al.* 2021), and measurement error (O'Meara & Beaulieu 2024). This puzzling and general phenomenon of apparent widespread negative rate-time scaling relationships has been recently highlighted as a major unsolved challenge in evolutionary biology (Henao Diaz *et al.* 2019; Harmon *et al.* 2021; Rolland *et al.* 2023). The renewed interest in such apparent time-dependence of evolutionary rates has rekindled long-standing ideas and hypotheses about fundamental disparities between micro- and macroevolution (Eldredge & Gould 1972; Gould & Eldredge 1977; Gould 1984; Gould & Eldredge 1993; Hansen & Houle 2004).

We here focus on elaborating the simplest explanation for such a pattern: the inevitable

negative correlation generated by plotting a ratio against its own denominator (Pearson 1897).

This is a well-known statistical issue across a range of scientific fields (Atchley *et al.* 1976;

Gingerich 1983; Prarie & Bird 1989; Jackson & Somers 1991; Arnold 2014), including research

on evolutionary rates (e.g., see Box 1 in Harmon *et al.* 2021). By revisiting the functional

dependence of rates and time, analyzing large existing datasets and using new simulations, we

show that a negative relationship between evolutionary rate and time is nearly inevitable,

regardless of the underlying evolutionary process. We show that the key feature underlying

negative rate-time relationships in empirical data is a weak, null, or variable relationship between

magnitude of evolution and time. While some of these points have been well-appreciated in the

past, our revisit to this phenomenon emphasizes that rate-time plots will nearly always appear to

indicate qualitative consistency of the evolutionary process, in the form of negative scaling

relationships, across types of evolutionary change.   Our analysis also highlights new challenges

in interpreting quantitative estimates of rate-time scaling patterns. We highlight the use of

segmented regression techniques that can identify significant breakpoints in evolutionary time

series

The negative rate-time association is nearly inevitable

Estimates of evolutionary rate can be modelled as a function of evolutionary change scaled by

time:

$$y = d/t \tag{1}$$

where y is the rate-measure, d is some measure of evolutionary change (e.g., change in

population mean phenotype, base pair substitutions, log change in number of species in a clade)

and *t* is some measure of time interval over which change was observed or inferred (e.g.

generations, or years). Some classical estimates of evolutionary rate are calculated directly by

dividing phenotypic change with time, the latter typically measured in generations or years. For

example, Darwins (Haldane 1949) $\left(\frac{\ln\,(\bar{z}_1-\bar{z}_2)}{\Delta t * 10^6}\right)$ and Haldanes (Gingerich 1993)

$\left(\frac{(\bar{z}_1-\bar{z}_2)}{\Delta t}, \text{were z is in units of phenotypic standard deviations}\right)$ have been used to describe

morphological rate, and other types of rate estimators measure per-capita origination rate of

fossil lineages (Foote 2000) and phylogenetic net diversification rate (Magallon & Sanderson

2001). Other estimates are obtained from more sophisticated statistical models of evolution (Nee

et al. 1994; FitzJohn 2012; Rabosky *et al.* 2014). Regardless, all evolutionary rate measures are,

per definition, scaled by time (e.g., waiting times between observed branching events on a

phylogeny are a direct component of the likelihood in maximum likelihood models of birth-death

diversification (Nee *et al.* 1994)).

The inevitable mathematical dependence between rate and time is an obvious challenge

in interpreting the time-dependence of evolutionary rate (Gingerich 1983). Even a random

association between evolutionary change and time will result in a strong negative scaling

relationship between rate and time (Kenney 1982). The strength of this negative relationship will

inevitably increase when a greater range of timescales is sampled (Pearson 1897). The problem

of interpreting such inevitable negative relationships between a rate and time interval have been

discussed in several fields outside evolutionary biology, including geology (Schlager *et al.* 1998)

and paleontology (Sheets & Mitchell 2001). The problem has also been raised in evolutionary

biology, both in the context of rates of morphological evolution (Gingerich 1983; Hendry &

Kinnison 1999; Roopnarine 2003; Estes & Arnold 2007; Uyeda *et al.* 2011; Arnold 2014) and

lineage diversification (Rabosky 2009; Wiens 2011; Rabosky *et al.* 2012).   Here, we revisit and

elaborate on the issues with interpreting rates as a function of time.

It is useful to ask, under what scenarios do we expect null or positive relationships

between rate and time? Consider rate as a function of time,

$$y = f(t) \qquad (2)$$

154   Where y is evolutionary rate (as in eqn 1). We also consider the amount, or magnitude, of

155   accumulated evolution (rate numerator) as a function of time,

$$d = g(t) \qquad (3)$$

where d is the accumulated evolutionary change. This could be the change in trait means

between allochronic or synchronic populations, difference in log number of lineages between

two sampling points in time (e.g., the stem age of a clade and present), or any other measure of

evolutionary change. Rates, $y = d/t$, will be constant over time when d scales linearly with t,

i.e. $g'(t)$ is a positive constant over the timescale in question, with prime denoting the first

derivative. Rates will increase with time, i.e. $f'(t) > 0$ when $g''(t) > 0$; that is, rates increase

over time when the amount of evolutionary change is an accelerating function of time.

Noteworthy is that under a null relationship between d and t, such that $g'(t) = 0$, the

logarithmic regression of rate versus time ($\log(y) \sim \mu + \beta^*\log(t)$) will yield a negative slope

estimate of $\beta = -1$ (Gingerich 1983). This can be seen most easily by expressing equation 3 as a

power function, e.g., $d = t^0$, in which case we can describe the regression of $\log(y) \sim \beta^*\log(t)$

as $\log(t^0/t) \sim \beta^*\log(t)$; solving for $\beta = \log(t^{-1})/\log(t) = -1$.

This negative slope estimate provides one cutoff of interest in assessing rate-time scaling

relationships: log-log regressions of rate vs time that are shallower than or not significantly

different from -1 are consistent with either a null relationship between evolutionary change and time (time independence) or an increasing relationship between accumulated change and time, respectively. For some cases, such as morphological evolution, it is possible to develop predictions for rate-time scaling parameters under various models of evolutionary change(Holstad *et al.* 2024).

The relationships between equations 1-3 are illustrated in Figure 2, which shows the relationship between rate and time. Figure 2A illustrate differing relationships between rate numerator and time illustrated in Figure 2B for a range of power functions. There are few theoretical models that predict the type of accelerating relationship between magnitude of evolution and time that are needed to produce a positive relationship between evolutionary rate and time. For example, neutral and adaptive models of phenotypic and molecular evolution predict either no relationship with time or linear accumulation (constant change) with time (Morgan 1998). Similarly, birth-death models of lineage accumulation also predict either a linear or a decelerating accumulation of log lineage number through time under most conditions. Even models of time-dependent lineage diversification make no prediction about accelerating log lineage number versus interval time across a sample of clades. Moreover, lineage-through-time (LLT) plots for single clades diversifying under such a process can produce complex lineage through time plots (Paradis 2015) that are consistent with several different underlying diversification processes (Louca & Pennell 2020).

Some biological and ecological scenarios could potentially lead to accelerating change with time, and thus generate positive relationships between evolutionary rates and time (Figure 2). Such scenarios include "diversity begets diversity" models of lineage diversification (Nee *et al.* 1994; Emerson & Kolm 2005), evolution by positive frequency-dependent selection (Chouteau *et al.* 2016), runaway sexual selection driven by female choice (Fisher 1930; Lande

1981; Kirkpatrick 1982), "tipping points" in the evolution of reproductive isolation (Nosil *et al.*

2017) and populations crossing critical thresholds followed by phase transitions between

alternative stable states (Scheffer 2009). Tracking of a constant-rate moving optimum can

generate short-term positive rate-time scaling until a population reaches its stable expected

lag(Lynch & Lande 1993; Bürger & Lynch 1995) (elaborated below). How common such

ecological and evolutionary scenarios are in nature is an open empirical question. However,

given the transient nature of such rapid and self-reinforcing evolutionary processes driven by

positive feedbacks (Lande 1981; Kirkpatrick 1982), we suspect that positive time-rate scenarios

are unlikely to be sustained over longer macroevolutionary time scales and should quickly reach

stable equilibria and largely be transient. Thus, such rapid and self-reinforcing evolutionary

processes are unlikely to proceed unchecked over millennia (Scheffer 2009), as would be

required to generate positive rate-time relationships in empirical data such as that shown in

Figure 1.

Finally, we can further decompose the covariance between rate and time, focusing on the

log-scaled case, where

$$Cov\left[log\left(\frac{d}{t}\right), \log(t)\right] = Cov[log(d) - \log(t), \log(t)]$$

211    $$= Cov[log(d), \log(t)] - Var[log(t)]$$

212   Which shows that the relationship between rate and time is governed both by the variance in time

213   interval as well as the relationship between accumulated change (*d*) and time.

Data and simulation reveal persistence of inevitable scaling relationships

Here we revisit five published empirical datasets of evolutionary rate. Reanalysis of these empirical datasets of evolutionary rate-time associations reveals little consistent patterns in the relationship between amount of evolutionary change and time, despite a pervasive negative relationship between rate and time, largely consistent with original conclusions of each individual study. For our first example, vertebrate body size evolution (Figure 1A, E), past work (Estes & Arnold 2007; Uyeda *et al.* 2011; Arnold 2014) has shown that body size changes are largely unrelated to time, and in time-series of extant populations found no detectable change (Sanderson *et al.* 2021). Although a log-log regression of rate vs time yields a slope that is nominally steeper than -1 (β = -1.019, 95%CI -1.031, -1.007), which suggests no accumulation of change with interval time, there is a breakpoint in the relationship between morphological change and time ($F_{2, 5388}$ = 207.2, P < 2.2 x 10^{-6}, breakpoint = -2.63 log MY, SE = 0.147). The result is an estimated weak negative relationship between time and evolutionary change, followed by an increasing slope after the breakpoint (Fig. 1A, F; or shallower negative slope on the log scale, Figure 1A inset panel), identical to that found by (Uyeda *et al.* 2011). Thus, for body size evolution, amount of change is largely unrelated to time interval except over the deepest periods of evolutionary time (Uyeda *et al.* 2011).

Similar results are seen in patterns of lineage accumulation in the fossil record (Figure 1B, G), where a strong negative rate-time relationship (found by(Henao Diaz *et al.* 2019) and replotted here) reflects a weak and variable relationship between evolutionary change and time (segmented regression $F_{2, 86}$ = 3.199, P = 0.046, breakpoint = -109 MY, SE = 33.13). However, this segmented regression model was not a significantly better fit than a model with only an intercept; $F_{3, 86}$ = 2.6, P = 0.057. Consistent with this finding, a log-log regression between rate

and time yields a slope that is significantly shallower than -1 (β = -0.24, 95%CI -0.36, -0.11) and

no significant evidence for a breakpoint ($F_{2, 75}$ = 1.71, P = 0.18), indicating that there is some

accumulation of diversity with interval time.

On phylogenetic trees (Figure 1C, D, G, H), there is also a consistent striking negative

relationships between rate and time (as found by the original studies; Scholl & Wiens 2016;

Henao Diaz *et al.* 2019) that corresponds to underlying variable association between diversity

and time (Rabosky *et al.* 2012; but see Scholl & Wiens 2016). We recover a weak positive linear

relationship between diversity and time in one dataset ($F_{1, 112}$ = 14.17, P = 0.000267; Figure 1H)

corresponding to a log-log regression that is significantly shallower than -1 (β = -0.53, 95%CI -

0.68, -.39), indicating some accumulation of diversity with time, and a segmented linear

relationship in another dataset (segmented regression $F_{2, 430}$ = 12.67, P = 4.474 x10^{-6}, breakpoint

= 4.6 log MY, SE = 0.108) corresponding to a log-log regression of rate and time with a slope

that is not significantly different from -1 (β = -1.04, 95%CI -1.1, -0.98), indicating the

accumulated diversity and interval time are decoupled.

Interestingly, we even recover a nonlinear negative relationship between evolutionary

rate and time when examining phenotypic change that occurred within a timeframe less than the

average generation time of the study organism (in this case, primarily long-lived fish; Figure 1E).

This within-generation dataset had a log-log regression of rate and time with a slope that was not

significantly different from -1 (β = -0.83, 95%CI -1.08, -0.58), indicating that there is no

accumulation of change with interval time for intervals less than one generation, as we may

expect. This final example demonstrates the appearance of a rate-time scaling relationship for a

case that obviously defies evolutionary explanation based on between-generation change. This

conclusion is further strengthened by the fact that the slope estimate does not significantly differ

from the expectation under a random relationship between rate numerator and time. That is,

scaling phenotypic change by time in order to calculate rate generates a non-linear negative

relationship with time even for this within-generation change (Figure 1E, J), that is likely to

reflect phenotypic plasticity, culling, or other non-evolutionary within-generational

environmental effects.

We can then decompose the covariance between rate and time for each of these datasets

into its components associated with variation in time and covariance between accumulated

change and time, as in equation 4. A caveat in this exercise is that not all of the rate estimates

are calculated directly as in equation 1, for example phylogenetic lineage diversification rates

in(Henao Diaz *et al.* 2019), and so we do not expect all of the variance in rate-time relationships

to be explained by these two components. Nonetheless, this analysis reveals that 99.7% (54%

with morphology data dropped) of the variance in rate-time relationships can be explained by

variance in time alone ($F_{1,3}$ = 916, P = 7.9x10^{-5}, Figure 3A), while change-time covariance alone

explains only 14.6 % (25% with morphology data dropped) of the variance in rate-time

relationships ($F_{1,3}$ = 0.51, P = 0.52, Figure 3B). Placing both predictors in a multiple regression

reveals support for variance in time (t = -25.97, P = 0.0015, df = 2), but not covariance between

change and time (t = 0.764, P = 0.52, df = 2), as a significant predictor of rate-time relationships.

In summary: the striking negative rate-time relationship shared by four independent

evolutionary datasets and one non-evolutionary (within generation) dataset reflects, primarily, a

lack of strong or consistent association between the amount of evolutionary change (rate

numerator) and the timescale over which this change took place (Figure 1 F-J). These results

largely recapitulate the findings of original studies from which these datasets were obtained,

although we have shown that a decoupling of amount of evolution and timescale of measurement

is likely a general feature across a range of evolutionary datasets, from morphological change to lineage diversification, that together describe the pace of life.

Simulations of classical constant-rate evolutionary models reveal that negative rate-time associations readily emerge from these existing models. Phenotypic evolution by random genetic drift results in a Brownian motion process wherein phenotypic variance across lineages increases linearly with time (Figure 4A), and evolutionary rate is time-independent when calculated for an entire clade (4E inset panel). Even this simple constant rate model results in a negative scaling relationship between lineage-specific estimates of evolutionary rate and time (Figure 4E), resulting in a scaling exponent of $-$ ½ in a log-log regression of rate versus time(Hansen 2024).

Lineage specific rates are even more strongly associated with time under adaptive model of natural selection towards a stationary optimum (an Ornstein-Uhlenbeck process), where a null relationship between time and divergence (Figure 4B) generates a strong negative relationship between per-lineage rate and time (Figure 4F) with a log-log slope of -1 over long timescales (Hansen 2024), reminiscent of empirical data from vertebrate body size evolution (Figure 1). However, we note that a stationary OU model readily produces negative rate-time scaling exponents that deviate from -1 when sampling lineages evolving under different values of genetic variance and strength of stabilizing selection (Figure 5). Adding any movement of the optimum in an OU process produces dramatic shifts in the form of rate time scaling, yet also indicates that a range of models incorporating stabilizing selection readily produce scaling relationships similar or identical to that expected under pure genetic drift (Figure 5).

Finally, the simplest model of lineage accumulation, a constant-rate pure-birth process,

also leads to these types of associations. The log number of lineages accumulates approximately

linearly through time in a pure-birth process, as seen when sampling pure-birth phylogenies

differing in age (Figure 4C, 4D). Yet, pure-birth estimators of diversification rate from these

phylogenies (Kendall-Moran Yule rates, Figure 4G, S1) as well as maximum likelihood

estimates of net diversification from a birth-death diversification model (Figure S2) nonetheless

show a negative scaling relationship with time. In principle Yule rates do not inherently show

time dependence when estimates of zero rates, which rarely result in phylogenies of more than a

single taxon, are included. For example this can be shown by the crown-age estimates using

clade age – time data (Magellon-Sanderson rate estimates, Figure 4H). However, even in this

case non-zero rate estimates show negative time scaling (Figure 4H). Similarly, sampling

directly from the theoretical distribution of pure-birth richness and age yields zero-rate estimates

that can cancel out non-zero rates for young clades (O'Meara & Beaulieu 2024), we note that

these zero rates are largely unobservable in actual data. Our simulations and others (O'Meara &

Beaulieu 2024) show that non-zero rates show negative time-scaling even under a constant-rate

pure-birth diversification process. This negative scaling relationships is driven largely by the

inclusion of high evolutionary rates estimated over short timescales (Figure 4G), yet the scaling

pattern can sometimes remain even when focusing only on larger and older clades (Figure S1).

This illustrates the inherent problems of interpreting evolutionary change scaled by time.

Moreover, we recover the same general pattern when simulating phylogenies of varying age

under an accelerating time-dependent diversification process (Figure S3).   These simulation

results are not in any way meant as evaluations of these models, rather a demonstration that

constant rate processes readily and almost inevitably will produce negative rate-time scaling

relationships at least in some circumstances.

Discussion

Here we have explored the problem of why all evolutionary rates appear to scale

negatively with time, and what information may be gleaned from these rate-time relationships.

First, it is readily apparent there will only exist a limited range of relationships between amount

of evolution and time that generate anything other than negative rate-time relationships. Second,

revisiting several independent datasets of evolutionary rates demonstrate that existing, widely-

documented negative rate-time scaling relationships clearly suggest weak and inconsistent

relationships between the amount of evolution and timescale of measurement, with no evidence

for a systematic slowdown in accumulated evolutionary change or time-dependency in

evolutionary change. Our analysis of these datasets reveals that variation in rate-time scaling

pattern is primarily driven by variation in timespan of the dataset rather than patterns of

accumulated evolutionary change. Finally, simulation of some of the most common process-

based models of constant-rate evolutionary change reveals that all can readily generate a range of

negative rate-time scaling relationships. Although many of these points have been discussed in

regards to specific datasets, our results unequivocally demonstrate the challenge in interpreting

widespread (Gingerich 1983; Henao Diaz *et al.* 2019; Harmon *et al.* 2021; Rolland *et al.* 2023)

negative rate-time scaling relationships. Our results have revealed that a negative rate-time

relationship is nearly inevitable under a wide range of biological scenarios and over different

temporal scales, and moreover suggest potential limitation in the unique information revealed by

quantitative estimates of negative rate-time scaling relationships.

That evolutionary rates scale negatively with the timeframe over which they are

measured is unsurprising given the inevitable dependence between rate and time, a point that has

been widely acknowledged (Gingerich 1983; Gould 1984; Hendry & Kinnison 1999; Harmon *et al.* 2021). Negative scaling relationships are therefore expected under a wide range of relationships between evolutionary change and time, in spite of fundamentally different underlying evolutionary processes behind the patterns (Figure 2). The fact that the scaling pattern is observed consistently across disparate types of data from different sources, for rates estimated in very different ways, and even within generations, strongly suggest that these negative relationships are unlikely to reflect a causal biological process (Harmon *et al.* 2021). As Gingerich (Gingerich 1983) emphasized, this suggests that the negative scaling relationship that is generated by plotting a rate against time interval should perhaps be accounted for before rate variation across time can be meaningfully compared or understood.

Yet, there is also widespread interest in understanding the extent to which evolutionary processes may contribute to such a pattern of rate-time scaling (Kinnison & Hendry 2001; Ho *et al.* 2011; Henao Diaz *et al.* 2019; Harmon *et al.* 2021; Louca *et al.* 2022; Rolland *et al.* 2023), and so there is justified interest in understanding the drivers of rate-time scaling relationships beyond the inevitable qualitative expectation of a negative relationship (Harmon *et al.* 2021). For example, analyses of rate-time relationships can provide new insights when coupled with explicit null hypothesis tests against scaling parameters expected under various evolutionary process models (as can be done for the case of morphological evolution; Hansen 2024; Holstad *et al.* 2024). It might also be possible to construct meaningful null expectations for other types of rate-time scaling patterns, such as lineage diversification. For example, in their assessment of negative scaling of diversification rates, Henao Diaz et al.(Henao Diaz *et al.* 2019) constructed a null expectation by simulating birth-death trees for the same age ranges as their empirical set of trees, under the mean values of birth and death rate observed for the oldest groups in the study. While such an approach is useful in identifying cases of negative rate-time scaling beyond what

may be an inevitable outcome from our imperfect statistical models, for many types of rate

estimate we lack the quantitative rate scaling predictions (such as those available for

morphological evolution). One point of our paper is that, without some sort of quantitative

expectation for a rate scaling relationship, the existence of a negative relationship between

empirical rates and time is not very informative.

As a counterpoint to the above, however, in some cases it may be difficult to reconcile

quantitative rate-time scaling patterns with specific evolutionary process models, especially in

large datasets of evolutionary rate spanning disparate lineages. For example, although a

stationary OU model can generate a -1 scaling relationship of rate with time (Hansen 2024), this

is only strictly true over moderate timescales when selection is strong and genetic variance is

moderate to high. Similarly, evolution by Brownian motion produces a scaling relationship of -

1/2, but so too can a random walk of the optimum under stabilizing selection (at least under some

conditions), a process which itself is not strictly Brownian unless all phenotypic variance has an

additive genetic basis.   Thus, while dramatic shifts in rate-time scaling relationships certainly

imply shifts in the mode of evolution (Hansen 2024), it seems likely that similar rate-time scaling

relationships may be generated by many disparate processes.

Relationships between the magnitude of evolutionary change (e.g., phenotypic change or

the log number of new lineages arising) and time can also be assessed directly, as we have done

here and which has also been done by some other researchers(Uyeda *et al.* 2011; Svensson

2019). One under-used statistical tool is, for example, piece-wise or segmented regression

(Schlager *et al.* 1998; Hendry & Kinnison 1999; Uyeda *et al.* 2011; Clapham & Karr 2012) that

can be used to identify significant breakpoints in evolutionary change across time. Such an

approach avoids the problem of statistical confounders between rate and time interval that was

highlighted by Gingerich (Gingerich 1983), at least when applied to analysis of change-time

relationships, and also allow for the possibility of identifying shifts in the form of rate-time

scaling relationships(Hansen 2024). These and related statistical approaches (Uyeda *et al.* 2011)

can be used to identify temporal shifts in the evolutionary process over time. Although analysis

of rate-time and change-time plots present the same total information, uninformed comparisons

of rate-time relationships will readily generate the appearance of shared features of the

evolutionary process. Our analysis revealed that variation in evolutionary rate-time relationships

across datasets revealed little information about variation in accumulated evolutionary change.

A main conclusion from our analysis is that we should generally be surprised when

evolutionary rates *do not* show negative time scaling. However, it is likely that some estimators

of evolutionary rate do not show the types of inevitable time scaling relationships we have

reported; for example, clade-level estimates of Brownian motion rate appear to be less affected.

Indeed, in their review, Harmon et al. (2021) draw a distinction between "summary rates" and

"parameter rates"; the former being descriptive summary statistics, such as haldanes, while the

latter are inferences of instantaneous rate parameters estimated from a process-based model of

evolutionary change, with Brownian motion rate or birth-death lineage diversification rate

presenting two examples. In this distinction, and barring inadequate models or data, parameter

rates from constant rate models should be free from inevitable time-scaling (Hunt 2012; Harmon

et al. 2021). Yet a challenge remains in that many maximum likelihood estimators of parameter

rates are ultimately simple functions of amount of evolution and time, and noteworthy is that

even most summary rates could in fact be considered parameter rates under appropriate

evolutionary models (Harmon *et al.* 2021). The haldane, for example is a parameter rate under

one very simple model of directional trait change (constant directional selection), but note that it

shows positive and negative time scaling in different process-based manifestations of directional

evolution models (see Fig. 5C). Given that we can never know the true process model giving

rise to an evolutionary dataset, and thus our models will always be wrong to some degree(Box

1976), it remains to be seen if there is a general distinction between these categories of rate

estimate in regards to prevalence of time scaling.

Our analyses of rate numerators versus time reveal lack of consistent time-dependency in

accumulated evolutionary change across datasets (Figure 1). This is also reflected in variation in

rate-time scaling slopes, where estimates of rate-time slope range from near unity

(morphological body size evolution, lineage net diversification rate) to modestly negative (fossil

lineage diversification). The former indicates that over some very broad time scales evolutionary

change is largely decoupled from time, while the later case indicates that there is some

meaningful accumulation of evolutionary change with time over some time intervals. We note

that these diverse datasets contain information from many thousands of species of extant and

extinct plants, animals, and prokaryotes, range in time interval from less than one generation to

hundreds of millions of years, and together span the entire history of life. One conclusion is that

the qualitative persistence of negative rate-time relationships do not provide evidence of shared

features of evolution across these disparate data. Existing data (Fig. 1F-J) suggest that

evolutionary change (rate numerator) is remarkably independent of time, across multiple

temporal scales. Such general and widespread time-independence of evolution becomes a new

challenge to explain. Time-independence of phenotypic evolution could be explained by

relatively-stable or slowly moving adaptive zones, within which lineages may evolve

substantially (Simpson 1953; Uyeda *et al.* 2011). For lineage diversification, disparity in

ecological opportunity among diversifying lineages may decouple clade age and species richness

across taxa (Rabosky 2009). We emphasize that while there is little consistent relationships

between amount of evolution and interval time, evolutionary events can still be substantial, as

shown in Figure 1. We also note that timing of key events in the history of life has, of course,

played a major role shaping the origins of diversity (Gould 1989). These include shifts in body

size evolution (Uyeda *et al.* 2011) or rapid jumps in bill evolution in birds (Cooney *et al.* 2017).

There is also evidence of substantial variation in evolutionary change in response to different

selective agents, including human disturbances and harvesting (Sanderson *et al.* 2021), but such

change in response to different environmental agents does not appear to be systematically linked

to time interval over which evolution was recorded.

Our results and other recent findings (Voje 2016; O'Meara & Beaulieu 2024) call into

question the value of the mere existence of rate-time scaling patterns as empirical evidence of a

fundamental disparity between micro and macroevolution, since the qualitative existence of a

negative relationship is readily explained by many constant-rate processes. For example,

consider the widely-appreciated fact that microevolutionary quantitative genetic models of

random genetic drift are inconsistent with the amount of evolutionary change in deep time

(Hansen & Houle 2004; Houle *et al.* 2017); we often find far less evolutionary change in deep

time than expected via drift alone, based on patterns of standing extant genetic variance.

However, it is noteworthy that even if phenotypic divergence in deep time was generally

consistent with drift under observed levels of standing variance, we would still expect to see a

negative scaling relationship between lineage specific rates of evolution and time interval (Figure

3). Our analysis suggests that the decoupling of amount of evolution and time applies not only to

morphological change, but also to lineage accumulation.   For morphological evolution, it is

indeed possible to construct explicit quantitative hypotheses for the form of negative scaling

relationship expected between rate and time (Holstad *et al.* 2024). However, as noted above,

currently we lack quantitative predictions for other forms of rate-scaling relationships.

Time-invariant evolutionary change still poses other challenges for reconciling micro-

and macroevolution (Uyeda *et al.* 2011). Constancy of evolutionary rates, and thus linear

accumulation of change with time, across temporal scales is expected and often observed at the

molecular level (Morgan 1998; Bromham & Penny 2003). It is more difficult to explain relative

time-independence in phenotypic evolution, where trait change is expected to accumulate with

time given strong and variable natural selection (Felsenstein 1988; Kingsolver *et al.* 2001), or

under neutral evolution (Felsenstein 1985; Lynch 1990). However, new empirical findings

indicate that phenotypic evolution over a range of timescales is proportional to standing

phenotypic and genetic variation (Hansen & Pélabon 2021). Such variation-limited evolution, if

general across taxa, could be one possible explanation for time-constancy in evolutionary

change, although it raises additional questions on how and why variational properties could be

conserved through time. Time-dependence, or rather lack thereof, therefore remains a major

open question in evolutionary biology.

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Fig. 1. Evolutionary rate-time relationships reflect null or variable underlying relationships between evolutionary change and time. Panels **A**-**E** show evolutionary rate plotted against the timescale of measurement (Rolland *et al.* 2023), with dashed red lines showing the least squares fit of the function *rate = a**time^b and inset panels showing the linear relationship on a log-log scale. Panels **F**-**J** plot the amount of evolutionary change (i.e., a rate numerator) against time frame for the same datasets, with dashed red lines showing the linear segmented regression, if statistically significant. Panels **A** and **F** show vertebrate body size evolution (Uyeda *et al.* 2011), Panels **B** and **G** show diversification of genera from fossil lineages (plants, mammals, and marine animals)(Henao Diaz *et al.* 2019), Panels **C** and **H** show diversification data estimated from time-calibrated molecular phylogenies (Henao Diaz *et al.* 2019), while Panels **D** and **I** show a larger database of phylogenetic diversification rates (Scholl & Wiens 2016) where rates were inferred directly from age and richness data (Magallon & Sanderson 2001). Panels **E** and **J** show within-generation morphological changes (mainly from fish harvesting). All nonlinear negative relationships plotted in **A**-**E** were statistically significant, whereas relationships in **F**-**J** were

738   variable, with statistically significant breakpoints found for morphology, fossil lineage

739   accumulation, and one estimator of phylogenetic diversification, and a positive linear

740   relationship for another estimator of phylogenetic diversification. No significant relationship was

741   found for the within-generation changes in panel **J**. Sample sizes for each column: **A** N = 5392

records of evolutionary change, **B** N = 90 lineages, **C** N = 114 clades, **D** N = 434 Orders, **E** N = 302 records of within-generation change.

A   **B**

Fig. 2. Extraordinary relationships between the accumulated amount of evolution and time are required to produce positive rate-time relationships. Panel **A** shows the relationship between rate and time for various functions of the rate numerator and time, which are plotted in the same color in Panel **B**. The black line is a reference point, where there is a null relationship between rate and time. Thus, each line in Panel **A** corresponds to a specific relationship between rate numerator and time, plotted in Panel **B**; only cases of an accelerating relationship between amount of evolution and time are expected to produce positive rate-time scaling relationships. We assume for this example a form of the relationship, *amount of evolution = time^b*, where the function was plotted for b ranging from -2 (blue) to 2 (red). Similar general patterns are observed for other functions of change and time. Note that because we are considering these relationships in light of large amalgamations of data from disparate groups (e.g., Figure 1), as opposed to within-lineage time series, negative relationships between amount of evolution and interval time are in principle possible, even if unlikely.

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Fig. 3. Time interval determines rate-time relationships across datasets. The covariance between rate and time
in the five empirical datasets shown in Figure 1 is almost entirely explained by variance in time (Panel **A**).
Covariance between change and time, also expected to be a component of the covariance between rate and time, is
not significantly associated (Panel **B**). Lines and 95% confidence intervals are from linear models fit separately to
each; a multiple regression with both var(time) and cov(change, time) as predictors yielded equivalent conclusions
(see text).
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Fig. 4. Simulations of constant-rate evolutionary models reveal persistence of negative rate-time relationships in resulting data. Panels **A** and **E** show a simulation of phenotypic evolution under random genetic drift in the absence of natural selection, which produces a Brownian motion process (Felsenstein 1988) where variance among lineages accumulates linearly with time (**A**). Although the rate of drift is constant (**E** inset), we will nevertheless obtain a negative scaling relationship between the lineage-specific per-generation rate of evolution (**E**). Panels **B** and **F** show a simulation of phenotypic evolution under drift and stabilizing natural selection, an Ornstein Uhlenbeck process (Lande 1976). This process generates no relationship between time and divergence (**B**), but again a strong negative scaling relationship with per-lineage per-generation evolutionary rate and time and hence a similar negative relationship (**F**). Panels **C** and **G** show a constant-rate pure-birth (i.e., no extinction) lineage diversification process (Yule process), where diversity accumulates approximately linearly with time (**C**). This scenario also produces a similar negative scaling relationship between the Kendall-Moran branch-length based rate estimator and time (**G**). Calculating Yule diversification rate for a different set of trees (**D**) based on the crown-age Magellon and Sanderson estimator yields a similar pattern (**H**), but in this case the inclusion of zero rate estimates (which are unlikely to be sampled in actual trees or in the simulated data in panel C) offsets (green line) the negative relationship between non-zero

810 observable rates and time (red line). The last 15 million years of the simulated data illustrates
811 there is no relationship between rate and time for this time interval (**H** inset).

Fig 5. Heterogeneity in rate-time scaling exponents under different forms of morphological
evolution. Panels **A** and **B** show simulated evolution under drift and stabilizing selection; an OU
process. When there is zero variance in the optimum, this is a stationary OU process generating

a scaling relationship of -1 over this timespan (9000 generations) only when genetic variation is
relatively high (Panel **A**), and selection is strong (a low value of ω and thus a strong curvature of
the fitness surface, (Panel **B**). Any variance in the optimum leads to a dramatic shift in the
scaling relationship. Noteworthy is that a wide range of parameter space, corresponding to
models of pure drift as well as models of pure fluctuating selection, can all produce a range of
similar scaling relationships particularly in the range of 0 to -1/2. For each parameter value in **A**
and **B**, the average scaling slope is shown from 10 simulation runs of 36 lineages each spanning
a time range of 1-9000 generations. Panel **C** shows evolutionary rate versus time for three
forms of directional evolution. In black is the rate estimate versus time for evolutionary change
under the breeders equation, $\Delta\bar{z} = G\beta$. Blue shows the rate estimate for evolution towards an
optimum that shifted 5 phenotypic standard deviations at generation 0, assuming the same form
of stabilizing selection as in Figure 3B, which is high over short timescales but decelerates as the
population adapts. Red shows the relationship for evolution towards an optimum that moves at
contant rate of .1 standard deviations per generation, starting at generation 0 with a population on
the optimum. In this model the accelerating rate-time relationship is due to the lag between
evolutionary rate and rate of peak movement that equilibrates when the population reaches its
equilibrium lag behind the optimum(Lynch & Lande 1993; Bürger & Lynch 1995). All of these
models produce directional evolutionary change, yet only for one specific model, $\Delta\bar{z} = G\beta$,
which is often thought to capture the main features of the two other models of directional
change, do we see a lack of time scaling.

Methods Details

Data. We analyze existing data on rates of vertebrate body size evolution (Uyeda *et al.* 2011),

which consists of data on log-fold change in body size as well as time interval over which this

change occurred. For phylogenetic lineage diversification, we analyze two datasets, one in

which diversification rates were estimated from the branching pattern of species-level

phylogenies (Henao Diaz *et al.* 2019), and another larger dataset (Scholl & Wiens 2016) where

diversification rates were estimated from clade diversity and age information. For fossil data, we

analyze an existing dataset (Henao Diaz *et al.* 2019) of emergence rates of new genera. For each

dataset, we plot the standard measure of rate against the timeframe over which that rate was

measured, fitting exponential linear models by nonlinear least squares (Rolland *et al.* 2023). We

also plot a measure of the rate numerator against time for each of these datasets, and fit

segmented linear regressions to identify significant linear relationships between amount of

evolution and time, as well as any potential shifts in the relationship between evolution and time.

For each dataset, we fit nonlinear models of the form *rate = a*time^b* using nonlinear least

squares (nls()) in R, as well as segmented regression using the segmented package. We compared

models fits of an ordinary linear regression to a model with a single breakpoint, and also when

appropriate to a null model containing only an intercept, using the anova() function in R. Data

presented in Figure 1 were obtained from ref 11 (available at

https://github.com/fhenaod/evol_time_scaling/tree/main/data), ref 29 (Dryad

doi:10.5061/dryad.7d580), ref 46, and ref 47 (database available at:

https://proceeddatabase.weebly.com/).

<u>Simulation</u> We simulated three different constant rate evolutionary process. The aim of our

simulations was not to evaluate the performance of statistical models used to estimate rates.

Rather, our aim was simple to examine scaling patterns observed in the simplest cases of

simulated constant rate evolution. For morphological evolution, we simulated random genetic

drift for 1-1000 generations assuming a heritability of 0.50 and a population size of 100. We also

simulated evolution under genetic drift and stabilizing selection, with the same demographic and

genetic assumptions but assuming weak selection ($\omega^2 = 15$) towards an optimum. Each

simulation was started with the population at its optimum. For morphological evolution, we

plotted rates in units of Haldanes (Gingerich 1993), which was natural as we simulated evolution

on the scale of phenotypic standard deviations. We then repeated our simulations of OU

evolution but exploring a range of parameter values for genetic variance, the strength of selection

(curvature of the fitness surface) and the stability of the optimum. For the later, we sampled

changes in the optimum from a normal distribution centered at zero and exploring different

values of the variance, producing a random walk of the optimum.

For lineage diversification, we simulated pure-birth phylogenies with a constant speciation rate

of 0.15, corresponding to a expected number of 2.3 taxa at timepoint 1 under a continuous time

pure birth process. We simulated pure-birth diversification because, while biologically

unrealistic, it excludes explanations for rate-time scaling patterns that are based on sampling

biases generated by extinction. We also note that although many challenges exist in sampling all

possible trees in a simulation, these are identical to challenges observed in actual data; namely,

inclusion of trees with zero diversification rate. Given the aims of our simulations noted above,

we proceeded by first simulating trees conditioned on number of tips as opposed to clade age,

focusing first on trees with at least 3 tip taxa (conclusions remain unchanged by focusing instead

on trees with 20 or more tips; Figure S3). We then calculated the Kendall-Moran estimator

(Baldwin & Sanderson 1998; Nee 2001) for the Yule process for these trees using the diversitree

package (FitzJohn 2012). We also estimated maximum likelihood birth-death diversification

rates for the same set of trees constraining diversification rates to be positive. Finally, we also

generated trees with ages ranging from 1-35 million years, and plot the maximum likelihood

estimator of the crown-age Yule diversification rate, $[\log(N)\text{-}\log(2)]/t$ (Magallon & Sanderson

2001). Our simulations of phenotypic evolution were performed using nested for() loops in R

and parameterized as described above. Our simulations of constant rate pure birth phylogenetic

diversification was performed using the pbtree() function in the phytools package (Revell 2012).

Our simulations of time-dependent pure birth diversification (Figure S3) were performed using

the TESS package (Hoehna 2013).

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Supplemental Material

Fig. S1. Negative time-scaling of ML lineage diversification rates for trees greater than or

equal to 20 tips. Shown are the scaling relationships for time and diversification estimators for

pure-birth phylogenies of size equal to or greater than N = 20. Panel A shows the net

diversification rate from a ML birth-death model, panel B shows the Yule estimator for the same

set of trees. Other simulation conditions were as in Figure 3C, G.

Fig S2. Birth-death estimator diversification rate for trees plotted in Figure 3D, H. Shown

is the ML estimate of the birth-death diversification rate λ for the same set of trees shown in

Figure 3D, H. Red dashed line shows the least squares fit of the model *rate = a*time^b*.

Fig. S3. Accelerating time-dependent diversification produces negative rate scaling

patterns. Panels show simulations of time-dependent pure birth diversification, repeated for

different timeframes from 1-35 million years under the same time-dependent diversification

model. In each simulation birth rates were assumed to be linearly related to time, $\lambda \sim 0.008*time$,

extinction rate $\mu = 0$. Panel **A** shows log of total diversity plotted against time for each

simulation run. Panel **B** shows the estimate of net speciation rate $\log(N)/t$ as a function of time.

975   Qualitative conclusions remain unchanged under different parameter values, with the one salient

976   feature being that the expected positive rate-time relationship is only recovered in deep time.