Predictive coding in the auditory brainstem

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Abstract.

Predictive coding is an influential concept in sensory and cognitive neuroscience. It is often understood as involving top-down prediction of bottom-up sensory patterns, but the term also applies to feed-forward predictive mechanisms, for example in the retina. Here, I discuss a recent model of low-level predictive processing in the auditory brainstem that is of the feed-forward flavor. Past sensory input from the cochlea is delayed and compared with the current input, with a delay that is tuned with the objective of minimizing prediction error. This operation can be performed uniformly across peripheral channels, or independently within each peripheral channel with parameters local to that channel. The result is a sensory representation that is invariant to a certain class of masking sounds (harmonic, quasi-harmonic, or spectrally sparse), thus contributing to Auditory Scene Analysis. The purpose of this paper is to discuss that model in the light of predictive coding, and examine how it might fit within a wider hierarchical model that supports the perceptual representation of objects and events in the world.

I. Introduction

In predictive coding, an incoming sensory pattern is compared with a predicted pattern, and the outcome of this comparison – the error – serves both to tune the predictive model, and as an input for the next stage of processing. Predictive coding is an influential idea in sensory and cognitive neuroscience (Attneave 1954, Barlow 1961, Srinivasan et al 1982, Rao and Ballard 1999, Clark 2013; Friston 2018). A perfectly predictable pattern carries no information beyond that carried by the predictor (it is redundant). Even if the prediction is imperfect, the error may be less costly to represent and/or easier to process and/or more informative than the raw input. Furthermore, the *parameters* of the predictive model, fit to the stimulus, characterize the stimulus, while the model itself, tuned over a longer time scale, captures the statistics of the sensory environment. Predictive coding is one of a constellation of related ideas, including unconscious inference (Alhacen 1030; Helmholtz 1867), efficient coding (Shannon 1948), epistemological automaton (MacKay 1956), redundancy reduction (Barlow 1961), forward models in motor control (Wolpert et al 1995), reverse hierarchy (Hochstein and Ahissar 2002), efferent copy (Crapse 2008), compression (Schmidhuber, 2009), homeostasis (Friston 2010), Bayesian inference (Aitchison and Lengyel 2017), and so on. In each case, an incoming observation is compared against an internally-generated template, and the mismatch used to adjust the model and remove redundancies.

However, "predictive coding" covers two quite different concepts (Spratling 2015). Given a hierarchy of processing levels, prediction can occur in the *ascending* direction (bottom-up Fig. 1 A) or *descending* direction (Fig. 1 B). An example of the former is center-surround receptive fields in the retina (Srinivasan et al 1982; Hosoya et al 2005), an example of the latter is the recurrent processing proposed for the visual cortex by Rao and Ballard (1999). Top-down prediction is usually assumed to operate within a *hierarchy* of predictive stages ordered from concrete to abstract (Fig. 1C) (e.g., Rao and Ballard 1999; Spratling 2017; Friston 2018), with messages exchanged in both directions. Bottom-up prediction is embodied in the Linear Predictive Coding (LPC) method popular for spectral estimation in speech processing (Markel and Gray 1976), while top-down prediction is related to Bayesian models of perception that combine a prior (parameters of the predictive model) and evidence (the sensory pattern) to infer the causes of sensory input. Both flavors of predictive coding could play a role within the auditory system (Heilbron and Chait 2018).

Fig. 1. Two forms of predictive coding. A: The prediction is produced by a feed-forward model (bot-

tom-up) fed from incoming patterns. B: The prediction is produced by a feed-back model (top-down)

fed from a higher-level representation. C: Hierarchy of predictive coding stages ordered from concrete

to abstract.

Here, I reinterpret a recent model of low-level auditory processing as a form of predictive cod-

ing of the bottom-up flavor: low-level sensory input is compared, at each instant, with a pre-

diction derived from its previous values. I then take advantage of this concrete, bottom-up

model to explore issues that arise when considering the alternative hypothesis of top-down

predictive coding, and discuss how the two approaches might complement each other.

II. The in-channel cancellation model

In-channel cancellation (ICC) is a hypothetical processing mechanism for auditory scene anal-

ysis, to help address a listener's need to handle "cocktail party" situations involving complex

acoustic scenes with multiple concurrent speakers or polyphonic music. In particular, it ac-

counts for our ability to ignore masking sounds that are *harmonic*, *quasi-harmonic,* or *spec-*

trally sparse. The structure and principle of the ICC model is outlined here, more details and

references are provided elsewhere (de Cheveigné 2023a).

Patterns of acoustic vibration are transduced within the cochlea and carried by an array of au-

ditory nerve fibers to the auditory brainstem (Palmer and Rees 2010), an auditory analog of the

retina in terms of level of processing (Sitko and Goodrich 2021). The cochlea implements a

bank of frequency-selective filters, with each channel transduced by one of ~3000 hair cells

into a pattern of spikes carried by a set of ~10 fibers (in human). In the ICC model, spikes

within a channel feed a "neural cancellation filter" that consists of a gating neuron with one

excitatory synapse fed directly, and one inhibitory synapse fed via an adjustable delay of du-

ration τ_k where k is the index of the channel (Fig. 2A, red). The properties of this neuron are

assumed to be such that every direct spike is transmitted *unless* a spike arrives simultaneously

on the delayed pathway, within some short time window of coincidence. The effect is to modify

the statistics of the spike train, depleting it of inter-spike intervals of duration close to τ_k.

The delay parameter τ_k is determined automatically based on a criterion of minimum output,

and it tends to lock on to the period (or pseudo period) of the signal that dominates the channel.

In the presence of a masking sound that is *harmonic*, *quasi-harmonic*, or *spectrally sparse*, the

filter cancels the correlates of that sound, potentially allowing components of a weaker con-

current sound to emerge. An earlier model (harmonic cancellation, HC, de Cheveigné 1993;

2021) used the same delay τ in all channels, making it effective only for the narrower class of

harmonic maskers, whereas the ICC model is more flexible. Together, the HC and ICC models

can account for a range of psychophysical results that involve masking with such sounds (as

reviewed by de Cheveigné 2021, 2023a). The neural circuitry required by these models (fast

excitatory-inhibitory interaction) is similar to that hypothesized by the classic equalization-

cancellation (EC) model of binaural unmasking (Durlach 1963), and the within-channel ver-

sion of that model (Culling and Summerfield 1995), for which physiological support has been

found within the lateral superior olive (LSO) (Biederbeck 2018; Franken et al 2021).

Fig. 2. A: Schematic representation of the cochlea as a bank of bandpass filters followed by a neural

cancellation filter (one channel shown). The neural cancellation filter depletes the auditory-nerve

spike train of intervals equal to τ, thus attenuating correlates of sound components with that period. B:

instantaneous spike probability at the excitatory synapse (top), inhibitory synapse (middle) and at the

output of the gating neuron (bottom) in response to a short periodic stimulus. Only the first period reaches the output.

In a linear approximation, the effects of this neural filter can be described by a delay-and-subtract filter of impulse response $h(t) = \delta(t - \tau_k) - \delta(t)$, where $\delta(t)$ is the Dirac function, followed by a half-wave rectifier that embodies the fact that probability is non-negative (de Cheveigné 1993, 2023a). If the delay equals the period of a sound, the response to that sound is suppressed, as illustrated in Fig. 2B: the predicted signal (middle) is subtracted from the input signal (top), suppressing all but the first period (bottom). In the frequency domain, the effect is to suppress all harmonics of $1/\tau$ (Fig. 3A, top). The cascade of cochlear and cancellation filters has a frequency characteristic that attenuates both power that is distant from the characteristic frequency (CF) *and* power that is harmonic with period τ (Fig. 3A, bottom).

As an example, Fig. 3B shows a cochleagram, a time-frequency representation based on a modeled cochlear filterbank (Slaney 1983) in response to a short snippet of speech ("wow cool", male voice). Panel C shows the gain of the time-varying cancellation filters applied to the output of the filterbank, also as a function of channel and time. The gain is reduced (by as much as -20dB) within the time-frequency pixels corresponding to high-amplitude components of this sound. Thus, if this speech sound were to mask a weaker target, that target might be detected or partially recovered by applying this array of time-varying filters to suppress the masker. This suggests that this hypothetical mechanism might effectively deal with highly non-stationary "real-world" sounds such as speech.

Fig. 3. A top: transfer function of delay-and-subtract filter for τ=2.5 ms, bottom: transfer function of cascade of this filter with a cochlear filter with CF=1.05 kHz. B: Cochlear excitation pattern in response to a short snippet of speech ("wow, cool!"). C: Attenuation factor of the cancellation filter array at each time and CF for the speech snippet in A.

III. ICC as predictive coding?

A. Bottom-up

The structure of the ICC model (Fig. 2) evokes predictive coding of the bottom-up flavor, similar to the model of Srinivasan et al (1982) in which the center of a retinal patch is predicted from its neighbors and/or previous values. Here, the incoming auditory nerve spike probability is predicted from its past values (Fig. 2, left). The model is also reminiscent of LPC (Gray and Markel 1996) in which each new sample of a sampled representation is predicted as a linear combination of N previous samples (where N is the order of the LPC model). The ICC model achieves both *redundancy reduction*, in that the cancellation filter strips the representation of redundant, periodic patterns (Fig. 2B), and *redundancy exploitation* (Attneave 1954; Barlow 1961), in that the optimal delay is the period of the sound, predictive of its pitch (de Cheveigné 1998; 2023). The period is an *abstract* quantity and, in this sense, ICC may contribute to the concrete-to-abstract hierarchy depicted in Fig. 1C (see also Sect. IV, B).

B. Top-down

There is a very different class of models in which incoming patterns are predicted from abstract internal models, according to a principle akin to "analysis by synthesis" (Helmholtz 1867; Braitenberg 1984; Kawato et al 1993; Friston 2002, 2018; Spratling 2017). There is keen interest in such top-down models, in particular due to theoretical properties of certain formulations (Friston 2010, 2018; Friston et al 2009; Bastos et al 2013; see also Sims 2017; Litwin and Miłkowski 2020; Andrews 2021; Williams 2021; Hemmatian 2023). Re-casting ICC as a top-down predictive model might allow us to "hitch onto that wagon" and reap its theoretical benefits. An additional motivation is the need to explain massive efferent pathways that link most stages of the auditory system between cortex and cochlea (Schofield 2012; Romero and Trussell 2022). Together, these reasons encourage us to consider whether it is possible to translate, or insert, ICC into a top-down model. Here I review three simple schemes, numbered for easy reference.

(1) Splitting the ICC model of Fig. 2A in two, parameters τ_k can be treated as message from a higher level that evaluates the filter output, to a lower level that implements the filter. This reformulation makes the model seem "top-down", but with little added value.

(2) The predictive filter of Fig. 4A can be modified by deriving the "prediction" from its output

(Fig. 4B) rather than input, thus making it "top-down." A moment's thought tells us this is a

bad idea: if prediction were effective, i.e., the error was zero, there would be nothing to feed

the prediction. If we persisted, we would discover that the filter has an infinite, non-decreasing

impulse response (Fig. 5B, bottom). This could be alleviated by introducing a gain factor in

the feedback loop, with a value less than one, but the impulse response would still be long

relative to that in Fig. 5A for no clear benefit.

(3) A third scheme, inspired from the concept of "analysis by synthesis" is to derive the pre-

diction via a generative model fed from a higher, abstract stage (Fig. 5C). This too cannot work,

because the temporal (or phase) information needed to correctly align the prediction with the

incoming pattern is not available. As pointed out by Mumford (1992), the higher, abstract stage

speaks a different "language" from the lower concrete layer. Abstraction is a many-to-one

transform, not invertible, and thus an abstract trace cannot translate unambiguously to a con-

crete one.

Fig. 4. A: The bottom-up predictive coding model embodied by ICC implements a filter with a very

compact impulse response that suppresses periodic input. B: Deriving the prediction from from the

output leads to a filter with an infinite, non-decreasing impulse response. C: Top-down prediction

from an abstract trace cannot work because temporal (or phase) information to align it with the input

is lacking.

Interim summary. The ICC model looks like a text-book example of bottom-up predictive

coding, but straightforward attempts to reformulate it as a top-down model are not fruitful. The

rest of this paper tries to better understand why, and salvage the idea in view of its multiple
benefits invoked at the beginning of this section.

IV. Let's try again

A. Top-down predictive coding revisited

Theories of perception mostly agree on a hierarchy of representations going from concrete
(sensory) to abstract (perceptual, or conceptual), with messages passed between levels in the
ascending and (for predictive coding) descending directions (Fig. 1C). As pointed out by Mum-
ford (1992), messages passed between different levels of abstraction require *translation*, which
could occur *before* the message is sent, or *after* it is received. Referring to Fig. 1C, the ascend-
ing error might be translated at either level n or level $n + 1$, and the same options are available
for the descending prediction, implying four different interpretations of Fig. 1C, each plausible
but with different implications and constraints. This is an example of questions that may arise
when trying to make sense of predictive coding.

Top-down translation presents two difficulties. One is the difference in representation format
(e.g., a retinotopic sensory pattern in a sensory area versus an abstract representation within a
face area), the other is that abstraction is not invertible. For the first, Mumford (1992) suggested
that a "template neuron" might code a detailed sensory pattern in the form of synaptic weights.
Bottom-up translation would be performed by weights between axons from neurons in level n
onto the dendrites of a template neuron in level $n + 1$, whereas top-down translation from that
template neuron is performed by weights of on its axonal terminals in layer n. Incidentally,
both sets of weights define the same "template," which raises the question of how they are
learned in sync. For the second difficulty, he proposed that a *family* of templates collectively
represents the set of inputs that map to the abstract trace. Top-down translation then involves
comparing all of these templates, sequentially or in parallel, to the input pattern, the error (or
residual) being presumably the vector difference between input and closest template.

Mumford (1992) further suggested that each template might be "flexible", for example defined
by a mean and covariance (analogous to a Gaussian mixture model), or alternatively as a col-
lection of extreme values (analogous to support vectors). This adds flexibility to the represen-
tation of the distribution of observations at level n that map to an abstract trace at level $n + 1$,
easing bottom-up translation, but it is less clear how the residual is defined. Is it the difference

from the mean of the nearest template? Is it the difference from the nearest "support vector"?

He further suggested that observations might be *transformed* before prediction (for example

by time-warping), increasing flexibility. As yet another alternative, Mumford (1992) also sug-

gested that each template might be formed as linear combinations of basis-functions, on the

lines of Poggio's (1990) "Hyper Basis Function" theory. An abstract trace is then a distribution

of sets of *coefficients* of such combinations, flexibility coming from the spread of this distribu-

tion rather than from the diversity of a set of templates, and/or their individual flexibilities.

In a similar direction, Rao and Ballard (1999) suggested that an abstract trace be defined based

on a linear combination of basis-functions u_j, plus a stochastic noise term:

$$\mathbf{I} = f(\sum_{j=1}^{k} u_j r_j) + \mathbf{n} \qquad (1)$$

where $\mathbf{I}$ is an input that maps to the abstract trace, f is a function (e.g., sigmoid), r_j is a coeffi-

cient ("cause") and $\mathbf{n}$ is a noise process. Here too, the abstract trace is defined as a set of coef-

ficients, but flexibility is now determined by the noise term, rather than by the distribution of

admissible sets of coefficients. Friston's (2009) "free energy principle" requires further that

this noise term be *Gaussian*: in the "Laplace approximation," an abstract trace translates to (or

is translated from) an ensemble of observations that is distributed normally in some space. The

prediction residual ("error" in Fig. 1) is defined as the vector difference between observation

and mean, possibly weighted by "precision" derived from the covariance matrix of the abstract

trace (e.g., Friston 2002), or of the observation (e.g., Heldman and Friston 2010), or perhaps

both. Redundancy reduction is achieved if fewer bits are required to represent the narrower

range of the error than of the observation.

The Gaussian assumption is restrictive compared to the arbitrarily-shaped distribution of Mum-

ford (1992), but Friston (2009, p298) argues that it can easily be satisfied by applying the ap-

propriate *non-linear transform* to the observations. This shifts the "heavy-weight lifting" of

modeling a complex distribution (e.g., visual patterns that match the concept "dog") to that

bottom-up transform. ICC might be interpreted as implementing one such transform, as it pro-

jects a diverse set of (quasi-)harmonic sounds to a space where they are distributed near zero.

Spratling (2017) pointed out the similarity between bottom-up predictive coding (e.g., LPC)

and top-down predictive coding (e.g., Rao and Ballard 1999) which can both be expressed by

an equation analogous to Eq. 1, in which the basis-functions u_j are intervals of recent

observations for LPC, while for top-down predictive coding they belong to an internal genera-

tive model, fixed or slowly-varying. This opens the possibility of *hybrid* ascending and de-

scending prediction, again suggesting a bottom-up component in top-down predictive coding.

If one insists on a "free-form" distribution (rather than Gaussian), the "error" cannot take the

form of a simple difference. For a single observation, it might be quantified by a measure of

surprise (a scalar), and for a set of observations (or an uncertain observation), by a measure

such as *KL divergence*, $D_{KL}(\mathcal{O} \parallel \mathcal{A})$, where $\mathcal{O}$ represents the distribution of the observation(s)

and $\mathcal{A}$ that of the abstract trace (e.g., Pinchetti et al 2002). If divergence is small, the abstract

trace is a good model of the observations, and so the error message can be empty. If divergence

is large, a useful message might consist of the surprising observations themselves, or some

transform thereof (e.g., statistic). Redundancy reduction is achieved if the latter event is rare.

Note, however, that KL divergence requires *parametrization* of the distributions, which re-

moves some (but not all) "freedom" from the free-form assumption.

It is worth noting also that KL divergence is not symmetric. $D_{KL}(\mathcal{O} \parallel \mathcal{A}) \approx 0$ means that *the*

observations fit the abstraction, whereas $D_{KL}(\mathcal{A} \parallel \mathcal{O}) \approx 0$ means that *the abstraction fits the*

observations. The former might be true and the latter not if recent observations are more tightly

distributed than expected, in which case a new abstraction might be considered, possibly nested

within the old (e.g., a category "poodle" within the category "dog"). For this to occur, the

distribution $\mathcal{O}$ must be reliable, which may require gathering multiple observations over some

interval of time. This, in turn, requires *chunking* the observation stream, yet another bottom-up

process. This suggests a different narrative: predictive coding achieves redundancy reduction

for the purpose of *efficient memory* of the stream of observations (de Cheveigné 2025).

Finally, in the "forward-reverse optics" model of Kawato et al (1993), a complex visual scene

is analyzed by a combination of two processes, one top-down, the other bottom-up. The former

attempts to generate retinal patterns from an internal representation of the scene, as in other

analysis-by-synthesis schemes. The authors refer to it as a "direct optics" model because it

mimics, within the brain, the optical pathway from scene to retina, along the lines of a forward

model in motor control (Wolpert and Kawato 1998). The bottom-up process, referred to as

"reverse optics," attempts to translate retinal patterns into a representation of the scene, as in a

classic computer vision system. This second, bottom-up, process does not need to perform

perfectly, and indeed, it cannot, given the ambiguity of scenes with occlusion, etc. Its role is to

provide an initial "guess" of the scene that allows the search space of the top-down process to

be pruned. Transposing to audition, we could hypothesize that ICC contributes to a "reverse

acoustics" model, applicable to parse scenes that include harmonic or quasi-harmonic sources.

In sum:

(1) The term "predictive coding" has been applied to a variety of very different concepts.

(2) "Analysis-by-synthesis" is problematic because abstraction is not invertible. "Prediction

error" may make sense in terms of surprise or KL divergence, but not in terms of a vector

difference unless restrictive assumptions apply. While a *property* of an observation may be

predicted from an abstract trace, the value of the observation may not.

(3) Top-down predictive coding relies on bottom-up processing for much of the "heavy lifting,"

in particular to perform abstraction between layers of a hierarchical representation.

B. In-channel cancellation contributes to abstraction

ICC was earlier presented as a kind of adaptive filter, the output of which has the same level

of abstraction as its input (i.e., a rapidly-varying pattern of firing probability). Here, I look at

how it might produce slowly-evolving abstract quantities, thus contributing to a first stage in a

hierarchy of abstractions.

A first such quantity is the *period*, estimated by fitting the ICC or HC model with a criterion

of minimum output (Fig. 5A). It is an abstraction in that different periodic sounds may share

the same period. A wider class of sounds are *approximately periodic* in various ways: limited

duration, slow amplitude or frequency changes, periodicity within a restricted spectral region,

etc. (as in the speech example of Fig. 3B). For these, a measure of *periodicity* may be informa-

tive, for example the cancellation filter output/input power ratio (as plotted in Fig. 3C for indi-

vidual channels over time). Period and periodicity are perceptually relevant, the former as a

cue to *pitch*, the second as a possible contributor to an aspect of *timbre*.

Fig. 5. ICC as abstraction. A: The period of a 200 Hz complex tone is estimated as the first non-zero lag that yields zero output, common over channels. The black line is for CF=500 Hz (this channel responds to both harmonics 2 and 3), the dotted lines are for CF=400 Hz (harmonic 2) and CF=600 Hz (harmonic 3). B: Optimal smoothing of a time-frequency representation. Left: raw cochleagram, right: cochleagram smoothed in time (kernel duration $T = 1/F_0$) and frequency (kernel width $F_0 = 1/T$). C: Chunking for redundancy reduction. Each stationary segment might be coded by the *waveform during one period* (or its Fourier transform), the value of the *period* (for periodic sounds) and the *duration* of the segment.

Another abstraction is the *spectrum*, which comes in many variants according to how it is calculated. A time-frequency representation can be calculated based on the short-term Fourier transform (*spectrogram*), or as instantaneous power at the output of a cochlear filterbank (*cochleagram*, e.g. Fig. 3B), or instantaneous probability at the output of a more realistic peripheral model. Again, it is abstract in that many different sounds share the same spectrum or spectrogram, and perceptually relevant as a predictor of *timbre*, for example that of a vowel. Unfortunately, this representation is not invariant relative to the fundamental frequency $F_0 = 1/T$ of a sound: individual harmonics may emerge at low frequencies, and a pulsed temporal structure may emerge at high frequencies (Fig. 5B, left), whereas timbre is usually thought to reflect the smooth time-frequency *envelope*. Here again, the ICC/HC model contributes by allowing

period-adaptive smoothing to approximate that envelope (Fig. 5B, right). This is the principle

of the well-known STRAIGHT method of spectro-temporal estimation (Kawahara et al 1999).

It offers yet another level of abstraction, as sounds with different spectra/spectrograms (due to

different fundamental frequency) map to the same smooth spectro-temporal envelope.

Yet another popular abstraction is the *modulation spectrum* (Viemeister 1979; Dau et al 1997;

Jepsen 2003; Joris et al 2004; Anden and Mallat 2014; Koumura et al 2019), defined as the

spectrum of the *temporal envelope* within peripheral channels, possibly averaged over channels.

It accounts for many aspects of sound, in particular speech (Elhilali et al 2003; Hermansky

2010) and, together with other statistics, captures the perceptually-relevant *texture* of many

natural sounds (McDermott and Simoncelli 2011; McDermott et al 2013). Local fluctuations

may serve also as cues to spectrally local features (Carney 2024). The quality of this abstraction

is improved if the temporal envelope is first smoothed with a kernel tailored to the period of

the sound (as described in the previous paragraph), to factor out periodicity-related fluctuations

from slower perceptually-relevant modulations, thus avoiding interference between the two

(Stein et al 2005).

Related to abstraction is *redundancy reduction*, and *summarization*. A benefit of detecting pe-

riodicity and estimating the period is that periodic segments can be cheaply represented by the

waveform over one period, or its spectral equivalent (Fig. 5C). The ICC model contributes by

detecting such periodic segments and their boundaries, and estimating the periods. This com-

bination of *segmentation* and summarization may be seen as an initial layer in a hierarchical

memory representation (de Cheveigné 2025).

This section hinted at various ways in which ICC *might* contribute to the elaboration of abstract

representations of sound that *might* contribute to some of the top-down prediction schemes

reviewed earlier. These ideas are presented schematically, obviously a more precise formula-

tion is required to take them seriously as models of sensory processing.

V. Discussion

378   This paper presented the low-level auditory processing model ICC as a form of *bottom-up*

379   predictive coding. However, much of the appeal of the concept of predictive coding is specific

380   to its *top-down* flavor; a reader who expected that flavor might feel short-changed. For this

381   reason, I also investigated how ICC might relate to, or contribute to top-down predictive coding.

382   At this point, the following hypothetical roles emerge:

1. The ICC model contributes an early link to the chain of abstractions postulated by most (all?) predictive coding models. One cannot achieve a hierarchy of abstraction if the output of each stage belongs to the same concrete space as its input, as is the case if each level sends a residual to the next. In contrast, the *parameters* of a model fit to a concrete pattern might be predicted, but this requires that that model (e.g., ICC) is defined.

2. The ICC model contributes to acoustic scene analysis, by its ability to suppress sounds with a harmonic, quasi-harmonic, or sparse spectrum. In this way, it might contribute to a "reverse acoustics" model on the lines of Kawato et al (1993).

3. The ICC model transforms input patterns that belong to the class of periodic sounds in such a way that they are distributed around zero, plausibly according to a Gaussian distribution. In this, it might play the role of a "Laplacifier" transform so that a predictive coding model on the lines of Friston (2009) meets its assumptions (Sect. IV, A).

4. The parameters of the ICC model (delays τ_k) might be under top-down control. For example, a musical context might prime a listener as to the next pitch, or a decision to listen to source might translate into top-down imposition of delays that suppress competing sources. Multiple top-down parameters might be tried in sequence (or in parallel) to find one for which ICC best "fits" the input.

5. If predictive coding is reinterpreted as forming a compact statistical model of the stream of observations, ICC can contribute to the initial "chunking" by detecting intervals of quasi-periodicity and their boundaries, and by removing redundancy within such intervals. The magnitude of the ICC output serves as a measure of surprisal relative to the assumption of periodicity.

A stumbling block is the notion of prediction error as a *difference*, or *residual*. It would seem

that Mumford's (1992) warning about the need for translation between levels of abstraction

was not heeded (including by Mumford himself). Objections to that notion are logical, as re-

viewed earlier, and also empirical. In a recent study, Furutachi et al (2024; Lowet and Uchida

2024) probed responses of putative "error neurons" in mouse primary visual cortex. With con-

ditions carefully designed to test the difference hypothesis, they found that a surprising obser-

vation elicited an *enhanced* stimulus-specific response, rather than a difference. It is plausible

that Mumford and others and others were aware of the issue, but that its implications got "lost
in translation" when trying to make the model intelligible (as in Fig. 1C).

A prime motivation of top-down predictive coding is the need to explain efferent pathways
within the brain. From the roles just enumerated it is not clear why they would need to be
massive. One might speculate that massive efferent pathways are required by the need to pro-
pose, at level $n + 1$, a large number of alternative abstract explanations to be tested at level n.

Focusing on the auditory brainstem, the working hypothesis of a *single* delayed feedforward
pathway within a channel might be over-restrictive. More plausible is a combination of multi-
ple, within-channel predictors (as in LPC), possibly complemented by cross-channel interac-
tions (e.g. Shamma 1984; Nelson and Carney 2004; de Cheveigné and Pressnitzer 2006; Car-
ney 2002, 2024) and binaural interactions (Durlach 1964; Culling and Summerfield 1995; Bei-
derbeck et al 2018; Franken et al 2021). The multiple parameters involved (weights, delays)
might help account for multiple efferent pathways.

An explanatory, reactive, or compressive model can better be fit and updated based on a buffer
that extends into the past (Schmidhuber 2009). Predictive coding may contribute to *memory* of
past observations (as opposed to a model of causes, decisions or actions) by helping to *segment*
the input stream, and more generally helping to code observations in terms of already-acquired
statistics, or internal explanatory models of the data. Rather than the message-passing hierarchy
of Fig. 1C, memory would form a hierarchy of increasingly abstract statistics (de Cheveigné
2025). "Prediction error" might take one of the following forms: (1) a simple binary flag (fit
vs no-fit) or a scalar (surprise), (2) a concise account of how the observation can be made to fit
(e.g., "apply delay τ to the ICC model"), (3) a more exhaustive record or summary of the mis-
fitting observations, "memorized" for future resolution.

To summarize, the simple bottom-up ICC model of auditory brainstem processing served as a
pretext to review issues related to top-down predictive coding, highlighting the conceptual dif-
ficulties involved, and outlining approaches to dealing with them.

Conclusion

The in-channel cancellation model describes a hypothetical form of low-level processing within the auditory brainstem, that offers a text-book example of predictive coding of the feed-forward, bottom-up flavor, similar to earlier proposals for retinal processing (Srivinasan et al 1982). This paper briefly reviewed the model and its relations to bottom-up predictive coding, and examined how it might form part of an early layer within a predictive coding model of the feed-back, top-down flavor. Specifically, its segregation properties might contribute to a bottom-up "analysis" pathway that works hand-in-hand with a top-down predictive "synthesis" pathway (Kawato et al 1993). It could also participate to an early stage of statistical chunking of the sensory input that reorganizes it for more effective predictive coding. It might contribute to transform a non-Gaussian distribution of sensory regularities to better fit the Gaussian approximation assumed by many models of predictive coding.

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Declaration of competing interests

none

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