Offspring size resolves a population growth paradox in rays and skates

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Abstract

The maximum intrinsic population growth rate, r_{max}, is a key determinant of the limits for sustainable fishing and is increasingly used in risk assessments. Metabolic theory suggests that r_{max} scales with adult body size, temperature (and hence depth) such that smaller-bodied species and those in warmer, shallower waters have greater r_{max} and, therefore, will be less sensitive to overexploitation. However, warm shallow-water tropical rays have lower r_{max} than cold deep-water temperate skates *contra* to the metabolic expectation. To resolve this paradox, we build from recent advances that suggest that offspring size may be key to understanding r_{max}. Specifically, we examine how r_{max} is related to adult size, offspring size, temperature, and depth across 85 ray and skate species. Our results show that offspring size mediates relationships between r_{max}, adult body size, temperature, and depth. Indeed, tropical rays had, on average, larger offspring and lower r_{max} compared to the temperate skates, despite living in warmer, shallower waters. Thus, despite the expectation from theory that tropical species should have faster life histories compared to temperate species, our result explains why tropical rays are actually less resilient. It remains unclear as to why tropical rays have such large offspring but we speculate that this is due to greater predation risk in shallow tropical waters driving the additional maternal investment in offspring size via the evolution of viviparity and matrotrophy. Our work highlights the complex relationships among life histories and the environment and may help explain global biogeographic patterns of intrinsic sensitivity to overexploitation.

1. Introduction

A key challenge in population biology is understanding global patterns of life histories, which is of both fundamental interest as well as useful for identifying species sensitivity to overfishing and other anthropogenic threats. Biogeographic patterns in life histories appear to be mediated by temperature (Beukhof *et al.*, 2019), for example, Bergmann's rule states that terrestrial endotherms in cooler environments will be larger-bodied than their warmer relatives (Bergmann, 1847). Similarly, the Temperature-Size Rule (TSR) describes the observed pattern that ectothermic populations and species generally grow faster to a smaller size at maturity (and presumably, smaller adult size) in warmer temperatures (Atkinson, 1994; Atkinson and Sibly, 1997; Atkinson, Morley and Hughes, 2006). Finally, metabolic theory suggests that species in warmer waters (e.g. in the tropics and shallow waters) with higher metabolic rates will tend to have 'faster' life histories than those in cooler waters (e.g. high latitude and deep waters) (Juan-Jordá *et al.*, 2013; Beukhof *et al.*, 2019; Wong, Bigman and Dulvy, 2021; Gravel *et al.*, 2024). Typically, species with faster life histories grow faster to a smaller maximum body size, mature earlier, and have shorter lifespans, resulting in higher maximum intrinsic rate of population increase, r_{max} (Hutchings *et al.*, 2012; Thorson, 2020; Gravel *et al.*, 2024).

r_{max} is the average annual number of female spawners produced per female spawner at low population density (i.e. in the absence of density-dependence). Hence, r_{max} is an essential component of fisheries management to determine fishing limits and species' recovery potentials (Cortés, 2016; Pardo *et al.*, 2016; Horswill *et al.*, 2025). There is considerable interest in calculating r_{max} for chondrichthyans but general patterns have proven hard to find (Mejía *et al.*, 2025) unless trait data are carefully matched from similar habitats and consistent models are used (Pardo and Dulvy, 2022; Gravel *et al.*, 2024; Moro *et al.*, 2025). According to metabolic scaling expectations, r_{max} will scale with (adult) body mass (with an exponent of -0.25) and, independently, increase with temperature (Brown *et al.*, 2004; Savage *et al.*, 2004). This has been shown empirically both in experimentally-manipulated populations as well as across species in the wild (Luhring and Delong, 2017; Bernhardt, Sunday and O'Connor, 2018). For example, a positive relationship between r_{max} and temperature exists across Atlantic cod (*Gadus morhua*, Gadidae), which has greater r_{max} in warmer, more southerly populations (Myers, Mertz and Fowlow, 1997; Savage *et al.*, 2004). Further, cooler, temperate tunas (Scombridae) with slower life histories experienced greater population declines than tropical lower-latitude tunas with faster life histories, after controlling for fishing mortality (Juan-Jordá *et al.*, 2011, 2015). More generally, the ratio of production to biomass (P:B) changes systematically with latitude across the world's fish communities, with high production and low standing biomass in the tropics compared to that found at cooler temperate and polar latitudes (Jennings *et al.*, 2008). Recent work suggests that in addition to temperature and adult size, offspring size may also be an important determinant of r_{max} (Neuheimer *et al.*, 2015; Denéchère, van Denderen and Andersen, 2022). This suggests that for two species with the same adult mass, one with larger offspring (and fewer of them) may have a lower r_{max} and therefore, offspring size could affect the scaling of r_{max} (Burger, Hou and Brown, 2019; Denéchère, van Denderen and Andersen, 2022).

Rays and skates of the superorder Batoidea are widely distributed across the world's oceans but with a distinct biogeographic separation (Figure 1). Skates have an anti-tropical distribution and are typically found in the cooler waters of polar and temperate seas, as well as deeper, cool waters in the tropics, although there are also a few shallow-water tropical species (e.g. Teevan's Skate *Dipturus teevani* and Rosette Skate *Leucoraja garmani*, Rajidae; Figure 1a). Whereas rays are generally found in the shallow tropics, subtropics and with

seasonal occurrence in temperate waters during summer (Figure 1b), but with some deep-
water exceptions (e.g. Deepwater Stingray *Plesiobatis daviesi*, Plesiobatidae, and Sixgill
Stingray *Hexatrygon bickelli*, Hexatrygonidae) (McEachran and Miyake, 1990; Ebert and
Compagno, 2007; Frisk, 2010). Metabolic theory suggests that warm-water rays should have
higher r_{max}, yet paradoxically, they have lower r_{max} than cold-water skates (Barrowclift *et al.*,
2023). Most rays are live-bearers with very low fecundity and generally, have larger
offspring (typically 1% of adult mass) compared to skates, which lay numerous eggs
(mermaid's purses) and overall, have smaller offspring (typically 0.1% of adult mass; Figure
2) (Goodwin, Dulvy and Reynolds, 2002; Mull *et al.*, 2024). Here, we investigate whether the
larger offspring size of tropical rays explains the paradox of their lower r_{max} compared to
skates, while accounting for temperature and depth for 85 batoid species.

2. Material and Methods

We first describe the mapping of batoid species richness. Second, we present the calculation of r_{max}, including the sources of the life history data used in the calculations. Third, we describe the calculation of environmental temperature-at-depth. Fourth, we summarise our analytical approach, including the statistical models used to assess different hypotheses of how r_{max} may vary with adult and offspring mass, temperature, and depth.

2.1 Mapping of ray and skate richness

We downloaded species distribution maps from the IUCN Red List as shapefiles (https://www.iucnredlist.org/resources/spatial-data-download). These were mapped to a hexagonal grid with cell sizes averaging 23,322 km^2 and species richness was calculated per cell for each of skate (Order Rajiformes) and ray species (Orders: Torpediniformes; Rhinopristiformes, and Myliobatiformes) (Dulvy *et al.*, 2014, 2021).

2.2 The calculation of r_{max} and source of life history data

The maximum intrinsic rate of population increase, r_{max}, was calculated using a modified Euler-Lotka model, with a mortality estimator that accounts for survival to maturity with the following equation:

$$l_{\alpha_{mat}}b \ = \ e^{r_{max}\alpha_{mat}} - e^{-M}(e^{r_{max}})^{\alpha_{mat}^{-1}},\qquad(1)$$

where $l_{\alpha_{mat}}$ is the proportion of individuals surviving to maturity, which is calculated from annual fecundity b and the species-specific instantaneous natural mortality rate M (Cortés, 2016; Pardo *et al.*, 2016). Natural mortality (M) was estimated as $M = 1/\omega$ (Dulvy et al., 2004) where ω is an estimate of average lifespan in years and was assumed to be the midpoint between age at maturity (α_{mat}) and maximum age (α_{max}) (Pardo *et al.*, 2016). The life history traits were sourced for 85 ray (Torpedo rays, Torpediniformes; Rhino rays, Rhinopristiformes; and stingrays, Myliobatiformes; n=53) and skate species (Rajiformes; n=32) (Figure 3). Three traits were geographically matched where possible to minimise spurious errors due to intraspecific life history variation (Gravel *et al.*, 2024; Moro *et al.*, 2025): 1) female age at 50% maturity (α_{mat}; years), 2) maximum age for females, where known (α_{mat}; years), and 3) annual reproductive output (number of female offspring assuming 1:1 sex ratio; b) reported in a published global life history database (Barrowclift and Dulvy, 2023) compiled in Barrowclift et al. (2023).

Adult body mass (maximum weight in grams) for the 85 batoid species was also sourced from the published life history database compiled in Barrowclift et al. (2023). Offspring mass (in grams) was estimated from offspring size measured as total length for skates or disc width for rays in centimetres (cm) as reported in Rays of the World (Last *et al.*, 2016), Sharkipedia (Mull *et al.*, 2022), and IUCN Red List assessments (Dulvy *et al.*, 2021). Offspring size was not available for 14 species and for these cases we estimated offspring size from related species with similar maximum length and body shape (Barrowclift and Dulvy, 2023). The median offspring length was calculated in cases when minimum and maximum offspring lengths were reported. The corresponding offspring mass was then calculated using length-weight regression coefficients extracted from FishBase using the package *rfishbase* (Boettiger, Lang and Wainwright, 2012; Froese and Pauly, 2022; Barrowclift and Dulvy, 2023). Length-weight regression coefficients were selected for females where possible. When

104 length-weight regressions were not available, we used parameters for a closely related species
105 with similar body shape and maximum size (Barrowclift and Dulvy, 2023).

2.3 Calculation of environmental temperature-at-depth

Median depth and environmental temperature for the 85 ray and skate species were also taken
from Barrowclift et al. (2023). Specifically, median depth estimates for each species were
taken from depth ranges of IUCN Red List assessments as compiled in Dulvy et al. (2021).
Temperature-at-depth data were determined by intersecting each species distribution map
with the International Pacific Research Center's interpolated dataset of gridded mean annual
ocean temperatures. This dataset is based on measurements from the Argo Project (data
available   at
http://apdrc.soest.hawaii.edu/projects/Argo/data/statistics/On_standard_levels/Ensemble_mea
n/1x1/m00/index.html). Species range maps were sourced from
https://www.iucnredlist.org/resources/spatial-data-download. Temperature grid points were
extracted across the species' distribution from the depth level that was closest to the species'
median depth and the median temperature calculated (Pardo and Dulvy, 2022; Barrowclift *et*
al., 2023).

2.4 Statistical inference

121 Metabolic scaling expectations for how r_{max} relates to adult body mass and temperature
122 (Savage *et al.*, 2004) can be estimated with the following linear model:

$$\ln(r_{max}) = \beta_0 + \beta_1 * \ln(M) + \beta_2 * 1/k_B T , \qquad (1)$$

where r_{max} is the maximum intrinsic rate of population increase (year^{-1}), β_0 is the intercept,
β_1 is the body mass-scaling coefficient, M is adult mass in grams, β_2 is the activation energy
E, T is the temperature (in Kelvin), and k_B is the Boltzmann constant (8.617×10^{-5} eV).

We modified this initial equation (1) above to test whether absolute offspring size ($M_{offspring}$)
and the adult to offspring mass ratio ($M/M_{offspring}$) explained variation in r_{max} across species in
addition to temperature and depth (Denéchère, van Denderen and Andersen, 2022).
$M/M_{offspring}$ was suggested by Denéchère et al., (2022) to be a better predictor of r_{max} than
either adult or offspring body mass and thus it is examined here. Specifically, we used an
information-theoretic approach to compare a total of 32 models that represented different
hypotheses as to how r_{max} may vary across species (see Table S1 for hypotheses, models, and
AIC values and weights).

For model fitting, r_{max}, adult and offspring masses were natural log-transformed, and
temperature and depth data were standardised (scaled and centred). We found that offspring
body mass and adult body mass (Figure 4a) as well as temperature and depth were collinear
(Pearson's r > 0.75), but there was no relationship between either adult or offspring body
mass and temperature (Figure 5). Thus, we only included either offspring body mass or adult
body mass and either temperature or depth in a given model, and did not consider interactions
between either mass and either temperature or depth. All models were run in a phylogenetic
comparative framework to account for the shared evolutionary history between species. To
do so, we fit phylogenetic generalised linear models using the *pgls* function in the *caper*
package (Orme *et al.*, 2018). Phylogeny was used as a random effect in all models using a
phylogenetic tree randomly drawn from the distribution of chondrichthyan trees (Stein *et al.*,

2018) (available at Vertlife.org; Figure 3). The binomial nomenclature of the trees was
updated to reflect current taxonomic nomenclature. The phylogenetic position of two species
was not known (*Aetobatus narutobiei*, Aetobatidae, and *Maculabatis ambigua*, Dasyatidae),
and therefore, two closely related species (*A. flagellum* and *M. gerrardi*, respectively) were
used instead. Models were refitted with an additional 10 random trees to test the sensitivity of
results to slight variations in the phylogenies; temperature and depth were interchangeable in
the top model, and therefore, results were reported for a single tree (Table S2 in the
Supporting Information). The corrected Akaike Information Criterion (AICc) were used to
compare models. If including a parameter improved the model's AICc by less than two units
(ΔAICc $\leq$ 2), it was considered relatively uninformative (Burnham and Anderson, 2002;
Arnold, 2010). All analyses were run in R version 4.1.2 (R Core Team, 2021) in RStudio
(RStudio   Team,   2021).

3. Results

Tropical rays had, on average, larger offspring and lower r_{max} compared to the temperate skates, despite living in warmer and shallower waters. We found that the ratio of adult to offspring size was not important in explaining variation in r_{max} and thus, we focus on the 11 models without this ratio in the main text (see Table S1 in the Supporting Information for results of the models with the adult to offspring size ratio). Our findings were insensitive to the exclusion of the two species with the largest offspring masses: *Mobula alfredi* and *M. birostris* (Mobulidae). The top models were the same and therefore results were presented for the full 85 species dataset (Table S3 in the Supporting Information).

Offspring size combined with either temperature or depth were the most important variables explaining the global variation in r_{max} across batoids (Figures 6 and 7). Of the 11 models examined, the most supported model suggests that r_{max} varies with offspring mass and depth (ΔAICc = 0), describing the greatest amount of variation in r_{max} across species (adjusted R^2 = 0.20; Table 1). The second-ranked model described r_{max} varying with offspring mass and temperature (ΔAICc = 0.3) and had approximately 86% of the support of the top-ranked model (when compare the Akaike weights) and accounted for slightly less variation (adjusted R^2 = 0.19; Table 1). These top two models – one with depth and one with temperature – were essentially equivalent in terms of support suggesting that either variable could be combined with offspring mass to explain the variation in r_{max} across rays and skates (Figure 6 and 7). Whether including temperature or depth as statistically the top model depended on the phylogeny (Table S2). In all models, the effect sizes of offspring mass, depth, and temperature had 95% confidence intervals that did not overlap zero (Figure 6). A model describing r_{max} varying solely with offspring mass received moderate support but with only 22% of the support of the top-ranked model and accounting for less variation (adjusted R^2 = 0.16). Therefore, including temperature or depth in the model improved the model support (based on AIC comparison; Table 1).

The effect of offspring mass on maximum population growth rate, r_{max}, of batoids is negative, indicating that r_{max} is lower in species with larger offspring sizes and higher in species with smaller offspring sizes (Figure 7; Table S4 in the Supporting Information). The effect of inverse temperature $1/k_B T$ and depth were negative across models indicating r_{max} is higher in warmer-shallower water species as would be expected from metabolic theory (Figure 7; Table S4). The scaling of temperature with r_{max} overlapped with the expectation of approximately -0.6 from metabolic theory (Figure 6; Table S4). r_{max} was greater for species at shallower depths (Figure 7a) or at warmer temperatures (Figure 7b) based on the fitted top two models for the predicted relationships across three depths and three temperatures, respectively.

By comparison, the remaining models were not well supported (ΔAICc > 6; Table 1). Adult mass did not have as much support as offspring mass in explaining variation in r_{max} across rays and skates and models without any measure of size were far less supported than those with either offspring or adult size (Table 1). Indeed, the effect of adult mass on r_{max} was approximately half (-0.12) than expected from metabolic theory (-0.25; Table S4 in the Supporting Information).

For all models, there was a strong phylogenetic signal from the residuals of r_{max} (Pagel's $\lambda \geq$ 0.79; Table S4 in the Supporting Information).

4. Discussion

We find that offspring size disrupted the well-studied relationships between r_{max}, (adult) body size, and temperature across 85 ray and skate species. Specifically, our results show that temperature (or depth) and adult body size alone – as previously thought – do not explain the variation in r_{max} across rays and skates. Instead, offspring size appears to be the key predictor of r_{max} in these taxa such that species with larger absolute offspring size have lower population growth rates, r_{max}. This finding helps explain the paradox of why tropical rays, which are found in warmer, shallower waters and should have higher r_{max} based on expectations from metabolic and life history theory, instead have lower population growth rates, compared to cold, deep-water skates (which have smaller offspring size).

Life history and metabolic theory suggest that in warmer temperatures, organisms generally grow faster, mature earlier, and attain smaller maximum body sizes resulting in faster generation times and higher production to biomass ratios (Beukhof et al., 2019; Jennings et al., 2008; Munch & Salinas, 2009). This would also lead to latitudinal and depth-related patterns of temperature and size, whereby organisms in shallower, warmer, and/or lower latitude waters have higher metabolic rates and therefore 'faster' life histories compared to organisms in deeper, cooler, and/or higher latitude waters (Juan-Jordá *et al.*, 2013; Wong, Bigman and Dulvy, 2021; Pardo and Dulvy, 2022; Gravel *et al.*, 2024). However, recent work found that compared to the cold water, deeper-dwelling skates, warm, shallow-water tropical rays have lower r_{max} and therefore greater intrinsic sensitivity to anthropogenic threats such as overfishing (Barrowclift *et al.*, 2023). Here, we delve into this paradox and uncover that offspring size modulates how r_{max} scales with temperature (or depth) and adult body size. Specifically, offspring size, and not adult size, was the most important size metric for explaining variation in r_{max} across batoid species and along with temperature or depth, explained the most variation. Generally, offspring size tends to have a negative relationship with temperature in vertebrates and invertebrates due to differences in maternal investment, with females producing larger, better-provisioned offspring in colder environments (Pettersen *et al.*, 2020; Marshall, 2021). This large-offspring-in-the-cold pattern is supported by both a cross cohort experiment of bryozoans (Marshall, 2021) and a metanalysis spanning 72 species from five ectotherm phyla (Pettersen *et al.*, 2020). However, tropical rays generally have larger offspring sizes than cooler-water-temperate skates. It may be that offspring size is largely independent of temperature for batoids, with both employing very different reproductive strategies, raising the question as to why large offspring sizes have evolved in shallow-water, tropical rays. Collectively, our work suggests that at least for some taxa, the pattern of reproductive investment into offspring size can interfere with the effect temperature and size typically has on other life history traits.

Our finding that offspring size explains variation in r_{max} across batoids follows from recent work suggesting that the scaling of r_{max} with adult body mass matches metabolic expectations only when offspring size is considered, and specifically, when offspring mass is proportional to adult mass (constant adult-to-offspring size ratio) (Denéchère, van Denderen and Andersen, 2022). For elasmobranchs, Denéchère *et al.* (2022) found that the scaling of r_{max} with adult mass matched metabolic expectations and that elasmobranchs had a constant adult-to-offspring ratio (the ratio of adult size to offspring size does not increase with adult mass). We found that the ratio of adult size to offspring size was not important in the scaling of r_{max} and that in batoids, this ratio increases with adult size (i.e. it is not constant as found in Denéchère *et al.* (2022) when examined across a broader diversity of elasmobranchs). Further, we found that the effect size of absolute offspring mass on r_{max} was larger than adult mass, suggesting that an increase in offspring size limits r_{max} more strongly than adult size, and that using the ratio of adult size to offspring size had low predictive power. Offspring

size, which reflects reproductive investment and life history trade-offs, greatly varied across
the 85 species we examined, which may be why we were able to detect the importance of this
trait. Specifically, the differences in r_{max} between warm, shallow-water rays and cold water,
deeper-dwelling skates are likely due to their different reproductive strategies – as live-
bearing rays have fewer, larger offspring compared to egg-laying skates with large numbers
of smaller offspring – as hypothesised in Barrowclift *et al.* (2023).

Live-bearing has been hypothesised to have evolved from egg-laying in order to increase the
survival of offspring through a controlled maternal environment and greater protection from
predators (Wourms, 1994; Goodwin, Dulvy and Reynolds, 2002). In live-bearing species,
offspring size is constrained by the size of the maternal body cavity but results in offspring
with greater survival (Wourms and Lombardi, 1992; Musick and Ellis, 2005). Whereas in
egg-laying species, size is limited by nutrients stored in the yolk sac (Carrier, Pratt and
Castro, 2004). The egg-laying reproductive strategy of skates is thought to be advantageous
because it requires less energy and shorter reproductive cycles but there will be survival
consequences for the offspring due to smaller size, and, thus, greater risk of predation
(Goodwin, Dulvy and Reynolds, 2002). Consequently, there is a trade-off between the
number and size of offspring resulting in a negative relationship between offspring size and
annual fecundity (Smith and Fretwell., 1974; Duarte and Alcaraz, 1989; Cortés, 2000). This
was evident in our batoid dataset along with the expectation that larger species tend to have
larger and more offspring (Cortés, 2000). Offspring size will affect juvenile survival to
maturity, which is important to consider, given the maternal trade-off between lifetime
reproductive output, which likely varies between egg-laying and live-bearing reproductive
modes (Pardo *et al.*, 2016). In the calculation of r_{max} for elasmobranchs, there is the
pragmatic assumption that juvenile survival to maturity is the same as the survival rate of
adult ages (a consistent mortality estimator). However, our key finding suggests the average
mortality depends on offspring size, presumably with larger absolute offspring sizes (typical
of tropical rays) having lower predation risk than smaller offspring (typical of colder-water
skates). This then leads to the question as to why it might be advantageous for tropical,
warm-water rays to have larger offspring than temperate, cold-habitat skates?

The ancestral reproductive mode of sharks and rays is egg-laying with the subsequent
evolution of live-bearing and a particularly high degree of maternal investment found in the
shallow-tropical elasmobranch species (Dulvy and Reynolds, 1997; Blackburn and Hughes,
2024; Mull *et al.*, 2024). The diversification and radiation of elasmobranchs throughout
shallow tropical shelf seas and the pelagic zone appears to be associated with the evolution of
live-bearing and multiple mechanisms for providing additional maternal investment in
offspring (Mull *et al.*, 2024). The question remains as to why live-bearing with additional
maternal investment has evolved. Predation tends to be size-based in the marine realm
(Verity and Smetacek, 1996; Barnes *et al.*, 2010). We speculate that shallow-water, tropical
rays have evolved larger offspring in response to selection pressure from greater predation
risk in the tropics. Increased offspring size reduces the threat of predation in systems
structured by size-based interactions, i.e. has been selected to reduce juvenile mortality
(Cortés, 2000; Olsson, Gislason and Andersen, 2016; Sibly *et al.*, 2018). We speculate that
this predation risk drove the evolution of live-bearing, and in particular the convergent
evolution of multiple forms of matrotrophy (maternal supply of nutrients during gestation).
Generally, offspring size is larger in chondrichthyans compared to teleost fishes in which
live-bearing appears to have evolved in particularly small-bodied taxa, suggesting the drivers
of viviparity are fundamentally different in chondrichthyans (Goodwin, Dulvy and Reynolds,
2002). Predation risk has generally been hypothesised to increase towards the tropics, with
recent empirical work finding greater predation rates on epifaunal communities in shallow,

tropical waters compared to high latitude waters (Ashton *et al.*, 2022). This is relevant to
potential greater predation on eggs and juveniles in tropical waters. Fisheries-driven decline
in sharks (which predate on batoids) has led to increases in ray abundance, consistent with
our hypothesis that predation is a major evolutionary force in tropical systems (Sherman *et*
al., 2020; Simpfendorfer *et al.*, 2023).

Given Bergmann's rule and the Temperature-Size-Rule (TSR), adult body size of temperate
skates in cooler waters would be expected to be larger than tropical rays in warmer waters.
However, our results suggest there is wide variation in adult body size across batoids and,
generally, the tropical rays are larger than cooler-water skates. We speculate above that the
larger offspring sizes and live-bearing are a result of elevated predation in the tropics; given
the body cavity constraint on offspring size of live-bearers we further speculate that large
offspring size would require the evolution of larger adult body sizes in tropical rays that
would allow greater maternal investment. This is consistent with the adult body size
differences being the opposite of what might be expected under a TSR hypothesis, i.e. larger
in tropical rays and smaller in cool-water skates, and may explain this exception to the TSR
where tropical rays attain larger sizes at higher temperatures (Atkinson, 1995). Instead, our
findings are more consistent with a mortality theory of life histories, and specifically the
mortality arising from predation risk and offspring size (Auer *et al.*, 2018; Glazier, 2023).

We found that offspring size, alongside temperature or depth, explained variation in r_{max} for
rays and skates rather than adult body size or the adult-to-offspring size ratio. Offspring size
reflects parental (mainly maternal) energy investment that is part of a key trade-off between
reproduction, growth, and survival. Offspring size has direct fitness consequences through the
allocation of resources provisioned to offspring for growth, survival, and reproductive
success, and therefore has ecological and evolutionary implications (Pettersen, Schuster and
Metcalfe, 2022). Given the strong phylogenetic signal in the r_{max} residuals, it is likely
maximum population growth rate is shaped by biological traits that are evolutionary
conserved, which would allow for predictive modelling of r_{max} based on phylogenetic
relationships (Pardo and Dulvy, 2022). Additional variation in r_{max} that was not explained by
our models may be explained by further environmental and physiological variables such as
dissolved oxygen or metabolic rate (Pardo and Dulvy, 2022; Gravel *et al.*, 2024). Indeed,
further understanding of the relationship between offspring size and metabolic rate is needed
(Pettersen, Schuster and Metcalfe, 2022). Empirical estimates of juvenile mortality for sharks
and rays are still required to better understand juvenile survival across species with different
life history strategies (incorporating how growth and mortality varies with body size). Whilst
the mortality estimator used in the modified Euler-Lotka model to calculate r_{max} accounts for
juvenile survival to maturity, there is a need for the development of size-dependent mortality
rates to investigate differences across reproductive and offspring size strategies. Our results
suggest that these differences may be key to understanding biogeographic patterns in
extinction risk. We posit that greater predation risk in the tropics has driven the evolution of
larger offspring size to increase offspring survival in tropical rays, potentially through live-
bearing reproductive mode, increased matrotrophy, and larger adult body sizes.
Consequently, shallow-water tropical rays have lower population growth rates and are more
intrinsically sensitive to overfishing than may be expected from metabolic ecology.

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Data Availability Statement

The datasets supporting this article are available at FigShare (DOI: https://doi.org/10.6084/m9.figshare.20182109). The R code to reproduce these analyses will be available at Github (https://github.com/EBarrowclift/batoid-rmax-offspring-scaling).

Conflict of Interest Statement

I confirm that all authors agree with the contents of the manuscript and its submission to Fish and Fisheries. All data and code sources have been made publicly available upon submission of the manuscript. Funding sources are fully acknowledged in the manuscript and the authors declare no competing interests.

CRediT author contributions

Ellen Barrowclift: Conceptualisation, Methodology, Formal analysis, Investigation, Validation, Data curation, Writing- Original draft preparation, Writing- Review & Editing, Visualisation, Funding acquisition; Jennifer S. Bigman: Formal analysis, Writing- Reviewing and Editing; Eric D. Digel: Formal analysis, Writing- Reviewing and Editing; Per Berggren: Writing- Reviewing and Editing, Supervision, Funding acquisition; Nicholas K. Dulvy: Conceptualisation, Methodology, Formal analysis, Investigation, Validation, Data curation, Writing- Original draft preparation, Writing- Review & Editing, Visualisation, Funding acquisition, Supervision.

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Tables

Table 1: The 11 models examined with associated hypotheses for how maximum intrinsic rate of population increase (r_{max}) varies with offspring
body mass ($M_{offspring}$), adult body mass M, inverse temperature $1/k_BT$, and depth. Comparison of models using corrected Akaike Information
Criteria (AICc), number of parameters (n), negative log-likelihood (-LL), adjusted R^2, difference in AICc from the top model (ΔAICc), and
Akaike weights. Models are ordered by ascending AICc, with models with AICc < 2 shown in bold.

Hypothesis	Model: ln(r_{max}) ~	n	-LL	AICc	R^2	Adj. R^2	ΔAICc	Weights
r_{max} varies with offspring body mass and depth	**ln($M_{offspring}$) + depth**	**3**	**-62.8**	**132**	**0.22**	**0.2**	**0**	**0.451**
r_{max} varies with offspring body mass and temperature	**ln($M_{offspring}$) + $1/k_BT$**	**3**	**-63**	**132.3**	**0.21**	**0.19**	**0.3**	**0.388**
r_{max} varies with offspring body mass only	ln($M_{offspring}$)	2	-65.4	135	0.17	0.16	3	0.101
r_{max} varies with adult body mass and temperature	ln(M) + $1/k_BT$	3	-66.1	138.5	0.14	0.12	6.5	0.017
r_{max} varies with adult body mass and depth	ln(M) + depth	3	-66.1	138.6	0.14	0.12	6.6	0.017
r_{max} varies with adult body mass and temperature, and the effect of mass scaling coefficient varies with temperature	ln(M) * $1/k_BT$	4	-65.7	139.8	0.16	0.13	7.8	0.009
r_{max} varies with adult body mass only	ln(M)	2	-68	140.2	0.1	0.09	8.2	0.007
r_{max} varies with adult body mass and depth, and the effect of mass scaling coefficient varies with depth	ln(M) * depth	4	-66.1	140.8	0.14	0.11	8.8	0.006
r_{max} varies with (inverse) temperature only	$1/k_BT$	2	-69.5	143.1	0.07	0.06	11.1	0.002
r_{max} varies with depth only	depth	2	-70.3	144.8	0.05	0.04	12.8	0.001
average r_{max} (i.e. intercept-only model)	1	1	-72.7	147.5	0	0	15.5	0

Figures

Figure 1. Biogeographic differences in the species richness of (A) skates (*n*=284 species of
Rajiformes), which have a more anti-tropical distribution, compared to (B) rays, which have
greater richness in the tropics (*n*=339 species of Torpediniformes, Rhinopristiformes and
Myliobatiformes), mapped to a hexagonal grid with cell size of ~ 23,322 km^2.

Figure 2: Relationship between adult to offspring size ratio (g) and adult mass (g) in log10
space for 85 rays (*n*=53, indicated by red points) and skates (*n*=32, indicated by blue points).
The grey bands around the fitted models show the confidence intervals and grey dashed lines
show adult to offspring size ratios of 1 to 4 where offspring size is 10 to 0.01% of adult body
mass, respectively.

Figure 3. Phylogeny, maximum intrinsic rate of population increase (r_{max}), adult and offspring mass (g), offspring to adult size ratio, depth (m), temperature (◦C) in log10 space for 85 rays (n=53, red points) and skates (n=32, blue points). Solid lines show median values. Uncertainty in r_{max} esti shown with 2.5% and 97.5% quantiles. Phylogenetic tree from Stein et al. (2018) (available on Vertlife.org) with binomial nomenclature updated to re current taxonomic nomencla

Figure 4. Relationships between offspring body mass and (a) adult body mass (with point
size showing median annual fecundity) and (b) median annual fecundity (with point size
showing adult mass) on a log10 scale for 53 rays (red points) and 32 skates (blue points).

Figure 5: Relationship between temperature (∘C) and a) offspring body mass (g) and b) adult
body mass (g) in log space for 85 rays (*n*=53, indicated by red points) and skates (*n*=32,
indicated by blue points). Median depth of occurrence (m) is shown by the point size, with a
linear model fitted to ray and skate data points. The grey bands around the fitted models show
the confidence intervals.

Figure 6: Coefficient plot showing the effect sizes for offspring body mass ($M_{offspring}$), depth,
and inverse temperature ($1/k_B T$) on r_{max} in the top two models. Error bars show the 95%
confidence intervals and effect sizes are considered significant when confidence intervals do
not overlap zero. The grey shaded box shows the expected effect size for temperature (-1.0 to
-0.6) based on metabolic theory.

Figure 7: Relationship between maximum intrinsic rate of population increase (r_{max}) and offspring body mass, showing the effects of either (a) depth or (b) environmental temperature for 85 rays (*n*=53, red points) and skates (*n*=32, blue points) in log10 space. Fitted lines show the predicted relationships for the two top models: (a) ln(r_{max}) ~ ln($M_{offspring}$) + depth for three depths (10, 500, 1000m) and (b) ln(r_{max}) ~ ln($M_{offspring}$) +   for three temperatures (6, 10, 20°C). Adult body mass is shown by the point size.