Spatially targeted inhibitory rhythms differentially affect neuronal integration

Drew B. Headley[1],*, Benjamin Latimer[2],*, Adin Aberbach[2], and Satish S. Nair[2]

AFFILIATIONS:
[1] Center for Molecular and Behavioral Neuroscience, Rutgers University – Newark, Newark, NJ, 07102, USA
[2] Electrical Engineering & Computer Science, University of Missouri, Columbia, MO, 65211, USA
* Contributed equally to this work

CORRESPONDENCE:
Satish S. Nair
Department of Electrical Engineering & Computer Science
University of Missouri, Columbia MO 65211
Phone: (573) 882-2964
E-Mail: nairs@missouri.edu
Website: https://nairs.mufaculty.umsystem.edu/

ABSTRACT
Pyramidal neurons form dense recurrently connected networks with multiple types of inhibitory interneurons. A major differentiator between interneuron subtypes is whether they synapse onto perisomatic or dendritic regions. They can also engender local inhibitory rhythms, beta (12-35 Hz) and gamma (40-80 Hz). The interaction between the rhythmicity of inhibition and its spatial targeting on the neuron may determine how it regulates neuronal integration. Thus, we sought to understand how rhythmic perisomatic and distal dendritic inhibition impacted integration in a layer 5 pyramidal neuron model with elaborate dendrites and Na^+, NMDA, and Ca^{2+} dendritic spikes. We found that inhibition regulated the coupling between dendritic spikes and action potentials in a location and rhythm-dependent manner. Perisomatic inhibition principally regulated action potential generation, while distal dendritic inhibition regulated the incidence of dendritic spikes and their temporal coupling with action potentials. Perisomatic inhibition was most effective when provided at gamma frequencies, while distal dendritic inhibition functioned best at beta. Moreover, beta modulated responsiveness to apical inputs in a phase-dependent manner, while gamma did so for basal inputs. These results may provide a functional interpretation for the reported association of soma-targeting parvalbumin positive interneurons with gamma, and dendrite-targeting somatostatin interneurons with beta.

INTRODUCTION

Cortical circuits are composed of sparsely connected networks of excitatory pyramidal neurons. To maintain a balanced level of excitability in the network, they form dense reciprocal connections with local inhibitory interneurons. The two largest subclasses of interneurons in the cortex are parvalbumin positive (PV) and somatostatin positive (SOM) cells [1]. A major distinction between PV and SOM interneurons is that they synapse onto different parts of the pyramidal neuron. PV tends to contact the soma and proximal dendrites (perisomatic), while SOM targets distal dendrites [2-5]. Many studies have identified differences in how they regulate the responsiveness of local excitatory principal neurons [6-8]. These differences could arise from their connectivity, intrinsic properties, or how they synapse onto pyramidal neurons. Indeed, the location of an inhibitory synapse qualitatively changes its effect on synaptic integration [5; 9-11].

Synaptic integration in pyramidal neurons arises from the interplay between passive and active ion channels and dendritic morphology [9; 12-14]. Dendrites produce regenerative spiking events, specifically Na^+, NMDA, and Ca^{2+} spikes. Their initiation depends upon the spatiotemporal coordination of excitatory synapses, and their interaction with the depolarization of dendritic branches. Incorporating just NMDA spikes into a model neuron radically increases the complexity of its dendritic integration [15]. Na^+ and NMDA spikes can drive somatic spiking in an *in vivo*-like model neuron [13]. A Ca^{2+} spike in the apical trunk converts a single somatic spike to a burst [9; 16], and may allow pyramidal neurons to act as multi-stage integrators [17; 18]. This complexity is only increased by including inhibition. The emission of bursts of action potentials is controlled by the timing and dendritic location of inhibition [9].

The rhythmicity of inhibition at distal dendrites can also affect somatic integration [19]. Reciprocal interactions between excitatory principal neurons and inhibitory interneurons gives rise to rhythmic activities (known as the PING mechanism). To initiate the rhythm, excitatory principal neurons activate inhibitory interneurons that deliver feedback inhibition to principal neurons. This transiently suppresses principal neuron firing. As the inhibition wanes, principal neurons resume their activity and reengage the inhibitory population, starting a new oscillatory cycle. Some evidence suggests that different interneuron subtypes pace rhythms at different frequencies, with gamma oscillations depending on PV [20-22], and beta oscillations on SOM [22].

Numerous cognitive processes are associated with these inhibitory rhythms in the cortex. Gamma oscillations are especially pronounced during stimulus presentation or behavioral initiation [23-25]. Beta rhythms occur during preparatory states or working memory [26; 27]. But fundamentally, these rhythms probably reflect different modes of local cortical activity and interregional communication [28-30]. For instance, gamma oscillations are associated with feedforward transmission of information in cortical circuits and beta oscillations may mediate feedback [28; 31]; but see [32].

Given all this, it is important to better understand how the complex integrative events in the dendritic tree are affected by the spatial targeting and rhythmicity of inhibition. Perhaps some rhythmic timescales are more effective in the dendrites, and others at the soma. Investigating this is beyond the reach of conventional experimental techniques. Moreover, computational models exploring how beta and gamma influence information processing have mostly relied upon simplified model neurons (e.g., [33; 34]). Thus, using a morphologically and biophysically detailed model layer 5 pyramidal neuron with Na^+, NMDA, and Ca^{2+} spikes, we investigated how perisomatic and distal dendritic inhibition impacted dendritic integration, and the modulation of these effects by beta and gamma rhythmicity.

RESULTS

Construction of a model cortical layer 5 pyramidal neuron

To study the effect of inhibitory rhythms on synaptic integration and somatic spiking, we adapted a previously published morphologically and biophysically detailed model of a cortical layer 5 pyramidal neuron (**Fig. 1A**; See methods for details). Modifications to the model were done in accordance with the published literature. In brief, this model featured a multicompartmental dendritic tree that produced dendritic Na^+, NMDA, and Ca^{2+} spikes, along with somatic action potentials that could backpropagate (**Fig. 1B**). We distributed conductance-based synapses across the dendritic and somatic compartments with an average density of 2.16 excitatory and 0.22 inhibitory contacts per µm. Presynaptic drivers of excitatory synapses were drawn from a pool of 5,200 point process sources that emulated correlated afferent drive with 2-8 synaptic contacts from the same presynaptic neuron. Inhibitory synapses were divided into two populations, those targeting the soma and proximal 100 µm of the dendrites (referred to as perisomatic), and those synapsing outside that area (referred to as distal). To capture excitatory/inhibitory (E/I) balance, a hallmark of cortical activity, the rate of inhibitory synaptic drive was a rescaled version of the rate of excitatory drive, lagged by 4 ms to emulate feedforward inhibition. Naturalistic presynaptic drive elicited a median firing rate of 5.3 Hz, in agreement with *in vivo* rates in cortex (**Fig. 1A** inset, [35]).

Dendrites were endowed with the following voltage-dependent conductances: a fast-inactivating Na^+ current (I_{NaT}), muscarinic K^+ current (I_m), fast non-inactivating K^+ current ($I_{Kv3.1}$), high voltage-activated Ca^{2+} current (I_{Ca_HVA}), low voltage-activated Ca^{2+} current (I_{Ca_LVA}), and Ca^{2+} activated K^+ current (I_{SK}). As a result, the basal and apical dendrites could generate Na^+ and NMDA spikes (**Fig. 1B**; [13]). Dendritic Na^+ spikes were regenerative events lasting less than 1 ms that were not preceded by somatic action potentials (**Fig. 1C1**; [36]). A Na^+ spike was detected when the dendritic Na^+ channel conductance (gNa) was higher than 0.3 mS/cm^2, except when this threshold was reached within 5 ms after a somatic action potential, to distinguish from backpropagating action potentials.

NMDA spikes occur when adjacent NMDA-bearing synapses were synergistically recruited by a combination of glutamatergic activation and local depolarization (**Fig. 1C2**; [18; 37]). They typically lasted between 20 and 80 ms. They were detected when a compartment's membrane voltage exceeded -40 mV for at least 26 ms and NMDA current exceeded -100 pA ms of charge.

Ca^{2+} spikes are depolarizations generated at the nexus of the apical trunk upon activation of voltage-gated Ca^{2+} channels (**Fig. 1C3**; [38; 39]). They lasted between 20 and 50 ms. To detect them, the membrane potential must exceed -40 mV for at least 26 ms, and the combined Ca^{2+} currents (LVA and HVA) had to be 1.3 times higher than when the voltage criterion was reached (t_v). The Ca^{2+} spike ended when this value fell to 1.15 times its value at t_v.

Altogether, under conditions that mirror *in vivo* afferent drive, our model reproduces the dendritic spikes of a layer 5 pyramidal neuron.

Relationship between dendritic and somatic spikes

Dendritic spikes induced by synaptic activity are the principal drivers of somatic action potentials. Prior experimental and modeling work has found this to be the case for layer 2/3 and layer 5 pyramidal neurons [13; 18; 40-42]. Layer 5 pyramidal neurons have a substantially longer apical trunk, which increases the electrotonic distance of their apical tuft from the soma (**Fig. 2A**), and diminishes the ability of tuft synapses to elicit action potentials. Voltage-gated Ca^{2+} channels at the apical nexus compensate for this by producing a robust Ca^{2+} spike that drives a burst of action potentials at the soma [17; 18]. Underscoring that Ca^{2+} spikes compensate for morphology, pyramidal neurons with shorter apical dendrites have weaker Ca^{2+} spikes that only elicit a single spike [43-45]. We thus assessed how dendritic spikes at different electronic distances from the

soma were related to action potential generation.
Dendritic compartments differed in their degree of passive electrical coupling to the soma
(i.e., electrotonic distance; **Fig. 2A**). We measured this by injecting a 20 Hz sinusoidal current in
each dendritic compartment, and then calculating the ratio of the membrane voltage response at
the soma over that at the dendrite. The apical trunk exhibited a relatively small attenuation ratio
of ~10%. Progressing distally into the apical tuft, attenuation reached 0.1%. Basal dendrites
showed greater attenuation than the apical trunk due to their smaller diameter. However, with an
attenuation ratio reaching ~1%, their distal tips were still electrotonically closer than the apical
tuft. Thus, large, and long-lasting changes in membrane potential, like those produced by dendritic
spikes, would be required to have any effect on the soma.
We examined this by measuring the spike-triggered average between somatic action
potentials and the presence of dendritic spikes across the dendritic tree. To simplify the complex
geometry of our model neuron, dendritic compartments were grouped into deciles by their
electrotonic distance, and whether they were on apical or basal branches. For each time lag from
the somatic action potential, we measured the percent change in dendritic spike incidence from
the mean rate across the entire simulation.
Dendritic Na^+ spikes increased 2-3 ms prior to somatic action potentials in both basal and
apical dendrites (**Fig. 2B**). This relationship was strongest for the compartments nearest the
soma, with the rate of Na^+ spikes in the apical trunk increasing 300% over baseline prior to
somatic action potentials, and 100% in basal compartments. This relationship fell off as the
dendritic spikes moved farther away from the soma, indicating that Na^+ spikes in distal branches
had little direct influence on somatic spiking.
The incidence of NMDA spikes increased ~25 ms prior to somatic action potentials, much
earlier than seen with dendritic Na^+ spikes (**Fig. 2C**). But, like dendritic Na^+ spikes, NMDA spikes
in the apical branch had a stronger coupling with somatic spiking than those in basal branches,
and this effect dropped with distance from the soma. NMDA spikes in the apical branch persisted
after an action potential, while those in basal dendrites did not, potentially because of the action
potential after-hyperpolarization.
Ca^{2+} spikes originate at the nexus of the apical dendrite. This region is electrotonically
close to the entire apical trunk, facilitating the propagation of Ca^{2+} spikes (**Fig. 3A**). In our model,
Ca^{2+} spike occurrence increased within 20 ms of somatic action potentials (**Fig. 3B**). Furthermore,
we found that NMDA spikes in the apical dendrites tended to precede Ca^{2+} spikes (**Fig. 3C**). Our
ionic current-based detection criteria allowed us to readily distinguish between these two
phenomena, despite their similar membrane voltage profiles. Since NMDA spikes in the apical
tuft normally have a weak relationship to somatic spiking (**Fig. 2D**), they may elicit somatic spiking
indirectly by driving Ca^{2+} spikes. Put another way, the apical nexus may serve as a thresholded
nonlinearity for NMDA spikes in the apical tuft to drive action potentials [18]. To test this, we
measured how a Ca^{2+} spike changed the spike-triggered average between apical tuft NMDA
spikes and action potentials (**Fig. 3D, top**). This revealed that action potentials preceded by a
Ca^{2+} spike (by up to 20 ms) had increased coupling with apical NMDA spikes. No such change
was seen in basal dendrites (**Fig. 3D, bottom**).
179
Effect of perisomatic and distal dendritic inhibition on controlling response gain
Subtypes of inhibitory interneurons synapse on distinct dendritic zones. PV interneurons mainly
synapse perisomatically, while SOM interneurons target distal dendrites [2-5]. These differences
may affect their modulation of synaptic integration [46], either by shifting the threshold for evoking
action potentials (a subtractive effect) or altering the slope of the relationship between excitation
and firing rate (a divisive effect). There is some disagreement about the degree to which PV and
SOM interneurons produce either of these effects [6-8], depending on the source of excitation
and local circuitry [47]. So, before we applied beta and gamma rhythmic inhibition in our model,
we studied the effect of tonically activating PV- and SOM-like inhibitory synapses.

To examine this, we doubled the rate of the inhibitory presynaptic drive onto either the PV-
targeted perisomatic compartments (somatic and dendritic compartments within 100 μm), or the
SOM-targeted distal (>100 μm) dendritic branches. Both decreased the firing rate of the pyramidal
cell from 5.5 Hz to less than 1 Hz (**Fig. 4A**; control: 5.5±0.85 Hz; distal: 0.20±0.15 Hz; perisomatic:
0.70±0.31 Hz; mean±SD). These comparable changes may reflect either subtractive or divisive
effects and could derive from different mechanisms.
To isolate these factors, we first assessed how doubling inhibition affected action potential
initiation at the soma. A series of current pulses were injected into the soma to measure the
relationship between firing rate and injected current (f-I curve), which captures the gain function
of the neuron (**Fig. 4B**). This revealed that both perisomatic and dendritic inhibition shifted the
current threshold for action potential initiation. Such an effect is subtractive. In addition,
perisomatic inhibition decreased the slope of the f-I relationship compared with the control, which
is consistent with a divisive effect.
Although perisomatic inhibition produced the strongest subtractive effect, distal dendritic
inhibition reduced firing rate the most (**Fig. 4A**). How can we reconcile these discordant findings?
One possibility is that distal inhibition substantially reduces Na^+, NMDA, or Ca^{2+} spikes. To
determine this, we examined the overall rate of dendritic spike events. Perisomatic inhibition did
not affect dendritic events compared to the control condition (**Fig. 4C-E**). By contrast, dendritic
inhibition decreased NMDA and Ca^{2+} spikes (**Fig. 4D,E**). Na^+ spikes were relatively unaffected
(**Fig. 4C**). This lack of effect may arise from a shortening of the inactivation for voltage-gated Na^+
channels balancing out the loss of excitatory drive.
210
Distinct excitation/inhibition balance effects of perisomatic and distal dendritic inhibition
The previous analysis found distinct effects on neuronal gain and dendritic spiking from tonic
changes in perisomatic and distal dendritic inhibition. But *in vivo* inhibition is dynamic and time
varying. PV and SOM interneurons form dense interconnections with local pyramidal neurons,
supplying time-lagged feedback inhibition. This helps maintain the balance of excitation and
inhibition (E/I) in the network by ensuring that an overall increase in excitatory activity is rapidly
counterbalanced by proportionate inhibition.
To emulate situations where E/I balance is important, we increased the dynamic variation
in excitatory drive (see Methods). As with the previous simulations, the rate of inhibitory synaptic
drive was a lagged and rescaled version of the overall excitation rate. Normally that lag is 4 ms,
in line with experimental estimates [48]. To probe whether perisomatic or distal dendritic inhibition
have distinct effects on E/I balance, we independently varied their lags (**Fig. 4F-I**). One was kept
at the nominal 4 ms lag, while the other was extended. Increasing either of their lags by 500 ms
produced obvious differences in the emission of dendritic spikes and their coordination with action
potentials (**Fig. 4F**). Normally dendritic spikes are evenly distributed in time and drive somatic
action potentials. Lagging distal dendritic inhibition clustered dendritic spikes together in time,
during which action potentials were emitted. Lagging perisomatic inhibition did not affect the
spacing of dendritic spikes, but decreased their coupling with somatic spiking.
We systematically characterized these lag effects for the following spiking events
modulated by tonic changes in inhibition: action potentials, Ca^{2+}, and NMDA spikes (**Fig. 4G**).
Increasing the lag of perisomatic inhibition lowered action potential firing, while for distal dendritic
inhibition, the firing rate decreased out to a lag of 125 ms, and then returned to normal at 500 ms.
To better understand these effects, we calculated the cross-correlation between dendritic spikes
and action potentials. Increasing the lag decreased the coordination between Ca^{2+} and somatic
spikes (**Fig. 4H**). For distal dendritic inhibition, this decrease was accompanied by a broadening
of their temporal relationship, while a sharp temporal relationship was maintained in the
perisomatic case. A similar pattern was observed with NMDA spikes on apical branches (**Fig. 4I**).
Basal branches, on the other hand, were relatively unaffected.

In summary, distal and perisomatic inhibition modulate the coupling between synaptic
drive and spiking through distinct processes. And while for both cases, the normal 4 ms E/I lag
produced maximal conversion of dendritic spiking events into action potentials, extending this lag
exerted distinct effects.
243
Effect of beta and gamma rhythmic inhibition on dendritic integration
The mechanisms modulating neuronal responsiveness during tonic inhibition of somatic and
dendritic compartments may extend to rhythmic inhibition. Thus, we emulated beta and gamma
rhythmic input (**Fig. 5A,F**). Depths of modulation were set to similarly entrain action potentials
(**Fig. 5B,G**), and were comparable to spontaneous and optogenetically-induced gamma and beta
bursts seen *in vivo* [49-52]. Beta rhythmic inhibition was modeled as a 16 Hz sinusoidally
modulated rate (20% depth) of the Poisson processes driving inhibitory synapses. Gamma
rhythmic inhibition was a 64 Hz sinusoidal modulation (40%) of inhibitory synapses. For both
cases, excitatory synaptic drive was a stable Poisson process.
Initially, we delivered beta rhythmic inhibition to the distal dendritic compartments, and
gamma to the perisomatic. Even though both rhythms produced similar depths of modulation of
somatic action potentials, the underlying causes were distinct. The phase of beta modulated the
occurrence of Ca^{2+}, NMDA, and Na^+ spikes, with each showing an ~75% depth of modulation with
respect to their mean level (**Fig. 5C-E**). These changes were seen across the entire dendritic tree,
spanning sites electrotonically close to and far from the soma. In addition, the impact on Na^+
spikes was unexpected (**Fig. 5E**), since delivery of the same inhibition tonically had little effect.
By contrast, gamma had virtually no effect on dendritic spikes (**Fig. 5F-H**). Its strongest impact
was on Na^+ spikes in basal dendritic compartments that were electronically close to the soma.
To uncover the modulation of action potentials by gamma, we turned our attention to
somatic action potential initiation (**Fig. 6**). For these analyses we divided the inhibitory rhythm into
two phases. During the *peak* phase, inhibition was greater than its mean rate, while during the
trough phase inhibition was lower (see **Fig. 5A,F**). We found that the somatic action potential
voltage threshold shifted lower during the 'trough' phase of gamma, when inhibition was at its
weakest (**Fig. 6A1**), and without any change in the mean membrane voltage (**Fig. 6A2**). This is
consistent with gamma phase modulating the shunting of voltage-gated Na^+ channel currents,
which occurs when GABAergic synapses co-locate with the channels mediating action potential
initiation [53]. We also observed changes in action potential initiation to beta rhythmic inhibition,
but through a different mechanism. During the 'peak' phase of beta, when inhibition was maximal,
the threshold for evoking an action potential increased, which may reflect an 'off-path' shunting of
excitatory current away from the soma and towards the dendrites (**Fig. 6B1;** [54]). Additionally,
there was a decrease in membrane voltage during the peak phase, which may correspond to
decreased excitation arising from the suppression of dendritic spikes (**Fig. 6B2**).
Accompanying these effects were changes in the rate of dendritic spikes compared with
the Poisson inhibition case. Beta increased the rate of Na^+ (+16.6%) and Ca^{2+} spikes (+15.1%)
but decreased the rate of NMDA spikes (-10.7%). Gamma caused no change in NMDA (+0.2%)
and a weak increase in Na^+ spikes (+6.4%), but a robust gain in Ca^{2+} spikes (+37.9%).
We next switched the portions of the pyramidal neuron targeted by the beta and gamma
rhythms. Beta rhythmic inhibition was delivered perisomatically and gamma rhythmic inhibition to
distal dendrites. While phase modulation of firing rate was maintained with both rhythms, the
overall level of spiking was dramatically reduced (**Fig. 5S1A,E**). Neither rhythm provided effective
modulation of Ca^{2+} or NMDA spikes (**Fig. 5S1B,C,F,G**). It is likely that the slow time scale of Ca^{2+}
and NMDA spikes, ~50 ms, is not optimal for the fast periodicity of the gamma rhythm, which
cycles every ~15 ms. In agreement with this, Na^+ spikes, which last less than 1 ms, did show
modulation by gamma rhythms delivered to the distal dendrites (**Fig. 5S1D,H**).
Swapping the location of beta and gamma synapses also altered their effects on somatic
excitability. Gamma rhythmic inhibition on the dendrites had minimal or no impact on action

potential threshold, but did shift the somatic membrane potential more negative (**Fig. 6S1A**). This
hyperpolarization was not dependent on gamma phase, and likely reflected an overall decrease
in the rate of dendritic spikes that could supply excitatory drive to the soma (NMDA: -26.1%, Na^+:
-12.2%, and Ca^{2+}: -39.9% compared with the Poisson inhibition case). By contrast, delivering beta
rhythmic inhibition to the soma raised the action potential threshold and hyperpolarized the
membrane potential during the peak phase (**Fig. 6S1B**). It also reduced the incidence of dendritic
spikes (NMDA: -17.1%, Na^+: -11.5%, and Ca^{2+}: -7.6%).
297    Putting all this together, the effectiveness of rhythmic inhibition depends on where it
298 impinges upon the neuron. Beta rhythms targeting the distal dendrites modulate the incidence of
299 dendritic spikes in a phase-dependent manner, while gamma rhythms delivered perisomatically
300 phase modulate somatic excitability. Swapping the locations of these rhythms diminishes these
301 effects and lowers overall excitability. Because of this, the subsequent simulations will be
302 restricted to the case of beta on distal dendrites and gamma on perisomatic compartments.
303
Modulation of dendritic spikes during oscillatory bursts
In vivo, beta and gamma rhythms occur as spontaneous bursts lasting less than a few hundred
milliseconds. Since the previous analyses relied on tonically delivered rhythms, we verified that
similar effects were observed with oscillatory bursts. Gamma and beta bursts were delivered to
the same model with mean depth of modulation similar to the tonic case (**Fig. 7A,F**; see Methods
for details).
310    Under the burst regime, both rhythms mirrored their behavioral effects. Gamma bursts
entrained spiking, with entrainment strongest during the middle of the burst (**Fig. 7B**). As with the
tonically imposed rhythm, there was none or minimal modulation of Ca^{2+} (**Fig. 7C**), NMDA (**Fig.
7D**), and Na^+ spikes (**Fig. 7E**). Beta rhythms entrained somatic action potentials (**Fig. 7G**), Ca^{2+}
spikes (**Fig. 7H**), NMDA (**Fig. 7I**), and Na^+ spikes (**Fig. 7J**). These modulations were evident
within the first few cycles of a burst, suggesting that they did not require a buildup or evolving
entrainment of an underlying process.
317
Effect of beta and gamma rhythms on responding to clustered synaptic drive
The results so far suggest that beta and gamma rhythms modulate synaptic integration through
different mechanisms depending on their phase and the location of the synapses on the dendritic
tree. To examine this further, we added patches of concentrated excitatory synaptic inputs onto
either the apical or basal dendrites (**Fig. 8A**), with densities similar to functional clusters *in vivo*
[55; 56]. Coactivated inputs were simulated by driving each synapse with a jittered (2 ms) Poisson
process. We ran six separate simulations, either with the apical or basal clusters engaged, and
under conditions of Poisson, beta, or gamma rhythmic inhibition.
326    To capture how beta and gamma influence synaptic integration we measured the cross-
correlation between presynaptic activations at the clustered input and somatic spiking. Separate
cross-correlograms were calculated depending on whether the presynaptic spikes occurred
during the peak or trough phase of the inhibitory rhythm. This necessarily introduced spurious
periodicities into the cross-correlogram that were compensated (see Methods for details). Relative
to the arhythmic Poisson inhibition case, beta rhythms enhanced the transmission of apical inputs
when inhibition was low (trough phase) and suppressed them when inhibition was high (peak
phase, **Fig. 8B, top left**). Basal inputs were either unaffected or moderately suppressed during
the trough and suppressed during the peak (**Fig. 8B, bottom left**). The opposite was the case for
gamma. It barely affected or moderately suppressed apical inputs (**Fig. 8B top right**), while basal
inputs were enhanced during the trough and suppressed during the peak (**Fig. 8B bottom right**).
337    Summarizing these results (**Fig. 8C**), we found that somatic spiking driven by clustered
338 basal synapses was bidirectionally modulated by gamma rhythms and suppressed by beta. On
339 the other hand, spiking driven by apical clusters was bidirectionally modulated by the beta rhythm

340   and suppressed by gamma. Thus, both rhythms regulate the sensitivity of pyramidal neurons to
341   afferents throughout the dendritic tree, but in a counterposed location-dependent manner.
342

DISCUSSION

Arising from multiple interneuron subtypes, inhibition sculpts pyramidal neuron activity by acting at different membrane regions and distinct rhythmic frequencies. Little was known about how these factors interact with the complexity of dendritic integration. To address this, we characterized the interaction between the location and rhythmicity of inhibition on integration in a morphologically and biophysically detailed layer 5 pyramidal neuron model with active dendrites. We found that distal dendritic inhibition modulated the occurrence of dendritic spikes, while perisomatic inhibition altered action potential generation. This translated into location-specific differences in the effectiveness of inhibitory rhythms. Beta rhythmic inhibition entrained dendritic spikes, focusing them into the phase when inhibition was at a minimum, but only when delivered to the distal dendrites. In contrast, gamma modulated the threshold for action potential initiation, but only when delivered perisomatically. As a likely result, beta oscillations bidirectionally controlled transmission in apical dendrites and suppressed those onto basal dendrites, while gamma oscillations did the opposite.

This indicates that the spatial targeting and timing of inhibition go hand in hand. Their alignment is thus fundamental to their distinct effects on neuronal integration. And in turn, this affects function at multiple levels, from synaptic responsiveness to neural coding, and microcircuit operation.

Synaptic responsiveness

Oscillatory rhythms potentially affect synaptic integration through several mechanisms. Early theorizing held that oscillations synchronize populations of excitatory neurons such that their efferent synapses benefit from spatiotemporal summation in eliciting action potentials [57]. Later it was proposed that if neurons in two regions exhibited coherent variations in their somatic membrane potentials, bringing them closer to or farther from action potential threshold, they could preferentially exchange activities [58]. Modeling and *in vitro* studies have shown that the phase of a sinusoidal current injected at the soma modulates the timing of evoked action potentials [59] or their probability of occurrence [60]. Similar gamma phase dependence has been found *in vivo* [61].

Rhythmic inhibition may also periodically modulate the sensitivity of the neuron to synaptic input. Inhibitory synapses achieve this by lowering the membrane resistance i.e., shunting [62]. This makes it harder for an excitatory synaptic current to drive the membrane voltage toward the action potential threshold. Indeed, optogenetically stimulating PV interneurons at gamma frequencies modulates the responsiveness of cortical neurons to sensory inputs in a phase-dependent manner [63]. However, normally PV interneurons are driven by local principal cells, so the inhibition they impose reflects the aggregate activity in the local network (leading to E/I balance, [64]). Model networks wired in this manner emit spontaneous gamma bursts that produce phase-dependent modulation of the relationship between EPSP amplitude and spiking probability, with a strong positive relationship during the trough of gamma, and a weak one during the peak [34]. Consistent with these results, putative monosynaptically connected pairs of single units recorded *in vivo* show an increase in spike transmission probability during the trough of gamma [65].

To summarize the present possibilities, oscillations could modulate a neuron's responsiveness by (1) synchronizing the synaptic inputs impinging upon it, (2) modulate how close the membrane potential is to the action potential threshold, or (3) vary its sensitivity to synaptic inputs via shunting inhibition.

Our results fill out this picture in two ways. First, we add a fourth mechanism, which is (4) the modulation of dendritic spiking events. Second, we found that beta and gamma oscillations differentially engaged these mechanisms. Beta oscillations primarily caused 2 via 4, and affected 3. Gamma, on the other hand, operated primarily through 3. It should be noted that to isolate these effects, our model had Poisson excitatory synaptic inputs, which precluded mechanism 1,

394 afferent synchrony. However, it is likely the degree of synchrony would impact both rhythms.
395 Supporting this, *in vivo* whole-cell recordings from neurons in mouse visual cortex exhibit brief
396 membrane depolarizations in synchrony with gamma [66].
397
Relevance to coding
Given that beta and gamma rhythms influence spiking via distinct mechanisms, they may also
differentially impact coding. During gamma bursts in V1, neurons show a stronger modulation of
their firing rate by the contrast of grating stimuli [67]. Gamma phase also modulates orientation
selectivity and correlated variability between neurons [68]. This enhancement is modulated by
attention [69]. Our results indicate that these effects reflect shifts in somatic sensitivity to
excitatory synaptic inputs.
Much less is known about the influence of beta oscillations on coding. In the visual cortex
of mice, activation of SOM interneurons increased with the visual stimulus size and homogeneity
([21], note that this study referred to the rhythm as low gamma). In a different study, using a
sequence working memory task in primates, the order of presented items corresponded to their
phase in the beta rhythm [70]. However, this does not indicate how coding varies with beta phase.
Considering our finding that beta synchronized dendritic spikes, it may operate by enabling the
summation of normally asynchronous afferents on distal dendrites, facilitating their ability to drive
somatic spiking.
413
Interaction with microcircuitry
Pyramidal neurons are embedded in a cortical column where they are sparsely connected
amongst themselves and densely connected with local interneurons. The dense connectivity with
interneurons is crucial for the generation of local beta and gamma rhythms [21; 22]. How might
this circuitry interact with the differential regulation of dendritic integration by beta and gamma?
We found that beta rhythms preferentially modulated a pyramidal neuron's response to
inputs on its apical dendrites. The apical tuft in the superficial layers of cortex primarily receives
long-range inputs from regions higher up in the cortical hierarchy [71; 72]. This makes beta
rhythms ideally positioned to modulate these top-down/feedback signals. Since the rhythm likely
derives from local activation of SOM interneurons, it is worth considering what situations would
activate those and how they might relate to the functioning of apical dendrites. SOM interneurons
receive facilitating synapses from local pyramidal neurons [73; 74], which would make them
especially sensitive to bursts of action potentials arising from Ca^{2+} spikes at the apical nexus [18].
Since Ca^{2+} spikes are driven by synaptic activation in the apical tuft, it is likely that beta rhythms
regulate the generation of action potential bursts arising from long-range inputs.
Our results indicated that gamma rhythms mainly affect processing in basal dendrites.
These are preferentially targeted by layer 5 pyramidal neurons, which sparsely interconnect with
projection-type specificity [75-77]. A confluence of evidence implicates PV interneurons in the
production of high-frequency inhibitory rhythms such as gamma [78; 79]. Given that PV
interneurons diffusely interconnect with local pyramidal neurons [80; 81], and the synapses they
receive from them are depressing [73; 74], they likely regulate abrupt increases in local ensemble
activity. Interactions within ensembles that precede activating the PV population will be boosted,
while those following will be attenuated.
437
Interneuron specializations and rhythmic timescales
Lastly, it is worth considering why beta and gamma rhythms are mediated by different types of
interneurons. One view is that the relative timing of their rhythms arises from the electrotonic
timescales of their feedback inhibition; SOM cells target distal dendrites and thus produce a
slower inhibitory feedback signal, versus the rapid perisomatic inhibition of PV cells. And when it
comes to explaining the emergence of PING rhythms at different timescales, this story is
sufficient, but incomplete.

We found that swapping the cellular compartments receiving beta and gamma rhythmic
inhibition impaired their effectiveness and lowered overall excitability. Thus, moving beyond mere
timing, our results suggest that the timescales of these rhythms align with the specialized impacts
of SOM and PV interneurons on neuronal integration.
449
Conclusion
For the most part, the study of beta and gamma rhythms has focused on their correlation
with task-related events and entrainment of neuronal firing. Fundamentally, these effects derive
from their influence on synaptic integration, which has multiple stages, from modulating the post-
synaptic response, inducing a dendritic spike, and triggering an action potential. Since beta and
gamma rhythms differentially impacted these processes, this invites a reappraisal of their role in
coding and communication, along with unveiling a new hypothesis space for understanding their
function.
458

REFERENCES

1. Tremblay R, Lee S, Rudy B (2016) Gabaergic interneurons in the neocortex: From cellular properties to circuits, Neuron 91, 260-292. PMC4980915.

2. Kawaguchi Y, Kubota Y (1997) Gabaergic cell subtypes and their synaptic connections in rat frontal cortex, Cereb Cortex 7, 476-486.

3. Wang Y, Toledo-Rodriguez M, Gupta A, Wu C, Silberberg G, Luo J, Markram H (2004) Anatomical, physiological and molecular properties of martinotti cells in the somatosensory cortex of the juvenile rat, J Physiol 561, 65-90. PMC1665344.

4. Kubota Y (2014) Untangling gabaergic wiring in the cortical microcircuit, Curr Opin Neurobiol 26, 7-14.

5. Kubota Y, Kondo S, Nomura M, Hatada S, Yamaguchi N, Mohamed AA, Karube F, Lübke J, Kawaguchi Y (2015) Functional effects of distinct innervation styles of pyramidal cells by fast spiking cortical interneurons, Elife 4. PMC4518632.

6. Wilson NR, Runyan CA, Wang FL, Sur M (2012) Division and subtraction by distinct cortical inhibitory networks in vivo, Nature 488, 343-348. PMC3653570.

7. Lee SH, Kwan AC, Zhang S, Phoumthipphavong V, Flannery JG, Masmanidis SC, Taniguchi H, Huang ZJ, Zhang F, Boyden ES, Deisseroth K, Dan Y (2012) Activation of specific interneurons improves v1 feature selectivity and visual perception, Nature 488, 379-383. PMC3422431.

8. Atallah BV, Bruns W, Carandini M, Scanziani M (2012) Parvalbumin-expressing interneurons linearly transform cortical responses to visual stimuli, Neuron 73, 159-170. PMC3743079.

9. Leleo EG, Segev I (2021) Burst control: Synaptic conditions for burst generation in cortical layer 5 pyramidal neurons, PLoS Comput Biol 17, e1009558.

10. Jadi M, Polsky A, Schiller J, Mel BW (2012) Location-dependent effects of inhibition on local spiking in pyramidal neuron dendrites, PLoS Comput Biol 8, e1002550. PMC3375251.

11. Ferguson KA, Cardin JA (2020) Mechanisms underlying gain modulation in the cortex, Nat Rev Neurosci 21, 80-92. PMC7408409.

12. Egger R, Narayanan RT, Guest JM, Bast A, Udvary D, Messore LF, Das S, de Kock CPJ, Oberlaender M (2020) Cortical output is gated by horizontally projecting neurons in the deep layers, Neuron 105, 122-137 e128. PMC6953434.

13. Goetz L, Roth A, Häusser M (2021) Active dendrites enable strong but sparse inputs to determine orientation selectivity, Proceedings of the National Academy of Sciences 118, e2017339118.

14. Ujfalussy BB, Makara JK, Lengyel M, Branco T (2018) Global and multiplexed dendritic computations under in vivo-like conditions, Neuron 100, 579-592.e575.

15. Beniaguev D, Segev I, London M (2021) Single cortical neurons as deep artificial neural networks, Neuron 109, 2727-2739.e2723.

16. Larkum ME, Zhu JJ, Sakmann B (1999) A new cellular mechanism for coupling inputs arriving at different cortical layers, Nature 398, 338-341.

17. Poirazi P, Brannon T, Mel BW (2003) Pyramidal neuron as two-layer neural network, Neuron 37, 989-999.

18. Larkum ME, Nevian T, Sandler M, Polsky A, Schiller J (2009) Synaptic integration in tuft dendrites of layer 5 pyramidal neurons: A new unifying principle, Science 325, 756-760.

19. Li X, Morita K, Robinson HP, Small M (2013) Control of layer 5 pyramidal cell spiking by oscillatory inhibition in the distal apical dendrites: A computational modeling study, J Neurophysiol 109, 2739-2756.

20. Sohal VS, Zhang F, Yizhar O, Deisseroth K (2009) Parvalbumin neurons and gamma rhythms enhance cortical circuit performance, Nature 459, 698-702.

509   21.   Veit J, Hakim R, Jadi MP, Sejnowski TJ, Adesnik H (2017) Cortical gamma band
510   synchronization through somatostatin interneurons, Nat Neurosci.
511   22.   Chen G, Zhang Y, Li X, Zhao X, Ye Q, Lin Y, Tao HW, Rasch MJ, Zhang X (2017)
512   Distinct inhibitory circuits orchestrate cortical beta and gamma band oscillations, Neuron
513   96, 1403-1418.e1406. PMC5864125.
514   23.   Headley DB, Weinberger NM (2013) Fear conditioning enhances γ oscillations and their
515   entrainment of neurons representing the conditioned stimulus, J Neurosci 33, 5705-
516   5717. PMC3645874.
517   24.   Murty D, Shirhatti V, Ravishankar P, Ray S (2018) Large visual stimuli induce two
518   distinct gamma oscillations in primate visual cortex, J Neurosci 38, 2730-2744.
519   PMC5852657.
520   25.   Muthukumaraswamy SD (2010) Functional properties of human primary motor cortex
521   gamma oscillations, J Neurophysiol 104, 2873-2885.
522   26.   Sanes JN, Donoghue JP (1993) Oscillations in local field potentials of the primate motor
523   cortex during voluntary movement, Proc Natl Acad Sci U S A 90, 4470-4474.
524   PMC46533.
525   27.   Lundqvist M, Rose J, Herman P, Brincat Scott L, Buschman Timothy J, Miller Earl K
526   (2016) Gamma and beta bursts underlie working memory, Neuron 90, 152-164.
527   28.   Bastos AM, Lundqvist M, Waite AS, Kopell N, Miller EK (2020) Layer and rhythm
528   specificity for predictive routing, Proc Natl Acad Sci U S A 117, 31459-31469.
529   PMC7733827.
530   29.   Bastos AM, Vezoli J, Bosman CA, Schoffelen J-M, Oostenveld R, Dowdall JR,
531   De Weerd P, Kennedy H, Fries P (2015) Visual areas exert feedforward and feedback
532   influences through distinct frequency channels, Neuron 85, 390-401.
533   30.   Michalareas G, Vezoli J, van Pelt S, Schoffelen JM, Kennedy H, Fries P (2016) Alpha-
534   beta and gamma rhythms subserve feedback and feedforward influences among human
535   visual cortical areas, Neuron 89, 384-397. PMC4871751.
536   31.   Vezoli J, Vinck M, Bosman CA, Bastos AM, Lewis CM, Kennedy H, Fries P (2021) Brain
537   rhythms define distinct interaction networks with differential dependence on anatomy,
538   Neuron 109, 3862-3878.e3865. PMC8639786.
539   32.   Vinck M, Uran C, Spyropoulos G, Onorato I, Broggini AC, Schneider M, Canales-
540   Johnson A (2023) Principles of large-scale neural interactions, Neuron 111, 987-1002.
541   33.   Tiesinga PH, Fellous JM, Salinas E, José JV, Sejnowski TJ (2004) Inhibitory synchrony
542   as a mechanism for attentional gain modulation, J Physiol Paris 98, 296-314.
543   PMC2872773.
544   34.   Feng F, Headley DB, Amir A, Kanta V, Chen Z, Paré D, Nair SS (2019) Gamma
545   oscillations in the basolateral amygdala: Biophysical mechanisms and computational
546   consequences, eNeuro 6, ENEURO.0388-0318.2018.
547   35.   Saiki A, Sakai Y, Fukabori R, Soma S, Yoshida J, Kawabata M, Yawo H, Kobayashi K,
548   Kimura M, Isomura Y (2018) In vivo spiking dynamics of intra- and extratelencephalic
549   projection neurons in rat motor cortex, Cereb Cortex 28, 1024-1038.
550   36.   Golding NL, Spruston N (1998) Dendritic sodium spikes are variable triggers of axonal
551   action potentials in hippocampal CA1 pyramidal neurons, Neuron 21, 1189-1200.
552   37.   Schiller J, Major G, Koester HJ, Schiller Y (2000) NMDA spikes in basal dendrites of
553   cortical pyramidal neurons, Nature 404, 285-289.
554   38.   Schiller J, Schiller Y, Stuart G, Sakmann B (1997) Calcium action potentials restricted to
555   distal apical dendrites of rat neocortical pyramidal neurons, J Physiol 505 (Pt 3), 605-
556   616. PMC1160039.
557   39.   Larkum ME, Zhu JJ (2002) Signaling of layer 1 and whisker-evoked Ca^{2+} and Na^+ action
558   potentials in distal and terminal dendrites of rat neocortical pyramidal neurons in vitro
559   and in vivo, J Neurosci 22, 6991-7005. PMC6757874.

560   40.   Smith SL, Smith IT, Branco T, Häusser M (2013) Dendritic spikes enhance stimulus
561   selectivity in cortical neurons in vivo, Nature 503, 115-120. PMC6319606.
562   41.   Helmchen F, Svoboda K, Denk W, Tank DW (1999) In vivo dendritic calcium dynamics
563   in deep-layer cortical pyramidal neurons, Nat Neurosci 2, 989-996.
564   42.   Xu NL, Harnett MT, Williams SR, Huber D, O'Connor DH, Svoboda K, Magee JC (2012)
565   Nonlinear dendritic integration of sensory and motor input during an active sensing task,
566   Nature 492, 247-251.
567   43.   Fletcher LN, Williams SR (2019) Neocortical topology governs the dendritic integrative
568   capacity of layer 5 pyramidal neurons, Neuron 101, 76-90.e74.
569   44.   Gidon A, Zolnik TA, Fidzinski P, Bolduan F, Papoutsi A, Poirazi P, Holtkamp M, Vida I,
570   Larkum ME (2020) Dendritic action potentials and computation in human layer 2/3
571   cortical neurons, Science 367, 83-87.
572   45.   Larkum ME, Waters J, Sakmann B, Helmchen F (2007) Dendritic spikes in apical
573   dendrites of neocortical layer 2/3 pyramidal neurons, J Neurosci 27, 8999-9008.
574   PMC6672209.
575   46.   Doiron B, Longtin A, Berman N, Maler L (2001) Subtractive and divisive inhibition: Effect
576   of voltage-dependent inhibitory conductances and noise, Neural Comput 13, 227-248.
577   47.   Seybold BA, Phillips EAK, Schreiner CE, Hasenstaub AR (2015) Inhibitory actions
578   unified by network integration, Neuron 87, 1181-1192. PMC4635400.
579   48.   Wehr M, Zador AM (2003) Balanced inhibition underlies tuning and sharpens spike
580   timing in auditory cortex, Nature 426, 442-446.
581   49.   Amir A, Headley DB, Lee SC, Haufler D, Pare D (2018) Vigilance-associated gamma
582   oscillations coordinate the ensemble activity of basolateral amygdala neurons, Neuron
583   97, 656-669.e657. PMC5809002.
584   50.   Onorato I, Neuenschwander S, Hoy J, Lima B, Rocha KS, Broggini AC, Uran C,
585   Spyropoulos G, Klon-Lipok J, Womelsdorf T, Fries P, Niell C, Singer W, Vinck M (2020)
586   A distinct class of bursting neurons with strong gamma synchronization and stimulus
587   selectivity in monkey v1, Neuron 105, 180-197.e185.
588   51.   Adesnik H (2018) Layer-specific excitation/inhibition balances during neuronal
589   synchronization in the visual cortex, J Physiol 596, 1639-1657. PMC5924838.
590   52.   Murthy VN, Fetz EE (1992) Coherent 25- to 35-hz oscillations in the sensorimotor cortex
591   of awake behaving monkeys, Proc Natl Acad Sci U S A 89, 5670-5674. PMC49354.
592   53.   Rojas P, Akrouh A, Eisenman LN, Mennerick S (2011) Differential effects of axon initial
593   segment and somatodendritic gabaa receptors on excitability measures in rat dentate
594   granule neurons, J Neurophysiol 105, 366-379. PMC3023370.
595   54.   Gidon A, Segev I (2012) Principles governing the operation of synaptic inhibition in
596   dendrites, Neuron 75, 330-341.
597   55.   Iacaruso MF, Gasler IT, Hofer SB (2017) Synaptic organization of visual space in
598   primary visual cortex, Nature 547, 449-452. PMC5533220.
599   56.   Fu M, Yu X, Lu J, Zuo Y (2012) Repetitive motor learning induces coordinated formation
600   of clustered dendritic spines in vivo, Nature 483, 92-95. PMC3292711.
601   57.   Salinas E, Sejnowski TJ (2000) Impact of correlated synaptic input on output firing rate
602   and variability in simple neuronal models, J Neurosci 20, 6193-6209. PMC6772574.
603   58.   Fries P (2005) A mechanism for cognitive dynamics: Neuronal communication through
604   neuronal coherence, Trends Cogn Sci 9, 474-480.
605   59.   Hopfield JJ (1995) Pattern recognition computation using action potential timing for
606   stimulus representation, Nature 376, 33-36.
607   60.   Volgushev M, Chistiakova M, Singer W (1998) Modification of discharge patterns of
608   neocortical neurons by induced oscillations of the membrane potential, Neuroscience 83,
609   15-25.

61. Vinck M, Lima B, Womelsdorf T, Oostenveld R, Singer W, Neuenschwander S, Fries P
(2010) Gamma-phase shifting in awake monkey visual cortex, J Neurosci 30, 1250-
1257. PMC6633799.
62. Prescott SA, De Koninck Y (2003) Gain control of firing rate by shunting inhibition: Roles
of synaptic noise and dendritic saturation, Proc Natl Acad Sci U S A 100, 2076-2081.
PMC149961.
63. Cardin JA, Carlen M, Meletis K, Knoblich U, Zhang F, Deisseroth K, Tsai LH, Moore CI
(2009) Driving fast-spiking cells induces gamma rhythm and controls sensory responses,
Nature 459, 663-667.
64. Ferguson BR, Gao WJ (2018) Pv interneurons: Critical regulators of e/i balance for
prefrontal cortex-dependent behavior and psychiatric disorders, Front Neural Circuits 12,
37. PMC5964203.
65. Headley DB, Kyriazi P, Feng F, Nair S, Pare D (2021) Gamma oscillations in the
basolateral amygdala: Localization, microcircuitry, and behavioral correlates, J Neurosci
41, 6087-6101. PMC8276735.
66. Perrenoud Q, Pennartz CM, Gentet LJ (2016) Membrane potential dynamics of
spontaneous and visually evoked gamma activity in V1 of awake mice, PLoS Biol 14,
e1002383. PMC4758619.
67. Perrenoud Q, Fonseca AHdO, Airhart A, Bonanno J, Mao R, Cardin JA (2022) Flexible
perceptual encoding by discrete gamma events, bioRxiv, 2022.2005.2013.491832.
68. Womelsdorf T, Lima B, Vinck M, Oostenveld R, Singer W, Neuenschwander S, Fries P
(2012) Orientation selectivity and noise correlation in awake monkey area v1 are
modulated by the gamma cycle, Proc Natl Acad Sci U S A 109, 4302-4307.
PMC3306673.
69. Lisitsyn D, Grothe I, Kreiter AK, Ernst UA (2020) Visual stimulus content in v4 is
conveyed by gamma-rhythmic information packages, J Neurosci 40, 9650-9662.
PMC7726541.
70. Siegel M, Warden MR, Miller EK (2009) Phase-dependent neuronal coding of objects in
short-term memory, Proc Natl Acad Sci U S A 106, 21341-21346. PMC2779828.
71. D'Souza RD, Burkhalter A (2017) A laminar organization for selective cortico-cortical
communication, Front Neuroanat 11, 71. PMC5572236.
72. Harris JA, Mihalas S, Hirokawa KE, Whitesell JD, Choi H, Bernard A, Bohn P, Caldejon
S, Casal L, Cho A, Feiner A, Feng D, Gaudreault N, Gerfen CR, Graddis N, Groblewski
PA, Henry AM, Ho A, Howard R, Knox JE, Kuan L, Kuang X, Lecoq J, Lesnar P, Li Y,
Luviano J, McConoughey S, Mortrud MT, Naeemi M, Ng L, Oh SW, Ouellette B, Shen E,
Sorensen SA, Wakeman W, Wang Q, Wang Y, Williford A, Phillips JW, Jones AR, Koch
C, Zeng H (2019) Hierarchical organization of cortical and thalamic connectivity, Nature
575, 195-202. PMC8433044.
73. Beierlein M, Gibson JR, Connors BW (2003) Two dynamically distinct inhibitory networks
in layer 4 of the neocortex, J Neurophysiol 90, 2987-3000.
74. Campagnola L, Seeman SC, Chartrand T, Kim L, Hoggarth A, Gamlin C, Ito S, Trinh J,
Davoudian P, Radaelli C, Kim MH, Hage T, Braun T, Alfiler L, Andrade J, Bohn P, Dalley
R, Henry A, Kebede S, Alice M, Sandman D, Williams G, Larsen R, Teeter C, Daigle TL,
Berry K, Dotson N, Enstrom R, Gorham M, Hupp M, Dingman Lee S, Ngo K, Nicovich
PR, Potekhina L, Ransford S, Gary A, Goldy J, McMillen D, Pham T, Tieu M, Siverts L,
Walker M, Farrell C, Schroedter M, Slaughterbeck C, Cobb C, Ellenbogen R, Gwinn RP,
Keene CD, Ko AL, Ojemann JG, Silbergeld DL, Carey D, Casper T, Crichton K, Clark M,
Dee N, Ellingwood L, Gloe J, Kroll M, Sulc J, Tung H, Wadhwani K, Brouner K, Egdorf T,
Maxwell M, McGraw M, Pom CA, Ruiz A, Bomben J, Feng D, Hejazinia N, Shi S, Szafer
A, Wakeman W, Phillips J, Bernard A, Esposito L, D'Orazi FD, Sunkin S, Smith K, Tasic
B, Arkhipov A, Sorensen S, Lein E, Koch C, Murphy G, Zeng H, Jarsky T (2022) Local

661   connectivity and synaptic dynamics in mouse and human neocortex, Science 375,
662   eabj5861. PMC9970277.

75.   Kawaguchi Y (2017) Pyramidal cell subtypes and their synaptic connections in layer 5 of
rat frontal cortex, Cereb Cortex 27, 5755-5771.

76.   Morishima M, Morita K, Kubota Y, Kawaguchi Y (2011) Highly differentiated projection-
specific cortical subnetworks, J Neurosci 31, 10380-10391. PMC6623049.

77.   Morishima M, Kawaguchi Y (2006) Recurrent connection patterns of corticostriatal
pyramidal cells in frontal cortex, J Neurosci 26, 4394-4405. PMC6674016.

78.   Buzsáki G, Wang X-J (2012) Mechanisms of gamma oscillations, Annu Rev Neurosci
35, 203-225.

79.   Fernandez-Ruiz A, Sirota A, Lopes-Dos-Santos V, Dupret D (2023) Over and above
frequency: Gamma oscillations as units of neural circuit operations, Neuron 111, 936-
953. PMC7614431.

80.   Packer AM, Yuste R (2011) Dense, unspecific connectivity of neocortical parvalbumin-
positive interneurons: A canonical microcircuit for inhibition?, J Neurosci 31, 13260-
13271. PMC3178964.

81.   Morishima M, Kobayashi K, Kato S, Kawaguchi Y (2017) Segregated excitatory-
inhibitory recurrent subnetworks in layer 5 of the rat frontal cortex, Cereb Cortex 27,
5846-5857. PMC5905586.

680
681

FIGURES

Figure 1: A model layer 5 pyramidal neuron with active dendrites. **(A)** The morphology of the neuron. Virtual recordings can be obtained from any desired compartment (colored pipettes). Inset, naturalistic presynaptic activity drives firing rates in our model like those in vivo. Each black cross is the mean rate for a different simulation. **(B)** Examples of membrane potentials recorded simultaneously across the dendritic tree (in color) and soma (black) during naturalistic drive. Regenerative events are indicated with arrows or text (AP: action potential, bAP: backpropagating action potential). **(C1-3)** Demonstration of our detection of dendritic spike events (top) and characterization of their properties (bottom). Events are binned according to the properties that were used in their detection. Bin edges for the event durations were not evenly set for panels **C2** and **C3**.

Figure 2: Influence of Na^+ and NMDA spikes on action potential generation. **(A)** Electrotonic distance between each dendritic compartment and the soma. **(B)** Dendritic compartments were grouped by their type (apical or basal) and electrotonic distance (percentile) from the soma. The percent change in Na^+ spike presence in those compartments relative to somatic spiking. Na^+ spikes increased immediately prior to action potentials in dendritic compartments that were electrotonically close to the soma. **(C)** Same format as **B**, but for NMDA spikes. These showed a similar degree of change, but a broader temporal coupling.

Figure 3: Influence of Ca^{2+} spikes on action potential generation, and their behavior as a second integrative mechanism. **(A)** Electrotonic distance between dendritic compartments and the apical nexus, where Ca^{2+} spikes are generated. **(B)** Change in the incidence of Ca^{2+} spikes at the nexus surrounding action potentials. **(C)** Percent change in NMDA spike presence in the apical dendrites centered on Ca^{2+} spike initiation. **(D)** Percent change in NMDA spike coupling with action potentials during Ca^{2+} spikes. Top, NMDA spikes in apical dendrites were more strongly coupled with action potentials during Ca^{2+} spikes. Bottom, this was not the case for basal dendrites.

Figure 4: Distal dendritic and perisomatic inhibition reduce action potential generation through different mechanisms. **(A)** Action potential rate during periods with normal inhibitory tone (Control), double rate on Distal branches, or double rate on Perisomatic. Both increases in inhibition dramatically reduced the firing of somatic action potentials. **(B)** Somatic excitability was measured by delivering current steps during the control, distal, and perisomatic inhibition states. Left, example somatic voltage responses to current steps. Right, spike frequency versus current (f-I) curve for each condition. The threshold for evoking an action potential shifted with 2X distal and perisomatic inhibition. Perisomatic, but not dendritic, inhibition changed the f-I slope (compare dashed lines with solid black). **(C)** Impact of altered dendritic inhibition on rate of Na^+ spikes in apical and basal dendrites. **(D)** Same format as **c**, but for NMDA spikes. **(E)** Rate of Ca^{2+} spikes in the apical dendrites. Basal dendrites lacked Ca^{2+} spikes and were excluded. All error bars are mean ± standard deviation. **(F)** Examples of membrane potential recorded in control (top), and both distal (middle) and proximal (bottom) inhibition lagged by 500 ms. **(G)** Change in firing rate for control (black dot) and for perisomatic (blue) and distal (red) lags in inhibition from 0 to 500 ms. **(H)** Change in incidence of Ca^{2+} spikes for distal (red, top) and proximal (blue, bottom) inhibition. The control case is shown in black in both panels. **(I)** Same as (H) but for NMDA spikes.

Figure 5: Phase-dependent effects of beta and gamma rhythmic inhibition on dendritic spikes. **(A)** Example data from the beta rhythmic inhibition simulation. Top, presynaptic spike counts. Bottom, voltage traces from somatic and dendritic compartments. Grayed periods are when inhibitory presynaptic spikes are peaking. **(B)** Action potential rate as a function of the phase of the beta rhythm. Dashed gray line shows the modulation of inhibitory drive with respect to phase.

(C) Percent change in Ca^{2+} spike presence at apical nexus by beta phase. **(D1-2)** Percent change of NMDA spike presence in apical (1) and basal (2) dendrites stratified by electronic distance from the soma. **(E1-2)** Same as **C**, but for Na^+ spikes. **(F, G, H, I1-2, J1-2)** Same format as above, but with events binned by the phase of gamma rhythmic inhibition. For all graphs phase is given in radians with inhibition at a minimum for -π and maximum at 0.

Figure 5, Supplementary 1: Phase-dependent effects on dendritic spikes of beta and gamma rhythmic inhibition delivered to opposite areas of the neuron. Beta was delivered perisomatically, while gamma was supplied to the distal dendrites. **(A)** Action potential rate as a function of the phase of the beta rhythm. Dashed gray line shows the modulation of inhibitory drive with respect to phase. **(B)** Percent change in Ca^{2+} spike presence at apical nexus by beta phase. **(C1-2)** Percent change of NMDA spike presence in apical (1) and basal (2) dendrites stratified by electronic distance from the soma. **(D1-2)** Same as **C**, but for Na^+ spikes. **(E, F, G1-2, H1-2)** Same format as above, but with events binned by the phase of gamma rhythmic inhibition. For all graphs phase is given in radians with inhibition at a minimum for -π and maximum at 0.

Figure 6: Phase-dependent effects of gamma and beta rhythmic inhibition on somatic excitability. **(A1)** A cumulative probability plot of the distribution of somatic membrane potentials 1ms prior to an action potential, sorted by whether they occurred during the gamma phase with maximal (Peak, red line) or minimal (Trough, blue line) inhibitory drive. Poisson (black) had no rhythmic modulation, but the same mean inhibitory rate. **(A2)** Probability distribution of somatic membrane voltage as a function gamma phase, normalized to the peak probability value. Lines have the same color scheme as in **A1**. **(B1)** Same format as **A1**, but for the beta rhythm. **(B2)** Same format as **A2**, but for the beta rhythm.

Figure 6, Supplementary 1: Phase-dependent effects on somatic excitability of beta and gamma rhythmic inhibition delivered to opposite areas of the neuron. Beta was delivered perisomatically, while gamma was supplied to the distal dendrites. **(A1)** A cumulative probability plot of the distribution of somatic membrane potentials 1ms prior to an action potential, sorted by whether they occurred during the gamma phase with maximal (Peak, red line) or minimal (Trough, blue line) inhibitory drive. Poisson (black) had no rhythmic modulation, but the same mean inhibitory rate. **(A2)** Probability distribution of somatic membrane voltage as a function gamma phase, normalized to the peak probability value. Lines have the same color scheme as in **A1**. **(B1)** Same format as **A1**, but for the beta rhythm. **(B2)** Same format as **A2**, but for the beta rhythm.

Figure 7: Phase-dependent effects of gamma and beta bursts on dendritic spikes. **(A)** Example data from the gamma rhythmic inhibition simulation. Top, Somatic potential (black line), with firing rate of perisomatic inhibitory synapses (blue line). Middle, voltage trace of apical compartment. Bottom, voltage trace of basal compartment. **(B)** Action potential rate as a function of the phase of the gamma rhythm. Blue line shows the modulation of inhibitory drive with respect to phase. **(C)** Percent change in Ca^{2+} spike presence at apical nexus by gamma phase. **(D1-2)** Percent change of NMDA spike presence in apical (1) and basal (2) dendrites stratified by electronic distance from the soma. **(E1-2)** Same as **C**, but for Na^+ spikes. **(F, G, H, I1-2, J1-2)** Same format as above, but with events binned by the phase of beta rhythmic inhibition. For all graphs cycle number is given relative to the amplitude peak of the burst.

Figure 8: Effect of beta and gamma rhythms on responsiveness to synaptic inputs targeting distinct regions of the dendritic tree. **(A)** Schematic of the location for clustered excitatory synaptic inputs. **(B)** Normalized cross-correlation between synaptic drive onto a clustered input and spiking at the soma, stratified by whether the presynaptic spike arrived during the Peak (red line) or Trough (blue line) of the rhythm. Solid bars correspond to the Poisson stimulation case where

inhibition was not rhythmically modulated. Top left, effect of beta on apical inputs. Top right, effect
of gamma on apical inputs. Bottom left, effect of beta on basal inputs. Bottom right, effect of
gamma on basal inputs. **(C)** Summary of effects in panel **B** where the strength of each normalized
cross-correlation was measured as its area under the curve. Dots are connected by dashed gray
lines if the data points came from the same simulation but at different phases of the rhythm. Solid
horizontal lines reflect the cross-correlation strength in the Poisson inhibitory case (no
rhythmicity).
791
792

METHODS

We adapted a previously published model of a L5 pyramidal neuron [1; 2] to the Brain Modeling Toolkit [3] format to facilitate reproducibility. This open-source software utilized NEURON 7.7 [4] with an integration time step of 0.1 ms for simulating the membrane potential. We added synapses and designed inputs in accordance with the literature to study synaptic integration in vivo. Details of the passive membrane properties and active conductances are only described briefly (full details can be found in [2]). Our focus here is on describing the enhancements we incorporated to mimic in vivo features in the model neuron.

L5 pyramidal cell compartmental model

Briefly, the cell was built on a morphological reconstruction of a L5 pyramidal tract neuron and included 10 active Hodgkin-Huxley conductances with kinetics taken from the literature [2]. These channels were a fast-inactivating Na$^+$ current (I_{NaT}), persistent Na$^+$ current (I_{NaP}), non-specific cation current (I_h), muscarinic K$^+$ current (I_m), slow inactivating K$^+$ current (I_{Kp}), fast inactivating K$^+$ current (I_{Kt}), fast non-inactivating K$^+$ current ($I_{Kv3.1}$), high voltage-activated Ca^{2+} current (I_{Ca_HVA}), low voltage-activated Ca^{2+} current (I_{Ca_LVA}), and Ca^{2+} activated K$^+$ current (I_{SK}). The somatic compartments contained all of these channels except I_m. Both the apical and basal dendrite compartments contained I_{Ca_LVA}, I_{Ca_HVA}, I_{SK}, $I_{Kv3.1}$, I_{NaT}, I_m, and I_h. The membrane capacitance was set to 1 μF/cm^2 for the soma and axon and 2 μF/cm^2 for the basal and apical dendrites to correct for dendritic spine area. Axial resistance was set to 100 W-cm and leak reversal potential was -90 mV.

Divergence, probability of transmission, and functional clustering

Experimental studies indicate that each presynaptic excitatory neuron forms 2-8 synapses with its pyramidal partners, with a release probability between 0.16 and 0.9 [5]. Further, the 2-8 synaptic contacts occur over a span of 20-100 μm [6]). We constrained our model to have these properties. In addition, since synapses may cluster on dendritic branches such that functional presynaptic cell assemblies activate the same branch within 5-10 μm [7; 8], we forced synapses coming from the same presynaptic cell assembly to cluster in this way. In summary, a single presynaptic input fiber could have 2-8 synapses, drawn from a uniform distribution with a release probability between 0.16 and 0.9, also drawn from a uniform distribution [5]. And the synapses from a functional group formed clusters within 5-10μm on the same dendritic branch over a span of 100 μm.

Synaptic conductances

We randomly distributed excitatory synaptic conductances following previous modeling work [9]. Maximum conductance values followed a log-normal distribution with a mean of 0.2 nS and standard deviation of 0.345 nS for excitatory synaptic conductances. Inhibitory synaptic conductances were fixed at 1 nS [1]. We validated these conductances against excitatory and inhibitory post-synaptic currents measured *in vitro.* The model's values are compared with experimental values in Table 1.

Synapse Density

Synapse density was based on a comprehensive report [10] that not only quantified the number of spines but also counted the synapses by identifying vesicle clouds and postsynaptic density using serial block-face electron microscopy. The authors found the apical tuft synapse density per micron as 2.16 ± 0.16 for excitatory and 0.22 ± 0.02 for inhibitory synapses (mean ± standard error of the mean). Other studies that only quantified spine density may undercount the true number of synapses by about 3 times because one can only count lateral spines, not

those in the z-axis [11]. With that adjustment, the other values reported – 0.47 ± 0.01 spines/μm
[12] and 0.53 ± 0.05 spines/μm [13]– are roughly in alignment with that in [10]. We used the
values from [10] for excitatory synapse density because we found the higher value for excitatory
synapse density was needed to achieve a reasonable baseline firing rate.
Morphological measurements (length of dendritic cable in μm) combined with these
synapse density estimates yield the following estimates for total number of synapses:
Excitatory: 16070 (2.16 syns/μm * 7440 μm) on apical dendrites and 10042 (2.16 syns/μm *
4649 μm) on basal dendrites. Inhibitory: 150 on soma [1; 14; 15] + (0.22 syns/μm *483 mm) =
256 perisomatic, 1637 (0.22 syns/μm * 7440 μm) on apical dendrites, 1023 (0.22 syns/μm *
4649 μm) on basal dendrites.
853
Synaptic kinetics and short-term plasticity
All excitatory transmission was mediated by AMPA/NMDA receptors and inhibitory transmission
by GABA$_A$ receptors as in our prior models. The rise/decay constants for the excitatory
connections were as follows: Rise/decay time constants of 0.6/6.9 ms for AMPA, and 3.7/125
ms for NMDA synapses, and a reversal potential of 0 for both. And for the inhibitory GABA-ergic
connections, the rise/decay time constants were 0.5 and 6.8 ms, respectively, with a reversal
potential of -75 mV. We implemented short-term depression in both the excitatory and inhibitory
synapses [16] via an exponential decay of synaptic weight over short time scales [17]. Following
[16] we calculated a short-term plasticity (STP) train-induction value by applying 8 pulses at 50
Hz to the synapse while in voltage clamp and measured the resulting postsynaptic current
(PSC). The 6th, 7th, and 8th PSCs were averaged, and the 1st PSC was subtracted from the
result. This value was divided by the max PSC current to yield the STP train-induction value.
Excitatory synapses to L5 pyramidal neurons had an STP train-induction value of -0.34.
Inhibitory synapses arising from PV+ basket interneurons making perisomatic contact had a
value of -0.60 and inhibitory synapses arising from SOM+ interneurons making dendritic contact
had a value of -0.10. The equations to model the synaptic currents and short-term depression
are provided in the next section.
871
872 *Modeling of synaptic currents*
873 The corresponding synaptic currents were modeled by dual exponential functions [18; 19]. All
874 excitatory transmission was mediated by AMPA/NMDA receptors and inhibitory transmission by
875 GABA$_A$ receptors. The corresponding synaptic currents were modeled by dual exponential
876 functions [18; 19], as shown in eqns. 1-3,
877

$$I_{AMPA} = w \times G_{AMPA} \times (V - E_{AMPA})$$
$$G_{AMPA} = g_{AMPA,max} \times D_{AMPA} \times r_{AMPA}$$
$$r_{AMPA}' = \alpha Tmax_{AMPA} \times ON_{AMPA} \times (1 - r_{AMPA}) - \beta_{AMPA} \times r_{AMPA} \quad (1)$$

$$I_{NMDA} = w \times G_{NMDA} \times (V - E_{NMDA})$$
$$G_{NMDA} = g_{NMDA,max} \times D_{NMDA} \times s(V) \times r_{NMDA}$$
$$r_{NMDA}' = \alpha Tmax_{NMDA} \times ON_{NMDA} \times (1 - r_{NMDA}) - \beta_{NMDA} \times r_{NMDA} \quad (2)$$

$$I_{GABAa} = w \times G_{GABAa} \times (V - E_{GABAa})$$
$$G_{GABAa} = g_{GABAa,max} \times D_{GABAa} \times r_{GABAa}$$
$$r_{GABAa}' = \alpha Tmax_{GABAa} \times ON_{GABAa} \times (1 - r_{GABAa}) - \beta_{GABAa} \times r_{GABAa} \quad (3)$$

where *V* is the membrane potential (mV) of the compartment (dendrite or soma) where the
synapse is located, *I* is the current injected into the compartment (nA), *G* is the synaptic

conductance (µS), w is the synaptic weight (unitless), and E is the reversal potential of the
synapse (mV). $g_{x,max}$ is the maximal conductance (µS), D implements short-term plasticity as
defined below, and r_x determines the synaptic current rise and decay time constants based on
the terms $\alpha Tmax$ and β [18]. The voltage-dependent variable $s(V)$ which implements the Mg^{2+}
block was defined as: $s(V) = [1 + 0.33 \exp(-0.06\ V)]^{-1}$ [20]. The terms ON_{NMDA} and ON_{AMPA} are
set to 1 if the corresponding receptor is open, else to 0. To calculate the factor D for depression:
$\tau\_D*dD/dt=1-D$ and D constrained to be ≤ 1. After each stimulus, D was multiplied by a constant
d (≤ 1) representing the amount of depression per presynaptic action potential and updated as
D→D*d. Between stimuli, D recovered exponentially back toward 1. We modelled depression
using two factors d1 and d2 with d1 being fast and d2 being slow subtypes, and d=d1*d2 was
constrained to be ≥ 1.
903
Synapse Distribution and Extrinsic inputs
We distributed 26,112 excitatory synapses over the cell. With an average of 5 synapses per pre-
synaptic neuron, this yielded 5,222 presynaptic nodes. To represent pre-synaptic cell
assemblies, we defined "functional groups" of presynaptic nodes. We put 100 nodes in each
functional group, yielding 52 functional groups. We found that varying the number of neurons in
the cell assembly did not qualitatively affect our results. To have exactly 100 nodes per
functional group we rounded the total number of nodes down to 5,200. Inhibitory inputs were not
defined by functional groups, but followed the literature cited in Table 1, with more than 1
synapse per pre-synaptic node. For example, with 1637 inhibitory synapses on the apical
dendrites and an average of 12 synapses per pre-synaptic node, there were about 136
inhibitory nodes that contacted the apical dendrites. The numbers and distributions of model
synapses along the dendrites are shown in Table 1.
The extrinsic inputs to the model were represented by spike trains arriving at the
corresponding synapses along the dendritic tree. The L5 pyramidal model is spatially
divided into the following sub-divisions: somatic, perisomatic, and proximal and distal
components of the apical and basal trees. We used standard definitions for these sub-
divisions except for perisomatic which is typically defined as the dendritic region within
100 µm of the soma [21].
Tonic inputs (Figs. 1-3): The firing rate of each excitatory spike train was randomly sampled
from an experimentally recorded distribution (Headley, personal communication). To reproduce
the 1/f spectrum that is widely found in neuronal spike trains, the 100 spike trains in each
functional group were modulated by a unique normalized (from 0.5 to 1.5) firing rate time series
that had a 1/f spectrum (more slow modulation of firing than fast) that was created by filtering
white noise using standard techniques. The normalized firing rate time series was then
multiplied with the mean firing rate of each of the 100 pre-synaptic nodes. Spike trains are then
generated by sampling from a Poisson distribution using the firing rate time series of each
presynaptic node of the functional group. In this way, spike trains that received the same
modulation trace would be statistically correlated, representing functional presynaptic cell
assemblies. Since feed-forward inhibition follows excitation in time, we averaged the firing rate
time series used to design the excitatory spike trains, shifted it forward in time by 4 milliseconds,
and used this to modulate the firing rate of the inhibitory spike trains.
Enhanced tonic inhibition (Fig. 4): Inhibitory synapses were divided into two groups, those
targeting perisomatic region that originate mainly from PV+ interneurons, and those on more
distal dendritic regions arising mainly from SOM+ interneurons [22; 23]. Perisomatic synapses
were defined as those within 100 µm of the soma with the properties specified in Table 1 under
"Inhibitory (Perisomatic and somatic)." Distal inhibitory synapses were greater than 100 µm from
the soma and had their properties specified in sections "Inhibitory (Basal)" and "Inhibitory
(Apical)" of the table To investigate if these inhibitory sources differentially regulated action

potential initiation and dendritic spiking, we doubled the rate of presynaptic events to one of
these inhibitory populations.
Investigation of E/I lag (Fig. 4F-I): We used the same scheme to design the extrinsic inputs as in
Figs. 1-3. However, to investigate the effect of E/I lag, we increased the variance of the overall
excitatory firing rate. So, while the mean rate stayed the same, we raised the modulatory trace
to the fourth power so that large deviations from the mean were exaggerated. This excitatory
firing rate trace was used to modulate the inhibitory firing rates (same as for Figs. 1-3). The
perisomatic and distal traces were shifted independently. One was fixed at 4 ms while the other
was shifted by 4, 125, 250, or 500 ms.
Rhythmic inhibition (Figs. 5 & 6): Gamma rhythms depend on PV+ interneurons, while beta
rhythms arise from SOM+ interneurons [24]. Thus, to emulate an inhibitory rhythm we
rhythmically modulated inhibitory synapses in the respective dendritic region (see description
above in "Enhanced tonic inhibition") at the appropriate frequency. Beta rhythms were emulated
by modulating distal inhibitory synapses at 16 Hz with a depth of 20%. Gamma rhythms were
emulated by modulating perisomatic synapses at 64 Hz with a depth of 40%. The different
depths of modulation ensured that these rhythms produced similar entrainment of action
potentials.
To generate inhibitory spike trains that produce rhythmic inhibition during oscillations, we
modulated their collective firing rate with a sine wave:
$$r[t] = A * (\sin(2 * \pi * f * t) + \phi) + off \qquad (4)$$
where $A = \frac{off}{\frac{1}{d}-1}$, f is the frequency, t is a vector representing time, ϕ is the phase, off is the
offset firing rate of the spike train being modulated, and $0 < d < 1$ is the depth of modulation
which represents the amplitude of the sine wave relative to off. To generate the spike train, a
random vector x[t] was created with values uniformly distributed between 0 and 1. A spike was
generated if $x[t] \leq r[t]dt$ where dt in our case was 1/1000.
Bursty inhibition (Fig. 7): We applied an envelope to the rhythmic inhibitory modulation trace to
simulate the bursty temporal nature of rhythms *in vivo*. The underlying sine wave was produced
in the same way as in the previous section. The envelope was a Gaussian kernel with a
standard deviation of two oscillatory cycles.
Clustered synaptic input (Fig. 8): For this experiment we kept everything the same as in the
rhythmic inhibition simulations, but introduced additional synapses driven by 40 pre-synaptic
spike trains. These spike trains were created by choosing one Poisson process and jittering the
spike times by ±2 ms. Each spike train drove an average of 4.6 synapses for a total of 187
synapses. These were placed either on the apical dendrites near the nexus or the basal
dendrites near the soma. For both nexus and basal clustered synapses, we targeted 140 μm of
dendritic cable length with 187 synapses yielding a synaptic density of 1.3 synapses per micron.
For the nexus case we targeted the 140 μm region starting at the bifurcation going toward the
apical dendrites. For the basal case, we targeted 3 basal dendrites that were directly connected
to the soma each one had a length of 40-50 μm adding up to 140 μm total (Figure 7A). The
synaptic weights were drawn from the distribution in Table 1.
982
983 *Detection of action potentials*
984 Action potentials were detected by the NEURON software as being any time point when the
985 somatic membrane potential crossed -10 mV with a positive first derivative.
986
Detection of dendritic spikes
Na+ and NMDA dendritic spike events were detected following the definitions developed in [9].
We developed our own detection algorithm for Ca^{2+} spikes since they were not previously
studied. Na+ spikes were detected if the voltage-gated sodium conductance density for a
compartment exceeded 0.3 mS/cm^2. If sodium spikes were within 2 ms of a somatic action

potential, they were assumed to be a consequence of a backpropagating action potential and
were not counted. An example of a Na^+ spike can be seen in Fig. 1C1.
NMDA spikes were detected by two criteria – voltage and current. The voltage
criteria were met if the membrane potential rose above -40 mV and remained there for
26 ms or more. The current criteria was met if the NMDA current exceeded 130% of the
current at the -40 mV crossing and continued to be met until the current fell to 115% of
that value. Whenever both the voltage and current criteria were met, an NMDA spike
was recorded. An example of an NMDA spike is shown in Fig. 1C2.
Ca^{2+} spikes were detected in the same way as NMDA spikes – using a voltage
and current threshold. The only difference was instead of NMDA current for the current
criteria we used the sum of HVA and LVA calcium currents. An example is shown in Fig.
1C3.
1004
Determination of electrotonic distance
We calculated electrotonic distance using NEURON's built-in Impedance method. The method
calculates signal attenuation between two compartments at a given frequency. We used 20 Hz
because the wavelength is on a time scale comparable to the membrane time constant (10s of
milliseconds). However, changing this frequency 10 Hz in either direction did not qualitatively
affect our results.
1011
Spike-triggered average (STA) of dendritic spikes (Figs. 2, 3)
For each dendritic compartment, we created a binary time series with 2 ms bins that was true
during periods where a dendritic spike was present (based on their detected start and stop
times). This was done separately for each type of dendritic spike (Na^+, NMDA, and Ca^{2+} spikes).
Each then had its spike-triggered average taken around the times of somatic action potentials
and their percent change from the mean across the entire simulation calculated. The STAs were
then grouped together based on their electrotonic distance percentile (10% bins) from the soma
and type of dendrite (apical or basal), and the median taken for each time lag.
1020
Generation of F-I curves (Fig. 4)
The model with Poisson excitation and inhibition was used. In the *perisomatic* condition, we
doubled the rate of inhibition to the somatic and proximal dendritic compartments (<100µm from
soma). In the *distal* case, we doubled the rate of inhibition to the distal dendritic compartments
(>100µm from soma). In each case, we injected 20 s current steps ranging from -1 nA to 2.4 nA
in 200 pA intervals.
1027
Phase histogram of dendritic spikes (Fig. 5)
Entrainment of dendritic spikes to inhibitory rhythms was calculated by first converting dendritic
spikes to a binary time series as was done for the STA calculation. The inhibitory rhythm was
then binned by phase, with bin widths of π/4, yielding 8 phase bins. The mean of the dendritic
spike binary series was taken for each phase bin. These were converted to percent change
from mean and their median taken across compartments by their electronic distance and
dendritic type (the same as in the STA calculation).
1035
1036　　*Determination of AP threshold and somatic membrane voltage distribution (Fig. 6)*
1037　　AP threshold was taken to be the voltage 1 ms prior to the peak of the spike. Voltage
1038　　distributions were calculated using 1 ms bins.
1039
1040　　*Phase histogram of dendritic spikes (Fig. 7)*
1041　　For calculating entrainment of dendritic spikes to the rhythm, we followed the same procedure
1042　　as detailed above for Fig. 5.

1043
Cross-correlation (CC) between presynaptic spikes and action potentials (Fig. 8)
We measured the effect of inhibitory rhythms on the coupling between concentrated synaptic
inputs and action potentials using a phase-stratified CC. Presynaptic spike times that drove the
concentrated synaptic inputs were grouped together and separated based on whether they
occurred during the positive or negative phase of the imposed inhibitory rhythm. Their CC with
somatic action potentials was then calculated using 1 ms bins. Since both the presynaptic and
action potential times had inherent periodicities, these had to be corrected for [25]. This was
performed by converting the CC and both autocorrelations to the frequency domain using the
fast Fourier transform, setting the coefficients at the inhibitory modulation rhythm to 0,
performing element-wise division of the CC by the square-root of the autocorrelations multiplied
together, and then converting back to the time domain using the inverse fast Fourier transform
on that result. To measure the strength of the cross-correlation peak, we identified the positive
peak of the CC nearest to zero time lag, and then integrated over its area with the edges
defined by when the CC crossed from positive to negative values.
1058

1059 **Table 1.** Inputs to L5 PN. L5 PN dendrites can course up to layer 1 and receive both excitatory
1060 and inhibitory inputs to their dendrites. Here we quantified, where possible, the experimental
1061 values for synaptic magnitude, firing rate, divergence, and release probability. We matched the
1062 model parameters to the experimental values as closely as possible while preserving a
1063 reasonable basal firing rate.
1064

Synapse type	Characteristics	Model	Experimental
Excitatory (Basal)	Magnitude of EPSCs	37.0 ± 32.3 pA	**30.6 ± 29.9 pA** [26]
	Firing rate	4.43 ± 2.9 Hz	**4.43 ± 2.9 Hz** (Headley personal comm.)
	Divergence	2-8	**2-8** [6; 15; 27]
	Number of synapses	10042	**10042** [10]
	Release probability	0.53 ± 0.22	**0.53 ± 0.22** [28]
Excitatory (Apical)	Magnitude	25.9 ± 24.9 pA	**30.6 ± 29.9 pA** [26]
	Firing rate	4.43 ± 2.9 Hz	**4.43 ± 2.9 Hz** (Headley personal comm.)
	Divergence	2-8	**2-8** [6; 15; 27]
	Number of synapses	16070	**16070** [10]
	Release probability	0.53 ± 0.22	**0.53 ± 0.22** [28]
Inhibitory (Perisomatic and somatic)	Magnitude	162.5 ± 103.1 pA	**208.3 ± 58.7 pA** [29]
	Firing rate	16.9 ± 14.3 Hz	**16.9 ± 14.3 Hz** [30]
	Divergence	2.8 ± 1.9	**2.8 ± 1.9**
	Number of synapses	406	**406** [10]
	Release probability	0.88 ± 0.05	**0.88 ± 0.05** [29]
Inhibitory (Basal)	Magnitude	24.3 ± 18.4 pA	**26.5 ± 1.6 pA** [29]
	Firing rate	3.9 ± 4.9 Hz	**3.9 ± 4.9 Hz** [30]
	Divergence	2.7 ± 1.6	**2.7 ± 1.6** [31; 32]
	Number of synapses	1023	**1023** [10]
	Release probability	0.72 ± 0.10	**0.72 ± 0.10** [29]
Inhibitory (Apical)	Magnitude	24.3 ± 33.1 pA	**26.5 ± 1.6 pA** [29]
	Firing rate	3.9 ± 4.9 Hz	**3.9 ± 4.9 Hz** [30]
	Divergence	12 ± 3	**12 ± 3** [33]
	Number of synapses	1637	**1637** [10]
	Release probability	0.30 ± 0.08	**0.30 ± 0.08** [33]

1065
1066

Table 2. Short term pre-synaptic plasticity. Parameters were tuned to match experimental recordings reported in [16]

Synapse type	tauD1 (ms)	d1	tauD2 (ms)	d2	Synaptic current @ 20 Hz	Train induction vs. frequency
Excitatory	35	0.95	250	0.8		
Perisomatic inh.	40	0.7	500	0.7		
Dendritic inh.	200	0.8	1	1		

References - Methods

1. Egger R, Narayanan RT, Guest JM, Bast A, Udvary D, Messore LF, Das S, de Kock CPJ, Oberlaender M (2020) Cortical output is gated by horizontally projecting neurons in the deep layers. Neuron 105, 122-137.e128.
2. Hay E, Hill S, Schürmann F, Markram H, Segev I (2011) Models of neocortical layer 5b pyramidal cells capturing a wide range of dendritic and perisomatic active properties. PLoS Comput Biol 7, e1002107.
3. Dai K, Gratiy SL, Billeh YN, Xu R, Cai B, Cain N, Rimehaug AE, Stasik AJ, Einevoll GT, Mihalas S et al. (2020) Brain modeling toolkit: An open source software suite for multiscale modeling of brain circuits. PLoS Comput Biol 16, e1008386.
4. Hines ML, Carnevale NT (1997) The neuron simulation environment. Neural Comput 9, 1179-1209.
5. Branco T, Staras K (2009) The probability of neurotransmitter release: Variability and feedback control at single synapses. Nature Reviews Neuroscience 10, 373-383.
6. Markram H, Lübke J, Frotscher M, Roth A, Sakmann B (1997) Physiology and anatomy of synaptic connections between thick tufted pyramidal neurones in the developing rat neocortex. J Physiol 500 (Pt 2), 409-440.

7.   Chen X, Leischner U, Rochefort NL, Nelken I, Konnerth A (2011) Functional mapping of
single spines in cortical neurons in vivo. Nature 475, 501-505.
8.   Takahashi N, Kitamura K, Matsuo N, Mayford M, Kano M, Matsuki N, Ikegaya Y (2012)
Locally synchronized synaptic inputs. Science 335, 353-357.
9.   Goetz L, Roth A, Häusser M (2021) Active dendrites enable strong but sparse inputs to
determine orientation selectivity. Proceedings of the National Academy of Sciences 118,
e2017339118.
10. Karimi A, Odenthal J, Drawitsch F, Boergens KM, Helmstaedter M (2020) Cell-type
specific innervation of cortical pyramidal cells at their apical dendrites. eLife 9, e46876.
11. Horner CH, Arbuthnott E (1991) Methods of estimation of spine density--are spines
evenly distributed throughout the dendritic field? J Anat 177, 179-184.
12. Tjia M, Yu X, Jammu LS, Lu J, Zuo Y (2017) Pyramidal neurons in different cortical
layers exhibit distinct dynamics and plasticity of apical dendritic spines. Frontiers in
Neural Circuits 11, 1-10.
13. Davidson AM, Mejiá-Gómez H, Jacobowitz M, Mostany R (2020) Dendritic spine density
and dynamics of layer 5 pyramidal neurons of the primary motor cortex are elevated with
aging. Cereb Cortex 30, 767-777.
14. Markram H, Muller E, Ramaswamy S, Reimann MW, Abdellah M, Sanchez CA, Ailamaki
A, Alonso-Nanclares L, Antille N, Arsever S et al. (2015) Reconstruction and simulation
of neocortical microcircuitry. Cell 163, 456-492.
15. Reimann MW, King JG, Muller EB, Ramaswamy S, Markram H (2015) An algorithm to
predict the connectome of neural microcircuits. Front Comput Neurosci 9, 1-18.
16. Campagnola L, Seeman SC, Chartrand T, Kim L, Hoggarth A, Gamlin C, Ito S, Trinh J,
Davoudian P, Radaelli C et al. (2022) Local connectivity and synaptic dynamics in
mouse and human neocortex. Science 375, eabj5861.
17. Varela JA, Sen K, Gibson J, Fost J, Abbott LF, Nelson SB (1997) A quantitative
description of short-term plasticity at excitatory synapses in layer 2/3 of rat primary visual
cortex. J Neurosci 17, 7926-7940.
18. Destexhe A, Mainen ZF, Sejnowski TJ (1994) An efficient method for computing synaptic
conductances based on a kinetic model of receptor binding. Neural Comput 6, 14-18.
19. Durstewitz D, Seamans JK, Sejnowski TJ (2000) Dopamine-mediated stabilization of
delay-period activity in a network model of prefrontal cortex. J Neurophysiol 83, 1733-
1750.
20. Zador A, Koch C, Brown TH (1990) Biophysical model of a hebbian synapse. Proc Natl
Acad Sci U S A 87, 6718-6722.
21. Freund TF, Katona I (2007) Perisomatic inhibition. Neuron 56, 33-42.
22. Kubota Y (2014) Untangling gabaergic wiring in the cortical microcircuit. Curr Opin
Neurobiol 26, 7-14.
23. Tremblay R, Lee S, Rudy B (2016) Gabaergic interneurons in the neocortex: From
cellular properties to circuits. Neuron 91, 260-292.
24. Chen G, Zhang Y, Li X, Zhao X, Ye Q, Lin Y, Tao HW, Rasch MJ, Zhang X (2017)
Distinct inhibitory circuits orchestrate cortical beta and gamma band oscillations. Neuron
96, 1403-1418.e1406.
25. Headley DB, Weinberger NM (2013) Fear conditioning enhances gamma oscillations
and their entrainment of neurons representing the conditioned stimulus. J Neurosci 33,
5705-5717.
26. Morishima M, Morita K, Kubota Y, Kawaguchi Y (2011) Highly differentiated projection-
specific cortical subnetworks. J Neurosci 31, 10380-10391.
27. Deuchars J, West DC, Thomson AM (1994) Relationships between morphology and
physiology of pyramid-pyramid single axon connections in rat neocortex in vitro. The
Journal of Physiology 478, 423-435.

28.   Brémaud A, West DC, Thomson AM (2007) Binomial parameters differ across
1144   neocortical layers and with different classes of connections in adult rat and cat
1145   neocortex. Proc Natl Acad Sci U S A 104, 14134-14139.
1146   29.   Xiang Z, Huguenard JR, Prince DA (2002) Synaptic inhibition of pyramidal cells evoked
1147   by different interneuronal subtypes in layer v of rat visual cortex. J Neurophysiol 88, 740-
1148   750.
1149   30.   Yu J, Hu H, Agmon A, Svoboda K (2019) Recruitment of gabaergic interneurons in the
1150   barrel cortex during active tactile behavior. Neuron 104, 412-427.e414.
1151   31.   Tanaka YH, Tanaka YR, Fujiyama F, Furuta T, Yanagawa Y, Kaneko T (2011) Local
1152   connections of layer 5 gabaergic interneurons to corticospinal neurons. Front Neural
1153   Circuits 5, 12.
1154   32.   Thomson AM, Deuchars J, West DC (1996) Neocortical local synaptic circuitry revealed
1155   with dual intracellular recordings and biocytin-filling. Journal of Physiology Paris 90, 211-
1156   215.
1157   33.   Silberberg G, Markram H (2007) Disynaptic inhibition between neocortical pyramidal
1158   cells mediated by martinotti cells. Neuron 53, 735-746.

A Morphology of Layer 5 neuron

Apical tuft

Apical nexus

Apical trunk

Basal dendrites

Spontaneous firing rates

B Membrane potentials recorded throughout the neuron during naturalistic synaptic drive exhibit regenerative events

bAP   bAP   bAP

AP   AP   AP

▼ NMDA spike
▼ Na+ spike
▼ Ca2+ spike

C1 Na+ spike example

Soma voltage
Dendrite voltage
NaP current

Na+ spike properties

C2 NMDA spike example

Soma voltage
Dendrite voltage
NMDA current

NMDA spike properties

C3 Ca2+ spike example

Soma voltage
Dendrite voltage
HVA current
LVA current

Ca2+ spike properties

A Electrotonic distance across the dendritic tree

Percent of signal at soma

B Na⁺ spikes on apical branches

Na⁺ spikes on basal branches

C NMDA spikes on apical branches

NMDA spikes on basal branches

A Electrotonic distance from apical nexus

100μm

Percent of signal at nexus

B Ca²⁺ spikes on apical dendrites

Percent change

Time from action potential (ms)

C NMDA spikes on apical branches

Electrotonic distance from nexus (percentile rank)

Far
Mid
Close

Time from Ca²⁺ spike at nexus (ms)

Percent change

D Modulation of NMDA spike/action potential coordination by Ca²⁺ spikes

NMDA spikes on apical branches

Electrotonic distance from soma (percentile rank)

Far
Mid
Nexus
Close

Time from action potential (ms)

Percent change

NMDA spikes on basal branches

Electrotonic distance from soma (percentile rank)

Far
Mid
Close

Time from action potential (ms)

Percent change

A Inhibitory modulation of action potentials

B f-I curve to characterize response gain

Control

Distal

Peri.

50 mV
500 ms

60 mV

-1000   0   1400pA

Control
Distal
Periosomatic
Shifted distal
Shifted perisomatic

C Inhibitory modulation of Na⁺ spikes

Control
Distal
Perisomatic

D Inhibitory modulation of NMDA spikes

E Inhibitory modulation of Ca²⁺ spikes

F Voltage traces with different E/I lags

Control

Soma
Apical
Basal

Distal inhibition lagged

Soma
Apical
Basal

50 mV
100 ms

Perisomatic inhibition lagged

Soma
Apical
Basal

G Firing rate vs. E/I lag

Perisomatic
Normal (4 ms)
Distal dendritic

H Ca²⁺ spikes vs. E/I lag

Distal inhibition

Perisomatic inhibition

E/I lag (ms)

I NMDA spikes vs. E/I lag

Distal dendritic inhibition

Apical branches   Basal branches

Perisomatic inhibition

Apical branches   Basal branches

A Modulation by beta rhythmic inhibition

Perisomatic presynaptic spikes

Distal dendritic presynaptic spikes

Membrane voltage traces

B Action potentials

C Ca²⁺ spikes

D1 NMDA Apical

D2 NMDA Basal

E1 Na⁺ Apical

E2 Na⁺ Basal

F Modulation by gamma rhythmic inhibition

Perisomatic presynaptic spikes

Distal dendritic presynaptic spikes

Membrane voltage traces

G Action potentials

H Ca²⁺ spikes

I1 NMDA Apical

I2 NMDA Basal

J1 Na⁺ Apical

J2 Na⁺ Basal

Gamma rhythmic inhibition

A1 Action potential threshold

Cumulative probability vs Membrane voltage (mV)
- Peak (red)
- Trough (blue)
- Poisson (black)

A2 Somatic membrane voltage distribution

Normalized probability vs Membrane voltage (mV)

Beta rhythmic inhibition

B1 Action potential threshold

Cumulative probability vs Membrane voltage (mV)
- Peak (red)
- Trough (blue)
- Poisson (black)

B2 Somatic membrane voltage distribution

Normalized probability vs Membrane voltage (mV)

A Modulation by gamma rhythmic inhibition

Inhibitory mod.
Soma
Apical
Basal

50 mV

F Modulation by beta rhythmic inhibition

Inhibitory mod.
Soma
Apical
Basal

200 ms

B Action potentials

Firing rate (Hz)

Burst cycle

C Ca²⁺ spikes

Percent change

Burst cycle

G Action potentials

Firing rate (Hz)

Burst cycle

H Ca²⁺ spikes

Percent change

Burst cycle

D1 NMDA Apical

Electrotonic distance from soma

Far
Mid
Close

Burst cycle

E1 Na⁺ Apical

Far
Mid
Close

Burst cycle

I1 NMDA Apical

Electrotonic distance from soma

Far
Mid
Close

Burst cycle

J1 Na⁺ Apical

Far
Mid
Close

Burst cycle

D2 NMDA Basal

Far
Mid
Close

Burst cycle

E2 Na⁺ Basal

Far
Mid
Close

Burst cycle

I2 NMDA Basal

Far
Mid
Close

Burst cycle

J2 Na⁺ Basal

Far
Mid
Close

Burst cycle

-100   0   100
Percent change

-100   0   100
Percent change

-100   0   100
Percent change

-100   0   100
Percent change

A Positioning of clustered excitatory synapses

Apical excitatory input

100um
100um

Basal excitatory input

B Effect of rhythmic inhibition phase on the cross-correlation between afferent excitation and somatic action potentials

Beta rhythmic inhibition

Gamma rhythmic inhibition

Apical excitation

Peak
Trough
Poisson

Cross-correlation (normalized × 10²)

Basal excitation

Peak
Trough
Poisson

Time from presynaptic spike (ms)

C Response strength by input location, inhibition type, and phase

Area under cross-correlation peak

Peak
Trough
Basal poisson
Apical poisson

16 Hz   64 Hz   16 Hz   64 Hz
Basal   Apical