Minimization of proteome reallocation explains metabolic transition in
hierarchical utilization of carbon sources

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Abstract

Cells choose between alternative pathways in metabolic networks under diverse environmental conditions, but the principles governing the choice are insufficiently understood, especially in response to dynamically changing conditions. Here we observed that a lactic acid bacterium *Bacillus coagulans* displayed homolactic fermentation on glucose or trehalose as the sole carbon source, but transitioned from homolactic to heterolactic fermentation during the hierarchical utilization of glucose and trehalose when growing on the mixture. We simulated the observation by dynamic minimization of reallocation of proteome (dMORP) using an enzyme-constrained genome-scale metabolic model of *B. coagulans*, which coincided with our omics data. Moreover, we evolved strains to co-utilize mixed carbon sources and repress the choice of heterolactic fermentation, and the dynamics after co-utilization of carbon sources could also be captured by dMORP. Altogether, the findings suggest that upon rapid environmental changes bacteria tend to minimize proteome reallocation and accordingly adjust metabolism, and dMORP would be useful in simulating and understanding cellular dynamics.

Introduction

Cells have alternative pathways, i.e., redundancy, in metabolic networks to adapt to diverse environmental conditions. For instance, while many microbes and mammalian cells use respiration for ATP production, some of them also harbor fermentation as an alternative ATP-producing pathway, which enables not only survival under anaerobic conditions but also fast growth in the presence of oxygen, i.e., aerobic fermentation[1]. The alternative pathways empower cells to choose between distinct metabolic strategies, but the principles governing the cellular choice are insufficiently understood[2].

Experimental and theoretical studies suggest that the choices of alternative pathways and metabolic strategies reflect tradeoffs, mostly between metabolic efficiency, e.g., yield, of pathways and cellular resources, e.g., proteome, invested for enzymes of the pathways[3-8]. For instance, fermentation has a lower ATP yield but is more proteome efficient than respiration, and therefore favors fast-growing cells subject to the limited proteome resources[9, 10]. These studies are predominantly focused on steady-state cultures, e.g., chemostats, of model microbes, and therefore the cellular choice might be a result of a relatively long-term adaption to the environment. However, much less is known whether and how cells can transition between alternative pathways under dynamically changing environments, which are ubiquitous in both natural and artificial biological systems[11, 12].

Here we studied a lactic acid bacterium *Bacillus coagulans*, which has alternative pathways for catabolizing glycolytic carbon sources, e.g., glucose, and generating energy, i.e., homolactic and heterolactic fermentation[13, 14]. The former converts glucose to lactate via the Embden–Meyerhof–Parnas (EMP) pathway with the theoretical yield being one gram lactate per gram glucose, while the latter via the phosphoketolase pathway with the halved yield due to the production of acetate and ethanol[15, 16]. We observed that *B. coagulans* displayed the homolactic fermentation on glucose or trehalose as the sole carbon source, but transitioned from homolactic to heterolactic fermentation in the hierarchical utilization of glucose and trehalose when growing on the mixture. We hypothesized that the metabolic transition could be interpreted by minimization of reallocation of proteome (MORP) and performed enzyme-constrained metabolic modeling and omics analysis to test the hypothesis. Finally, by adaptive laboratory evolution (ALE) we evolved strains that can co-utilize the mixed carbon sources, which showcased another application of MORP.

Results

Lactate yield significantly changed in hierarchical utilization of glucose and trehalose

B. coagulans is widely used in the industrial lactate fermentation[14, 17, 18], where hydrolysates of low-cost starch-based materials are commonly used as the carbon sources[19, 20] considering cost and benefit. However, the co-existence of multiple carbon sources in the medium may lead to the hierarchical utilization[21-26] and thus the waste of substrates[27], the extension of fermentation cycle [28] and the difficulty in product separation and purification[29]. Notably, the hierarchical utilization with the transition from homolactic to heterolactic fermentation led to the significantly reduced yield of lactate in the industrial fermentation by *B. coagulans*[13, 14]. Therefore, identifying the principles governing the dynamic behavior of *B. coagulans* during the

hierarchical utilization of mixed carbon sources would be of significance from both basic and
applied science perspectives.

We performed batch fermentation of *B. coagulans* on the mixture of glucose and trehalose, a
disaccharide with a high percentage in the hydrolysates(30). We observed the hierarchical
utilization of glucose and trehalose, which divided the entire fermentation process into three phases
(Fig. 1A). In the glucose utilization phase (P_{gluc}, 0-12 h), glucose was exclusively consumed and
lactate was rapidly produced with the lactate yield on glucose being 0.897 g/g, which was similar
to the yield (i.e., 0.882 g/g) on glucose as the sole carbon source (Fig. 1B) and close to the yield of
homolactic fermentation(15, 31). Upon glucose depletion, the lag phase occurred (P_{lag}, 12-16 h), in
which the lactate production stopped, the biomass concentration (measured by OD_{620}) declined
(Fig. 1A) and a few organic acids were slightly consumed (Supplementary Fig. 1). The biomass
decline was also observed in the growth profiles on a mixture of glucose and xylose and
switchgrass hydrolysate(32). We confirmed that the growth arrest was not caused by the depletion
of nutrients such as amino acids (Supplementary Fig. 2). In the trehalose utilization phase (P_{tre}, 16-
84 h), trehalose was consumed, and lactate was produced again (Fig. 1A). Interestingly, the lactate
yield on trehalose in P_{tre} was only 0.526 g/g, which was much lower than that (i.e., 0.851 g/g) on
trehalose as the sole substrate (Fig. 1B) and close to the theoretical lactate yield of heterolactic
fermentation(15). This was in line with the increased yields of byproducts in P_{tre} (Supplementary
Table 1). The significant change in the lactate yield during the hierarchical utilization of glucose and
trehalose indicated distinct strategies to catabolize the carbon sources in P_{gluc} and P_{tre}.

Carbon source conditions	P_{gluc}	P_{tre}	Glucose	Trehalose
Lactate yield (g/g)	0.897±0.015	0.526±0.041	0.882±0.006	0.851±0.044

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Figure 1. Fermentation on various carbon sources in 5 L bioreactor by *B. coagulans*. (A)
Fermentation processes on glucose and trehalose as the mixed carbon sources (left), sole glucose
(middle) and sole trehalose (right). Data in the plots are shown with mean ± s.d. of three biological
replicates. (B) Lactate yields under various phases and conditions. Data in the table are shown with
mean ± s.d. of three biological replicates.

Dynamic minimization of reallocation of proteome predicted metabolic changes
To gain a systematic understanding, we reconstructed a genome-scale metabolic model of the
strain *B. coagulans* DSM 1 = ATCC 7050(33) called iBcoa620, which was evaluated by the Memote
score(34) and validated by growth on various carbon sources (Supplementary Fig. 3).

Subsequently, we converted iBcoa620 into an enzyme-constrained version eciBcoa620 using the
GECKO toolbox(35), allowing for understanding of metabolic changes by taking into account the
enzyme usage and proteome allocation(36-38).

To predict the changes during the fermentation process, we performed dynamic flux balance
analysis (dFBA)(39) with eciBcoa620 (Fig. 2A). The dFBA approach can divide the entire period
into multiple time intervals and obtain the flux distribution at each time interval by performing
classical FBA(40) which requires a predefined objective function. While growth maximization(41)
as the objective function appeared reasonable to simulate for P_{gluc}, it could not predict the cellular
behavior after glucose depletion (Fig. 2B), meaning that cells might adjust the objective in response
to the changing environment. Therefore, we attempted other commonly used objective
functions(42), including to maximize lactate production and to maximize non-growth-associated
maintenance (NGAM), and found that they also failed to capture the cellular behavior in P_{tre}
(Supplementary Fig. 4), i.e., predicted either much higher lactate concentrations than
measurements or no lactate production (Fig. 2B).

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Figure 2. Simulation of batch fermentation under mixed carbon sources by eciBcoa620. (A)
Simulation of the fermentation process. In the dFBA simulation of P_{gluc} the growth rate was
maximized. To simulate P_{tre}, various objective functions could be adopted within the dFBA
framework. Additionally, we developed an approach to dynamically minimize the proteome
reallocation with the enzyme-constrained models. (B) Simulation of lactate production using
different objective functions. Minimization of proteome reallocation predicted the lactate production
in P_{tre} better than the others including maximizing lactate, NGAM and growth. Data in the plot are
shown with mean ± s.d. of three biological replicates. (C) Root mean square errors of the different
objective functions in predicting P_{tre}. Root mean square error quantifies the difference between the

predicted and experimental concentrations of detected products, including lactate, acetate,
pyruvate, acetoin and ethanol. (D) Comparison of the relative fluxes of the central carbon
metabolism (CCM) between P_{gluc} (represented by 7 h) and P_{tre} (represented by 48h). Relative flux
is calculated as the percentage of the absolute flux of each reaction to the substrate uptake flux.
Note that one unit of trehalose uptake flux was converted to two units of glucose uptake flux.
Abbreviations: T6P, trehalose 6‑phosphate; G6P, glucose 6‑phosphate; F6P, fructose 6‑
phosphate; FBP, fructose 1,6‑bisphosphate; DHAP, dihydroxyacetone phosphate; G3P,
glyceraldehyde 3‑phosphate; 13BPG, glycerate 1,3‑bisphosphate; 3PG, 3-phosphoglycerate;
2PG, 2-Phospho-D-glycerate; PEP, phosphoenolpyruvate; 6PG, gluconate 6‑phosphate; E4P,
erythrose 4‑phosphate; S7P, sedoheptulose 7-phosphate; R5P, ribose 5‑phosphate; RL5P,
ribulose 5‑phosphate; XL5P, xylulose 5-phosphate; Acetyl-P, Acetyl phosphate; PGI, glucose-6-
phosphate isomerase; PKFA, 6-phosphofructokinase; FBA, fructose-1,6-bisphosphate aldolase;
GAP, glyceraldehyde-3-phosphate dehydrogenase; PGK, phosphoglycerate kinase; GPMI,
phosphoglycerate mutase; ENO, enolase; PYK, pyruvate kinase; LDH, L-lactate dehydrogenase;
RPI, ribose 5-phosphate isomerase; RPE, ribulose-phosphate 3-epimerase; XFP,
phosphoketolase; FSA, fructose-6-phosphate aldolase; TKT, transketolase; BUDA, acetolactate
decarboxylase; ACKA, acetate kinase; ALD, aldehyde dehydrogenase; ADHP, alcohol
dehydrogenase.
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Considering the fact that proteome reallocation requires frequent protein synthesis and
degradation, which is of high cost to cells(42), we hypothesized that cells tend to dynamically
minimize the proteome reallocation in response to rapid environmental changes. To test it, we
developed the approach MORP and extended to the dynamic version dMORP to simulate the
cellular behavior after glucose depletion, and the enzyme usage in the last time point of the glucose
phase was the reference for the first time point for of the simulations by dMORP (Fig. 2A) (Materials
and Methods). The dMORP approach leverages the enzyme-constrained models and minimizes
the sum of absolute differences of all enzyme usage values between previous and current time
intervals (Materials and Methods). By employing dMORP, we found that the lactate production in
P_{tre} was well predicted (Fig. 2B). Moreover, dMORP outperformed other tested objective functions
as it led to the smallest Root Mean Square Error (RMSE) (Fig. 2C) and it predicted production of
byproducts in P_{tre} such as acetate, acetoin and ethanol (Supplementary Fig. 4). Furthermore, we
compared the metabolic fluxes predicted by various objective functions with those by random
sampling, which enables unbiased estimations of metabolic fluxes subject to experimentally
measured constraints. For reactions in the central carbon metabolism (CCM), the fluxes predicted
by dMORP were generally within the ranges of the sampled fluxes, while the fluxes by other
objective functions notably deviated (Supplementary Fig. 5). Therefore, we demonstrated that
dMORP could be a more realistic objective function for describing the cellular behavior after
glucose depletion.
169
To explain the observed lower lactate yield in P_{tre} with dMORP, we compared the relative fluxes,
i.e., normalized to carbon source uptake, of the CCM reactions in P_{tre} (simulated at 48 h, i.e., middle
in P_{tre}) to those in P_{gluc} (simulated at 7 h, i.e., mid-exponential phase in P_{gluc}). We found in P_{tre} a
much greater fraction of carbon flux toward phosphoketolase (Fig. 2D), resulting in carbon loss in

the form of acetate and ethanol and thereby the decreased lactate yield(14). This was also similar
with the comparison between P$_{tre}$ and the sole trehalose condition (Supplementary Fig. 6). In
addition, we compared the absolute fluxes simulated at 7 h, 14 h and 48 h, representing P$_{gluc}$, P$_{lag}$
and P$_{tre}$, respectively (Fig. 3). We found that the metabolic fluxes in P$_{lag}$ and P$_{tre}$ were comparable
and generally less than those in P$_{gluc}$ (Fig. 3), exemplified by the glycolytic fluxes, which was due
to the considerably slower substrate uptake (Supplementary Table 1). By comparing P$_{gluc}$ and P$_{tre}$,
we found that the phosphoketolase pathway displayed smaller decreases in fluxes than glycolytic
reactions (Supplementary Fig. 7) and thus accounted for a greater fraction of carbon flux, which
explained the higher yields of acetate and ethanol.
183

185   **Figure 3. Fluxes of the CCM reactions in the fermentation process predicted by eciBcoa620.**
186   The metabolic flux distributions of the CCM at 7 h, 14 h, and 48 h. These three time points represent
187   P$_{gluc}$, P$_{lag}$ and P$_{tre}$, respectively. At 7 h the objective function was to maximize growth while at 14 h
188   and 48 h it was to minimize the proteome reallocation.
189

Omics data coincided with dynamic minimization of proteome reallocation
To systematically unravel the molecular mechanisms, we collected transcriptomics and proteomics
data at 7 h, 14 h and 48 h, representing P$_{gluc}$, P$_{lag}$ and P$_{tre}$, respectively. The transcriptomics and
proteomics data, which showed high consistency among biological triplicates while clear variability
among different phases (Supplementary Fig. 8), were used for identifying differentially expressed
transcripts and proteins (Materials and Methods). Enrichment analysis of the differential expression
showed that from P$_{gluc}$ to P$_{lag}$ and P$_{tre}$ pathways were mostly downregulated, particularly those
related to translation, e.g., ribosome and aminoacyl-tRNA biosynthesis (Supplementary Fig. 9), in
line with the observed growth arrest (Fig. 1A). Moreover, the differential expression was enriched
in amino acid pathways, which could be associated with the significant changes in the
concentrations of intracellular amino acids (Supplementary Fig. 10).
201

202   Given that the enzyme-constrained models can simulate enzyme usage for metabolic reactions,
203   we compared the simulated enzyme usage to the measured mRNA and protein levels for CCM

reactions. We simulated dynamic changes in the enzyme usage using dMORP and dFBA with
maximization of growth, lactate and NGAM, and found that dMORP resulted in the least decrease
in the enzyme usage upon glucose depletion (Fig. 4), indicating the effectiveness of MORP in
minimizing the proteome reallocation during the transition. Notably, the enzyme usage simulated
by MORP captured the measured mRNA and protein levels for CCM reactions much better than
those simulated by the other objective functions (Fig. 4).

Figure 4. Comparison of simulated enzyme usage and measured mRNA and protein levels.
Taking the PGI reaction as an example, the log2FC value represents the change in enzyme usage,
mRNA or protein level relative to the 7 h point. The enzyme usage was predicted by different

215 objective functions. The mRNA and protein levels represent average values of biological triplicates
216 from measured transcriptomics and proteomics data.
217
To further compare with MORP, we performed simulations by constraining exchange rates with
measurements and minimizing the total proteome (Materials and Methods), and thus estimated the
most efficient usage of the enzymes that maintain the experimentally observed metabolic states.
This manner, which is widely adopted for enzyme-constrained simulations(35, 43), also performed
worse than MORP in terms of simulating the dynamics of the enzyme usage (Supplementary Fig.
11). In addition, this may indicate suboptimal performance of enzymes during the transition as
predicted by MORP (Supplementary Fig. 12), which could be associated with enzyme occupancy
by substrates and thermodynamics(44).
226
227 In conclusion, the model simulations and experimental measurements demonstrated that the
228 cellular proteome maintained minimal adjustment upon rapid environmental changes, i.e., after
229 glucose depletion cells tended to utilize the proteome expressed on glucose phase to consume
230 trehalose.
231

Application of MORP to evolved strains capable of co-utilizing mixed carbon sources
Given that the hierarchical utilization of carbon sources was accompanied by the metabolic
transition from homolactic to heterolactic fermentation, we expected that co-utilization of carbon
sources would avoid heterolactic fermentation and thus enhance lactate yield. To this end, we
carried out ALE (Materials and Methods) (Fig. 5A) and obtained four evolved strains that can co-
utilize glucose and trehalose (Supplementary Fig. 13). Whole-genome sequencing identified the
mutation in the gene *crr* encoding glucose-specific phosphotransferase enzyme IIA component in
all evolved strains (Supplementary Table 2), in line with the findings of the microbes with diminished
glucose repression(45-47).
241

We grew one of the evolved strains Ev3 on the mixture of glucose and trehalose in the 5 L
bioreactor cultivation and monitored biomass and extracellular metabolite levels (Supplementary
Fig. 14). We found that Ev3 utilized glucose and trehalose simultaneously until 14 h when trehalose
was exhausted, and then glucose served as the sole carbon source. By calculating the lactate yield
for these two phases, we found that Ev3 performed homolactic fermentation on both phases, which
led to a higher total lactate yield than the wildtype strain (Supplementary Fig. 14).
248

249 Furthermore, the dynamics from mixed carbon sources to glucose utilization provided another
250 scenario that could test MORP. To this end, we simulated the fermentation process of Ev3 within
251 the dFBA framework, in which the first phase (before 14 h) was simulated by maximizing growth

252 and the second (after 14 h) by MORP. We showed that MORP could also capture the physiological
253 changes after trehalose depletion (Fig. 5B), and thus foresee more applications of MORP.
254

255
Figure 5. Adaptive laboratory evolution and fermentation process of the evolved strain. (A)
Brief diagram of adaptive laboratory evolution experiment. The addition of 2-Deoxy-D-glucose to
trehalose aimed at efficiently utilizing trehalose in the absence of glucose, with the intention of
eliminating the catabolite repression effect. After 40 generations, growth and lactate production
were basically stable. The strains with notably improved lactate production were selected for
subsequent shake flasks validation and 5 L bioreactor experiments. (B) Fermentation with mixed
carbon sources in 5 L bioreactor by the evolved strain Ev3. Simulations were performed for the
fermentation process, in which dFBA with maximization of growth was performed in the phase of
simultaneous utilization of glucose and trehalose and dMORP was performed after trehalose
depletion. Data are shown with mean ± s.d. of three biological replicates.
266

Discussion

Here, we observed that *B. coagulans* utilized glucose and trehalose hierarchically and transitioned
from homolactic to heterolactic fermentation during the hierarchical utilization (Fig. 1). We
hypothesized that the dynamic minimization of proteome reallocation might result in this
observation. To test it, we reconstructed the enzyme-constrained genome-scale metabolic model
of *B. coagulans*, and developed MORP and its dynamic version dMORP. The model with dMORP
captured the transition from homolactic to heterolactic fermentation (Fig. 2) and simulated minimal

adjustment of proteome during the transition as indicated by the omics data (Fig. 4). We therefore
concluded that the dynamic minimization of proteome reallocation could explain the microbial
choice of the metabolic strategies upon environmental changes, e.g., changes in the availability of
carbon sources in the medium. Last, with the evolved strain we used dMORP to simulate the
transition from the co-utilization of glucose and trehalose to the utilization of glucose after trehalose
depletion (Fig. 5), demonstrating the extended applications of MORP and dMORP.
280
The biological basis of the minimization of proteome reallocation is the high cost and slow
adjustment of protein synthesis and degradation(42, 48, 49) that the cells should consider when
adapting to rapid perturbations. Additionally, the minimization of proteome reallocation is in line
with the findings of proteome reserves(50, 51), i.e., the proteome is not fully optimized for the
environmental condition where the cells are living, as a suboptimal proteome could reduce the cost
and time of reallocation upon the adaption to a new condition. By integrating the minimization of
proteome reallocation into the constraint-based modeling framework, we developed MORP and
dMORP that introduce the past proteome as an internal constraint, which provide additional
objective functions for simulating cellular behaviors(52). Particularly, dMORP would serve as a
promising algorithm in the field of dynamic metabolic modeling to predict cellular kinetics(53, 54)
and history-dependent behaviors(48, 55, 56).
292
The approach of minimization of metabolic adjustment (MOMA) has been widely used to simulate
cellular behaviors in response to genetic or environmental perturbations(57-59) by minimizing the
sum of absolute changes in metabolic fluxes before and after perturbations(60). Compared with
minimizing the adjustment of metabolic fluxes, we argue that it is more biologically meaningful to
minimize the adjustment of proteome, which now can be achieved by MORP using enzyme-
constrained models. It should be noted that MORP can predict the mismatch between enzyme and
flux levels, which appears to be an impossible mission for the MOMA approach implemented on
conventional GEMs. In addition, it is less computationally expensive to perform the dynamic
simulations on enzyme-constrained models than on fine-grained models, such as ME-models(61,
62) that explicitly formulate gene expression processes(26, 63). Therefore, we expect extensive
applications of MORP and dMORP with the development of enzyme-constrained models(64).
304
In summary, we applied systems biology approaches to decipher the principles of the cellular
response of *B. coagulans* upon the hierarchical utilization of mixed carbon sources, and identified
the dynamic minimization of proteome reallocation to be the cellular objective that dominates the
metabolic behavior in response to rapid environmental changes. In addition, we implemented the
minimization of proteome reallocation as an effective objective function in the metabolic modeling
framework, which would be useful for simulating and understanding cellular responses upon
perturbations.
312
313 **Materials and Methods**
314 **Microorganism, media and culture conditions**
315 *B. coagulans* DSM 1 = ATCC 7050 was purchased from the American Type Culture Collection.
316

317   Seed medium was MRS medium(65), simplified chemically defined medium (CDM) used for
318   fermentation in this study, i.e., MCDM3++, which was developed in our previous study(33). 20 g/L
319   glucose and 20 g/L trehalose were used as the mixed carbon source to better reproduce the
320   phenomenon of hierarchical utilization.
321
Seed culture and shake flask fermentation were performed in 250 mL shake flasks with 100 mL
working volume at 50 °C and 100 rpm, pH was buffered with $CaCO_3$. The cells in seed culture were
collected and washed twice using 100 mM phosphate buffer at around 12 h. Collected cells were
resuspended in ultrapure water with a determined volume and then transferred to the fermentation
medium in shake flasks or 5 L bioreactors. Shake flask fermentation was used to investigate the
metabolic properties of different combinations of mixed carbon sources.
328
329   Batch fermentation was performed in a 5 L bioreactor with 4 L working volume at 50 °C, 100 rpm
330   and 7.2 L/h aeration, and pH was automatically controlled at 5.5 using 25% w/v $Ca(OH)_2$. The
331   samples of different phases were collected for determination of biomass, metabolites,
332   transcriptome and proteome. Fermentations were performed in triplicates for all conditions.
333

Determination of biomass and metabolites
335   The optical density (OD) was detected using a spectrophotometer at 620 nm to characterize the
336   biomass concentration.
337
Lactate, acetate, citate, pyruvate and acetoin in the fermentation broth were determined by high
performance liquid chromatography (HPLC) (Shimadzu LC‑20AT)(13). The Hi-Plex H (300 mm ×
7.7 mm) column was used with 210 nm wavelength and 50 °C column temperature; the mobile
phase was 0.01 mol/L sulfuric acid solution and the flow rate was set to 0.4 mL/min. The HPLC
detection method for ethanol is as follows: the Aminex HPX-87H (300 mm × 7.8 mm) column was
used with refractive index detector and 60 °C column temperature; the mobile phase was 0.01
mol/L sulfuric acid solution and the flow rate was set to 0.6 mL/min.
345
The carbon sources in the fermentation broth were determined by ion chromatography (Dionex
ICS-3000) with Dionex Carbopac PA 20 column, the method was referred to the previous
description(30) and modified. The pretreatment process of the samples was performed as follows:
1) The samples were diluted to achieve sugar concentrations within the detection range. 2)
$Na_2C_2O_4$ was used to precipitate calcium ions in the culture medium. 3) Proteins were removed
from the samples using ethanol. 4) The processed solution was evaporated to obtain the solid form
of the sugar, which was then dissolved in water to obtain the sample for testing. The mobile phase
was ultrapure water and 200 mmol/L NaOH, respectively. The elution procedure was ultrapure
water and 200 mmol/L NaOH eluted at 9:1 ratio for 18 min, then adjusted the ratio to 2:8 to elute
for 17 min, and finally adjusted to 9:1 to balance the column for 35 min, and the flow rate for the
entire process was set to 0.4 mL/min.
357

Reconstruction of genome-scale metabolic models

The model iBcoa620 was reconstructed based on the first *B. coagulans* model iBag597(14): 1) A
combined draft model from KEGG(66) and MetaCyc(67) pathway databases based on the genome
sequences of *B. coagulans* DSM 1 = ATCC 7050 (GCF_000832905.1) was reconstructed by
RAVEN 2.4.0(68). 2) Another draft model was reconstructed by ModelSEED(69) database based
on the genome annotation of RAST(70). 3) Shared reactions in the draft models were integrated
with iBag597. 4) The IDs of genes, metabolites, and reactions were unified into the form of the
KEGG database. 5) Reactions with mass imbalance were corrected. 6) The memote score system
was used to assess the model quality. 7) The model was validated by comparing the predicted and
measure growth rates under different carbon sources.
368
369 The enzyme-constrained model eciBcoa620 was reconstructed using the GECKO toolbox 3.0.
370 Note that k_{cat} values were obtained from BRENDA(71) and GotEnzymes(72) databases and
371 predicted using DLKcat tool(73). Molecular weights of all enzymes were obtained from UniProt(74)
372 database.
373

Simulation methods
MORP is implemented on the enzyme-constraint models, which can estimate both metabolic and
enzyme usage fluxes. MORP estimates the metabolic and enzyme usage fluxes of the model upon
a perturbation based on the minimization of proteome reallocation. Thus, the fluxes of the model
from a reference condition should be used as the input of MORP, which can be obtained in advance
by other algorithms, e.g., FBA, with the enzyme-constraint models. The core of MORP is to
minimize the sum of absolute differences of enzyme usage fluxes between the reference and the
perturbed conditions:

$$\min \quad \sum_{i=1}^{m} |v_{enzyme,i,perturb} - v_{enzyme,i,ref}|$$

$$\text{subject to} \quad \boldsymbol{S} \cdot \boldsymbol{v} = \boldsymbol{0}$$

$$lb_j \leq v_j \leq ub_j$$

385
386 where $v_{enzyme,i,perturb}$ and $v_{enzyme,i,ref}$ represent fluxes of enzyme usage reaction i under perturbed and
387 reference conditions, and m represents the total number of enzyme usage reactions in the model.
388 As MORP estimates fluxes for the perturbed condition, $\boldsymbol{S}$ and $\boldsymbol{v}$ represent the stoichiometric matrix
389 and flux vector of the model for the perturbed condition, and v_j, lb_j and ub_j are the flux, lower and
390 upper bounds of the reaction j, respectively.
391
dFBA based on static optimization approach (75) was used to simulate for the hierarchical
utilization of glucose and trehalose, in which an objective function should be determined for different
time intervals. As mentioned before three objective functions were used, i.e., maximization of
growth, lactate production and NGAM. Generally, dFBA solves:
$$\max \quad v_{o,k} \quad k \in N$$

$$\text{subject to} \quad \boldsymbol{S} \cdot \boldsymbol{v} = \boldsymbol{0}$$

398
$$v_{s,k} = \frac{v_{s,max}[S]_{k-1}}{K_m + [S]_{k-1}}$$

399
$$lb_j \le v_j \le ub_j$$

where k represents the k_{th} time interval, N represents the number of time intervals of the phase of
interest and thus is a positive integer, $v_{o,k}$ is the flux of the objective reaction in P_{gluc}, i.e., the
biomass formation, or the flux of the objective reaction after glucose depletion, i.e., the biomass
formation, lactate production, or NGAM production, $v_{s,k}$ is the flux of the uptake reaction of the
sugar, i.e., glucose or trehalose, of the kth time interval, $[S]_{k-1}$ is the sugar concentration of the (k-
$1)_{th}$ time interval, $v_{s,max}$ is the maximum sugar uptake rate, and K_m is the sugar saturation constant.
The constraints in dFBA were derived from experimentally measured sugars, amino acids, organic
acids data.
408
409 dMORP was proposed to simulate the entire period after glucose depletion in the hierarchical
410 utilization of glucose and trehalose. Here dMORP solves:

411
$$\min \quad \sum_{i=1}^{m} |v_{enzyme,i,r} - v_{enzyme,i,r-1}| \quad r \in N$$

412
$$\text{subject to} \quad \boldsymbol{S} \cdot \boldsymbol{v} = \boldsymbol{0}$$

413
$$v_{s,r} = \frac{v_{s,max}[S]_{r-1}}{K_m + [S]_{r-1}}$$

414
$$lb_j \le v_j \le ub_j$$

415 where r represents the r_{th} time interval after glucose depletion, N represents the number of time
416 intervals of the phase of interest and thus is a positive integer, $v_{enzyme,i,r}$ and $v_{enzyme,i,r-1}$ represent the
417 flux of enzyme usage reaction i for the r_{th} and (r-1)$_{th}$ time interval, respectively, $v_{s,r}$ is the flux of the
418 trehalose uptake reaction of the r_{th} time interval, and $[S]_{r-1}$ is the trehalose concentration of the (r-
419 $1)_{th}$ time interval.
420
421 Minimization of the total proteome was performed to estimate the most efficient usage of the
422 enzymes that maintain the experimentally observed metabolic states:

423
$$\min \quad v_{total\ proteome}$$

424
$$\text{subject to} \quad \boldsymbol{S} \cdot \boldsymbol{v} = \boldsymbol{0}$$

425
$$lb_i \le v_i \le ub_i$$

426 where $v_{total\ proteome}$ represents the flux of total proteome usage, v_i represents the flux of exchange
427 reaction of detected extracellular metabolite, lb_i and ub_i are lower and upper bounds based on
428 measurements.
429

All the simulations were performed with the COBRA toolbox 3.0(76) on Matlab R2019a, and the
solver was Gurobi 9.1 (https://www.gurobi.com/).

Transcriptome analysis
We collected transcriptomics samples at 7 h, 14 h and 48 h, representing P_{gluc}, P_{lag} and P_{tre},
respectively. Cells in the fermentation broth were collected and washed three times with phosphate
buffer saline for subsequent RNA extraction. Total RNA was isolated from cells using TRIzol
Reagent following the instructions and genomic DNA was removed using DNase I (TaKara).
Subsequently, RNA quality was determined using a Agilent2100 Bioanalyzer and quantified using
ND-2000 (NanoDrop Technologies).

RNA library construction was performed using TruSeqTM RNA sample preparation Kit from Illumina
(San Diego, CA). The rRNA was removed using Ribo-Zero Magnetic kit (epicenter), and double-
stranded cDNA was reverse transcribed using random primers (Illumina) and SuperScript double-
stranded cDNA synthesis kit (Invitrogen, CA). To synthesize the second strand of cDNA, it uses
dUTP instead of dTTP, and then eliminates the second strand of cDNA containing dUTP, so that
the library contained only the first strand of cDNA. After PCR amplification by Phusion DNA
polymerase (NEB) and TBS380 (Picogreen) quantification, paired-end RNA-seq sequencing library
was sequenced with the Illumina Novaseq (2 × 150bp read length).

The data generated from Illumina platform were used for bioinformatics analysis, and the reference
genome and gene annotation files of *B. coagulans* DSM 1 = ATCC 7050 were downloaded from
the National Center for Biotechnology Information. All of the analyses were performed using the
free online platform of Majorbio Cloud Platform (www.majorbio.com).

Proteome analysis
We collected proteomics samples at 7 h, 14 h and 48 h, representing P_{gluc}, P_{lag} and P_{tre},
respectively. Cells in the fermentation broth were collected and washed three times with phosphate
buffer saline for subsequent protein extraction. Sample lysis and protein extraction were performed
using SDT (4% SDS, 100 mM Tris-HCl, 1 mM DTT, pH 7.6) buffer, and the protein was quantified
using the BCA Protein Assay Kit (Bio-Rad, USA). Protein digestion was performed with trypsin
following the filter-aided sample preparation (FASP) procedure. The digested peptides from each
sample were subsequently desalted (Empore™ SPE Cartridges C18 (standard density), bed I.D. 7
mm, volume 3 mL, Sigma) and concentrated. The protein for each sample were quantified by SDS-
PAGE. 100 μg peptide mixture for each sample was labeled using TMT reagent according to the
instructions (Thermo Scientific). The labeled peptides were separated by High pH Reversed-Phase
Peptide Fractionation Kit (Thermo Scientific) to obtain 10 different fractions, the collected fractions
were desalted on C18 Cartridges and concentrated.

LC-MS/MS analysis was performed using a Thermo Scientific Q Exactive mass spectrometer
equipped with the Easy nLC system (Proxeon Biosystems, Thermo Fisher Scientific). Peptides
were trapped on a reverse phase trap column (Thermo Scientific Acclaim PepMap100, 100 μm ×
2 cm, nanoViper C18) and separated on the C18-reversed phase analytical column (Thermo

Scientific Easy Column, 10 cm long, 75 μm inner diameter, 3 μm resin). The separation was
achieved using buffer A (0.1% formic acid) and buffer B (84% acetonitrile and 0.1% formic acid) at
a constant flow rate of 300 nL/min controlled by IntelliFlow technology. The mass spectrometer was
operated in positive ion mode. MS/MS analysis was performed using the data-dependent top10
method for high-energy collision dissociation (HCD) fragmentation by selecting the most abundant
precursor ion (300-1800 m/z) in the measurement scan. The MS raw data was subjected to
identification and quantitative analysis using MASCOT engine (Matrix Science, London, UK;
version 2.2) and Proteome Discoverer 1.4 software. The proteome detection and analysis process
were conducted in shanghai applied protein technology co.ltd.
482
483   **Differential expression analysis**
484   Significance analysis between two conditions or phases were performed using the two-sided *t*-test,
485   and a cut-off adjusted *P* value ($P_{adjusted}$) of 0.01 was adopted for identifying differentially expressed
486   transcripts and proteins based on transcriptomics and proteomics data.
487
Determination of intracellular metabolites
The absolute quantification of intracellular amino acids was performed using gas chromatography-
mass spectrometry (Agilent, GC-7890A, MS-5975C). Before the extraction of intracellular
metabolites, a quenching step was performed to terminate cell metabolism. 2 mL of fermentation
broth were added to a 50 mL centrifuge tube containing 30 mL of 60% methanol pre-cooled to -
27 °C. After quenching for 5 minutes, filter paper with attached cells was obtained by filtration.
Simultaneously, 100 μL of U-^{13}C-labeled cell extracts was added to the filter paper as internal
standards. The filter paper was then placed in a 75% ethanol solution pre-heated to 80 °C and
boiled for 5 min. The filter paper was removed, and the remaining liquid was concentrated to 600
μL using rapid evaporation. A 100 μL portion was taken as the sample and subjected to freeze-
drying before derivatization(14, 77, 78).
499
Amino acids derivatization method: 100 μL of pyridine was added to the freeze-dried sample, and
the mixture was dissolved in a 65 °C for 1 hour. After the sample reached room temperature, 100
μL of derivatization reagent (N‑tert‑butyldimethylsilyl‑N-methyl-trifluoroacetamide with 1%
tert‑butyldimethylchlorosilane) was added, and derivatization was carried out in a 65 °C oven for
1 hour. The sample was then centrifuged at 12000 rpm for 5 min, and the supernatant was
subjected to GC-MS analysis.
506
The GC-MS detection conditions were as follows: the interface temperature of the GC-MS was set
at 280 °C, the transfer line temperature was 250 °C, Ionization was done by electron impact with
the temperature being 230 °C, the quadrupole temperature was 150 °C, and the injection volume
was 1 μL. The chromatographic column used was HP-5MS with dimensions of 30 mm × 0.25 mm
× 0.25 μm. For amino acids, the temperature program consisted of an initial column temperature
of 100 °C for 1 minute, followed by an increase at a rate of 10 °C/min to reach 320 °C, which was
then maintained for 10 minutes.
514
515   **Adaptive laboratory evolution**

The adaptive laboratory evolution strategy was performed in a 250 mL shake flask with complex medium, 100 rpm, 50 °C. Alternating cultures of glucose and trehalose were utilized, while the trehalose was supplemented with glucose structural analogue (2-deoxy-D-glucose), which can be absorbed but not be metabolized. Therefore, other sugars are still able to be metabolized even in the presence of glucose, so 2-deoxy-D-glucose can be used for screening mutant strains without catabolite repression effect (79, 80). The aim was to obtain strains that could utilize glucose and trehalose simultaneously. During the evolution process, the cells were transferred to new medium in the exponential phase and maintained the same concentration (OD_{620} about 0.5) after inoculation. The initial total sugar concentration during evolution was kept constant at 130 g/L (glucose 130 g/L, 2-deoxy-D-glucose 40 g/L + trehalose 90 g/L). 40 g/L of 2-deoxy-D-glucose was selected as no growth occurred at higher concentrations. Four evolved strains with the expected phenotypes were examined by MRS plate culture, and the strain with faster sugar consumption rate and higher lactate yield was selected for fermentation experiments in 5 L bioreactor.

Whole-genome sequencing

Cells from the exponential phase in seed shake flasks were collected for genome sequencing. Genomic DNA of *B. coagulans* DSM 1 = ATCC 7050 was extracted using Wizard Genomic DNA Purification Kit (Promega) according to the protocol. Purified genomic DNA was quantified by TBS-380 fluorometer (Turner BioSystems Inc., Sunnyvale, CA). Whole-genome sequencing of wildtype strain and four evolved strains was performed using the de novo sequencing method based on the Illumina NovaSeq6000 platform in this study. The final genome of five strains were annotated from KEGG, GO, COG and other databases using BLASTP, Diamond and HMMER. The same mutated genes of four evolved strains were considered to be genes that could cause phenotypic change.

Data availability

The genome sequences of four evolved strains have been deposited in NCBI database under the BioProject accession number of PRJNA1012373. The transcriptomics data have been deposited in NCBI database under the BioProject accession number of PRJNA1012495. The mass spectrometry proteomics datasets have been deposited in the ProteomeXchange with the dataset identifier PXD045169.

Code availability

The models and code are available at https://github.com/ChenYuGroup/MORP.

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Author contributions

Y.C. and Y.W. conceived the study. Z.L., M.C. and J.H. performed the experiments. Z.L. and Y.C. constructed the models and performed the simulations. Z.L. and Y.C. analyzed the data. Y.C., Z.L. and Y.W. wrote the paper. All authors approved the final paper.

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