1 Creating something out of nothing: Symbolic and non-symbolic

2 representations of numerical zero in the human brain

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16 Summary

17	Representing the quantity zero is considered a unique achievement of abstract human thought.
18	Despite considerable progress in understanding the neural code supporting natural numbers, how
19	numerical zero is encoded in the human brain remains unknown. We find that both non-symbolic
20	empty sets (the absence of dots on a screen) and symbolic zero ("0") occupy ordinal positions
21	along graded neural number lines within posterior association cortex. Neural representations of
22	zero are partly independent of numerical format, exhibiting distance effects with countable
23	numerosities in the opposing (symbolic or non-symbolic) notation. Our results show that format-
24	invariant neural magnitude codes extend to judgements of numerical zero, and offer support to
25	theoretical accounts in which representations of symbolic zero are grounded in more basic
26	representations of sensory absences.
27	

28 Keywords: zero, numerosity, magnitude codes, sensory absence, perception, decoding,

29 representational similarity analysis, MEG

30 Introduction

The number zero plays a central role in science, mathematics, and human culture (Kaplan, 1999; 31 32 Nieder, 2016) and is considered a unique property of abstract human thought (Bialystok & Codd, 33 2000; Nieder, 2016). The psychological basis of zero is unusual: while natural numbers correspond to the observable number of countable items within a set (e.g., one bird; three 34 35 clouds), an empty set does not contain any countable elements. To conceptualise zero, one must instead abstract away from the (absence of) sensory evidence to construct a representation of 36 numerical absence: creating 'something' out of 'nothing' (Butterworth, 1999; Nieder, 2016; 37 38 Wellman & Miller, 1986). Given these differences, it remains an open question as to how zero is 39 represented in relation to other numbers.

40

In contrast to zero, the neural representation of natural numbers is better understood. Distinct 41 neural populations are selective for specific numerosities, exhibiting overlapping tuning curves 42 43 with neighbouring populations tuned to adjacent numerosities (Kutter et al., 2018; Piazza et al., 2004). This architecture underpins a so-called distance effect (Dehaene et al., 1998), where 44 45 numbers close together in numerical space have similar neural representations. For instance, neural responses to numbers one and two are more similar than neural responses to one and ten 46 47 (Borghesani et al., 2019; Luyckx et al., 2019; Piazza et al., 2004). Importantly, a component of 48 this neural code is thought to be invariant to numerical format (Damarla et al., 2016; Eger et al., 2003, 2009; Piazza et al., 2007; Teichmann et al., 2018) such that, for example, neural 49 50 representations of 'six' are shared across symbolic and non-symbolic notations (e.g., both the Arabic numeral "6" and six dots; although see Cohen Kadosh et al. (2007)). In humans, these 51

52 format-invariant representations of numerical magnitude have been localised to the parietal 53 cortex (Damarla et al., 2016; Eger et al., 2009; Piazza et al., 2007), with topographic maps 54 underpinning numerosity perception more broadly being found across association cortex (Harvey 55 et al., 2013; Harvey & Dumoulin, 2017). 56 57 Compared to natural numbers, zero is associated with distinct behavioural and developmental 58 profiles. For instance, the reading times of human adults are increased for zero compared to non-59 zero numbers (Brysbaert, 1995), and zero concepts emerge later in children than those for natural 60 numbers (Krajcsi et al., 2021; Merritt & Brannon, 2013; Wellman & Miller, 1986). Distinct 61 behavioural characteristics associated with zero are not unsurprising given the heightened degree 62 of abstraction required to conceptualise numerical absence. In turn, it is plausible that neural 63 representations of zero are distinct to the scheme that has been discovered for natural numbers 64 (e.g Schubert et al., 2020). Initial research in non-human animals has indicated that numerical 65 zero shares some neural properties with natural numerosities, such as overlapping tuning curves 66 and associated distance effects, along with invariance to particular stimulus properties 67 (Kirschhock et al., 2021; Okuyama et al., 2015; Ramirez-Cardenas et al., 2016). However, it 68 remains unknown whether the symbolic, human conceptualisation of numerical zero, which 69 emerged independently of natural numbers (Ifrah, 1985; Kaplan, 1999), engenders 70 representations of zero that are both distinct from other numbers and which studies in non-human animals may have failed to reveal. 71 72

73 Investigating neural representations of both non-symbolic and symbolic zero can also shed light
74 on how a symbolic concept of numerical absence emerged in human thought. One intriguing idea

75	is that, across phylogeny and ontogeny, low-level perceptual representations tracking an absence							
76	of sensory stimulation (e.g. Merten & Nieder, 2012; Goh et al., 2023) gave rise to conceptual							
77	representations of numerical zero (Nieder, 2016). Specifically, an ability to represent perceptual							
78	absences is hypothesised to support an ability to quantify 'none' as less than one, which, in turn,							
79	may have given rise to our ability to reason and calculate with an abstract symbol – zero –							
80	denoting lack of quantity (Nieder, 2016). Asking whether symbolic neural representations of							
81	zero share variance with non-symbolic empty sets provides an initial empirical test of this							
82	hypothesis.							
83								
84	We tackled these questions by employing two qualitatively different numerical tasks in humans							
85	while leveraging methodological advances to reveal the representational content of neural							
86	responses to numerical stimuli in MEG data (Kriegeskorte & Diedrichsen, 2019; Luyckx et al.,							
87	2019). We assay both neural representations of non-symbolic numerosities (dot patterns),							
88	including zero (empty sets), and symbolic numerals, including symbolic zero. We show how							
89	neural representations of zero are situated along a graded neural number line shared with other							
90	natural numbers. Notably, symbolic representations of zero generalised to predict non-symbolic							
91	empty sets – consistent with a hypothesis that human zero is grounded in perceptual absence							
92	(Nieder, 2016). We go on to localise abstract representations of numerical zero to posterior							
93	association cortex, extending the purview of parietal cortex in human numerical cognition to							
94	encompass representations of zero (Harvey & Dumoulin, 2017; Piazza et al., 2007).							

95

96 **Results**

97 29 human participants (24 after exclusions; see Methods for details) took part in a 98 magnetoencephalography (MEG) experiment involving two numerical tasks. The first was a non-99 symbolic match-to-sample task (Figure 1A) where participants observed two sequentially presented dot patterns that ranged in number from zero dots (empty set) to five dots (Ramirez-100 101 Cardenas et al., 2016). Participants were asked to report whether the patterns contained the same 102 number of dots or not. We employed two sets of dot patterns: a standard set which randomised 103 the size of dots within each pattern, and a control set which kept size, density, and luminance 104 constant across numerosities (Figure 1D). The second task was a symbolic averaging task 105 (Figure 1B; Luyckx et al., 2019). Here, participants observed a rapid serial presentation of 10 symbolic numerals from zero to five (0, 1, 2, 3, 4, 5), divided into orange and blue sets (5 106 107 numbers in each). Participants were asked to report the set of numbers with the higher or lower 108 average. Decision type (higher or lower) was counterbalanced across participants. The use of two 109 different tasks (match-to-sample, averaging), and two different decision types in the averaging 110 task ensured neural patterns induced by the perception of zero are unlikely to be driven by 111 specific task features or calculation requirements.

112

In the non-symbolic match-to-sample task, participants accurately determined whether dot patterns had the same or different numbers of dots (*Mean_{accuracy}*: 0.92, *SE*: 0.16). Plotting behavioural tuning curves revealed near-ceiling performance across all numerosities (Figure 1C), with the exception of five-dot patterns which were more often confused with four-dot patterns than three-dot patterns (t(23) = 4.97, p < .001) – consistent with numerosity tuning curves

- 118 becoming wider as number increases (Dehaene et al., 1998). In the symbolic task, participants
- 119 could reliably perform the task regardless of whether they were reporting the higher
- 120 (Meanaccuracy: 0.71, SE: 0.23) or lower (Meanaccuracy: 0.68, SE: 0.27) average (Figure 1D), and
- there was no difference between performance across decision types (t(22) = -0.88, p = 0.39).
- 122



124 **Figure 1. Experimental Procedure.** A. Trial structure for the non-symbolic match to sample task. Participants observed a sample dot pattern followed by a test dot pattern before reporting 125 126 whether the two patterns had the same or different numbers of dots. B. Trial structure for the 127 symbolic averaging task. Participants observed a sequence of blue and orange numerals before 128 reporting which set of numerals had the higher or lower average. C. Behavioural tuning curves in 129 the non-symbolic task. Each curve reflects the percentage of trials that participants judged the 130 test numerosity to be the same as the sample numerosity. Each colour represents trials with 131 specific sample numerosities. The peak of each curve illustrates correct performance when the sample and test numerosities matched. Data points either side of the peak represent non-match 132 trials. Error bars indicate SEM. D. Accuracy in the symbolic task split across participants who 133

judged which set of numbers was higher, and those who judged which was lower. *E. Stimulus sets for dot task.* Dot size was pseudorandomised in the standard set, while low level properties
of the dots including size, density, and luminance were held constant in the control set.

137

138 Identifying Neural Representations of Number

We next asked whether neural patterns recorded by MEG were sensitive to numerosity, by 139 140 timelocking our data to the presentation of the dot pattern/symbolic numeral stimuli. Multiclass 141 decoders were trained to classify different numerosities (zero to five) in both the non-symbolic 142 and symbolic tasks. The frequency with which the decoders confused numerosities for one another is illustrated in Figure 2A. Here, individual panels represent trials where a particular 143 144 numerosity was presented to the classifier, and the coloured lines indicate the proportion of those 145 trials where the classifier predicted each one of the possible classes (zero to five) over the trial epoch. For example, the "NS-one" panel shows that when one dot is presented in the non-146 147 symbolic task, the classifier predominantly and correctly labels this stimulus as numerosity one 148 (yellow curve), with the next most likely error being a misclassification as the number two 149 (green curve). Across all numbers and both formats, the classifiers successfully predicted the 150 numerosity participants were viewing from their neural data, including zero numerosities.

151

We next leveraged temporal generalisation analysis to ask whether numerosity representations were stable over time (King & Dehaene, 2014) (Figure 2B). When training and testing on all combinations of time points, stable time-windows where numerical information could be decoded above chance level were identified in both tasks from shortly after stimulus presentation

156	up until the end of the analysed time window (non-symbolic: 70ms – 800ms; symbolic 56.7ms –
157	800ms). These time windows in which stable numerosity representations were identified were
158	used to create time-averaged data for use in subsequent population tuning curve (Figure 2D) and
159	multidimensional scaling (Figure 2E) analyses.
160	
161	A Neural Number Line from Zero to Five
162	A fundamental feature of neural codes for natural numbers is a distance effect, whereby numbers
163	closer together in numerical space are closer together in representational space (Dehaene et al.,
164	1998; Nieder & Dehaene, 2009). Here we asked whether numerical zero exhibits similar distance
165	effects with other numbers, consistent with it sharing a neural number line with countable
166	numerosities. A Representational Similarity Matrix (RDM) describing a distance effect from
167	zero to five successfully predicted neural data across both non-symbolic and symbolic numerical
168	formats (Figure 2A). In the non-symbolic task, an RDM generalising numerical information
169	across the two non-symbolic stimulus sets significantly predicted neural responses throughout
170	the trial, indicating that neural correlates of number were independent of the physical properties
171	of the dot stimuli (Supplemental Figure 1). Multidimensional scaling of neural representations
172	of numerosity in turn illustrates a distance effect (Figure 2E), with the numbers zero to five
173	occupying positions along a single, ordered dimension, while a second dimension loosely
174	distinguished intermediate numerosities (one to four) from the extremes (zero and five).

175

176 A stronger test of a distance effect in neural data is furnished by examining the confusability177 between neighbouring numerosities using population tuning curves (Figure 2D). These plots are

178	time-averaged versions of the classifier confusion matrices in Figure 2A, i.e. the proportion of							
179	trials where the classifier predicted a particular numerosity as a function of the true numerosity							
180	within the time window in which numerical information could be reliably decoded (Figure 2B).							
181	For example, the red curve in Figure 2D indicates that the proportion of trials predicted as being							
182	zero peaks when the numerosity seen by the decoder was also zero, is next highest when the							
183	numerosity seen by the decoder was "one", and so on.							
184								
185	In the non-symbolic task (Figure 2D, left), the classifier confuses zero with one							
186	$(Mean_{proportion \ predicted} = 0.218)$ more often than it confuses zero with two							
187	$(Mean_{proportion \ predicted} = 0.138)$ (t(23) = 6.23, $p < .001$). Similarly, it confuses one with two							
188	$(Mean_{proportion\ predicted} = 0.206)$ more often than with three $(Mean_{proportion\ predicted} = 0.206)$							
189	0.155) (t(23) = 4.76, $p < .001$),. This pattern of results is indicative of a gradedness in the							
190	representation of numerical magnitude across non-symbolic numerosities. In contrast, in the							
191	symbolic task (Figure 2D, right), the multiclass classifier does not confuse zero with one							
192	$(Mean_{proportion \ predicted} = 0.159)$ significantly more than it confuses zero with two							
193	(<i>Mean</i> _{proportion predicted} = 0.163) (t(23) = -0.61, $p = 0.54$), nor does it confuse one with two							
194	$(Mean_{proportion \ predicted} = 0.153)$ significantly more than it confuses one with three							
195	(<i>Mean</i> _{proportion predicted} = 0.143) (t(23) = 1.67, $p = 0.11$). This difference in distance effects							
196	between non-symbolic and symbolic formats was statistically significant for both zero ($t(23) =$							
197	5.45, $p < .001$) and one (t(23) = 3.48, $p = .002$), and is suggestive of more gradedness in the							
198	representation of non-symbolic than symbolic numerosities, consistent with previous work							
199	describing narrower tuning curves for symbolic numerals (Eger et al., 2009; Kutter et al., 2018).							

201



Figure 2. A Neural Number Line from Zero to Five. *A*. Across-time confusion matrices for
multiclass decoders classifying non-symbolic (top) and symbolic numerosities (bottom).
Individual panels represent trials where particular numerosities were presented to the classifier.
Coloured lines indicate the proportion of those trials where the classifier predicted each
numerosity. *B*. Temporal generalisation of multiclass decoders trained to decode numerosities

208 zero to five in the non-symbolic (left) and symbolic (right) task reveals stable numerical 209 representations over time in both tasks emerging shortly after stimulus presentation. Black lines 210 illustrate timepoints where decoding was significantly above chance (p < .05, corrected for 211 multiple comparisons). These stable time windows were used in the time-averaged analyses 212 depicted in panels D and E. C: A model representational dissimilarity matrix (RDM) describing 213 a distance effect from zero to five significantly predicted neural data in both non-symbolic and 214 symbolic tasks. The diagonal of the RDM was not included in this analysis, preventing the self-215 similarity of each number from trivially explaining our results. Shaded areas indicate 95% 216 confidence intervals. Horizontal lines show clusters of time where dissimilarity correlations were 217 significantly above 0, p < .05 corrected for multiple comparisons. D. Population level tuning 218 curves derived from decoder confusion matrices. Each curve represents the proportion of trials 219 the classifier predicted a particular numerosity (indicated by the curve's colour) as a function of 220 the numerosity the decoder actually saw. For example, the red curve illustrates how the 221 prediction of numerosity zero is distributed across different presented numerosities. For non-222 symbolic numerosities, the classifier confused numbers as a function of their numerical distance, 223 consistent with a graded representation of numerical magnitude. In the symbolic task, 224 representations were more categorical than graded. Error bars represent SEM. E. 225 Multidimensional scaling of numerical representations in both tasks revealed a principal 226 dimension which tracks numerical magnitude and a second dimension which loosely 227 distinguishes extreme values from intermediate values.

228

229 <u>Representations of Zero are Shared Between Symbols and Empty Sets</u>

230 Together, our previous analyses establish that neural representations of zero are graded 231 (especially for non-symbolic numerosities) and situated within a number line spanning other 232 countable numerosities from 1 to 5. We next asked whether representations of zero were format-233 and task-independent – generalising across non-symbolic (empty set) and symbolic ("0") stimuli, 234 and across the same/different and averaging tasks. To test this hypothesis, we performed further 235 decoding analyses focused on dissociating numerical zero from non-zero numerosities. If a 236 binary classifier trained to distinguish zero from non-zero numerosities in one numerical format 237 is subsequently able to separate zero from non-zero numerosities in another numerical format, 238 this furnishes evidence for an abstract neural representation of numerical absence that is common 239 to both formats.

240

241 Decoders trained to distinguish numerical absence within each format separately revealed stable 242 representations of numerical zero from approximately 100ms to 450ms after stimulus 243 presentation, before exhibiting a more dynamic temporal profile until the end of the trial epoch 244 (Figure 3A, top). Crucially, these decoders could also successfully classify representations of 245 zero in the opposing format to which they had been trained (Figure 3A, bottom) – both when 246 generalising from empty sets to the decoding of symbolic numerosities, and when generalising 247 from symbolic zero to non-symbolic dot stimuli. This cross-decoding was successful over the 248 initial 350ms period where the within-format decoders identified stable representations of 249 numerical absence, although generalisation was generally stronger when generalising from 250 symbolic zero to empty sets than vice-versa.





253 Figure 3. Abstract and Graded Representations of Numerical Absence. A. Representations 254 of numerical absence generalise over numerical format. Top: A decoder trained to decode zero from natural numbers reveals stable representations of zero up to ~450ms after stimulus 255 256 presentation for both non-symbolic (left) and symbolic (right) formats, with more dynamic / 257 unstable representations observed towards the end of the epoch. Bottom-left: A decoder trained 258 to decode empty sets also distinguished symbolic zero from non-zero symbolic numerals. 259 Bottom-right: A decoder trained to distinguish symbolic zero from non-zero symbolic numerals 260 also distinguished empty sets from non-symbolic numerosities. Black lines indicate clusters of 261 significantly above chance decoding, p < .05, corrected for multiple comparisons. B. Left: Illustration of the hypothesis that abstract representations of numerical absence are situated on a 262 graded number line that generalises across format, with empty sets represented as more similar to 263 symbolic numeral one than numeral five (top), and symbolic zero as more similar to one dot than 264 265 five dots (bottom). Centre: Training a classifier to decode non-symbolic empty sets from non-

266	symbolic numerosities and testing it on symbolic numbers in a pairwise manner revealed
267	increasing discriminability as distance from zero increased (top). The same cross-format distance
268	effect is observed when training a classifier on symbolic zero and testing it on non-symbolic
269	numerosities (bottom). Shaded areas represent 95% CIs. Right: clusters of significant differences
270	between different numerosities' discriminability from zero, p<.05, corrected for multiple
271	comparisons. An increase in discriminability for numbers further from zero reveals a cross-
272	format distance effect.
273	
274	Graded Representations of Zero are Invariant to Numerical Format
275	Next, to establish the representational structure of cross-format representations of zero, we
276	leveraged the numerical distance effect already identified for within-format representations
277	(Figure 2). To test for such effects, we computed the discriminability between zero and each
278	non-zero numerosity in the alternative numerical format (Figure 3B, middle). Strikingly, neural
279	representations of symbolic zero ("0") were more often confused with one or two dots in the
280	non-symbolic task, than they were with four or five dots (Figure 3B, middle). Similarly, neural
281	representations induced by non-symbolic zero (empty sets) were more often confused with the
282	symbolic numeral 1 or 2 than they were with symbolic numerals 4 or 5. Pairwise tests comparing

the discriminability of different non-zero numerosities from zero revealed clusters of significant

285 discriminability. Together, these cross-format analyses support a hypothesis that an approximate,

differences in discriminability (Figure 3B, right), with an increased distance from zero increasing

286 graded representation of numerical absence is engaged not only by symbolic zero ("0") but also

287 by lower-level perceptual absences (empty set stimuli).

288

284

We also sought to test a more stringent hypothesis that abstract, format-independent neural 289 290 representations of zero are themselves situated within a cross-format neural number line – 291 essentially extending the question of format-independence to now include all numerosities from 0 to 5. A representational dissimilarity matrix situating abstract numerosity representations 292 293 within a graded number line significantly predicted the neural data (Supplemental Figure 2, left). 294 Testing for cross-format distance effects between all numerosities using RSA also revealed a qualitative distance effect, although this did not reach statistical significance (Supplemental 295 Figure 2, right). Finally, multidimensional scaling of neural representations induced by symbolic 296 297 and non-symbolic numerosities in a shared space corroborated evidence for a distance effect for 298 zero across tasks (Supplemental Figure 3). 299

300 <u>Abstract Representations of Numerical Zero are Localised to Posterior Association Cortex</u>

301 Finally, we sought to reconstruct and compare source-level neural activity for zero and non-zero 302 numerosities in both the non-symbolic and symbolic tasks. By performing mass-univariate 303 contrasts of broadband source power (zero > non-zero numerosities) in both the non-symbolic 304 (Figure 4A top; peak voxels (xyz): left hemisphere = -36, -24, 56; right = 60, -64, -24) and 305 symbolic (Figure 4A bottom; peak voxels (xyz): left hemisphere = -28, -56, 32; right = 28, -72, 8) 306 tasks and computing the conjunction between these two contrasts (Figure 4B; peak voxels within 307 conjunction (xvz): non-symbolic task: left hemisphere = -20, -64, 32; right = 60, -64, -24; symbolic task: left hemisphere = -28, -56, 32; right = 20, -48, -64), we are able to show that 308 309 neural activity induced by numerical absence is distributed across the posterior association cortex 310 (Figure 4B). Neural responses to zero within this conjunction map were again situated within a



312 dimension that was similar for both symbolic and non-symbolic formats (Figure 4, bottom-right).



cortex. *A*: Mass univariate contrasts of source power revealed regions more active following presentations of zero vs. non-zero numerosities in non-symbolic (top) and symbolic (bottom) tasks. Colour represents t-value and only clusters significant at p < .05 are presented, corrected for multiple comparisons. *B*: A conjunction of zero > non-zero contrasts in both numerical formats yielded a map identifying broad regions of the posterior association cortex as representing numerical absence across numerical formats. Multidimensional scaling of each

numerosity's neural pattern within these regions revealed a graded representational structure ofnumerical magnitude along a single dimension that was similar for both formats.

334

335 **Discussion**

336 The number zero is associated with unique psychological properties compared to natural 337 numbers. Here, we characterise the neural representation of numerical zero in the human brain. We describe how numerical zero occupies a slot at the lower end of neural number lines for both 338 339 symbolic and non-symbolic numerical formats. Strikingly, we show that a component of this representation is both task- and format-independent, such that empty sets – the absence of dots – 340 341 generalised to predict the neural profiles and distance effects observed for symbolic zero. These 342 abstract, format-invariant representations of zero were situated at the lower end neural code for number that was localised across the posterior association cortex. 343

344

345 That zero is situated at the lower end of a neural number line in the human brain is consistent 346 with an emerging body of work examining representations of zero in non-human animals 347 (Kirschhock et al., 2021; Okuyama et al., 2015; Ramirez-Cardenas et al., 2016). Across two 348 different studies, single neurons selective for non-symbolic empty sets were found in the parietal 349 and prefrontal cortex of non-human primates (Okuyama et al., 2015; Ramirez-Cardenas et al., 350 2016). In line with the present results, many of these neurons – but not all – were found to 351 exhibit distance effects with non-zero numbers. When comparing non-symbolic and symbolic 352 instances of zero, we found symbolic instances were more discrete and less graded than non-353 symbolic instances, consistent with work describing sharper tuning curves for symbolic number

representations (Eger et al., 2009; Kutter et al., 2018). Recent single-cell recordings in the human
medial temporal lobe have also identified discrete symbolic zero-selective neurons that did not
exhibit graded activations in relation to non-zero symbolic numerals (Kutter et al., 2023).
Strikingly, however, the majority of our analyses revealed a graded representation of zero that
generalised across both symbolic and non-symbolic formats, in keeping with behavioural
findings that situate zero at the lower end of a graded psychological number line in humans
(Merritt & Brannon, 2013).

361

362 Our finding that representations of numerical absence have a format-invariant component 363 extends previous work documenting neural representations of numerosity that generalise across 364 countable non-symbolic elements and their symbolic counterparts (Eger et al., 2009; Libertus et 365 al., 2007; Piazza et al., 2007). Here we show how neural representations of non-symbolic empty 366 sets, which do not contain any countable items, also share variance with symbolic zero (Figure 367 3). These abstract representations of zero were localised to regions of the posterior association 368 cortex that have previously been associated with numerical processing (Figure 4B; Arsalidou & 369 Taylor, 2011; Eger et al., 2003; Harvey & Dumoulin, 2017; Piazza et al., 2007). It remains 370 debated whether findings of format-invariant numerical codes are explained by single neurons 371 coding for the same numerosities across formats, or whether they reflect the recruitment of 372 neighbouring format-specific neural populations that are interdigitated within a numerosity map 373 (Cohen Kadosh & Walsh, 2009). Future intracranial recording studies will be required to 374 determine whether single cells in the human brain code for numerical zero in both non-symbolic 375 and symbolic formats. However, our finding of cross-format distance effects is more consistent 376 with a shared neural code, as it is less likely that spatially overlapping but format-specific neural

377 codes would also generalise to exhibit cross-format distance effects with more distant378 numerosities.

379

380 Finding shared neural representations of non-symbolic empty sets and symbolic zero lends 381 weight to recent suggestions that representations of numerosity zero may have emerged from 382 more fundamental representations of sensory absence (Nieder, 2016). On this account, low-level 383 perceptual representations indicating an absence of sensory stimulation (e.g. Merten & Nieder, 384 2012; Goh et al., 2023) provide the perceptual grounding for a conceptual representations of 385 numerical zero (Nieder, 2016) - consistent with a broader principle that the human brain co-opts 386 basic sensory and motor functions in the service of more complex cognitive abilities (Dehaene & 387 Cohen, 2007). Such a hypothesis is consistent with similar behavioural signatures for the 388 processing of absence across perceptual and numerical domains. For instance, reading times are 389 increased for number zero compared to non-zero numbers (Brysbaert, 1995), whilst reaction 390 times for deciding a stimulus is absent are higher than for deciding a stimulus is present (Mazor 391 et al., 2020, 2021). Additionally, judgements about the absence of features mature later in 392 children than judgements about presence (Coldren & Haaf, 2000; Sainsbury, 1971), a 393 developmental pattern mirrored by the late mastery of numerical zero in children (Krajcsi et al., 394 2021; Merritt & Brannon, 2013; Wellman & Miller, 1986). We note however that the neural 395 responses recorded in our study to empty-set stimuli were still within the context of a numerical 396 task – and, as such, only provide initial evidence for a perceptual grounding of zero. A stronger 397 test of this hypothesis would examine shared representations of numerical and perceptual 398 absence - for instance, classifying a stimulus as absent in a non-numerical task (Mazor et al., 399 2020; Merten & Nieder, 2012; Barnett et al., 2023).

400

401	We took care to ensure that the neural representations of zero identified in our data were not
402	trivial consequences of zero being classified as the "lowest" stimulus in our tasks. The concern
403	here is that if our tasks required participants to adopt a particular mathematical attitude towards
404	zero, then decoding of this task-dependent concept would confound any results aimed at
405	identifying task-invariant representations of numerical absence. We consider this explanation of
406	our results as unlikely, however, as, by design, the symbolic and non-symbolic tasks required
407	adopting qualitatively distinct mathematical attitudes towards zero stimuli: the match-to-sample
408	task necessitated deciding whether two dot stimuli were the same or different, whereas the
409	symbolic task required maintenance of condition-specific numerical averages. Because the non-
410	symbolic task did not require participants to order stimuli, any format-invariant representations
411	of zero cannot be explained by a generic requirement to identify lower vs. higher numerosities.

412

413 The adoption of the number zero has enabled great advances in science and mathematics 414 (Kaplan, 1999). Here, we show that the human brain represents this unique number by 415 incorporating representations of numerical absence into a broader neural coding scheme that also supports countable numerosities. Representations of numerical zero were found to be format-416 417 invariant and graded with respect to non-zero numerosities, and were localised to regions of the 418 posterior association cortex previously implicated in numerical cognition. Our results 419 demonstrate that neural number lines include zero, and, more importantly, provide initial 420 evidence that the abstract concept of symbolic zero is linked to representations of non-symbolic 421 empty sets. Our study lays the foundations for a deeper understanding of how the human ability

to represent the number zero may be grounded in perceptual capacities for detecting an absenceof sensory stimulation.

424

425 Materials and Methods

426 <u>Participants</u>

427 29 participants (M_{age} : 29.27 years, SD_{age} : 10.69) took part in the MEG experiment at the

428 Wellcome Centre for Human Neuroimaging, University College London. 5 participants either

429 failed to follow task instructions (chance performance on one or more tasks) or did not complete

the experiment and were therefore excluded from analysis. All analysis was performed on the

431 remaining sample of 24 participants. Informed consent was given before the experiment and

432 ethical approval was granted by the Research Ethics Committee of University College London

433 (#1825/005).

434

435 <u>Stimuli</u>

Numerical dot stimuli were created using custom MATLAB (Mathworks) scripts and consisted 436 437 of different numbers of dots (from zero to five) on grey backgrounds (Figure 1C). There were 438 two sets of dot stimuli, a standard set and control set. In the standard set, dot size was 439 pseudorandomly specified, while in the control set, low level visual properties of the stimuli (dot 440 size, density, luminance) were constant across numerosities. Empty set stimuli contained only a 441 grey background in both stimulus sets. To help prevent participants relying on low level visual 442 cues in identifying empty set stimuli, the background luminance was varied within and across stimulus sets, the background square size was randomly varied across all stimuli, and 50% of 443

444	dots were white rather than black. A control analysis confirmed that numerical information was
445	extracted from the stimuli independently from physical features (see Representational Similarity
446	Analysis; Supplemental Figure 1).
447	
448	Experimental Procedure
449	The tasks were presented to subjects using MATLAB (Mathworks) and the Psychophysics
450	Toolbox (Brainard, 1997; Kleiner et al, 2007). Participants practiced the tasks on a computer
451	before the MEG session. In the MEG scanner, the tasks were performed in alternating
452	miniblocks with 35 symbolic trials and 54 non-symbolic trials per MEG recording block. The
453	order of the tasks would swap on each block, and the starting order was counterbalanced across
454	participants. There were 9 MEG blocks in total, resulting in 315 symbolic numeral trials and 486
455	non-symbolic dot trials across the whole experiment. Participants responded using two buttons
456	and their right thumb.

457

458 Non-symbolic Task

Participants performed a match to sample task on dot stimuli (Kirschhock et al., 2021; Ramirez-Cardenas et al., 2016). On each trial, participants saw a sample image containing between zero and five dots for 250ms followed by a fixation cross for 800ms. A test image, also containing between zero and five dots, was then presented for 250ms, followed before another 800ms fixation period (Figure 1A). Within a trial, a single stimulus set was used for both the sample and test image. Participants reported whether the number of dots in the test stimulus matched that of the sample stimulus, or not. The response was followed by feedback in the form of a coloured

466 rectangle surrounding the response options, with green and red used to indicate correct and 467 incorrect answers, respectively. Response options were positioned randomly on each trial to 468 eliminate any correlation between the decision and motor response. Intertrial intervals were also 469 sampled randomly from a uniform distribution between 500-1000ms.

470

471 Symbolic Task

472 We adapted the symbolic numeral averaging task introduced by Luyckx et al. (2019) to include 473 the number zero. In one trial, ten numerals ranging from zero to five were presented in a random 474 order (Figure 1B). Five of the numerals were blue and five were orange. Each numeral was displayed for 250ms with an interstimulus interval of 100ms. The numerals were randomly 475 476 selected on each trial to obey the constraint that the mean of the blue numerals could not equal 477 the mean of the orange numerals. The response required at the end of each trial was 478 counterbalanced across subjects, with half of the subjects reporting which set of numerals 479 (orange or blue) had the highest average, and the other half reporting the set with the lowest 480 average. Participants had 2000ms to respond, after which they were given feedback in the form 481 of a green (correct) or red (incorrect) rectangle surrounding the response options. Again, to 482 disentangle participants' decisions from motor responses, response options were positioned 483 randomly on each trial. Intertrial intervals were randomly sampled from a uniform distribution 484 between 500-1000ms.

485

486 <u>MEG Preprocessing</u>

MEG data were analysed using FieldTrip (Oostenveld et al., 2011). MEG was recorded 487 488 continuously at 600Hz using a 273-channel axial gradiometer system (CTF Omega, VSM MedTech) while participants sat upright inside the scanner. To remove line noise, the raw MEG 489 490 data were preprocessed with a Discrete Fourier Transform and bandstop filter at 50Hz and its 491 harmonics. The numeral task was segmented into epochs of -500ms to 4000ms relative to trial 492 onset. For the dot task, the segments were from -200ms to 2500ms. Baseline correction was performed where, for each trial, activity in the pre-trial window was averaged and subtracted 493 494 from the entire epoch per channel. The data were downsampled to 300Hz to conserve processing 495 time and improve signal to noise ratio. During artefact rejection, trials with high kurtosis were 496 visually inspected and removed if they were judged to contain excessive artefacts. To assist in 497 removing eye-movement artefacts, an independent components analysis was carried out on the 498 MEG data, and the components with the highest correlation with eye-tracking data were discarded after visual inspection. Components showing topographic and temporal signatures 499 500 typically associated with cardiac artefacts were also removed by eye. This procedure was 501 performed separately for the numeral and dot task. Finally, a second stage of epoching was 502 performed to generate trials of individual numerosities. In the numeral task, trials were 503 segmented into -100ms to 800ms epochs around each numeral onset. Trials were then baseline 504 corrected again using the pre-stimulus window. In the dot task, trials were segmented into two 505 different -200ms to 800ms epochs with respect to the onsets of the sample and test stimuli. All 506 analyses used the sample images only. Finally, all analyses focusing on shared representations 507 across notational formats were performed on the shared timepoints of -100ms to 800ms relative 508 to stimulus presentation.

509

510 <u>Representational Similarity Analysis</u>

511 Representational Similarity Analysis (RSA) allows us to test specific hypothesis about how 512 neural representations are structured (Kriegeskorte & Kievit, 2013). Here, we tested for the 513 existence of a distance effect across numerosities (Figure 2C). To do this, we defined a model 514 representational dissimilarity matrix (RDM) that describes the dissimilarity of two numerosities 515 as a function of their numerical distance. To compare this model dissimilarity matrix with the 516 neural data we first created a neural dissimilarity matrix that represents the similarity in neural 517 patterns associated with each numerosity. To do this, we first ran a linear regression on the MEG 518 data with dummy coded predictors for each of the six numerosities (trial numerosity coded with 519 a 1, alternative numerosities coded with a 0). This produced a coefficient weight for each 520 numerosity at each time point and sensor. These weights were then combined into a vector, 521 representing the multivariate neural response for each numerosity, averaged over trials. To create the neural RDM, we computed the Pearson distance between each pair of condition weights over 522 523 sensors, resulting in a 6x6 neural RDM reflecting the pairwise similarity of neural patterns 524 associated with each numerosity. These neural RDMs were smoothed over time via convolution 525 with a 60ms uniform kernel. To compare the neural and model RDMs, at every time point we 526 correlated the lower triangle of each matrix (excluding the diagonal) using Kendall's Tau rank 527 correlation (Nili et al., 2014).

528

Cross-task RSA was performed in the same manner, except here there were 12 predictors in the
linear regression (0-5 symbolic, 0-5 non-symbolic). This resulted in a 12x12 neural RDM, of
which we used the quadrant representing the cross-task pairwise similarities between
numerosities when comparing with the model RDM (Supplemental Figure 2). The whole

quadrant including the diagonal was used in this analysis. This is because here the diagonal does
not contain redundant information, but rather the similarity of the same numerosity across two
different notations, and cells in the upper triangle represent different pairwise similarities to
those in the lower triangle.

537

Finally, to test whether numerical information was decodable from non-symbolic stimuli over
and above the physical features of the stimuli, we ran a cross-stimulus set RSA in the same
manner as above, except now we tested exclusively within the non-symbolic task (Supplemental
Figure 1). As such, the 12 predictors were: 0-5 from the standard set and 0-5 from the control set.
This RSA established whether representations of numerical magnitude generalised across
stimulus set, and therefore went beyond information that could be derived solely from physical
features of the stimuli.

545

546 Decoding Analyses

To examine the representational structure of the number zero more specifically across symbolic 547 548 and non-symbolic formats, we employed different decoding techniques using both multiclass and 549 binary decoders. First, to reveal the temporal profile of numerosity representations, we trained a 550 multiclass Linear Discriminant Analysis (LDA) decoder to decode numerosities zero to five 551 (Figure 2B). This was performed in a temporal generalisation procedure, whereby the classifier 552 was trained on each time point and tested on all other time points (King & Dehaene, 2014). This 553 process results in a train time x test time decoding accuracy matrix, which illustrates how stable 554 representations of numerosity are over time.

555

556	We performed both within-notation and cross-notation decoding procedures. Within-notation
557	decoding involved training and testing a classifier to identify numerosities on trials from one
558	notation (e.g. numerals or dots). In cross-notation decoding, we trained the classifier on one
559	notation and tested it on the other (e.g., training on symbolic trials and testing on non-symbolic
560	trials, and vice versa). For the within-notation approach, we implemented a 5-fold cross-
561	validation strategy. Prior to decoding, five trials per numerosity were averaged and the resulting
562	average trials was balanced per numerosity. It is worth noting that cross-validation is not
563	required in cross-notation decoding because the test data is never seen by the classifier during
564	training, and thus there is no risk of overfitting. Cross-notation decoding allows us to empirically
565	assess whether the neural patterns associated with numerals share a common neural code across
566	notations.

567

568 To complement our RSA analyses and isolate the representational structure underpinning 569 numerical zero specifically, we extracted the confusion matrices from the decoders (Figure 2A, 570 2D). Confusion matrices indicate how often different stimulus classes (i.e., numerosities) are confused for one another, and this information can be used to infer the organisation of neural 571 572 representations. For example, a decoder that confuses zero with the number one more than the 573 number two displays evidence for a numerical distance effect. The data used to train the decoders 574 from which these confusion matrices were extracted was time-averaged over the timepoints 575 where the initial multiclass decoder could decode numerosity significantly above chance (nonsymbolic: 70ms - 800ms, symbolic 56.7ms - 800ms; Figure 2B). We also computed confusion 576 577 matrices across time (Figure 2A).

578

579	To examine whether representations of zero could reliably be dissociated from numerosities
580	presented in the alternative format, we created a decoding procedure using a binary LDA
581	classifier to decode zero vs. non-zero numerosities (Figure 3A). Within this training regime, the
582	number of trials per non-zero numerosities was kept equal, and the number of zero trials vs. non-
583	zero numerosity trials was also balanced. The resulting 'zero' decoder was uniquely trained to
584	identify neural representations of numerical zero in symbolic or non-symbolic notation and was
585	tested on the other format to identify format-invariant representations of zero.

586

587 Finally, to reveal whether abstract representations of numerical zero exist on a graded number 588 line, or whether they are categorically distinct from other numbers, we ran a new cross-format 589 decoding analysis using binary classifiers. Here, we trained the decoders to discriminate zero vs. 590 all non-zero numerosities (one to five) separately, and then tested these binary decoders on the 591 corresponding numerosities in the opposite notation. This resulted in five different classifiers per 592 notation. Specifically, we trained five different decoders to dissociate: symbolic zero vs symbolic 593 one, symbolic zero vs symbolic two, symbolic zero vs symbolic three, symbolic zero vs 594 symbolic four, and symbolic zero vs symbolic five. We then tested these decoders on empty sets 595 vs one dot, empty sets vs two dots, empty sets vs three dots, empty sets vs four dots, and empty 596 sets vs five dots, respectively. This was also done in the reverse direction: training on non-597 symbolic trials and testing on symbolic numerals. We used the area under the receiver operating 598 characteristic (AUROC) as a metric for discriminability between each pair of classes. In line 599 with the hypothesis that format-invariant representations of zero exist on a graded, abstract 600 neural number line, we expected the discriminability to improve as the numerical distance from

601	zero increased (Figure 3B). To statistically test whether this was the case, we performed one-
602	tailed, paired comparisons between the discriminability of successive numbers with zero (e.g., by
603	comparing 0-2 vs. 0-1, 0-3 vs. 0-2, etc.; Figure 3B).

604

For all decoding analyses, we utilized multiclass or binary LDA decoders in conjunction with the
MVPA-light toolbox (Treder, 2020) integrated with FieldTrip. To improve the robustness of the
classifier, we applied L1-regularization to the covariance matrix, and the shrinkage parameter
was automatically determined using the Ledoit-Wolf formula within each training fold (Ledoit &
Wolf, 2004).

610

611 <u>Source Reconstruction</u>

612 Both FieldTrip's template single shell head model and its standard volumetric grid (8mm 613 resolution) were warped to participants' individual fiducial points, generating a subject-specific 614 forward model aligned in MNI space. Source reconstruction was performed using a linearly constrained minimum variance (lcmv) beamformer (Van Veen et al., 1997) which applies spatial 615 616 filters to the MEG data to generate source-level time courses. To reduce the impact of noise on 617 the source estimates, we used a regularisation parameter of lambda = 5%. For each task, spatial 618 filters were calculated by combining the leadfield matrix with the data covariance matrix across 619 all numerosities and the timepoints coinciding with the stable cluster of significantly above-620 chance decoding in the zero vs. non-zero cross-task classifier (100 - 450 ms). These spatial filters 621 were then applied to zero trials and non-zero trials separately, generating reconstructed maps of 622 source activity for these two trial types. We contrasted the broadband source power of zero >

623	non-zero trials in a mass-univariate procedure across subjects for each task separately (Figure
624	4A) with an alpha parameter of $p < .05$, corrected for multiple comparisons. For binary LDA
625	classifiers, this is equivalent to localising the classifier weights (Haufe et al., 2014), and therefore
626	gives an indication of which brain regions drove our decoding results. We computed the
627	conjunction of these two contrasts, revealing the voxels where zero stimuli were dissociable from
628	other numbers in both symbolic and non-symbolic notations (Figure 4B).
629	
630	Multidimensional scaling of source space activity was performed using the same beamforming
631	parameters to calculate spatial filters over combined non-symbolic and symbolic trials. Using
632	these filters, virtual channels were created for each source location within the map defined by the
633	conjunction analysis. The virtual channels were then used to create a cross-task representational
634	dissimilarity matrix in the same manner as described for the cross-task RSA sensor-level
635	analysis. This was then submitted to MATLAB's cmdscale function for multidimensional
636	scaling.
637	
638	Statistical Inference
639	Across sensor and source level analyses, cluster-based permutation testing was used to
640	statistically test hypotheses and correct for multiple comparisons (Maris & Oostenveld, 2007).
641	For all analyses (decoding, RSA, and source-level contrasts), 1000 permutations were used with

- 642 cluster-forming alpha parameter of .05 and a significance threshold of .05. It is important to
- 643 emphasize that this cluster-based permutation testing approach does not provide information
- 644 about when neural representations emerge. This limitation arises because the statistical inference

- 645 process does not focus on individual time points; instead, it relies on cluster-level statistics that
- 646 encompass multiple time points (Sassenhagen & Draschkow, 2019).

647

648 **References**

- 649 Arsalidou, M., & Taylor, M. J. (2011). Is 2+2=4? Meta-analyses of brain areas needed for
- numbers and calculations. *NeuroImage*, *54*(3), 2382–2393.
- 651 https://doi.org/10.1016/j.neuroimage.2010.10.009
- 652 Bialystok, E., & Codd, J. (2000). Representing quantity beyond whole numbers: Some, none,
- and part. *Canadian Journal of Experimental Psychology*, *54*(2), 117–128.
- 654 https://doi.org/10.1037/h0087334
- Borghesani, V., de Hevia, M. D., Viarouge, A., Pinheiro-Chagas, P., Eger, E., & Piazza, M.
- 656 (2019). Processing number and length in the parietal cortex: Sharing resources, not a
 657 common code. *Cortex*, *114*, 17–27. https://doi.org/10.1016/j.cortex.2018.07.017
- Brysbaert, M. (1995). Arabic Number Reading: On the Nature of the Numerical Scale and the
- 659 Origin of Phonological Recoding. *Journal of Experimental Psychology: General*, 124(4),
- 660 434–452. https://doi.org/10.1037/0096-3445.124.4.434
- 661 Butterworth, B. (1999). *The mathematical brain* (1. publ). Macmillan.
- 662 Cohen Kadosh, R., Cohen Kadosh, K., Kaas, A., Henik, A., & Goebel, R. (2007). Notation-
- Dependent and -Independent Representations of Numbers in the Parietal Lobes. *Neuron*,
 53(2), 307–314. https://doi.org/10.1016/j.neuron.2006.12.025
- Cohen Kadosh, R., & Walsh, V. (2009). Numerical representation in the parietal lobes: Abstract
 or not abstract? *Behavioral and Brain Sciences*, *32*(3–4), 313–328.
- 667 https://doi.org/10.1017/S0140525X09990938
- 668 Coldren, J. T., & Haaf, R. A. (2000). Asymmetries in infants' attention to the presence or
- absence of features. *Journal of Genetic Psychology*, *161*(4), 420–434.
- 670 https://doi.org/10.1080/00221320009596722

- 671 Damarla, S. R., Cherkassky, V. L., & Just, M. A. (2016). Modality-independent representations
- of small quantities based on brain activation patterns. *Human Brain Mapping*, *37*(4),
- 673 1296–1307. https://doi.org/10.1002/hbm.23102
- 674 Dehaene, S., & Cohen, L. (2007). Cultural Recycling of Cortical Maps. *Neuron*, 56(2), 384–398.
- 675 https://doi.org/10.1016/j.neuron.2007.10.004
- 676 Dehaene, S., Dehaene-Lambertz, G., & Cohen, L. (1998). Abstract representations of numbers in
- the animal and human brain. *Trends in Neurosciences*, 21(8), 355–361.
- 678 https://doi.org/10.1016/S0166-2236(98)01263-6
- 679 Eger, E., Michel, V., Thirion, B., Amadon, A., Dehaene, S., & Kleinschmidt, A. (2009).
- 680 Deciphering Cortical Number Coding from Human Brain Activity Patterns. *Current*

681 *Biology*, *19*(19), 1608–1615. https://doi.org/10.1016/j.cub.2009.08.047

- Eger, E., Sterzer, P., Russ, M. O., Giraud, A.-L., & Kleinschmidt, A. (2003). A supramodal
- number representation in human intraparietal cortex. *Neuron*, *37*(4), 719–725.
- 684 https://doi.org/10.1016/s0896-6273(03)00036-9
- Goh, R. Z., Phillips, I. B., & Firestone, C. (2023). The perception of silence. *Proceedings of the*
- 686 *National Academy of Sciences*, *120*(29), e2301463120.
- 687 https://doi.org/10.1073/pnas.2301463120
- Harvey, B. M., & Dumoulin, S. O. (2017). A network of topographic numerosity maps in human
 association cortex. *Nature Human Behaviour*, 1(2). https://doi.org/10.1038/s41562-0160036
- 0000
- Harvey, B. M., Klein, B. P., Petridou, N., & Dumoulin, S. O. (2013). Topographic
- 692 Representation of Numerosity in the Human Parietal Cortex. *Science*, *341*(6150), 1123–
- 693 1126. https://doi.org/10.1126/science.1240405

- Haufe, S., Meinecke, F., Görgen, K., Dähne, S., Haynes, J. D., Blankertz, B., & Bießmann, F.
- 695 (2014). On the interpretation of weight vectors of linear models in multivariate
- 696 neuroimaging. *NeuroImage*, 87, 96–110.
- 697 https://doi.org/10.1016/j.neuroimage.2013.10.067
- 698 Ifrah, G. (1985). From one to zero: A universal history of numbers. (*No Title*).
- 699 Kaplan, R. (1999). The Nothing that Is: A Natural History of Zero. Oxford University Press.
- 700 King, J.-R., & Dehaene, S. (2014). Characterizing the dynamics of mental representations: The
- temporal generalization method. *Trends in Cognitive Sciences*, 18(4), 203–210.
- 702 https://doi.org/10.1016/J.TICS.2014.01.002
- 703 Kirschhock, M. E., Ditz, H. M., & Nieder, A. (2021). Behavioral and Neuronal Representation of

Numerosity Zero in the Crow. *The Journal of Neuroscience*, *41*(22), 4889–4896.

- 705 https://doi.org/10.1523/jneurosci.0090-21.2021
- 706 Krajcsi, A., Kojouharova, P., & Lengyel, G. (2021). Development of Preschoolers'
- 707 Understanding of Zero. *Frontiers in Psychology*, 0, 3169.
- 708 https://doi.org/10.3389/FPSYG.2021.583734
- 709 Kriegeskorte, N., & Diedrichsen, J. (2019). Peeling the Onion of Brain Representations. Annual
- 710 *Review of Neuroscience*, *42*(1), 407–432. https://doi.org/10.1146/annurev-neuro-080317-
- 711 061906
- 712 Kriegeskorte, N., & Kievit, R. A. (2013). Representational geometry: Integrating cognition,
- computation, and the brain. *Trends in Cognitive Sciences*, 17(8), 401–412.
- 714 https://doi.org/10.1016/J.TICS.2013.06.007

- 715 Kutter, E. F., Bostroem, J., Elger, C. E., Mormann, F., & Nieder, A. (2018). Single Neurons in
- the Human Brain Encode Numbers. *Neuron*, *100*(3), 753-761.e4.
- 717 https://doi.org/10.1016/j.neuron.2018.08.036
- 718 Kutter, E. F., Dehnen, G., Borger, V., Surges, R., Mormann, F., & Nieder, A. (2023). Distinct
- neuronal representation of small and large numbers in the human medial temporal lobe.

720 *Nature Human Behaviour*, 1–10. https://doi.org/10.1038/s41562-023-01709-3

- 721 Libertus, M. E., Woldorff, M. G., & Brannon, E. M. (2007). Electrophysiological evidence for
- notation independence in numerical processing. *Behavioral and Brain Functions*, *3*.
- 723 https://doi.org/10.1186/1744-9081-3-1
- Luyckx, F., Nili, H., Spitzer, B., & Summerfield, C. (2019). Neural structure mapping in human
 probabilistic reward learning. *eLife*, 8. https://doi.org/10.7554/eLife.42816
- 726 Maris, E., & Oostenveld, R. (2007). Nonparametric statistical testing of EEG- and MEG-data.

Journal of Neuroscience Methods, *164*(1), 177–190.

- 728 https://doi.org/10.1016/j.jneumeth.2007.03.024
- 729 Mazor, M., Friston, K. J., & Fleming, S. M. (2020). Distinct neural contributions to
- 730 metacognition for detecting, but not discriminating visual stimuli. *eLife*, *9*, e53900.
- 731 https://doi.org/10.7554/eLife.53900
- 732 Mazor, M., Moran, R., & Fleming, S. M. (2021). Metacognitive asymmetries in visual
- perception. *Neuroscience of Consciousness*, 2021(1), 1–15.
- 734 https://doi.org/10.1093/nc/niab025
- 735 Merritt, D. J., & Brannon, E. M. (2013). Nothing to it: Precursors to a zero concept in
- preschoolers. *Behavioural Processes*, 93, 91–97.
- 737 https://doi.org/10.1016/j.beproc.2012.11.001

- 738 Merten, K., & Nieder, A. (2012). Active encoding of decisions about stimulus absence in primate
- 739 prefrontal cortex neurons. *Proceedings of the National Academy of Sciences of the United*
- 740 States of America, 109(16), 6289–6294. https://doi.org/10.1073/pnas.1121084109
- 741 Nieder, A. (2016). Representing Something Out of Nothing: The Dawning of Zero. *Trends in*
- 742 *Cognitive Sciences*, 20(11), 830–842. https://doi.org/10.1016/j.tics.2016.08.008
- 743 Nieder, A., & Dehaene, S. (2009). Representation of number in the brain. Annual Review of
- 744 *Neuroscience*, *32*, 185–208. https://doi.org/10.1146/annurev.neuro.051508.135550
- 745 Nili, H., Wingfield, C., Walther, A., Su, L., Marslen-Wilson, W., & Kriegeskorte, N. (2014). A
- Toolbox for Representational Similarity Analysis. *PLoS Computational Biology*, *10*(4).
- 747 https://doi.org/10.1371/journal.pcbi.1003553
- Okuyama, S., Kuki, T., & Mushiake, H. (2015). Representation of the Numerosity 'zero' in the
 Parietal Cortex of the Monkey. *Scientific Reports*, 5(1), Article 1.
- 750 https://doi.org/10.1038/srep10059
- 751 Oostenveld, R., Fries, P., Maris, E., & Schoffelen, J. M. (2011). FieldTrip: Open source software
- for advanced analysis of MEG, EEG, and invasive electrophysiological data.
- 753 *Computational Intelligence and Neuroscience*, 2011.
- 754 https://doi.org/10.1155/2011/156869
- 755 Piazza, M., Izard, V., Pinel, P., Le Bihan, D., & Dehaene, S. (2004). Tuning curves for
- approximate numerosity in the human intraparietal sulcus. *Neuron*, 44(3), 547–555.
- 757 https://doi.org/10.1016/j.neuron.2004.10.014
- 758 Piazza, M., Pinel, P., Le Bihan, D., & Dehaene, S. (2007). A Magnitude Code Common to
- 759 Numerosities and Number Symbols in Human Intraparietal Cortex. *Neuron*, 53(2), 293–
- 760 305. https://doi.org/10.1016/j.neuron.2006.11.022

761	Ramirez-Cardenas, A.	, Moskaleva,	M., &	Nieder, A.	(2016)). Neuronal F	Representation of	эf
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- 762 Numerosity Zero in the Primate Parieto-Frontal Number Network Article Neuronal
- 763 Representation of Numerosity Zero in the Primate Parieto-Frontal Number Network.
- 764 *Current Biology*, 26, 1285–1294. https://doi.org/10.1016/j.cub.2016.03.052
- 765 Sainsbury, R. (1971). The "feature positive effect" and simultaneous discrimination learning.
- *Journal of Experimental Child Psychology*, *11*(3), 347–356.
- 767 https://doi.org/10.1016/0022-0965(71)90039-7
- 768 Sassenhagen, J., & Draschkow, D. (2019). Cluster-based permutation tests of MEG/EEG data do
- not establish significance of effect latency or location. *Psychophysiology*, *56*(6), 1–8.
- 770 https://doi.org/10.1111/psyp.13335
- 771 Schubert, T. M., Rothlein, D., Brothers, T., Coderre, E. L., Ledoux, K., Gordon, B., &
- 772 McCloskey, M. (2020). Lack of awareness despite complex visual processing: Evidence
- from event-related potentials in a case of selective metamorphopsia. *Proceedings of the*
- 774 *National Academy of Sciences*, *117*(27), 16055–16064.
- 775 https://doi.org/10.1073/pnas.2000424117
- 776 Teichmann, L., Grootswagers, T., Carlson, T., & Rich, A. N. (2018). Decoding Digits and Dice
- with Magnetoencephalography: Evidence for a Shared Representation of Magnitude.
- Journal of Cognitive Neuroscience, 30(7), 999–1010.
- 779 https://doi.org/10.1162/jocn_a_01257
- 780 Treder, M. S. (2020). MVPA-Light: A Classification and Regression Toolbox for Multi-
- 781 Dimensional Data. *Frontiers in Neuroscience*, *0*, 289.
- 782 https://doi.org/10.3389/FNINS.2020.00289

- 783 Van Veen, B. D., van Drongelen, W., Yuchtman, M., & Suzuki, A. (1997). Localization of brain
- 784 electrical activity via linearly constrained minimum variance spatial filtering. *IEEE*
- 785 *Transactions on Bio-Medical Engineering*, 44(9), 867–880.
- 786 https://doi.org/10.1109/10.623056
- 787 Wellman, H. M., & Miller, K. F. (1986). Thinking about nothing: Development of concepts of
- 788 zero. British Journal of Developmental Psychology, 4(1), 31–42.
- 789 https://doi.org/10.1111/j.2044-835X.1986.tb00995.x

790

791 Supplemental Figures



Supplemental Figure 1. Cross-stimulus set representations of numerosity in non-symbolic stimuli. A representational dissimilarity matrix (RDM) was constructed that modelled the distance effect between non-symbolic numerosities across stimulus sets (top). This model tests whether numerical information is shared across the standard and control set, independently of their unique physical features. Numerical distance effects could be extracted from the neural data independently of the stimulus set soon after stimulus presentation and for the remainder of the epoch (bottom). Horizontal line represents time points where the correlation of the model RDM

- 811 with the neural data was significantly above zero with an alpha of p < .05, corrected for multiple
- 812 comparisons.



826 Supplemental Figure 2. Cross-Task RSA reveals a format-invariant neural code for number. An 827 RDM modelling numerical information as shared between numerical format successfully 828 predicted our neural data at two different timepoints. Removing the diagonal from this RDM 829 removes the shared exemplars from the model (empty sets and zero, one dot and symbolic one, 830 etc.) providing a strong test of the hypothesis that abstract numerical information also exhibits a 831 distance effect. This model showed a similar pattern of prediction to the full model with shared 832 exemplars yet failed to reach statistical significance. Broad confidence intervals, represented by 833 the shaded area, suggest this may be an issue of limited statistical power. Horizontal lines

- 834 indicate clusters where the model RDM correlated with the neural data significantly more than
- 835 zero, p < .05, corrected for multiple comparisons. Shaded areas represent 95% confidence
- 836 intervals.

837



848

Supplemental Figure 3. *Multidimensional scaling of numbers across format*. Performing
multidimensional scaling on numerosity representations in a shared space revealed alignment
along an axis defining numerical magnitude (dimension two). This illustrates the cross-task
distance effect, where empty sets (blue zero) are represented more closely to symbolic one (red
one) than symbolic five (red five), and vice versa. Dimension one discriminates between the two
tasks.