Is facultative sex is the best of both worlds in the parasitoid wasp *Lysiphlebus fabarum?*

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Abstract

The prevalence of sexual reproduction has long puzzled evolutionary biologists. This is because asexual reproduction is a far more efficient way to transmit copies of one's own genome to the next generation, and, all-else-being-equal, should predominate over sex. Asexual reproduction is not without its disadvantages though, the lack of genetic recombination can render parthenogenetic lineages vulnerable to extinction under environmental change, or compromise fitness due to the buildup of deleterious recessive mutations. Facultative sex, where individuals retain the ability to reproduce sexually and asexually, has been touted as 'the best of both worlds', providing the long-term genetic benefits of sex without the short-term costs. In this study I tested whether sex is facultative in the aphid parasitoid *Lysiphlebus fabarum,* and if so whether facultative sex is 'the best of both worlds'. I found that females from asexual populations mate with males produced by females from an obligately sexual population, and produced offspring with paternal genetic contributions, confirming facultative sex in this species. I then assayed the fitness of these facultatively sexual wasps and found, contrary to predictions that they actually had significantly lower fitness than asexual or obligately sexual females, as their daughters were up to 40% more likely to fail to reproduce entirely. In contrast, obligately sexual females were not at a disadvantage compared to asexual females in this species; they had increased fecundity compared to asexual females which compensated for the costs of sex. In *L. fabarum* it seems that all is not equal; the fecundity advantage that obligate sex provides, along with the costs of occasional facultative sex by asexuals may balance the scales and allow stable coexistence of the different reproductive modes in nature.

1. Introduction

Understanding how sex became the dominant reproductive strategy in eukaryotes has long been a major theme in evolutionary biology [1–3]. The initial interest in this question arose from the observation that asexual reproduction should, in theory, predominate because it is a far more efficient way to transmit copies of one's own genome to the next generation. An asexually reproducing individual is expected to have double the genetic representation of itself in the next generation compared to an equivalent sexual individual. This became known as the 'twofold cost of sex' [1]; early explanations considered 'genome dilution' to be the cause of this cost, whereby a sexually reproducing female 'dilutes' her genetic contribution to the next generation, halving her fitness compared to an asexual female. It is now accepted that 'genome dilution' is not the source of the 'twofold' cost of sex (as only genes for reproduction matter in this context, see [4] for an in-depth explanation), instead the

49 twofold cost arises because sexual individuals must 'waste' resources on producing males,
50 which do not efficiently convert resources to offspring [4]. When the sex ratio is 50:50,
51 sexuals produce half as many daughters as asexuals, so the twofold cost of sex is
52 sometimes known as the 'twofold cost of males' [1–4].
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Given this cost, how then did sex become more prevalent than asexual reproduction in
eukaryotes after it evolved over two billion years ago? And more recently, given that asexual
reproduction readily re-evolves in eukaryotes [2] why does sex still dominate? Historically,
two broad models which encompass different types of benefits have been proposed to
answer these questions. The first group are the mutational models, which emphasize the
importance of sex in exposing mutations to selection, so that deleterious mutations can be
purged, and beneficial mutations can be fixed more effectively [3,5–8]. The second group
are ecological models, which emphasize the benefits of sex for adaptive potential; by
creating new gene combinations sex facilitates adaptation under environmental change [9].
Mutational and ecological benefits of sex are not mutually exclusive however and can
interact in complex and context-dependent ways, which may explain why phylogenetic
patterns point to reproductive mode being more evolutionarily labile than expected in the
eukaryotes [2–4,10,11].
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The picture becomes more complex in light of mounting evidence that many species thought
only to reproduce through obligate sex or asexual reproduction are actually sexually plastic
[10]. Many species reproduce asexually only some of the time, either as an obligate part of
their lifecycle (as in cyclical parthenogens like many aphids and *Daphnia*; [11]), facultatively
when a suitable mate can't be found [12], or sometimes spontaneously (so-called
Tychoparthenogenesis [2,13]. Facultative sex has been touted as the 'best of both worlds' as
it can, in theory, provide both the short-term demographic benefits of asexual reproduction
and the long-term genetic benefits of sex [11]. Integrating sexual plasticity in all its forms into
theoretical and phylogenetic models which aim to reconstruct the evolution of reproductive
mode is the obvious next step in answering the longstanding question 'why sex?', but this
requires more data, not only about the occurrence of facultative sex (which is often cryptic),
but also its costs and benefits relative to obligate strategies [4].
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The sexual-asexual aphid parasitoid wasp *Lysiphlebus fabarum* offers an ideal system to
explore whether facultative sex really does represent 'the best of both worlds'. We already
have a comprehensive understanding of the molecular basis and population genetics of
reproductive mode in *L. fabarum* [14–16]. Asexual reproduction seems to have initially arisen
0.5 million years ago from ancestral obligate sex in *L. fabarum,* and it is determined by the
inheritance of a single recessive allele which results in parthenogenesis by central-fusion
automixis (the haploid products of meiosis I fuse to form diploid gametes which develop
without fertilisation; [16,17]). Whilst this form of parthenogenesis does maintain
heterozygosity to some extent, because recombination still occurs, asexual lineages can
only become more homozygous, eventually resulting in inbreeding depression and
associated reductions in fitness [2]. However, population genetic studies show that
parthenogenetic populations of *L. fabarum* have high levels of heterozygosity and allelic
variation even compared to sexuals [14,15]. This genetic diversity has been proposed to
exist due to occasional bouts of rare sex by normally asexual females, as well as
'contagious' parthenogenesis, where rare males produced by asexual females cross with
sexual females, creating new asexual lineages [14,15]. Regardless of the mechanism, this

genetic variation is thought to underlie the success of asexual reproduction in this species, resulting in parthenogenetic populations dominating across Europe [14,15]. Obligately sexual populations are less commonly encountered in the field, but sex does persist in *L. fabarum*, and even occurs in sympatry with asexuality in some regions [17, 18].

This study aims to test whether facultative sex occurs in *L. fabarum* and if it does, whether it represents the 'best of both worlds', providing the short-term benefits of asexual reproduction and long-term genetic benefits associated with sex [12]. To do this I gave female *L. fabarum* from 7 asexual lines and one outbred sexual population aphid hosts to parasitise after (i) being exposed to males (from the sexual population) or (ii) being kept in isolation (due to haplodiploidy sexual females can produce unfertilised eggs that develop as male offspring). I found that asexual females copulated when they were exposed to males and so in a follow-up experiment, I genotyped their G1 offspring to test whether mating reflects a behavioural vestige of sexual reproduction without fertilisation or whether these females can still reproduce sexually. I also assayed the reproductive success of daughters produced by asexual females which either mated or remained virgin. This allowed me to test whether putative facultative sex allows females to reap the short-term demographic benefits of asexual reproduction (not producing males) and also gain the long-term genetic benefits of sex (which only appear in hybrid offspring).

2. Methods

(a) Study system

In the aphid parasitoid *Lysiphlebus fabarum* both sexual and asexual populations exist, separately as well as in sympatry in some regions [14,15]. Asexual reproduction is inherited via a single recessive allele which appeared approximately 0.5 million years ago [14]. Inheritance of two copies of the asexual allele results in parthenogenetic asexual reproduction through central-fusion automixis, where the products of meiosis 1 fuse and recombine, restoring diploidy without integrating paternal DNA [16]. A panel of microsatellite markers has been developed to study the population genetics of *L. fabarum,* one of which, *Lysi07*, shows perfect linkage to the recessive genetic factor associated with asexual reproduction [18].

(b) Lab rearing

This study used females from 7 asexual lines and males and females from an outbred obligately sexual population of the aphid parasitoid *Lysiphlebus fabarum*. These lines were provided by Prof Christoph Vorburger (EAWAG, Zürich, Switzerland) who has been maintaining them since they were collected between 2006 and 2017 (see [16] for details). The wasps have been cultured at the University of Stirling under equivalent conditions since March 2023 and are regularly genotyped to check their genetic identity has been maintained. The wasps are given black bean aphid (*Aphis fabae*) colonies to parasitise; they are able to parasitise all instars of aphid but prefer 1st instar nymphs [19]. Female wasps lay a single egg inside each aphid (they are solitary endoparasitoids) and the host continues to grow as the wasp larva develops (they are koinobionts; [19]). In the lab aphids are maintained on broad bean seedlings (*Vicia faba*). All insects are kept in climate-controlled chambers at

144 20°C, 70% RH on a 16:8 hour light:dark cycle. Under these conditions the generation time of
145 *L. fabarum* is 12-14 days.
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147 (c) Experimental design
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To measure the benefits and costs of sex in *L. fabarum* I assayed offspring production by
obligately sexual and asexual *L. fabarum* females (referred to as G0) which were exposed to
a male (from the obligately sexual population), M, or remained virgin, V (fig 1a). All females
(including asexuals) in the M treatment readily copulated with the male, so I refer to these
females as 'mated'. To test for longer-term costs of mating (and potentially facultative sex) I
repeated the same fitness assays with the unmated daughters of V and M asexual females
(fig 1c; V_2 and M_2; referred to as G1 females). The fitness measures I used were: (i) the
number of aphid mummies (parasitised dead aphids) produced and (ii) the number of
mummies from which adult wasps successfully emerged (fig 1b and 1d). Emerging wasps
(1b and 1d) were also sexed in order to test whether asexual females avoid the 'twofold' cost
of male production regardless of their mated status. To test whether asexual females that
mated reproduced by facultative sex (i.e. used sperm to fertilise their eggs) I genotyped full
broods of emerged wasps (fig 1b and 1d) to test for the presence of sexual alleles their
offspring.
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To assess the 'twofold' cost of sex (male production) and determine whether it applies to
facultative (mated asexual) and obligately sexual females I looked at the number of sons and
daughters produced by V, M and V_2 and M_2 females. To estimate this cost of sex in the case
of obligate sex I compared son and daughter production between G0 obligately sexual
mated M females and all (V and M) G0 asexual females (fig 1, grey boxes). To test whether
the cost of male production also applies to facultatively sexual females (asexual M females) I
compared son and daughter production of (i) G0 asexual V and M females (fig 1, dashed
outlined boxes) and (ii) G1 asexual V_2 and M_2 females (fig 1 grey ovals). I predicted that the
'twofold' cost of sex (producing males) would only be paid by obligately sexual females
(sexual M); who would produce ~50% male offspring and as a consequence would produce
around half as many daughters as asexual females (asexual M and V). I predicted male
production would be negligible for all asexual females, including those which mated with a
sexual male (M) or whose mother had mated (M_2). Below (in section e) I outline the
statistical models applied to make these comparisons.
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Figure 1 Schematic of the experimental design showing (a) the 2 treatments (virgin, V;
mated, M) that sexual and asexual females were subjected to initially (G0). On day 0 mated
females were paired with a male (produced by a virgin sexual female) and observed until
copulation was recorded. Virgin females were kept in isolation. All wasps were then given
aphid nymphs on a broad bean leaf disc to parasitise for 3 days after which the parasitised
aphids were moved onto a broad bean seedling in a cellophane bag. After 14 days
parasitised aphid mummies and live emerged wasps were collected (G1), (b) sexed and
counted, and preserved in ethanol (c) for DNA extraction. I retained 1 live G1 asexual female
per replicate from (b) to test for effects of mothers mated status on reproductive success
(virgin mothers, V_2 or mated mothers, M_2). I took two live G1 daughters from each mated G0
sexual mother (d), one was isolated as a mummy before emergence and remained virgin
(V_2) and one was allowed to mate naturally in the cellulose bag (M_2). These G1 females
were given aphids to parasitise on the day they emerged, which, as with G0, were moved
onto a broad bean seedling after 3 days. When the next generation (G2) wasps emerged (d)
they, and all mummies, were counted and sexed. Boxes around focal wasps (in a and c)
indicate treatments which were compared to each other to estimate the costs of male
production for obligate sexuals compared to asexuals (grey rectangles) and facultative sex
versus asex (grey ovals).

(d) Experimental set up

Generation -1: standardised rearing

I set up a 'G-1' generation to standardise rearing conditions for females to be used in
experiments; recently emerged females were removed from stock for all lines (7 asexual and
1 sexual) and 20 females per line were transferred onto broad bean seedlings infested with
A. fabae in cellulose bags (Celloclair, Liestal, Switzerland). To generate enough males for
the mating treatments 20 virgin sexual *Lysiphlebus* females were allowed to parasitise an
aphid colony. Virgin sexual females lay only unfertilised eggs that develop as haploid males.
To ensure virginity parasitised aphid 'mummies' were removed from infested plants in the
sexual stock cage before the wasps emerged and were isolated in cellulose pill capsules.
When the wasps emerged, 20 females were transferred onto broad bean seedlings infested
with *A. fabae* in a cellulose bag. This process was repeated for each asexual line and the
sexual population to generate focal females, but emerged females were removed from stock,
and not isolated as mummies. This process was repeated with freshly emerged wasps every
day for 3 days to stagger the emergence of focal wasps to increase the sample size by
conducting the experiment across 3 blocks.
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219 *Generation 0: mating treatments*
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Ten to 12 days after aphids were exposed to the G-1 wasps I checked the seedlings for the
presence of parasitised aphid 'mummies' and isolated any that I found into cellulose pill
capsules. These were labelled with the line ID, whether the mother was mated or virgin (for
sexuals) and the date the mummy was isolated. Mummies were checked regularly for
emergence. On the peak emergence days (day 13) I selected focal females and males and
assigned them to mating treatments. I set up between 3 and 11 females per treatment for
each asexual line and 18 and 22 sexual females for the virgin and mated treatments
respectively resulting in a total sample size of N = 126.
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Asexual female wasps from 7 lines and sexual females were assigned to either mated (M) or
virgin (V) treatments. For the M treatments a male produced by a sexual virgin female was
introduced into the pill capsule with the female, the pair was observed continuously for 30
minutes or until copulation occurred. In *Lysiphlebus fabarum* it is possible to determine
successful mating visually, the female becomes quiescent and lowers her antenna and the
male is able to insert his aedeagus into her vagina. Females often reject male mating
attempts in this species by curling their abdomen under and moving rapidly. For all M
females I recorded whether males attempted copulation and if so whether females rejected
or accepted the mating attempt. For M females that accepted copulation, the male was
removed from the pill capsule and the female was retained (I did not assay the fitness of M
females which did not copulate in this experiment). For the V treatments no male was added
to the females pill capsule, to control for potential mechanical costs of mating, V females
were gently moved around in their pill capsule using a paintbrush.
243
On each day that wasps were put into M and V treatments (over 3 days) once all females
had been subjected to their mating treatment, they were transferred onto broad bean leaves
cut into discs and embedded in 6mL 1% agarose gel in an insect rearing dish with a mesh
ventilation hole (diameter, 15mm depth; SPL Life Sciences, Pocheon-si, South Korea). Leaf
discs had been infested with 5 adult aphids 5 days previously. On the day of the experiments
the adult aphids were removed from the leaf disc and the nymphs that they produced were
counted and numbers recorded. Wasps on leaf discs were checked every day between 9:00-
10:00, 12:00-13:00 and 17:00-18:00 for 3 days after they were set up and any dead females

were recovered, and their time and date of death recorded. After 3 days the leaf disc was
removed from the agar and transferred onto a 2-week-old broad bean seedling in a
cellophane bag. If the female wasp was still alive, she was transferred onto the seedling
along with the aphids.
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Twelve days after the aphids had been exposed to the wasps, I cut the stem of the seedling
and closed the bag (still containing the seedling) with a bulldog clip. Cutting the plant
resulted in any unparasitized aphids dropping off the plant before wasps started to emerge.
The bags were checked each morning from day 12 to day 16 and any emerging wasps were
collected. I collected one female from each replicate (with the exception of sexual virgin
females, which do not produce daughters) to start generation G1 (see below). The rest of the
G1 brood were collected into 99% ethanol for genotyping. Bags containing mummies were
retained and the mummies counted after all wasps had emerged.
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266 *Generation 1: daughters of mated and virgin females*
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To test whether mothers mated status influences the fitness of asexuals, I assayed the
fitness of the daughters produced by G0 asexual females in the M and V treatments and G0
sexual females in the M treatment (sexual V females produced only sons). Generation G1
asexual females which had emerged into cellulose bags were collected and subjected to the
same protocol as G0 females, but G1 focal females all remained virgin; they were the
daughters of asexual females that had either mated (labelled M_2) or remained virgin (labelled
V_2). I took two G1 daughters from each mated sexual G0 female, one was isolated before
emergence and so remained virgin (V_2), and the other was allowed to emerge and mate
naturally in the cellulose bag (M_2: see figure 1). Females were placed onto leaf discs for 3
days, which were then moved onto seedlings. The number of aphid nymphs and wasp
survival on leaf discs was also recorded for these G1 females. I counted the number of
mummies and emerged wasps produced by these G1 females. For each combination of line
by treatment set up between 3 and 11 focal females, resulting in a total sample size of N =
80 G1 females.
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283 (d) Assaying sperm use by asexual females
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To test whether asexual females used sperm from sexual males after they mated I
genotyped 41 whole broods of offspring (8 broods from asexual virgin females, 29 broods
from mated asexual females, and 4 broods from sexual females) using a single microsatellite
marker (*Lysi07*; Sandrock et al 2007) which exhibits complete linkage with the asexuality-
inducing allele (Sandrock and Vorburger 2011). DNA was extracted in a pooled reaction (up
to 10 wasps from one brood per reaction) using the Qiagen DNAeasy blood & tissue kit
(QIAGEN Inc, Hilden, Germany). After extraction DNA was amplified in a multiplex PCR
reaction using fluorescently labelled *Lysi07* primers. PCR reactions were carried out using a
Qiagen Multiplex PCR kit (QIAGEN Inc. Hilden, Germany) in 11 µl reactions and contained:
1 µL DNA template, 10 µL PCR mastermix (made up 1x QIAGEN Multiplex PCR mix and
0.1µM of each locus-specific labelled (forward) and unlabelled (reverse) primer). PCR
conditions were as follows: initial denaturation at 95°C for 15 min, followed by 30 cycles of
94°C for 30 s, 58°C for 90 s, 72°C for 60 s, and final extension at 60°C for 30 min. PCR
amplification was performed using a DNA Engine Tetrad ® Thermal Cycler (MJ Research,
Bio-Rad, Hemel Hempstead, Herts, UK). PCR products were then sent to MRC PPU DNA

sequencing and services at the University of Dundee for fragment analysis. This involves capillary electrophoresis which provides a series of different coloured peaks which vary in location on an X-axis based on the size of the microsatellite fragment. I scored these peaks using the software Geneious™. For *Lysi07,* peaks scored at 184 are found exclusively in asexual wasps and 192 in sexual wasps. When a sample had scores at both 184 and 192 it indicated the presence of both sexual and asexual alleles suggesting that an asexual wasp had mated and used sperm.

(e) Statistical analysis
Parasitism failure, mummy production and wasp emergence

To test whether mated status (and reproductive mode) were related to reproductive success I ran 3 sets of generalised linear mixed models (GLMMs) with the following response variables: (i) parasitism failure (binomial, scored as 1 if no mummies were recovered; using the glmer function in the lme4 package in R; [20]), (ii) number of mummies (negative binomial, count of the number of mummies recovered from each replicate; using *glmmTMB* in R;[21]), (iii) proportion of mummies that emerged as adult wasps (binomial, modelled using the cbind function in R and using *glmmTMB*).

The G0 models included reproductive mode (sexual or asexual), mated status (virgin or mated) and their interaction effect as fixed factors. Covariates were also fitted; these were the number of aphid nymphs on the leaf disc and female wasp survival (in hours; up to a maximum of 72 hours for all wasps which survived until transfer to seedling). I also included a random effect of Line ID nested within reproductive mode. Block was not included in any model; treatments were replicated evenly across daily blocks and in no case did I find a significant effect of block on any outcome variable, nor did inclusion of block in any models influence the results. Broods that were recorded from two G0 virgin sexual females were removed from the analyses as female offspring were recovered (virgin sexual females only produce unfertilized eggs which develop as males) suggesting mislabeling.

The G1 models were similar but the data was only from asexual females, so no fixed effect of reproductive mode was fitted. The only fixed effects were mother's mated status, (mated or virgin), survival of the focal female and number of nymphs (as covariates), and Line ID was included as a random effect. The package *DHARMa* [22] was used to check that all models were appropriately specified.

Daughter production and the cost of males

To compare the traditional 'twofold' cost of sex (male production), I tested whether obligately sexual females produced fewer daughters than all asexual females (grey boxes in fig. 1). To do this I ran a model using data from G0 females, with the number of female offspring produced as the outcome variable (negative binomial in *glmmTMB*). Data from virgin sexual females were not used for this model (as virgin sexual females produce only male offspring) but data from M sexual and asexual and V asexual G0 females was included. This G0 model included a fixed effect of reproductive mode. The number of male offspring produced was also included as a covariate, and as an interaction with reproductive mode, to test for a trade-off between son and daughter production.

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I ran two additional models to test whether facultative sex (by normally asexual females)
imposes a cost due to male production. These models had the same structure but included
data either from only G0 or only G1 asexual females and included fixed effect of mated
status (or mother's mated status) and the number of male offspring produced (as a
covariate), as well as their interaction effect. The G0 model tested whether asexual females
that mated produced fewer daughters than females which remained virgin (grey boxes with
dashed outlines in fig.1). The G1 model tested whether females with mated mothers
produced the same number of daughters as females with virgin mothers (grey ovals in fig.
1). As with the other models mothers' survival and number of nymphs were included as
covariates and random effects were Line ID nested within reproductive mode or and Line ID
only (if only data from asexual females was used).
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359 *Estimating overall fitness*
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To test whether sex, either obligate or facultative, or asexual reproduction is associated with
higher reproductive success overall I used the data from G0 and G1 females (including
those which failed to parasitise any aphids or produce any offspring) to estimate a
standardised measure of overall fitness (W) for every experimental female in both
generations, calculated as $PP \ x \ SP \ x \ N$ where PP is the proportion of aphid nymphs
recovered as mummies (proportion parasitised; note that if the number of mummies was
higher than the number of nymphs provided, due to continued aphid reproduction after
counting, this was set as 1), SP is the proportion of mummies that produced an adult female
offspring, (successful parasitism) and N is the total number of offspring produced. While this
method does have its shortfalls, in particular it neglects the complexities of fitness returns
through males, it does provide a useful standardised way to test for differences in overall
fitness according to reproductive mode. To test whether obligately sexual, facultatively
sexual or asexual females have the highest fitness I ran a zero-inflated Gamma GLMM with
fixed effects of 'reproductive mode' and 'generation', plus their interaction effect with 'W' as
the dependent variable. Reproductive mode was included as a fixed factor with 3 levels in
the model, obligately sexual (M and M_2 sexual females; V sexual females which only
produce males were not included), facultatively sexual (M and M_2 asexual females) and
asexual (V and V_2 asexual females). Generation was a fixed factor with 2 levels which
indicated the mother's generation (G0 and G1).
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381 **3. Results**
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383 (a) Summary
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In the first generation (G0) 103 females were offered a male to mate with (M) and 66 were
not (they remained virgin, V). Of the 103 females assigned to the M treatment, 70 mated.
Thirty-three M females did not mate either because males failed to initiate courtship (N =
10), or the female did not signal receptivity (N = 23). The 70 M and 66 V female wasps were
given aphids to parasitise. Table 1 shows the numbers of females which remained virgin (V),
mated (M), or did not mate (due to rejection or no attempt) by line.
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Table 1. Number of first generation G0 females that remained virgin (V), accepted a mating
(M: successful matings), did not accept a mating because the male did not attempt

courtship, or because the female rejected the male. Also shown are the proportion of male-
female introductions that resulted in a successful mating by line. A significantly lower
proportion of pairings involving asexual females resulted in successful mating (X^2=10.430, df
= 1, p = 0.0012: asexual = 0.6, sexuals = 0.96).
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Line	N	Remained virgin	Attempted matings	Successful matings	No attempt	Rejected	proportion attempts successful
CHC17-66	10	5	5	5	0	0	1.00
CV17-84	10	4	6	5	0	1	0.83
IL06-658	8	3	5	5	0	0	1.00
IL07-64	36	11	25	10	4	11	0.40
IL09-348	24	10	14	8	1	5	0.57
IL09-402	30	10	20	10	4	6	0.50
IL09-554	10	5	5	5	0	0	1.00
Sexual	41	18	23	22	1	0	0.96

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Of the 136 G0 females that were given aphids to parasitise 58 died before they were
transferred onto the seedlings and 70 survived. In the second generation (G1), I took the
daughters of 40 M and 40 V G0 asexual mothers and put them on leaf discs. Of the 80 G1
females put onto leaf discs 57 survived and 23 died before being transferred to seedlings 72
hours later (note that there was no effect of mating treatment on wasp survival in the first 72
hours in either the G0 or G1 generations: G0 (effects of reproductive mode and mated
status): Log-rank X^2= 1.4, df = 3, p = 0.70 and G1 (mated status only): Log-rank X^2 = 2.8, df
= 1, p = 0.33).
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410   (b) Sperm use
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Forty-one broods were genotyped in total (see table S1 for a summary of brood genotypes
broken down by treatment and line). All broods produced by sexual females were
homozygous for the sexual allele (peak 192) at *Lysi07*. Broods produced by asexual females
were significantly more likely to test positive for sexual alleles if the female had mated (M)
than if she was virgin (V) (X^2 =4.56, df = 1, p = 0.03); 9/30 broods produced by mated M
asexual females were homozygous for the asexual allele (peak 184), 19/30 were
heterozygous for sexual and asexual alleles (184/192) and the 2 were homozygous for the
sexual allele (192; most likely due to a PCR failure/scoring error or misnumbering of a
replicate as there is no evidence for introgression of sexual alleles in the stock lines these
females were derived from). Only 1 brood produced by a virgin (V) asexual female was
scored as positive (heterozygous) for the sexual allele (suggesting either mislabelling or
contamination between samples); the other 7 V asexual broods were homozygous for the
asexual allele.
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(c) Parasitism success
In some cases, no mummies were recovered from aphids that were exposed to *L. fabarum*
females, suggesting that these females either failed to oviposit, or their eggs failed to
hatch/larvae to develop resulting in complete reproductive failure. In G0 100 out of 126
females successfully parasitised aphids and produced adult offspring. A few individuals
successfully produced a small number of mummies but no adult offspring (12), these

females were excluded from the analyses below as I did not dissect the uneclosed mummies
to determine whether the larvae died before emergence or had entered diapause. In the first
generation G0, sexual females were more likely to fail to parasitise aphids than asexual
females (χ^2 = 4.49, df = 1, 124, p = 0.03). Mating had no effect on G0 females ability to
parasitise and this was true for both sexual and asexual females (χ^2 = 1.54, df = 1,124, p =
0.21. Interaction effect between reproductive mode and mated status: χ^2 = 0.42, df = 1, 124,
p = 0.52; fig. 2a).

54/80 G1 daughters of asexual G0 females successfully parasitised aphids and produced
adult offspring, 6 females successfully produced a small number of mummies but no adult
offspring (again, females which produced mummies but not adult offspring were removed
from the analysis below). In G1 there was a large negative effect of mothers mated status on
parasitism success. The G1 daughters of mated M G0 asexual females were 25% more
likely to fail to parasitise aphids than the daughters of virgin V females (χ^2 = 7.43, df = 1,79,
p = 0.0.006; fig. 2b).

Figure 2. Bar plot showing the effect of mated status on % parasitism success in **(a)** G0
across 7 asexual lines and one outbred sexual line of *L. fabarum*. In G0 sexual females were
more likely to fail to parasitise than asexuals but there was no effect of mated status and **(b)**
G1 asexual daughters of G0 females; daughters of mated M females were significantly more
likely to fail to parasitise than daughters of virgin V females.

(d) Mummy production and emergence

Although sexual females in G0 were more likely to fail to parasitise any aphids, when I
considered only the females that did parasitise, sexual females were at an advantage as
they produced more mummies (χ^2 = 5.04, df = 1, 98, p = 0.03; fig. 3a) more of which
produced a wasp (χ^2 = 4.41, df = 1, 98, p = 0.03; fig. 3c) than their asexual conspecifics.
Whilst sex had an effect on mummy production in G0 there was no effect of mating; virgin V
and mated M females produced the same numbers of mummies (χ^2 = 0.30, df = 1, 98, p =
0.59) regardless of whether they were sexual or asexual (interaction: χ^2 = 0.29, df = 1, 98, p
= 0.59; fig. 3a). There was an effect of mating on adult offspring production though; virgin V
G0 mothers were more successful (χ^2 = 3.85, df = 1, 98, p = 0.05; fig. 3c) for sexual and
asexual mothers (interaction: χ^2 = 0.78, df = 1, 98, p = 0.38).

These results were not replicated in the second generation, there was no effect of G0
mother's mated status on the number of mummies their G1 daughters produced ($X^2 = 2.41$,
df = 1, 52, p = 0.121; fig. 3b) or the proportion of these mummies from which a wasp

G0: 1st generation   G1: 2nd generation

emerged ($X^2 = 0.21$, *df = 1, 52, p = 0.65*; fig. 3d).

Figure 3 Number of mummies produced (**a & b**) and % mummies adult wasps emerged
from (**c & d**) in G0 (**a & c**) and G1 (**b & d**). G0 sexual females produced more mummies than
asexual females (**a**) which were more likely to emerge as adult wasps (**c**). Mummies
produced by virgin G1 mothers (sexual and asexual) were also more likely to emerge as
adult wasps (**c**). For asexual G1 females there was no effect of mothers mated status on
mummy production (**b**) or the proportion of mummies that successfully emerged (**d**). Black
points are means and error bars represent standard errors estimated by nonparametric
bootstrapping.

Daughter production and the cost of producing males

To test whether the classic 'twofold' cost of sex applies in *L. fabarum* I looked at daughter
production by focal females. In G0, obligately sexual females did not produce fewer
daughters than asexual females (M or V; $X^2 = 0.02$, *df = 1, 98, p = 0.90).* Contrary to
expectations females that produced more males did not produce fewer daughters (number of
sons: $X^2 = 0.68$, *df = 1, 98, p = 0.40),* a pattern that was the same for sexual and asexual

females (reproductive mode*number male offspring: $ = 3.23, df = 1, 98, p = 0.07$). I ran a
second model with sexual females removed to test whether facultative sex by G0 mated
asexual females imposes a cost in terms of male production, but again M and V females
produced the same number of daughters ($ = 0.49, df = 1, 71, p = 0.48$). Son production
was very low for M and V asexual females in G0 (< 5 per mother) and there was no
evidence that females which produced more males produced fewer daughters (mated status:
$ = 0.49, df = 1, 71, p = 0.48$; male production; $ = 3.22, df = 1, 71, p = 0.07$; mated
status*number male offspring $ = 0.36, df = 1, 71, p = 0.55$).

I found the same pattern in the second generation (G1); male production was again very low
for all asexual females and had no effect on daughter production ($ = 1.88, df = 1, 52, p =$
0.17) regardless of mothers mated status (mothers mated status*number male offspring:
$ = 0.65, df = 1, 52, p = 0.42$). Importantly the G1 daughters of mated M G0 females (some of
which are facultatively sexual) produced the same number of daughters as females
produced asexually by virgin V G0 mothers ($ = 2.24, df = 1, 52, p = 0.14$). Taken together
these results from G0 and G1 suggest that 'all-else-is-not-equal' in this system, so the
twofold cost of male production does not constrain the fitness of (obligately or facultatively)
sexual females compared to asexuals in *L. fabarum*.

Estimating overall fitness through granddaughters
501
Fitness estimates were significantly lower for facultatively sexual females compared to
obligately sexual females in G0 (z = 1.25, p = 0.04) and G1 (z = 2.37, p <0.001). Asexual
and facultatively sexual females had equivalent fitness in G0 (z = 0.47, p = 0.42), the
difference in fitness increased in G1, with asexual females having higher fitness, but this was
not statistically different (z = 0.1.21, p = 0.059). Asexual and obligately sexual females did
not differ significantly in overall fitness in G0 (z = 0.78, p = 0.27) or G1 (z = 1.17, p = 0.11;
overall effect of reproductive mode: $ = 16.23, df = 2, 90, p = 0.0003$; fig. 4).

Figure 4 Fitness estimates for asexual (asexual V), facultatively sexual (asexual M) and
obligately sexual (sexual M) G0 females. Fitness estimates were calculated by multiplying
the proportion of aphid nymphs parasitized (PP), the proportion of mummies yielding adult
wasps (SP), and the number of adult wasps (N). Black points represent means and error
bars are standard errors estimated by nonparametric bootstrapping.

4. Discussion

Populations of the aphid parasitoid *Lysiphlebus fabarum* vary in their reproductive mode:
asexual (parthenogenetic) reproduction dominates across Europe, but sexual populations
persist in sympatry with asexuals in some regions [14,15]. In this study I show for the first
time that asexual *L. fabarum* females are sexually functional and can use sperm to fertilise
eggs and produce daughters. I found that between 40-100% (x = 60%) offemales from all 7
asexual *L. fabarum* lines assayed were facultatively sexual; they mated with sexual males
and produced offspring with genetic contributions from both parents. However, asexual
females that reproduced sexually did not get the best of both worlds, in terms of short-term
benefits of parthenogenesis (higher daughter production) or genetic benefits of sex
(increased fecundity or offspring emergence). In fact, the pattern was quite the opposite,
facultatively sexual females suffered high costs of reproductive failure associated with sex
and lower fecundity associated with asexual reproduction; they get the worst of both worlds.
528
The main short-term benefit of asexual reproduction is that it eliminates the 'twofold cost of
males'. In *L. fabarum,* asexuals do occasionally produce male offspring, Sandrock and
Vorburger [16] found that around 1 in every 3000 asexual wasps is male in the lab. In the
current study I also found low rates of male production by *all* asexual females, but crucially
asexual females did not produce more daughters than sexual females rendering this cost
negligible. This is because the assumption that 'all-else-is-equal' does not hold; obligately
sexual females had higher fecundity than females from asexual lines, such that despite
producing many more sons they produced the same number of daughters as asexuals,
suggesting a long-term genetic benefit of sex. Females from asexual lines which engaged in
facultative sex did not gain this benefit of sex though, the fecundity of asexual females was
not influenced by their mated status or their mother's mated status. There was, however, a
significant fitness cost to sex, it increased the risk of reproductive failure by 12% compared
to parthenogenesis. This cost was even higher for asexual females that mated and
reproduced sexually; when asexual G0 females mated and could reproduce sexually, 40% of
their G1 daughters failed to reproduce compared to only 10% of the G1 daughters of asexual
G0 females that did not mate. When all measures of reproductive success were combined to
estimate a standardised measure of fitness asexual and obligately sexual females did not
differ, which may explain why sexual and asexual populations exist in nature. Facultatively
sexual females on the other hand had lower fitness, presumably due to the combined effects
of high reproductive failure associated with sex, and lower fecundity associated with
parthenogenesis (asex).
550
Asexual reproduction is thought to have first evolved approximately 0.5 million years ago in
L. fabarum, arising through the inheritance of a single recessive allele which results in the
haploid products of meiosis I fusing to form diploid gametes which develop without
fertilisation (central-fusion automixis; [17]). Although asexuality may have arisen 0.5 million
years ago it is unlikely that the asexual lineages I tested have existed for so long without sex

and recombination (see [17]). The asexual lines used in this experiment have, however been
reared in the lab for 7-18 years without sex. Despite the lack of sex (potentially for up to 400
generations) some females from all seven asexual *L. fabarum* populations exhibited sexual
behaviour and were able to integrate paternal DNA into the female offspring they produced.
The maintenance of sexual traits in *L. fabarum* makes them unique compared to many other
asexual eukaryotes, where sexual traits such as mate location, attraction, allowing
copulation and storing sperm decay rapidly due to high costs of maintenance [23-26].
563
It is unclear is why sexual traits have persisted in asexual *L. fabarum*as I found that
facultative sex is costly for reproductive success in this species; 40% of the daughters of
mated asexual females failed to reproduce entirely, which should result in strong selection
on asexual females that do not invest in sexual signalling or accept matings. There are
multiple possible reasons that sex, in particular facultative sex, might increase the risk of
reproductive failure. One explanation for is that some of the daughters of some daughters of
G0 M asexual females are triploid with low fertility. Triploid females may represent the
proportion of the females in G1 that failed to produce any offspring. Whilst I was unable to
detect triploids using multiplex PCRs here (as broods were pooled) Sandrock et al [15] found
that around 2% of females in all-female broods were triploid in asexual *L. fabarum* in the
field, supporting this possibility. However, triploidy is not a given under central-fusion
automixis as eggs are laid when they are in metaphase I, but diploidy is not restored until
anaphase II [17]. Another non-mutually exclusive possibility is that 'genetic slippage' occurs,
resulting in lower fitness of sexually produced offspring. Genetic slippage, essentially
outbreeding depression, occurs when combinations of genes that normally work well
together are broken up by sex, creating new genotypes which have low fitness [3–8,12]. Sex
and recombination can produce novel multilocus genotypes that perform better than the
parental genotypes in some environments, but genetic slippage can mean that they perform
much worse [12]. In this study it may be that the new genotypes created by sex were costly
for *L. fabarum,* and this cost may have been more severe under facultative sex because of
the greater genetic differentiation between asexual females and sexual males. Follow up
studies which replicate this experiment, but genotype individual mothers and offspring are
needed to shed light on the extent to which triploidy leads to reproductive failure. Similarly,
repeating this study but using rare males that are produced by asexual females will allow for
more explicit tests of the genetic slippage hypothesis, as facultative sex with more closely
related mates should in theory be less costly.
590
The mating systems and population dynamics characteristic of aphid parasitoids like
Lysiphlebus might explain why facultative sex has persisted in *L. fabarum* despite the costs.
Parasitoid abundance increases over the season as hosts become more numerous, until
populations crash later in the summer [27]. At the end of the season the abundance of *L.*
fabarum females in parasitised aphid colonies can become very high which could have a
number of effects on the rate of facultative sex and its consequences. First, high population
densities are expected to increase the likelihood that normally asexual females will
encounter and mate with rare asexual males (or sexual males in regions of sympatry).
Second, mating between kin is common in parasitoids because many females parasitise
aphids in the same colony that they emerged from (they are quasigregarious), which may
counter the detrimental effects of genetic slippage (i.e. they are less likely to produce low
fitness recombinants with closely related mating partners: [28]). Genetic slippage is
essentially a form of severe outbreeding depression [29], and so its costs may be reduced

under inbreeding. Third, the main cost of sex (increased reproductive failure), may be
relaxed at certain times in the season. For instance, during the 'mid-season crash' aphid
populations become locally extinct over just a few days, in part due to high natural enemy
pressure [30]. At such times the cost of sex may be less significant if the costs of host-finding
and host competition constrain parasitoid fitness to a greater extent.
609
In addition to relaxed costs, facultative sex could also be an important 'bet-hedging' strategy
for *L. fabarum* late in the season if it reduces the variation in fitness across environments
compared to parthenogenesis. Bet-hedging has been proposed to maintain traits that are
costly for individual fitness, like sex (and polyandry [31,32]) ensuring the genes underlying
these traits persist even if the traits themselves can be costly to the bearers. Williams [33]
used the analogy of reproduction as a lottery to explain sex as bet-hedging: in this analogy
asexual reproduction is like buying many lottery tickets with the same number, if you win,
you win big. Reproducing sexually, you don't buy so many tickets, but they have different
numbers, increasing the chances you win, but reducing the amount you win. Sex and
recombination result in more genetically diverse offspring, which differ from each other and
their parents. By producing sexual offspring with more diverse genotypes, some of them will
have low fitness in the same conditions as their parents. The genotypes that perform poorly
in the parental environment may be better adapted to different conditions, they may thrive
when the environment changes [8,33]. Asexual reproduction on the other hand tends to
result in offspring that are genetically very similar, if not identical, to their parents, and so do
very well in the same conditions their parents experienced, but if the environment changes,
they are more likely to fail to reproduce entirely. Under bet-hedging, sex is a risk-averse
strategy associated with moderate fitness under a range of environments, while asexual
reproduction could provide big benefits under a stable environment but is risky if conditions
change. The scenario that aphid parasitoids like *L. fabarum* face at the end of the season
may increase the importance of facultative sex as a bet-hedging strategy because some
offspring will need to survive overwinter as diapause pre-pupae and reproduce the following
spring, in drastically different environmental conditions from their parents.
633
When viewed in the light of the natural history of aphid parasitoids like *L. fabarum* the results
of this study suggest that relatively frequent sex, potentially between closely related males
and parthenogenetic females, may be responsible for maintaining high levels of genetic
variation and heterozygosity in asexual *L. fabarum*. If sex occurs mainly late in the season it
is also likely to be fairly synchronous, mirroring the reproductive phenology of their cyclically
parthenogenetic aphid hosts. When normally parthenogenetic individuals all reproduce
sexually at the same time in this way, Kokko [11] has shown that facultative sex is more
stable and robust to the invasion of obligate asexual reproduction. Synchronous seasonal
sex between siblings may explain not only the how heterozygosity and allelic diversity is
maintained in asexual *L. fabarum* [14,15] but also why sex and its associated traits have
persisted. Studies that measure the frequency of sex in the field, and its associated costs will
reveal the full extent of facultative parthenogenesis and its evolutionary significance in *L.*
fabarum, so that we can establish whether facultative sex has in this case made asexual
reproduction more successful.
648
649 **Data, script and code availability**
650

651 All data, code and supplementary information can be accessed here:
652 https://osf.io/qb7yz/?view_only=bbb5677d9ce14c6dab3ac42b94345c17
653

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659 **Conflict of interest disclosure**
660
661 The author declares that they have no conflict of interest relating to the content of this article.
662

663 **References**
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