multimedia: Multimodal Mediation Analysis of Microbiome Data

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ABSTRACT

Mediation analysis has emerged as a versatile tool for answering mechanistic questions in microbiome research because it provides a statistical framework for attributing treatment effects to alternative causal pathways. Using a series of linked regression models, this analysis quantifies how complementary data modalities relate to one another and respond to treatments. Despite these advances, the rigid modeling assumptions of existing software often results in users viewing mediation analysis as a black box, not something that can be inspected, critiqued, and refined. We designed the multimedia R package to make advanced mediation analysis techniques accessible to a wide audience,

ensuring that all statistical components are easily interpretable and adaptable to specific problem contexts. The package provides a uniform interface to direct and indirect effect estimation, synthetic null hypothesis testing, and bootstrap confidence interval construction. We illustrate the package through two case studies. The first re-analyzes a study of the microbiome and metabolome of Inflammatory Bowel Disease patients, uncovering potential mechanistic interactions between the microbiome and disease-associated metabolites, not found in the original study. The second analyzes new data about the influence of mindfulness practice on the microbiome. The mediation analysis identifies a direct effect between a randomized mindfulness intervention and microbiome composition, highlighting shifts in taxa previously associated with depression that cannot be explained by diet or sleep behaviors alone. A gallery of examples and further documentation can be found at https://go.wisc.edu/830110.

IMPORTANCE

Microbiome studies routinely gather complementary data to capture different aspects of a microbiome's response to a change, such as the introduction of a therapeutic. Mediation analysis clarifies the extent to which responses occur sequentially via mediators, thereby supporting causal, rather than purely descriptive, interpretation. multimedia is a modular R package with close ties to the wider microbiome software ecosystem that makes statistically rigorous, flexible mediation analysis easily accessible, setting the stage for precise and causally informed microbiome engineering.

INTRODUCTION

Treatments often cause change indirectly, triggering a chain of effects that eventually influences outcomes of interest. A standard approach to disentangling these pathways is to distinguish between indirect paths through candidate mediators and direct paths from treatment to outcome. Fig. 1A represents this graphically, with separate paths for treatment $T \rightarrow$ mediator $M \rightarrow$ outcome Y and treatment $T \rightarrow$ outcome Y. In the causal inference literature, this exercise is called mediation analysis, and various techniques have

49 emerged to support it [29, 8]. Several adaptations have been proposed for the microbiome
50 setting, where mediators, outcomes, and controls may be high-dimensional [38, 48, 5, 23].
51 These efforts have already uncovered clinically relevant relationships, like the existence of
52 microbial taxa that mediate the success of chemotherapy treatments [41].

FIG 1 A. The graphical model underlying mediation analysis. Using combined
mediation (purple) and outcome (blue) models, mediation analysis makes it
possible to distinguish between direct and indirect causal pathways between
treatments and outcomes. The conventional mediation analysis typically
requires all nodes except for the covariates X to be univariate, whereas our
package operates without such constraints. B. The overall multimedia workflow.
Multimedia defines a modular interface to mediation analysis with utilities for
summarizing and evaluating uncertainty in estimated effects.

Despite these successes, existing methodology places strong requirements on the
distribution of the mediators or outcome variables and the functional form of their
relationships. For example, [38, 56, 48, 55] assume that mediators are compositional and
that outcomes are univariate, focusing on how microbiome relative abundance profiles
mediate treatment effects on downstream host phenotypes, like the relationship between
fat intake and body mass index [38]. This precludes analysis where outcomes are
multidimensional, like metabolic profiles, or where mediators are clinical measurements.
Further, with the exception of the mediation package [44], existing implementations are

not modular, fixing the estimator used in both the mediation and outcome regressions.

This rigidity limits the range of settings in which mediation analysis can be applied.

Moreover, it discourages critical evaluation or interactive model building, since model

components are difficult (or impossible) to interchange. Unfortunately, even the adaptable

mediation package is limited to one-dimensional mediator and outcome variables.

To enable more flexible and transparent mediation analysis of microbiome data, we

extend the methodology of [24, 44] to high-dimensional mediator and outcome variables.

This makes it possible to include sparse regression, logistic-normal multinomial, random

forest, and hierarchical bayesian mediation and outcome models within a uniform

package interface. Moreover, we have documented the process of inserting custom

models into the overall workflow. These models can all be specified using R's formula

notation, and components can be easily interchanged according to context. We include

operations for summarization, alteration, and uncertainty quantification for the resulting

models, encouraging interactive and critical microbiome mediation analysis. We ensure

strong ties to the wider microbiome software ecosystem by including methods to convert

to and from phyloseq [30] and SummarizedExperiment [18, 26] data structures.

Altogether, the multimedia package unlocks the potential for mediation analysis for

microbiome studies with complex experimental designs, enabling model-based

integration of diverse data types, including microbial community composition,

high-throughput molecular profiles, and host health surveys.

RESULTS

Mediation analysis with our package is a three-step process. First, users specify the

hypothesized causal relationships between variables with a concise syntax that represents

diverse modeling choices (**Model Setup**). Next, they estimate the model parameters and

the associated causal effects (**Counterfactual Analysis**). Finally, they can compare

synthetic data from alternative models and calibrate inferences using either bootstrap

confidence intervals or hypothesis tests (**Evaluating Uncertainty**). This overall workflow

is illustrated in Fig. **1**B and detailed in the first three sections below. A summary of key

package functions is given in Table **1**. The last two sections demonstrate the package
workflow with case studies on metabolomic data integration and the gut-brain axis.

Stage	Function	Description
Model Setup	mediation_data	Convert phyloseq, SummarizedExperiment, or data.frame objects into S4 classes representing all components of a mediation analysis study.
	multimedia	Define the form of the mediation and outcome models for estimation and effect calculations.
Counterfactual Analysis	direct_effect	Given fitted models, estimate direct effects for each outcome using Equation 7.
	indirect_overall	Given fitted models, estimate aggregate indirect effects for each outcome using Equation 8.
	indirect_pathwise	Given fitted models, estimate indirect effects for each mediator-outcome pair using Equation 9.
Statistical Inference	bootstrap	Re-estimate models and effects on bootstrap resampled versions of the experiment.
	nullify	Define a version of an existing model with a subset of edges removed from either the mediation or outcome model.
	fdr_summary	Calibrate a false discovery rate controlling selection rule using synthetic null data and Equation 11.

TABLE 1 Core functions for problem specification, effect estimation, and uncertainty quantification available through the multimedia package.

Model Setup To estimate a mediation model, it is necessary to fully specify the nodes
and edges in Fig. **1**A. The nodes are used to divide data sources into categories according
to their role in the causal model. Edges correspond to mediation and outcome models.
Rather than requiring specification of all mediation analysis components at once in a
single function, multimedia allows users to define separate components and then glue
them together to define an overall analysis. The package exports a mediation_data data
structure for storing the samples used in model fitting. We use an R's S4 system [50] to
define separate slots for each node in Fig. **1**A. This data structure can be created by
applying the accompanying mediation_data function to accompanying R data.frame,

phyloseq, and SummarizedExperiment objects. We support tidyverse-style syntax [51],
meaning that many variables can be assigned to a node using concise queries. For
example, mediation = starts_with("diet") will search the input data for any features starting
with the string "diet" and will tag them as mediators in the downstream analysis. This
efficient matching simplifies data manipulation in high-dimensional settings, where the
user may need to work with hundreds of mediators or outcomes.

Next, we must specify the mediation and outcome models. The package exports
wrappers to several regression families, ensuring that, despite their differing underlying
methodology, all families can be used interchangeably for estimation, sampling, and
prediction in the overall mediation analysis workflow. Specifically, multimedia includes
(1) linear regression, which ensures that the package generalizes the earlier mediation
package, (2) ℓ^1 and ℓ^2-regularized linear regression [17, 43], which can be more stable and
interpretable in the presence of numerous predictors, (3) random forests [53], which
supports detection of nonlinear relationships between variables, and (4) hierarchical
Bayesian regression [3], which can be useful for sharing information across related groups.

Counterfactual Analysis After using the estimate function to fit models to the
observed data, we can reason about potential outcomes under different treatment regimes.
This allows us to clarify the relative importance of direct and indirect pathways. For
example, to estimate a direct effect $(T \rightarrow Y)$, we can block effects that travel along the
indirect path $(T \rightarrow M \rightarrow Y)$ and measuring the changes to the response that persist.
Formally, in the counterfactual language of the Materials and Methods, direct and indirect
effects are estimated using predicted mediators $\hat{M}(t_i)$ and outcomes $\hat{Y}(t_i', \hat{M}(t_i))$, where
t_i and t_i' correspond to mediator and outcome-specific treatment assignments. To this end,
multimedia defines a data structure for storing (t_i, t_i') within two data.frames whose rows
are samples and columns are treatment settings. The predict and sample methods allow
users to compute expected values and draw samples according to arbitrary treatment
profiles (t_i, t_i'). Note that, in addition to the standard treatment vs. control setup,
multimedia supports treatment profiles with multiple concurrent treatments and
multilevel or continuous treatment.

Given a fitted model, multimedia outputs estimated direct and indirect effects. We
formally define these effects in Equations 8 - 10. Here, we offer an overview of their
motivation and interpretation. Direct effects are the changes we would observe in the
outcome if we changed the treatment node in Fig. 1A but held all the mediators fixed.
This is the effect that travels along the edge $T \rightarrow Y$, and it measures the extent to which
the treatment can influence the outcome while bypassing the mediators. We estimate
different direct effects for each outcome. For example, in the mindfulness case study
below, direct effects can be interpreted as microbiome shifts (changes in Y) following the
mindfulness training (treatment T) that are not a consequence of changes in participant
sleep or diet behaviors (mediators M). Next, we support estimation of two types of
indirect effects. Overall indirect effects measure the changes in the outcome when setting
all mediators to their predicted values when the treatment is present, keeping the
contribution of the direct path $T \rightarrow Y$ fixed. This aggregates the effect across the full
collection of indirect paths. In contrast, pathwise indirect effects measure the changes in
outcome when comparing counterfactuals that are equal except at a single mediator. This
isolates the indirect effect along a single indirect path. In this case, an indirect effect is
reported for each outcome-mediator pair, rather than only for each outcome.

To increase modeling transparency, multimedia includes functions for interacting with
and altering fitted models. Direct and indirect effects can be visualized within context of
the original data. This can serve as a sanity check and guide further model refinements.
Outputs are created with ggplot2 [49], which allows users to customize plot appearance.
The case studies include outputs from these helper visualization functions. Further, given
a fitted model, we allow users to refit new versions with sets of edges removed. Fig. 2
illustrates the main idea with a toy dataset. In the second column, the mediator takes on a
larger value under the red treatment, while in the third, the mediators have identical
distributions under the two treatments. Similarly, in the fourth, the relationship between
the mediator and outcome no longer depends on treatment status. We can also alter the
overall model structure, like the switch to a linear outcome model in the last column. If
the model quality deteriorates significantly in a altered submodel, then those edges play a
critical role. This heuristic is formalized in the synthetic null hypothesis testing strategy

discussed below. Finally, we have built the package with extensibility in mind. If
functions can be written for estimation and prediction from a new model type, then it can
be passed in to multimedia as a custom mediation or outcome model.

FIG 2 Samples from altered versions of a mediation analysis model fitted to the
toy data at the far left. Each row describes a different outcome variable, and
colors represent different treatments. The first column gives the original data,
and the remaining columns give simulated data from alternative models
specified by the DAGs on the top and column titles.

Statistical Inference The multimedia package offers bootstrap [13, 14, 15] and
synthetic null hypothesis testing [27, 40, 39] approaches for quantifying uncertainty in
estimates of mediation effects. To bootstrap in the mediation analysis context, we refit the
mediation and outcome models to bootstrap resampled versions of the data and compute
summary statistics (e.g., direct effect estimates) on each bootstrap sample. The percentiles
of the resulting summary statistic distribution defines the bootstrap confidence interval.
Importantly, the bootstrap is model agnostic and can apply to any instantiation of the
counterfactual mediation analysis framework. The primary assumption made by the
bootstrap is that its test statistics vary smoothly to small perturbations of the data. For this
reason, it is worthwhile to check that the histogram associated with the full bootstrap
distribution is well-behaved before computing confidence intervals. Like the boot
function in base R, multimedia's bootstrap uses a functional implementation – any
function that transforms an experiment and fitted model into a summary statistic can be

used as input. For example, it can accept a list of direct and indirect effect estimators, and
these will be computed on bootstrap resample.

An alternative approach to inference in high-dimensions is based on synthetic null
hypothesis testing. In this approach, rather than resampling the original data, the modeler
simulates synthetic data from an assumed null distribution. Effect estimates are computed
using both the original and the synthetic null data, and the fraction of synthetic null
"negative controls" among the strongest observed effects can be used to calibrate a
selection rule with false discovery rate control. The alteration functions above can be used
to define synthetic nulls; e.g., after zeroing out the edges from either $T \rightarrow M$ or $M \rightarrow Y$,
any estimated indirect effects can be treated as negative controls. Two advantages of the
synthetic null approach are that (1) it only requires the mediation and outcome models be
estimated twice and (2) multiple hypothesis testing is accounted for via the false
discovery rate. The key disadvantage of this approach, relative to the bootstrap, is that it
requires a realistic synthetic null data generating mechanism. For example, if the synthetic
null data are generated from a linear model, but real effects are nonlinear, then the
resulting selection sets will not provide valid false discovery rate control.

Microbiome-Metabolome Integration We next illustrate the multimedia workflow
with case studies. Our first concerns Inflammatory Bowel Disease (IBD), which is closely
tied to gut microbiome community composition [31]. [16] investigated the relationship
between the gut microbiome and metabolome between IBD patients and healthy controls,
concluding that microbial community members may be partly responsible for the
formation of metabolites that lead to inflammation and IBD. By applying clustering and
canonical correlation analysis to untargeted mass spectrometry data, they flagged a
number of disease-relevant metabolites. We re-analyze the data using model-based
mediation analysis, viewing IBD status – Healthy Control, Ulcerative Colitis (UC),
Crohn's Disease (CD) – as treatments T, metabolic profile as the outcome Y, and
microbiome community composition as a mediator M. The data are downloaded from the
microbiome-metabolome curated data repository [32]. We have further filtered to the top
173 and 155 most abundant microbes and metabolites, and we apply centered log-ratio

(CLR) and $\log{(1 + x)}$ to each source, respectively. Further details about the experimental

cohort and data preparation are available in the Materials and Methods.

We use parallel linear and ℓ^1-regularized regression for mediation and outcome

models, respectively. Note that treatment is the only predictor in the mediation model,

which is why no regularization is required. We ran the bootstrap for 1000 iterations, and

95% confidence intervals and bootstrap distributions for the features with the strongest

direct and overall indirect effects contrasting CD with healthy controls are shown in Fig. 3.

Metabolites with strong indirect effects are influenced by IBD-induced changes in

microbiome community composition, while those with large direct effects change due to

other unknown factors. Fig. 4 contextualizes a small subset of these overall effects by

overlaying metabolite abundances onto multidimensional scaling (MDS) plots derived

from microbiome community profiles. Though metabolites with strong direct effects have

differential abundance across IBD and healthy groups, only metabolites with indirect

effects show variation that is also associated with microbiome composition.

FIG 3 95% Bootstrap confidence intervals for metabolites with the strongest estimated direct and overall indirect effects associated with CD. Effects are sorted according to magnitude, and only the top 15 of each type are shown. Within the interval, the inner rectangle captures 66% of the bootstrap samples. In this data, indirect effects are stronger than direct effects.

FIG 4 Microbiome composition and metabolite abundance for three metabolites with the strongest direct (top row) and indirect (bottom row) effects. Samples (points) are arranged according to an MDS on CLR transformed microbiome profiles with Euclidean Distance. Axis titles give $\frac{\lambda_k}{\sum_{k'} \lambda_{k'}}$ from the associated eigenvalues. Each panel corresponds to a metabolite, and point size encodes metabolite abundance, normalized to panel-specific quantiles. Metabolites with strong indirect effects vary more systematically with microbiome composition – for example, samples with low abundance of lithocholate are localized to the right of the MDS plot.

Moreover, by analyzing pathwise indirect effects, we can uncover genus-level
relationships. A subset of the strongest pathwise indirect effects are shown in Fig. 5.
Among the microbe-metabolite pairs with the strongest pathwise indirect effects, we find
a relationship between metabolites of taurine and *Bilophila* (Fig. 5). High levels of fecal
taurine, one of the primary conjugates of primary bile acids [52], has been previously
associated with IBD [25, 46]. It has also been found that *Bilophila wadsworthia*, one of the
most prominent taurine metabolizers, is often associated with lower levels of taurine [46].
Here, our results suggest that higher levels of taurine in IBD patients is mediated in part,
by the abundance of *Bilophila*. We also find microbes in the genus *Firmicutes* bacterium
CAG:103, are paired with several metabolites: cholate, chenodeoxycholate, and
7-ketodeoycholate (Fig. 5). Cholate and chenodeoxycholate are primary bile acids

produced by the host, which are the metabolized by gut bacteria to form secondary bile
acids. 7α-dehydroxylation, is one of the pathways that bacteria metabolize primary bile
acids, an intermediate of which is 7-ketodeoycholate [36]. Recent work has found that
bacteria closely related to *Firmicutes* bacterium CAG:103 contain the majority of predicted
genes associated with the 7α-dehydroxylation pathway within metagenomic samples [45].
Our results suggest that the increasing abundance of *Firmicutes* bacterium CAG:103, may
be driving to the decrease in these primary bile acid metabolites and intermediates, which
is associated more with the non-IBD controls [42]. Host deficiency in creatine uptake has
been associated with poor mucosal health in IBD patients [10]. In our results we find that
there is a strong microbe-metabolite pair between microbes in the genus *Choladousia*
(family: *Lachnospiraceae*) and creatine/creatinine levels. *Lachnospiraceae*, (which is often at
lower levels in IBD patients), are known to produce short chain fatty acids, that have been
shown to help with mucosal health [33] (Fig. 5). Overall, these results suggest that
Choladousia may utilize creatine/creatinine as a nitrogen source, thus explaining its higher
abundance in the controls.

FIG 5 Microbe-metabolite pairs with the strongest pathwise indirect effects
from IBD status. Each panel corresponds to one pair, CLR-transformed genus
abundance is given on the *x*-axis, and $\log(1+x)$-transformed metabolite
abundance is given on the *y*-axis. Effects are sorted from most negative (top left)

to most positive (bottom right). For a pathwise indirect effect to be strong, there must be both a shift in microbe abundance due to IBD state ($T \rightarrow M$) and also an association between microbe and metabolite abundance ($M \rightarrow Y$).

Note that, since this mediation model is built from a regularized linear regression
outcome model, it is more sensitive to linear associations between microbe and metabolite
abundances. The official package documentation includes an alternative bayesian hurdle
outcome model, which exhibits higher sensitivity to outcomes with changes in metabolite
presence-absence probability. The easy interchangeability of mediation analysis
components makes this contrasting analysis simple to implement — it only requires
change in a single line of code — and reflects multimedia's modular design.

Evaluating a Mindfulness Intervention Studies of the gut-brain axis have yielded
experimental evidence for interactions between the gut microbiome and the brain. For
example, germ-free mice colonized with the microbiota from human patients with clinical
depression develop depression-like symptoms [28, 11], and observational studies have
linked particular bacterial taxa to depression [2, 35]. Given this growing body of evidence,
a team from the UW-Madison Center for Healthy Minds and the Wisconsin Institute for
Discovery profiled microbiome composition, surveyed psychological symptoms, and
tracked behavior change among 54 subjects before and after participation in a two-month
mindfulness training [7, 20] – see the Methods and Materials for details of the study
design and data processing. This study aimed to determine the nature of the
mindfulness-microbiome relationship and to identify potential causal pathways. Such
understanding could lead to novel interventions that influence mood through the
microbiome. As a first step, we use mediation analysis to understand the mechanisms
linking mindfulness and the microbiome in this randomized controlled trial. Our
intervention T is the mindfulness training program, the outcome of interest is microbiome
composition Y, and mediators M are survey responses related to diet and sleep that are
hypothesized to influence the microbiome. To control for subject-to-subject level variation,
participant ID is used as a pretreatment variable X.

For mediation and outcome models, we apply ridge and logistic-normal multinomial regressions, respectively [22, 54]. We choose a ridge regression model so that intercepts across the large number of participants are shrunk towards their global mean. We choose logistic-normal multinomial regression to jointly model microbiome composition. We also define altered submodels where all direct and indirect effects have been removed. Simulated genera compositions from all models are shown in Fig. 6. In the newly simulated data, subjects have been randomly re-assigned to the treatment and control groups. These submodels can support synthetic null hypothesis testing, since the synthetic null data appear to capture relevant properties of the real microbiome composition profiles, like the average relative abundances across genera and the range of observed abundances within most genera. Their main limitation is that some genera, like *Methanobrevibacter*, *Paraprevotella*, and *Akkermansia*, have much wider ranges than the synthetic data, and Fig. S1 suggests that this is due to a failure to capture the unusually high zero inflation present in these genera.

For synthetic null hypothesis testing, models without $T \rightarrow Y$ and $M \rightarrow Y$ associations are used to generate negative controls for direct and overall indirect effect estimates, respectively. Fig. 7 shows the estimated effects from real and synthetic data, together with the estimated false discovery rates. At a level $q = 0.15$, five genera are selected as having either significant direct or indirect effects. Fig. S2 provides the analog of Fig. 5 for this case study. Indirect effects are an order of magnitude weaker than direct effects, suggesting that changes in microbiome composition following the mindfulness intervention cannot simply be attributed to changes in diet or sleep alone.

We cannot externally validate these findings, since there is no consensus on the relationship between specific taxonomic groups and common psychiatric disorders (for a description of current sources of controversy, see [1]). However, our findings are broadly consistent with those from a recent large-scale human cohort, which found that most genera belonging to the families *Ruminococcaceae* were depleted in people with more symptoms of depression and that *Bifidobacterium* was an important predictor of depressive symptoms in a random forest classifier [2].

FIG 6 Real and synthetic null relative abundances across a subset of genera at different overall relative abundances. Color distinguishes whether the participant belonged to the treatment (mindfulness training) or control groups. The full model (left panel) captures the overall abundances and trajectories present in the real data, though it tends to underestimate the heaviness of the tails. The second and third panels show the analogous models with direct $(T \rightarrow Y)$ and indirect $(M \rightarrow Y)$ effects removed.

FIG 7 Estimated overall effects and false discovery rates derived from real and synthetic null data. Each point corresponds to one genus in either real (blue) or simulated (orange) data. The genera selected to control the false discovery rate at $q \leq 0.15$ are drawn larger than the rest. Direct effects are both larger in magnitude and easier to distinguish than their indirect counterparts.

DISCUSSION

Mediation analysis makes it possible to study causal pathways in multimodal
microbiome data, and it is an essential tool for discovery of subtle relationships that span
multiple host measurements and high-throughput assays. Statistical techniques in this
space are needed to support interrogation of varied causal relationships, not simply
studies where microbiome profiles serve as mediators and outcomes are one-dimensional,
as has been the historical focus of the field.

Our case studies illustrate the flexibility and analytical depth supported by
multimedia. Unlike traditional microbiome mediation analysis software, the package
allows specification of diverse regression components, and the interface simplifies
interpretation of effect types and model criticism. In this way, multimedia encourages
interactive, rigorous mediation analysis for microbiome data. It is written to interface
closely with the existing microbiome software ecosystem, and since analysis are carried
out in reproducible code notebooks, it supports scientific transparency.

We have created a gallery of example notebooks that use the multimedia package.

These include alternative analyses of the IBD and mindfulness data explored here. We

invite users to contribute further examples, and we plan to structure further

developments according to community needs.

MATERIALS AND METHODS

Counterfactual framework Consider random samples indexed by i. Let $T_i \in \mathbb{R}$ be the

experimental treatment of interest, $Y_i \in \mathbb{R}$ be the outcome, and $X_i \in \mathbb{R}^P$ be the

pretreatment covariates. For simplicity, we assume T_i is a binary indicator of either

treatment ($T_i = 1$) or control ($T_i = 0$), though multimedia supports categorical,

continuous, and multi-treatment cases.

To what extent is the effect of the treatment on the outcome modulated by

intermediate variables? Mediation analysis answers this question by positing mediators

M_i on the causal path from T_i to Y_i. Adopting a counterfactual perspective, we define

$M_i(t')$ as the potential outcome of the mediator under $T_i = t'$ and $Y_i(t, m)$ as the potential

outcome of the response under $T_i = t$ and $M_i = m$ with $t, t' \in \{0, 1\}$. Therefore, we can

express the outcome variable as $Y_i(t, M_i(t'))$. In a randomized experiment, we can only

ever observe the case where t and t' are the same, i.e., $Y_i(1, M_i(1))$ in the treated group

and $Y_i(0, M_i(0))$ in the control group – but conceptually t and t' can be different. For

example, $Y_i(0, M_i(1))$ represents the potential outcome when only mediators are

intervened upon and $Y_i(1, M_i(0))$ represents the potential outcome when we make

interventions while keeping mediators at their values under the control.

Analogous to the traditional average treatment effect, [24] defines the indirect effect to

be the treatment effect obtained through mediators,

$$\delta(t) = \mathbb{E}\{Y_i(t, M_i(1)) - Y_i(t, M_i(0))\} \tag{1}$$

and the direct effect to be the effect of treatment through other mechanisms,

$$\zeta(t') = \mathbb{E}\{Y_i(1, M_i(t')) - Y_i(0, M_i(t'))\} \tag{2}$$

for $t, t' \in \{0, 1\}$. It has been shown that both effects are identifiable under assumptions (3) to (6):

$$\{Y_i(t', m), M_i(t)\} \perp\!\!\!\perp T_i \mid X_i = x \tag{3}$$

$$Y_i(t', m) \perp\!\!\!\perp M_i(t) \mid T_i = t, X_i = x \tag{4}$$

$$\mathbb{P}(T_i = t \mid X_i = x) > 0 \tag{5}$$

$$p_{M_i(t)}(m \mid T_i = t, X_i = x) > 0 \tag{6}$$

341 for $t, t' \in \{0, 1\}$ and all $m \in \mathcal{M}$ and $x \in \mathcal{X}$, where $\mathcal{M}$ and $\mathcal{X}$ represent the supports of M_i
342 and X_i, respectively.

In addition, under a no interaction assumption, $\delta(t) = \delta(t')$ and $\zeta(t) = \zeta(t')$ for any $t \neq t'$. We define the overall indirect effect and direct effect as follows,

$$\bar{\delta} = \frac{1}{2} \sum_{t=0}^{1} \mathbb{E}\{Y_i(t, M_i(1)) - Y_i(t, M_i(0))\} \tag{7}$$

$$\bar{\zeta} = \frac{1}{2} \sum_{t'=0}^{1} \mathbb{E}\{Y_i(1, M_i(t')) - Y_i(0, M_i(t'))\} \tag{8}$$

Large magnitudes of $\bar{\delta}$ and $\bar{\zeta}$ suggest strong effects of the treatment on the outcome via mediators and mechanisms other than mediators, respectively. To define pathwise indirect effects, we apply different treatment assignments across coordinates of the mediators $M_i = (M_{i1}, \ldots, M_{iK})$,

$$\bar{\omega}_k = \frac{1}{2} \sum_{t'=0}^{1} \mathbb{E}\{Y_i(t', (M_{i1}(t'), \ldots, M_{ik}(1), \ldots, M_{iK}(t'))) - \tag{9}$$

$$Y_i(t', (M_{i1}(t'), \ldots, M_{ik}(0), \ldots, M_{iK}(t')))\}.$$

In practice, the population quantities $\bar{\delta}, \bar{\zeta}$, and $\bar{\omega}$ are unknown, and the expectations are replaced with fitted values from the mediation and outcome models $\hat{M}$ and $\hat{Y}$, respectively. For example, the direct effect is estimated using

$$\hat{\bar{\zeta}} = \frac{1}{2} \sum_{t'=0}^{1} \sum_{i=1}^{n} \hat{Y}_i(1, \hat{M}_i(t')) - \hat{Y}_i(0, \hat{M}_i(t')). \tag{10}$$

Bootstrap and synthetic null testing Form a bootstrap resample of the data

$\mathcal{D}^* = (\mathbf{X}^*, \mathbf{M}^*, \mathbf{T}^*, \mathbf{Y}^*)$ by independently resampling the n observations with replacement.

A summary statistic computed on the bth resampled dataset is denoted by $\hat{\theta}^{*b}(\mathcal{D}^*)$. For

brevity, we will omit the data arguments. For example, $\hat{\theta}^{*b}$ could correspond to an

estimator of $\bar{\delta}$ or $\bar{\zeta}$ derived from mediation and outcome models learned from $\mathcal{D}^*$.

Repeating this process B times, we refit $\hat{M}(t, x)$, $\hat{Y}(t, m, x)$ and the provided summary

statistic $\hat{\theta}$ for each of the B bootstrap the datasets. We can obtain the bootstrap distribution

$\left(\hat{\theta}^{*b}\right)_{b=1}^{B}$. Let $q_{\frac{\alpha}{2}}$ and $q_{1-\frac{\alpha}{2}}$ represent the $\frac{\alpha}{2}$ and $1 - \frac{\alpha}{2}$ quantiles of this collection. Then

$\left[q_{\frac{\alpha}{2}}, q_{1-\frac{\alpha}{2}}\right]$ forms an α-level bootstrap confidence interval associated with the statistic $\hat{\theta}$.

    For synthetic null hypothesis testing, estimate mediation and outcome models $\hat{M}_{\text{sub}}(t, x)$, $\hat{Y}_{\text{sub}}(t, m, x)$ using only a subset of edges within the DAG. This defines the null data generating mechanism. Using the same pretreatment and treatment profiles X_i, T_i from the original experiment, simulate synthetic null data $\mathbf{M}^{*0}, \mathbf{Y}^{*0}$ from the submodel. For D taxa of interest, compute summary statistics $\left(\hat{\theta}_d^1\right)_{d=1}^{D}$ and $\left(\hat{\theta}_d^0\right)_{d=1}^{D}$ based on the original and the synthetic null data, respectively. For example, $\hat{\theta}_d^1$ could estimate taxon d's direct effect $\hat{\bar{\delta}}_d$ using the original data, and $\hat{\theta}_d^0$ could be the corresponding estimate derived from synthetic null data. Next, for any threshold t, we estimate the false discovery rate using

$$\widehat{\text{FDR}}(t) := \frac{\#\left\{d : |\hat{\theta}_d^0| > t\right\}}{\#\left\{d : |\hat{\theta}_d^0| > t\right\} + \#\left\{d : |\hat{\theta}_d^1| > t\right\}}. \tag{11}$$

The numerator counts the number of estimates from the synthetic null data that are larger

than t, and the denominator counts the number of discoveries across either simulated or

real data at that threshold. Given a desired FDR level q, the selection rule is defined by

selecting $t^* = \min\left\{t : \widehat{\text{FDR}}(t) \leq q\right\}$ and selecting all features d such that $|\hat{\theta}_d^1| > t^*$. Under

the null samples generated by $\hat{M}_{\text{sub}}(t, x)$, $\hat{Y}_{\text{sub}}(t, m, x)$, this rule controls the false

discovery rate below level q, regardless of the choice of estimator $\hat{\theta}_d$, though better

estimators lead to improved power.

Microbiome-metabolome data processing We obtained the data from the

microbiome-metagenome curated database. Details of the library preparation and

bioinformatics can be found in [34]. Briefly, metagenomic sequencing was done on an
Illumina HiSeq 2500, and metabolites were profiled using LC-MS in non-targeted mode.
For metagenomics, fastp was applied to raw reads for quality filtering, adapter trimming,
and deduplication. bowtie2 was used to remove human reads by aligning to the hg38.
kraken2.1.1 and braken 2.8 were used to estimate taxonomic relative abundances.

A total of 11,720 taxa and 8,848 metabolites are present in the public data. We applied
a centered log-ratio transformation to the microbiome relative abundances profiles:
$\text{CLR}(x_1, \ldots, x_D) := \left(\log(x_d) - \frac{1}{D} \sum_{d'} \log x_{d'} \right)_{d=1}^{D}$. We then filtered to taxa whose average
transformed abundance was larger than 3, which reduced the number of taxa to 173. We
kept only metabolites with confident HMDB assignments, applied a $\log(1 + x)$
transformation, and further filtered to those whose average transformed intensity was
larger than 6. This resulted in 155 well-annotated and generally abundant metabolites.

Mindfulness study design and processing The initial Center for Healthy Minds study
recruited 114 police officers participants across two cohorts. Microbiome samples were
obtained only from participants in the second cohort ($n = 54$), who were randomly
assigned to mindfulness training or waitlist control with 27 cases each. We removed four
participants due to incomplete responses – three lacked microbiome data, and one had
missing mediators. Our analysis considers a mindfulness training treatment group of size
$n = 24$ and a waitlist control group of size $n = 26$. Participants in the mindfulness group
took part in an 8-week, 18-hour mindfulness training developed specifically for their
career and inspired by Mindfulness-Based Stress Reduction and Mindfulness-Based
Resilience Training [7]. Weekly two-hour classes (and a four-hour class in week 7)
consisted of didactic instruction, embodied mindfulness practices, and individual and
group-based inquiry (for full intervention details, see [21]). Microbiota and behavioral
survey data were gathered at 2 - 3 timepoints for each participant — samples in the
treatment group provided data before, within two weeks following, and, in a subset of
cases, four months after the 8-week intervention, resulting in 118 samples total.

Gut microbiome composition was assessed using 16S rRNA gene sequencing, and
participants completed surveys, as reported previously [21]. One to four technical

replicates (on average, 2.6) were sequenced for each 16S rRNA gene sample, resulting in 307 microbiome composition profiles in total. Amplicon Sequence Variants (ASV) were called using the DADA2 pipeline [4]. The first ten base pairs were removed, and all reads were truncated to a length of 250. Otherwise, we set all pipeline hyperparameters to their defaults. Since the total number of participants is relatively small, we chose to concentrate on the core microbiome [37]. To this end, we assigned taxonomic identity to each ASV using the RDP database and aggregated all counts to the genus level [9]. We removed any genera that did not appear in at least 40% of the samples, thereby generating a core microbiome. On average, this preserved 98.7% of the reads within each sample. After filtering to the core microbiome, sequences for 55 genera remained. To define mediators, we manually selected four variables from the National Cancer Institute Quick Food Scan and self-reported questionnaires on fatigue and sleep disturbance scores based on the Patient-Reported Outcomes Measurement Information System subscale [6]. We concentrated on these questions because changes in both diet and sleep have previously been associated with mindfulness interventions and the microbiome [19, 12, 47].

In detail, we consider four mediators – two diet mediators from the National Cancer Institute Quick Food Scan and two stress variables from the Patient-Reported Outcomes Measurement Information System (43-item inventory; version 2.0) following [6]. They are all calculated from questionnaires. The two diet variables indicate the frequency that participants eat cold cereal and fruit (not juices), respectively, in the past 12 months (Supplementary Table 1). The two stress variables, fatigue and sleep disturbance, profile the stress of a participant in the past 7 days (Supplementary Table 2).

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DATA AVAILABILITY STATEMENT

The multimedia package is available at https://go.wisc.edu/830110. Notebooks to reproduce the case studies are available at https://go.wisc.edu/787g25.

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CONFLICTS OF INTEREST

State all conflicts of interest here or say, "The authors declare no conflict of interest."

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