

# 1 **Does Sex-Differential Gene Expression Drive Sex-Differential** 2 **Selection in Humans?**

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10

## 11 **Abstract**

12 Sex differences in human transcriptomes have been argued to drive sex-differential natural  
13 selection (SDS). Here, we show that previous evidence supporting this hypothesis has been  
14 largely unfounded. We develop a new method to test for a genome-wide relationship between  
15 sex differences in expression and selection on expression-influencing alleles (eQTLs). We apply  
16 it across 39 human tissues and find no evidence for a general relationship. We offer possible  
17 explanations for the lack of evidence, including that it is due in part to eQTL ascertainment bias  
18 towards sites under weak selection. We conclude that the drivers of ongoing SDS in humans  
19 remain to be identified.

## 20 Introduction

21 Sex-differences in gene expression have been theorized to be the *result* of long-term sex-  
22 differential selection (SDS), where allelic fitness effects differ between males and females<sup>1,2</sup>.  
23 When a gene product is only beneficial in one sex, it is expected that expression modifiers will  
24 evolve to increase expression for that sex and decrease expression in the other<sup>3</sup>. The reverse  
25 causality has also been proposed: sex differences in gene expression might be the *driver* of SDS  
26 on expression modifiers<sup>1,4</sup>.

27 SDS acting on viability within the current generation can generate between-sex  
28 differences in allele frequency<sup>5,6</sup> at expression modifiers (expression Quantitative Trait Loci, or  
29 eQTLs)<sup>3</sup>. Sexually dimorphic traits (diseases being one example with strong repercussions on  
30 survival<sup>6,7,8,9</sup>) may be subject to SDS acting through viability. Previous work has proposed and  
31 tested theoretical models for relating divergence in eQTL allele frequencies with differential  
32 expression between sexes<sup>1,10,11</sup>. Some of the empirical results have, however, been called into  
33 question<sup>12,13,14</sup>.

34 A controversial result by Cheng and Kirkpatrick (2016)<sup>1</sup> (hereafter “CK16”) is a  
35 characteristic pattern relating between-sex  $F_{ST}$ <sup>1,5,15</sup> (henceforth “ $F_{ST}$ ”) to sex differences in gene  
36 expression (henceforth “ $\Delta$ ”). They observed high  $F_{ST}$  values at intermediate values of  $\Delta$  and  
37 near-zero values of  $F_{ST}$  when a gene is expressed evenly between the sexes ( $\Delta = 0$ ) or is only  
38 expressed in one sex ( $\Delta = \pm 1$ ). They nicknamed this bimodal pattern “Twin Peaks”. The Twin  
39 Peaks pattern has been used as a signal to detect SDS in several species<sup>1,4,16,17</sup>.

40 Here, we revisit the CK16 model and statistical approach. We find that their  
41 interpretation was based on previously unappreciated statistical artifacts. We then refine their  
42 model and apply it to new, more extensive data on gene expression and allele frequencies.  
43 Across 39 human tissues, we find no evidence for a genome-wide relationship between viability  
44 SDS and  $\Delta$ . We discuss how a bias in eQTL discovery towards eQTLs under weaker selection  
45 can explain the lack of signal for a relationship between SDS and  $\Delta$ , and how the drivers of SDS  
46 may still be investigated.

47

## 48 Results

### 49 Twin Peaks is a Statistical Artifact

50 We begin by revisiting the Twin Peaks pattern with a critical eye towards caveats in its  
51 application and interpretation. Most importantly, we reconsider the model that CK16 proposed to  
52 explain the pattern. It is based on two key assumptions. First, the relationship between a gene's  
53 expression levels and its effect on fitness in each sex is linear. Second, sexually antagonistic  
54 selection is symmetric, meaning selection coefficients are equal in magnitude and opposite in  
55 sign between sexes. This yields a quadratic relationship between  $F_{ST}$  and  $\Delta$  at a biallelic site  
56 affecting expression. At small absolute values of  $\Delta$ ,

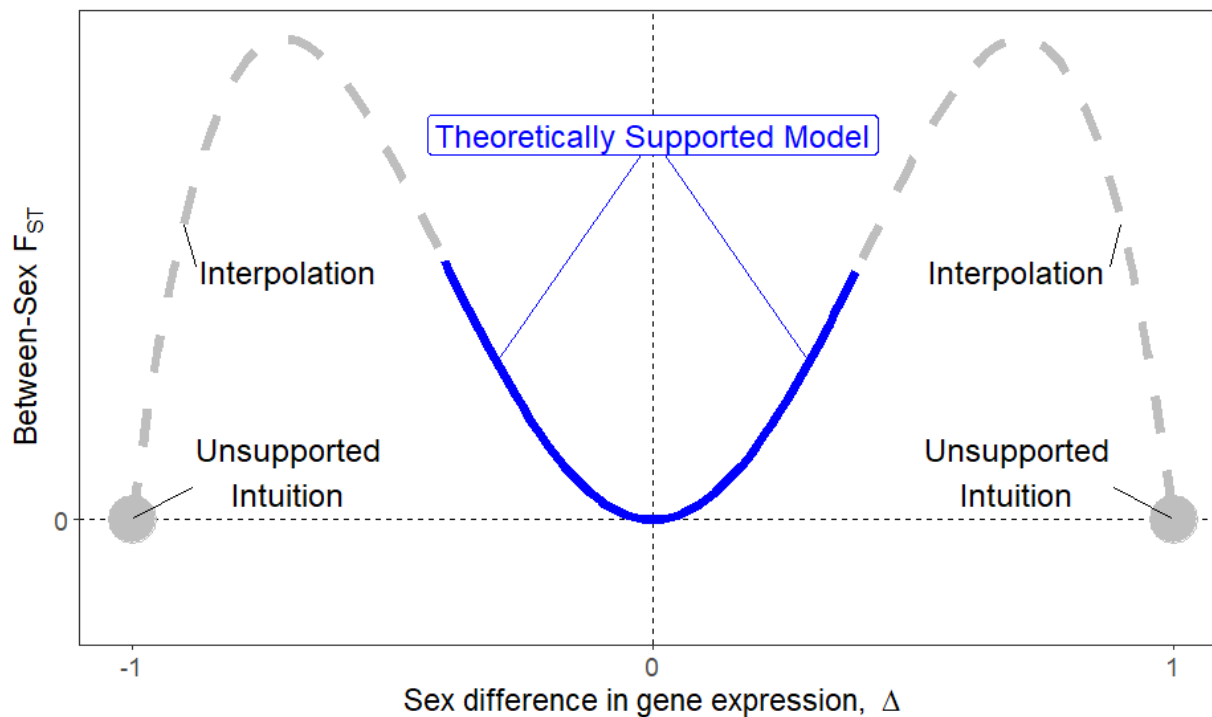
$$57 \quad F_{ST} = 4pq\Delta^2 A, \quad (1)$$

58 where  $p$  is the allele frequency in zygotes and  $q = 1 - p$ .  $F_{ST}$  is the between-sex fixation index<sup>18</sup>  
59 which is used to quantify allele frequency differences between males and females. In the model,  
60 these differences are due solely to the sex differences in post-zygotic fitness effects of alleles.  
61 The quantity  $\Delta$  is the sex difference in gene expression (**Methods**). Finally,  $A$  is a compound  
62 parameter involving the within-sex effect of gene expression level on fitness.

63 The expectation in CK16 for  $F_{ST}$  at extreme expression differences ( $|\Delta| \rightarrow 1$ ), however, is  
64 based on intuition rather than a model. The authors suggest that if a gene is not expressed in one  
65 sex ( $\Delta = \pm 1$ ), then selection will not act on it. Selection on the other sex should optimize  
66 expression levels, so under the symmetrical selection assumption there will be no ongoing  
67 directional selection in that sex either. As neither sex experiences selection, there will be no  
68 force driving increased  $F_{ST}$ . CK16 then interpolate a bimodal shape by joining the quadratic  
69 relationship at low  $|\Delta|$  and the expectation for  $F_{ST} = 0$  at  $\Delta = \pm 1$  (**Fig. 1**).

70 However, the assumption of symmetric selection used at low values of  $\Delta$  may be  
71 inappropriate for large  $\Delta$  values. In particular, when  $\Delta = \pm 1$ , the lack of expression in one sex  
72 plausibly suggests different selection between males and females. It is therefore not intuitive that  
73  $F_{ST}$  should simply go to zero at sites regulating expression in these genes. Additionally, although  
74 the quantity  $2pq$  appears in **Eq. 1**, CK16 did not include that term in fitting the model,  
75 effectively assuming it to only contribute random noise to the relationship between  $F_{ST}$  and  $\Delta$ .

76 Because of these caveats to the model, we decided to revisit the support for Twin Peaks.  
77 We first ask whether the Twin Peaks pattern is due to SDS by applying the statistical tests of  
78 CK16 to data generated under a null hypothesis of no relationship between  $\Delta$  and SDS. We  
79 replicated the pattern shown in CK16 by using the same data and methods. Namely, we  
80 performed a 4<sup>th</sup> degree polynomial regression of  $F_{ST}$  on  $\Delta$ , using allele count data from 1000



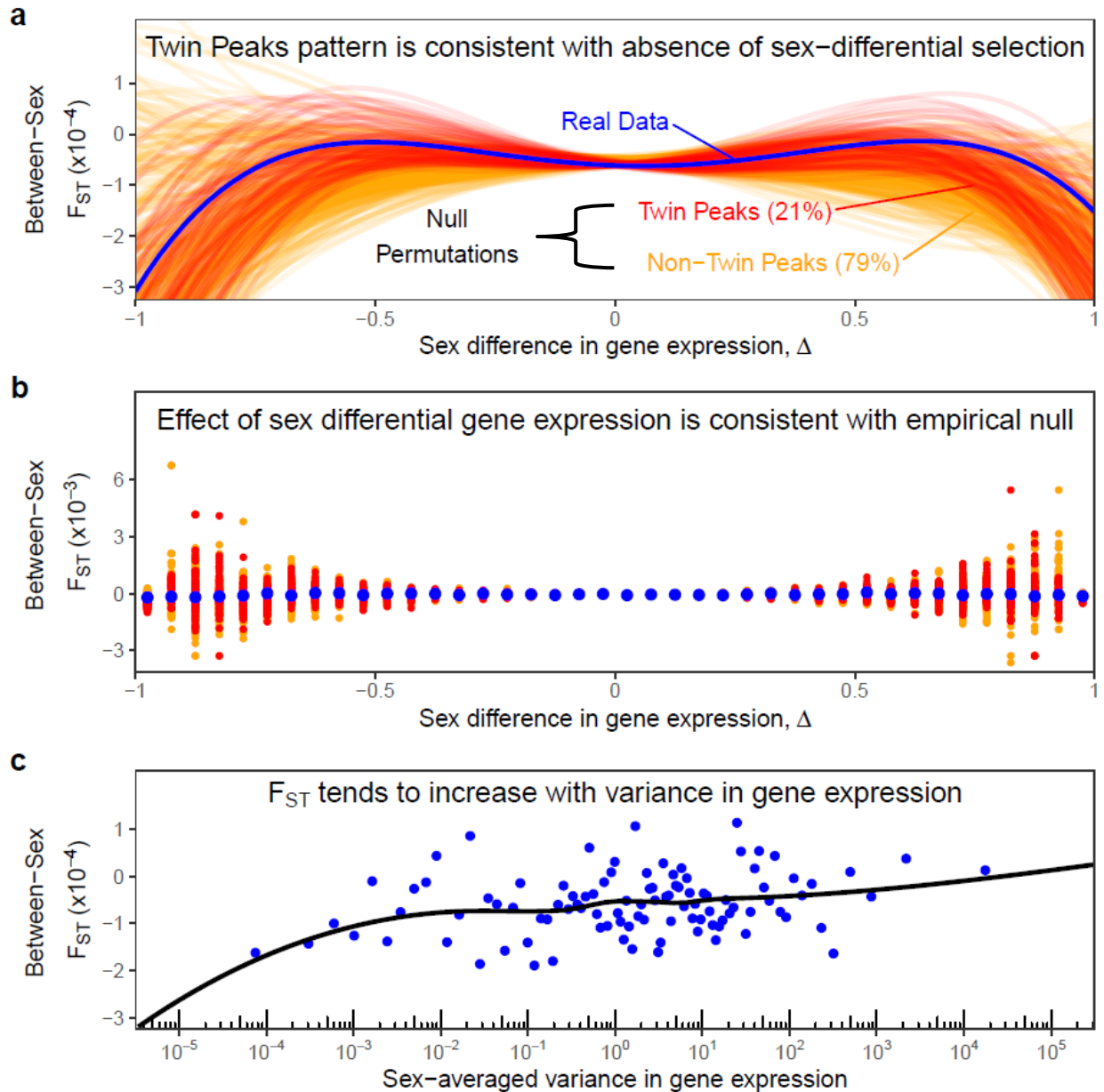
81

82 **Figure 1: Revisiting the Twin Peaks theoretical expectation.** Cheng and Kirkpatrick (2016)  
83 derive an expectation for a quadratic relationship at low values of  $\Delta$  (solid blue line). However,  
84 their expectation for “Twin Peaks” is based on a reasoning for  $F_{ST} = 0$  at genes with sex-specific  
85 expression ( $\Delta = \pm 1$ ) that is unsupported. Additionally, values between the theoretically  
86 supported region and the extremes are based on qualitative interpolation (dashed line). The  
87 portions of the model which are not supported are shown in grey.

88

89 Genomes<sup>19</sup> and expression data from the gonads (ovaries and testes) in GTEx v3<sup>20</sup>. The curve  
90 and associations generated using these datasets we refer to as the “real data” (blue line in **Fig.**  
91 **2a**).

92 We then generated an empirical null by permuting ovary and testes tissue labels in the  
93 expression data but retaining sex labels associated with  $F_{ST}$  values (**Methods**), then recomputed  
94  $\Delta$  values, and again fit a 4<sup>th</sup>-degree polynomial. We find 21% of permutations qualify as Twin  
95 Peaks according to the criteria used by CK16, and that the polynomial fit to the real data is not  
96 visually distinct from those fits to the null (**Fig. 2a**). Higher order polynomial regressions can  
97 also yield spurious fits because distant points have an oversized impact<sup>21,22</sup>. We therefore binned  
98 genes by  $\Delta$  values and examined the relationship with mean  $F_{ST}$  in each bin. Again, the real data  
99 shows no unusual relationship between  $F_{ST}$  and  $\Delta$  compared to null data (**Fig. 2b**). From these  
100 results, we conclude the Twin Peaks pattern is not statistically significant.



101

102 **Figure 2. The Twin Peaks pattern is the result of statistical artifacts.** a) A 4<sup>th</sup>-degree  
103 polynomial regression of between-sex  $F_{ST}$  to sex differences in gene expression for the real data  
104 is shown in blue. Red and yellow curves shown are fits based on samples from an empirical null  
105 generated by permuting the sex labels in expression data. In red (yellow) are null iterations  
106 classified as consistent (inconsistent) with the Twin Peaks expectation according to criteria  
107 employed by Cheng and Kirkpatrick (2016). b) The data was split into 40 evenly spaced bins of  
108 sex difference in gene expression to visualize mean trends. The x-axis values show the midpoint  
109 of each bin, and the y-axis values show mean male-female  $F_{ST}$  of biallelic sites within each bin. c)  
110 A positive relationship between  $F_{ST}$  and variance in gene expression (regardless of sex) may  
111 contribute to the genome-wide relationship between sex differences in gene expression and  
112 selection. Genes are divided into 100 evenly sized bins of sex-averaged sample variance in gene

113 expression. The y-axis values show the mean male-female  $F_{ST}$  for all biallelic sites for all genes  
114 in each the bin. The black curve shows a LOESS fit to the non-binned data.  
115

116 Importantly, this permutation method differs from the method used in CK16, which  
117 permuted  $\Delta$  values across genes. Both methods break the associations between  $F_{ST}$  and  $\Delta$  as  
118 desired. Our sex -label permutation method, however, preserves  $F_{ST}$  associations with the gene's  
119 overall expression, maintaining gene features such as expression variance which the CK16  
120 method does not. This explains why their reported  $p$ -value for Twin Peaks curves (0.016) is  
121 lower than our (0.21).

122 We hypothesized that one reason for the spurious Twin Peaks pattern is confounding. In  
123 particular, variance in expression (regardless of sex) is positively correlated with both  $\Delta$  and  $F_{ST}$ .  
124 Previous work has shown that genes subject to weaker stabilizing selection show higher variance  
125 in expression<sup>23</sup>. Higher variance means larger differences between randomly selected subgroups,  
126 and therefore it should translate to larger values of  $\Delta$  even in the absence of SDS. In turn,  
127 stronger (sex-agnostic) selection can lead to stronger drift at linked sites<sup>24,25,26,27</sup>. Taken together,  
128 the confounding with variance in gene expression could generate a relationship between SDS  
129 and  $|\Delta|$  in the absence of SDS. Indeed, expression variance and  $F_{ST}$  are positively correlated  
130 (Pearson  $p = 0.011$ ; **Fig. 2c**), consistent with this hypothesis. In sum, we do not find support for  
131 Cheng and Kirkpatrick's conclusion that there is a genome-wide relationship between  $F_{ST}$  and  $\Delta$ .

132

### 133 **No evidence for genome-wide SDS on eQTLs**

134 Although we do not find support for a relationship between sex differences in gene expression  
135 and selection using CK16's methodology for generating Twin Peaks, one may still exist. We test  
136 this hypothesis across many tissues using improved statistical modeling, data, and methods.  
137 Despite the caveats to portions of the model discussed above, we believe that CK16's theoretical  
138 expectation of a quadratic relationship between  $F_{ST}$  and small values of  $\Delta$  is valid. We therefore  
139 built on that model by introducing the compound parameter  $\delta^2 = 4qp\Delta^2$  and rewriting **Eq. 1** as

$$140 \quad F_{ST} = A\delta^2. \quad (2)$$

141 (**Methods**). To estimate  $A$ , for each gene-tissue pair, we used the single *cis*-eQTL from GTEx  
142 v8<sup>28</sup> with the strongest association with its expression. Our estimator of  $A$  is then the inverse-  
143 variance-weighted linear regression of  $F_{ST}$  on  $\delta^2$  (**Eq. 2**). The advantages of this formulation  
144 over CK16's are that it allows direct estimation of  $A$ , the strength of SDS on sex differences in

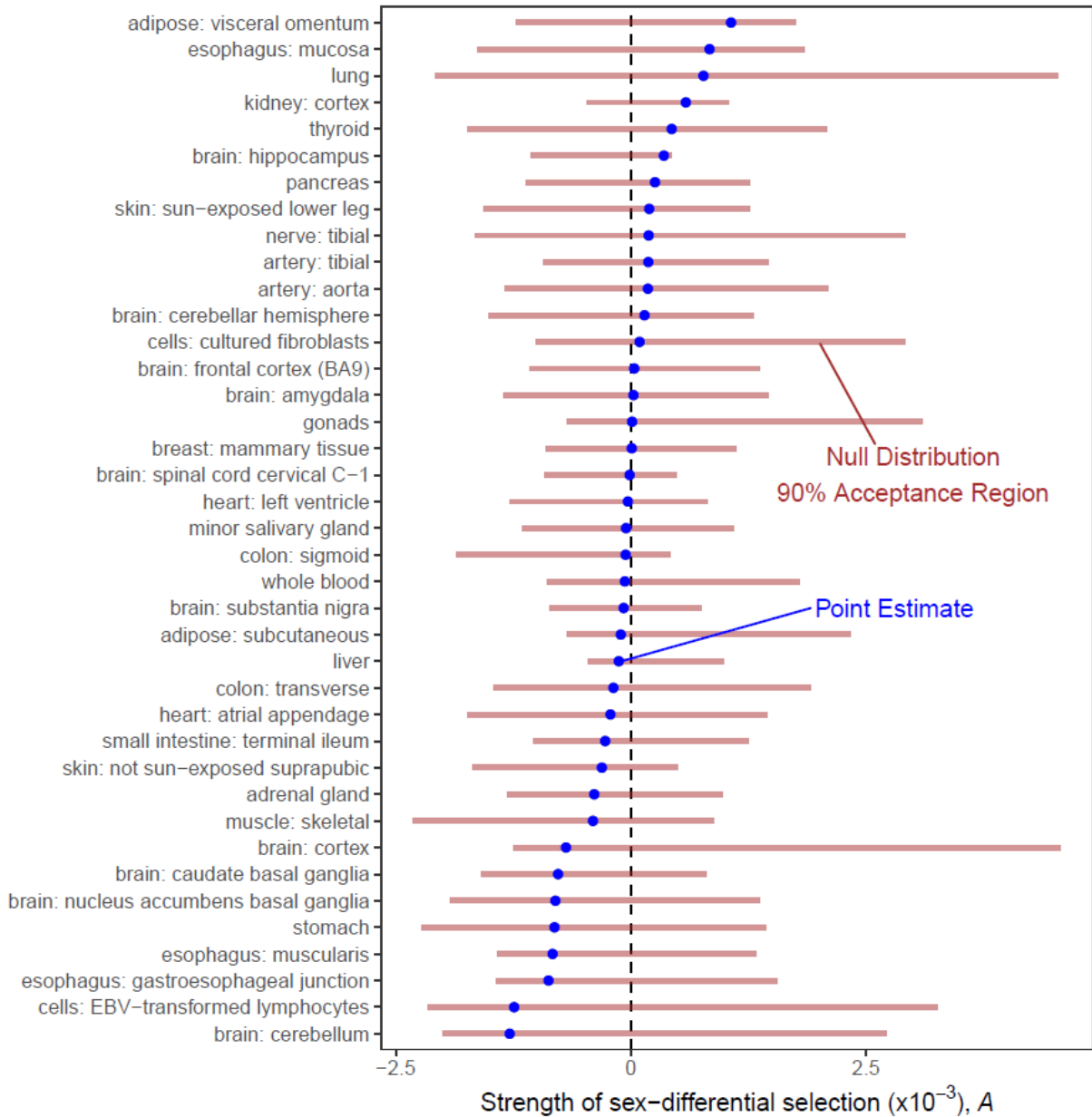
145 expression. This model also accounts for variation in allele frequencies across sites. Further, by  
146 using a single eQTL to calculate  $F_{ST}$  for the whole gene, we circumvent biases which can arise  
147 when using a simple mean to estimate gene-wide  $F_{ST}$ <sup>29,30</sup>.

148 To accompany the updated regression methodology, we also updated the datasets for both  
149 allele frequencies and gene expression. For allele frequencies, we used the Non-Finnish  
150 European subset in gnomAD v3 (averaging over 60,000 allele samples per site)<sup>31</sup>. We used  
151 expression data from 49 tissues from the GTEx v8 dataset<sup>28</sup> (averaging over 200 male samples  
152 and 150 female samples). Both datasets greatly expand our sample size compared to CK16, and  
153 GTEx v8 provides sample-specific sex labels for calculating  $\Delta$  across multiple tissues instead of  
154 just the gonads—ovaries and testes—as in the original Twin Peaks paper.

155 Using the updated statistical framework method, we find no evidence that  $A$  differs  
156 significantly from zero in any tissue (**Fig. 3; Methods**). One explanation for the absence of a  
157 pattern may be found in recent work by Mostafavi et al. (2023). The authors contrasted how  
158 selection impacts the discovery of genome-wide association study (GWAS) hits with the  
159 discovery of eQTLs. Variants with large effects on phenotypes are expected to segregate at low  
160 frequencies, reducing discovery power. In GWAS, this is counterbalanced by increased power  
161 due to their large effect sizes. Consequently, in GWAS, low frequency variants can still be  
162 detected if their effect is large enough. In contrast, eQTL discovery is based only on the effect of  
163 genotype on gene expression which does not necessarily translate to fitness-relevant trait  
164 variation. Detection of strongly selected sites is therefore less likely<sup>32</sup>. This ascertainment bias  
165 can weaken the relationship between  $\Delta$  and  $F_{ST}$  at eQTLs, as sites with high  $F_{ST}$  are less likely to  
166 be eQTLs.

167 In “**Twin Peaks is a Statistical Artifact**”, we suggested that large sex differences in  
168 expression may be entirely unrelated to SDS—for instance, merely tagging genes with high  
169 expression variance. There are other potential explanations for the lack of a genome-wide  
170 relationship. While some sex differences in expression may be driven by or drive SDS, these are  
171 the exception rather than the rule. The majority of sex differences in expression may be a  
172 regulatory side effect of SDS on different genes. Lastly, sex-differential gene expression may be  
173 due to past SDS, but not drivers of current SDS<sup>33</sup>. Regardless of the reason, if a causal  
174 relationship between  $\Delta$  and  $F_{ST}$  is rare in the genome, it would be difficult to detect using  
175 models that assume a pervasive, persistent relationship between the two.





176

177 **Figure 3. Lack of evidence for sex-differential selection on sex-differential gene expression**  
 178 **using newer data.** Shown are estimates of  $A$  (Eq. 2). Acceptance regions are based on the 5<sup>th</sup> to  
 179 95<sup>th</sup> quantiles of an empirical null distribution generated by permuting sex labels in the gene  
 180 expression data.

181

182 **Conclusion** Previous work suggested a genome-wide relationship between sex differences in  
 183 expression and SDS. However, this work was based on statistical artifacts and confounded  
 184 effects, such as stabilizing selection and variance in gene expression. Even when using newer  
 185 data and improved statistical methods, we found no evidence for a genome-wide relationship



186 between sex-differential expression and contemporary SDS. In contrast, studies that measured  
187 SDS irrespective of expression or trait variation have reported pervasive, genome-wide signals of  
188 SDS in the human genome<sup>5,10,34</sup>. While causal relationships, past and present, between SDS and  
189 sex-differential gene expression in humans remain plausible, they are yet to be fully elucidated.

190

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195

## 196 **Materials and Methods**

### 197 **Permuting Twin Peaks sex-labels**

198 In the section “**Twin Peaks is a Statistical Artifact**”, we demonstrate that the Twin Peaks curve  
199 presented in CK16 is not statistically significant compared to a permuted null. To do so, we used  
200 the methods and datasets described in CK16 and **Eq. 1**. We computed allele count using the  
201 1000 Genomes dataset<sup>19</sup> and calculating  $F_{ST}$ . We filtered out any sites with only a single  
202 alternative allele in either males or females (i.e., singletons). We used the Transcripts Per Million  
203 (TPM) normalized GTEx v3 (referred to as “pilot” on the download page) dataset<sup>20</sup> for  
204 expression levels for calculating  $\Delta$ . Because GTEx v3 does not have individual sample labels,  
205 this analysis only compared expression in the gonads (ovaries and testes) where expression level  
206 summaries represent a single biological sex. We used the Ensembl GRCh38 v77<sup>35</sup> annotation file  
207 for gene annotations. Following CK16, we limited our analysis to protein-coding genes.

208 To estimate  $F_{ST}$ , we used Hudson’s estimator<sup>36</sup> based on the R package used in CK16<sup>37</sup> as  
209 presented by Bhatia et al. (2013)<sup>29</sup>,

$$210 \quad \hat{F}_{ST} = \frac{(p_m - p_f)^2 - \frac{p_m(1-p_m)}{n_m-1} - \frac{p_f(1-p_f)}{n_f-1}}{p_m(1-p_f) + p_f(1-p_m)}. \quad (3)$$

211 Here,  $p_m$  and  $p_f$  are the allele frequencies in males and females respectively, and  $n_m$  and  $n_f$  are  
212 the number of males and females respectively. As a measure of sex-differential expression we  
213 used  $\Delta$  as defined in CK16:

214 
$$\Delta = \frac{x_m - x_f}{x_m + x_f} \quad (4)$$

215 Here,  $x_m$  and  $x_f$  are sex-averaged TPM-normalized expression levels in males and females  
216 respectively. Because  $\hat{F}_{ST}$  in **Eq. 3** is a site-specific estimator while  $\Delta$  is gene-wide, we generated  
217 a gene-wide estimate of  $F_{ST}$  by taking a simple average of all sites within a gene body plus  
218 1000bp upstream and downstream. To generate the Twin Peaks curve, we used a 4<sup>th</sup>-degree  
219 polynomial regression between  $\hat{F}_{ST}$  and  $\Delta$ . We note that here and in CK16, this regression  
220 therefore ignores variation in heterozygosity across sites (**Eq. 1**). In our improved model  
221 (**Results: “No evidence for SDS on eQTLs across all genes in multiple tissues”** and **Methods:**  
222 **“Applying a new model and method for SDS-expression regression”**) we correct this  
223 omission.

224 To compare the original Twin Peaks curve to curves generated under the null of no SDS,  
225 we generated an empirical null distribution of 4<sup>th</sup>-degree regression curves using sex-label  
226 permutations of gene expression data. We permuted the ovary and testes labels for each GTEx  
227 sample, then recalculated  $\Delta$  for all genes. We then re-performed the 4<sup>th</sup>-degree polynomial  
228 regression on the new  $\Delta$  values (the  $F_{ST}$  values remain unchanged). This was repeated 500 times.  
229 By permuting sex labels, we break the association between sex-differential expression and sex-  
230 differential expression, while preserving other gene-level features. To quantitatively evaluate the  
231 significance of Twin Peaks in the null distribution, we used the three criteria laid out by Cheng  
232 and Kirkpatrick (2016) for classifying a curve as Twin Peaks. Namely, a 4<sup>th</sup>-degree polynomial  
233 must 1) be significant ( $p < 0.05$ ) for the 4<sup>th</sup>-degree term by ANOVA, 2) have a negative  
234 coefficient for the  $\Delta^4$  term, and 3) have three real roots. Any 4<sup>th</sup>-degree regression passing all  
235 three criteria is classified as Twin Peaks.

236

### 237 **Applying a new model and method for SDS-expression regression**

238 In the section **“No evidence for SDS on eQTLs across all genes in multiple tissues”**, we  
239 described a revised method for testing a genome-wide relationship between SDS and  $\Delta$ . For this  
240 analysis, we revised the inference model and data. We used the Non-Finnish European subset in  
241 the gnomAD V3 dataset<sup>31</sup> to calculate between-sex  $F_{ST}$  and heterozygosity at each eQTL. This  
242 set of samples has an order of magnitude more individuals (average of 31,470 samples per site)  
243 compared to 1000 Genomes data (average of 2,300 samples per site when combining all ancestry

244 groups) originally used in CK16. Additionally, we used the normalized TPM from the current  
245 GTEx v8 for expression level data, which includes many more samples (average of 236 male and  
246 168 female samples per tissue) than the pilot (8 male samples and 13 female samples in the  
247 gonads)<sup>28</sup>. This version also provides sample-specific sex labels, enabling us to use additional  
248 tissues beyond gonads.

249 The equation we base our regression on is the model relating  $F_{ST}$  with  $\delta^2$  shown in **Eq. 2**.  
250 Now, rather than performing a 4<sup>th</sup>-degree polynomial regression as in the analysis for “**Twin**  
251 **Peaks is a Statistical Artifact**”, we perform a weighted linear regression of  $F_{ST}$  to  $\delta^2 = 4pq\Delta^2$ ,  
252 isolating  $A$  as the coefficient of regression. Note that by including  $4pq$  in the independent  
253 variable, we allow information about heterozygosity to affect the SDS-expression relationship.  
254 We weighted each point of the regression by  $1/Var(expression)$ , where  $Var(expression)$  is  
255 the averaged variance in expression of each sex. This should decrease the leverage of points with  
256 large  $|\Delta|$ . To get a gene-wide estimate of  $F_{ST}$ , we used eQTLs from GTEx as mapped in the v8  
257 study<sup>31</sup>. For each gene, we chose the single *cis*-eQTL (within 1Mbp of the gene’s midpoint) with  
258 lowest  $p$ -value for association with the gene and use that site for calculating  $F_{ST}$ ,  $p$ , and  $q$ . By  
259 using an eQTL selected this way, we tried to isolate the effect of selection on gene expression to  
260 the site presumed to be contributing most to expression changes in that gene.

261 To determine the significance of our  $A$  estimates, we generated 90% null acceptance  
262 regions by permuting sex labels. We permuted sex labels as in “**Twin Peaks sex-label**  
263 **permutation**” such that for each tissue, sex labels are permuted in GTEx expression samples and  
264  $\Delta$  is recalculated across all genes. Then, for each iteration  $A$  is recalculated by linear regression  
265 using the new  $\Delta$  values ( $F_{ST}$  and  $4pq$  remain unchanged). The 90% null acceptance region was  
266 obtained by the 5<sup>th</sup> and 95<sup>th</sup> percentiles of 1,000  $A$  values calculated on permuted expression data.

## 267 Literature Cited

- 268 1. Cheng, C., & Kirkpatrick, M. (2016). Sex-specific selection and sex-biased gene  
269 expression in humans and flies. *PLoS Genetics*, *12*(9).
- 270 2. Naqvi, S., Godfrey, A. K., Hughes, J. F., Goodheart, M. L., Mitchell, R. N., & Page, D. C.  
271 (2019). Conservation, acquisition, and functional impact of sex-biased gene expression in  
272 mammals. *Science*, *365*(6450).
- 273 3. Rice, W. R. (1984). Sex chromosomes and the evolution of sexual dimorphism. *Evolution*,  
274 *735-742*.
- 275 4. Wright, A. E., Fumagalli, M., Cooney, C. R., Bloch, N. I., Vieira, F. G., Buechel, S. D., ...  
276 & Mank, J. E. (2018). Male-biased gene expression resolves sexual conflict through the  
277 evolution of sex-specific genetic architecture. *Evolution Letters*, *2*(2), 52-61.
- 278 5. Zhu, C., Ming, M. J., Cole, J. M., Edge, M. D., Kirkpatrick, M., & Harpak, A. (2023).  
279 Amplification is the primary mode of gene-by-sex interaction in complex human traits.  
280 *Cell Genomics*, *3*(5).
- 281 6. Oliva, M., Muñoz-Aguirre, M., Kim-Hellmuth, S., Wucher, V., Gewirtz, A. D., Cotter, D.  
282 J., Parsana, P., Kasela, S., Balliu, B., ... & Stranger, B. E. (2020). The impact of sex on  
283 gene expression across human tissues. *Science*, *369*(6509).
- 284 7. Khramtsova, E. A., Wilson, M. A., Martin, J., Winham, S. J., He, K. Y., Davis, L. K., &  
285 Stranger, B. E. (2023). Quality control and analytic best practices for testing genetic  
286 models of sex differences in large populations. *Cell*, *186*(10), 2044-2061.
- 287 8. Ober, C., Loisel, D. A., & Gilad, Y. (2008). Sex-specific genetic architecture of human  
288 disease. *Nature Reviews Genetics*, *9*(12), 911-922.
- 289 9. Connallon, T., & Hall, M. D. (2018). Environmental changes and sexually antagonistic  
290 selection. *eLS*, 1-7.

- 291 10. Ruzicka, F., Holman, L., & Connallon, T. (2022). Polygenic signals of sex differences in  
292 selection in humans from the UK Biobank. *PLoS Biology*, *20*(9), e3001768.
- 293 11. Ellegren, H., & Parsch, J. (2007). The evolution of sex-biased genes and sex-biased gene  
294 expression. *Nature Reviews Genetics*, *8*(9), 689-698.
- 295 12. Mank, J. E., Shu, J. J., & Wright, A. E. (2020). Signature of sexual conflict is actually  
296 conflict resolved. *Molecular Ecology*, *29*(2): 215–217.
- 297 13. Cheng, C., & Kirkpatrick, M. (2020). The signal of sex-specific selection in humans is  
298 not an artifact: Reply to Mank et al. *Molecular Ecology*, *29*(8), 1406.
- 299 14. Kasimatis, K. R., Abraham, A., Ralph, P. L., Kern, A. D., Capra, J. A., & Phillips, P. C.  
300 (2021). Evaluating human autosomal loci for sexually antagonistic viability selection in  
301 two large biobanks. *Genetics*, *217*(1).
- 302 15. Kirkpatrick, M., & Guerrero, R. F. (2014). Signatures of sex-antagonistic selection on  
303 recombining sex chromosomes. *Genetics*, *197*(2), 531-541.
- 304 16. Dutoit, L., Mugal, C. F., Bolívar, P., Wang, M., Nadachowska-Brzyska, K., Smeds, L.,  
305 Yazdi, H. P., Gustafsson, L., & Ellegren, H. (2018). Sex-biased gene expression, sexual  
306 antagonism and levels of genetic diversity in the collared flycatcher (*Ficedula albicollis*)  
307 genome. *Molecular Ecology*, *27*(18), 3572-3581.
- 308 17. Vaux, F., Rasmuson, L. K., Kautzi, L. A., Rankin, P. S., Blume, M. T. O., Lawrence, K.  
309 A., Bohn, S., & O'Malley, K. G. (2019). Sex matters: otolith shape and genomic  
310 variation in deacon rockfish (*Sebastes diaconus*). *Ecology and Evolution*, *9*, 13153–  
311 13173.
- 312 18. Wright, S. (1949). The genetical structure of populations. *Annals of Eugenics*, *15*(1), 323-  
313 354.
- 314 19. 1000 Genomes Project Consortium. (2015). A global reference for human genetic  
315 variation. *Nature*, *526*(7571), 68.

- 316 20. Lonsdale, J., Thomas, J., Salvatore, M., Phillips, R., Lo, E., Shad, S., Hasz, R., Walters,  
317 G., Garcia, F., Young, N., & Moore, H. F. (2013). The genotype-tissue expression (GTEx)  
318 project. *Nature Genetics*, *45*(6), 580-585.
- 319 21. Harrell, F. E. (2001). *Regression modeling strategies: with applications to linear models,*  
320 *logistic regression, and survival analysis* (Vol. 608). New York: springer.
- 321 22. Magee, L. (1998). Nonlocal behavior in polynomial regressions. *The American*  
322 *Statistician*, *52*(1), 20-22.
- 323 23. Glassberg, E. C., Gao, Z., Harpak, A., Lan, X., & Pritchard, J. K. (2019). Evidence for  
324 weak selective constraint on human gene expression. *Genetics*, *211*(2), 757-772.
- 325 24. Charlesworth, B. (1994). The effect of background selection against deleterious  
326 mutations on weakly selected, linked variants. *Genetics Research*, *63*(3), 213-227.
- 327 25. Hudson, R. R., & Kaplan, N. L. (1995). Deleterious background selection with  
328 recombination. *Genetics*, *141*(4), 1605-1617.
- 329 26. Hudson, R. R., & Kaplan, N. L. (1995). The coalescent process and background selection.  
330 *Philosophical Transactions of the Royal Society of London. Series B: Biological Sciences*,  
331 *349*(1327), 19-23.
- 332 27. Murphy, D. A., Elyashiv, E., Amster, G., & Sella, G. (2022). Broad-scale variation in  
333 human genetic diversity levels is predicted by purifying selection on coding and non-  
334 coding elements. *Elife*, *12*.
- 335 28. GTEx Consortium. (2020). The GTEx Consortium atlas of genetic regulatory effects  
336 across human tissues. *Science*, *369*(6509), 1318-1330.
- 337 29. Reynolds, J., Weir, B. S., & Cockerham, C. C. (1983). Estimation of the coancestry  
338 coefficient: basis for a short-term genetic distance. *Genetics*, *105*(3), 767-779.

- 339 30. Bhatia, G., Patterson, N., Sankararaman, S., & Price, A. L. (2013). Estimating and  
340 interpreting FST: the impact of rare variants. *Genome Research*, 23(9), 1514-1521.
- 341 31. Chen, S., Francioli, L. C., Goodrich, J. K., Collins, R. L., Kanai, M., Wang, Q., Alföldi, J.,  
342 Watts, N. A., Vittal, C., Gautier, L. D., ... & Karczewski, K. J. (2024). A genomic  
343 mutational constraint map using variation in 76,156 human genomes. *Nature*, 625(7993),  
344 92-100.
- 345 32. Mostafavi, H., Spence, J. P., Naqvi, S., & Pritchard, J. K. (2023). Systematic differences  
346 in discovery of genetic effects on gene expression and complex traits. *Nature Genetics*,  
347 55(11), 1866-1875.
- 348 33. Muralidhar, P., & Coop, G. (2024). Polygenic response of sex chromosomes to sexual  
349 antagonism. *Evolution*, 78(3), 539-554.
- 350 34. Cole, J., Scott, C.B, Johnson, M.M., Golightly, P.R., Carlson, J., Ming, M.M., Harpak, A.,  
351 Kirkpatrick, M. (2024). The battle of the sexes in humans is highly polygenic. Preprint.
- 352 35. Cunningham, F., Allen, J. E., Allen, J., Alvarez-Jarreta, J., Amode, M. R., Armean, I. M.,  
353 Austine-Orimoloye, O., Azov, A. G., Barnes, I., Bennett, R., ... & Flicek, P. (2022).  
354 Ensembl 2022. *Nucleic Acids Research*, 50(D1), D988-D995.
- 355 36. Hudson, R. R., Slatkin, M., & Maddison, W. P. (1992). Estimation of levels of gene flow  
356 from DNA sequence data. *Genetics*, 132(2), 583-589.
- 357 37. Pfeifer, B., Wittelsbürger, U., Ramos-Onsins, S. E., & Lercher, M. J. (2014). PopGenome:  
358 an efficient Swiss army knife for population genomic analyses in R. *Molecular Biology*  
359 *and Evolution*, 31(7), 1929-1936.