Title: **Activation and regulation of a p38α MAPK by its downstream MAPKAP kinase**

**through feedback phosphorylation and LLPS-driven condensate formation.**

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**Highlights:**

• PMK3 participates in a feedback phosphorylation loop with its downstream kinase

MAK2 that leads to the phosphorylation of the activating TxY motif.

• MAK2 Phosphorylates PMK-3 at Ser, Thr and Tyr residues and that is a dual specificity

kinase rather than a Ser/Thr kinase.

• MAK2 but not PMK3 alone forms condensates through liquid liquid phase separation

(LLPS).

• While PMK3 alone is prone to aggregation, MAK2 prevents aggregation of PMK3 via

LLPS-mediated condensate formation when present together.

**Abstract:**

**MAP kinases (MAPKs) represent a class of evolutionarily conserved signaling**

**molecules that respond to an array of extracellular stimuli and stresses. p38 group of**

**MAPKs have been implicated in a multitude of signal transduction pathways known to**

**be activated by dual-specific upstream MAPK kinases and also by**

**autophosphorylation. They activate MAPK activated protein kinases (MAPKAPKs) in a**

**context dependent manner by specific phosphorylation, and together they play crucial**

biological roles. One such pair in *C. elegans* consists of PMK3, p38$\alpha$-MAPK and its cognate MAPKAPK, MAK2 downstream of DLK1 (MAPK kinase kinase) and MKK4 (MAPK kinase). They are implicated in axonal regeneration, degeneration and synaptic pruning in response to neuronal injury. Here, we report that PMK3 participates in a feedback loop with MAK2 leading to phosphorylation-mediated activation of both kinases. Interestingly, MAK2 that is a Ser/Thr kinase phosphorylates PMK3 at its TxY-motif required for the manifestation of full activity of PMK3. This observation identifies MAK2 as a dual specificity kinase. Distribution of phosphorylation sites on either kinase and presence of long intrinsically disordered regions in each of them indicate the possibility of conformational plasticity in the PMK3:MAK2 complex. Furthermore, MAK2 increases bioavailability of aggregation-prone PMK3 by forming LLPS-driven condensates. PMK3 and MAK2 retain the feedback phosphorylation relationship and enzymatic activities in the condensate state as well. Our observations establish an unreported feedback relationship between a MAPK and its downstream MAPKAPK through phosphorylation and LLPS-driven condensate formation.

**Significance Statement:**

MAPK family of protein kinases are evolutionarily conserved and participate in a diverse array of signaling events. p38 MAPKs are key players in cellular phenomenon involving cell survival, differentiation, metabolic processes, and neuronal response to injury. They are activated through phosphorylation by upstream MAPK kinases (MAP2Ks) or by autophosphorylation. We found that a *C. elegans* MAPK (PMK3) engages in a feedback phosphorylation loop with its downstream effector kinase MAK2, but not the upstream MAP2K MKK4, that ensures robust activation of PMK3 by MAK2 without requiring MKK4. In addition, MAK2 increases bioavailability of activation-competent and active PMK3 by preventing its aggregation through LLPS-driven condensate formation. This feedback relationship between a MAPK and its downstream MAPKAPK might ensure rapid activation of this pathway in response to nervous system injury or stress.

**Introduction:**

Protein kinases are implicated in almost, if not all, signaling events in eukaryotes (Manning et al., 2002). Mitogen activated protein kinases (MAPKs) are activated by a variety of extracellular stimuli that regulate a plethora of cellular processes including but not limited to gene expression, cell cycle, cell survival, infection, inflammation, apoptosis, differentiation and metabolism (Battagello et al., 2020; Bouhaddou et al., 2020; Cuadrado and Nebreda, 2010; Luecke et al., 2024; Widmann et al., 1999). They are one of the most ancient signal transduction molecules observed throughout evolution. Multiple MAPK pathways are found to operate in concert in eukaryotes. A canonical MAPK module consists of two upstream kinases, MAPK kinase (MAPKK or MAP2K) and MAKK kinase (MAPKKK or MAP3K)(Pearson et al., 2001). In response to extracellular stimuli, a MAP3K activates its cognate MAP2K that in turn activates the downstream MAPK – making it a three-kinase signaling module where the signal transmits from the MAP3K to MAPK via the MAP2K. Activation of p38$\alpha$ by autophosphorylation has also been documented (Ge et al., 2002) apart from the canonical mode of MAPK activation by MAP2K suggesting multiple modes of MAPK-activation in play. MAPKs are Ser/Thr kinases that phosphorylate different kinds of protein substrates in cells including transcription factors and specific protein kinases called the MAPK activated protein kinases (MAPKAPKs) (Cargnello and Roux, 2011).

p38 group of MAPKs are perhaps the most widely implicated and most well-studied pathways among the four distinct subgroups of the MAPK family (Canovas and Nebreda, 2021; Cuadrado and Nebreda, 2010). In mammals, there are four isoforms of p38: $\alpha$, $\beta$, $\gamma$ and $\delta$. Among these p38$\alpha$ is the most well studied one. Among many substrates of p38$\alpha$ MAPKAPK2 or MK2 have been implicated in many cellular processes that phosphorylate substrates including small heat shock protein 27 (Hsp27), cAMP response element-binding protein (CREB), lymphocyte-specific protein 1 (LSP1), transcription factor ATF1 etc (Zarubin and Han, 2005). p38 MAPKs are present both in the cytoplasm and nuclei of cells and are sequestered mostly in the nuclei in certain stress conditions. Nucleocytoplasmic shuttling of the p38 MAPKs is also regulated by their association with the MAPKAPKs (Ben-Levy et al., 1998).

*C. elegans* genome consists of three genes, *pmk1, pmk2* and *pmk3* that code for three p38 MAPK isoforms: PMK1, PMK2 and PMK3, respectively. These three genes constitute an operon with a polarity from *pmk1* to *pmk3*, and are expressed under the influence of a single promoter (Berman et al., 2001). Among these three p38 MAPK isoforms PMK3 has been implicated in axonal regeneration acting as the MAPK downstream of MAP2K, MKK4 that is activated by the MAP3K, DLK1 in both *C. elegans* and other organisms (Hammarlund et al., 2009; Hao et al., 2016; Shin et al., 2012; Yan et al., 2009). This signaling mechanism is also

implicated in synaptic maturation in multiple organisms, which is under the tight regulation of
E3 ubiquitin ligase (Lewcock et al., 2007; Nakata et al., 2005; Schaefer et al., 2000). In the
axonal regeneration pathway involving DLK-1, the terminal kinase however is not the MAPK
but a cognate MAPKAPK of PMK3 known as MAK2 (Fig 1A). MAK2 is involved in the
maintenance of the neuronal synapses and axon morphology. It has also been shown that
MAK2 regulates touch neuron axon regeneration by modulating *cebp-1* mRNA stability in
response to axon injury in nematode (Yan et al., 2009). A search for the protein-protein
interaction networks related to PMK3 and MAK2 on the STRING database revealed strong
interactions between the two proteins (Fig S1A). We asked the question, whether activation,
regulation and mutual relationship of p38$\alpha$ and its MAPKAPK established in mammalian
systems also holds true in the PMK3:MAK2 system, which is involved in multiple cellular
responses such as axon regeneration (Hammarlund et al., 2009), degeneration (Asghari Adib
et al., 2018), and synaptic pruning (Asghari Adib et al., 2024) following neuronal injury.  We
used the nematode specific counterparts of MAPK and MAPKAP as our model system. Our
biochemical, computational and mass spectrometric analyses revealed that PMK3
participates in a hitherto unknown feedback phosphorylation loop with its downstream kinase
MAK2 that leads to the phosphorylation of the activating TxY motif. This observation in turn
proved that MAK2 is a dual specificity kinase rather than a Ser/Thr kinase as it is annotated
in the different databases. We also found that, MAK2 but not PMK3 forms condensates
through liquid liquid phase separation (LLPS). Intriguingly, while PMK3 alone is prone to
aggregation -- MAK2 prevents aggregation of PMK3 via LLPS-mediated condensate formation
when present together. The feedback phosphorylation relationship remains functional in the
condensate state. These observations point towards an unknown regulatory aspect of a
kinase (PMK3) wherein it is regulated by its cognate downstream kinase (MAK2) not only by
means of its catalytic activity to chemically modify (activating phosphorylation) but also
through change of physico-chemical microenvironment in the form of condensates. Overall,
our study revealed a new mechanistic understanding of the regulation of the injury sensing
MAPK PMK-3 via its downstream kinase MAPKAP MAK-2.
131
**Results:**
***In vitro* reconstitution of a MAPK-MAPKAPK module implicated in axonal regeneration**
**in *C. elegans*:**
PMK3 (Uniprot id: O44514, M.W. 54.9kDa) is a p38 MAPK in *C. elegans* (Fig 1B). It
participates in the DLK1-dependent signaling cascade in axonal regeneration pathway
downstream of the MAP2K, MKK4 (KEGG pathway cel04361) (Hammarlund et al., 2009; Yan
et al., 2009). DLK1 acts as the MAP3K in the said pathway. PMK3 phosphorylates a
downstream kinase MAK2 (Uniprot id: Q965G5, M.W. 41.5kDa), a MAP kinase activated

protein kinase (MAPKAPK) (Fig 1B). The involvement of MAK2 in this cascade turns the
canonical three-kinase MAPK-module into a four-kinase module. To understand the mutual
relationship between these two terminal kinases in further details, we sought to purify PMK3
and MAK2 recombinantly (see materials and methods). Of note, PMK3 showed highest
similarity with the p38α MAPK when compared with the four p38 MAPKs of the human origin
(Fig S1B). PMK3 was overexpressed in *E. coli* and purified as a 6X-His tagged protein from
the soluble fraction. Interestingly, fractions eluted from Ni-NTA column (Fig S1C, left panel)

**Figure 1*: In vitro* reconstruction of a MAPK-MAPKAPK module involved in axonal regeneration in *C. elegans.***
**(A)** Schematic representation of the unique four-kinase DLK-1 MAPK signaling pathway in *C. elegans*. PMK3 (MAPK) and MAK2 (MAPKAPK) act as the two terminal kinases in this module.
**(B)** Top: Domain architecture of PMK3 depicting the kinase domain and the T-X-Y motif within
the activation loop. Lower panel: Domain architecture of MAK2 depicting the kinase domain,
the nuclear export signal (NES) and the nuclear localization signal (NLS). The domain borders
have been numbered. **(C)** Comparison of the size exclusion profiles of 6X His-PMK3 and a molecular weight standard resolved on a preparative gel filtration column. The absorbance at
280nm has been plotted against the elution volume. The larger molecular weight fractions
constitute Peak 1 and the lower molecular weight fractions constitute Peak2. **(D)** *In vitro* radioactive kinase assay with purified, recombinant PMK3 and MAK2 using myelin basic
protein (MBP) as a generic substrate. **(E)** *In vitro* radioactive kinase assay with purified,
recombinant PMK3 and MAK2. PMK3 from two peaks in SEC was used for the assay in different reactions.

separated into two distinct peaks corresponding to molecular weight (MW) greater than

670kDa (oligomer) and greater than 44kDa but less then 158kDa (possibly a dimer) when

**Figure S1**

161 resolved on a preparative Superdex 200 SEC column (Fig 1C; corresponding Coomassie

162 brilliant blue stained SDS-PAGE is shown in Fig S1C, right panel). MAK2 was similarly purified

from *E. coli*. Unlike PMK3, MAK2 eluted as a single peak when resolved on the same SEC column (Fig S1D, left panel; corresponding Coomassie brilliant blue stained SDS-PAGE is shown in Fig S1D, right panel). MAK2 and low MW fraction of PMK3 were then subjected to *in vitro* radioactive kinase assay using myelin basic protein (MBP) as a generic substrate (Cicirelli et al., 1988). Both of these kinases phosphorylated MBP, wherein PMK3 was found to phosphorylate MBP more efficiently than MAK2 (Fig 1D).

It is expected that active PMK3 would phosphorylate its downstream kinase MAK2. We wanted to confirm this phenomenon with our purified recombinant kinases. PMK3 from the two peaks eluting from the SEC column were subjected to *in vitro* kinase assays using $\gamma$-$^{32}$P-ATP as the phosphate donor and MAK2 as the substrate. Substrate phosphorylation and autophosphorylation was monitored by autoradiography (Fig 1E). PMK3 from the smaller MW peak displayed huge activity towards MAK2 (lane 6) while the same protein in the large MW fraction did not show any detectable activity in the same assay (lane 3). These observations hinted that oligomerization of PMK3 into a large self-assembly was detrimental to its activity. Interestingly, when PMK3 was subjected to same assay without the MAK2 it displayed much lower level of autophosphorylation (lanes 4,5) compared to that in the presence of MAK2 (lane 6). Furthermore, MAK2 alone showed very low level, if any, of autophosphorylation signal (lanes 7,8) in absence of PMK3. Enhancement of phosphorylation of MAK2 in presence of PMK3 was expected owing to the fact that MAK2 is an MAPK activated protein kinase and is assigned down stream of its cognate MAPK, PMK3. However, it came as a surprise when phosphorylation of PMK3 was profoundly increased in presence of its downstream substrate kinase, i.e., MAK2 pointing to a plausible feedback phosphorylation loop (Fig 1E).

**PMK3 participates in a feedback phosphorylation loop with downstream kinase MAK2 but not with upstream kinase MKK4:**

The above set of experiments hinted to the possibility of existence of a feedback phosphorylation loop between the MAPK (PMK3) and its downstream kinase MAK2. We wanted to further analyze this possibility using our *in vitro* assay system using purified

recombinant proteins. 1uM of PMK3 was incubated with 6uM of MAK2 in presence of $\gamma$-$^{32}$P-

ATP as the phosphate donor for different time intervals at 25°C, and the resulting reaction

mixtures were resolved on an SDS-PAGE prior to detecting the phosphorylation signal by

phosphor-imaging after drying the gel. Respective kinases were incubated alone at the same

concentration as in the mixtures for the same time intervals to assess self-phosphorylation. It

was observed that, both PMK3 and MAK2 were heavily phosphorylated in a time dependent

manner when incubated together (lanes 5-8) (Fig 2A). Those kinases, however, did not show

appreciable autophosphorylation when incubated alone in the same assay conditions (lanes

1-4 and 9-12) (Fig 2A). This result confirmed the presence of a feedback phosphorylation loop

between these two kinases (Fig 2A). We next wanted to check if this feedback phosphorylation

is dependent upon the relative stoichiometry of the two participating kinases. To this end, we

used equimolar concentration of the kinases (~2uM each) and followed their phosphorylation

in the same conditions as mentioned above.  Like the last assay, both PMK3 and MAK2 were

heavily phosphorylated when incubated together as expected suggesting that the feedback

phosphorylation was independent of the relative stoichiometry of the two kinases (lanes 9-12)

(Fig 2B). MAK2 did not show appreciable autophosphorylation (lanes 5-8), however, PMK3

showed higher levels of autophosphorylation (lanes 1-4) (Fig 2B) compared to that in Fig 2A

raising the possibility that autophosphorylation of PMK3 could be a concentration dependent

phenomenon as we used more kinase in this assay (Fig 2B) that the earlier assay shown in

Fig 2A.

It was reported earlier that, active MKK4 is able to activate PMK3 by phosphorylation

(Nakata et al., 2005) reminiscent of similar findings in human where MKK6 phosphorylates

p38$\alpha$ (Han et al., 1996; Moriguchi et al., 1996a; Moriguchi et al., 1996b).  We wanted to find

out if the newly discovered feedback loop is specific for PMK3 with its downstream kinase

MAK2, or it could also participate in a similar feedback loop with its upstream MAP2K MKK4

as well. Similar assay as above was performed using recombinantly purified PMK3 and MKK4.

Phosphorylation level of PMK3 was much higher in presence of MKK4 (Fig 2C, lanes 4-6)

compared to PMK3 alone (Fig 2C, lanes 7-9). Interestingly, while MKK4 could efficiently trans-

phosphorylate its downstream kinase PMK3 as expected (Fig 2C, lanes 4-6), no feedback

phosphorylation from PMK3 to MKK4 could be discerned in this assay as MKK4 also showed

comparable high signal for autophosphorylation in the absence of PMK3 (Fig 2C, lanes 1-3;

compare lanes 1-3 and 4-6).

The above set of results brings out an unreported feedback phosphorylation loop

between a p38 MAPK and its cognate MAPKAPK (Fig 2D). PMK3 specifically engages in such

a feedback relationship with its downstream MAK2 but not with its upstream MKK4 (MAP2K)

*Figure 2*

**Figure 2: PMK3 engages in feedback phosphorylation with the downstream Kinase MAK2, but not the upstream kinase MKK4.**

**(A-C)** *In vitro* radioactive phosphorylation assays with recombinant PMK3 (MAPK), MAK2 (MAPKAPK) and MKK4 (MAP2K), elaborating on the feedback loop. (A) MAK2 phosphorylates PMK3 by a feedback mechanism in a time dependent manner. (B) The feedback phosphorylation loop between PMK3 and MAK2 is independent of the relative stoichiometry of the two constituent kinases. (C) This mechanism of signal transmission is specific for PMK3 and its downstream substrate MAK2 and does not occur for the upstream kinase MKK4. **(D)** A schematic illustration depicting the phenomenon of feedback phosphorylation between PMK3 and MAK2, but not between PMK3 and MKK4. **(E)** Bioinformatic modelling of the effect of feedback loop on the overall phosphorylation kinetics of the two kinases. The temporal evolution of relative concentrations of $Y_p$ (phosphorylated PMK3) and $Z_p$ (phosphorylated MAK2) are presented with respect to total kinase amount of each kinase for different values of feedback strengths ($A_{Z_p}$), which is a dimensionless measure of feedback strength and sensitivity. **(F)** Superimposition of the AlphaFold predicted structure of *C. elegans* PMK3 on Protein kinase A (PKA) structure. The conserved ATP binding Lys residue has been marked in both the structures.

(Fig 2D). In order to understand the effect of such feedback relationship, we modeled the

system as depicted in Fig 2E; wherein X denotes MKK4 (MAP2K), Y denotes PMK3 (MAPK)

and Z denotes MAK2 (MAPKAPK). $Y_p$ and $Z_p$ represent the phosphorylated versions of the

respective kinases and are considered active. For simplicity, we did not differentiate between

multiple phosphorylated versions, if any. We modeled the entire scheme by writing down

coupled ordinary differential equations. The model clearly captures the effect of feedback on

the phosphorylation kinetics and relative amounts of phosphorylated kinases (with respect to

the total kinase amount) (Fig 2E). The effect of feedback is accounted by considering a

dimensionless parameter $A_{Z_p}$, called feedback strength and sensitivity (for details see

materials and methods). Clearly, such feedback is advantageous to generate active pools of

those kinases than without feedback.

It is understood that activities of both kinases are required to propagate this feedback

phosphorylation loop between PMK3 and MAK2. However, it is not clear activity of which

kinase is mandatory for kickstarting this feedback loop: whether the upstream kinase (PMK3)

must phosphorylate the downstream kinase (MAK2) first or *vice versa* to make this feedback

loop operative. To analyze these possibilities, we took advantage of a mutant PMK3 where

invariant ATP binding Lys, K150 was replaced by Met giving rise to PMK3 K150M mutant

kinase. This ATP-anchoring Lys is conserved in all eukaryotic protein kinases that positions

the ATP in the kinase (Fig 2F) resulting in a productive phospho-transfer reaction. Mutation of

this invariant residue leads to abrogation of kinase activity, in essence such mutants are either

kinase dead or retain minimal activity, if any. We performed a similar *in vitro* phosphorylation

assay with PMK3 K150M and MAK2 using radioactive ATP. We observed that, the feedback

phosphorylation of the respective kinases did not occur (Fig 2G, lanes 5-8). Furthermore, no

autophosphorylation signal was observed for PMK3 when it was incubated with radioactive

ATP in the absence of MAK2 (Fig 2G, lanes 1-4). MAK2 underwent faint autophosphorylation

when incubated alone (Fig 2G, lanes 9-12), which was comparable to that in the reactions in

presence of its dead upstream kinase (Fig 2G, compare lanes 5-8 and 9-12). This experiment

proved that initiation and further propagation of the feedback phosphorylation loop is critically

dependent upon active PMK3. We surmise that active PMK3 is necessary and active MAK2

is not sufficient to initiate this feedback phosphorylation loop though it is understandable that

activities of both kinases would be required for the maintenance/propagation of the feedback

loop.

We have established the specific feedback phosphorylation relationship between

PMK3 and MAK2; however, it is unclear what could be the possible role of PMK3-

phopshorylation by MAK2. It is known that MAPKs require TxY phosphorylation to become

fully active and it is canonically done by its upstream dual specificity kinase MAP2K (here

MKK4). On the other hand, MAK2 which is placed downstream of PMK3 is annotated as a

Ser/Thr kinase in the UniProt database (EC number EC:2.7.11.1). In order to activate PMK3

fully, MAK2 must phosphorylate PMK3 at Thr as well as Tyr. As we lacked any specific

antibody to detect the phosphorylated TxY motif of PMK3, we tested the pan-tyrosine

phosphorylation of PMK3 by MAK2. We found that, MAK2 is capable of phosphorylating PMK3

on tyrosine residues (Fig 2H). This unexpected discovery identifies MAK2 as a dual specificity

kinase rather than a Ser/Thr kinase and raises the possibility that MAK2 might be capable of

activating PMK3 to ensure robust activation of such an important kinase.

**Mass spectrometric analyses of PMK3 and MAK2 phosphorylation:**

p38-MAPKs require phosphorylation of the TxY motif in their activation loop to unleash

their kinase-activity. Phosphorylation of both T and Y in the motif usher maximum activity while

phosphorylation of only T show much reduced activity and that of only Y renders the kinase

inactive (Zhang et al., 2008). In the previous sections we have seen that PMK3 and MAK2

engage in an unreported feedback phosphorylation relationship. It was also observed that,

phosphorylation on both PMK3 and MAK2 increased many folds when they were both present

in the reaction compared to the lone-kinases. However, it is unknown which sites in these

kinases get phosphorylated in such a situation. To this end, we performed high resolution LC-

MS/MS experiments after digesting a mixture of PMK3 and MAK2 with Trypsin after the

mixture was incubated with ATP. Resulting phospho-peptides were enriched after Trypsin-

digestion using Fe-NTA column before separation on a nano-LC. Both the kinases were found

to be heavily phosphorylated as 32 (MAK2-18, PMK3-14) phospho-peptides were detected.

We only show residues with probability of phosphorylation greater than 0.9 (Fig 3A-B). In

PMK3, six phosphorylated residues (T285, Y287, Y300, S347, T354, Y418) were located

within the kinase domain, while T107 was located just before the beginning of the kinase

domain, and S423 and S464 were situated after the kinase domain. In case of MAK2, three

residues (S148, T173, Y180) were located within the kinase domain, of which T173 and Y180

are situated in the activation loop of the kinase prior to the APE motif. No residue prior to the

kinase domain at the N-terminus was found to be phosphorylated in MAK2. T285, S290 and

S313 after the kinase domain were found to be phosphorylated of which S313 is positioned

within the nuclear export signal (NES) of MAK2. The TxY motif of PMK3 (T285-x-Y287) was

found to be phosphorylated in the reaction mixture strongly pointing to the ability of MAK2 to

activate PMK3 by a feedback mechanism. This result strongly suggests that activation of a central kinase like PMK3 can be achieved by both upstream kinase MKK4 (canonical activation) and/or downstream kinase MAK2 (noncanonical feedback activation).

**Figure 3: Identification of phosphorylation sites on PMK3 and MAK2.**
**(A-B)** LC-MS/MS analysis reveals the amino acid residues phosphorylated on both these kinases in the feedback loop. (A) Right panel: Domain organization of PMK3 showing the identified phosphorylated residues. The residues have been colour coded as per the STY phosphorylation probability scale. Left panel: A zoomed in view of the AlphaFold predicted 3-D structure of PMK3, with the highlighted phosphorylation sites. (B) Right panel: Domain organization of MAK2 showing the identified phosphorylated residues. The residues have been colour coded as per the STY phosphorylation probability scale. Left panel: A zoomed in view of the AlphaFold predicted 3-D structure of MAK2, with the highlighted phosphorylation sites. **(C)** Distribution of the phospho-sites on distinct faces of the kinases points the dynamic nature of the PMK3:MAK2 complex with different possible modes of binding.

For both PMK3 and MAK2, we have depicted the phosphorylation sites in the context of the individual 3D-structures of these kinases. No experimentally derived three-dimensional structure of PMK3 or MAK2 is available in the database. For structural analyses we took

AlphaFold2 predicted complex of PMK3 and MAK2

**Figure S2:** Ribbon representation of the AlphaFold2 predicted complex of PMK3 and MAK2. The phosphorylated residues identified by mass-spectrometric analyses have been highlighted (red and purple) on both the kinases.

advantage of the AlphaFold-predicted structures (Jumper et al., 2021) of these kinases. Closer

look at the positions of phosphorylation sites on the 3D-structures of PMK3 and MAK2

revealed that they were dispersed on distinct faces of the kinases (Fig 3A- B). We further

wanted to understand the implications of such distribution of phosphorylation sites in terms of

the structure of the PMK3:MAK2 complex. However, no experimentally-derived structure of

this complex is available in the literature. Firstly, we superimposed AlphaFold-derived

structures of PMK3 and MAK2 on to the experimentally derived structure of the human

p38$\alpha$:MK2 complex. When Phosphorylation sites on both PMK3 and MAK2 were highlighted

it became clear that it was impossible for either kinase to access all the phosphorylation sites

on the other kinase from this single pose (Fig 3C, left and right panels). Neither could these

kinases autophosphorylate themselves at sites far from the respective active sites. We also

created a model of the PMK3:MAK2 complex using AlphaFold2 and highlighted the

phosphorylation sites (Fig S2). It was evident that this pose would not suffice to explain the

distribution of phosphorylation sites on these two kinases either through trans-phosphorylation

by each other or by self-phosphorylation. We surmised that PMK3:MAK2 complex is dynamic

in nature that may exploit multiple mode of binding giving rise to an ensemble of

conformations, and experimentally derived pose of the human p38$\alpha$:MK2 complex or

AlphaFold2-derived PMK3:MAK2 complex are insufficient to capture the dynamicity of the said

complex.

**Sequence and structural analyses of PMK3 and MAK2:**

Primary sequence of PMK3 was aligned with the four human p38 isoforms to reveal

that PMK3 shared highest sequence similarity with p38α (Fig S1B). We also subjected primary

sequence of MAK2 to sequence alignment with three human MAPKAPKs, viz. MK2, MK3 and

**Figure S3**

360 **Figure S3: (A)** Left panel: Multiple sequence alignment (MSA) of MAK2 with the human
361 MAPKAPKs MK2, MK3 and MK5. Right panel: The percent identity matrix shows that MAK2
362 shares more than 50% sequence similarity with MK2 and MK3. **(B-C)** Superimposition of the
362 ED and CD domains of PMK3 and human p38α. The respective sequence alignments have
363 been shown in the lower panel. The changes in the nature of amino acids have been
highlighted in boxes. **(D)** Superimposition of the docking sites of MAK2 and MK2 reveals that
the involved residues are less conserved in MAK2 than in the human MKs.

MK5 (Fig S3A). It was found that, MAK2 shares more than 50% identity with two human

MAPKAPKs, MK2 and MK3 (Fig S3A). In the context of binary complex between p38α and

MK2, we wanted to glean into the complex between PMK3 and MAK2. We superimposed the

respective kinases on the existing p38α:MK2 complex (pdb id: 2oza) and analyzed the regions

known to contribute to such complex formation. On the MAPK, there are two regions known

as CD and ED domains that contribute majorly to binding with the MAPKAPKs (Tanoue et al.,

2000; Tanoue et al., 2001). Fig S3B and S3C depict the superposition of ED and CD domains,

respectively along with their sequence alignment. Residues in the ED domain of these two

largely conserved with the exception of N159 of p38α changed to another polar residue T261

in PMK3, and C162 of p38α changed to S264 in PMK3 that merely changes -SH to -OH. In

the CD domain, however, changes are more drastic; acidic D313 of p38α changed to

hydrophobic L424 in PMK3 and polar, phosphorylatable Y131 of p38α changed to

hydrophobic, phospho-ablative F422 in PMK3. When we turned our attention to the p38-

docking site (R/K–R/K–$X_{10}$–R/K–R/K–R/K–R/K–R/K), we realized that this region of MAK2 is

not so conserved as compared to its human counterparts MK2 and MK3 (Fig S3D). For

example, $2^{nd}$ R/K (K374 of MK2) and last R/K (K389 of MK2) have been changed to S325 and

G340, respectively in MAK2 (Fig S3D). Such changes in the interacting residues in the partner

kinases in the human and nematode raises the possibility that the ensuing PMK3:MAK2 may

not be exactly the same as the p38α:MK2 complex and they may differ in spatial arrangements

as well as affinity.

In the previous section we found out that the existing experimentally derived structural

models of human p38:MK2 structures and predicted PMK3:MAK2 structures were not

adequate to capture the nuances of the said complex of the nematode origin. We also found

out that the interacting residues are not entirely conserved in the nematode kinases. We

further noticed that PMK3 contains a long (~90aa) insert at the N-terminus before the kinase

domain that is absent in the human p38 isoforms. MAK2, on the other hand does not contain

any long N-terminal insertion before the beginning of the kinase domain that is present in MK2

and MK3 but not in MK5. MAK2, however has a highly charged C-terminal region beyond the

MAPK-docking sequence that is absent in MK2 or MK3. Both the N-terminal extension in

PMK3 and C-terminal extension in MAK2 are largely unstructured.

Such differences in their amino acid compositions prompted us to extensively analyze

those sequences using web-based tools to gain further insights on their physico-chemical

properties as presence of long IDRs entail possibility of condensate formation through liquid

liquid phase separation. We subjected both PMK3 and MAK2 sequences for such analyses

using multiple web-based tools to better understand the properties and outcomes of those

inserts before or after the well folded kinase domains present in them. We primarily used

MolPhase, FuzDrop, IUPred3, PONDR and FoldIndex webservers (Erdos et al., 2021; Hatos

et al., 2022; Liang et al., 2024; Prilusky et al., 2005). In Fig 4A, results of PMK3 sequence

analyses on MolPhase and FuzDrop are shown along with the AlphaFold-predicted structure colored according to the pLDDT scores that informs about the confidence of the prediction,

**Figure 4: PMK3 and MAK2 harbor unstructured, disordered regions and propensity to undergo phase separation**

**(A)** Left panel: MolPhase analysis of the primary sequence of PMK3 shows that the kinase consists of an intrinsically disordered region (IDR) at its N-terminus. Right panel: FuzDrop prediction shows the droplet promoting regions (DPRs) along with the aggregation hotspots in the PMK3 sequence. The AlphaFold predicted structure of PMK3 has been shown. The structural elements have been colour coded according to the pLDDT score that signifies the confidence of prediction. The data shows that the N-terminus of PMK3 forms a disordered region with a pLDDT score of less than 50. **(B)** Left panel: MolPhase and analysis of the primary sequence of MAK2 shows that the kinase consists of an intrinsically disordered region (IDR) in the middle (217-229) and at the C-terminus Right panel: FuzDrop prediction shows the droplet promoting regions (DPRs). The number of aggregation hot spots in the MAK2 sequence is distinctly lower than those found in PMK3.The AlphaFold predicted structure of MAK2 has been shown. The structural elements have been colour coded according to the pLDDT score that signifies the confidence of prediction. The data shows that the C-terminus of PMK3 forms a disordered and unstructured region with a pLDDT score of less than 50.

rest of the predictions are shown in Fig S4A. Similarly, prediction results for MAK2 are shown in Fig 4B and Fig S4B. It was observed in both cases, MolPhase and FuzDrop predictions correlated well with the AlphaFold prediction confidence score, i.e., pLDDT score (Jumper et al., 2021). For PMK3, the pLDDT score was lowest at the N-terminus prior to the kinase domain; the same region was predicted to be intrinsically disordered by each of the predictive

424    tools employed (Fig 4A and S4A). Similarly, MAK2 C-terminus beyond the kinase domain

**Figure S4**

showed lowest confidence in the AlphaFold prediction that was also found to be intrinsically disordered by the predictive tools used in this study. Presence of intrinsically disordered regions (IDRs) bestow their parent protein with multivalency of interaction (Babu et al., 2011; Wright and Dyson, 2015). Since both PMK3 and MAK2 are found to contain long IDRs, it is possible that they would be capable of interacting with each

**Figure S4: (A-B)** IUPred3, PONDR and FoldIndex webserver-based predictions of PMK3 (A) and MAK2 (B) primary sequences.

other in multiple ways giving rise to an ensemble of intermolecular poses. It will posit residues

of each kinase with respect to the active sites of the other kinase making phosphorylation of

residues on opposite faces of the kinases plausible. Presence of IDRs also gives rise to the

possibility of formation of molecular condensates through liquid liquid phase separation

(LLPS). MolPhase score for PMK3 and MAK2 was 0.995 and 0.939, respectively strongly

suggesting that these proteins are likely to form condensates through LLPS.

**MAK2, but not PMK3, undergoes liquid-liquid phase separation:**

Analyses of the primary and AlphaFold predicted structure of MAK2 revealed the

presence of a long intrinsically unstructured/disordered region (IDR) at the C-terminus of the

**Figure 5: MAK2 undergoes liquid- liquid phase separation (LLPS) to form condensates, whereas PMK3 forms aggregates.**

*In vitro* droplet formation assays. **(A)** Fluorescein labelled MAK2 was incubated with varying concentrations of PEG-8000 for different time periods and imaged under the microscope. MAK2 undergoes phase separation to form the round droplets under both the conditions. Images are representative of three independent experiments. Scale bar is 10µm. **(B)** A MAK2 construct with a GFP tag at its C-terminus (MAK2-GFP) could also successfully form these condensates through LLPS at the different PEG concentrations used. Images are representative of three independent experiments. Scale bar is 10µm **(C)** F-MAK2 and MAK2-GFP were subjected to phase separation in presence of increased amount of NaCl, wherein the droplet formation was significantly inhibited in both the cases at 600mM NaCl. Images are representative of two independent experiments. Scale bar is 8µm (upper panel) and 10µm (lower panel) respectively.

**(D)** FRAP analysis on the phase separated MAK2-GFP condensates at different PEG concentrations (left). Scale bar is 10μm.The fluorescence recovery in each case was followed up to 60 seconds post bleaching and the normalized fluorescence intensity was plotted against time (right). The data values are shown as mean±s.d. of normalized fluorescence intensity values from three independent measurements (n=3). **(E)** *In vitro* droplet formation assays with fluorescein labelled PMK3 show that PMK3 forms aggregates at different protein concentrations in the presence of 10% PEG-8K. Images are representative of three independent experiments. Scale bar is 10μm. **(F)** PMK3 forms aggregates even in the presence of chaperone Hsp90 or a non-specific interacting protein, BSA. Scale bar is 10μm.

protein with high probability of forming liquid droplets. LLPS-mediated condensate formation is a well-established mechanism to regulate a number of biological processes (Alberti and Dormann, 2019; Banani et al., 2017; Boeynaems et al., 2018; Franzmann and Alberti, 2019; Hyman et al., 2014; Peeples and Rosen, 2021; Posey et al., 2018). To test if MAK2 indeed forms droplets through liquid-liquid phase separation (LLPS) we prepared recombinant MAK2 labeled with Fluorescin (F-MAK2) and subjected it to treatment with varying concentration of PEG 8000 to drive phase separation at a MAK2 concentration of 10uM and 150mM NaCl. We found that MAK2 forms condensates through LLPS at concentration of PEG 8% and above (Fig 5A). It was observed that, with the increase in PEG concentration both the number and size of the condensates increased. At 12% PEG, the condensates seemed to be transitioning from a liquid-like state to an arrested state. To further confirm that LLPS in MAK2 was not due to the specific labeling of the protein with Fluorescin, we generated and purified a MAK2 construct containing GFP at its C-terminus (MAK2-GFP). MAK2-GFP protein also underwent LLPS to form condensate in a range of PEG concentration ranging from 8-12% (Fig 5B) (Chauhan et al., 2024). Next, we checked the effect of protein concentration on LLPS by treating different concentration of MAK2-GFP with a fixed concentration of PEG (10%) (Chauhan et al., 2024). This assay revealed that size of the condensates increased as protein concentration was increased from 6uM to 10uM or more (Fig S5A). To assess the liquid like properties of the condensates we performed FRAP experiments at different concentrations of PEG (Taylor et al., 2019). It was observed that the fluorescence fully recovered within 60s of bleaching at 8% PEG while it was gradually arrested as the PEG concentration was increased to 10% and 12% (Fig 5D). To assess if LLPS in MAK2 was irreversible or reversible in our experimental conditions, we subjected both F-MAK2 and MAK2-GFP to condensate formation through LLPS at different concentrations of NaCl (Krainer et al., 2021; Posey et al., 2018; Sanulli and Narlikar, 2021). It was observed that, LLPS of MAK2 was severely compromised at higher concentration of NaCl both in case of F-MAK2 and MAK2-GFP (Fig 5C). These observations indicate that MAK2 LLPS is a reversible process energetics of which is likely dominated by electrostatic interactions (Posey et al., 2018; Sanulli and Narlikar, 2021).

As mentioned earlier, analysis of PMK3 sequence using web-based tools also predicted to contain long droplet promoting regions at its N-terminus, and a small region at the

*Figure S5*

C-terminus. We wanted to check if PMK3 also formed droplets through LLPS. Recombinantly purified PMK3 was labeled with Fluorescin (F-PMK3). Different concentrations of F-PMK3 was incubated with different concentrations of PEG 8K to check for LLPS. It was observed that, F-PMK3 formed aggregates instead of phase-separated droplets at the protein

527
528  **Figure S5: (A)** Concentration dependent phase separation of MAK2-GFP in presence of 10%
529  PEG. MAK2-GFP was mixed with 10% PEG at different protein concentrations up to 15µM and
      imaged under the microscope to check for visible droplet formation. Scale bar is 10µm. **(B)** F-PMK3
530  undergoes aggregation at different protein concentrations in the presence of 12% PEG-8K. Scale
      bar is 10µm.

concentrations tested in the same conditions that lead to LLPS-mediated droplet formation in

MAK2 (Fig 5E and S5B). Furthermore, this aggregation of F-PMK3 could not be prevented by

the chaperone HSP90 or a non-interacting non-specific protein, BSA (Fig 5F).

**MAK2 prevents aggregation and drives LLPS of PMK3:**

In the previous section we have seen that, PMK3 protein is aggregation prone that was

refractory to the presence of HSP90 or a non-interacting protein. We also observed that PMK3

and MAK2 participate in a hitherto unreported feedback phosphorylation loop. Furthermore,

MAK2 undergoes LLPS in presence of molecular crowders at different protein and PEG

concentrations. Taken together, we sought out to investigate if MAK2 could prevent the

aggregation of PMK3 and lead to LLPS-mediated droplet formation in PMK3. To this end, we

took fixed concentration F-PMK3 and incubated it with 10% PEG 8K in absence or presence

of increasing concentration of unlabeled MAK2, and monitored F-PMK3 droplet formation at

different time interval. Interestingly, MAK2 was able to prevent aggregation of PMK3 and drove

**Figure 6: MAK2 mediated phase separation prevents the aggregation of PMK3.**

**(A)** F-PMK3 was mixed with unlabelled MAK2 at two different concentrations in presence of 10% PEG and imaged at 10 minutes and 2 hours respectively. In presence of MAK2, PMK3 undergoes liquid-liquid phase separation to form globular droplets instead of aggregates. Images are representative of two independent experiments. Scale bar is 10μm. **(B)** MAK2 and PMK3 co-localize within the same phase separated droplets. MAK-GFP (green) and Alexa 594 labelled PMK3 (red) were mixed together in presence of varying concentrations of PEG-8K (8-12%) and imaged at two time points. Merged (yellow) images show the co-localization of the two kinases within a single droplet. At 3 hours, the droplets exhibit a tendency to form aggregates with an increase in PEG concentration. Images are representative of two independent experiments. Scale bar is 8μm. **(C)** In presence of MAK2-GFP, PMK3 undergoes LLPS even in the absence of any crowding agent or as low as 1% PEG-8K. Scale bar is 8μm.

droplet formation in PMK3 through LLPS (Fig 6A). The above experiment proved that presence of MAK2 hinders aggregation pf PMK3 and induces LLPS-mediated droplet formation. Next, we asked whether this is a bystander-effect of MAK2 on PMK3. To this end, we wanted to see if the same droplets contain both MAK2 and PMK3. To distinguish between

the two under the microscope, we used MAK2-GFP and PMK3 was labeled Alexa Fluor 594

(AF-PMK3) for this study. AF-PMK3 and MAK2-GFP were mixed together and incubated in

presence of increasing concentration of PEG 8K for different time intervals before imaging.

We observed that, AF-PMK3 and MAK2-GFP colocalized in the same droplets in all the PEG

concentrations tested as early as 10 mins post incubation (Fig 6B). At 3 hours post incubation,

droplets showed tendency to aggregate with increasing concentration of PEG (Fig 6B).

Interestingly, AF-PMK3 and MAK2-GFP complex formed droplets through LLPS at PEG

concentration as low as 1-2%, very few droplets were seen even when no PEG was present

(Fig 6C).

**Effect of auto- and feedback phosphorylation on LLPS of the MAK2-PMK3 complex:**

It was evident from our biochemical analyses that MAK2 and PMK3 participate in a

feedback phosphorylation (trans-) loop whereas they undergo very little, if any, self-

phosphorylation when incubated alone with ATP. We wanted to see how these self- vs. trans-

phosphorylation modulate LLPS-mediated droplet formation and *vice-versa*. Firstly, we

wanted to compare the pan-phosphorylation abilities of PMK3 and MAK2 in LLPS-inducing

conditions. We employed two different reaction conditions, sets A and B, as outlined in Fig S6

(see materials and methods for further details). In set A, PMK3 was incubated alone in

presence of 10% PEG 8K that is known to cause aggregation of the kinase, and then MAK2

was added. In this condition, only the fraction of PMK3 that is available in solution or

condensate would serve as the kinase to phosphorylate MAK2 and as the substrate to be

phosphorylated by MAK2. In set B, PMK3 and MAK2 were incubated together in 10% PEG

8K. As we know, the PMK3:MAK2 complex will form condensate and a larger fraction of PMK3

should be biochemically available to serve as the kinase or the substrate. In our laboratory we

developed a non-hazardous, non-radioactive technique to detect this pan-phosphorylation

(*Borar et. al., unpublished data, manuscript in preparation*) using ATP-γ-S and PNBM followed

by detection of the p-thio-ester by immunoblotting using a specific antibody (Adler et al., 2013).

As expected, it was observed that in case of set A, phosphorylation signal for PMK3 was much

less as not much protein was available in solution/condensate even though catalytic amount

of PMK3 was available to allow phosphorylation of MAK2 (Fig 7A, left panel, lanes 1-3). In set

B, where PMK3:MAK2 complex was allowed to form the condensate both proteins underwent

significant phosphorylation (Fig 7A, left panel, lanes 4-6). We also checked if MAK2 was able

to phosphorylate PMK3 on tyrosine(s) when both were present in the condensate (set B).

Indeed, in the PMK3:MAK2 condensate MAK2 was able to phosphorylate tyrosine residue(s)

on PMK3 (Fig 7A, right panel) as was observed when both were present in solution (Fig 2H).

Next, MAK2-GFP was treated with ATP (200μM) and the mixture was incubated with crowding

agent and imaged at different time interval. When compared with the same protein in absence

**Figure 7: Effect of auto- and feedback phosphorylation on LLPS of the MAK2-PMK3 complex.**

**(A)** MAK2 phosphorylates PMK3 on tyrosine residues within the condensates. PMK3 and MAK2 were incubated as per the reaction scheme in Figure S6, resolved by SDS-PAGE and probed using anti thio phosphate ester antibodies to detect the pan phosphorylation or anti p-tyrosine antibodies to detect phosphorylation at the tyrosine residues of the two kinases. Experiments were performed thrice with similar results.

**(B)** Effect of auto phosphorylation on the LLPS of MAK2. MAK2-GFP undergoes phase separation in the presence of ATP i.e. auto phosphorylation has no effect on the ability of MAK2 to form liquid condensates. Scale bar is 8µm. **(C)** Auto phosphorylated PMK3 forms aggregate in presence of 8% PEG-8K. Alexa 594 labelled PMK3 was used in this assay. Scale bar is 8µm. **(D)** Effect of trans-phosphorylation on PMK3: MAK2 condensates. Scale bar is 8µm. In presence of ATP, the PMK3: MAK2 droplets maintained their globular look even at 3 hours post incubation. (E) A graphical model depicting mutual relationship and signal transmission through PMK3 and MAK2. PMK3, a neuronal p38-MAPK is activated by its downstream MAPKAPK MAK2 without requiring the presence of canonical activator MAP2K, MKK4. MAK2 increases bioavailability of aggregation prone PMK3 by LLPS-driven condensate formation.

### Figure S6

of ATP in the same assay condition they behaved similarly as to form droplets through LLPS (Fig 7B). We subjected AF-PMK3 to the same assay and found that presence of ATP did not change the fate to PMK3 to undergo aggregation as the AF-PMK3 alone in presence of the crowding agent (Fig 7C). Together these results inform us that autophosphorylation, if any, or

in other words mere presence of ATP is not sufficient to change PMK3's tendency to aggregate or MAK2's ability to from condensates through LLPS. Next, we incubated the MAK2-GFP and AF-PMK3 complex with crowding agent in presence and absence of ATP. MAK2:PMK3 complex underwent droplet formation through LLPS both in absence (Fig S6B), as was already seen, and presence of ATP (Fig 7D). Interestingly, we noticed that after prolonged incubation the complex also showed tendency to aggregate in absence of ATP but such a tendency to aggregate was not apparent in presence of ATP.

**Figure S6: (A)** Outline of the reaction schemes followed for the *in vitro* LLPS and their subsequent Western blot analyses using anti thio-phosphate ester and anti p-tyrosine antibodies. **(B)** Condensate formation of the PMK:MAK2 complex through LLPS in absence of ATP.

In presence of ATP the droplets generated through LLPS maintained their rounded-looks even

after 3hrs post-incubation. These results show that PMK3 might require the presence of MAK2

even in the presence of ATP that is abound in cellular milieu to remain bio-available in the

form of condensates along with MAK2, and that MAK2 is able to activate PMK3 in the

condensate state as well.

**Discussion:**

MAPK signaling modules have remained in the forefront of signal transduction

research for many years. A flood of research articles employing biochemical, structural,

genetics and other approaches helped the field to understand the importance of these kinases

and their regulatory mechanisms in great details (Cargnello and Roux, 2011; Chang and Karin,

2001; Goldsmith et al., 2010). Studies of MAPKs in multicellular (mammalian) and unicellular

(yeast) organisms show that they follow a unidirectional path starting from a MAP3K that

activates a cognate MAP2K to activate its downstream MAPK upon encountering extracellular

stimuli. Basic structure and skeleton of this three-kinase module is preserved wherein

MAP2Ks are dual specificity kinase required to phosphorylate the conserved TxY motif on the

activation loop of the MAPKs essential for the MAPKs to realize their full scale of activity

(Zhang et al., 2008). The three-kinase MAPK modules exhibit their roles either by directly

phosphorylating effector-substrates (like transcription factors) or by activating a downstream

kinase, MAPKAPK, by phosphorylation that ultimately carry out the phosphorylation of the

effector-substrates (Cargnello and Roux, 2011). This makes the module a four-kinase MAPK

module. Role of such MAPK-MAPKAPK duo are very well studied and well established in

literature and have been heavily implicated in mammalian biology especially in the realm of

immune signaling (Gaestel, 2006; Menon et al., 2017; Menon et al., 2018). Heterodimeric

p38$\alpha$:MK2 complex is known to orchestrate modulation of proinflammatory cytokine

productions (Menon and Gaestel, 2018). The complex is resident in the nucleus in resting

cells however migrates to the cytoplasm in response stimuli (Ben-Levy et al., 1998). p38$\alpha$

lacks NES however is transported to the cytoplasm in complex with MK2 that has an NES.

MK2-NES remains masked in its inactive form, phosphorylation (Thr334 in human) of NES by

p38$\alpha$ unmasks it (Ben-Levy et al., 1998; Engel et al., 1998; Meng et al., 2002).

As mentioned earlier, MAPK pathways represent one of the most ancient eukaryotic

signal transduction pathways throughout evolution. It is thus not surprising that they yet hold

many mysteries even though a great deal is already unearthed. For example, in *C. elegans*

PMK3 and MAK2 are greatly implicated in the axon regeneration pathway downstream of

DLK1 (MAP3K) and MKK4 (MAP2K) (Hammarlund et al., 2009; Yan et al., 2009). The DLK1

pathway is negatively regulated by the E3 ubiquitin ligase RPM-1/Highwire/Phr in worm, fly

and mice in order to stabilize the synaptic connections (Chang and Balice-Gordon, 2000;

Lewcock et al., 2007; Nakata et al., 2005; Schaefer et al., 2000). PMK3 and MAK2 were shown

to interact by yeast two hybrid assay and in a co-immunoprecipitation assay performed in

HEK293T cells (Yan et al., 2009).  As expected PMK3 was able to phosphorylate MAK2 *in*

*vitro.* We found that, PMK3 tends to form large oligomeric forms in solution along with low

molecular weight fractions and that the oligomeric form is incapable of activating MAK2 by

phosphorylation. PMK3 phosphorylates MAK2 at T173 and Thr285 in addition to other

residues. It was shown that phospho-ablative double mutant of MAK2 (T173A T285A) failed

to exert its role in axonal regeneration in nematode (Yan et al Cell 2009). Thr285 in MAK2 is

equivalent to Thr334 in human MK2 located in the NES region, phosphorylation of which has

been well established in the activation and nuclear export of MK2 and p38$\alpha$:MK2 complex in

human to exert their signaling roles. Surprisingly, we found that the activated MAK2

phosphorylates PMK3 in return at multiple locations including the TxY (T285-x-Y287) motif

essential for PMK3 to attain its highest-activity state. This observation is unreported in the

literature, which proposes that MAK2 is actually a dual specificity kinase and not a Ser/Thr

kinase. Identification of phosphorylation site not only ascribes the novel specificity of MAK2, it

also provokes us to propose this newly found feedback loop as a mechanism that ascertain

the activation of a critical kinase like PMK3 by its downstream kinase in a situation when the

upstream MAP2K is absent/inactive. Of note, MK2 (mammalian counterpart of MAK2) has

been reported to participate in a feedback relationship with RIPK1 that downregulates RIPK1

activity (Menon et al., 2017; Menon et al., 2018). We speculate that the feedback loop either

may act as a fail-safe mechanism to activate PMK3 in a situation when MKK4 is either absent

or inactivated or it may help gain quicker and more robust response of this pathway as and

when required. Since DLK-1 signaling is used in multiple phenomena such as axon

regeneration (Hammarlund et al., 2009), degeneration (Asghari Adib et al., 2018; Gerdts et

al., 2016), and synaptic pruning (Asghari Adib et al., 2024) in response to nervous system

injury, it might need a fail-safe and seamless mechanisms for robust activation and faithful

transmission inside the cell. A critical dependence on two different P38 MAPK cascades

involving DLK-1 and MLK-1 for axonal regeneration, indicates a robust cross-talk between

parallel signaling kinases in neuronal injury response (Nix et al., 2011). Future course of

studies will shed light on the scenario in the cellular context in presence and absence of MKK4.

Phosphorylation mediated regulation of kinases is a common theme in kinase biology.

Distribution of phosphorylation sites on either kinase in this study suggested that the existing

structural models with similar kinases from other organisms were inadequate to capture the

possible modes of binding between PMK3 and MAK2 to enable such distribution of

phosphorylation sites. In addition, both these kinases contained IDRs and showed theoretical

propensity to form droplets. These observations led us to hypothesize that droplet/condensate

formation through LLPS might be a plausible mechanism to accommodate the ensemble

conformational space of this complex. In many cases, kinases have been found to depend
upon scaffolding proteins to undergo phosphorylation by a trans-kinase or to attain a critical
local concentration self-phosphorylation. Activation of IKK-complex is a classic example of
scaffolding protein (NEMO) dependent kinase (IKK) activation. It was recently shown that IKK-
complex undergo condensate formation through LLPS in the signaling context in a NEMO-
dependent manner (Du et al., 2022). Regulation of kinase function through LLPS-driven
condensate formation have been reported in many other cases as well (Lin et al., 2022; Lopez-
Palacios and Andersen, 2023; Sang et al., 2022; Schlutermann et al., 2021; Zhang et al.,
2020; Zhu et al., 2023). However, to the best of our knowledge, LLPS-mediated formation of
kinase-condensate that relies upon the presence of a trans-phosphorylating kinase is not
known. Here, for the first time we report that an aggregation-prone p38 MAPK (PMK3) is kept
bio-available by its activating downstream kinase MAPKAPK (MAK2) by formation of
condensates through LLPS. Furthermore, this LLPS-mediated condensate formation leads to
productive association between two kinases where the feedback phosphorylation relationship
is functional unlike the inactive oligomeric state. Interestingly, it has been shown recently that
human MKK6:p38$\alpha$ is also highly dynamic in nature and the disordered N-terminal linker of
the MAP2K (MKK6) plays critical role in determining specificity of the MAPK to be activated
by phosphorylation (Juyoux et al., 2023). This report and our observations provoke us to
speculate that MAPK activation across species might occur through a highly dynamical
engagement of the MAPK with its upstream (MAP2K) or downstream (MAPKAP) kinases with
ensuing conformational plasticity.

Together, we propose a hitherto unreported regulatory mechanism in kinases wherein
a critical signaling kinase is kept bio-available through LLPS by its downstream substrate
kinase that in turn activate the upstream kinase through a feedback phosphorylation loop (Fig
7E). Future course of studies will shed light whether this is a rare, kinase-specific mechanism
active in a particular organism or a more wide-spread aspect in kinase activation and
regulation.
770

**Materials and Methods:**
**Cloning of expression constructs:**
For large scale protein purification, the DNA encoding full length *C. elegans* PMK3 was
cloned within the EcoRI and XhoI restriction sites of a modified pET24d vector (pET24d-
HisTEV) designed to incorporate a N-terminal 6X His tag in the recombinant protein, followed
by a TEV protease cleavage site to remove the tag, if required. MAK2 was cloned within the
BamHI and SalI sites of pET24d-HisTEV. This plasmid consists of a kanamycin resistance
gene, a T7 promoter and a lacI coding sequence that allows for the IPTG-induced expression
of the cloned DNA. For the expression of GFP tagged MAK2, the insert was ligated to a

modified pET24d-HisTEV vector with a C-terminal GFP tag. The kinase dead PMK3 (K150M)
mutant was generated by site directed mutagenesis using Pfu DNA polymerase (Agilent). For
the purification of 6X His-MKK4 from Sf9-baculovirus expression system, the full-length
protein from *C. elegans* was cloned in pFastBacHT B vector at BamHI and XhoI restriction
sites. All the restriction enzymes and T4 DNA ligase were purchased from New England
Biolabs and ThermoFisher Scientific respectively.

**Culture growth conditions**

For recombinant protein expression, the plasmid constructs were transformed into *E.
coli* Rosetta 2 (DE3) strain. The transformants were selected on LB-agar plates supplemented
with 50μg/ml kanamycin. An overnight saturated culture of the transformed cells was used to
inoculate fresh Luria Bertani (LB) media supplemented with 50ug/ml of antibiotic kanamycin
(secondary culture) and incubated at 37°C up to an $OD_{600}$ of 0.5-0.6. The cells were then
induced with 0.25mM IPTG and grown overnight for 18-20 hours at 16°C, harvested by
centrifugation at 4500g and stored in -80°C until further processing.

**Protein purification from bacterial expression system**

For purifying the 6X His tagged recombinant proteins, bacterial cell pellet with
overexpressed protein of interest was re-suspended in a lysis buffer composed of 50mM Tris
pH 8.0, 200mM NaCl, 10mM imidazole, 10% glycerol, 5mM β-Me and 1mM freshly added
PMSF. Cells were lysed on ice using an ultra-sonic processor (Cole Parmer) and the crude
cell extract was clarified by centrifugation at 15000g for 1 hour. The supernatant was collected
and mixed with pre-equilibrated Ni-NTA agarose beads (Qiagen) at 4°C for 2 hours in batch
mode. The resin was washed with 10 CV (column volume) lysis buffer and 20 CV wash buffer
with 25mM imidazole. The bound protein was eluted with a buffer containing 50mM Tris pH
8.0, 200mM NaCl, 5% glycerol, 250mM imidazole, 5mM β-Me and 1mM PMSF. The protein
fractions were analysed by SDS-PAGE and stained with Coomassie Brilliant blue G-250
(Merck). The fractions with the desired protein were pooled together, filtered through a 0.22μm
filter and loaded on to a preparative HiLoad 16/600 Superdex 200 pg column (GE Healthcare),
connected to an ÄKTApure chromatography system (GE Healthcare), equilibrated with a
buffer consisting of 50mM Tris pH 8.0, 100mM NaCl, 3% glycerol, 5mM β-Me and 2mM EDTA.
The peak fractions were collected and run on SDS-PAGE. The proteins were further
concentrated, if required, using a 30kDa cut-off centrifugal protein concentrator (Vivaspin,
Sartorius). The final protein concentration was estimated using a microplate
spectrophotometer (Multiskan SkyHigh, Thermo Scientific) and the fractions were stored in -
80°C in small aliquots.

**Protein purification from Sf9-baculovirus expression system**

His-MKK4 was overexpressed in and purified from Sf9 (Thermo Scientific) cells.
Recombinant bacmid generation, transfection of the insect cells, generation and amplification

of recombinant baculovirus stock were done following the Bac-to-bac Baculovirus Expression

System user's manual (Thermo Scientific, MAN0000414). For large-scale purification, Sf9

cells in suspension at a cell density of 1X $10^6$ cells/ml were infected with P3 generation

baculoviruses and incubated at 27°C for 60-72 hours post-infection under shaking condition.

Cultures were harvested by centrifugation at 1200g for 30 minutes at 4°C, pellets were washed

with 1X TBS with 2mM EDTA and stored in -80°C. For protein purification, the cell pellets were

thawed, re-suspended in a lysis buffer containing 50mM Tris pH 8.0, 200mM NaCl, 10mM

imidazole, 10% glycerol, 5mM β-Me, 1mM PMSF and 1X protease inhibitor cocktail (Sigma-

Aldrich) and lysed on ice using sonication. The protein of interest was purified by Ni-NTA

affinity chromatography (as described above), followed by size exclusion chromatography

using a preparative HiLoad 16/600 Superdex 200 pg column (GE Healthcare) column. The

protein was eluted in a buffer containing 50mM Tris pH 8.0, 100mM NaCl, 3% glycerol, 5mM

β-Me and 2mM EDTA, concentrated using a centrifugal protein concentrator and stored in -

80°C in small aliquots.

***In vitro* radioactive kinase assays**

*In vitro* radioactive kinase assays were performed to determine the functional status of

the purified recombinant kinases and to understand their mutual interactions. γ$^{32}$P-ATP was

used as the phosphor donor to detect the auto and trans phosphorylation events. Reactions

were carried out with the purified kinases, 200µM cold ATP mixed with γ$^{32}$P-ATP (hot ATP),

in presence of a kinase assay buffer composed of 20mM HEPES pH 7.7, 20mM β-

glycerophosphate, 100mM NaCl, 100µM sodium orthovanadate, 10mM $MgCl_2$, 10mM sodium

fluoride, 1mM PMSF and 2mM DTT (freshly added). The purified myelin basic protein (MBP)

used as a generic substrate was purchased from Sigma-Aldrich. All the reactions were

incubated at 25°C, up to different time intervals, terminated with 4X SDS protein loading dye,

boiled for 5 minutes at 100°C and resolved by SDS-PAGE. To confirm the amount of each

protein in the respective samples, the polyacrylamide gels were stained with Coomassie dye.

The Coomassie stained gels were subsequently dried using a gel drying equipment (Biorad

Model 583) and placed inside an exposure cassette (GE Healthcare). The phosphor signal

from each gel was captured on a phospho imager screen (GE Healthcare) and scanned using

an Amersham Typhoon Imager (GE Healthcare). The data was quantified using the ImageJ

software.

**Sample preparation for mass spectrometric analysis by LC-MS/MS**

To identify the residues phosphorylated on PMK3 and MAK2 by the feedback loop,

MS samples were prepared and analysed by LC-MS/MS. *In vitro* phosphorylation assay was

performed with cold ATP (200µM) in 1X kinase assay buffer using both proteins (30µg of

PMK3 and 100µg of MAK2). Reaction was incubated for 1 hour at 25°C. The sample was

passed through Zeba Spin de-salting columns (Thermo Scientific) and exchanged to a buffer with 50mM ammonium bicarbonate and 5mM DTT (Promega). Resulting sample was incubated at 56°C for 45 minutes, the final DTT concentration was subsequently adjusted to 10mM and further incubated for 15 minutes at 90°C. The reaction mixture was then cooled to room temperature, and iodoacetamide (IAA; Promega) was added to a final concentration of 20mM and incubated for 1 hour at room temperature in the dark. 5mM DTT was further added to the sample and incubated for another 30 minutes at room temperature neutralize excess IAA in the reaction. The trypsin stock was prepared in 50mM ammonium bicarbonate and added at a ratio of 1:100 (w/w). The added trypsin was diluted around 50-fold in the digestion reaction by additional 50mM ammonium bicarbonate. The trypsin was added in two steps: after the initial addition, the samples were incubated at 37°C for 1 hour, followed by the addition of another round of trypsin and overnight incubation at 37°C. Reactions were stopped with 0.1% trifluoroacetic acid (TFA) to reduce the pH below 4. The samples were vacuum-dried in a SpeedVac (Thermo Scientific, Savant SPD111V) and the resulting peptides were selectively enriched using the Thermo Fisher High-Select $TiO_2$ Phosphopeptide Enrichment Kit (Cat. No A32993), following the manufacturer's instructions.

Digested peptides were desalted and enriched using Pierce C18 Tips (Thermo Scientific). Eluted peptides were resuspended in 5% (v/v) formic acid and sonicated for 5 min. Samples were analyzed on Orbitrap Exploris™ 240 mass spectrometer (Thermo Scientific) coupled to a nanoflow LC system (Easy nLC II, Thermo Scientific). Peptide fractions were loaded onto a PepMap™ RSLC C18 nanocapillary reverse phase HPLC column (75 μm × 25 cm; 2μm; 100 Å) and separated using a 60 min linear gradient of the organic mobile phase [5% Acetonitrile (ACN) containing 0.1% formic acid and 95% ACN containing 0.1% formic acid]. For identification of peptides the raw data was analyzed on MaxQuant proteomics computational platform (Ver. 1.6.8) (Cox and Mann, 2008) and searched against UniProt amino acid sequences (Uniprot ID: Q965G5; O44514) using phosphorylation (STY) as a variable modification. The MS-based proteomics data of these experiments have been deposited in the ProteomeXchange Consortium via the PRIDE partner repositiory with the dataset identifier PXD054369 (Vizcaino et al., 2014).

**Fluorescent labelling of proteins**

Purified MAK2 was labelled with Fluorescein-5-Maleimide (Thermo Fisher Scientific) for the fluorescent detection of the proteins under confocal microscope. The proteins were prepared in a 20mM potassium phosphate buffer pH 7.2 with 100mM NaCl, 3% glycerol, 2mM EDTA and 50μM TCEP. The fluorophore was added to the protein at a molar concentration ratio of 8:1 and incubated on ice for 4-5 hours with intermittent mixing. The reaction was terminated with 5mM DTT. The excess dye was removed using a PD SpinTrap G-25 (GE Healthcare) desalting column and subsequent dialysis in 25mM Tris pH 8, 100mM NaCl, 3%

glycerol, 5mM β-Me and 1mM EDTA buffer. The samples were resolved by SDS-PAGE and

scanned in an Amersham Typhoon Imager (GE Healthcare) to confirm the labelling efficiency.

For PMK3, labelling was done with both Fluorescein-5-Maleimide (Thermo Fisher Scientific)

and Alexa Fluor 594 NHS Ester (Thermo Fisher Scientific). In case of Alexa Fluor 594, PMK3

was dialyzed against 20mM potassium phosphate buffer pH 8, 100mM NaCl, 3% glycerol,

5mM β-Me and 2mM EDTA and the protein to dye molar ratio was maintained at 1:5.

**_In vitro_ droplet formation assay**

The _in vitro_ LLPS of all proteins was performed either in presence of varying

concentrations of PEG-8000 (v/v) (Promega) or without any crowding agent in a dilution buffer

composed of 50mM Tris pH 8, 50mM NaCl, 2% glycerol, 5mM β-Me and 2mM EDTA. Proteins

in different concentrations/conditions were mixed with the desired amount of PEG-8000

solution and incubated at 25°C for different time periods. Liquid condensate or droplet

formation due to phase separation was followed by the visual turbidity of the samples and their

imaging in confocal microscope. 12µl of each sample was pipetted on to a glass slide and

covered with a cover slip for imaging. All fluorescent images were acquired using a Leica TCS

SP8 confocal microscope (63X oil immersion objective lens) or Leica Stellaris 5 laser scanning

microscope (100X oil immersion objective lens), equipped with SuiteX (Las X software).

Further image analyses were performed using the ImageJ software.

**Fluorescence recovery after photobleaching**

Fluidity and dynamics of the phase separated globular condensates were analysed

through FRAP. The FRAP experiments were performed on MAK2-GFP droplets within 20-30

minutes of the reaction initiation, using the FRAP module on the Leica microscope. Imaging

was performed using a 488nm laser for GFP at 100% power. 3 pre-bleach control images

were taken and subsequently a small circular ROI within a single droplet was bleached for 4

seconds. The fluorescence recovery within the bleached region was monitored for 90 seconds

post-bleaching (10seconds/frame). The fluorescence intensities at the post-bleach points

were normalized to the pre-bleach intensity and plotted to understand the degree of

fluorescence recovery.

**_In vitro_ kinase assay using ATP-ɣ-S**

To monitor the de novo phosphorylation events involving the different kinases, _in vitro_

non-radioactive kinase assays were performed using the ATP analogue, ATP-ɣ-S (Enzo Life

Sciences). The LLPS samples under different conditions were incubated with 150µM ATP-ɣ-

S in a kinase assay buffer with 2mM TCEP and incubated at 25°C for the various mentioned

time points. Kinase reactions were quenched with 20mM EDTA. The proteins were then

alkylated with 1mM p-Nitrobenzyl mesylate (PNBM, Sigma Aldrich) and incubated further at

room temperature for 2 hours in the dark. Samples were subsequently boiled with SDS loading

dye and resolved by SDS-PAGE. The proteins were transferred on to PVDF membranes by

using semi-dry transfer apparatus. Blocking was done for 1 hour at room temperature with 5% BSA in TBS-T buffer, following which the membranes were incubated in the primary antibody (Thiophosphate Ester Specific RabMAb; Abcam) overnight at 4°C. An HRP-conjugated anti rabbit IgG (Thermo Fisher Scientific) was used as the secondary antibody. The protein bands were detected using enhanced chemi luminescence substrates (Thermo Scientific SuperSignal West Pico Chemiluminescent Substrate or Bio-Rad Clarity Western ECL substrate) in Amersham Imager 600.

**Immunoblotting using p-tyrosine antibodies**

To detect the pan-tyrosine phosphorylation on PMK3 and MAK2, kinase assays were set up with 200µM cold ATP in 1X kinase assay buffer and incubated at 25°C for the mentioned time intervals. Reactions were terminated with SDS loading dye, boiled at 100°C for 5 minutes, resolved by SDS-PAGE and subsequently transferred on to nitrocellulose or PVDF membranes. Following blocking for 1 hour in 5% BSA in TBS-T, the membranes were incubated in the specific p-tyrosine antibodies (BD Biosciences), overnight at 4°C. An HRP-conjugated anti mouse IgG (Thermo Fisher Scientific) was used as the secondary antibody.

**Kinetic Modelling:**

*Fig. 1 The Schematic of the phosphorelay kinetics of PMK3 (Y) and MAK2 (Z) mediated by MKK4 (X).*

The detailed kinetic steps of phosphorylation processes are the following:

$X$ mediated phosphorylation of $Y$ ($Y \xrightarrow{X} Y_p$)

$$\text{Y} + X \underset{k_2^-}{\overset{k_2^+}{\rightleftarrows}} YX \xrightarrow{k_2} Y_p + X$$

$$( 1 )$$

$Z_p$ mediated phosphorylation of $Y$ ($Y \xrightarrow{Z_p} Y_p$)

$$\text{Y} + Z_p \underset{k'^-_2}{\overset{k'^+_2}{\rightleftarrows}} YZ_p \xrightarrow{k'_2} Y_p + Z_p$$

$$( 2 )$$

$Y_p$ mediated phosphorylation of Z ($Z \xrightarrow{Y_p} Z_p$)

$$Z + Y_p \underset{k_3^-}{\overset{k_3^+}{\rightleftarrows}} ZY_p \overset{k_3}{\rightarrow} Z_p + Y_p$$

<div align="right">(3)</div>

949    *Y* mediated phosphorylation of *Z* ($Z \overset{Y}{\rightarrow} Z_p$)

$$Z + Y \underset{k'^-_3}{\overset{k'^+_3}{\rightleftarrows}} ZY \overset{k'_3}{\rightarrow} Z_p + Y$$

<div align="right">(4)</div>

We considered a Michaelis-Menten kinetic model, where the phosphorylation takes
place through an intermediate complex formation, which either produce the phosphorylated
form of the kinase or revert back to the unphosphorylated kinase form (Ferrell, 2022; Huang
and Ferrell, 1996; Tian and Song, 2012). The respective rate constants for each kinetic steps
are provided in the kinetic scheme (Eqs. (1-4)). We employ a coarse-grained approach for
dephosphorylation processes ($Y_p \rightarrow Y$ and $Z_p \rightarrow Z$), assuming a direct conversion from the
phosphorylated kinase back to the unphosphorylated kinase form. This simplification is
appropriate when the focus lies on capturing the overall effect of phosphorylation kinetics on
the larger network. We, now, formulate the system of coupled ordinary differential equations
(CODEs) that describe the temporal evolution of each component considering both
phosphorylation and the simplified dephosphorylation processes.

$$\frac{d[Y]}{dt} = -k_2^+[Y][X] + k_2^-[YX] - k_2'^+[Y][Z_p] + k_2'^-[YZ_p] + k_{-2}[Y_p] - k_3'^+[Z][Y]$$
$$+ (k_3' + k_3'^-)[ZY]$$

<div align="right">(5)</div>

$$\frac{d[Y_p]}{dt} = k_2[YX] + k_2'[YZ_p] - k_{-2}[Y_p] - k_3^+[Z][Y_p] + (k_3 + k_3^-)[ZY_p]$$

<div align="right">(6)</div>

$$\frac{d[Z]}{dt} = -k_3^+[Z][Y_p] + k_3^-[ZY_p] - k_3'^+[Z][Y] + k_3'^-[ZY] + k_{-3}[Z_p]$$

<div align="right">(7)</div>

$$\frac{d[Z_p]}{dt} = -k_2'^+[Y][Z_p] + (k_2' + k_2'^-)[YZ_p] + k_3[ZY_p] + k_3'[ZY] - k_{-3}[Z_p]$$

<div align="right">(8)</div>

<div align="center">33</div>

$$\frac{d[YX]}{dt} = k_2^+[Y][X] - (k_2 + k_2^-)[YX]$$

$$( 9 )$$

$$\frac{d[YZ_p]}{dt} = k_2'^+[Y][Z_p] - (k_2' + k_2'^-)[YZ_p]$$

$$( 10 )$$

$$\frac{d[ZY_p]}{dt} = k_3^+[Z][Y_p] - (k_3 + k_3^-)[ZY_p]$$

$$( 11 )$$

$$\frac{d[ZY]}{dt} = k_3'^+[Z][Y] - (k_3' + k_3'^-)[ZY]$$

$$( 12 )$$

969 In the above CODEs, the rate constants for dephosphorylation of $Y_p$ and $Z_p$ are denoted as
970 $k_{-2}$ and $k_{-3}$, respectively. We define the Michaelis-Menten constants for each
971 phosphorylation steps (Eqs. (1-4)) as,

$$K_M^{(2)} = \frac{k_2 + k_2^-}{k_2^+}, K_M'^{(2)} = \frac{k_2' + k_2'^-}{k_2'^+}, K_M^{(3)} = \frac{k_3 + k_3^-}{k_3^+}, K_M'^{(3)} = \frac{k_3' + k_3'^-}{k_3'^+} \qquad ( 13 )$$

For $X$ regulated phosphorylation of $Y$ (Eq. (1)), we define a dimensionless parameter $A$, called
activity of the corresponding regulatory molecule which modulate the phosphorylation process
of the downstream kinase. Specifically, for $X$ mediated phosphorylation of $Y$ (Eq. (1)), we
define the activity of $X$ as $A_X = k_2/K_M^{(2)}$. Similarly, for $Y_p$ mediated phosphorylation of $Z$ (Eq.
(3)) activity of $Y_p$ is defined as $A_{Y_p} = k_3/K_M^{(3)}$ and for $Y$ mediated phosphorylation of $Z$ (Eq.
(4)) activity of $Y$ is defined as $A_Y = k_3'/K_M'^{(3)}$. In the feedback loop where $Z_p$ induces
phosphorylation of $Y$ (Eq. (2)), the activity of $Z_p$ is defined as $A_{Z_p} = k_2'/K_M'^{(2)}$. The activity, $A_{Z_p}$,
also represents feedback sensitivity and strength (FSS). A higher value of $A_{Z_p}$ indicates
stronger and more sensitive feedback regulation. Specifically, a higher $k_2'$ value increases the
strength of feedback regulation, while a lower $K_M'^{(2)}$ value signifies higher sensitivity in the
feedback regulation. In our model, we adjust the FSS ($A_{Z_p}$) to investigate the role of $Z_p$
feedback regulation in the dynamics of phosphorylation kinetics. The activities of the

regulators $X, Y$, and $Y_p$ ($A_X$, $A_Y$, and $A_{Y_p}$, respectively) can also be described in similar fashion

in terms of regulatory sensitivity and strength.

**Parameters used:**

Total concentration of $X$, $[X] = 5\ \mu M$

Total concentration of $Y$, $[Y]_{\text{Total}} = 10\ \mu M$

Total concentration of $Z$, $[Z]_{\text{Total}} = 10\ \mu M$

Where,

991
$$[Y]_{total} = [Y] + [Y_p] + [YX] + [YZ_p] + [ZY_p] + [ZY]$$

992
$$[Z]_{total} = [Z] + [Z_p] + [YZ_p] + [ZY_p] + [ZY]$$

994
$$k_2^+ = 1.0\ \mu M^{-1}s^{-1}, k_2^- = 0.9\ s^{-1}, k_2 = 0.1\ s^{-1}, k_{-2} = 0.3\ s^{-1}$$

995
$$k_3^+ = 2.0\ \mu M^{-1}s^{-1}, k_3^- = 0.9\ s^{-1}, k_3 = 0.1\ s^{-1}, k_{-3} = 0.3\ s^{-1}$$

996
$$k_3'^+ = 0.1\ \mu M^{-1}s^{-1}, k_3'^- = 0.9\ s^{-1}, k_3' = 0.1\ s^{-1}$$

997
$$k_2'^- = 1.0\ s^{-1}, k_2' = 1.0\ s^{-1}$$

998 Based on these parameter values, the Michaelis-Menten constants take the values $K_M^{(2)} =$

999 $1\ \mu M$, $K_M^{(3)} = 0.5\ \mu M$, and $K_M'^{(3)} = 10\ \mu M$. Similarly, the activity values are, $A_X = 0.1$, $A_Y = 0.01$,

1000 and $A_{Y_p} = 0.2$.

1001 We tune $k_2'^+$ so that $K_M'^{(2)}(= 1/k_2'^+)$ takes on different values allowing us to ultimately tune $A_{Z_p}$.

1002 This approach helps us explore how variations in FSS influence the phosphorylation kinetics.

1003

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1012

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1014 Conceptualization: SP; Experimental design: SP and PR; Investigation: PR, PRT, AH, SM

1015 (structural modeling) and MN (kinetic modeling); Data analysis: SP, PR, AGR, SRC, PRT;

1016 Figure: SP, PR, PRT, MN, SM; First draft: SP; Editing: PR, AGR, PRT, MN

1017

1018 **Competing interests:** Authors declare no competing financial interests.

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