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4   The size-weight illusion and beyond: a new model of perceived weight

7   Veronica Pisu[1*], Erich W. Graf[1], Wendy J. Adams[1]

11   [1] School of Psychology, University of Southampton, Southampton, United Kingdom

14   * Corresponding author

15   Email: Veronica.Pisu@soton.ac.uk (VP)

Abstract

In the size-weight illusion (SWI), the smaller of two same-weight, same apparent material objects is perceived as heavier. The SWI has proved difficult to explain via traditional Bayesian models, which predict the opposite effect: expected weight from size (smaller = lighter) should be integrated with felt weight, such that the smaller object should be perceptually lighter. Other authors have proposed that weight and density are combined according to Bayesian principles, or that Bayesian models incorporating efficient coding can predict the SWI via 'likelihood repulsion'. These models, however, have been evaluated only under the narrow conditions of typical SWI stimuli. Here we establish a general model of perceived weight for pairs of objects that differ in weight and / or density and / or size by varying amounts. In a visuo-haptic task, participants (N = 30) grasped and lifted pairs of cubes, and reported their perceived heaviness. We report that the SWI occurs even at very small density differences, repudiating the idea that the illusion requires a significant conflict between expected and felt weight. Across all object pairs, perceived weight was well explained by a model (R^2 = .98) that includes a positive influence of both objects' weights and the judged object's density, but a negative influence of the other object's density. Critically, the influence of both densities on perceived weight is strongly modulated by weight difference, being three times as large for zero / small weight differences than large differences. Thus, it is only under the unusual conditions of typical SWI studies that we confuse weight with density to a substantial extent. Unlike existing models, that are inconsistent with our more comprehensive dataset, our model provides a quantitative, accurate and generalised account of weight perception for pairs of objects across various weight and size conditions.

Author summary

Knowing how heavy an object is allows us to grasp and lift it efficiently and without mishaps. Surprisingly, humans make systematic errors when judging the weight of objects of different

size. For example, when two objects differ in size but have identical weight, the smaller object

feels heavier. This is the 'size-weight illusion'. The illusion is strong and reliable and occurs

even when we know that the two objects actually have the same weight. The size-weight illusion

demonstrates that the human perceptual system doesn't work like a weighing scale, but

instead takes into account other object features such as size or density, alongside weight. In

this paper, we present a model that allows us to predict perceived weight in the size-weight

illusion and across a wide range of objects of different weight / size / density, where previous

models have failed. Understanding how weight perception works has a wealth of practical

applications, including in virtual reality and in the development of prosthetics that provide

users with a more naturalistic experience.

1. Introduction

In the well-known size-weight illusion (SWI) (1), participants are typically presented with

one large and one small object, apparently of the same material, but in fact of equal weight. On

lifting, the smaller object is perceived as heavier than the larger one. The illusion is robust,

persisting even when the lifter knows that the objects have equal weight (2,3), and after

grasping forces have adapted to the actual weight of the objects (4).

Although the SWI has long been investigated as a means to understanding human

heaviness perception, its mechanism remains largely unexplained (for reviews, see (3,5,6)).

Early descriptive accounts suggested that the SWI is caused by a contrast / repulsion effect,

where the felt weights of the two objects conflict with those predicted by assuming equal

density. Other accounts have suggested that the lifter confounds / combines felt weight with

other physical features (generally density: (7–9); but also rotational inertia: (10,11).

In 'contrast' or 'violated expectation' accounts it is noted that object size is used as a

predictive feature for object weight (12–14). Smaller objects are expected to be lighter than

larger objects, particularly when they are apparently made of the same material – that is, of

equal density. Upon lifting, the smaller object is heavier than expected, and this disparity

between expectation and sensory evidence is suggested to cause the illusion. Evidence for this

conflict between expected and actual weight comes from the forces used to grip and lift the two

objects. On initial lifts, participants use more force to lift the larger (expected to be heavier)

object than to lift the smaller one (4,15). These misapplied forces have thus been suggested to

drive the illusion: the larger object, being lighter than expected, is lifted faster, and vice versa,

producing a mismatch between the expected and actual sensory feedback (5,15). However, it

has been widely reported that grasping forces adjust to the weight of the object after a few lifts,

while the illusion persists (4,16–18)).

Because the illusion is at odds with the perceiver's prior expectations (that the smaller

object should be lighter) the SWI has been labelled 'anti-Bayesian' (19,20). The Bayesian

framework has successfully described numerous perceptual phenomena in terms of the

integration (generally a weighted averaging) of prior expectations with current sensory cues (21–

26). In the SWI, however, the Bayesian prediction is that the smaller object will be perceived as

lighter than the larger object, given an assumption of equal density for the two objects. Figure 1

illustrates this: Figure 1A represents the stimulus space, with different possible combinations

of two stimuli (weight, volume and density log ratio) indicated by the text labels. Figure 1B

shows three hypothetical priors on the same axes: The red lines show theoretically sensible

priors, given natural statistics: (i) the larger object is heavier and same-density (solid line), or (ii)

the larger object is heavier but slightly less dense (dashed line) (see (27). Both of these priors

predict the opposite of the empirical SWI (black dots show stimuli, arrowheads give perceived

log weight ratio, taken from current study). Note that the empirical SWI involves biases away

from the theoretically sensible priors in red, hence the 'anti-Bayesian' label. The green line

shows a hypothetical prior (smaller = heavier) that would predict the SWI. However, this prior is

implausible, given environmental statistics in which size and weight are positively correlated.

Figure 1 (A) Stimulus space for pairs of stimuli in log-log coordinates, showing log weight ratio
and log volume ratio. A value of zero indicates that the two objects have equal weight (or
volume). The solid diagonal line indicates equal density, i.e. log density ratio of 0. The labels
indicate possible stimulus combinations relating object 1 to object 2. (B) SWI and three
hypothetical priors over log volume ratio and log weight ratio. The black dots show SWI stimuli
(equal weight but different volume) and arrows show the empirical bias, i.e. the perceived
weight ratio, for the same stimuli (data from the current experiment, see below). The green line
represents one hypothetical prior (smaller is heavier) that would predict the SWI. In contrast,
the red lines show plausible priors in which weight increases with size, as per environmental
statistics. (C) Peters and colleagues' (28) model sub-priors, each corresponding to a different
density / volume relationship (R); R_1 = equal-density prior; R_2 = smaller is denser and heavier; R_3
= smaller is less dense and lighter. Note that Peters and colleagues represented their priors in
terms of log density ratio and log volume ratio; here they are shown in log weight *ratio*, log
volume ratio space for a more intuitive representation.

Despite this, Bayesian models of the SWI have been proposed (28,29). Peters and

colleagues (28) proposed a Bayesian model that includes three sub-priors over the relationship

between the log volume ratio of two objects and their log density ratio (see Figure 1C). Each

sub-prior represents a categorical density relationship; R_1: objects have equal density, R_2:

smaller objects are denser and heavier than larger ones and R_3: smaller objects are less dense

(much lighter) than larger objects. When a typical SWI stimulus pair (e.g. log weight ratio = 0, log

volume ratio = 0.5) is encountered, the 'smaller is denser and heavier' prior (R_2 in Figure 1C)

dominates, resulting in an illusion (although the priors from Peters and colleagues (28) predict a

smaller SWI than reported here). It is not clear whether the model can account for weight

perception more broadly as it was only evaluated on pairs of equal-weight objects (i.e., typical

SWI stimuli); predicted biases in weight perception depend on the volume and density ratios of

the stimuli and thus which sub-prior dominates perception.

Wei and Stocker (30,31) have suggested that contrast effects analogous to the SWI, i.e.

biases away from the prior, can be predicted by Bayesian models incorporating efficient coding

of stimulus properties (32,33). Wei and Stocker note that when efficient coding maximises

Fisher information (i.e., to reflect the stimulus distribution in the environment), this results in

likelihoods that are systematically skewed with a long tail away from the peak of the prior. If a

symmetric loss function is also employed (e.g., L2 loss, selecting the mean rather than the

maximum of the posterior), estimates will be systematically biased away from the prior, relative

to the peak of the likelihood ('likelihood repulsion'), see 'Modelling' section for more detail.

Recently, Bays (29) has proposed a Bayesian model of the SWI that incorporates efficient

coding and a prior reflecting a positive association between size (volume) and weight. However,

Bays' model has only been tested on Peters and colleagues (28) dataset.

Other authors suggest that we are unable to fully separate density and weight (34), or

proactively combine them (9). Under these models, denser objects are systematically

perceived as heavier. Indeed, heaviness and density estimation appear to be closely related:

perceived weight difference increases with increasing density difference weight (34); objects of

greater weight are reported as denser (35), and weight difference discrimination is improved

when density varies in the same direction as weight (36). Within typical SWI stimuli, weight is

kept constant such that density is negatively correlated with volume. Thus, size contributes to

the illusion as it is used to infer density ('density-weight-illusion' (7,9,37)).

Wolf and colleagues (8,9) proposed a cue-integration model in which perceived

heaviness is a weighted average of two heaviness estimates, one from the object's felt weight

and one derived from the object's inferred density. Because denser objects tend to be heavier,

the authors suggest that it is adaptive / Bayesian to combine estimates of weight and density

when estimating weight to obtain more reliable (less noisy) weight estimates. In the model, the

relative influence of density depends on its relative reliability; when the reliability of (visual or

haptic) size information is reduced, density has less effect on the final heaviness estimate (9).

In the limiting case, of course, when size information is completely absent (objects lifted via

strings / a handle, and no vision), the illusion disappears (9,38,39). It is not clear, however, why

we should combine weight and density information in this way, when volume information is

available to condition the density-weight relationship. Not only is density a poor cue to weight

(when not conditioned on size) but the two estimates will also have correlated noise (thus

negating some benefits of integration).

It is well known that the SWI magnitude increases with volume (density) difference

(6,28,34,38,40) and this relationship is predicted by all of the above models. SWI

demonstrations tend to use fairly large, obvious differences in object volume, in order to obtain

a reliable illusion. However, under small conflicts between size-based expectations of weight

and direct sensory evidence, these estimates might be integrated; we know that integration

occurs for small conflicts but breaks down under conditions of large conflict (41,42) . If

integration (the opposite of the SWI) occurs under small conflicts, while the SWI only occurs

with large conflicts, this would be broadly in line with the idea that the SWI is driven by violated

expectations. This would also be consistent with the effect of the equal density sub-prior in

Peters and colleagues model (28). However, integration under small density differences would

be at odds with models in which weight and density are confounded / integrated in general

(8,9). Furthermore, it is unclear whether humans conflate weight and density in all situations

(such as when a smaller object is slightly less dense), or only in the specific and non-accidental

conditions of SWI stimuli, when weight is held constant and volume varies.

Here we asked: Can we develop a generalised model of weight perception for varied

combinations of size, weight and density? To this end we measured perceived weight for pairs

of cubes from a large set in which volume, and / or weight, and / or density were varied in small

steps. Size and density were uncorrelated in the full set to prevent learning of unusual size -

weight associations. To preview the main findings: 1) The SWI occurred even at very small size

(density) differences, and thus does not rely on large conflicts. 2) Perceived weight was

positively correlated with the true weight of both the judged and other stimulus, in addition to

the judged object's density. 3) The effect of both objects' densities on perceived weight was

strongly modulated by the weight difference between the two objects: three times larger at

small / zero weight differences than at large weight differences. In fact, the other object's

density had an effect only when the two objects had similar weight, when it was negatively

associated with the judged object's perceived weight. Thus, the perceptual system does

conflate weight and density, but this effect is much larger in the specific and peculiar

conditions of typical studies of the SWI. We provide a model (R^2 = .98) that captures biases in

perceived weight in the SWI and across the full stimulus set. In addition, we compare this

model to existing models of the SWI, and to a novel efficient-coding Bayesian model of the SWI.

2. Materials and Methods

2.1 Participants

Thirty naïve participants (age *M* 21.4, *SD* 5.6 years) from the University of Southampton

Psychology student community took part in the experiment; undergraduate students were

compensated for their participation with course credits. All reported normal or corrected-to-

normal eyesight and no upper limb impairment. The experiment was approved by the University

of Southampton Psychology Ethics Committee; all participants gave prior informed consent.

 2.2 Stimuli

Stimuli were 15 plastic cubes (3D-printed in black polylactic acid (Figure 2A–B). Each

cube was filled with sand, polystyrene pellets, and / or brass to create the desired volume,

weight and density values for the different stimulus sets, depicted in Figure 2A. The centre of

mass of the cubes remained at the geometric centre and the filling did not move inside the

cubes during lifting. A panel concealed at the bottom kept the appearance homogeneous.

Weight was measured with a 0.1 g resolution.

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200 Figure 2 Stimulus set. (A) Full stimulus set, see legend in (D). Note that the stimuli are shown
201 upside-down in the picture. (B) 500 cm^3 stimulus for scale. (C) Stimulus volume as a function of
202 weight. (D) Stimulus density as a function of weight.
203
The complete stimulus set included three subsets (Figure 2C–D), corresponding to

different volume / weight relationships: 1) Equal density (red): weight increased linearly with

volume (as for 'normal' same-material objects); 2) Equal weight (green): density decreased with

increasing size (typical SWI stimuli); 3) Increasing density with increasing size (blue): both

weight and density increased with size. The middle cube (volume, weight, density: 750 cm^3, 375

g, 0.5 g / cm^3) was common to all three subsets. Volumes within each set increased in 100 cm^3

steps, with the addition of 50 cm^3 steps below and above the middle stimulus in the fixed

density set. Minimum (maximum) volume, weight, density differences across any stimulus pair

were: 50 (250) cm^3, 25 (200) g, 0.02 (0.18) g / cm^3, respectively. Density ratios for stimulus pairs

ranged between 0.47–0.97 (less dense / denser stimulus), 0.58–0.89 for equal weight (SWI)

stimulus pairs. In comparison, previously reported density ratios (less dense / denser) for the

minimal density differences have been: 0.67 (43); Experiment 4); 0.64 (44); 0.52 (38), 0.51 (45),

Experiment 1); the largest density ratio tested by Peters and colleagues was 0.42 (28). Larger

density ratios were tested by Wolf and colleagues (9): 0.87, in a set of same-volume (increasing

density) stimuli. To our knowledge, only Kawai and colleagues (46) investigated smaller

differences (density ratio: 0.98), by manipulating the visual size of stimuli lifted via strings in an

augmented-reality setting; although they suggest that heaviness perception might be veridical

at very small (but still detectable) volume differences, it should be noted that the magnitude of

the SWI is expected to be smaller in absence of haptic size cues (38,47) and in virtual

environments (48,49).

2.3 Task and trials

Stimuli were presented in pairs. In each trial, participants simultaneously grasped and

lifted both cubes in full visuo-haptic conditions, and verbally reported both objects' weights

using magnitude estimation. This paired presentation (common in SWI experiments) allowed us

to model the perceived weight of each object in addition to the pair's perceived weight

difference or weight ratio. Experimental trials included all possible stimulus pairs (same- and

different-subset pairs), excluding pairs of identical stimuli. This gave 105 unique pairs and 133

pairs in total (trials including the middle / common stimulus were repeated due to a coding

error). Each stimulus pair was presented twice, with left and right position switched between

the two trials (266 trials in total). Trials were randomised for each participant.

2.4 Setup

The participant and the experimenter sat at opposite sides of a table covered in thick

felt to muffle auditory cues to the objects' weights. Two numbers (1, 2) marked the positions of

the stimuli on the table (centre-to-centre distance between stimuli, centre of stimuli to table

edge: both 20 cm) and served to remind participants the order in which to report their

estimates. A frame-mounted black curtain was used to control stimulus presentation, such

that the participant only ever saw the two stimuli of the current trial. A desktop computer

running MATLAB (The MathWorks Inc., 2020) was used to randomise stimulus presentation and

record participant responses.

2.5 Procedure

The experiment was completed in two identical laboratory sessions on separate days,

each lasting 60–90 minutes. At the beginning of each session, participants were presented with

the middle cube (750 cm^3, 375 g) as the reference stimulus, and told that this had a weight of

'50' (arbitrary units). The reference was presented again every 20 trials. Participants were

instructed to look at the stimuli while lifting. Exploration mode was not restricted: participants

were free to grasp and lift the cubes as they thought best; they were not restricted to use index

and thumb only. This was done to provide the most reliable size estimates (9). Trials were not

timed, but participants were encouraged to give an answer if they waited more than 30 seconds

(approx.).

3. Results

Participants' magnitude estimates were transformed into grams and then normalised to

remove individual differences in how the response scale was used: Each participant's

estimates were multiplied by the ratio of their individual grand mean across stimuli to the grand

mean across all participants (thus, after normalisation, each observer had the same mean

response). Outliers per condition were then removed iteratively: for each object within each

stimulus pair, values more than 5 SDs, then 4 SDs, and 3.5 SDs from the mean across

observers were removed (65 datapoints in total, or 0.4%). Data were re-normalised after each

iteration. All further analyses were conducted on the resulting dataset.

Weight estimates for within-subset pairs (i.e., both objects from the same subset) are

shown in Figure 3, alongside model fits (see below, Equation 1–2). Data have been collapsed

across repetitions within participants and *SE* bars show inter-observer variation. We present

the perceived weight of the judged object (i.e., the object within each pair whose weight is being

reported) in terms of its own properties (weight / density) and the properties (weight / density) of

the other object in the pair. Each object in turn was considered the judged object.

For equal density, i.e. 'normal' object pairs (Figure 3A–B), weight estimates were highly

correlated with the true weight of the judged object, as expected. However, they were also

positively correlated with the weight of the other object (denoted by symbol size in Figure 3A;

see the vertical spread corresponding to weight of other object); note that this is an averaging,

rather than a contrast effect. Perceived weight difference (perceived 'judged' weight - perceived

'other' weight) was linearly related to stimulus weight difference (Figure 3B; data are

symmetrical in all difference plots (B, D, F) as each object in each stimulus pair serves as

'judged').

Figure 3 Perceived weight (A, C, E) / weight difference (B, D, F) for within-subset stimulus pairs,
averaged across participants; error bars show ± 1 SEM; solid lines / open symbols show the
model predictions (described below, Equation 1 and 2); (A, B, E, F) the dashed lines are identity
lines. (A–B) Equal density pairs: (A) Weight estimates as a function of stimulus weight; symbol
size indicates the weight of the other stimulus in the pair. (B) Data re-expressed as perceived
weight difference. (C, D) Equal weight (SWI) pairs: (C) Weight estimates as a function of
stimulus density; symbol size indicates the density of the other stimulus in the pair. (D)
Perceived weight difference, as a function of density difference; symbol size indicates the
average density. (E, F): Increasing density pairs: (E) Symbol size indicates the other stimulus
weight; (F) Symbol size indicates the average density.

Weight estimates for the equal weight (SWI) pairs are shown as a function of the judged

object's stimulus density (x-axis) and the other object's density (symbol size, Figure 3C). In line

with the size-weight illusion, perceived weight was positively correlated with object density:

denser (and smaller) stimuli were perceived as heavier (overall positive slope of the data).

Perceived weight was also negatively correlated with the other object's density, the judged

object appearing heavier when judged next to less dense (larger) objects (see the vertical

spread of data points in 3C). The data are re-expressed as perceived weight difference as a

function of density difference in Figure 3D. It is clear that the magnitude of the SWI (i.e.

deviation from veridical perception) increases with density difference, but still occurs with

small density (or volume) differences. Thus, we find no evidence for integration of expected and

sensory weight estimates under small conflicts.

Lastly, in the increasing density pairs (Figure 3E), weight estimates were positively

correlated with the object's weight, but also correlated with the other object's weight (as in the

equal-density pairs; see vertical spread of data in 3E). Figure 3F shows that perceived weight

difference increases linearly with true weight difference. In this set, weight (or weight

difference) is correlated with density (or density difference); the effect of density contributes to

the increased slope of the data, relative to veridical perception (identity line).

Figure 4A summarises results for all trials, including across-subset pairs (i.e. each

object in a pair from a different stimulus subset), in a format that illustrates the variable

influence of density on perceived weight. For every stimulus pair (represented by a dot),

perceived weight difference (y-axis) is presented as a function of stimulus weight difference (x-

axis) and stimulus density difference (colour). Lines show the model fit (see Equation 2 below).

The overall slope of the data shows the strong relationship between true and perceived weight

difference. The vertical spread of the different colours shows the effect of density difference on

perceived weight difference. The two are not independent: there is a central 'bulge', where the

effect of density is larger (more vertical spread). This plot shows that the effect of density (or

density difference) on perceived weight (or perceived weight difference) is strongly modulated

by stimulus weight difference, being much greater for small / zero weight differences. Figure 4B

summarises the influence of the two objects' densities on perceived weight, as captured by the

model's density coefficients (see below). The conflation of weight and density is dramatically

increased under the conditions of typical size-weight stimuli, where weight difference is zero.

Figure 4 (A) Perceived weight difference as a function of weight difference and density
difference in the full dataset. Markers show the data, solid lines show the model predictions
(see Equation 2) at equally spaced density differences. The vertical spread of the data with
density difference (marker colours) shows the effect of density in typical SWI stimuli (i.e., equal
weight: vertical dotted line) and across the full set. The dashed diagonal line shows veridical
perception. (B) The influence of density (i.e., density coefficients) as a function of weight
difference in the model.

4. Modelling

4.1 Descriptive model

We developed a model to capture perceived weight ($\hat{w}_1$) for all stimulus combinations,

as a function of the weight and density of the judged (w_1, d_1) and other object (w_2, d_2). All

analyses were done in MATLAB and optimal coefficients (minimising the summed squared

residuals, SSR) were identified via gradient descent. Alternative candidate models are

presented in Supplementary Table 1 alongside model comparison statistics. Models including

the objects' volumes (v_1, v_2) instead of density were also tested, see Supplementary Table 2. To

prevent over-fitting, we used leave-one-out cross-validation on the normalised dataset, leaving

out each participant in turn. The best model (Equation 1) explains 98% of the variance in the full

dataset:

$\hat{w}_1 = C + \beta_1 w_1 + \beta_2 d_1 + \beta_3 w_2 + \beta_4 d_1 N(|w_1 - w_2|, 0, \sigma^2) + \beta_5 d_2 N(|w_1 - w_2|, 0, \sigma^2)$ (1)

Model predictions for $\hat{w}_1$ as a function of the observed values are shown in Figure 5B.

Figure 5 (A) Variance in perceived weight explained by the addition of each predictor in the
model (bars) and corresponding SSR (magenta lines and markers). The order of predictors
follows the maximum increase in R^2 with each addition (see SI, Table S1); $X = N(|w_1 -$
$w_2|, 0, \sigma^2)$. (B) Predictions of perceived weight from the best-fitting model (Equation 1) as a
function of participants' estimated weight for each stimulus, across all object pairs. The dashed
line shows equality. Error bars give ± 1 SEM.
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Accordingly, the perceived weight difference ($\hat{w}_1$ - $\hat{w}_2$) between two stimuli can be predicted via

the following equation:

$\hat{w}_{diff} = (\beta_1 - \beta_3)(w_1 - w_2) + \beta_2(d_1 - d_2) + (\beta_4 - \beta_5)(d_1 - d_2) N(|w_1 - w_2|, 0, \sigma^2)$ (2)

Perceived weight was positively correlated with the object's weight (β_1 = 1.23) and its

density (β_2 = 126.43), and with the other object's weight (β_3 = 0.13). However, the influence of

density on perceived weight was modulated by weight difference, as captured by the two

Gaussians (see the central 'bulge' in Figure 4A). The density of the judged object positively

influenced its perceived weight (β_4 = 27814), whereas the other object's density had a negative

influence (β_5 = -2566.2). Sigma for the Gaussian components was 76.44. Figure 4B shows the

influence of both objects' densities as a function of weight difference: the combined influence

of the two densities on perceived weight was approximately three times larger for zero weight

differences than for large weight differences.

4.2 Efficient coding Bayesian ratio model

Traditionally, Bayesian models have been employed to account for perceptual biases

towards a prior (i.e. towards the most frequent or probable stimuli). Examples in the literature

include biases for light-from above (50), isotropy assumptions when interpreting foreshortening

(41), global convexity of surfaces (51), and 'slow and smooth' motion (52). However, as

described by Wei and Stocker (30,31), Bayesian models incorporating efficient coding of

stimulus features can also predict repulsion biases, i.e. biases *away* from the prior. Given that

the SWI (and not integration) is observed even for very small density differences, we asked

whether such a model might provide a quantitative, Bayesian model of the SWI as a 'repulsion'

effect, where perception is biased away from a prior for equal density. Wei and Stocker (30,31)

show that the expected perceptual bias $b(\theta_0)$ for a stimulus value θ_0 from a stimulus

distribution θ can be predicted from the prior, p(θ) (in fact from the slope of its squared

reciprocal), as in Equation 3:

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$$b(\theta_0) \approx C(1/p(\theta_0)^2)' \qquad\qquad (3)$$

We present a simple model that includes a prior over two objects' relative weights and

densities: the two dimensions of log weight ratio and log volume ratio. Such a prior, if aligned

with the log weight ratio = log volume ratio unity line, represents the assumption that the two

objects have equal density. Perceptual biases away from this prior would be consistent with the

'contrast' or 'repulsion' explanation of the SWI that has prevailed for decades (5,16). For pairs

of objects, considering ratios of weight, volume and / or density (rather than their differences) is

a natural choice: any two of these ratios define the third, as $(w_1/w_2) / (v_1/v_2) = d_1/d_2$. Taking the

log ratio gives a useful symmetry: $\log(w_1/w_2) = -\log(w_2/w_1)$; allowing us to predict the same

magnitude of bias, irrespective of which object in a pair is designated as object 1. Our prior is

defined by a mixture of three bi-variate Gaussians centred on [0, 0], i.e. equal weight and

volume (Figure 6A). This mixture-model allowed us to explore variations in the shape of the

prior; there is no reason to assume that it should be a perfect bivariate Gaussian. Model

parameters and model comparisons given priors of different complexity are provided in SI,

Table S3.

Similarly to Bays (29), we employ the simplifying assumption that perceptual estimates

of volume ratio are relatively precise, and thus not significantly affected by the prior. Indeed,

there is no clear evidence that objects with unexpected weights (e.g. typical SWI objects) cause

biases in *volume* perception (i.e., a 'weight-size illusion' (53,54)). Thus, we estimated the

expected bias in perceived log weight ratio by taking a slice through the prior at the true value of

log volume ratio, and finding the slope of this 1D prior with respect to log weight ratio (Figure

6B). If volume ratio judgements were also available, one could drop the simplifying assumption,

and simultaneously fit biases in log weight ratio and log volume ratio. The resultant fitted prior

would have a slightly different shape.

We fitted the model via gradient descent to optimally predict biases in perceived log

weight ratio, averaged across participants, for all unique stimulus pairs (N = 105). (For this

model, we calculated each participant's ratio of weight estimates on each trial). Figure 6 shows

the empirical biases in perceived log weight ratio (C) and those predicted by the model (D). The

model accounts for perceived log weight ratio well, with 12 parameters (R^2 = .988; see SI S2.

Efficient-coding Bayesian ratio model; Table S3). However, goodness-of-fit is poorer than our

descriptive model (Equation 1, 7 parameters), when parameters are optimised to minimise the

SSR in perceived log weight ratio (R^2 = .991, see also cross-validation errors, SI Table S1).

Nonetheless, this efficient-coding Bayesian model provides a theoretically appealing account

of the SWI; biases in perceived log weight ratio are minimal around the $d_1=d_2$ identity line

(dashed red lines in Figure 6 C-D) and increase with log density ratio, in line with repulsion away

from an equal-density prior. Indeed, biases in log weight ratio correlate quite strongly with log

density ratio (R^2 = .691).

Figure 6 (A-B). Likelihood repulsion predicted by Wei and Stocker (30). (A) Bi-variate prior over
log weight and log volume ratio, optimised to minimise errors in predicted log weight ratio. (B)
The 1-D prior slice (solid black line) through the prior at the true log volume ratio (dashed line in
A), and a schematic of a median (unbiased / noise-free) observer likelihood and posterior for an

example stimulus pair (red asterisk in A). Efficient coding of stimulus properties results in
skewed likelihoods (solid red line) with a long tail away from the peak of the prior. The posterior
is also skewed (solid blue line). When a symmetric loss function is chosen, e.g. the mean (L2,
blue dashed line) of the posterior, a bias away from the prior is predicted, i.e. the posterior
estimate is shifted away from the prior peak, relative to the peak of the likelihood.
(Nonetheless, this loss function minimises expected mean squared error). Measurement noise
(expected to be skewed in stimulus space) further increases the predicted repulsive bias (30).
(C-D) Biases in perceived log weight ratio. Contour lines show the prior; black dots show the
stimulus pairs; arrows show the magnitude and direction of the bias for each pair; the red
dashed line shows equal density. (C) Empirical biases; (D) predicted biases.

Tempting as it is to break out the champagne and toast our Bayesian brains, this may be

premature. Closer inspection yields some difficulties with this model. First, the model is

agnostic regarding how the bias in log weight ratio is split across the two objects. A reasonable

assumption is that the prior has equal and opposite effects on the perceived weights of the two

objects. However, this is not observed: there is only a weak correlation (R^2 = .283) between

biases in estimates of log weight ratio and biases in estimates of $\log w_1$ and $\log w_2$ ($\log \hat{w}_1 - \log$

w_1, $\log \hat{w}_2 - \log w_2$); biases in estimates of $\log w_1$ and $\log w_2$ are largely independent of the two

objects' relative densities (R^2 = .215). Whilst biases in log weight ratio are *correlated* with log

density ratio, the pattern of bias is fairly well approximated by a model that predicts each

object's perceived weight from its weight and density, that is, independently of any interaction

between the two objects (R^2, log weight ratio = .984; R^2, biases in log weight ratio =. 847 see SI,

Table S1). This suggests that, although empirical biases are consistent with repulsion from an

equal-density prior (Figure 6B), this might not be the underlying mechanism. Observed and

predicted biases in judgements of $\log w_1$ and $\log w_2$ are shown in supplementary Figure S1.

Second, the model gives predictions for both biases and reliability (discrimination

thresholds or estimate variability). According to the efficient coding model, more frequently

observed stimuli are represented more precisely, such that discrimination thresholds are

proportional to the reciprocal of the prior. At the individual observer level, our data provide poor

estimates of discrimination (only two estimates per pair). However, at the group level, a

systematic pattern is clear (see SI, Figure S2). Response variance is significantly correlated with

the log weight ratio (R^2 = .532); observers' judgements of relative weight are more reliable when

the two objects' weights are similar. The Bayesian model provides a poorer account of

response variance (model vs empirical: R^2 = .444, see SI, Figure S2). Indeed, as captured by our

descriptive model, the effect of density on perceived weight is the largest when the weights of

the two objects are similar (see Figure 4), that is, when the response variance is the smallest

(see SI, Figure S2A). This is at odds with the efficient coding Bayesian prediction, in which more

reliable judgements are associated with the least bias (see SI, Figure S2B). Unfortunately,

therefore, this Bayesian model is not consistent with the behavioural data.

Finally, we also considered Bayesian models of perceptual bias involving a 2D prior over

differences in weight and *differences* in volume or density (i.e. $w_1 - w_2$, $v_1 - v_2$, $d_1 - d_2$). A prior /

model defined with regards to weight and volume differences is problematic: knowing the

weight difference and volume difference of a stimulus pair leaves the density difference

undetermined. This model thus (nonsensically) gives identical predictions of bias for a given

weight difference, with either positive or negative density differences. In principle, a prior over

weight and density difference is more plausible, given that our descriptive model predicts

perceived weight difference as a function of weight difference and density difference. In

practice, however, this model provides a worse fit to the observed biases in perceived weight

difference (mixture of 2 Gaussian priors, 8 parameters; R^2 = .7690, SSR = 87140) than our

descriptive model (which reduces to 4 parameters when predicting perceived weight

differences, see Equation 2; R^2 = .9117, SSR = 1025.1). Moreover, the model predicts a

completely different pattern of variance in estimated weight difference than the one observed

(R^2 = .0017, p = .55).

4.3 Other models

We also fitted existing models by Bays (29), Peters and colleagues (28), and Wolf and

colleagues (9) (see Introduction) to our data.

Bays (29) proposed a Bayesian model of the SWI, which, as above, predicts biases away

from the prior, given efficient coding and an L2 loss function (30). However, rather than

considering object pairs, Bays' model employs a bivariate Gaussian prior over the perceived

weight and volume of single objects, i.e., a positive association between weight and size.

Supplementary Figure S3 shows the model's fit to our data. We extended the model to

incorporate a mixture of Gaussians prior (see SI, Table S4 for model parameters and model

comparisons). Whilst the model captures the mean bias for each stimulus reasonably well, it

cannot capture the way in which perceived weight is modulated by the other object in the pair,

nor is it consistent with the pattern of response variance (see SI Figure S2).

We fitted Peters and colleagues' (28) model to our data. As described in the

Introduction, Peters and colleagues assume a prior over weight and density ratio that is

comprised of three sub-priors, representing three different classes of weight-density

relationships (here re-expressed as weight-volume relationships, see Figure 1C). Figure 7

shows the empirical biases in perceived log weight ratio (A) and the predicted biases from the

best-fitting model parameters (B). Sub-priors (represented by dashed lines) are encoded as

bivariate Gaussians (See SI, Table S5 for model parameters and model comparisons).

Unfortunately, the model cannot account for the set of biases in perceived log weight ratio

across all stimulus pairs (R^2 = 0.413). It predicts a negative influence of log density ratio for

some stimulus pairs; the predicted effect depends on where the stimuli lie relative to the three

sub-priors. For example, in pairs of equal-volume (different weight, density) stimuli, log weight

ratio is predicted to be underestimated as log density ratio, log weight ratio increase, whereas

empirically it is overestimated.

Figure 7 Biases in perceived log weight ratio. Dotted lines show the optimal three sub-priors from Peters and colleagues' model when fitted to our data. Black dots show the stimulus pairs; arrows show the magnitude and direction of the bias. (A) empirical biases; (B) predicted biases according to Peters and colleagues' model.

503   Finally, we evaluated Wolf and colleagues' (9) model with our data. In this model,

504   perceived weight is a weighted average of weight and density estimates, weighted according to

505   their relative reliabilities. Estimates are modelled as power functions of the corresponding

506   physical feature. As we didn't manipulate the reliability of size information, the model reduces

507   to:

508                                    $$\widehat{w} = \beta_1 w^x + \beta_2 d^y$$ (4)

The model provides a reasonable account of perceived weight (R^2 = .96), although, like

Bays' (29), it does not capture the contextual effects of the other object. Figure S5 (SI), shows

Wolf and colleagues' (2018) model fit to our data, for comparison with Figure 3; for model

parameters and model comparisons see SI Table S6). Wolf and colleagues (9) suggest that the

influence of density on heaviness perception depends solely on the reliability of size

information used to infer density. In our experiment, therefore, with full access to visual and

haptic cues, the contribution of density should have been constant. However, the influence of

density was strongly modulated by weight difference (as shown in Figure 4A). As presented, our

model does not encapsulate the additional effect of varying the reliability of size estimation;

this would be accommodated by modulating the coefficients associated with density to reflect

the availability of visual-haptic size cues (β_2, β_4, β_5, Equation 1). Lastly, Wolf and colleagues'

model perceived weight and density as power functions of their physical counterparts.

However, additional exponent parameters for weight or density were not statistically supported

by our data. Wolf and colleagues had a 5:1 ratio of heaviest to lightest stimuli, compared to our

reduced 3.3:1 ratio. It is likely that, given an increased range of stimulus weights / densities,

our descriptive model would need to similarly include power functions of weight and / or

density, in tandem with setting our intercept to 0.

5. Discussion

We investigated perceived heaviness in a set of stimuli which varied in weight and / or

volume, and / or density in small steps. We report several novel findings: 1) The SWI occurs

even at very small density (size) differences; 2) Across all stimuli, an object's weight and density

are confounded / integrated to estimate weight; 3) Perceived weight is affected by the weight of

the other object in a pair, but is largely invariant to the other object's density. 4) However, the

influences of both objects' densities on perceived weight are strongly modulated by weight

difference, with a negative, or 'contrast' effect of the other object's density appearing for similar

weight pairs.

Our descriptive model captures the above effects, providing an excellent account of

perceived heaviness (R^2 = .98) that captures the SWI as well as biases in perceived weight

across a range of variations in pairings of stimulus weight and density. Additionally, we

evaluated a novel efficient-coding Bayesian model of perceived weight ratios, alongside

previously proposed models of the SWI. Here we will discuss our findings within the existing

literature.

The magnitude of the SWI increased, as expected, with increasing density (size)

difference (28,34,38,40). We extended this, by measuring the SWI with smaller density

differences than those previously tested. We hypothesised that under small conflicts, the SWI

might reverse (i.e., to show integration: smaller stimuli would be perceived as lighter). However,

the SWI was clearly present for all equal-weight pairs, at odds with the idea that the SWI is

driven by a (substantial) conflict between expected and perceived weight.

Our results are inconsistent with Peters and colleagues' (28)Bayesian mixture model.

Also, at a conceptual level, the subdivision of the continuous world of size and volume/density

into three relatively narrow categories is difficult to reconcile with environmental statistics. The

best fitting parameters for our data assigns a prior probability of near 0 to equal-density objects

(R_1, see Figure 7, and SI, Table S5). The other two sub-priors encapsulate the expectation that

smaller objects are either much heavier and denser (R_2) or much lighter and less dense than

larger ones (R_3), both at odds with reported natural statistics for everyday liftable objects (27).

The efficient-coding Bayesian ratio model provides a theoretically appealing account of

the SWI, predicting a repulsion away from a plausible equal-density prior. However, neither our

efficient-coding Bayesian ratio model, nor that recently proposed by Bays (29) satisfactorily

account for our pattern of data. Whilst our efficient-coding model provides a reasonable fit to

the empirical biases in perceived log weight ratio, the inferred biases in perceived log w_1 and log

w_2 do not match those observed (which are largely invariant to the ratio of the two densities). In

addition, as highlighted by the descriptive model, the perceived weight of an object is *only*

influenced by the other object's density when the two weights are similar, i.e. when

discrimination thresholds are smallest. In contrast, the efficient-coding Bayesian model

predicts that biases will be smallest when discrimination is best (see SI, Figure S2).

As noted above, neither Bays' model (29) nor Wolf and colleagues' model (9) account

for contextual bias effects found in our data (influence of w_2 and, in certain conditions, d_2), and

neither is Bays' model consistent with empirical patterns of response variance.

So, is the SWI Bayesian after all? We don't think so; the SWI does not appear to be

caused by repulsion from an equal-density prior. It is reasonable to assume that the perceptual

system does expect same-material objects to be same-density. Indeed, the sensorimotor

system may rely on an object's size, together with density expectations for classes of objects /

materials to infer the weight of a stimulus prior to lifting (12). Such expectations presumably

drive the initial (erroneous) forces used when lifting SWI objects (55). However, the illusion

persists after forces quickly adapt to the true weights, and the SWI is just as large when same-

density cues are reduced, i.e., when the colour or surface material of the two stimuli differs

(56,57).

In general, perceived weight was modulated by density; denser objects are perceived as

heavier than less dense objects, consistent with previous literature (9). In line with Wolf and

colleagues (8,9) weight does appear to be routinely confounded / integrated with density

information. However, our data reveal that the effect of density is substantially increased when

equal-weight objects are encountered, as in the typical size-weight illusion. Thus, like Bays' (29)

model, Wolf and colleagues' (9) model fails to capture the contextual effects of the other

object. Rather, these models predict biases in perceived weight that occur in single-object

judgements (see, e.g., (58)). Obviously, object perception occurs in various contexts, not only

object pairs. Our model could be generalised to judgements of single objects, by replacing the

other object's properties with a weighted combination of previously encountered stimuli.

6. Conclusions

Our study situates the SWI in the broader context of weight perception under varied conditions (combinations of volume, weight, and density) allowing us to evaluate different models of weight perception, including our own model.

Our explorations reveal that, whilst the SWI magnitude increases with size / density difference, it occurs even for small density differences. Second, we showed that typical SWI experiments have inflated estimates of the influence of density on weight perception more generally. The effect of density on perceived weight is substantially smaller when two objects of different weights are encountered. Our simple model provides an excellent *descriptive* account of perceived weight under various combinations of size, weight, and density. Our model, however, is not explanatory: We still don't know why the SWI occurs. Why do we conflate weight and density, and why is this effect magnified when weight differences are small?

We explored different avenues to reconcile the SWI within the Bayesian framework, given the appeal of finding a model that could provide an explanatory account of weight perception in the SWI and beyond. However, none of the Bayesian models we tested, including efficient-coding models that do predict biases away from a prior, could successfully account for our data.

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