Spatiotemporal structure and substates in facial expressions and speech

movements

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Abstract

Ranging from overt emotion displays to the understated eyebrow raise accompanying speech, facial expressions are indispensable cues in social interaction. Yet, how these inherently dynamic cues contribute to emotion signalling remains only partially understood. One overlooked factor is how facial actions combine and recombine over time to produce nuanced expressions. Moreover, although most face-to-face interactions naturally involve speech, its contribution to facial emotion signalling has been largely neglected. Building on motor control principles and employing a novel data-driven pipeline - combining spatiotemporal dimensionality reduction, dynamic feature extraction, classification and clustering - we investigated the structure and function of facial dynamics in both *Expression only* and *Emotive speech* signals. We show that a few fundamental spatiotemporal patterns reliably differentiated between specific emotion dynamics such as happy, sad and angry as well as between *Expression only* and *Emotive speech* signals. Furthermore, these spatiotemporal components exhibit meaningful substates, which reflect transient dynamics that are diagnostic of emotion content. This underlying spatiotemporal structure represents an efficient encoding strategy, optimising the transmission and perception of emotion and non-emotion facial signals. These findings have implications for understanding normative and "atypical" face-to-face signalling and can inform the design of expressive emotive capabilities in artificial social agents. Moreover, our data-driven pipeline can be extended to study broader aspects of multimodal social signalling.

Keywords: Facial expressions, movement, spatiotemporal, dimensionality reduction, emotion, signalling.

Significance Statement

In face-to-face interactions, facial movements convey both emotional and speech-related information, yet their complex dynamic signalling remains only partly understood. This study explores how facial movements evolve over time, integrate emotional and speech cues. Using advanced techniques to measure and analyse moment-to-moment changes in dozens of facial muscles we identified fundamental movement patterns that differentiate emotional signals. These dynamic patterns enable both isolated emotional signalling and simultaneous emotion cues during speech. These findings can inform understanding of typical and atypical face-to-face interactions abilities and enhance the design of human-like facial expressions in social robots and virtual agents. We also contribute a novel data-driven pipeline for analysing facial dynamics, applicable to broader facets of multimodal social communication.

Introduction

The human face is an incredibly versatile signalling tool for social interaction (1) capable of producing a rich array of non-verbal signals through the coordination of basic motor facial action units (AUs) (2). For example, frowning (AU4) combined with pursed lips (AU24) can convey a prototypical facial expression of anger; while raising the cheeks (AU6) and pulling back the lip corners (AU12) can signal a smile. In addition to ostensive non-verbal emotional cues, in real-life social interaction, facial expressions simultaneously modulate verbal communication. A slight tightening of the eyelids (AU7) for example, can make a "neutral" verbal utterance appear slightly angrier. The mechanisms that afford such flexible expressive capabilities to facial expressions remain only partly understood.

One overlooked aspect in previous research is the dynamic nature of facial expression signalling, with a large focus instead on the static aspects of facial behaviour or approaches ignore temporal dynamics (3). Moreover, although most face-to-face interactions naturally involve speech, the role of speech-related facial dynamics in emotion signalling has been largely neglected. Yet these dynamic cues in conversational or speech-related facial expressions can enhance the simultaneously transmission of visual signals for emotion and verbal communication (3–6). Nonetheless, a few key studies have provided important insights on the role of facial expression dynamics to emotion signalling. Psychophysics inspired approaches have combined generative synthesis of facial movements (7) and reverse correlation to parametrically map the spatiotemporal features of AUs to perceptual representations of emotion categories (8), valence-arousal dimensions (9) and even social traits (10). Similarly, a recent production and perception study recorded participants' facial

movements during signalling of anger, happiness, and sadness, as well as during

spoken sentences conveying the same emotions (11). Kinematic analysis revealed

faster movements for high-arousal emotions (happiness, anger) compared to slower

movements for low-arousal emotions (sadness). Thus, suggesting that facial

dynamics carry a diagnostic signal for differentiating emotional expressions at both the

production and perception stages.

Nevertheless, a detailed account of the spatiotemporal structure of facial signals—

how AUs dynamically combine and unfold to signal emotions and simultaneously

convey speech-related information—remains lacking. One significant challenge to

studying the role of spatiotemporal structure in facial expression signalling is the lack

of an integrated theoretical and methodological framework. Such a framework should

ideally integrate the dynamic nature of facial expression signals with their socio-

communicative functions and provide an appropriate modelling strategy. In this work,

we build on the observation that facial expressions, like other facial and bodily

movements, are controlled by an underlying motor system (12, 13). We explore the

application of theoretical and analytical principles drawn from the motor control

literature to understand the spatiotemporal structure and function of dynamics in facial

expressions.

A motor control perspective provides two useful insights that are applicable to studying

the spatiotemporal structure and function of facial expression dynamics. First, a

longstanding motor control hypothesis suggests that body movements are generated

by a low-dimensional mechanism that underpins their effective neural control and

physical execution (14–16). Such low-dimensionality of motor control and execution

might reflect the brain's solution to the problem of controlling numerous muscles and components of the motor system whilst minimising computational demands - often referred to as the "degrees of freedom" problem (17–19). Crucially, such low dimensionality has been shown to describe motion patterns during walking (20), whole body pointing (21), eye movements (22) and articulatory speech movements (23). These movements also convey emotion-related information (24–26) suggesting the potential for shared control mechanisms for social and non-social aspects of movement. Similarly, dynamics underlying facial expressions, and their ability to multiplex information (e.g., visually signal emotion and speech), may be structured around flexible low-dimensional spatiotemporal patterns. Such low dimensional patterns could, for example, reflect how AUs combine and evolve over time during facial expression production and simultaneously encode emotion in speech-related facial movements. This perspective also suggests a methodological framework to model spatiotemporal nature of movement, which is rare in the study of facial expression production. For instance, this can be explored using data-driven models that learn a reduced dimensionality from high-dimensional AU movement data (27).

A second insight from the motor-control literature is the observation that although outwardly fluid, body movements can often be segmented into distinct 'substates' often seen in differential modulation of kinematics (e.g., speed, displacement of motor actions). For instance, walking movements can be segmented into 'swing' or 'stance' phases (20) or eye movements into 'fixations' and 'saccades' (28), and even more fine-grained states (sub movements) (29). Facial expressions are likely to have substates related to the biomechanics of how they are produced, encompassing 'transitions'—where AUs are initiated or inhibited, - and 'stability' – where AUs are sustained (30,

31). However, to date facial expressions substates of facial expressions and speech

movements have not been formally characterised, and whether and how they relate

to emotional signalling is unknown. Similar to spatiotemporal components, substates

can be explored in a data-driven fashion, using methods such as spatiotemporal

clustering (27, 32, 33) without *apriori* defined kinematic profiles.

Some prior work has indeed proposed and employed similar motor-centric theoretical

and methodological approaches to account for and leverage the rich dynamics of facial

signals in perception and production of emotion cues. Arguably, the majority and

significant contributions in this area have focused on perception e.g. - (8, 34) rather

than production which is the focus of the current study. Notwithstanding, a few recent

studies have employed motor-informed spatiotemporal dimensionality reduction

approaches to identify dynamic motifs in facial expression production data (e.g. (18,

35, 36). Nonetheless, the reliance on only single to a handful signallers or actors

arguably limits the dynamic range and variability the facial signals analysed. Hence,

it's unclear whether the observed low dimensionality in these studies, genuinely reflect

the underlying mechanisms for facial expression signalling or simply results from

restricted variability in signal dynamics. It is also unclear how well these findings

generalise to other emotional expressions and conditions (e.g., emotive speech facial

dynamics), and signallers. Furthermore, the majority of these studies still relies on

averaging across the spatiotemporal dimensions when comparing expressions and

conditions, potentially overlooking how inherent dynamic patterns relate to emotion

signalling (see Methods). Consequently, the functional role of facial dynamics—

including both low-dimensional spatiotemporal patterns and substates—in emotional signalling remains only partially explored.

In contrast, probing the underlying spatiotemporal dimensions and substates in facial expressions enables a richer characterisation of facial dynamics that is both holistic, i.e., captures overall spatiotemporal patterns, but also focal as it can capture micro spatiotemporal patterns in movement data. Crucially, we hypothesise that these underlying patterns are not merely incidental; rather, they are diagnostic of emotional content, reflecting how facial movements are optimised for social signalling.

The current study therefore aims to (1) describe the spatiotemporal structure underlying facial expression production; (2) explore and characterise potential facial expression substates, and 3) evaluate the diagnostic value of spatiotemporal structure and substates for emotion signalling. To capture wider facial dynamics relevant for social interaction, we recorded participants facial movements while they signalled different emotions in a) *Expression only* and b) *Emotive speech* conditions across two separate sessions. We used automated Facial Action Coding System (FACS) to describe the spatiotemporal patterns of the facial AUs (e.g., mouth widening, eyebrow raise, etc). We then employed a novel data-driven pipeline combining dimensionality reduction, dynamic feature extraction, and spatiotemporal classification and clustering; to identify diagnostic latent spatiotemporal patterns (groups of co-activated AUs and salient temporal patterns) underlying optimal emotion signalling in both Expression only and Emotive speech facial dynamics.

To precis our results, we find that *Expression only* and *Emotive speech* facial dynamics can be distilled into a of small set of fundamental spatiotemporal

components that form the basis for flexible signalling. Specifically, the three emotions

(happy, angry, sad) and two conditions (*Expression only* and *Emotive speech*) studied

are differentiated by synergistic mixing of components and subtle local substate

differences related to expression transitions. These results suggests that the complex

and flexible signalling of emotional through facial movements, is achieved through

variations in a small number of spatiotemporal components and substates.

Results

Spatiotemporal components for facial expression production.

We report results for *Expression only* and *Emotive speech* expressions separately for

clarity, however we note that these patterns were consistent when analysed together.

<u>Spatiotemporal patterns during facial *Expression only* condition</u>

We first looked at the spatiotemporal components identified via the Non-Negative

Matrix Factorization (NMF), which represent the underlying (reduced) spatiotemporal

patterns (e.g., groups of AUs with common activation timecourses and salient

temporal patterns). The optimal number of spatiotemporal components (k) optimising

for various fit indices (see Methods) – was consistently three (see Fig 1 – top panel)

(see also *Expression only* condition - NMF validation analysis in Supplementary

Information – Fig S1-3).

Figure 1. Spatiotemporal components for facial expressions only production.
The top panel (A) shows that expression production can be summarised by three components, capturing spatiotemporal patterns for upper face AUs (component 1), lower face AUs (component 2) and a combination of both lower and upper face AUS (component 3). Top - middle and right columns show approximate spatial distribution of components in an average face model and how it changes over time, respectively. The bottom panel (B) highlight spatiotemporal profiles for angry, happy and sad expressions. Coef = coefficient from the NMF, brighter colours indicate stronger activation. Note while heatmaps are drawn to scale, face maps are drawn for visualisation purposes only.

Evaluating the spatiotemporal patterns revealed that component 1 (C1) had stronger

activation of the upper face-related AUs (e.g., AU4 brow lowerer, AU7 lid tightener)

compared to other AUs. Component 2 (C2) had strong activation of both lower and

upper face-related AUs (e.g., AU25 lips part, AU14 dimpler). Component 3 (C3) was

mostly dominated by lower face actions (e.g., AU17 chin raiser) with some small

activation of upper face AUs (e.g. AU45 blink). We name these components, upper

face AUs (C1), lower face AUs (C2) and lower-to-upper face AUs (C3). The temporal

profile of these components is shown in Fig 1 B. C1 (upper face AUs) and C2 (lower

face AUS) had a common inverted-U shape with a clear singular peak, whereas C3

(lower to upper face AUs) had a less pronounced but more dynamic pattern (e.g.

bimodal peaks).

Next, we assessed the diagnostic value of the spatiotemporal components, by

analysing how their dynamic features differed between expressions and validated it in

a held-out test set (see Methods - *Multivariate Timeseries Classification*). When

assessing spatiotemporal components' ability to classify expressions we achieved

significantly above chance accuracy of over 90% (ACC (accuracy)= 0.91 [BalACC

(balanced accuracy) = .93], Kappa = 0.87; AUC(Area Under the Curve) mean = 0.98,

$p < .001$ see Fig 2). These results indicate strong agreement between prediction and

ground-truth – see also SI1 – Table S1-2

Figure 2. Spatiotemporal classification of facial expressions only production.
Notes: The left panels show decision boundaries (filled backgrounds) across spatiotemporal components (Comp1: upper AUs, comp2: lower face AUs; comp3: lower to upper face AUs) estimated on a training set to predict emotion classes (angry, happy, sad). Coloured dots represent individual ground-truth expressions from both training and held-out test data. Dots within a matching background indicate correct classifications, while mismatches indicate misclassifications. The results demonstrate robust classification, with at least one component combination separating an expression from the rest. e.g. comp1 vs 2 and comp-2 vs 3 robustly distinguishes happy expressions. The top right panel presents Receiver Observer Characteristics (ROC) curves, showing good model performance (higher True Positive Rate [TPR] and lower False Positive Rate [FPR]) with the diagonal dashed line representing chance). The bottom right panel displays a confusion matrix. Brighter colours indicate higher accuracy along the diagonal elements, with off-diagonal showing little to no confusions (darker colours).

We also found distinct temporal profiles for each emotion. Angry expressions (BalACC

= .91, AUC=.97, p < .001) were characterised by strong temporal coactivation of C1

(upper face AUS) and C2 (lower face AUS). Happy expressions (BalACC = .98, AUC

= .99, p < .001) were dominated by C2 (lower face AUs); and sad (BalACC = .98, AUC

= .90, p<.001) characterised by moderate changes in all three components. To further

validate our model, we conducted a Fisher's exact test on the confusion matrix (see

Methods), which confirmed significant pairwise differentiation of all expressions on the

basis of their spatiotemporal patterns (angry vs happy; angry vs sad; and happy vs

sad: p.corrected < .001). These results reinforce the robustness of our classification

model, demonstrating that spatiotemporal patterns differ between emotional

expressions.

<u>Spatiotemporal patterns for *Emotive speech* facial expressions</u>

Similar to the *Expression only* condition, we found that three components effectively

represented the spatiotemporal patterns of facial AUs in *Emotive speech* expressions

(see SI1 – Fig S4-6). However, there were some notable differences in the spatial and

temporal patterns, which likely reflect the fact that, in contrast with the *Expression only*

videos, the *Emotive speech* videos comprise a combination of facial expression and

speech AUs. Specifically, the *Emotive speech* components comprised a mix of both

lower and upper face AUs, in comparison to mostly lower vs upper face AUs for

Expression only conditions (see Fig 3).

Figure 3. Spatiotemporal components for *Emotive speech* facial expression production. The top panel (A) shows that *Emotive speech* facial expression production can be summarised by three underlying components, capturing synergies between upper to lower face AUs (Component 1), lower-mid-upper AUs (component 2) and lower to upper face AUs (component 3). Top - middle and right columns show approximate spatial distribution of components in an average face model and how it changes over time, respectively. The bottom panels (B) show how components change over time, highlighting different profiles for angry, happy and sad expressions. Coef = coefficient from the NMF, brighter colours indicate stronger activation. Note while heatmaps are drawn to scale, face maps are not a one-to-one map and are drawn for visualisation purposes only.

Component 1 included strong activation of upper and lower face Aus (e.g., AU4 - brow lowerer; AU17 - chin raiser) peaking at both early and late time points. Component 2

(lower-mid-upper face AUs) combined strong activation of AUs in the lower (e.g., AU25

- lips part), middle (e.g., AU14 - dimpler) and upper face areas (e.g., AU7 - lid

tightener). Component 3 primarily featured activation of lower face AUs, such as AU25

(lips part) and AU26 (jaw drop), plus additional moderate activation for AU 45 (blink).

Henceforth component 3 is referred to as lower to upper face AUs (see Fig 3). C2

(lower-mid-upper face AUS) and C3 (lower to upper face AUs) had an inverted-U

shape with C3 peaking earlier than C2 (Fig 3C).

As with facial *Expression only* production, *Emotive speech* expressions were also

characterised by distinct spatiotemporal patterns. That is, a classifier trained on

timeseries-based features of the spatiotemporal components (e.g., curvature, entropy)

achieved significant accuracy in classifying expressions on a held-out test set, with

performance at 70% (ACC = 0.69, 95% CI: 0.53, 0.81; BalAcc = .76 Kappa = 0.53, p

< 0.001). These results indicate moderate to strong agreement between prediction

and ground-truth emotional expression labels.

Class-wise, the spatiotemporal components significantly distinguished all expressions.

Happy had the highest accuracy (BalACC = 0.91, AUC = 0.97, p < .001), suggesting

a clear and distinct spatiotemporal profile, notable in the increased activation in C2

(lower-mid-upper face AUs) over time (see Fig 4).

Figure 4. Spatiotemporal classification of *Emotive speech* facial expressions.
The left panels show decision boundaries (filled backgrounds) across spatiotemporal
components (comp1: upper to lower face AUs, comp2: lower to upper face AUs;
comp3: upper-to-lower face AUs) estimated on a training set to predict emotion
classes (angry, happy, sad). Coloured dots represent individual ground-truth
expressions from both training and unseen test data. Dots within a matching
background indicate correct classifications, while mismatches indicate
misclassifications. The results demonstrate robust classification, with component
combinations effectively separating the expressions in at least one combination.
The top right panel presents ROC curves, showing good model performance (higher
True Positive Rate [TPR] and lower False Positive Rate [FPR]), with the diagonal
dashed line representing chance. The bottom right panel displays a confusion matrix.
Brighter colours indicate higher accuracy along the diagonal elements, and confusion
off-diagonal (e.g., happy shows high accuracy and low confusion, whereas angry
shows higher confusion than all expressions).

Angry had the lowest classification accuracy compared to all other expressions, yet
still significantly above chance (BalACC = 0.67, AUC = 0.83, p = .01), reflecting a more
complex and less distinct pattern across all components. Similar to happy, sad
expressions were classified reliably above chance (BalACC = 0.72, AUC = 0.84, p =
0.001). Fisher's exact test on the confusion matrix confirmed significant pairwise
differentiation between happy and sad expressions (p < .001) and between angry and

happy (p < .001). However, it suggested confusions between and angry and sad (p =

0.12) (see Fig 4; SI1 - Table S3-4).

In summary, we found three latent spatiotemporal components that reliably described

the dynamics of facial expressions during *Expression only* and *Emotive speech*

conditions. Robust train-test classification on unseen held-out data, indicates that

spatiotemporal components carry information that is diagnostic of emotional content.

Substates reveal emotion diagnostic transitory patterns and sequences in facial

signals

The second objective of this study was to identify and characterise facial expression

substates, such as transition and sustain periods, and their diagnostic value for

emotion signalling (i.e., whether they differ between emotions: happy, angry and sad

expressions). We identified three primary substates through spatiotemporal clustering

that segmented periods with robust local dynamics in the spatiotemporal components

(see Methods: *Spatiotemporal clustering for substates analyses*). Visual

representation of the kinematic profiles of each substate (Fig 5A-B) suggest the

substates correspond to relaxed, transition, and sustain periods for spatiotemporal

components. The overall pattern of substates is also consistent across participants

(see Fig 5 C-D).

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Figure 5. Illustration of facial expression substate profiles.
A-B. Example of substate clusters (1 (green) = relaxed, 2 (peach) = transition; 3
(purple) = sustain). C-D show overall the speed distribution for *Expression only* and
Emotive speech expressions for all subjects.

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To illustrate the pattern of facial expression substates and how it differs between

emotions (anger, sadness and happy) and conditions (*Expression only vs Emotive*

speech), we computed two metrics: (1) speed within the substate hence providing a

kinematic characterisation of each substate, and (2) entropy, which provides a view of

overall dynamics of substates (e.g., how they change over time) (Fig 5) – see also

Methods. Similar measures have been shown to capture diagnostic information about

facial expression movement patterns (8, 11).

<u>Transition substate speeds differentiate emotional expressions</u>

A mixed-effects model (see Methods) predicting speed from emotion (happy, angry,

sad), condition (*Expression only, Emotive speech*), and substate (relaxed, transition,

sustain) showed strong total explanatory power (conditional R2 = 0.6 (66%)) with the

fixed effects alone (marginal R2) accounting for 0.63 (63%) of the variance. All main

effects were significant. First, there was a small significant effect of emotion ($F_{(2,1990)}$

= 12.89, $p < .001$; η_p^2= 0.02, 95% CI [0.009, 0.10]). Pairwise tests showed that angry

expressions were significantly slower than happy expressions (angry < happy; beta =

-0.028, SE = 0.008, t(1207) = -3.398, p = 0.002). Happy expressions were faster than

sad expressions (happy > sad; beta = 0.041, SE = 0.008, t(1207) = 4.92, $p < 0.001$).

There were no significant differences in speed between angry and sad expressions

(beta = 0.012, SE = 0.008, t(1207) = 1.53, p.corrected = 0.38). There was a significant

main effect of condition ($F_{(1, 1190)}$ = 369.41, $p < .001$; η_p^2 = 0.24, 95% CI [0.20, 1.00])

with *Expression only* condition moving faster than spoken (beta = 0.13, SE = 0.007,

t(1207) = 19.08, $p < .001$). Finally, there was a main effect of substate ($F_{(2, 1190)}$ =

687.90, $p < .001$; η_p^2 = 0.54, 95% CI [0.51, 1.00]) where sustain had higher speed than

relaxed (beta = -0.16, SE = 0.008, t(1207) = -19.52, p.corrected < .001); transition had

higher speed than relaxed (beta = -0.307, SE = 0.008, t(1207) = -36.80, p.corrected <

.001) and transition had higher speed than sustain (beta = -0.144, SE = 0.008, t(1207)

= -17.28, p.corrected < .001).

All three two-way interactions were significant. First, there was a significant interaction

between emotion and substate ($F(4, 1190) = 15.24$, $p < .001$; $\eta_p^2 = 0.05$, 95% CI [0.03,

1.00]). Pairwise tests showed that differences in speed between happy, angry and sad

emotional expressions were statistically significant for the transition substate only

(happy>anger, beta = -0.077 SE = 0.014, $t(1207) = -5.36$, p.corrected < .001; sad<

angry, beta = 0.053, SE = 0.014, $t(1207) = 3.64$, p.corrected < 0.001; sad< happy,

beta = 0.130, SE = 0.014, $t(1207) = 9.005$, p.corrected < .001). There were no speed

differences between emotions for the relaxed substate (angry vs. happy, beta = -0.005,

SE = 0.014, $t(1207) = -0.348$, p.corrected = 1.0; angry vs. sad, beta = 0.007, SE =

0.014, $t(1207) = 0.498$, p.corrected = 1.0; happy vs. sad, beta = 0.012, SE = 0.014,

$t(1207) = 0.846$, p.corrected = 1.0) nor the sustain substate (angry vs. happy, beta =

-0.003, SE = 0.014, $t(1207) = -0.177$, p.corrected = 1.0; angry vs. sad, beta = -0.022,

SE = 0.014, $t(1207) = -1.501$, p = 0.40, p.corrected; happy vs. sad, beta = -0.01913,

SE = 0.0144, $t(1207) = -1.325$, p.corrected = 0.5567). These results suggest that

transition substate kinematics (but not relaxation or sustainment kinematics) carry

diagnostic information about the emotional content of facial expressions (Fig 6).

Figure 6: Summary of speed and entropy of substate patterns.

Substate cluster: 1-relaxed, 2-sustained, 3-transition. *Expression only* condition has faster than *Emotive speech*, with transition substates being faster; Entropy mainly differentiates *Expression only* and vs*. Emotive speech* condition, with the latter exhibiting more complex patterns. Entropy also differed between happy and all other expressions, with substate patterns being more predictable for former.

In addition, there was a significant two-way interaction between emotion and condition ($F(2) = 3.54$, $p = 0.029$; $\eta_p^2 = 0.006$, 95% CI [3.15e-04, 1.00]). For the *Expression only* condition, there were significant speed differences between two out of the three emotion expression pairs: specifically, happy > angry (beta = -0.045, SE = 0.012, $t(1207) = -3.84$, p.corrected < 0.001); happy > sad (beta = 0.06171, SE = 0.0118, $t(1207) = 5.232$, p.corrected < .001); and no differences between angry vs. sad (beta = 0.016, SE = 0.012, $t(1207) = 1.39$, p.corrected = 0.492). In contrast, for the *Emotive speech* condition, there were no significant differences in speed between the emotional expressions (angry versus happy, beta = -0.011, SE = 0.012, $t(1207) = -0.97$, p.corrected = 1.0; angry versus sad, beta = 0.009, SE = 0.012, $t(1207) = 0.77$, p.corrected = 1.0; happy versus sad, beta = 0.020, SE = 0.012, $t(1207) = 1.73$, p.corrected = 0.25).

Finally, there was a significant two-way interaction between condition and substate ($F(2) = 183.65$, $p < .001$; $\eta_p^2 = 0.24$, 95% CI [0.20, 1.00]). For the *Expression only* condition, there were significant differences in speed between all substates such that sustain was faster than relaxed (relaxed < sustain, beta = -0.153, SE = 0.012, $t(1207) = -12.96$, p.corrected < .001); transition was faster than relaxed (relaxed < transition, beta = -0.439, SE = 0.012, $t(1207) = -37.23$, p.corrected < .001), and faster than sustain (beta = -0.286, SE = 0.0118, $t(1207) = -24.271$, p.corrected < .001). These patterns were overall similar for the *Emotive speech* condition where relaxed periods were significantly slower than sustain (beta = -0.173, SE = 0.0118, $t(1207) = -14.647$,

p.corrected < .001) and transition periods (beta = -0.175, SE = 0.012, t(1207) = -14.82,

p < .001). However, there was no statistically significant difference between sustain

and transition speeds (beta = -0.002, SE = 0.012, t(1207) = -0.169, p.corrected = 1.00).

In sum, speed analysis confirm that subset clustering is associated with differences in

kinematics, and these also differs between expressions and between *Expression only*

and *Emotive speech* signals.

<u>Substate dynamics differentiate emotion content</u>

Here we used entropy as a metric to statistically describe the dynamics of facial

expression substates in terms of how temporally structured/predictable they are ((37).

see Methods). High entropy equates with high complexity in substate patterns, and

low entropy with low complexity. Fig 5, for example, illustrates that substate transitions

are more complex (i.e., high entropy, less predictable) in the *Emotive speech* condition

where visual pattern differences between emotions are harder to discern than in the

Expression only condition (see Methods: *Spatiotemporal clustering for substates*

analyses).

The entropy mixed model explained 67% of the variance (R^2 = 0.67). The fixed effects

alone (emotion, and expression condition) accounted for 57% of the variance

(marginal R^2 = 0.57). The main effect of emotion was statistically significant (F(2, 340)

= 12.27, p < 0.001; ηp^2 = 0.07, 95% CI [0.03, 1.00]). Pairwise contrasts revealed that

sad expressions had a significantly higher entropy (more unpredictable substate

sequences) compared to happy expressions (estimate = -0.027, SE = 0.0055, t(344)

= -4.897, p < 0.0001). There were no statistically significant differences in entropy

between angry and happy expressions (estimate = 0.011, SE = 0.006, t(344) = 1.996,

p = 0.14), but there was a significant difference between angry and sad expressions

(estimate = -0.016, SE = 0.0055, t(344) = -2.90, p = 0.012).

The largest effect was the main effect of condition (F(1, 34) = 429.10, p < 0.001; ηp²

= 0.93, 95% CI [0.89, 1.00]), with the *Expression only* condition demonstrating

significantly lower entropy than *Emotive speech* expressions (β = -0.208, SE = 0.017,

t(35) = -12.594, p < 0.001). This suggests more complex movement dynamics in the

Emotive speech compared to the *Expression only* condition (see heatmaps in Fig 5).

There was no significant interaction between emotion and condition (F(2, 340) = 0.03,

p = 0.970; ηp² = 0.0002, 95% CI [0.00, 1.00]). In summary, *Expression only* substates

are more temporally structured than those in *Emotive speech* expressions.

Nonetheless, substates patterns differentiate expressions with sad expressions

having a more complex pattern of substates than happy and sad expressions.

To summarise, in addition to the low-dimensional spatiotemporal patterns that are

diagnostic of emotion and expression condition, we also identified three substates

reflecting periods of relaxation, transition, and sustainment of facial actions. These

substates are distinguished by their unique kinematic and dynamic (complexity)

profiles which differ between emotional expressions and *Expression only* versus

Emotive speech conditions.

Discussion

The current study explored how the underlying dynamics of facial movements relate

to their emotional signalling function. Building on a motor-theoretic inspired approach

we employed a novel data-driven pipeline - integrating spatiotemporal dimensionality

reduction, timeseries feature extraction, classification and clustering; to identify

diagnostic patterns underlying emotion signalling in both *Expression only* and *Emotive*

speech. We consistently identified a small number of components that reliably

described the time courses and covariance patterns of over a dozen action units. The

identification of these components suggests that emotion signalling through facial

expressions and speech-related cues is achieved by just a few fundamental dynamic

patterns; combinations of these dynamic patterns differentiate angry, happy and sad

expressions. Second, we showed that these spatiotemporal patterns exhibit substate-

like structure, which reflect transient periods of relaxation, transition, and sustainment

of expressions. The kinematic profiles of these substates differed by emotion category

as well as between *Expression only* and *Emotive speech* conditions.

The low dimensionality of the spatiotemporal patterns of facial expressions, that we

have uncovered, is intriguing given the various combinations of AUs that can

contribute to the same expressions (3) as well as the variability in how people produce

expressions (38). A low-dimensional spatiotemporal structure may reflect flexibility for

signalling, as a variety of expressions can be rapidly produced by relying on just a few

interchangeable dynamic patterns. Such flexibility is likely beneficial in face-to-face

interaction, where facial expressions may need to be quickly adapted according to

interaction demands (3, 39) or where it is necessary to accentuate emotional

information during speech (4, 40). These findings are also consistent with the

observation of low-dimensional spatiotemporal patterns facial (18, 36) as well as other

body movements (17, 19, 21) which also have the capacity to signal emotion

information (24, 41, 42). Thus, it suggests the potential for shared control mechanisms

for social and non-social aspects of movement including speech movements.

An important question concerns whether our results are representative of facial

expression signalling in general, or simply an outcome of the particular methodology

we employed. For example, it could be argued that we identified a small number of

spatiotemporal components because we asked participants to demonstrate relatively

simplistic expressions which can be signalled by activating just a few action units. We

argue that this is not the case because a) the *Emotive speech* condition was also

specifically designed to dissuade participants from relying on overly simple and

caricatured expressions and to introduce dynamic variability and b) compared to

previous work (18, 36) we provide a substantially wider range of signallers and hence

capturing wider idiosyncrasies and variability in dynamics. It could also be argued that

our results are simply a consequence of dimensionality reduction, as any set of data

can in theory be represented by a lower-dimensional structure. Yet, as we showed in

a series of validation and sensitivity analyses, the components learned carry

diagnostic information about emotions, which is robust to comparisons against

appropriate randomised dynamic patterns and generalises to unseen data. Thus, we

have not generated a "non-sense" low dimensional structure but rather a meaningful

way to represent the data.

An intriguing question concerns why this low-dimensional spatiotemporal structure

emerges. One possibility is that receivers only attend to a reduced subset of

spatiotemporal patterns and so, correspondingly, signallers tend to only move a

reduced subset of features, or to move them in predictable ways. In support of this,

studies have found that even when observers are presented with dozens of biologically

plausible face movements, their perceptual representations suggest that they only rely

on a reduced subset (34). Since human infants learn to produce and recognise facial

expressions throughout a protracted period of development (43), it is possible that

humans learn to optimise signals based on how these are optimally perceived and

responded to, creating a reciprocal dynamic interaction between these processes.

Thus, the low-dimensional organisation of facial expressions may reflect the

optimisation of social signals according to perceptual demands and these perceptual

demands, themselves, may be influenced by the low-dimensional organisation of facial

expressions (44). An alternative possibility is that there are savings (e.g.,

energy/computational) to be had from moving the face according to a few

spatiotemporal patterns.

The identification of substates in emotional facial dynamics also goes beyond previous

work on facial expression production. On the one hand substates likely reflect the

biomechanics of producing facial expressions, which inevitably result in periods of

relaxation, transition and sustainment of facial motor actions (45). Yet, the fact that the

patterns of these substates vary with different emotions and expressive conditions,

suggests that the local dynamics are sensitive to the communication of different

emotions.

In real-life interaction, facial movements subserving verbal and nonverbal expressions

are often seamlessly integrated. Our findings in the *Emotive speech* condition raise

the possibility that verbal and nonverbal face dynamics when signalling emotion are

integrated by modulating different spatiotemporal components. For example, during

speech, lip movement might covary with articulation and sound production while

simultaneously, the tightening of the lips and lowering the eyebrows can accentuate

the emotion signal. Indeed, the observation of mostly part-based profiles (e.g., lower

vs upper face AUs) in *Expression only* conditions, contrasting the involvement of both

mouth and non-mouth-related components in *Emotive speech* expressions supports

this assertion. Interestingly, the higher entropy observed in the substate patterns of

Emotive speech may reflect the competing demands placed on facial dynamics by

speech articulation and emotional expression resulting in more complex

spatiotemporal patterns. However, while we included the facial dynamics of speech,

this study was not optimised to account for the vocal or prosodic dynamics of speech.

Given that social signalling is inherently multimodal—with tone of voice, vocal prosody,

and facial expressions capable of conveying emotion both independently and in

combination— a future challenge is to understand the extent to which these modalities

act redundantly (conveying the same information) or synergistically (combining to

produce qualitatively richer meaning) for emotion signalling (1, 9, 46).

There are three important caveats that warrant consideration. First, including more

detailed descriptors of face movements (including head motion see (36)) and speech-

optimised facial dynamics, may require additional dimensions to capture the full

complexity of facial behaviour. Similarly, different emotional expressions (e.g.,

surprise, fear, disgust), free spoken and conversational contexts, and inclusion of

multimodal cues may also demand higher-dimensional representations. Second, a

different number of substates might be discovered using physiological approaches,

such as electromyography (EMG). Such approaches are sensitive to subtle motor

potentials and therefore may capture more substates including preparatory or

corrective movement impulses not apparent in FACS resolution. Lastly, our approach

focuses on exhaustively describing spatiotemporal features, such as curvature

patterns and entropy, that account for variance in the signal. However, it does not

isolate specific features (or groups of features) nor assess their individual diagnostic

value for classifying emotions. While such analysis is beyond the scope of this study,

it can be easily integrated with our approach.

Despite these caveats, our results and approach contribute new insights for future

research on facial expression signalling. Spatiotemporal structure and substates might

be important to better understand the mechanisms underlying differences in social

communication. This may provide useful insight into clinical conditions such as autism

and depression particularly in exploring the potential role of atypical facial expression

production in contributing to social interaction difficulties (47, 48). These findings also

have practical applications in fields such as social robotics and human-computer

interaction. A significant challenge in these fields relates to endowing social agents

(robots, digital agents) with convincing and adaptable repertoires of social behaviour,

including facial signalling (49). Spatiotemporal components and substates underlying

facial expression production could provide actionable targets to enhance the design

of flexible realistic and expressive agents without the need to painstakingly craft each

signal feature into the architecture of these systems.

Conclusion

In conclusion, we revealed a low-dimensional spatiotemporal structure with distinct

substates that underpin emotional signalling in in *Expression only* and *Emotive speech*

facial dynamics. We provide a framework to advance the development of novel

theoretical and methodological accounts of the structure and function of expressive

facial dynamics. This framework can be extended to other modalities and has practical

implications for understanding emotional signalling and perception in human and

machine systems.

Materials and Methods

Participants

43 healthy volunteers from the university community (24 female; mean age = 26), took

part in a study for course credit or monetary incentive. All participants gave informed

consent, and all procedures of the study were approved by the institutional ethics

committee. The dataset in this study was collected as part of a larger project

investigating facial expression production kinematics and perception – see (11).

However, all the variables and analyses reported here are novel and specific to this

study and not discussed in any previous papers.

Experimental procedure

In two separate sessions, across two days, participants' facial movements were

captured during a facial expression production task. Participants were asked to signal

three emotional expressions: anger, happiness, and sadness in two counterbalanced

conditions. An *Expression only* condition where participants simply produced facial

movements to signal each expression, and an *Emotive speech* condition where they

produce a fixed spoken sentence in emotional fashion (e.g., "My name is John and I'm

a scientist"). The conditions are motivated by the fact that in social interaction, facial

expressions can be signalled both in isolation and embedded within *Emotive speech*,

meaning that facial movements might signal information relevant to emotion and

speech simultaneously, yet how this is achieved in unclear. We focused on those

expressions because they represent basic emotion signals which are often expressed

in social interaction and communication (50). While we focus on three emotions only,

the inclusion of a wider range of participants, speech and non-speech conditions, and

data across multiple days provides richer representations of facial dynamics and

variability compared to previous work in this area, which is often restricted to a few

signallers, emotions, and conditions.

Facial movements were recorded with participants seated with their head at the centre

of a polystyrene frame to ensure central positioning towards the camera, positioned 1

meter from a tripod-mounted video camcorder, sampling at 60Hz f/s (Sony Handicap

HDR-CX240E). The start and end points were signalled using an audible beep, which

allowed us to align the recordings of facial expressions. See the schematic illustration

in Fig 7.

Analytical approach

Data processing. Facial expression videos were processed using OpenFace (51), an

open-source suite for automated face-tracking, landmarking and facial action unit

detection based on the facial action coding system (FACS) (2). We focused on Action

Units (AUs), which code for the observable presence and intensity of basic face

actions (e.g., blinking, mouth widening, eyebrow-raising) that can be used to produce

almost any facial expression. We estimated the temporal activation weights for 18

AUs. Only videos with a tracking accuracy of over 90% and with participant data across

two sessions were used, resulting in a total of 532 videos with approximately 240 time

points each. Based on visual inspection of the movement profiles, we applied a moving

average (window = 3 frames) to smooth out the slight jitter inherent in face tracking

and AU estimation, while preserving the underlying trends and dynamic range. To

ensure an equal temporal window for spatiotemporal analyses, AU timeseries were

reduced into 100-time bins for each video. Binning was preferred over more

computationally expensive alternatives such as dynamic time-warping (DTW) for

practicality since the overall timeseries duration was very similar across videos, and

visual comparisons between binning and DTW tests on our data showed negligible

differences.

Figure 7. Schematic illustration of methodological and analytical approach. Left
panel illustrates the facial expression production task, video capture and OpenFace
processing for landmark and action unit (AU) estimation. The right panel summarises
the procedure for the concatenation of AU timeseries data and the application of Non-
Negative Matrix Factorization (NMF) to learn an underlying low-dimensional
spatiotemporal representation of the data. The accuracy and effectiveness of this
lower-dimensional representation were validated through a series of sensitivity and
classification analysis (lower right panel). Time series clustering was used to identify
distinct substates or 'phases' in facial movement components.

Spatiotemporal analysis

Timeseries of AU weights for the full facial expression production task were analysed

using Non-Negative Matrix Factorization (NMF) (52). NMF is a multivariate

dimensionality reduction method that decomposes a high-dimensional dataset into two

non-negative matrices that form a part-based representation of the data (i.e., the

original data is achieved by combining/adding components). The non-negativity

constraint is particularly well suited for representing movement and AU data, which is

typically positive, and the two-matrix part-based decomposition can intuitively

represent spatial vs time-varying aspects in the data – see Fig 7 (see also: (18, 34,

52)). The NMF takes the concatenated AU timeseries as input, denoted by a matrix

M, which is a product of two low-dimensional matrices (*T* and *S*), *T* represents the

temporal weights (basis values for time bins), and *S* represents the spatial weights

(face action activation weights). The product of *T* and *S* matrices denoted by *M'*

represents an approximation of the full original matrix such that *M~M' = T * S.* The

algorithm works by initialising the values for *T* and *S* (e.g., with random values) and

using an iterative multiplicative update rule to sequentially update *T* and *S* by a factor

that minimises the approximation error (i.e., residuals). While the iterative nature of

NMF means that the solution is non-deterministic (i.e., you can learn multiple equally

effective part-based representations), these update rules have been shown to

guarantee convergence (i.e., stability of the cost function) after a relatively low number

of iterations (53). The optimal number of spatiotemporal components (*k*) was assessed

computationally by fitting a range of values (*k* = 2 to 6) and choosing a *k* that optimised

various model fit metrics (e.g., residual sum of squares, silhouette for clustering

cohesion, cophenetic coefficient, see below). We also evaluated the final solution

against NMF results on a permutated dataset, using block-based time shuffling. This

resulted in an appropriate null dataset that destroyed the inherent spatiotemporal

pattern in the data but retained some temporal ordering. We then compared fit metrics

between original and permutated NMF (see also *Classification and clustering*

analysis). We used the NMF decomposition functions in the NMF package for R (54).

To visualise our NMF results in an intuitive manner, we trained a custom model to

predict aligned Facial Landmark displacements (after correcting for rotation,

translation and looming) from AUs, based on original data using partial least squares

regression. Note however that the AU to Landmark face model is not a perfect one to

one map between NMF results and visualisation, given the many-to-one relationship

between facial landmarks and AUs.

Multivariate timeseries classification

We used a supervised classification approach to validate the diagnostic value of

spatiotemporal components for emotion expression. This involved five steps:

(1) Data splitting: We began by splitting the original pre-NMF data into training (80%)

and testing (20%) sets, ensuring that each set contained complete AU time series for

each video. This split was performed before any further analyses, and all subsequent

steps maintained this separation ensuring further processing and model training was

only done on the training set, and then applying results to the test set (55, 56). Hence

any mention of "training", always refers to operations on the respective training set.

(**2) NMF re-training and projection:** We then re-trained the NMF model using only

the training set data and projected the test set onto the trained NMF model space to

ensure consistency of components for classification.

(**3) Feature extraction:** Because standard classification approaches do not account

for inherent spatiotemporal structure of the NMF components, we opted for an

approach that represents the spatiotemporal structure via interpretable theoretic time

series features (e.g., curvature, entropy, predictability, peak, trend) (57) consistent

with features suggested to capture diagnostic information for classification of facial

expressions and body movements (8, 11, 58, 59). Feature extraction was done

separately for train and test sets. Then, a Principal Component Analysis (PCA) was

used to reduce the timeseries features that explained the majority of the variance in

the train set while retaining a number of dimensions equal to the number of NMF

components for consistency. The test set features were then transformed using the

PCA model fitted on the training set features to be used in the next step. The

component scores were used as inputs for classification analysis in the next step.

(4) Classification training and testing. We the trained a classifier on spatiotemporal

component features derived from step 3 and applied to predict emotion expression in

a held-out test set. Specifically we used a Random Forests (RF) Classifier - a

supervised learning method that learns a discriminant model between a set of input

variables (e.g., spatiotemporal components) and a set of target classes (expressions).

Note, that we achieved similar results with different methods (e.g., Support Vector

Machine, Linear Discriminant Analysis), thus our results are not a function of the

analytical approach. The Random Forests Classifier has the advantage of being

relatively more robust to overfitting and able to capture non-linear relationships and

therefore was preferred. We used cross-validation during training, where multiple

training sets are created, and the data not included in the test set is used to test the

accuracy and tune the model parameters. Reliable classification on the test set would

indicate that the underlying spatiotemporal components (identified by the NMF

analysis) carry diagnostic information for differentiating expressions. We derived

significance tests for our classification results using binomial tests to determine

whether the model's accuracy on the test set was significantly greater than what would

be expected by random guessing (by comparing it to a no information rate). These

binomial p-values were compared with permutation-based p-values, which were

generated by comparing the observed accuracy to the distribution of accuracies

obtained from shuffling the labels (expressions) in the test set (N = 1000). The

negligible differences between the binomial and permutation-based p-values for our

dataset validated the robustness of our results, so we primarily report the binomial p-

values. Additionally, we used Fisher's Exact Test to assess the statistical significance

of the confusion matrix, by comparing pairwise expression differentiation with

adjustments for multiple comparisons. The null hypothesis is that there is no

association between rows and columns, or in other words differences in cell values

(frequency) are due to chance. A low p-value in Fisher's exact test indicates

statistically significant differences between pairs, meaning the pattern in the confusion

matrix is unlikely to have occurred by chance.

While a handful of previous studies previous work has employed elements of our

proposed pipeline such as the dimensionality reduction of facial movement data

across entire datasets, our approach is unique in that it explicitly builds in the

generalisability and robustness of the spatiotemporal patterns we uncover.

Furthermore, the spatiotemporal classification pipeline enables us to directly link the

inherent dynamics (represented through the extracted features) to their diagnostic

value in differentiating emotions.

Spatiotemporal clustering for substates analyses

We investigated whether reliable substates could be extracted from the spatiotemporal

patterns of *Expression only* and *Emotive speech* facial movements. We considered

substates as local intervals where the components exhibit salient signatures that are

consistent across expression timeseries. This can be through of as a segmentation of

a multivariate timeseries into finer temporal segments with arbitrary lengths. To do this

we first derived speed and displacement for spatiotemporal components, as these

features are sensitive to segment characteristic of other body movements (e.g., swing

and stance signatures in walking, fixation and saccades in eye movements) (19, 28,

29, 60). Second, we applied spatiotemporal clustering using the *dtwclust* package in

R. This was motivated by the fact that, unlike other movements with well-established

kinematic profiles, we have no *a priori* knowledge regarding the characteristics of facial

expression substates. Given the computational complexity of DTW, we tested cluster

sizes on a smaller subset of *Expression only and Emotive speech* data. We used

visualisations which suggested (Fig 5) two to three interpretable segments described

transition and stability phases in spatiotemporal components of facial expressions in

line with the hypothesised patterns of transition, sustainment and relaxation of AUS.

To describe the pattern of substates and whether they differentiate emotion and

conditions, we computed two metrics: (1) speed within the substate and (2) entropy;

both which have been shown to capture diagnostic information about facial expression

movement patterns (8, 11). Specifically given that speed contributes to the clustering,

statistically comparing speed give insights into how the clusters were generated (see

Fig 5). Entropy, an information-theoretic measure of complexity, is directly related the

dynamics of state transitions (or sequences) within a system (37). In this context,

entropy provides a suitable summary of the dynamics of substates in a single statistic,

describing how complex or unpredictable the sequence of these substates is (e.g.,

how much information about the current substate can predict the next substate). This

statistic aimed at quantifying, for example, the apparent differences in the temporal

patterns of substates between expressions and conditions (see Fig 5). We computed

entropy using the transition entropy function (for state change entropy) from the

GrpString package for R (61) but for simplicity we refer it as entropy. To improve

interpretability, entropy was normalised by dividing it by the maximum theoretical

entropy for a system with the same number of substates.

Both speed and entropy measures were computed for each individual expression and

analysed using a mixed-effects model to test the effect of emotion (happy, angry, sad),

condition (*Expression only*, *Emotive speech*), and substate (relaxed, transition,

sustain) as fixed effects and subject (face id) as a random effect. Entropy was log

transformed to correct for non-normal residuals. Substate metrics were analysed using

linear mixed models as opposed to the classification pipeline, due to the more complex

and nested structure of the data which also makes classification overly complex to

structure and present. Linear mixed models were fitted using the lme4 package for R

(62).

Data availability statement

Supporting data is available in the Open Science Framework (OSF):

https://osf.io/3nzk7/?view_only=db7d9467423f42b794385e549b6aa96a

All code for pre-processing and models is available at https://github.com/hcuve/spat-

tmp-emo-faces

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Author Contributions (CRediT)

HCC, Conceptualisation, Data Curation, Formal Analysis, Funding Acquisition,

Investigation, Methodology, Software, Validation, Visualisation, Writing – Original

Draft Preparation, Writing – Review & Editing

SSC, Methodology, Validation, Writing – Review & Editing, Resources

JC, Conceptualization, Funding Acquisition, Methodology, Writing – Review & Editing,

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References

1.   R. E. Jack, P. G. Schyns, The human face as a dynamic tool for social
communication. *Curr. Biol.* **25**, R621-34 (2015).

2.   P. Ekman, W. V. Friesen, Facial action coding system. *Environmental*
Psychology & Nonverbal (1978).

3.   E. G. Krumhuber, L. I. Skora, H. C. H. Hill, K. Lander, The role of facial
movements in emotion recognition. *Nat. Rev. Psychol.* (2023)
https:/doi.org/10.1038/s44159-023-00172-1.

4.   K. R. Scherer, H. Ellgring, Multimodal expression of emotion: affect programs
or componential appraisal patterns? *Emotion* **7**, 158–171 (2007).

5.   A. A. Ghazanfar, D. Y. Takahashi, Facial expressions and the evolution of the
speech rhythm. *J. Cogn. Neurosci.* **26**, 1196–1207 (2014).

6.   C. Chandrasekaran, A. Trubanova, S. Stillittano, A. Caplier, A. A. Ghazanfar,
The natural statistics of audiovisual speech. *PLoS Comput. Biol.* **5**, e1000436
(2009).

7.   R. E. Jack, P. G. Schyns, Toward a social psychophysics of face
communication. *Annu. Rev. Psychol.* **68**, 269–297 (2017).

8.   R. E. Jack, O. G. B. Garrod, P. G. Schyns, Dynamic facial expressions of
emotion transmit an evolving hierarchy of signals over time. *Curr. Biol.* **24**,
187–192 (2014).

9.   M. Liu, *et al.*, Facial expressions elicit multiplexed perceptions of emotion
categories and dimensions. *Curr. Biol.* **32**, 200-209.e6 (2022).

10.   D. Gill, O. G. B. Garrod, R. E. Jack, P. G. Schyns, Facial movements
strategically camouflage involuntary social signals of face morphology.
Psychol. Sci. **25**, 1079–1086 (2014).

11.   S. Sowden, B. A. Schuster, C. T. Keating, D. S. Fraser, J. L. Cook, The role
of movement kinematics in facial emotion expression production and
recognition. *Emotion* **21**, 1041–1061 (2021).

12.   A. M. Burrows, The facial expression musculature in primates and its
evolutionary significance. *Bioessays* **30**, 212–225 (2008).

13.   C. C. Sherwood, Comparative anatomy of the facial motor nucleus in
mammals, with an analysis of neuron numbers in primates. *Anat. Rec. A*
Discov. Mol. Cell. Evol. Biol. **287**, 1067–1079 (2005).

14.   E. Todorov, Optimality principles in sensorimotor control. *Nat. Neurosci.* **7**,
907–915 (2004).

15.   R. Pang, B. J. Lansdell, A. L. Fairhall, Dimensionality reduction in
neuroscience. *Curr. Biol.* **26**, R656-60 (2016).

16.   M. L. Latash, J. P. Scholz, G. Schöner, Toward a new theory of motor
synergies. *Motor Control* **11**, 276–308 (2007).

17.   E. Chiovetto, A. Salatiello, A. d'Avella, M. A. Giese, Toward a unifying
framework for the modeling and identification of motor primitives. *Front.*
Comput. Neurosci. **16**, 926345 (2022).

18.   E. Chiovetto, C. Curio, D. Endres, M. Giese, Perceptual integration of
kinematic components in the recognition of emotional facial expressions. *J.*
Vis. **18**, 13 (2018).

19.   O. Labaune, T. Deroche, C. Teulier, B. Berret, Vigor of reaching, walking, and
gazing movements: on the consistency of interindividual differences. *J.*
Neurophysiol. **123**, 234–242 (2020).

20.   Y. P. Ivanenko, R. E. Poppele, F. Lacquaniti, Five basic muscle activation
patterns account for muscle activity during human locomotion. *J Physiol*
(Lond) **556**, 267–282 (2004).

21.   E. Chiovetto, B. Berret, T. Pozzo, Tri-dimensional and triphasic muscle
organization of whole-body pointing movements. *Neuroscience* **170**, 1223–
1238 (2010).

22.   A. Zangrossi, G. Cona, M. Celli, M. Zorzi, M. Corbetta, Visual exploration
dynamics are low-dimensional and driven by intrinsic factors. *Commun. Biol.*
4, 1100 (2021).

23.   V. Ramanarayanan, L. Goldstein, S. S. Narayanan, Spatio-temporal
articulatory movement primitives during speech production: extraction,
interpretation, and validation. *J. Acoust. Soc. Am.* **134**, 1378–1394 (2013).

24.   A. Barliya, L. Omlor, M. A. Giese, A. Berthoz, T. Flash, Expression of emotion
in the kinematics of locomotion. *Exp. Brain Res.* **225**, 159–176 (2013).

25.   J. M. Montepare, S. B. Goldstein, A. Clausen, The identification of emotions
from gait information. *J. Nonverbal Behav.* **11**, 33–42 (1987).

26.   E. S. Dalmaijer, A. Lee, R. Leiter, Z. Brown, T. Armstrong, Forever yuck:
Oculomotor avoidance of disgusting stimuli resists habituation. *J. Exp.*
Psychol. Gen. **150**, 1598–1611 (2021).

27.   E. L. Mackevicius, *et al.*, Unsupervised discovery of temporal sequences in
high-dimensional datasets, with applications to neuroscience. *eLife* **8** (2019).

28.   M. Rucci, M. Poletti, Control and Functions of Fixational Eye Movements.
Annu. Rev. Vis. Sci. **1**, 499–518 (2015).

29.   F. Torricelli, *et al.*, Motor invariants in action execution and perception. *Phys.*
Life Rev. **44**, 13–47 (2023).

30.   E. G. Krumhuber, K. R. Scherer, Affect bursts: dynamic patterns of facial
expression. *Emotion* **11**, 825–841 (2011).

31.   K. L. Schmidt, J. F. Cohn, Y. Tian, Signal characteristics of spontaneous
facial expressions: automatic movement in solitary and social smiles. *Biol.*
Psychol. **65**, 49–66 (2003).

32.   S. Aghabozorgi, A. Seyed Shirkhorshidi, T. Ying Wah, Time-series clustering
– A decade review. *Inf. Syst.* **53**, 16–38 (2015).

33.   C. C. Aggarwal, "An introduction to cluster analysis" in *Data Clustering:*
Algorithms and Applications, C. C. Aggarwal, C. K. Reddy, Eds. (Chapman
and Hall/CRC, 2018), pp. 1–28.

34.   I. Delis, *et al.*, Space-by-time manifold representation of dynamic facial
expressions for emotion categorization. *J. Vis.* **16**, 14 (2016).

35.   S. Namba, K. Nakamura, K. Watanabe, The spatio-temporal features of
perceived-as-genuine and deliberate expressions. *PLoS ONE* **17**, e0271047
(2022).

36.   D. M. Watson, B. B. Brown, A. Johnston, A data-driven characterisation of
natural facial expressions when giving good and bad news. *PLoS Comput.*
Biol. **16**, e1008335 (2020).

37.   C. E. Shannon, W. Weaver, *The mathematical theory of communication*
(books.google.com, 1998).

38.   T. Le Mau, *et al.*, Professional actors demonstrate variability, not
stereotypical expressions, when portraying emotional states in photographs.
Nat. Commun. **12**, 5037 (2021).

39.   B. Parkinson, "Social Functions" in *Heart to Heart: How Your Emotions Affect*
Other People, (Cambridge University Press, 2019), pp. 215–240.

40.   A. W. Siegman, S. Feldstein, Eds., *Multichannel integrations of nonverbal*
behavior (Psychology Press, 2014) https:/doi.org/10.4324/9781315802305.

41.   M. S. Gobel, H. S. Kim, D. C. Richardson, The dual function of social gaze.
Cognition **136**, 359–364 (2015).

42.   D. M. Wolpert, K. Doya, M. Kawato, A unifying computational framework for
motor control and social interaction. *Philos. Trans. R. Soc. Lond. B Biol. Sci.*
358, 593–602 (2003).

43.   S. M. Bell, M. D. Ainsworth, Infant crying and maternal responsiveness. *Child*
Dev. **43**, 1171–1190 (1972).

44.   C. Rowe, Receiver psychology and the evolution of multicomponent signals.
Anim. Behav. **58**, 921–931 (1999).

45.   G. B. Duchenne de Boulogne, *The mechanism of human facial expression*,
R. A. Cuthbertson, Ed. (Cambridge University Press, 1990)
https:/doi.org/10.1017/CBO9780511752841.

46.   E. A. Hebets, *et al.*, A systems approach to animal communication. *Proc.*
Biol. Sci. **283**, 20152889 (2016).

47.   R. Brewer, *et al.*, Can neurotypical individuals read autistic facial
expressions? atypical production of emotional facial expressions in autism
spectrum disorders. *Autism Res.* **9**, 262–271 (2016).

48.   A. Haque, L. Fei-Fei, M. Guo, A. S. Miner, Measuring Depression Symptom
Severity from Spoken Language and 3D Facial Expressions. *Machine*
Learning for Health (ML4H) Workshop at NeurIPS 2018, Montréal, Canada
(2018).

49.   N. Rawal, R. M. Stock-Homburg, Facial emotion expressions in human–robot
interaction: A survey. *Int. J. Soc. Robot.* **14**, 1583–1604 (2022).

50.   M. G. Calvo, A. Gutiérrez-García, A. Fernández-Martín, L. Nummenmaa,
Recognition of Facial Expressions of Emotion is Related to their Frequency in
Everyday Life. *J. Nonverbal Behav.* **38**, 549–567 (2014).

51.   T. Baltrušaitis, P. Robinson, Openface: an open source facial behavior
analysis toolkit. *2016 IEEE Winter* (2016).

52.   D. D. Lee, H. S. Seung, Learning the parts of objects by non-negative matrix
factorization. *Nature* **401**, 788–791 (1999).

53.   X. Fu, K. Huang, N. D. Sidiropoulos, W.-K. Ma, Nonnegative matrix
factorization for signal and data analytics: identifiability, algorithms, and
applications. *IEEE Signal Process. Mag.* **36**, 59–80 (2019).

54.   R. Gaujoux, C. Seoighe, A flexible R package for nonnegative matrix
factorization. *BMC Bioinformatics* **11**, 367 (2010).

55.   N. Kriegeskorte, W. K. Simmons, P. S. F. Bellgowan, C. I. Baker, Circular
analysis in systems neuroscience: the dangers of double dipping. *Nat.*
Neurosci. **12**, 535–540 (2009).

56.   G. Varoquaux, O. Colliot, "Evaluating machine learning models and their
diagnostic value" in *Machine Learning for Brain Disorders*, O. Colliot, Ed.
(Humana, 2023) https://doi.org/10.1007/978-1-0716-3195-9_20.

57.   F. J. Baldán, J. M. Benítez, Multivariate times series classification through an
982   interpretable representation. *Inf Sci (Ny)* **569**, 596–614 (2021).

983   58.   K. Dobs, *et al.*, Quantifying human sensitivity to spatio-temporal information
984   in dynamic faces. *Vision Res.* **100**, 78–87 (2014).

985   59.   N. Furl, *et al.*, Face space representations of movement. *Neuroimage* **212**,
986   116676 (2020).

987   60.   J. G. V. Miranda, *et al.*, Complex Upper-Limb Movements Are Generated by
988   Combining Motor Primitives that Scale with the Movement Size. *Sci. Rep.* **8**,
989   12918 (2018).

990   61.   I. Hooge, G. Camps, Scan path entropy and arrow plots: capturing scanning
991   behavior of multiple observers. *Front. Psychol.* **4**, 996 (2013).

992   62.   D. Bates, M. Mächler, B. Bolker, S. Walker, Fitting linear mixed-effects models
993   using lme4. *arXiv preprint arXiv:1406.5823* (2014).