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**The evolution, diversity, and
genetic architecture of sex in waterhemp
(*Amaranthus tuberculatus*)**

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34 **Abstract**

35

36 The evolution of separate sexes is hypothesized to occur through distinct pathways involving few
37 large-effect or many small-effect alleles. However, the genetic architecture of sex may itself
38 evolve through selection to suppress recombination in order to maintain beneficial combinations
39 of alleles, potentially at the cost of losing functional genetic variation. To explore these
40 processes, we leveraged the recent transition of *Amaranthus tuberculatus* to dioecy within a
41 predominantly monoecious genus, along with a sex-phenotyped population genomic dataset, and
42 six newly generated chromosome-level haplotype phased assemblies. We identify a ~4 Mb
43 region strongly associated with sex through genotype and sequence-depth based analyses.
44 Comparative genomics of these proto-sex chromosomes within the species and across the
45 *Amaranthus* genus demonstrates remarkable variability in their structure and genic content,
46 including numerous polymorphic inversions. No such inversion underlies the extended linkage
47 we observe associated with sex determination. Instead, we identify a complex copy number
48 polymorphism that is differentiated across sexes, is variable across ancestral lineages,
49 geographical scales, and habitats, but incompletely explains sex as phenotyped—over 10% of
50 individuals show phenotype-genotype mismatch in the sex-linked region. Together with our
51 novel observation of leakiness in expression of sex within the species, these findings imply the
52 presence of multiple interacting determinants of sex. The evolution of separate sexes and its
53 genetic architecture in *A. tuberculatus* therefore appears to be ongoing, with modifiers of sex that
54 permit gene exchange and the maintenance of diversity in proto-sex chromosomes.

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57 Introduction

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59 Dioecy is thought to primarily evolve from cosexuality through two distinct pathways
60 (gynodioecy and monoecy-paradioecy) that result in contrasting predictions about the importance
61 of small versus large effect mutations [1]. In the gynodioecy pathway, the intermediate stage can
62 be characterized by a single large-effect male sterility mutation that invades a cosexual
63 population and transitions it to polymorphic for females and hermaphrodites, eventually resolved
64 to dioecy by the invasion of a female sterility mutation [2]. Recombination suppression is
65 thought to evolve to prevent fully sterile genotypes, and may be further extended due to sexually
66 antagonistic selection that assembles male and/or female beneficial alleles on alternate
67 haplotypes [3]. The lack of recombination in the sex-linked region is thought to drive the
68 degeneration of the non-recombining Y/W chromosomes, although contemporary work shows
69 extensive variation in size and the degree of degeneration, which is not a simple function of age
70 [4] [5–9]. Nonetheless, young sex determining systems in the early stages of this process more
71 often tend to demonstrate incomplete recombination suppression and leaky sex determination,
72 despite multiple sexually antagonistic polymorphisms having evolved [10,11].

73

74 In dioecious species that evolve through the monoecy-paradioecy pathway, selection is thought
75 to act on quantitative variation for sex allocation. Populations transition from individuals which
76 are equally invested in male and female function to alternately fixed for one or the other through
77 gradual disruptive selection [12–14]. Tests of this route to separate sexes have been limited by
78 the relative infrequency of dioecious species in predominantly monoecious plant genera and
79 families (but see *Sagittaria* [1], *Urtrica* [15], and *Poplar* [16]). Dioecious species that have
80 recently evolved from monoecy are particularly prone to leakiness in gender expression [13,17–
81 19], implicating the possible role of gradual evolution of sex allocation, multiple loci and/or
82 expression modifiers governing this transition. Recent models suggest that while polygenic
83 variation for sex allocation is initially selected upon, this pathway may also resolve in the
84 subsequent emergence of single-locus sex determination[14]. Therefore, recent transitions to
85 dioecy from monoecy provide the opportunity to investigate the timescale of recombination
86 suppression and the evolution of the genetic architecture of sex allocation and determination.

87

88 The genus *Amaranthus* (Amaranthaceae) contains about 70 species, of which the vast majority
89 are monoecious. There have likely been multiple relatively recent transitions to dioecy, as two to
90 three dioecious clades are spread across two out of the three subgenera (*Amaranthus* and *Acnida*,
91 but not *Albersia*) [20–23]. All dioecious species in this genus are thought to result from a male
92 heterogametic (XY) system, with homomorphic (lack of apparent morphological differences) sex
93 chromosomes [24,25]. The genus is economically important, as it contains both domesticated
94 pseudograin crops and invasive agricultural weeds, including the focal species for this study, the
95 wind pollinated and annual *A. tuberculatus* (common waterhemp). *Amaranthus tuberculatus* can
96 hybridize with monoecious relatives at relatively high rates under field conditions, highlighting
97 the recent evolution of dioecy in the clade [24,26,27]. Understanding the genetic basis of sex in
98 the genus is therefore important for improving breeding efforts and the efficiency of artificial
99 selection (e.g. [28]), as well as for informing evolutionary management approaches such as gene
100 drive to suppress females and accelerate local extirpation of invasive weed populations [29,30].

101

102 Work on the causes and consequences of sex in *A. tuberculatus* illustrates sexual dimorphism,
103 apparent at both the phenotypic and genomic level, despite the likely recent origin of separate
104 sexes. Phenotyped males and females are differentiated in key life history traits, with males
105 being faster growing and earlier flowering than females, and with sex differences in genome size
106 and content of particular repeat classes [31,32]. Furthermore, levels of sexual dimorphism
107 between males and females vary by environment (whether plants were collected from natural or
108 agricultural habitats) [32], suggesting that sexually antagonistic selection is heterogeneous across
109 environments. Recent genomic work confirmed a male heterogametic system, with a cumulative
110 4.6 Mb of male-specific sequence identified through sex-specific RAD-tags [30], with loci
111 spread across multiple scaffolds, likely due to reference quality. Following this work, Raiyemo et
112 al. [33] produced a phased reference genome identifying chromosome 1 as enriched for sex
113 linked SNPs, although their assemblies lacked a contiguous sex-linked region based on genome
114 wide association (GWA) and F_{ST} analyses.

115
116 Here, we generate several new haplotype-phased assemblies and analyze them along with
117 considerable resequencing resources to resolve the diversity and evolution of proto-sex
118 chromosomes in *A. tuberculatus*. We first implement population genomic approaches to resolve
119 the location of the SDR along the chromosome. Leveraging our multiple assemblies and
120 comparative genomic approaches, we show sex determination in *A. tuberculatus* to result from a
121 polymorphic region ~4.5 Mb long, not found within an inversion but rather differentiated in copy
122 number across the sexes. The lack of 1:1 mapping of phenotype onto any genotype across the
123 genome suggests that additional genetic or environmental modifiers may be contributing to sex
124 expression in the system, and/or that unnoticed quantitative variation for sex may exist. This
125 unquantified variation in the determination and expression of sex has allowed for on-going gene
126 exchange between the proto-X and -Y, such that sex-linked haplotypes retain remarkable levels
127 of variability structured by ancestry, geography, and habitat. Taken together, our results reveal
128 the genomic heterogeneity in sex determination and expression that can result during the
129 transition from monoecy to dioecy.

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133 Results

134

135 *Characterization of the copy number polymorphic sex-linked region*

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137 To identify the location of the sex-linked region in our newly produced reference genomes, we
138 performed a GWA using 186 sex-phenotyped individuals (96 female, 92 male) from paired
139 environmental collections [31] that we mapped to one randomly chosen haplotype (haplotype 2)
140 of the highest coverage (70X) assembly. This genome came from a male plant from Walpole,
141 Ontario, Canada, a population admixed for ancestry between the two varieties, var. *rudis* and var.
142 *tuberculatus*. A GWA identified the largest scaffold, Scaffold_1 as highly enriched for sex-
143 linked alleles, consistent with recent work ([33]; **Sup Figure 1**). To attempt to resolve the
144 mapping of reads with orthology to both the putative X and Y, we used the enrichment of sex-
145 linked SNPs on Scaffold_1 to inform the production of a modified phased-haplotype level
146 reference: containing only haplotype 1 for all scaffolds except Scaffold_1, which was
147 represented by both haplotype 1 and 2. We remapped, recalled, and refiltered SNPs (see
148 methods) before reanalyzing genome-wide associations (and all other population genomic
149 analyses) for sex using this competitive mapping approach.

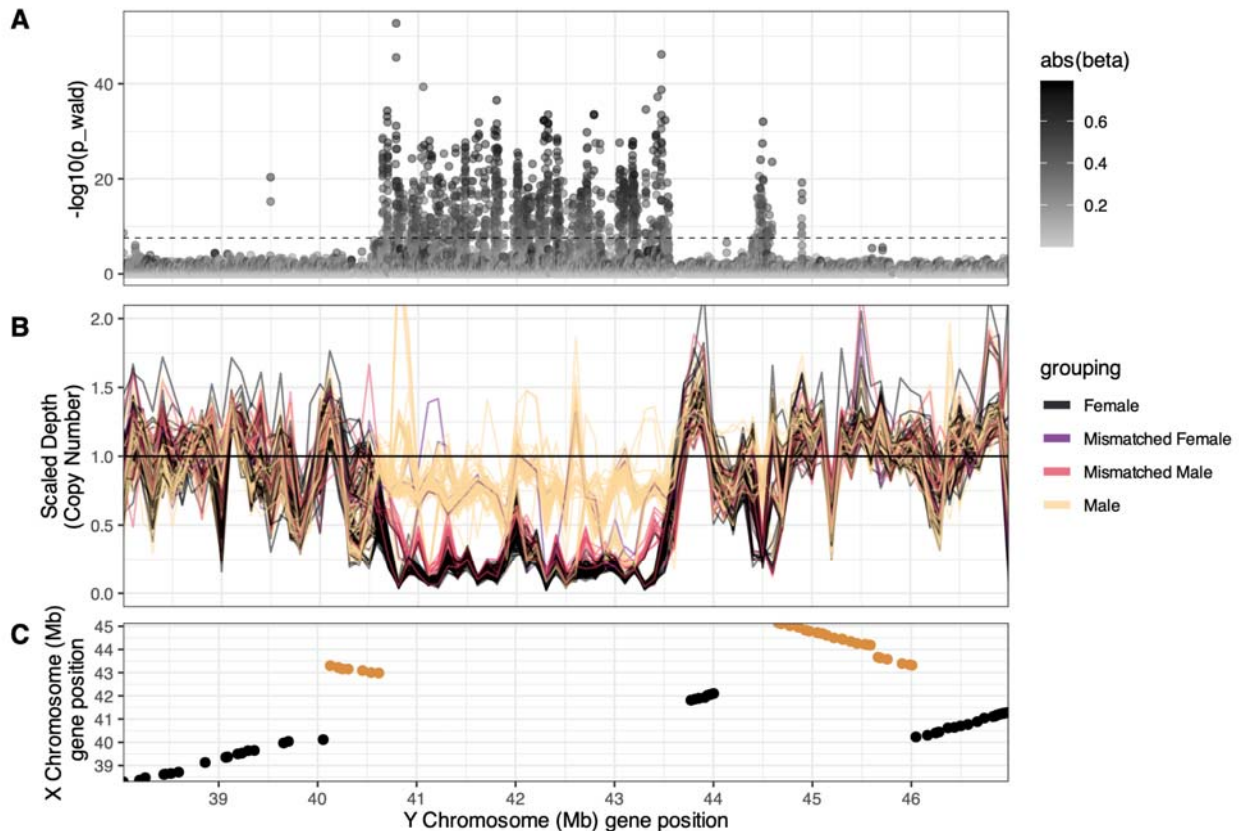
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151 Genotype-phenotype associations resolved a large sex-linked region, ~4.0 Mb long, with a near
152 continuous butte of extreme genotypic correlations with sex on Scaffold 1, haplotype 2, but not
153 haplotype 1 (**Figure 1A**; **Sup Fig 2**; but note associations found across other scaffolds, explored
154 further in *Complex copy number variation*). This sex-linked region contained 103 annotated
155 genes, including sex-determining (SD) candidates such as TOE2 (*Target of Early Activation*)
156 [34], RAP2 [35], MADS8 [36], and FT/HD3 [37]. Notably, the sex-linked region is about 10 Mb
157 downstream of the putative centromeric region according to RepeatOBserver (which uses a
158 Fourier transform of DNA walks to identify putative centromere locations; [38]). Even relative to
159 the nearby centromere, this region shows the highest patterns of 0-fold diversity and lowest gene
160 density across the chromosome based on local regression fits (**Sup Fig 3**, **Sup Figure 4**). This
161 GWA also shows a large number of significant associations (beyond Bonferroni correction) off
162 of Scaffold 1. We tested the redundancy/information value of these off-scaffold hits using a lasso
163 regression approach. For the 595/2356 loci with no-missing data out of those with p values < 10⁻
164 ¹⁵, allowing for the optimal shrinkage of predictors results in 26 loci with non-zero effects on
165 sex, for which 22 are found on Scaffold 1 (**Sup Figure 5**).

166

167 To identify whether the sex-linked region was male or female specific, we estimated copy
168 number in these same samples. By scaling each individual's median read-mapped coverage in
169 100bp windows within the sex-linked region, by the median read-mapped coverage on
170 Scaffold_1 outside of the sex-linked region, we attained estimates of fine-scale copy number. We
171 see that while median male and female copy number show complete overlap for most of
172 Scaffold_1, we see clear divergence among sexes in sequence presence/absence between 40.5-
173 43.5 [and a secondary peak around 44.5] Mb. Most males show a median copy number on
174 average around 0.75 across this region (light yellow in **Figure 1B**), while most females (black in
175 **Figure 1B**) show a median copy number closer to 0.25. While this is distinct from the
176 expectation of a Y-specific region, for which the median copy number should hover around 1
177 and 0 in the Y and X respectively, low divergence between the proto-sex chromosomes means
178 that even with competitive mapping, Y reads may map to the X and vice-versa. These coverage

179 based analyses suggest that the sex-linked region identified in the GWA (and supported by
180 further *F_{st}* and heterozygosity based analyses; **Sup Figure 6**) maps to the Y, which has either
181 recently expanded in gene content relative to the X, or these genes have have been recently lost
182 on the X. Comparison of the synteny of Scaffold_1 haplotype 1 and haplotype 2 assemblies
183 using genespace[39] supports these population-level copy number polymorphism inferences, as
184 we find our haplotype 2 (proto-Y) reference lacks syntenic orthologous genes on haplotype 1
185 (proto-X) in the SLR.
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189 **Figure 1. The sex-linked region (SLR) in *A. tuberculosis* on Scaffold 1.** A) A GWA resolved strongly sex-linked
190 alleles along a 4 Mb stretch on haplotype 2 of Scaffold 1, between 40.65-43.5[44.5] Mb. Color of points depicts the
191 absolute allelic effect size from mixed model associations. The horizontal dashed bar represents the Bonferroni
192 $p=0.05$ threshold. B) Sex-based differentiation in copy number in the SLR illustrates fine-scale variation within
193 sexes, and genotype-phenotype mismatch. Copy number was calculated through scaling depth in the SLR, by
194 coverage on Scaffold_1 outside of the SLR, in 50 kb genomic windows. C) Genes falling within the SLR on the Y
195 (haplotype 2 assembly) lack orthologous copies on the X (haplotype 1 assembly).
196

197 Given the apparent role of copy number variation in sex-determination, we tested whether
198 genome-wide sex-associated loci also showed such a signal. To do so, we extracted all sex-
199 associated alleles passing multiple test correction off of Scaffold_1 ($n_{\text{genome}}=864$, $n_{\text{scaffold}_1}=2011$)
200 and calculated the SNP-level ratio of male:female coverage. Coverage at these sites are elevated
201 to an average ratio of 1.2 (95% CI = [1.01,1.52]). The mean of the distribution of male:female
202 coverage at these genome-wide loci is similar to as is seen in the SLR (mean = 1.49; 95% CI =
203 [0.99, 2.59]; **Sup Figure 7**). Since it is unlikely these represent independent sex-linked CNV
204 distributed all across the genome, and as these reads/SNPs do not drop out after stringent

205 filtering based on mapping quality, this suggests that about 20% of males have sex-linked
206 paralogues on their Y haplotype that are absent in our reference Y (as in [40]). Therefore, while
207 Y-linked regions are typically thought of as degenerate and lacking variation, the Y haplotypes
208 studied here are surprisingly diverse.

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211 *Structural variation across male waterhemp genomes and the sex-linked region*

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213 The six haplotype-phased chromosome-level assemblies we generated with PacBio HiFi and Hi-
214 C data provided the opportunity to further resolve the extent of structural heterogeneity and
215 evolution in *Amaranthus* (**Sup Table 1**). Consistent with recent reports, our analyses show that
216 the two largest scaffolds/chromosomes in *A. tuberculatus* (chromosomes 1 and 2) were formed
217 through a chromosomal fusion (i.e. Robertsonian translocation) since the split of *A. tuberculatus*
218 to *A. tricolor*, *palmeri*, and *crutensius* (**Figure 2A**).

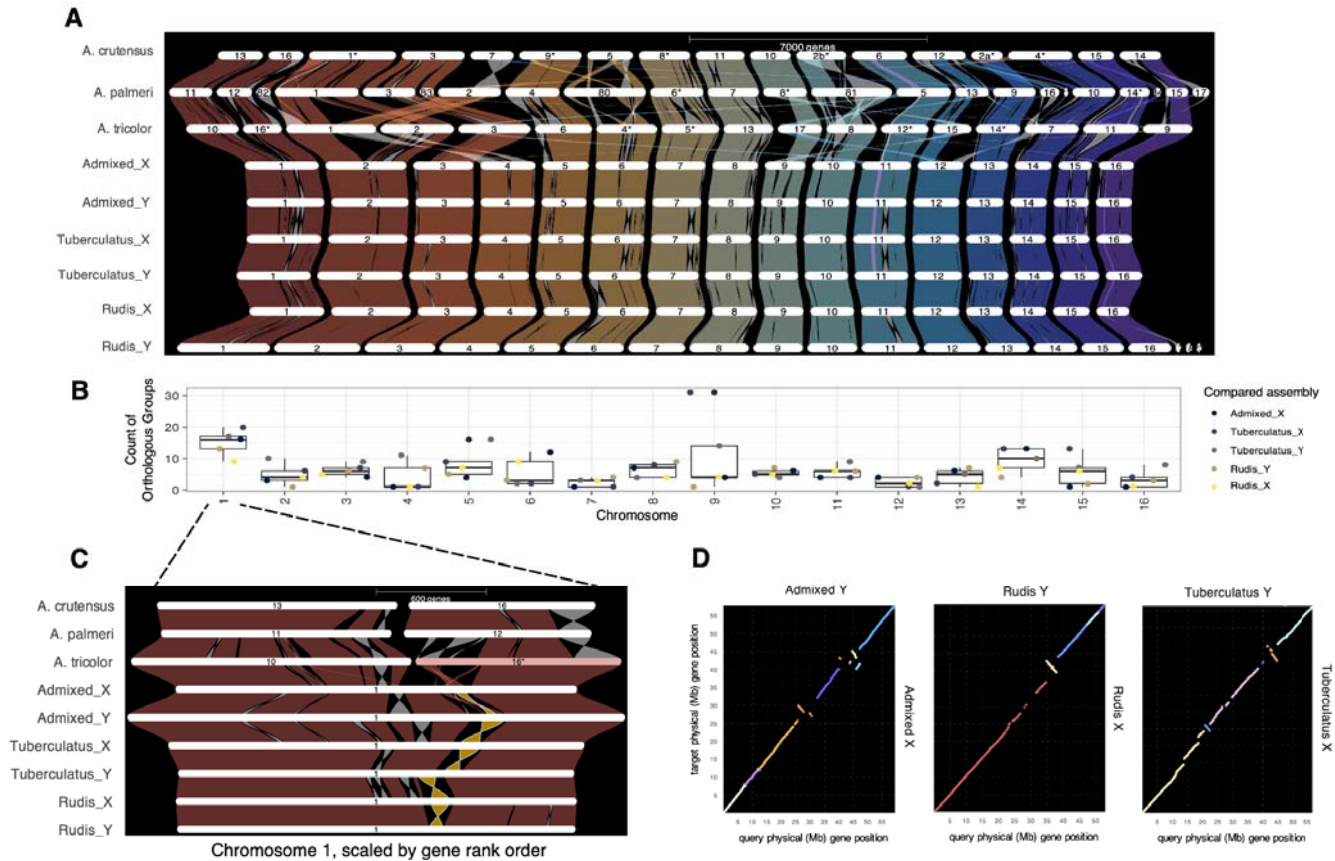
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220 We find widespread signals of intraspecific structural variation in *A. tuberculatus*. Each genome
221 shows widespread signals of an ancient whole genome duplication as suggested in [41], with
222 ohnologues present on alternate scaffolds (e.g. **Sup Figure 8, 9**). When comparing the 6 *A.*
223 *tuberculatus* haplotype assemblies to each other, we find numerous inversions, duplications, and
224 translocations (**Figure 2A**). To quantify the extent of structural rearrangement, we calculated the
225 number of orthologous groups (contiguous tracks of syntenic sequence) within each scaffold for
226 each pair of haplotype assemblies. We found on average ~5-8 orthologous groups per scaffold
227 depending on the paired comparison (**Figure 2B**). Notably, the SDR containing Scaffold_1 is
228 significantly enriched over all other scaffolds for the number of orthologous groups (with the
229 upper and lower quartile ranging from 13-20; chromosome effect: $F = 2.9352$, $P = 0.00157$, all
230 pairwise comparisons $p < 0.05$ except for with Scaffold_9), as is particularly apparent by the
231 large number of inversions segregating across these haplotypes ($n = 11$; **Figure 2C, D**).
232 Scaffold_1 is the largest scaffold in the assembly, and if we control for scaffold length, it is no
233 longer an outlier for the number of orthologous groups. This suggests that while the amount of
234 structural variation scales with chromosome size, sex-determining and sex-linked regions (SLRs)
235 may be more likely to arise on or result in regions of the genome enriched for structural
236 complexity.

237 Given the number of structural rearrangements present on the chromosome containing the SLR,
238 and the common role of structural variation in limiting recombination along SLRs [42–44], we
239 tested the extent to which they may be sex-linked. To do so, we interrogated both pairwise
240 comparisons of the X-containing and Y-containing haplotypes of Scaffold_1 within an
241 individual, and all-vs-all assembly comparisons (i.e. Genespace). While a number of private and
242 low frequency inversions are present, segregating between just X-containing assemblies (**Sup**
243 **Fig 10**) and between just Y containing assemblies (**Sup Fig 11**), one inversion appears to
244 segregate consistently between the three X and Y containing haplotypes (**Figure 2C, 2E, Sup**
245 **Table 2**). This inversion is directly upstream and neighboring the sex-linked region, but
246 remarkably lacks any substantial signal of sex-linkage itself based on population genomic
247 inference (i.e. GWA in **Figure 1**; F_{ST} and Heterozygosity in **Sup Fig 6**). We turned back to our
248 population genomic data to further test whether there was any cryptic population structure by sex
249 or other variables within the bounds of these inversions based on PCA derived from SNP
250 genotypes. Sex does not predict PC1, PC2, or PC3 for any of the inversions contained on
251 Scaffold_1 (**Sup Figure 12**). However, other variables do: ancestry (proportion of var. *rudis*

252 versus var. *tuberculatus* based on K=2 grouping of a structure plot) loads on PC2 of Inversion3,
253 PC1 on Inversion11, and PC1 of Inversion12; longitude on PC1 and PC3 of Inversion12;
254 environment (Natural or Agricultural) marginally on PC3 of Inversion8; and latitude marginally
255 on PC2 of Inversion8. These results imply inversions are not facilitating population-level
256 recombination suppression in or around the sex-linked region.

257
258 Gene-presence absence variation in the sex-linked region is not specific to just X-Y haplotypic
259 comparisons. When we look directly at the 4Mb sex-linked region and compare gene presence
260 absence across other Y assemblies, we find a stark contrast in the relative abundance of core
261 genes (present in all assemblies) versus pan genes, with core genes being at a frequency of 62%
262 (15,002/24173) genome wide, but only 10% among Y haplotypes within the SLR. Indeed, this is
263 also visually apparent in dot plot based pairwise comparisons of the Y haplotypes, for which
264 orthologous synteny is variable within the sex-linked region (**Sup Fig 13**). Since this is a
265 particularly copy number variable and relatively low gene-density region, it is also plausible that
266 technical issues with assembly of this region has led to gene dropout.



267 **Figure 2. Structural variation within *A. tuberculatus* is enriched on the chromosome containing the sex-linked**
 268 **region.** **A)** A synteny plot from Genespace highlighting the syntenic gene orthologues within *A. tuberculatus* among
 269 haplotype-phased assemblies and between *A. tuberculatus* and three congeners (*A. tricolor*, *A. palmeri*, and *A.*
 270 *crutensius*) with chromosome level assemblies. Inversions are highlighted in light grey, as are translocations which
 271 can be distinguished from inversions by their connections between distinct chromosomes. **B)** The count of
 272 orthologous groups between the Y-containing admixed, Walpole genome and each haplotype-level assembly, along
 273 with box plot summaries. **C)** A zoomed in synteny plot of Chromosome 1, which contains the SLR, illustrating the
 274 widespread occurrence of inversions and a inversion (highlighted in yellow) that is heterozygous in all three of our
 275 males. **D)** Pairwise dot plots of syntenic genes between the proto-X and proto-Y chromosome-level assemblies for
 276 each male.

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279 *Genotype-phenotype mismatch and population structure in the sex-linked region*

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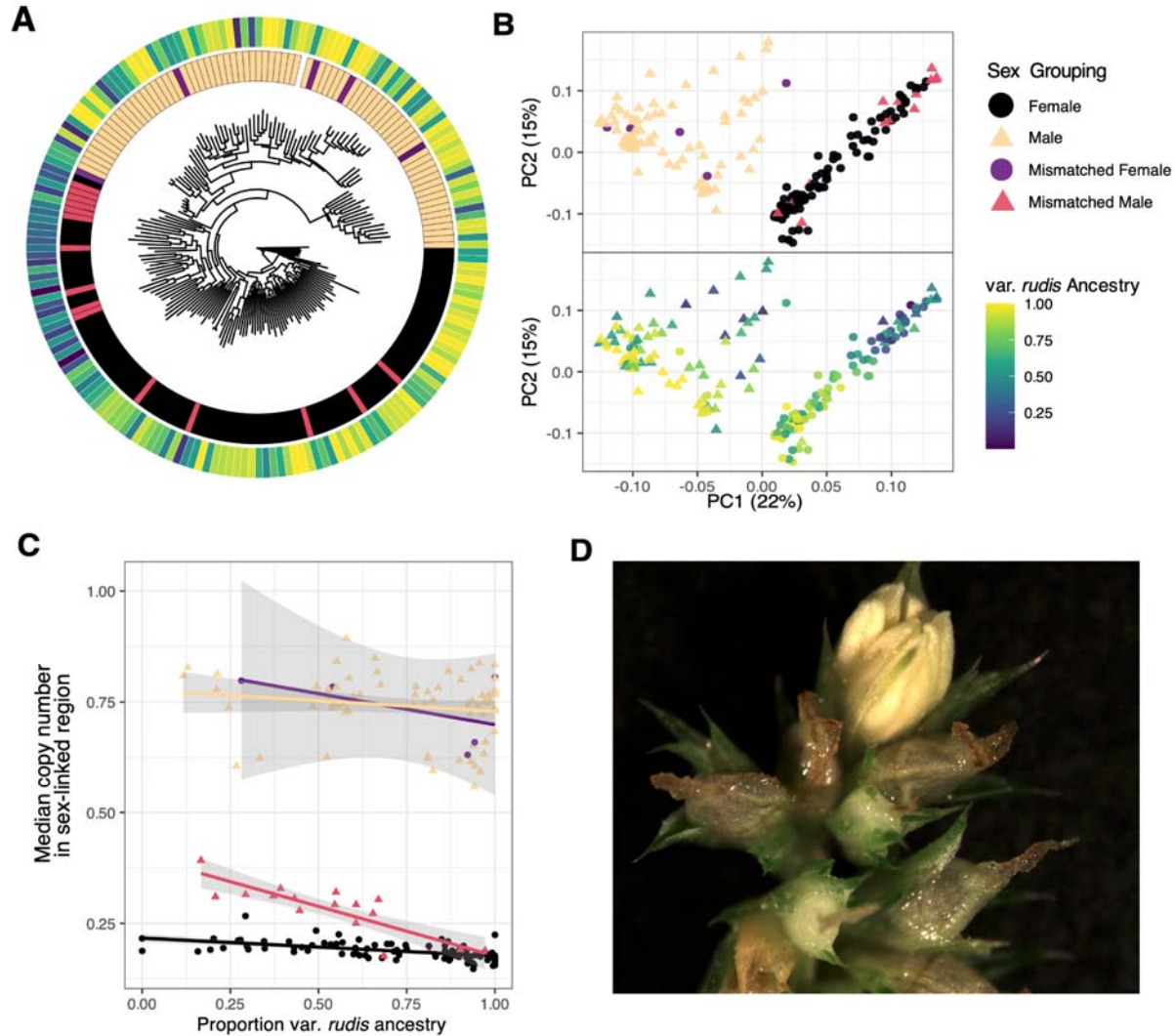
281 While in many systems, a single locus is sufficient to fully explain phenotypic variation in sex,
 282 this seems not to be the case in *A. tuberculatus*. We see a strong notable exception to the excess
 283 of male:female coverage in the SLR for ~10% of individuals in this dataset, which show a
 284 mismatch between sex and their average coverage in the SLR (**Figure 1B**; **Figure 3**). This
 285 genotype-phenotype mismatch is apparent not only based on copy number profiles (**Figure 1B**,
 286 **Figure 3C**) but also through PCA and phylogenetic reconstruction of unphased but
 287 competitively mapped genotypes in this region for 5/94 (5.3%) and 17/89 (19.1%) of individuals
 288 phenotyped as females and males, respectively (**Figure 3A, B**).

289

290 One might expect that individuals that are proximal to the opposite sex in the genotype of their
291 SLR would show phenotypic evidence of this intermediacy. Alternatively, one might consider
292 the possibility of whether sex was mis-phenotyped. To consider these two possibilities, we first
293 independently validated our findings of genotype-phenotype mismatch with a dataset of sexed
294 herbarium sequenced samples for which phenotypes can be reexamined, finding that again,
295 nearly 10% of samples show a genotype-phenotype mismatch (**Sup Fig 14**). While neither the
296 herbarium or common garden population genomic datasets provided evidence of phenotypic
297 variation in the expression of sex, careful observation of waterhemp reproductive structures in
298 other contexts revealed leakiness in its expression, which we revisit and report for the first time
299 here. As pictured in **Figure 3D**, we discovered an individual from a separate accession and a
300 separate grow out that is made up of entirely female flowers except for one male flower atop an
301 inflorescence. At other times throughout the numerous years of growing waterhemp, we have
302 observed other forms of leaky sex-expression in *A. tuberculatus*, including entire branches that
303 have oppositely sexed flowers relative to the rest of the plant, and even a predominantly female
304 plant with several perfect (hermaphroditic) flowers. This quantitative variation for sex-
305 expression supports the role of multiple SD loci or modifiers acting in the system.

306

307 Mean copy number in the SLR (**Figure 3C**) is structured not just by their sex grouping (i.e.,
308 genotype-phenotype status; $F_{3,173} = 1867$, p-value $< 2 \times 10^{-16}$), but also by var. *rudis* ancestry
309 ($F_{1,173} = 7.38$, p-value = 0.0073), the interaction between ancestry and the ancestry and sex
310 grouping ($F_{3,173} = 4.38$, p-value = 0.0054), and marginally habitat type (agricultural or natural;
311 $F_{1,173} = 3.3849$, p-value = 0.067) (**Figure 3**). Genotypic structure in this region depicts an even
312 stronger role of ancestry in shaping sex-linked haplotypes (ancestry: $F = 59.6$, p-value = 8×10^{-13} ;
313 ancestry x sex grouping: ($F_{3,173} = 3.5$, p-value = 0.016) in addition to sex grouping ($F_{3,176} = 33$,
314 p-value $< 2 \times 10^{-16}$), latitude ($F_{1,173} = 15.75$, p-value = 0.0001), and habitat type (agricultural or
315 natural; $F_{1,173} = 4.17$, p-value = 0.043). Clearly, the sex-linked region in *A. tuberculatus* retains
316 plenty of diversity that reflects both deep and recent evolutionary history.



317
318 **Figure 3. The sex-linked region shows SNP and copy number diversity that reflects strong population**
319 **structure and leaky sex expression.** A) A phylogeny inferred from IQtree of genotypes in the sex-linked region,
320 with tips colored by sex grouping and *var. rudis* ancestry proportion (legend in B). B) PCA of genotypes the sex-
321 linked region, colored by sex grouping and *var. rudis* ancestry composition. C) The median copy number in the SLR
322 is predicted by the proportion of *var. rudis* ancestry, and by the interaction of sex grouping x ancestry. D) A male
323 flower (emerging anthers in light yellow) atop a predominantly female inflorescence (stigmas in brown) in a
324 waterhemp individual.

325
326 While multiple loci or modifiers may interact to determine sex, this architecture might also
327 facilitate the maintenance of diversity in the sex-linked regions by allowing for gene-exchange.
328 To test this, we performed LD based inference of recombination rate with LDhat [45] with the
329 competitively mapped reads along Scaffold_1 (Sup Fig 15). While the mean effective
330 recombination rate ($4N_eR$) shows a clear drop-off at the border of the sex-linked region, the
331 smoothed moving average does not go to zero, and further indicates peak in recombination in the
332 center of the SLR. Rare recombination events in the SLR might leave a geographic signal. We
333 investigated this by calculating the difference between an individual's copy number in the SLR
334 and the mean value for its respective sex-matched copy number, visualizing its distribution on a
335 map (Sup Fig 16), and modeling its predictors in a multiple regression. The degree of copy

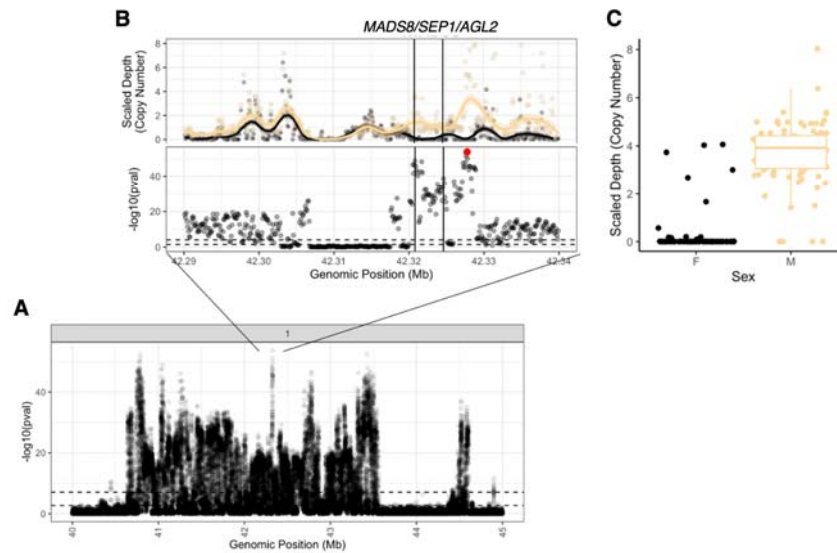
336 number mismatch shows a widespread geographic distribution, with mismatched individuals
337 present in most populations. While latitude, longitude, environment, and ancestry do not predict
338 the degree of mismatch, state is a significant predictor ($F_{4,178} = 2.4607$, $p = 0.047$). While this LD
339 based inference of recombination is not free from technical artifacts resulting from mismapping
340 of repetitive sequence, together these results suggest that gene exchange between the sexes is
341 likely on-going, and contributes to variation at the SLR we describe here.

342
343 Despite the average genotype in the SLR being commonly mismatched to phenotypic sex, we
344 sought out fine-scale locus-specific copy number variation that remained unique to one sex—a
345 strong candidate for a SDR. To do so, we performed a GWA for sex based on copy number in
346 100bp windows, which further resolved heterogeneity in sex-linkage even within this 4Mb
347 region (**Figure 4A**). While copy number variation at the edges of the SLR tend to show the
348 strongest fidelity between sexes, a CNV within a narrow 100kb tract around 42.32 to 42.33 Mb
349 shows the strongest association with sex despite being surrounded by a valley of significance,
350 and is more closely associated with sex than any SNP-based genotype genome wide (r^2 , p-value
351 for top SNP = 0.73, 2×10^{-53} ; r^2 , p-value for top CNV locus = 0.73, 1.2×10^{-54} ; **Figure 4B**). Just
352 downstream of the most significant locus lies the MADS-box transcription factor, SEP1,
353 necessary for petal, stamen and carpel development in Arabidopsis. Copy number at this
354 upstream 100bp window is on average 4 in males and 0 in females, although males show
355 substantial variation (between 0 - 8). The genotype to sex association at this locus is still
356 imperfect however, with a fewer number of mismatched individuals, only 4 males and 7 females
357 resembling the copy number of the opposite sex (~5% percentage mismatch) (**Figure 4C**).

358
359 Previous common garden phenotyping of these samples, not just for sex, but for key life history
360 traits identified a continuum of sexual-dimorphism [31,32], allowing us to test hypotheses about
361 the timing of the evolution of sexual dimorphism versus separate sexes[46,47]. When we
362 perform GWA of traits with significant sexual dimorphism (i.e., biomass, flowering time), only
363 the most sexually dimorphic trait – biomass – produces a GWA profile loaded onto the sex-
364 linked alleles. Genotype-phenotype associations for dry biomass showed a 99.99% overlap with
365 SNPs associated with sex, whereas flowering time, the second most dimorphic, showed 0 overlap
366 with sex-associated SNPs (**Sup Fig 17**). This suggests that shifts in size may have occurred
367 through primary genetic changes during the transition to separate sexes, whereas flowering time
368 may have been a secondary genetic change [46]. Furthermore, we tested whether genotype-
369 phenotype mismatched individuals were more likely to have trait values of the opposite sex, as
370 might be expected if these individuals represent sex intermediates. However, we see no such
371 pattern (**Sup Fig 18**).

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391 **Figure 4. Copy number GWA resolves fine-scale variation in the association with sex within the sex-linked**
392 **region. A)** The Manhattan plot of significance of the association of sex with copy number in 100bp windows across
393 the sex-linked region. **B)** Zooming in on the region of the genome with strongest copy number association with sex,
394 [upper] the distribution of mean copy number in 100bp windows for individuals phenotyped as male (yellow) and
395 female (black) [lower] and the significance profile of this copy number variation with sex. **C)** Copy number
396 variation at the 100bp window with the strongest association with sex, highlighted in red in B).

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Discussion

400

401 Our results demonstrate a proto-XY system in *A. tuberculatus* that retains considerable
402 complexity and diversity despite evidence of extended linkage of loci associated with sex. We
403 find that copy number polymorphism between the proto-X and proto-Y are involved in sex
404 determination. However, we find no locus for which copy number variation (or SNP variation)
405 fully explains sex as phenotyped. Nearly 10% of individuals phenotyped as male or female
406 display the genotype of the alternate sex in the SLR. Together with observations of leaky sex
407 expression in the species, our results implicate additional SD factors that facilitate on-going gene
408 exchange at the primary sex-linked locus and therefore the maintenance of diversity in the
409 architecture and expression of sex.

410

411 The evolution of dioecy from monoecy has classically contrasted pathways that rely on large or
412 small effect mutations [1]. Recent models on the gradual evolution of separate sexes through
413 selection on sex allocation however outline how polygenic variation for sex allocation can be
414 concentrated to a single locus through ecological selection for sex specialization [14]. Under
415 such a model, XY systems are more likely to evolve when fitness exponentially relates to female
416 allocation, which could result from the coupling of survival and seed production in highly fecund
417 females. Such a scenario is plausible in *Amaranthus tuberculatus*, as it is remarkably difficult to
418 manage in field settings due to the large crop of seed produced by females, estimated to range up
419 to 35,000-1,200,000 seeds per plant [48]. While we identify a large-effect locus capable of
420 explaining 76% of the variation in sex, no SNP or copy number variant within the chromosome 1
421 SLR shows a perfect correlation with sex. Thus, despite *A. tuberculatus* showing a significant

422 concentration of the genetic architecture of sex within this region, the persistence of variation in
423 sex determinants suggests that separate sexes may still be actively evolving. The integration of
424 gene expression data with expanded GWA studies holds significant promise for uncovering
425 additional modifiers of sex expression, while estimates of sex allocation-fitness curves in closely
426 related monoecious species will be instrumental in elucidating the importance of a quantitative
427 pathway towards separate sexes.

428
429 Species that have evolved dioecy under the quantitative monodioecy-parodioecy pathway are
430 hypothesized to be more susceptible to modifiers of sex-expression [49], whether genetic or
431 environmental. Extensive phenotypic observation of field and herbarium samples in the *Siparuna*
432 genus, where multiple transitions to dioecy has occurred from monoecy, revealed inconsistent or
433 “leaky” sexes as a relatively common phenomenon [50–52], as is also observed in *Mercurialis*
434 [53]. The waterhemp congener, *A. palmeri* which likely represents an independent transition to
435 dioecy [23,29], shows transient hermaphroditism with initial staminate (male) flowers producing
436 both male and female reproductive organs, but the with development of the gynoeceum primordia
437 halted early on [54]. At the scale of phenotyping we performed in our initial common garden
438 experiment, nearly four thousand individuals for numerous phenotypes [31], it is possible that we
439 missed cryptic variation in sex expression amongst the millions of flowers present. In the
440 meantime, evidence of leaky sex expression from waterhemp individuals reared in a separate
441 experiment has come to light, with a predominantly female individual displaying a single male
442 flower atop its inflorescence. That variation for sex-determination and expression still exists
443 supports genomic evidence that the transition to dioecy is not complete, and that the evolution of
444 separate sexes in *Amaranthus* proceeded through the quantitative monoecy-parodioecy pathway.
445 Crossing of individuals with alternate matching and mismatching status at the primary SLR will
446 help to map the number and effect size of secondary SD loci, if segregating.

447
448 Multiple mechanisms of sex determination might be selectively favored to prevent the
449 degeneration of sex-linked regions [55]. The sex-linked locus shows evidence of substantial copy
450 number heterogeneity both within and among sexes, with copy number in 1kb windows (even
451 within genes) varying between 0 - 39.3X for males and 0 - 13.5X for females. When this fine-
452 scale variability in copy number is associated with sex, it displays a characteristic “suspension
453 bridge” pattern typical of recombination suppressed regions, with divergence concentrated near
454 the breakpoints at the center of the region where selection counters recombination [43,56,57].
455 However, the peak of $4NeR$ in the center of the sex-linked region, along with a 10% rate of
456 phenotype-genotype mismatch, suggests that on-going gene exchange (i.e., “flux” through gene
457 conversion or double recombination events) may be a considerable force countering sex-specific
458 selection [58,59]. The distribution of genotype-phenotype mismatch does not show a particularly
459 strong geographic signal, with mismatched individuals being present in nearly all populations,
460 although home state is a significant predictor. This suggests that either recombination between
461 sex chromosomes is not particularly rare, or that rare recombination is complemented by
462 environmental modifiers of sex. In terms of a mechanism of gene exchange, gene conversion
463 among sex-chromosomes has been observed in a number of species, from fruit flies to humans
464 [60,61], and when combined with high levels of copy number variation as is seen here, may
465 counteract the accumulation of deleterious mutations in recombination suppressed regions [62].
466

467 On-going gene flux has likely bolstered the maintenance of variation in sex-linked haplotypes
468 across the native range of *A. tuberculatus*. Similar results have recently been observed for
469 recombining inversions encoding *Heliconius* wing coloration[63], while remarkable diversity
470 among Y haplotypes has been recently observed in guppies and fruit flies [40,64]. We see
471 structure in sex-linked haplotypes shaped by ancestry and latitude. On one hand, this may be
472 consistent with neutral divergence and a history of diverging sex-chromosomes on either side of
473 the Mississippi river before secondary contact of var. *rudis* and var. *tuberculatus* [48], but may
474 also result from clinal selection from multivariate climatic conditions. Previous analyses have
475 suggested an interaction between sexual and natural selection for flowering time, with males
476 showing stronger divergence from females at lower latitudes [31,32], potentially supporting a
477 role of divergent sex-linked haplotypes in climate adaptation.
478

479 Despite the potentially homogenizing force of gene exchange between the X and Y, we observe a
480 narrow peak of association in the middle of the SLR at MADS8 and a relative dearth of
481 associations around it suggests particularly strong sex-specific effects [65–67]. MADS box
482 transcription factors play an exceptional role in developmental novelties, with their duplication
483 and neofunctionalization in plants resulting in sex-specific development, flowers, fruits, and
484 seeds ([68–71]), and in *Populus*, potentially even the transition from male to female [72].
485 MADS8 in particular has been characterized as a gene indispensable for female development in
486 Rice (*Oryza sativa*) under high temperatures [36]. Such an environmental-dependent pathway
487 could explain the lack of complete phenotype-to-genotype mapping we observe for MADS8.
488 This might also explain the same finding for the gene *FloweringTime*, which previous work
489 identified as a candidate for SD gene having been differentially expressed across male and
490 female flowers and showing sex-specific markers [23,33], given that our assemblies show
491 presence/absence variation of this gene within the Y itself. Quantifying differential expression of
492 sex-linked genes in response to varying exogenous cues will help resolve the potential role and
493 nature of environmental modifiers of sex in this system.
494

495 These results provide support for the concentration of the genetic architecture of sex during the
496 transition from dioecy to monoecy. While large-effect alleles have accrued on the extended sex-
497 linked region on chromosome 1, it seems likely the evolution of separate sexes is still
498 incomplete, with multiple SD factors and variation in sex-expression still segregating, along with
499 on-going gene exchange between the proto-X and Y. The practical implications of this
500 complexity in genetic architecture of sex are that propositions of using gene drive on the SD
501 locus as a mechanism of weed control may be practically challenging to implement. Further
502 work to decipher the genetic architecture and fitness curve of sex-allocation in close monoecious
503 relatives will help resolve the ecological mechanisms and the variation that has been lost during
504 the evolution of separate sexes in *Amaranthus*.
505

506

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508

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511 for gene annotation. Thanks to Federico Trucco for observing the leaky sexed waterhemp
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516
517

518 **Methods**

519

520 *Data Production*

521

522 Based on previous analyses of population structure across populations of *Amaranthus* spanning
523 Ontario and the Midwestern United States [31,73], we selected three populations that spanned
524 predominantly var. *Rudis* (Nune), admixed (Walpole), and predominantly var. *tuberculatus* (Nat)
525 ancestry. Further, we selected an individual from a maternal line in an admixed population where
526 its sibling was previously genotyped as segregating for high EPSPS copy number (~28 copies
527 [73]). For each population, seed from 2 maternal lines were sown into 5 pots each in growth
528 chambers in the Biodiversity Research Centre with day and night temperatures set to (15 degrees
529 C/12hr, 25 degrees C/8hr). After germination, pots were thinned to a single plant, and relocated
530 to the greenhouse in early May where they would grow under lengthening days to maximize
531 tissue production and delay the time to flowering. From each line, we collected tissue from one
532 male numerous times over the summer to maximize tissue for high molecular weight DNA
533 extractions and Hi-C.

534

535 Hi-C libraries were prepared using a protocol based on Padmarasu *et al.*, 2019 [74] and Dong
536 and Zhong, 2020 [75], with modifications. In brief, young leaves were collected and flash-frozen
537 in liquid nitrogen. Approximately 0.75-1 g of tissue were used as starting material. Leaves were
538 pulverized using a mortar and pestle, and nuclei were cross-linked in 1X PBS buffer + 1.5%
539 formaldehyde for 15 minutes at room temperature in a rotisserie oven. Cross-linking was halted
540 by adding glycine at a final concentration of 250 mM, and incubating the tissue for 5 minutes at
541 room temperature, with rotation. Tissue was washed once in ice-cold 1x PBS buffer and
542 resuspended in 10 ml of cold Nuclei Isolation Buffer (20 mM HEPES pH 8.0, 250 mM sucrose,
543 1 mM MgCl₂, 5 mM KCl, 40% glycerol v/v). It was then filtered, in successions, through two
544 layers of cheesecloth and one layer of miracloth (MilliporeSigma, Burlington, MA, USA).
545 Nuclei were then washed in Nuclei Isolation Buffer and fractionated using a 95% Percoll
546 (MilliporeSigma) gradient buffer. DNA in purified nuclei was then treated with DpnII restriction
547 enzyme, biotinylated, and proximity-ligated. DNA was extracted from the nuclei using
548 phenol:chloroform:isoamyl alcohol (Invitrogen, Waltham, MA, USA) and quantified using a
549 Broad Range kit on a Qubit fluorometer (Invitrogen). Biotinylated DNA fragments were isolated
550 from 1-4 µg of the resulting DNA, and Illumina libraries were prepared following Todesco *et al.*
551 2020 [76]. Preliminary experiments performed in sunflower and cannabis showed that, due to the
552 abundance of repetitive sequences in plant genomes, large fractions of read pairs in Hi-C
553 libraries are not informative. Both proximally-ligated fragments in a read pair need to be mapped
554 uniquely to the genome to provide information about long-range interactions; if one of the
555 fragments derives from a repetitive region, and can therefore not be uniquely mapped, the read
556 pair becomes uninformative. To reduce the abundance of repetitive regions in the Hi-C libraries,
557 and therefore increase the proportion of informative reads, we applied an enzymatic repeat
558 depletion treatment [76]. Hi-C libraries were sequenced by Novogene Corporation Inc.
559 (Sacramento, CA, USA).

560

561 HMW DNA for PacBio sequencing was extracted using a CTAB-based protocol adapted from
562 Stoffel, K. *et al.*, 2012 [77] in the Rieseberg Lab at UBC. Briefly, 0.8 g of flash frozen young
563 leaves of *Amaranthus tuberculatus* were ground to thin powder using mortar and pestle in liquid

564 nitrogen. The powder was thoroughly resuspended in Extraction Buffer (100mM Tris-HCl pH
565 8.0, 1.4M NaCl, 20 mM EDTA pH 8.0, 2% w/v CTAB and 1% v/v b-mercaptoethanol) and
566 incubated 1 hour at 55°C. Eventually the tube was cooled down to RT and extracted with one
567 volume of chloroform:isoamyl alcohol (24:1). The aqueous phase was supplemented with NaCl
568 up to a final concentration of 2.6 M and re-extracted with chloroform:isoamyl alcohol. The new
569 aqueous phase was transferred to two new tubes that were topped up with at least 6 volumes of
570 Precipitation Buffer (50 mM Tris-HCl pH8.0, 10 mM EDTA pH 8.0 and 1% w/v CTAB). Tubes
571 were centrifuged for 30 minutes at RT and the combined pellets were washed with milliQ water.
572 Eventually the pellet was gently and fully resuspended in NaCl 1.5 M and incubated with
573 RNaseA for two hours at 37 degrees. After the RNase treatment, a third chloroform extraction
574 was followed by two washes with 75% ethanol. Finally the fully dried pellet was allowed to
575 resuspend overnight in 10 mM Tris-HCl pH 8.0 at 4°C. Pipetting was reduced to the minimum
576 along the procedure and if done was exclusively handled with wide-bore tips to avoid damaging
577 DNA. HiFi sequencing was performed at the Yale Genomics Centre. We decided to sequence
578 one individual from Walpole, Ontario, Canada, to high coverage (70X), and the other two
579 individuals to the minimum coverage recommended by HiFiASM for haplotype-phased
580 assembly + HiC to assess assembly quality at varying coverages (25X) [78].

581
582 HiFiASM was used to produce haplotype-phased assembly, informed by Hi-C data for each
583 sample. Default settings were used, except for one sample (which happened to be lower
584 coverage; var. *tuberculatus*) which showed asymmetric assembly sizes between haplotypes. As
585 recommended, the setting for heterozygosity was adjusted to multiple values, however with little
586 effect. We found that removing the Hi-C data from the initial HiFiASM assembly for this sample
587 led to a much more symmetric haplotype size, and thus we proceeded with this approach. After
588 the assembly of each haplotype's contigs, contigs were further scaffolded using the Hi-C data
589 with the program YaHS [79], and the resulting scaffolds were then manually curated with
590 Juicebox based on the contact map. Briefly, scaffolds were joined together that had
591 overrepresentation of long-distance contacts, and contigs were flipped in orientation that showed
592 an excess of long range compared to short-range contacts within the scaffold. Finally, we
593 performed pairwise mapping of each haplotype to each other, and to one haplotype of each other
594 individual, using the SynMap2 tool in Coge [80] to confirm the consistency of scaffold naming
595 among assemblies (such that Scaffold_1 is syntenic to Scaffold_1, and Scaffold_2 to Scaffold_2,
596 etc., across all haplotypes).

597
598 All six haplotype assemblies were then annotated with Maker [81], using *ab-initio* prediction,
599 along with protein sequence from a previous *Amaranthus tuberculatus* assembly [73], its
600 congener *Amaranthus hypochondriacus* [82], and using transcriptomic data we produced from
601 24 individuals spanning two populations from southwestern Ontario found in a Natural and
602 Agricultural setting, with 12 males and 12 females sequenced. For these transcriptomes, RNA
603 was extracted using RNAeasy plant kits in the Wright Lab, and libraries were prepared and
604 sequenced at the Sickkids, Toronto sequencing facility on Illumina single-end 100bp technology.
605

606 607 *Comparative Genomics* 608

609 To identify orthologous groupings among assemblies and visualize their synteny, we ran
610 Genespace [39] on all 6 *A. tuberculatus* assemblies along with three other congeners with

611 recently produced chromosome-level reference genomes: *Amaranthus cruentus* [83],
612 *Amaranthus tricolor* [84], and *Amaranthus palmeri* [85]. We used the `gghits` and `riparian_plot`
613 functions to visualize pairwise and all vs all synteny. We also investigated the number of
614 orthogroups (defined by the presence of X-1 breaks in synteny) between each genome and across
615 each scaffold. To identify core genes and pan genes, we queried pangenes for their
616 presence/absence across assemblies at the genome-wide level, and for particular chromosomes of
617 interest. We refined these comparisons to assemblies we hypothesized to contain the male SDR.

618

619 *Centromere identification and Repeat Calling*

620

621 Previous work generated de-novo TE libraries [32] for a previous draft *A. tuberculatus* reference
622 genome [73]. We used repeat masker based on these libraries to identify previously characterized
623 repeats in all 6 of the new haplotype-phased chromosome level assemblies produced here. We
624 also ran RepeatOBserver to identify the putative centromeres in our assembly, as inferred from
625 the Shannon diversity index of Fourier transforms of DNA walks, with low diversity indicating
626 highly repetitive low complexity regions as is typically found in centromeric regions [38].

627

628 *Population genomics*

629

630 We leveraged 187 resequenced individuals from 17 pairs of neighboring natural-agricultural
631 populations collected from Michigan to Kansas (from [31]) to understand population genomic
632 patterns of separate sexes. The samples were grown as a part of a much larger common garden
633 experiment, in which 6000 individuals were grown, and ~4000 sexed and phenotyped for
634 numerous traits [31]. Important to this study, plants were sexed at the early to mid-stages of
635 flowering and so based on only a small proportion of flowers. Furthermore, due to the large-scale
636 nature of this study, and the sheer number of flowers produced by an individual, we did not make
637 an effort to look for variation in sex expression (nor did we know it existed). As a result, we
638 could not comment on whether any individuals showed leakiness in their sex expression. In the
639 meantime, the Tranel lab at University of Illinois Urbana-Champaign was performing a routing
640 grow out of waterhemp for herbicide phenotyping, and noticed the individual pictured (**Fig 3D**).
641 In addition to the pictured female individual that harbors a male flower, the Tranel lab has
642 observed, rarely, other instances of leaky sex expression including: a predominantly female
643 individual with an entire branch of male flowers, and an individual that contained a perfect
644 (hermaphroditic) flower.

645

646 We re-aligned the raw reads from this resequencing dataset using BWA-mem [86] to a randomly
647 chosen haplotype of the highest-coverage individual (70X in total, 35X per haplotype; an
648 individual from an admixed population in Ontario segregating for high EPSPS copy number).

649 After calling SNPs using freebayes (options `--use-best-n-alleles 2 --report-monomorphic`) and
650 filtering SNPs (using the following expressions in BCFtools [87]: `QUAL >= 30, 'AB >= 0.25 &`
651 `AB <= 0.75 | AB <= 0.01', SAF > 0 & SAR > 0, MQM >=30 & MQMR >= 30', ((PAIRED >`
652 `0.05) & (PAIREDR > 0.05) & (PAIREDR / PAIRED < 1.75) & (PAIREDR / PAIRED > 0.25))`
653 `| ((PAIRED < 0.05) & (PAIREDR < 0.05))'`) we performed a genome-wide association study of
654 the 11,040,109 SNPs genome-wide with sex using gemma and a minor allele threshold of 5%
655 [88]. This GWAS identified Scaffold_1 as containing the major sex-linked region. Having
656 applied a Bonferroni multiple test correction, we extract the genotypes of all remaining

657 significant SNPs and performed a lasso regression analysis on them to determine their co-
658 linearity in explaining sex, after first performing cross-validation to identify the value of the
659 shrinkage penalty (λ) that minimizes the mean-square error. On this same genome, we also
660 re-mapped two traits, biomass and flowering time, that were measured for these samples in [31].
661

662 To further distinguish population-level patterns between haplotypes (i.e. whether it was a ZW or
663 XY system) and to distinguish between reads with the ability to map to both haplotypes, we
664 produced a modified assembly that contained both haplotype 1 and haplotype 2 of Scaffold_1,
665 but only haplotype 2 of all other scaffolds. All raw resequenced reads were then remapped to this
666 modified assembly, but SNPs were only re-called on haplotype 1 and 2 of Scaffold_1. 1,881,197
667 SNPs were associated sex across both haplotype of Scaffold_1 in the subsequent association
668 study.
669

670 Using competitively mapped SNPs, we then implemented a number of population genetic
671 investigations. PCAs were performed on particular regions of interest, including each of the
672 inversions identified in Genespace and the major sex-linked region on Scaffold_1 using plink2 (-
673 -pca). Previous work inferred the ancestry of each sample with FastStructure at $K=2$ [31], and we
674 used these ancestry proportions that relate to the proportion of var. *rudis* or var. *tuberculatus*
675 ancestry in a multiple regression along with sex-grouping (with female, male, mismatched
676 female, mismatched male as factor levels), the ancestry x sex-grouping interaction, habitat
677 (natural or agricultural), latitude, and longitude of a sample to predict PC values of each
678 inversion. To compare the proportion of heterozygous genotypes between males and females for
679 each locus, we used the --geno-count option in plink for separate runs that included either only
680 males or only females. For each sex, we then calculated the heterozygous proportion as the
681 number of heterozygous genotypes divided by the total number of genotypes called at that locus
682 (i.e. accounting for missing data at each locus). We also inferred the phylogenetic tree of the sex-
683 linked region using IQtree2 [89], with the algorithm that accounts for invariant sites (options -st
684 DNA -nt 80 -m TESTONLY+ASC). Finally, we used $Pi_{XY[90]}$ to calculate weir and cockerham's
685 F_{ST} and diversity between and within sexes, while controlling for missing data. For both F_{ST} and
686 the difference in the proportion of heterozygous genotypes between males and females, we used
687 R to calculate the 95% confidence interval of all autosomal scaffolds using `quantile(probs =`
688 `c(0.025,0.975)` to provide context for their distributions along the sex-linked region on
689 Scaffold_1. All plotting was done with `ggplot2` [91] and the `cowplot` [92] packages in R.
690

691 We calculated fine-scale copy number in 100bp windows along the sex-linked region.
692 Specifically, we used `mosdepth` [93] to estimate coverage in 100bp windows for each individual
693 directly from mapped reads. We calculated copy number as the depth in a focal 100bp window
694 along Scaffold_1 (the SLR contained scaffold) divided by the mean coverage outside of the SLR
695 on Scaffold_1. To visualize fine-scale copy number by sample in the sex-linked region and
696 reduce noise in these estimates, we plotted the smoothed means of copy number in 100 kb
697 windows. Mean individual copy number was also calculated across the entire sex-linked region.
698 Using this estimate of an individual's mean copy number in the SLR, we performed multiple
699 regression analyses with var. *rudis* ancestry proportion, sex grouping (defined based on male and
700 female, and whether or not they were genotype-phenotype matched [n=4 groups]), latitude,
701 longitude, and habitat (natural or agricultural) as predictors. We also performed a copy number-
702 phenotype association analysis for each 100bp window on Scaffold_1. This was done using a

703 custom script, for which a linear regression of sex against copy number was run for each window
704 across Scaffold_1. The $-\log_{10}(\text{p-value})$ of these tests were plotted, after inferring the raw p-
705 value cutoff using a Bonferroni multiple test correction threshold of 0.05.

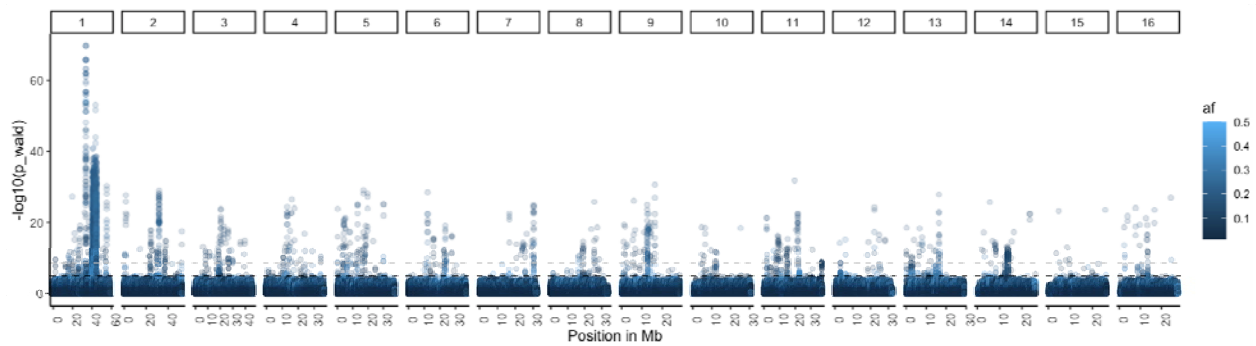
706
707 To validate the likelihood of sex mis-phenotyping, we investigated patterns of genotype-
708 phenotype mismatch in an independent dataset, inferred local recombination rate, and the
709 distribution of genotype-phenotype mismatch across the range. We mapped resequenced
710 herbarium samples [94] for which the phenotype value for sex was verified and validated based
711 on deposited images, to our focal reference genome. Mapping was performed after merging and
712 de-duplicated reads with DeDup [95], and rescaling base-quality scores to account for DNA
713 damage [96]. As for our contemporary samples, we then inferred copy number based on scaled
714 depth in the sex-linked region. On contemporary samples, we inferred the effective population
715 recombination rate (ρ) using LDhat [45]. To do so, we used a precomputed look up table (θ
716 = 0.01) and a subsampled VCF with 100 genotypes (25 males and 25 females). ρ was
717 computed between each SNP, each point estimate was plotted along with the loess curve along
718 Scaffold_1. Since we also had phenotype data for these samples, we were able to perform a
719 multiple linear regression analysis for two key traits (biomass and flowering time), to ask
720 whether genotype-phenotype match status predicted trait values, while controlling for
721 experimental treatment, environment, geography, and sex of samples. Finally, we calculated the
722 difference in an individual's copy number relative to the respective sex-matched mean value. We
723 tested whether there was a strong geographic signal in the distribution in the degree of this
724 mismatch in a multiple regression framework, with latitude, longitude, environment, and state as
725 predictors.

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728 **Supplementary Figures**

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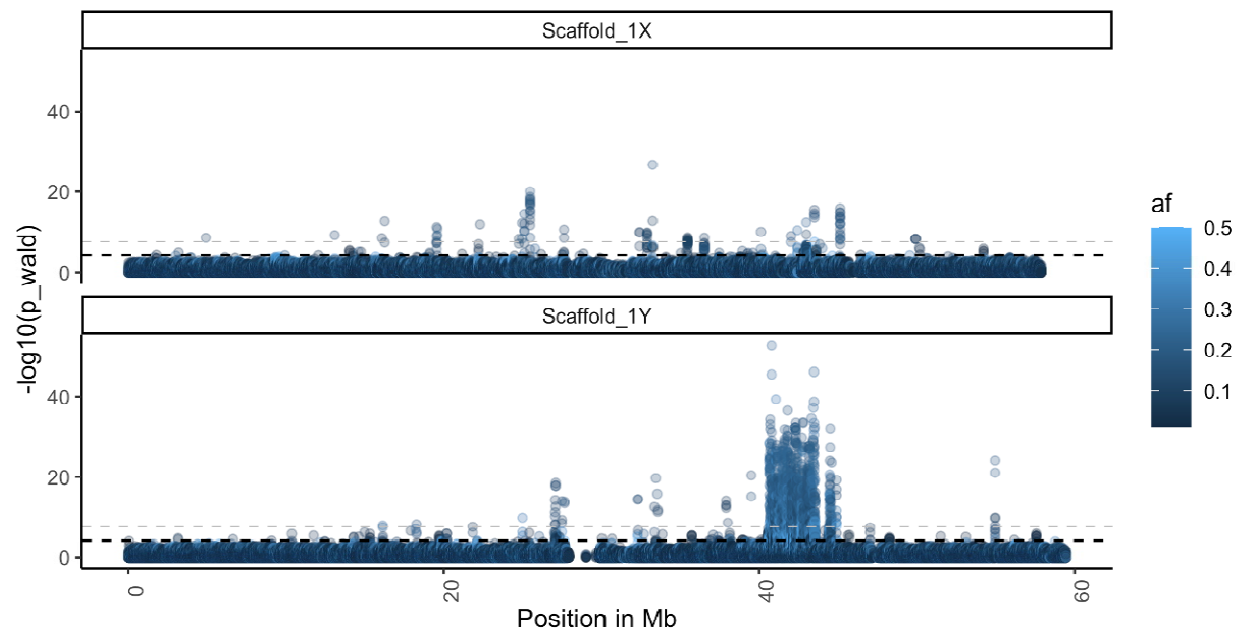
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733 **Sup Figure 1.** A Manhattan plot of the strength of the $-\log_{10}(p\text{-value})$ of the association of SNPs
734 across the genome with sex phenotypes. Analysis was done on SNPs called from reads mapped
735 only to haplotype_2 (i.e., not competitively mapped).

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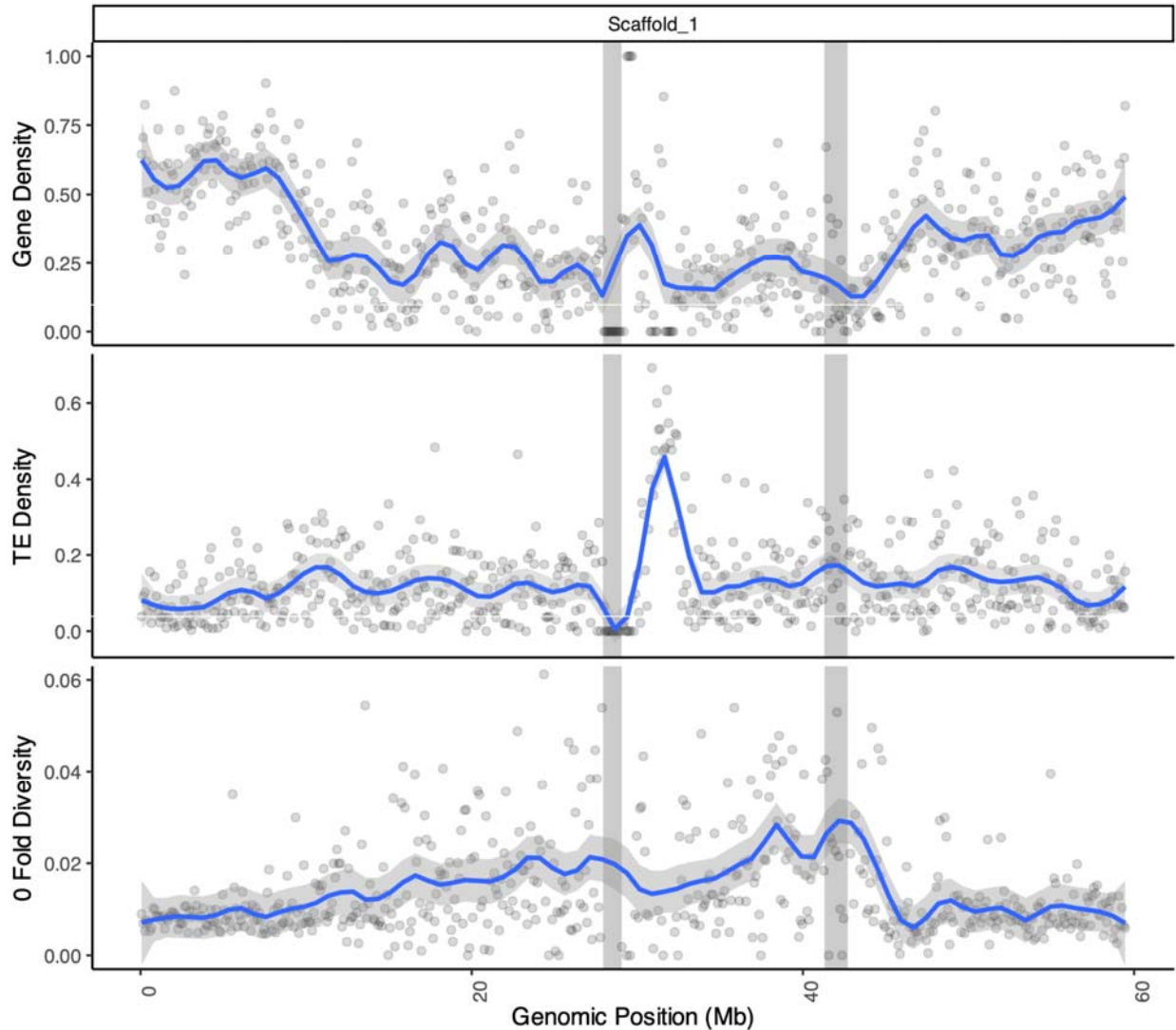


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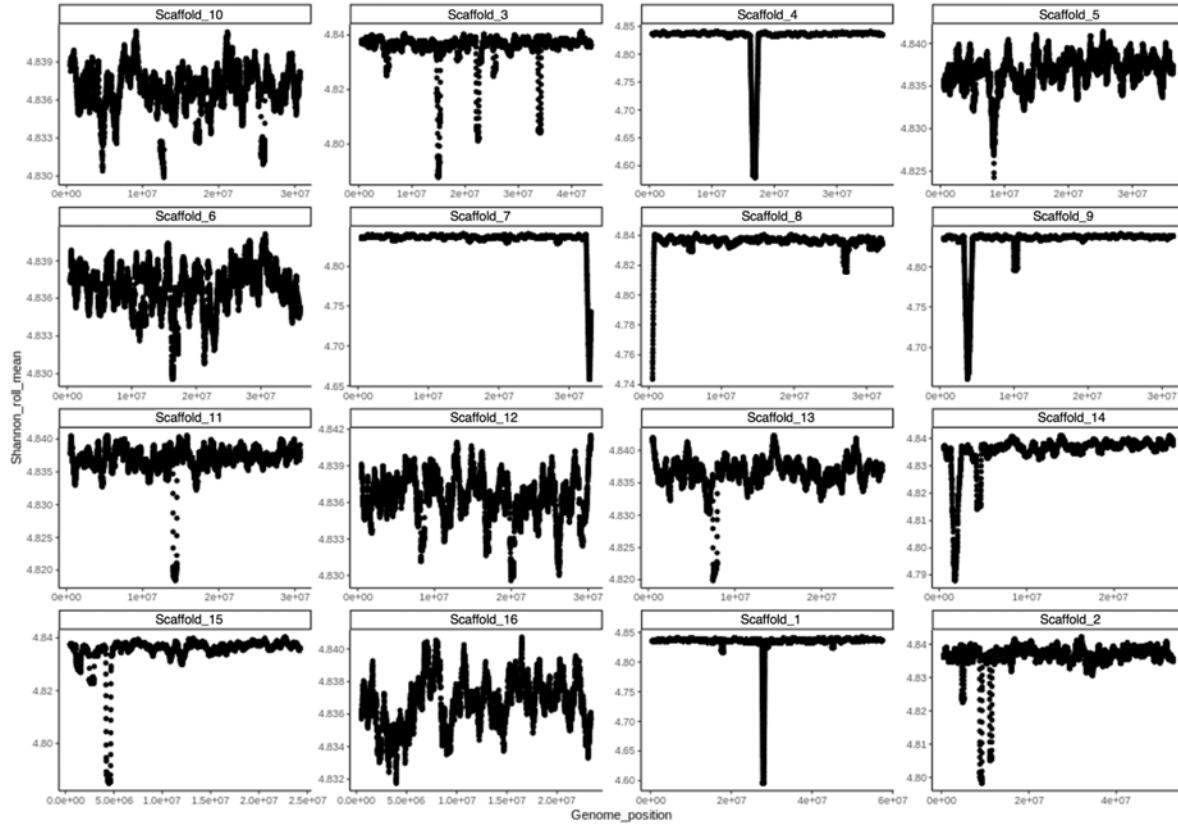
740 **Sup Figure 2.** A Manhattan plot of the strength of the $-\log_{10}(p\text{-value})$ of the association of SNPs
741 along haplotype_1 (the proto-X) and haplotype_2 (the proto-Y) of Scaffold 1. Analysis was done
742 on SNPs called from reads competitively mapped to haplotype 1 and 2.

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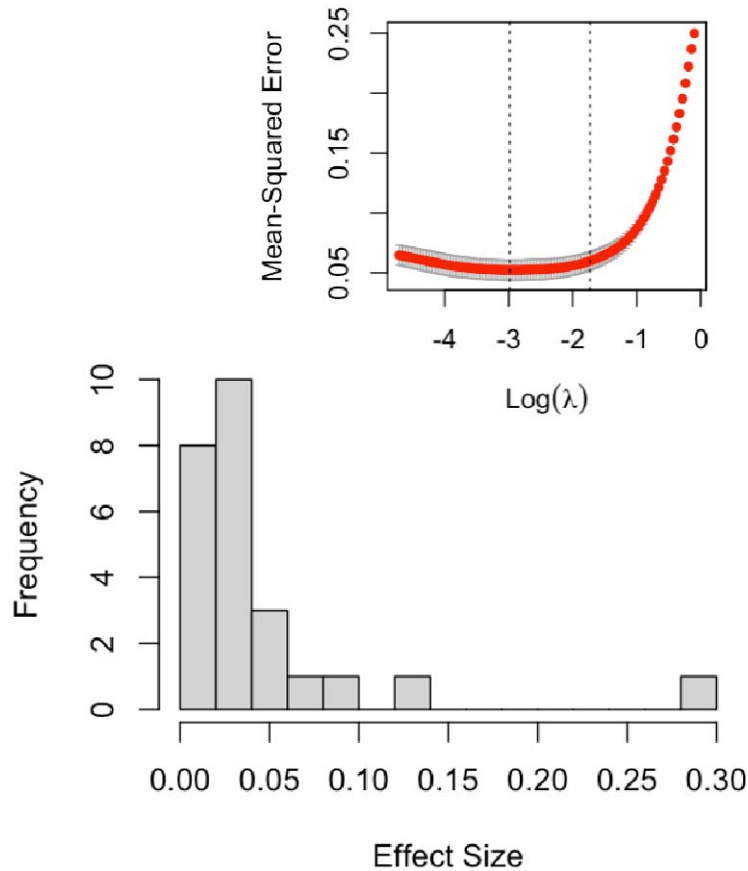


745
746 **Sup Figure 3.** Structure across chromosome 1, containing the sex determining region between
747 40-43.5 Mb (right vertical bar), a region which shows the highest 0 fold diversity and among the
748 lowest gene density across chromosome 1. Analysis was done by mapping all reads to only
749 haplotype 2 (i.e. no competitive mapping). TE density (based on a previously curated TE library)
750 is greatly enriched at ~32 Mb, just neighboring the inferred location of the centromeric region
751 (left vertical bar; as inferred from RepeatOBserver).
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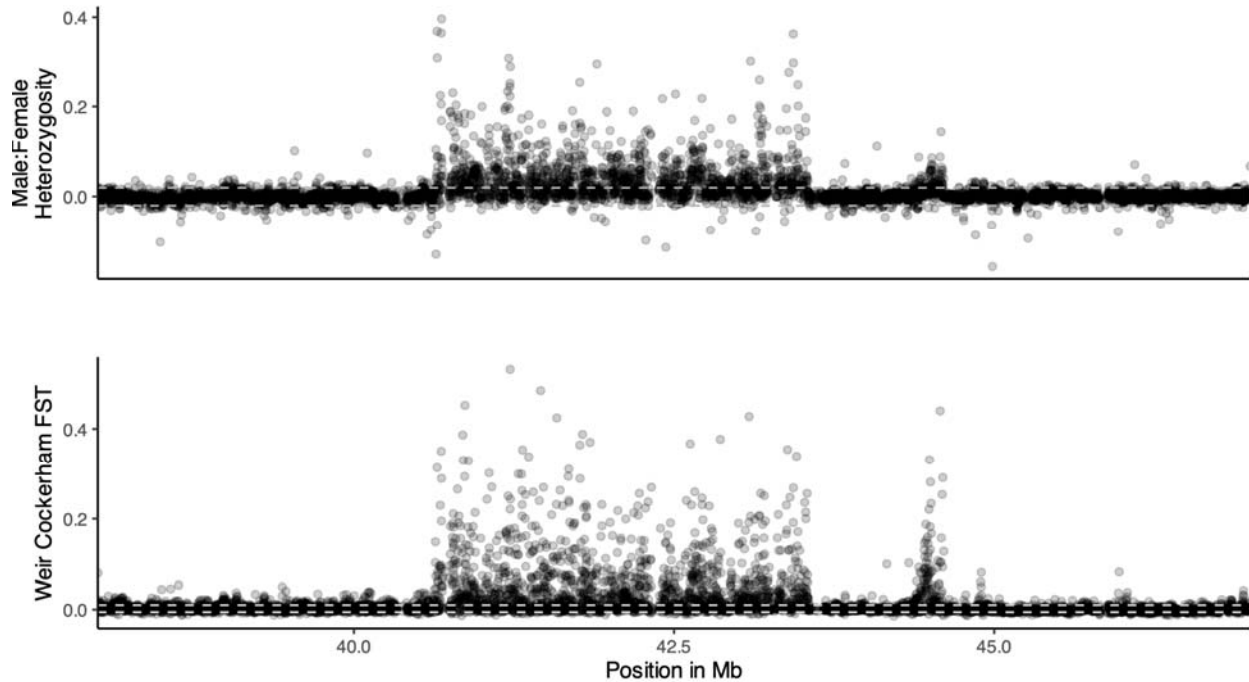
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Sup Figure 4. RepeatOBserver inferred shannon-diversity index of sequence complexity across each scaffold for our focal reference, where minimum values are predictive of centromere location. The sex-linked region region is present on Scaffold_1 around ~41Mb, and shows a tertiary minimization of Shannon diversity.



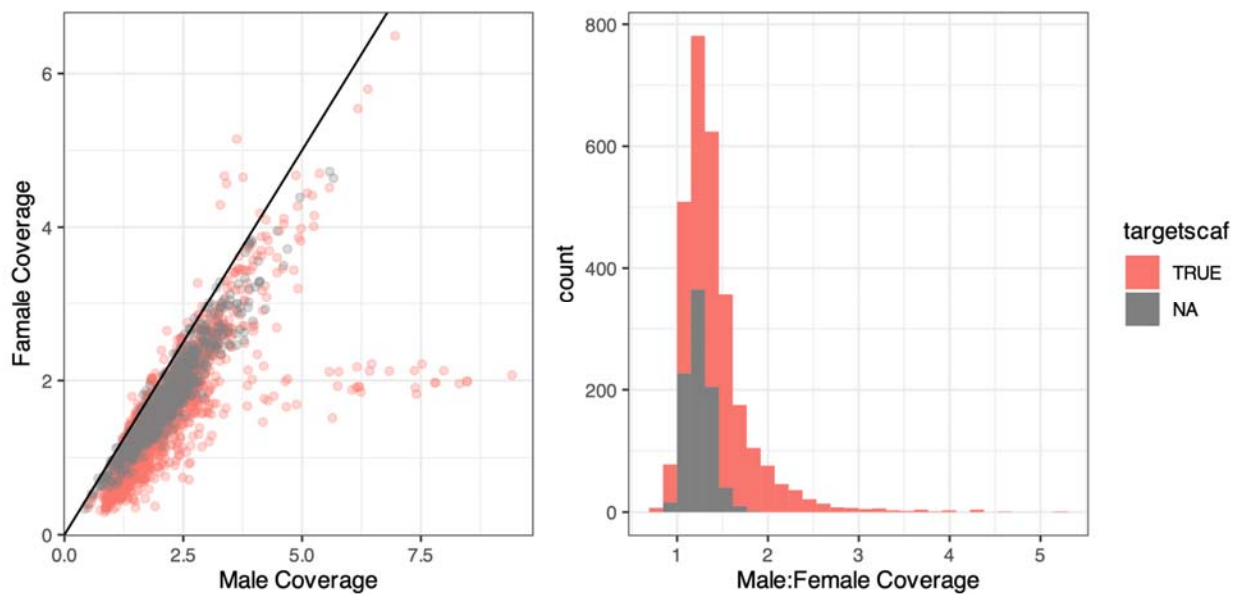
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Sup Figure 5. Results for the lasso regression analyses of the predictive independence of loci with significant associations with sex, after Bonferroni correction. Upper) The minimization of MSE occurs when lambda approaches zero (~ 0.01), such that no one predictor is eliminated from the model, their coefficients are just shrunk towards 0. B) The distribution of effect sizes for the 26 loci with remaining non-zero effects on sex.



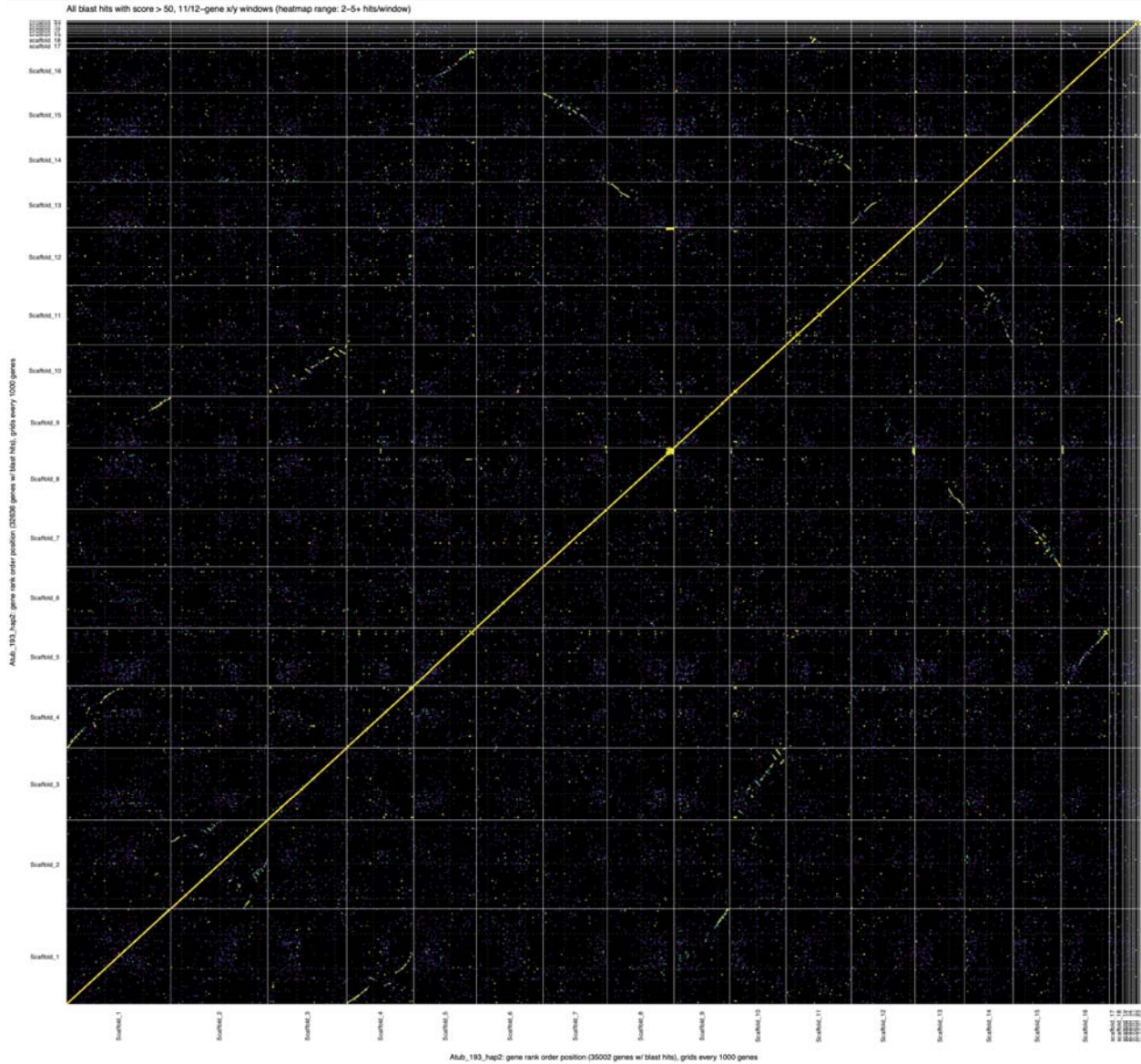
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776 **Sup Figure 6.** Upper) The difference in heterozygosity between males and females is heightened
777 in the sex-linked region, along with allelic differentiation (Fst: Middle Lower) between males
778 and females, where points represent the mean in 1 kb genomic windows. In both plots, the 95%
779 CI of these summary statistics across autosomes is delimited by the horizontal dashed white
780 lines.

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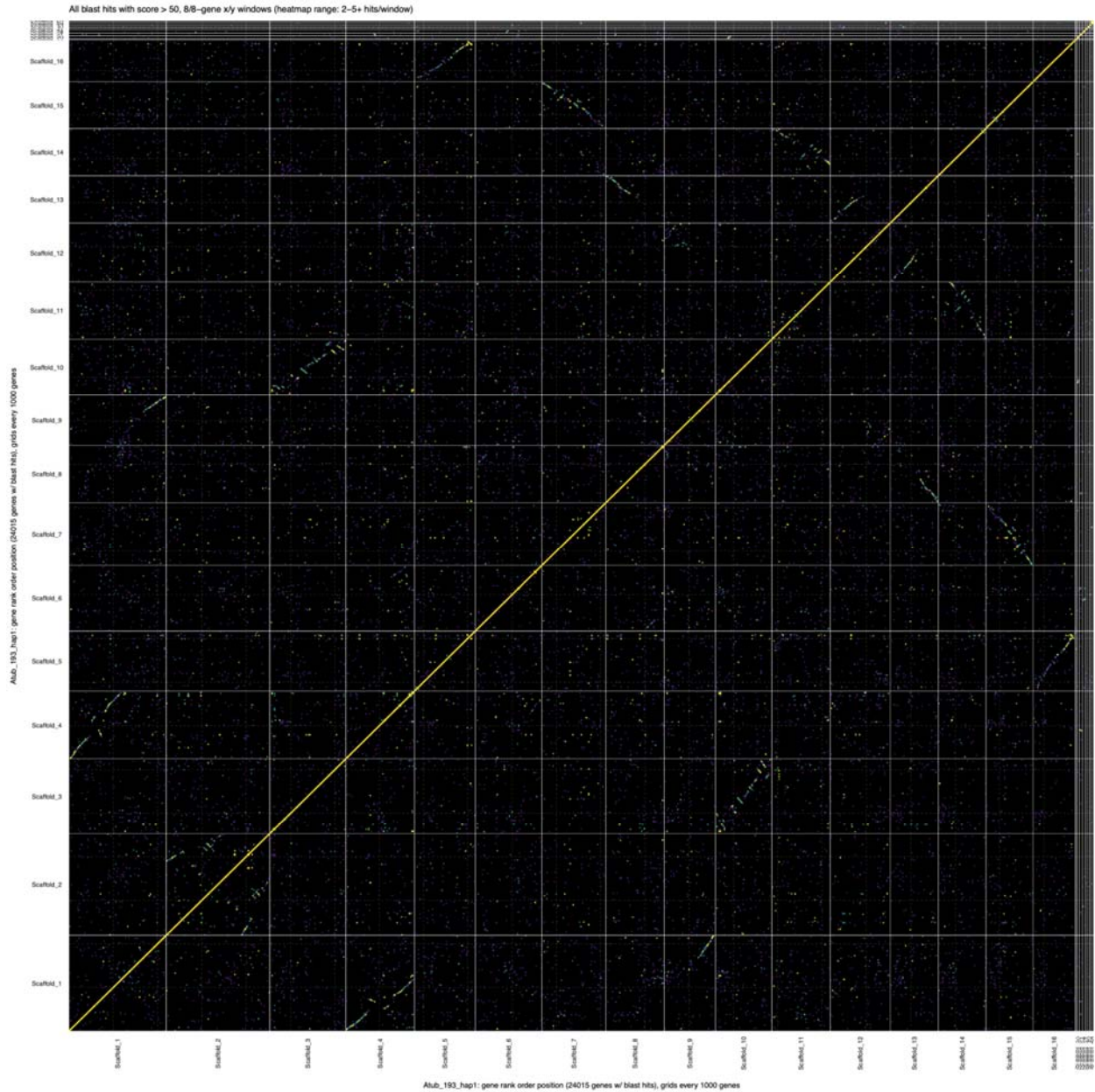
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790 **Sup Figure 7.** Male versus Female coverage for loci significantly associated with sex (FDR <
791 0.05). Color indicates whether loci are located on the sex-linked, “target” scaffold_1, or on other
792 scaffolds across the genome.

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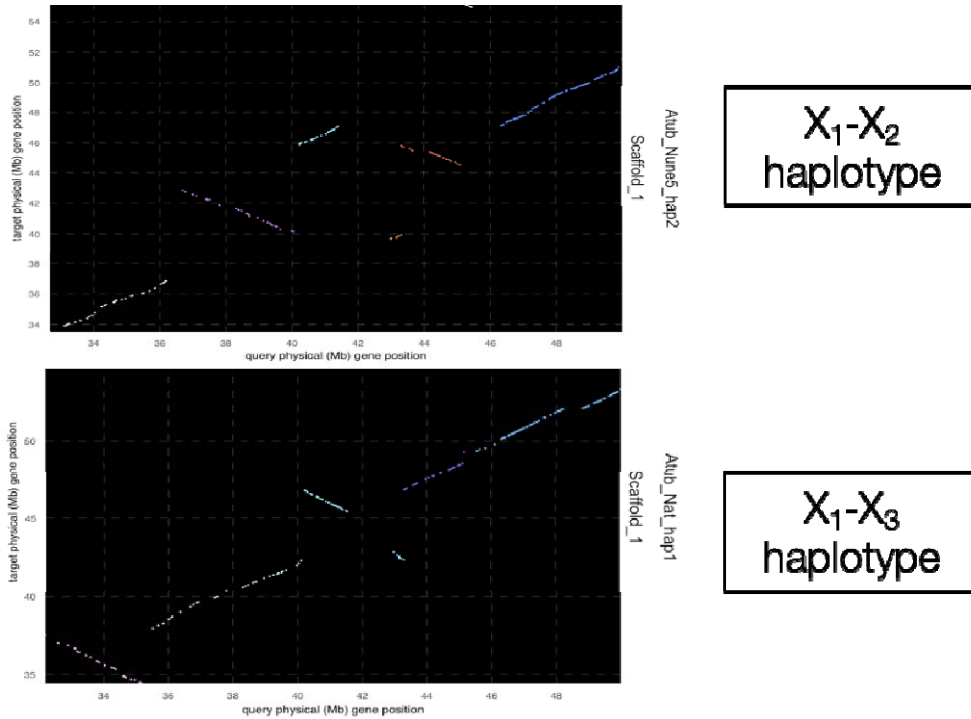
Sup Figure 8. Dotplot of synteny between haplotype 2 and itself (our focal assembly for which population genomic was aligned to, the individual from Walpole], where dots are gene blast hits with score > 50 inferred from the genespace pipeline. Evidence of a past whole-genome duplication event is evident, as every scaffold shows contiguous stretches of synteny with one or more scaffolds.



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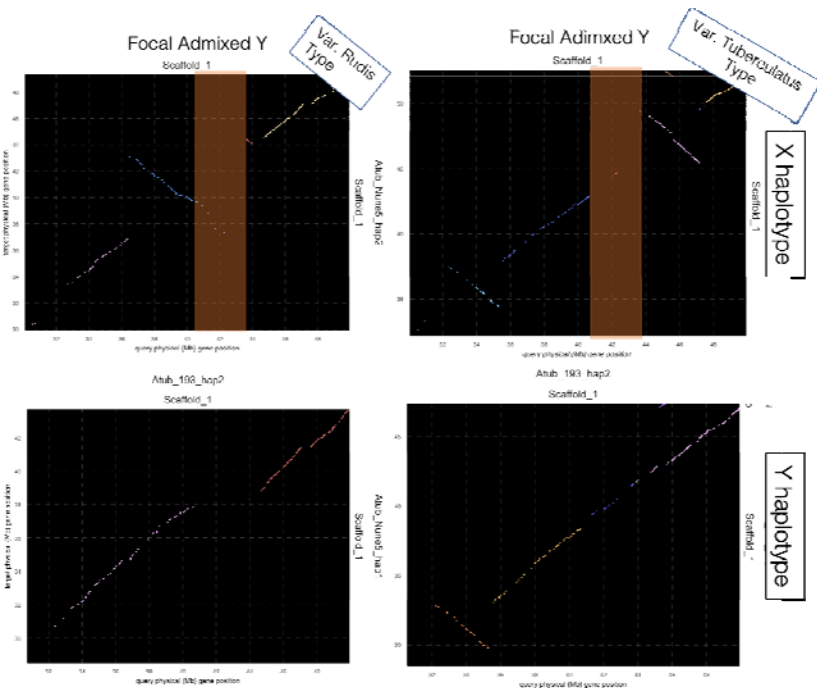
Sup Figure 9. Dotplot of synteny between haplotype 1 against itself [from the Walpole male], where dots are gene blast hits with score > 50 inferred from the genespace pipeline. Evidence of a past whole-genome duplication event is evident, as every scaffold shows contiguous stretches of synteny with one or more scaffolds.

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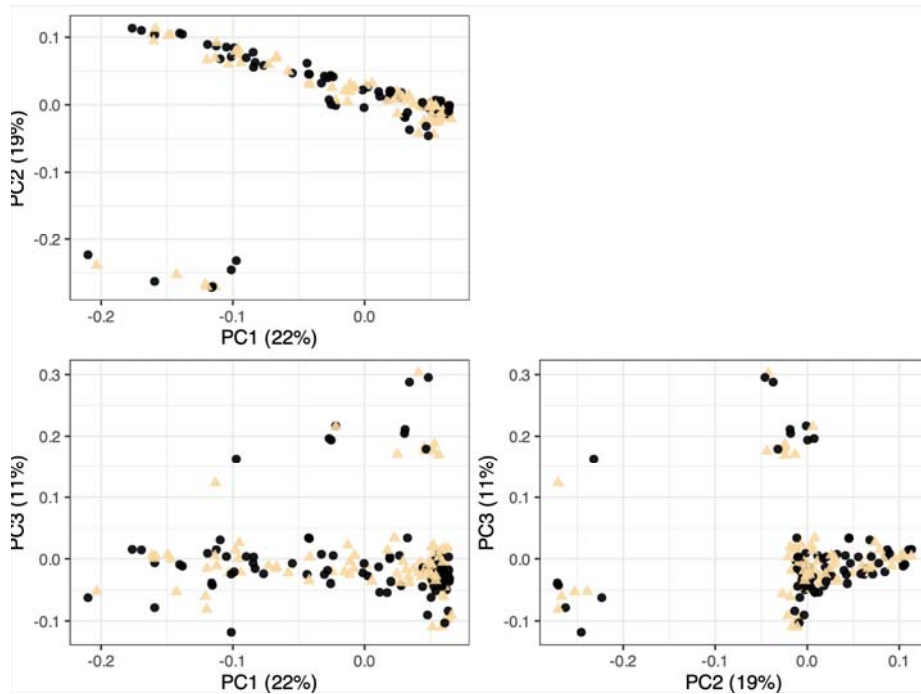
Sup Figure 10. Dotplots of syntenic genes between X haplotype assemblies of the sex-linked region. Colors represent orthologous grouping (i.e. tracts of contiguous syntenic sequence).



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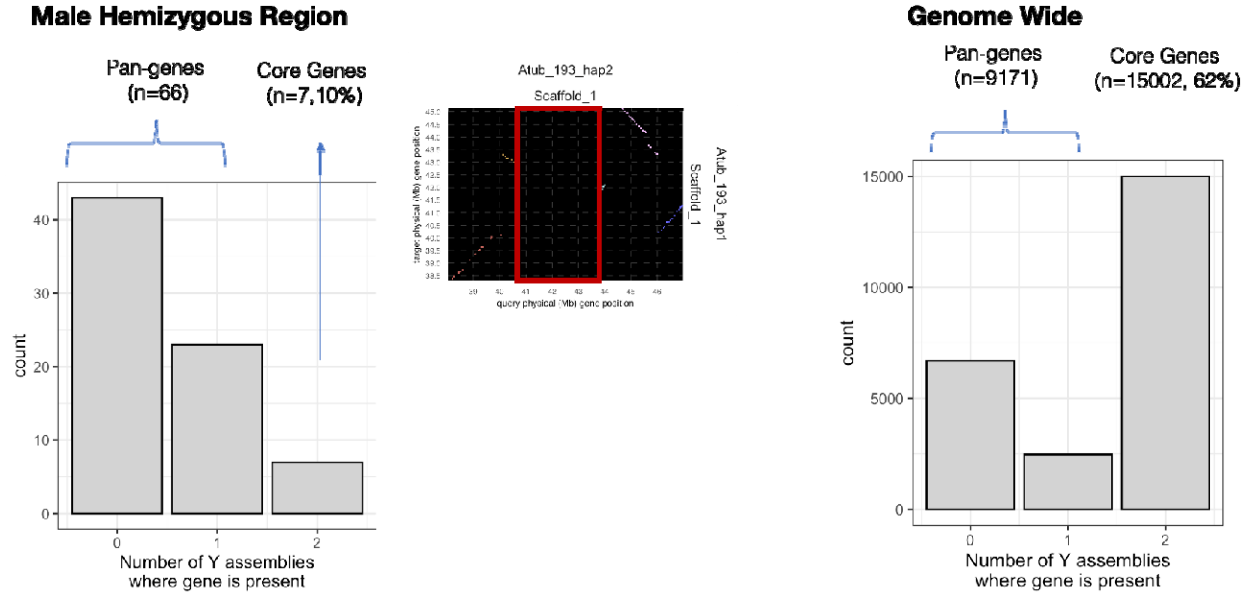
Sup Figure 11. Pairwise comparisons of synteny for our focal-Y (admixed type) and the X and Y haplotypes of the var. *rudis* type individual (left) var. *tuberculatus* type (right).

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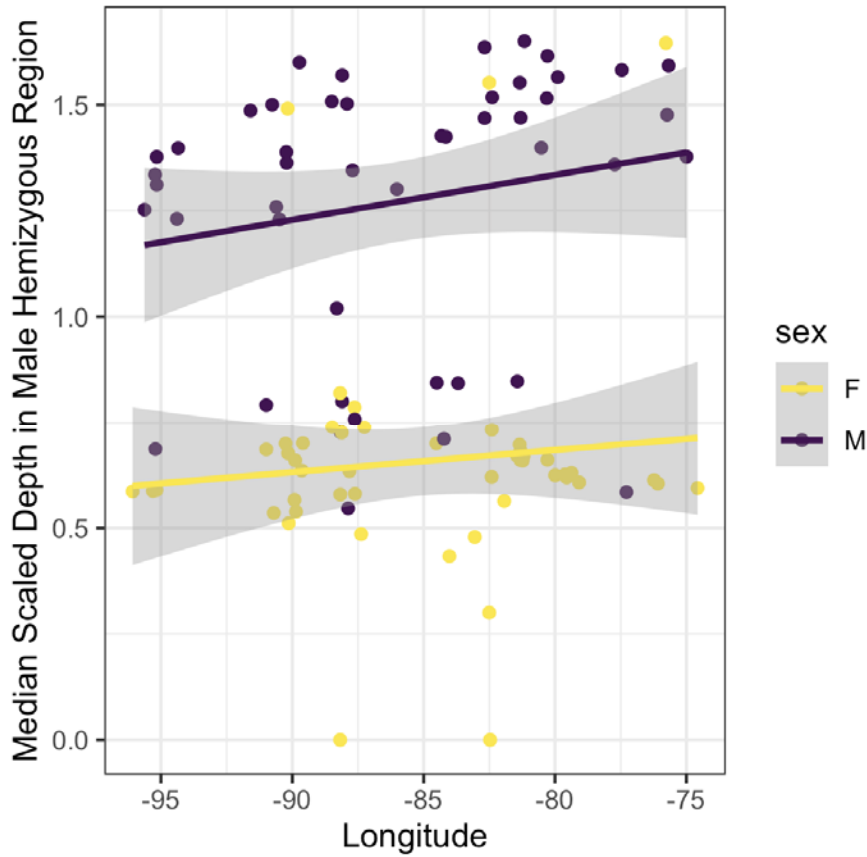
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Sup Figure 12. Structure in the inversion (Sup Table 1 number 5* and 14*) just upstream of the sex-linked region. Points (individual genomes) coloured by phenotypic sex assignment (cream = male, black = female), illustrating the lack of sex-based structure in this inversion.



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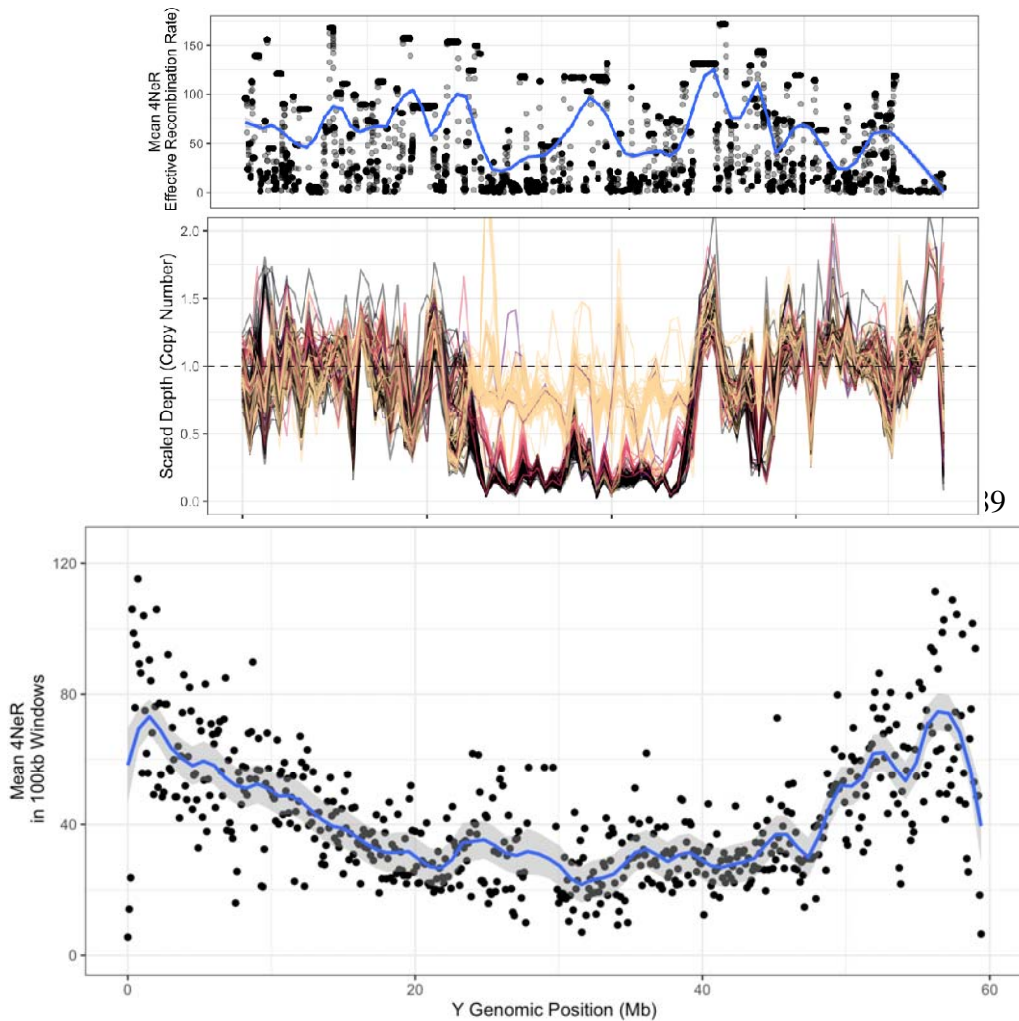
Sup Figure 13. Enriched gene presence-absence variation in the sex-linked region, compared to genome wide.



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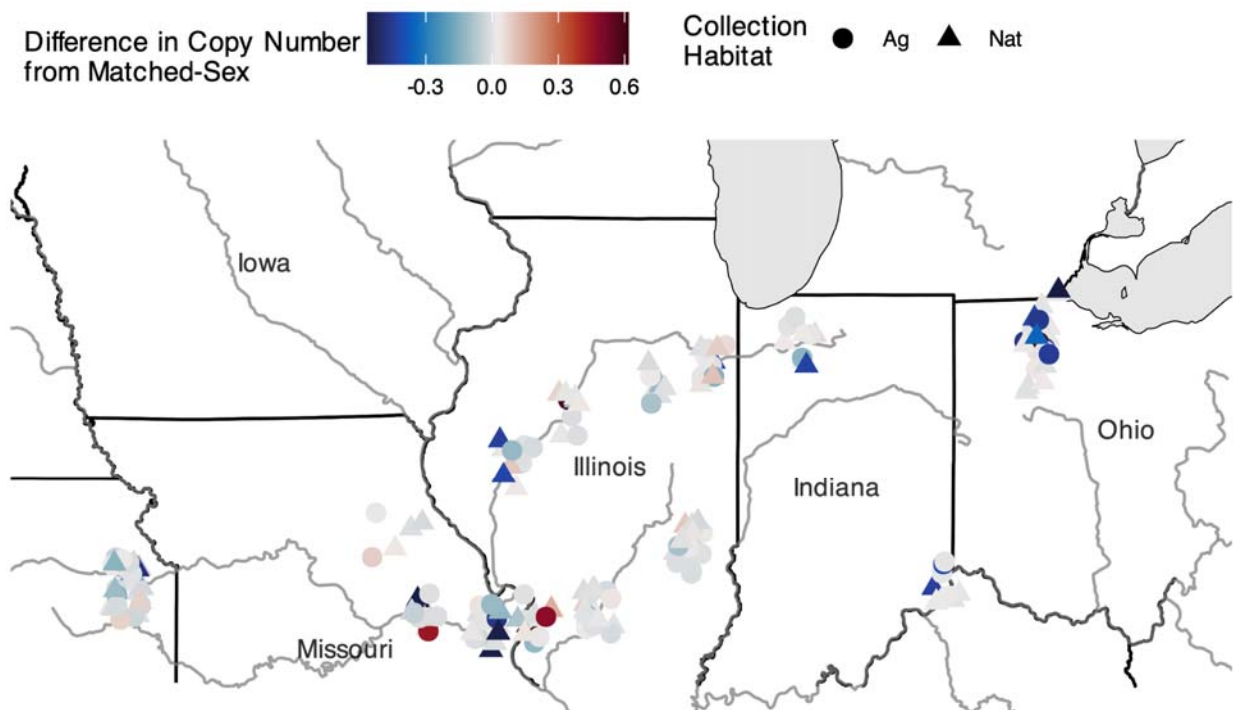
855 **Sup Figure 14.** Median scaled depth in sex linked region for an independent dataset [94],
856 illustrating genotype-phenotype mismatch. 10 males show depth profiles more similar to females
857 than expected, and 3 females show depth profiles more similar to females.
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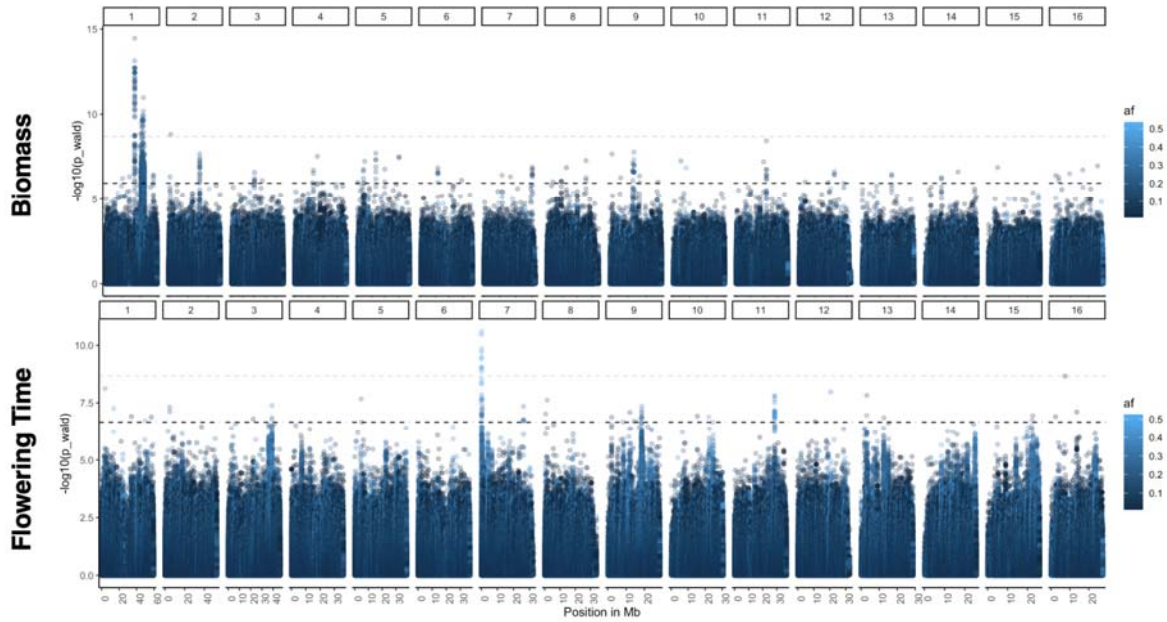
Sup Figure 15. LDhat inferred effective recombination rate. *Top*) Effective recombination rate along the sex linked region on haplotype 2 (the Y containing haplotype) of Scaffold 1, along with copy number variation for context (*Middle*), and the effective recombination rate landscape across the entire haplotype 2 of Scaffold 1 (*Bottom*).



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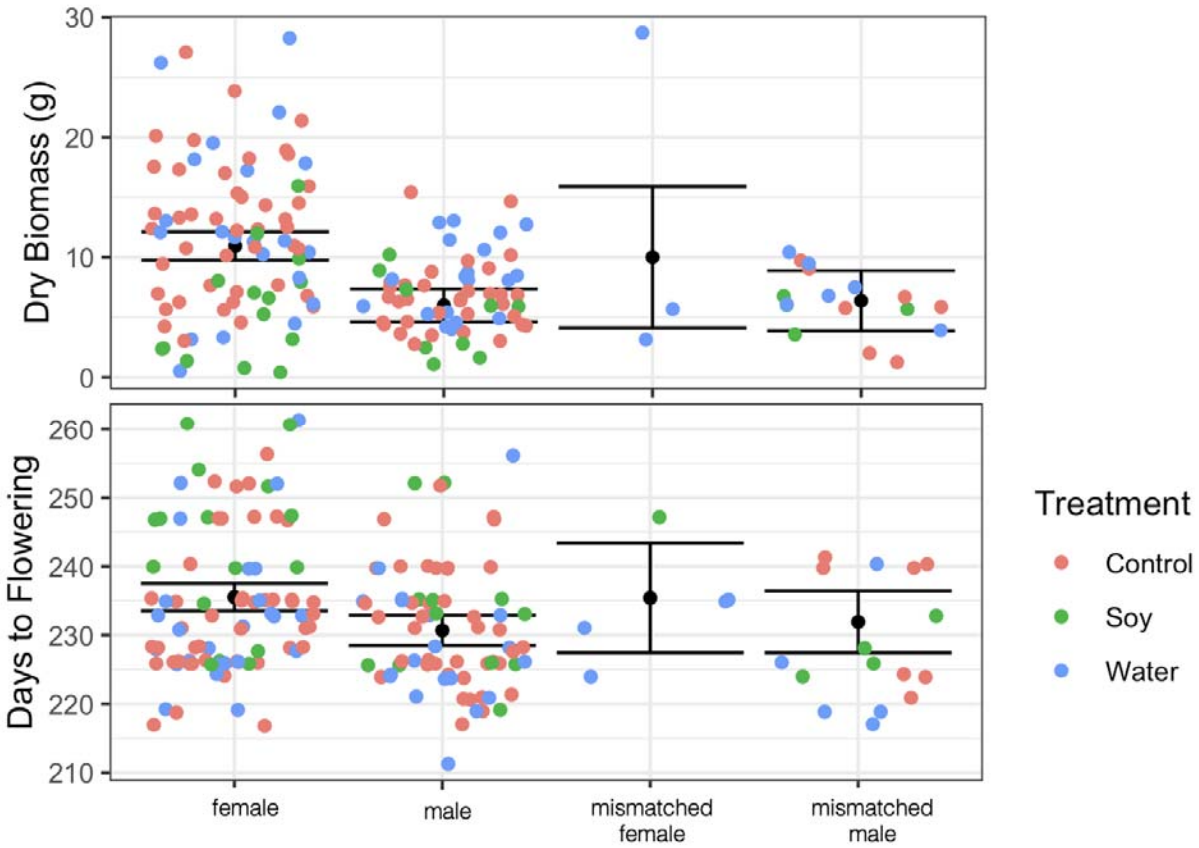
Sup Figure 16. The geographic distribution of the difference in copy number between an individual and mean copy number of their respective sex-matched genotype. Color coding represents the degree of mismatch based on an individual's mean copy number across the region, and the mean copy number of the average sex-matched individual. Negative numbers indicate males who genotypically resemble most females, and who therefore have less sequence content in the SLR than most males, whereas positive values indicate females who genotypically resemble most males (have an excess of sequence content in the SLR).

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Sup Figure 17. Manhattan plots of GWA of family-mean biomass (top) and family-mean flowering time, based on mapping of reads to haplotype 2 of the Walpole admixed reference. The lower black horizontal dashed line represents the 5% FDR p-value threshold, while the upper dashed horizontal line represents the Bonferroni corrected 5% p-value threshold.



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942 **Sup Figure 18.** The distribution of biomass and days to flowering for individuals with different
943 phenotype-genotype groupings for sex. We see no significant difference in phenotypes between
944 mismatched individuals and their respective matched sex.
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961 **Supplementary Tables**

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964 **Sup Table 1.** Statistics for 6 haplotype-phased chromosome-level assemblies, from 3 male *A.*
 965 *tuberculatus*. *indicates that the initial HiFiasm assembly step was performed without Hi-C data.

	Walpole_hap1	Walpole_hap2	Nune_hap1	Nune5_hap2	Nat_hap1*	Nat_hap2*
Main genome scaffold total	1984	1060	1570	777	1652	574
Main genome contig total	2464	1497	2167	1311	2153	1001
Main genome scaffold seq total	678.737 MB	654.704 MB	648.107 MB	620.003 MB	646.622 MB	647.614 MB
Main genome contig seq total	678.641 MB	654.616 MB	647.988 MB	619.896 MB	646.522 MB	647.528 MB
Gap	0.014%	0.013%	0.018%	0.017%	0.015%	0.013%
Main genome scaffold N/L50	9/32 MB	8/34.048 MB	8/33.576 MB	8/33.357 MB	8/33.422 MB	8/33.162 MB
Main genome contig N/L50	48/2.327 MB	41/2.803 MB	51/2.194 MB	48/2.368 MB	53/2.428 MB	45/3.333 MB
Main genome scaffold N/L90	122/136.416 KB	25/910.168 KB	42/371.629 KB	16/24.153 MB	47/312.591 KB	17/3.405 MB
Main genome contig N/L90	498/93.793 KB	339/247.302 KB	467/152.867 KB	348/275.056 KB	421/155.35 KB	277/375.396 KB
Max scaffold length	57.876 MB	59.453 MB	54.404 MB	59.099 MB	61.224 MB	56.815 MB
Max contig length	19.248 MB	20.689 MB	16.635 MB	17.086 MB	19.341 MB	21.347 MB
Number of scaffolds > 50 KB	426	353	317	287	301	280
% main genome in scaffolds > 50 KB	93.24%	96.46%	94.88%	97.78%	93.96%	98.63%

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 968 **Sup Table 2.** List of Inversions relative to Atub_Walpole_hap2. Note that letter code demarcates
 969 the same inversion present across multiple pairwise comparisons (each referenced by the
 970 inversion number and alt_genome). Inversion C (5 and 14) represent the variant directly
 971 neighboring the SLR in Atub_Walpole_hap2.

Inversion Number	Ref_Scaf	Start	End	Alt_Genome
1	Scaffold_1	25970434	30554490	Atub_Walpole_hap1
2A	Scaffold_1	7153812	7609088	Atub_Walpole_hap1
3	Scaffold_1	40126975	40143010	Atub_Walpole_hap1
4B	Scaffold_1	11910786	11950873	Atub_Walpole_hap1
5C	Scaffold_1	44656825	46017919	Atub_Walpole_hap1
6A	Scaffold_1	7153812	7609088	Atub_Nune_hap2
7	Scaffold_1	36429003	43364478	Atub_Nune_hap2
8	Scaffold_1	43375038	44017851	Atub_Nune_hap2
9A	Scaffold_1	7153812	7609088	Atub_Nune_hap1
10A	Scaffold_1	7153812	7609088	Atub_Nat_hap1
11B	Scaffold_1	11910786	12359692	Atub_Nat_hap1
12D	Scaffold_1	20165508	21398392	Atub_Nat_hap1
13	Scaffold_1	32372322	35290168	Atub_Nat_hap1
14C	Scaffold_1	43649837	47205224	Atub_Nat_hap1
15A	Scaffold_1	7153812	7609088	Atub_Nat_hap2
16D	Scaffold_1	20165508	21398392	Atub_Nat_hap2
17	Scaffold_1	21953637	23506917	Atub_Nat_hap2
18	Scaffold_1	32218868	35290168	Atub_Nat_hap2

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