Temporally delayed representations in alpha and beta rhythms in higher-

order cortical networks track increasing relational integration demands

Conor Robinson[1,2*], Luca Cocchi[1,2], Takuya Ito[3], Luke Hearne[1*]

[1]Clinical Brain Networks Group, QIMR Berghofer Medical Research Institute, Brisbane, QLD, Australia

[2]Faculty of Medicine, University of Queensland, Brisbane, QLD, Australia

[3]T.J. Watson Research Center, IBM Research Yorktown Heights, NY, USA

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*Corresponding authors

conor.robinson@qimrberghofer.edu.au, luke.hearne@qimrberghofer.edu.au

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Abstract

Relational reasoning is the ability to infer and understand the relations between multiple elements.
In humans, this ability supports higher cognitive functions and is linked to fluid intelligence.
Relational complexity (RC) is a cognitive framework that offers a generalisable method for
classifying the complexity of reasoning problems. To date, increased RC has been linked to static
patterns of brain activity supported by the frontoparietal system, but limited work has assessed the
multivariate spatiotemporal dynamics that code for RC. To address this, we conducted
representational similarity analysis in two independent neuroimaging datasets (Dataset 1 fMRI,
n=40; Dataset 2 EEG, n=45), where brain activity was recorded while participants completed a
visuospatial reasoning task that included different levels of RC (Latin Square Task). Our findings
revealed that, spatially, RC representations were widespread, peaking in brain networks associated
with higher-order cognition (frontoparietal, dorsal-attention, and cingulo-opercular). Temporally,
RC was represented in the 2.5 - 4.1 seconds post-stimuli window and emerged in the alpha and
beta frequency range. Finally, multimodal fusion analysis revealed the information carried in the
representation is concordant with the theorised RC model relative to a model of cognitive effort in
higher-order cortical networks. Altogether, the results further our understanding of what
information is held during relational processing, highlight the spatially distributed nature of RC
representations, and emphasise the importance of late frequency-resolved neural processes to
resolve RC.

Significance statement

Assessing cognitive abilities in human reasoning requires a cognitive framework that can define a
problem's complexity. Relational complexity (RC) theory has emerged as a robust framework,
parameterising complexity based on the number of relations that must be processed in parallel to
solve a problem's underlying relational representation. To investigate 'where' or 'when' the brain
codes for this cognitive abstraction, our study examined multimodal whole-brain activity during
short reasoning problems at various complexity levels. We found that higher-cortical networks
coded a representation tracking the transition between complexity demands, emerging during late-
stage cognitive processing. Our findings provide neuroscientific evidence for a neural coding of
relational complexity, pinpointing the frequency-resolved dynamics associated with these
mechanisms.

Introduction

Relational reasoning, the ability to mentally manipulate and integrate relationships between interacting elements, is a core component of higher-order cognition and a hallmark of human intelligence (Waltz et al., 1998; Halford et al., 2010). Studies on relational reasoning reveal fundamental capacity limitations in the number of relations that can be processed simultaneously (Halford et al., 2005). This constraint is formalised within relational complexity (RC) theory, a framework that has uncovered performance boundaries in everyday problem-solving (Boag et al., 2006), neurodevelopment (Halford et al., 1998; Eslinger et al., 2009; Todd et al., 2019), and clinical populations (Goel and Grafman, 1995; Hearne et al., 2019). While numerous studies have demonstrated the broad utility of RC theory, a key open question remains: where and when does the brain represent RC?

Functional magnetic resonance imaging (fMRI) work has provided a map of the brain *spatial* correlates of relational reasoning (Wertheim and Ragni, 2018). This body of work has led to the perspective that a frontoparietal network (FPN), also known as the multiple-demand network, is essential for performing relational reasoning tasks (Duncan and Owen, 2000; Cocchi et al., 2013; Hearne et al., 2017; Holyoak and Monti, 2021; Morin et al., 2022). Further work has emphasised interactions between the FPN and other brain systems, such as the cingulo-opercular and sensory networks while performing complex reasoning tasks (Cocchi et al., 2013; Cole et al., 2013; Hearne et al., 2017). Studies have typically emphasised the univariate association between specific brain activations (or functional connections) and relational demands, rather than how a given brain region might code for reasoning complexity (Freund et al., 2021). Thus, it remains unclear how the spatial correlates described by prior work relate to neural representations underlying RC.

Despite significant advances in the spatial mapping, the temporal dynamics of RC have not been well documented. A handful of electroencephalography (EEG) event-related studies have investigated reasoning demands, typically reporting deviations in the amplitude of event-related potentials as a function of complexity (Cutmore et al., 2015; Xiao et al., 2022). However, these studies did not analyse the entire cognitive processing period or frequency-resolved activity, largely due to uncertainties about how relational processing unfolds in time. While distinct from RC (Halford et al., 1998; Andrews et al., 2006), research on working memory in humans and non-

human primates has demonstrated the crucial role of synchronised neural oscillatory activity in

alpha and beta frequency bands (Miller et al., 2018; John et al., 2022; Fulvio et al., 2024).

Combining fMRI mapping with an analysis of the oscillatory temporal dynamics underpinning RC

is likely to assist in the delineation of a core temporal and spatial signature supporting the neural

representation of abstract relational integration.

To explore the spatiotemporal representation of RC, we used the Latin Square Task (LST), a

visuospatial reasoning task where participants solve short Sudoku-like puzzles (Birney et al., 2006;

Hearne et al., 2020). Cognitive demands were modulated by changing the minimum number of

relations that needed to be integrated to infer the solution. Representational Similarity Analysis

(RSA) provided a means to fuse multiple datasets rich in multimodal spatial and temporal

information to assess where and when RC is represented in the brain (Kriegeskorte et al., 2008).

To this end, we pooled data from two independent studies assessing brain activity using fMRI and

EEG while participants completed the LST at three levels of relational complexity. In line with

prior studies, we predicted that RC representations would emerge in higher-order associative

networks responsible for executive control in relational integration (Cocchi et al., 2013). We

anticipated that the emergence of a RC representation via the integration of information across

distinct brain systems would be observable in alpha and beta oscillations. Finally, we extended our

analysis by employing a model-based fusion approach (Cichy et al., 2014) to quantify the unique

contribution of RC to the shared spatiotemporal representation between neuroimaging datasets.

Materials and Methods

Participants

Participants were pooled across two independent datasets. In the first dataset, sixty-five healthy,

right-handed participants completed the LST while undergoing fMRI (final n = 40, see exclusion

criteria in the *fMRI preprocessing* section below; mean = 23 years old; age range = 18 - 33; 60%

female). This dataset has been used in prior publications (Hearne et al., 2017; Shine et al., 2019).

In the second dataset, forty-seven healthy participants completed the LST concurrently with EEG

(final n=45, see the *EEG preprocessing* section for exclusions; mean = 25; age range = 19 - 33;

62% female). Ethics approval was granted by the University of Queensland Human Research

Ethics Committee (dataset one) and the QIMR Berghofer Research Ethics Committee (dataset

two). In both experiments, participants provided written informed consent and were eligible if aged

between 18 - 35 with no previous reported history of mental health or neurological disorder.

Experimental design

The LST is a nonverbal relational reasoning experimental task (Birney et al., 2006). Each LST

puzzle involves the presentation of a four-by-four grid populated by shapes (squares, triangles,

circles and crosses) and a target question mark. Participants are asked to solve what shape the

question mark must be, given that *an item or object can only exist once in every row and column*

(similar to sudoku). As shown in **Figure 1a**, puzzle complexity (Binary, Ternary and Quaternary)

was modulated by modifying the number of items that needed to be interrelated in one step to solve

the problem. Binary relations required linking items across a row or column, Ternary relations row

and column, and Quaternary problems multiple rows and columns. In the second dataset, puzzles

consisted of different coloured circles, rather than different shapes (A, B, C and D).

Each relational complexity condition comprised of twelve unique puzzle designs. Additional trials

were generated by rotating each puzzle by 90 degrees (Hearne et al., 2020; Hartung et al., 2022).

In the first dataset, this was performed twice to generate 36 trials at each complexity level. In the

second dataset, this was performed thrice to generate 48 trials at each complexity level. Increased

trial numbers were warranted in the second dataset due to EEG artefact rejection. For each dataset,

the puzzle rotations were averaged to generate brain activation estimates for twelve trials per

condition, thirty-six trials in total (see the *representation similarity analysis* section below for

details).

Trials were presented in a pseudo randomised order, ensuring that two trials of the same

complexity level were not presented sequentially. To optimise the number of trials for imaging

acquisition the stimulus duration was slightly modified for each modality. In the first dataset,

problems were presented for 5 seconds, with a further 2 seconds to respond via a response screen.

In the second dataset, the stimulus time was 4.5 seconds puzzle onset and a 1.75 second response

window.

Neuroimaging acquisition, preprocessing and activation estimation

fMRI Dataset

As reported previously (Hearne et al., 2017), fMRI data were acquired on a 7 Tesla Siemens

scanner equipped with a 32-channel head coil at the Centre of Advanced Imaging, The University

of Queensland, Brisbane. Whole-brain echo-planar images were collected with the following

parameters: isotropic 2 mm voxels, TR = 586ms, TE = 23ms, flip angle = 40°, FOV = 208mm, 55

axial slices, multiband acceleration factor = 5. The LST was performed over three 12-minute runs

(1250 volumes). Structural scans (MP2RAGE) used in the preprocessing pipeline were acquired

with the following parameters: isotropic 0.75 mm voxels, TR = 4300ms, TE = 3.44 ms, and 256

slices. Stimuli were presented using PsychToolBox 3.0 (Brainard, 1997) onto a screen located at

the head end of the MR scanner, and participants viewed the projected stimuli via a mirror head-

mount. The grid layout of the puzzle was sized to fit within the field of view of participants,

removing the need for large eye-moment to peruse the grid space.

Data were preprocessed using fMRIPrep 21.0.1 (Esteban et al., 2019) [RRID:SCR_016216],

which is based on *Nipype* 1.6.1 (Gorgolewski et al., 2011) [RRID:SCR_002502]. Due to

differences in signal intensity in the temporal cortex with the rest of the brain, the raw T1-weighted

(T1w) images were intensity corrected using the SPM segmentation tool prior to the fMRIPrep

pipeline. Based on quality control checks this step ensured that different tissues were correctly

identified during the preprocessing pipeline. Following this, within the fMRIPrep pipeline, the

T1w image was corrected for intensity non-uniformity (INU) with N4BiasFieldCorrection

(Tustison et al., 2010), distributed with ANTs 2.3.3 (Avants et al., 2008) [RRID:SCR_004757],

and used as T1w-reference throughout the workflow. The T1w-reference was then skull-stripped

with a *Nipype* implementation of the antsBrainExtraction.sh workflow (from ANTs), using

OASIS30ANTs as target template. Brain tissue segmentation of cerebrospinal fluid (CSF), white-

matter (WM) and gray-matter (GM) was performed on the brain-extracted T1w using fast (FSL

6.0.5.1:57b01774, RRID:SCR_002823, (Zhang et al., 2001)). Brain surfaces were reconstructed

using recon-all (FreeSurfer 6.0.1, RRID:SCR_001847, (Dale et al., 1999)), and the brain mask

estimated previously was refined with a custom variation of the method to reconcile ANTs-derived

and FreeSurfer-derived segmentations of the cortical gray-matter of Mindboggle

(RRID:SCR_002438, (Klein et al., 2017)). Volume-based spatial normalization to standard space

was performed through nonlinear registration with antsRegistration (ANTs 2.3.3), using brain-

extracted versions of both T1w reference and the T1w template. *FSL's MNI ICBM 152 non-linear*

6th Generation Asymmetric Average Brain Stereotaxic Registration Model was used for spatial

normalisation   [(Evans   et   al.,   2012),   RRID:SCR_002823;   TemplateFlow   ID:

MNI152NLin6Asym].

For each of the three BOLD runs found per subject the following preprocessing was performed.

First, a reference volume and its skull-stripped version were generated by aligning and averaging

1 single-band references (SBRefs). Head-motion parameters with respect to the BOLD reference

(transformation matrices, and six corresponding rotation and translation parameters) are estimated

before any spatiotemporal filtering using mcflirt (FSL 6.0.5.1:57b01774, (Jenkinson et al., 2002)).

BOLD runs were slice-time corrected to 0.268s (0.5 of slice acquisition range 0s-0.535s) using

3dTshift from AFNI ((Cox and Hyde, 1997), RRID:SCR_005927). The BOLD time-series were

resampled onto their original, native space by applying the transforms to correct for head-motion.

These resampled BOLD time-series will be referred to as *preprocessed BOLD in original space*,

or just *preprocessed BOLD*. The BOLD reference was then co-registered to the T1w reference

using bbregister (FreeSurfer) which implements boundary-based registration (Greve and Fischl,

2009). Co-registration was configured with six degrees of freedom. First, a reference volume and

its skull-stripped version were generated using a custom methodology of *fMRIPrep*. The three

signals are extracted within the CSF, the WM, and the whole-brain masks. The BOLD time-series

were resampled onto *fsaverage* surface space. *Grayordinates* files (Glasser et al., 2013) containing

91k samples were also generated using the highest-resolution fsaverage as intermediate

standardized surface space. All resamplings can be performed with *a single interpolation step* by

composing all the pertinent transformations. Gridded (volumetric) resamplings were performed

using antsApplyTransforms (ANTs), configured with Lanczos interpolation to minimize the

smoothing effects of other kernels (Lanczos, 1964). Non-gridded (surface) resamplings were

performed using mri_vol2surf (FreeSurfer). Given the RSA calculates similarities between voxel

/ vertex activation patterns without spatial smoothing, any subjects exceeding 2 mm of head motion

(six rotation and translation parameters) were excluded from further analysis (final *n*=40). After

fMRIPrep, the functional data were further denoised by regressing fourteen nuisance signals (mean

cerebrospinal fluid and white matter signals, along with the six motion parameters and their

derivatives) using Nilearn (Abraham et al., 2014).

To estimate brain activations, whole-brain general linear model (GLM) analyses were conducted

using Nilearn (Abraham et al., 2014) for each participant's grayordinate surface and volumetric

data. Using a previously established method to estimate trial-by-trial activation patterns (Mumford

et al., 2012), a separate GLM was performed for each of the 36 puzzles in the experiment. Each

design matrix included two regressors; one for the three trials of interest (three rotations of the

puzzle) and another for all other trials in the experiment. Each trial was modelled as a five second

boxcar regressor convolved with the canonical hemodynamic response function. Three additional

regressors were included to account for each run of the experiment. This procedure resulted in

brain activation estimates for each of the 36 puzzles across the brain which were subsequently

analysed using RSA.

EEG Dataset

EEG recordings were digitised at 2000 Hz using an ANT-neuro system with a 64 channel cap

arranged in the 10-20 layout. Experimental stimuli were presented on a BenQ 24 inch computer

monitor with the task paradigm implemented using PsycoPy toolbox (v2020.2.10) (Peirce et al.,

2019). Similar to Dataset 1, the grid layout of the puzzle was sized to fit within the field of view

of participants.

EEG recordings were preprocessed offline using EEGLAB (Delorme and Makeig, 2004). The

continuous data underwent high-pass finite impulse response (FIR) filtering at 0.5 Hz to remove

low-frequency drifts. Line noise centred at 50 Hz was eliminated using a notch filter spanning

47.5-52.5 Hz, followed by a 97 Hz low-pass filter to attenuate harmonic components. Bad

channels, identified through visual inspection, were excluded before re-referencing to the average

of all remaining channels, excluding the M1, M2, and EOG electrodes. The data were then

downsampled to 250 Hz. Trial epochs were generated using the stimulus onset as a marker

resulting in a -400 ms pre-stimulus and 4500 ms post-stimulus window. After independent

component analysis (ICA) based artefact rejection, the excluded bad channel data were

reconstructed using spherical spline interpolation. Finally, the signal underwent band-pass filtering

within the EEG observable range of 1-45 Hz. Two subjects were removed from the final analysis

due to excessive muscle artefacts.

EEG data was further processed and frequency decomposition performed using the MNE Python

library (Gramfort et al., 2013). Epochs were baseline-corrected by subtracting the mean signal

during the pre-stimulus period from the entire epoch (stimuli onset to 4500 ms). To investigate

oscillatory dynamics across different frequency bands, the epoched timeseries data were

decomposed into canonical frequency bands using zero-phase bandpass filtering. Specifically, the

following frequency ranges were extracted: theta (4-8 Hz), alpha (8-12 Hz), beta (13-30 Hz), and

gamma (30-45 Hz).

Representation similarity analysis

fMRI and EEG puzzle-induced brain activity were transformed to a common representational

"puzzle space" using RSA (Kriegeskorte et al., 2008). RSA aims to model the similarity structure

of brain activation patterns in response to differing tasks, conditions, or stimuli (**Figure 1**).

Specifically, we estimated (dis)similarity between brain responses evoked by the 36 LST puzzles

using the squared Euclidean distance. Representational dissimilarity matrices (RDMs), generated

in both the fMRI and EEG datasets, were compared to a cognitive model, as well as each other

(described below).

fMRI dataset

fMRI-RDMs were generated for 376 brain regions using the Glasser cortical parcellation (Glasser

et al., 2016), and the Melbourne 3T S1 subcortex parcellation (Tian et al., 2020). For each

participant and brain region, fMRI GLM coefficients (z-scored) for each of the 36 LST puzzles

were organised into a puzzle-by-vertex (or voxel, in subcortex) activity pattern matrix. The RDM

was then calculated as the puzzle-by-puzzle (36 x 36) squared Euclidean distance. Additionally,

the resulting RDMs were averaged into thirteen previously established functional brain networks

(Ji et al., 2019): auditory, cingulo-opercular, default, dorsal-Attention, frontoparietal, language,

orbito-Affective, posterior-multimodal, somatomotor, subcortical, ventral-multimodal, and visual

brain networks.

EEG dataset

For each participant and time point (1225 time points sampled at 250 Hz), preprocessed sensor-
level EEG responses were organised into a puzzle-by-sensor activity pattern matrix. The RDM
was then calculated as the puzzle-by-puzzle (36 x 36) squared Euclidean distance. This was
performed for broadband signals and specific frequency ranges (theta, alpha, beta, and gamma,
described previously). Following this, the RDMs were down-sampled into 50 sequential time
segments of 100 ms each.

Relational complexity model
The RDM coding for the cognitive construct of relational complexity (Halford et al., 1998) is
shown in **Figure 1B**. According to this model, puzzles within the same complexity condition
(Binary, Ternary, or Quaternary) evoke *similar* brain activation patterns, regardless of the specific
visual configuration of stimuli within the puzzle (e.g., squares, triangles, circles and crosses). This
model also predicts that puzzles from different complexity conditions will elicit *dissimilar*
activation patterns in a graded fashion, with Binary (easy puzzles) and Quaternary (difficult
puzzles) conditions being maximally distant. Therefore, brain regions or time periods exhibiting
high correspondence to this cognitive model would provide evidence that the underlying neural
representations are tracking relational complexity demand rather than other factors (e.g., stimulus
arrangement).

Cognitive effort model
In a similar approach to Chiou et al. (2024), we defined a data-driven 'cognitive effort' model. The
model was generated using behavioural performance from both datasets. Specifically, the
Euclidian distance was calculated between each puzzle's accuracy and response time (averaged
across participants). In this model, problems that participants found easier or harder are clustered
together regardless of complexity level.

Figure 1: *Stimulus design and multivariate analysis approach*. Latin Square problems shown on the left required participants solve for the target square (solution highlighted in red) adhering to the rule that each item could only appear once in each row and column. Relational complexity was manipulated by varying the minimum number of interrelating rows and columns (highlighted in yellow) to solve for the missing item. The three puzzles illustrate example Binary, Ternary, and Quaternary complexity levels. Each cell in the corresponding-coloured vector represents one of the 36 original puzzle designs, with 12 puzzles per complexity level. While completing the task, brain activity was recorded using fMRI (dataset 1, top, gold) and EEG (dataset 2, bottom, light green). Neurophysiological responses were converted into puzzle representational dissimilarity matrices (RDMs) based on the distances between activation patterns evoked by different puzzles. Spatial fMRI RDMs were derived by correlating vertex or voxel activity patterns within parcellated brain regions for each puzzle. Temporal EEG RDMs were generated by correlating sensor-level activity patterns at each timepoint across puzzles. These spatial and temporal RDMs were (1) compared to the theoretical relational complexity model (B) and (2) assessed for spatial-temporal co-occurrence.

fMRI-EEG fusion analysis

We used commonality analysis (Hebart et al., 2018) to determine how much of the shared variance between EEG and fMRI RDMs could be explained by our RC and cognitive effort models. The commonality coefficient compares two semi-partial correlation coefficients (Spearman correlation). The first specifies the proportion of variance shared between EEG and fMRI when partialling out all model variables except the model of interest (e.g., the RC model) from fMRI. The second reflects the proportion of shared variance between EEG and fMRI after partialling out

328　　all model variables (including the variable of interest). The commonality coefficient is the

329　　difference between both coefficients of determination (R^2). We performed this analysis for each

330　　brain network and time point, tracking the unique contributions of each model across space and

331　　time. Formally, for time t and network j the commonality coefficient is defined as:

332
$$C_{X_t,(Y_j,A)} = R^2_{X_t,(Y_j.B)} - R^2_{X_t,(Y_j.A,B)}$$

where X indicates EEG, Y indicates fMRI, A reflects the RC model, and B reflects the cognitive

effort model.

Follow-up fMRI frontoparietal and EEG whole-brain sensor activity

As a supplementary analysis, we examined how activity in the FPN varied across the three

complexity conditions. To do so, we averaged the GLM beta coefficients across each condition for

each participant within each FPN region. These values were averaged across regions to generate a

single value per participant, per condition.

For the spectral characteristics of the EEG data, we computed the power spectral density (PSD)

using Welch's method within the data-driven beta RSA time window of interest, spanning 2.1 to

4.2 seconds post-stimulus onset. The PSD was calculated using segments of 500 samples with a

50% overlap. We applied a frequency range of interest from 2 to 45 Hz. Each participant's PSD

were averaged over trials and channels to obtain a whole-brain sensor level measure of power for

each complexity condition.

The periodic and aperiodic spectral parameterisation algorithm (version 2.0.0rc2) was used to

parameterise neural power spectra (Donoghue et al., 2020). Settings for the algorithm were set as:

peak width limits: (0.5, 12.0); max number of peaks: inf; minimum peak height: 0.0; peak

threshold: 2.0; and aperiodic mode: 'fixed'. Power spectra were parameterized across the frequency

range 2.0 to 45.0 Hz. High model fits of the parametrised spectrum were consistent across

complexity conditions: $R^2_{Binary} = 0.975 \pm 0.014, R^2_{Ternary} = 0.973 \pm 0.013, R^2_{Quaternary} =$

$0.973 \pm 0.014, F(2,88) = 0.318, p = 0.729.$ Using the previously defined fixed beta (13-30 Hz)

frequency range we extracted the periodic peak frequency for each subject across conditions from

the modelled spectrum. Five subjects were excluded as a peak could not be defined across all

conditions.

Statistical analysis

Task performance (accuracy and response time) in each dataset was assessed using a one-way repeated measures ANOVA. To compare performance between the datasets, Spearman correlations were conducted on the participant-averaged puzzle level performance (accuracy and response time) between the two datasets.

The spatial (fMRI) and temporal (EEG) RDMs were compared with the relational complexity model RDM (**Figure 1B**) using Spearman rank correlation without tie correction (Nili et al., 2014). For each participant and each brain region, network, or epoch, the vectorized upper triangle of each empirical RDM was correlated with the vectorized upper triangle of the model RDM. These correlation values - or coding strengths - underwent normalisation via the Fisher z-transformation, and were entered into a one-sample t-test (Vallat, 2018). All three analyses were multiple comparisons corrected using the False Discovery Rate (FDR), $\alpha = 0.05$ (fMRI $n_{regions} = 376$, $n_{networks} = 13$, EEG $n_{epochs} = 50$) (Benjamini and Yekutieli, 2001).

Statistical significance in the fMRI-EEG fusion analysis was assessed using a permutation test within each time bin (N=5000, (Hebart et al., 2018)). For each permutation, we randomly shuffled the rows and columns of the EEG RDMs (Kriegeskorte et al., 2008) and recomputed the commonality coefficients, generating a null distribution of coefficient time courses for each network. P-values were calculated as the proportion of permutations that exceeded the empirical commonality coefficient. These p-values were subsequently corrected for multiple comparisons using FDR.

Finally, an exploratory analysis was conducted to relate individual differences in brain representations and LST performance. Specifically, a Spearman correlation was performed between the relational complexity model coding strength and LST accuracy. For the EEG data, each individual's peak coding value was used. Given the exploratory nature of this analysis it was only performed in networks and frequency bands that demonstrated high coding strengths in the initial analyses (four networks and two frequency bands). A one-way repeated measures ANOVA

389 was used to assess the follow-up brain activation measures of the frontoparietal network and the

390 beta band power.

392 **Code and data availability**

Results

Effect of relational complexity on accuracy and response time

Participants completed relational reasoning problems at three complexity levels (**Figure 2**). As

shown in **Figure 2A** (top), results from both fMRI and EEG datasets demonstrated the

characteristic degradation in performance accuracy as complexity increased: Binary ($Mean_{fMRI}$ =

96.66%, $Mean_{EEG}$ = 95.00%), Ternary ($Mean_{fMRI}$ = 87.02%, $Mean_{EEG}$ = 80.69%), and Quaternary

($Mean_{fMRI}$ = 66.25%, $Mean_{EEG}$ = 56.30%); $F(2, 78)_{fMRI}$ = 80.61, $p < 0.0001$, and $F(2, 88)_{EEG}$ =

101.60, $p < 0.0001$. Correspondingly, response times **Figure 2A** (bottom), increased with

complexity: Binary ($Mean_{fMRI}$ = 0.74 ms, $Mean_{EEG}$ = 0.61 ms), Ternary ($Mean_{fMRI}$ = 0.81 ms,

$Mean_{EEG}$ = 0.78 ms), and Quaternary ($Mean_{fMRI}$ = 0.93 ms, $Mean_{EEG}$ = 0.87 ms); $F_{fMRI}(2, 78)$ =

51.09, $p < 0.0001$ and $F(2, 88)_{EEG}$ = 108.00, $p < 0.0001$. To assess consistency across datasets,

puzzle performance was averaged across participants in each dataset and correlated. Both accuracy

(rs = 0.95, $p < 0.001$) and response time (rs = 0.83, $p < 0.001$) demonstrated a high correspondence

between datasets (**Figure 2B**).

Figure 2. *Behavioural performance in the Latin Square Task*. **A.** Results replicated the expected degradation in accuracy (top panel) and delay in response time (bottom panel) associated with increased relational complexity across both fMRI (n=40) and EEG (n=45) datasets. **B.** Participant performance on the original 36 puzzles showed a positive correlation between fMRI and EEG datasets for both accuracy (top panel, rs = 0.95, p < 0.001) and reaction time (bottom panel, rs = 0.83, p < 0.001).

Spatial and temporal emergence of relational complexity

We conducted an RSA comparing the relational complexity model (**Figure 1b**) to representations derived from puzzle-evoked fMRI and EEG data. In the fMRI data, analyses were conducted at the region (**Figure 2a**) and network level (**Figure 2b**). Surprisingly, we observed strong relational complexity coding expressed across the whole brain. Of the 376 possible brain regions tested, 367 demonstrated significant correspondence to the model (p_{FDR} < 0.05). However, as expected, peak representational values were observed in prefrontal and parietal cortices: the superior premotor subdivision (6a), superior parietal cortex (7PL, 7Pm, 7Am, VIP, AIP, MIP), inferior parietal cortex (IP2, PGp), dorsal visual transitional area (DVT), anterior ventral insular area (AVI), medial prefrontal cortex (8bm) and dorsolateral prefrontal cortex (8C, i6-8). Accordingly, transmodal brain networks associated with goal-directed behaviour and higher-order cognition (Cole and Schneider, 2007; Duncan, 2010; Assem et al., 2020) demonstrated the strongest similarity to the

relational complexity model. Similar to the findings of the region-wise analysis, all networks

showed statistical similarity to the model (all networks survived $p_{FDR} < 0.05$).

To identify when the relational complexity construct emerged in time, the model was correlated

across the RDMs derived from the EEG broadband timeseries. The similarity timeseries (**Figure**

2c) revealed that relational complexity representations emerged during the 2.5 – 4.1 seconds

puzzle-stimuli window ($p_{FDR} < 0.05$). At the group level, the temporal trend of the representation

built over time, peaking at 4.1 s (peak correlation z = 0.037).

As a follow up analysis, we repeated the analysis in four canonical frequency bands (**Figure 3d**).

Interestingly, we only found significant RC model coding in alpha and beta frequencies (alpha 2.3

– 4.2 s, beta 2.1 – 4.2 s, $p_{FDR} < 0.05$). Both frequencies mirrored the temporal trend of the

broadband signal, peaking at 4.1 s (peak correlation, z = 0.049) and 3.2 s (peak correlation z =

0.052) for alpha and beta, respectively. Together, our results suggest that RC is i) most strongly

represented in brain networks supporting goal-directed external behaviour (e.g., dorsal attention

and frontoparietal networks), ii) emerges late in the trial period, and iii) is specifically related to

alpha and beta frequency bands.

Figure 3. *Spatial and temporal signatures of relational complexity derived from fMRI and EEG data.* **A.** Group averaged brain-wide correlations between fMRI-informed representations and the relational complexity model, colour bar indicates a transition from low (blue) to high (red) correspondence. Underneath a histogram displays the frequency ROI correlations mapped onto brain surface renderings (Glasser et al., 2016; Tian et al., 2020). **B.** fMRI results when down sampled into canonical brain networks (Ji et al., 2019), ordered by effect size. **C.** Group averaged correlation between EEG-informed representations and the RC model across time. Confidence intervals indicate standard error of the mean. Black line above indicates statistically significant time bins ($p_{FDR} < 0.05$). **D.** Frequency band derived EEG representations and the RC model across time, theta (4-8 Hz, pink), alpha (8-12 Hz, gold), beta (13-30 Hz, teal), and gamma (30-45 Hz, purple). Confidence intervals indicate standard error of the mean. Highlighted segments represent time periods where the EEG signal significantly correlated with the relational complexity model ($p_{FDR} < 0.05$).

Cross-modal fusion analysis of time and frequency-resolved patterns of network representations

Next, we asked when the representational structure in a given brain network (determined from fMRI) corresponds with the representations from the time-resolved EEG signal. Using the shared representation between modalities, we further wanted to determine how much RC accounted for the explained variance in the representation. To do so, we performed a model-based fMRI-EEG

fusion commonality analysis (**Figure 4a**) (Cichy et al., 2014; Hebart et al., 2018). This approach

also allowed us to compare a complementary cognitive effort model derived using participant

performance (details in Methods). In contrast to RC, the cognitive effort model proposes that the

information content coded in the representation can be retrospectively explained by the challenge

in mapping the underlying abstraction due to a confluence of puzzle-specific properties (such as

the number or configuration of items). Conversely, RC ignores puzzle-specific properties and

proposes that the information in the signal codes for the dimensionality of the abstraction.

Although both models aimed to capture different theoretical constructs (effort vs. complexity),

they showed a high correlation (rs = 0.81, p < 0.001). Based on the prior results (**Figure 3d**), we

narrowed our focus to the alpha and beta frequency bands.

The peak commonality coefficients from the fMRI-EEG fusion results in alpha and beta frequency

bands are shown in **Figure 4b**. Most networks exhibit a similar peak onset time at 3.8 s in the

alpha, while beta appeared to emerge 200 ms earlier at 3.6 s. Higher-order dorsal attention (peak

alpha R^2 = 0.35, beta R^2 = 0.33), cingulo-opercular (peak alpha R^2 = 0.36, beta R^2 = 0.32) and

frontoparietal (peak alpha R^2 = 0.34, beta R^2 = 0.34) networks shared the highest peak similarity

between imaging modalities. The top networks showing the highest peak representation were

consistent across both frequency-resolved timeseries. To further analyse the variance explained by

our proposed cognitive models (**Figure 4a**), we selected the dorsal-attention (top) and

frontoparietal (middle) networks, shown in Figure 4c, since they shared the highest cross-modal

commonality. We also selected the default mode network (bottom), a transmodal network known

to be anti-correlated in response to RC demands (Hearne et al., 2015) that showed relatively low

peak fusion similarity (**Figure 4b**). The variance captured between modalities, Figure 4c, alpha

(left) and beta (right) is shown by the shaded area. A shared representation in the beta band for

both dorsal attention (alpha 2.3 – 4.2 s, beta 2.1 – 4.2 s, $p_{FDR} < 0.05$) and frontoparietal networks

(alpha 2.3 – 4.2 s, beta 2.1 – 4.2 s, $p_{FDR} < 0.05$) preceded and maintained longer representation

than the alpha band. The default mode network did not show any period with a significant

commonality coefficient.

The commonality coefficients of the RC and cognitive effort models showed a similar trend to the

overall correlation between the two imaging modalities over time. After 2.5 seconds post stimuli

onsets both models exhibited higher commonality coefficients than would be expected by chance.

Of note, between both models, RC accounts for most of the variance of the shared representational

structure. The cognitive effort model was not present in the default mode network. However, the

RC model was detected in the signal despite the low shared variance between EEG and fMRI.

Figure 4. *Model based EEG-fMRI fusion-analysis*. **A.** Commonality analysis schematic. The

commonality coefficient (CC) reflects the variance shared between the fMRI and EEG signal that

can be attributed to specific task models (RC and Cognitive effort). **B.** Peak correlations between

averaged fMRI and EEG data for each network within the alpha (gold) and beta frequencies (teal).

C. Commonality coefficient timecourses for the RC model (orange line) and cognitive effort model

(green line) in three exemplar brain networks (dorsal-Attention; top, frontoparietal; middle, default

mode; bottom) in both the alpha (right) and beta (left) frequency bands. The shaded area indicates

the proportion of variance shared between EEG and fMRI data over time.

Peak representation of RC and individual task performance

In a final exploratory analysis, we correlated individual participant task accuracy with: i) RC model
coding strength across brain networks and ii) peak oscillatory RC model coding strength in the
alpha and beta frequency. We observed a negative correlation between task accuracy and RC
model coding strength in the frontoparietal (rs = -0.32, p = 0.045) and cingulo-opercular networks
(rs = -0.33, p = 0.038, **Figure 5A**). Focusing on the Frontoparietal network (**Figure 5C**), we
observed an increase in network activation as RC increased: Binary (Mean = -0.027), Ternary
(Mean = 0.547) and Quaternary (Mean = 0.786); F(2, 78) = 117.00, p < 0.001.

In the EEG dataset, task accuracy also had a negative correlation with the temporal peak
representation in the beta oscillatory band (rs = -0.33, p = 0.026), while no relationship was found
in the alpha band (rs = 0.00, p = 0.982, **Figure 5B**). Further exploration of sensor-level activity
during the RC coding window of the beta band (**Figure 2D,** 2.1 s to 4.2 s) showed a decrease in
peak beta power with RC: Binary (Mean = 0.437), Ternary (Mean = 0.380) and Quaternary (Mean
= 0.388); F(2, 80) = 9.68, p < 0.001. While the reported correlations do not survive appropriate
correction for multiple comparisons, the reliable pattern of results across key cognitive control
networks and modalities supports the genuine association between task-accuracy and the strength
of RC brain representations.

Figure 5. *Correlation between participant accuracy (y-axis) and RC model coding strength (x-*
axis) with corresponding brain activation across complexity levels. **A.** fMRI RC model coding
strengths for the frontoparietal (left) and cingulo-opercular (right) networks. **B.** EEG frequency
derived peak RC model coding strengths in the alpha (8 – 12 Hz, left) and beta (13 – 30 Hz, right)
bands. rs represents Spearman's rank correlation coefficient; p-values are uncorrected. **C.**
Frontoparietal activation (β coefficients) across complexity levels. **D.** Periodic peak beta power
calculated across all EEG electrodes in each complexity condition during the 2.1s to 4.2 s time
window.

Discussion

In this multimodal study, we assessed the brain basis of RC representations in the context of a
visuospatial reasoning task. Using representational similarity analysis, we showed that RC is
supported by a widespread network of regions, with core contributions from functional brain
networks associated with external goal-directed control. Results from the analysis of macroscale
temporal dynamics showed that trial-based RC representations are supported by alpha and beta
brain rhythms and emerged gradually, with peak correspondence in the 2.5 – 4.1 second post-
stimuli onset window. The RC model showed stronger links with the shared representational
structure of brain activity compared to a cognitive effort model, with individual RC model coding
strength linked to variations in task performance. This set of results advances our understanding
of the spatiotemporal dynamics underpinning complex reasoning, importantly unveiling that RC
is coded in the representation of problems. Considering the strong association between RC and
intelligence (Hansell et al., 2015), our findings showcase how distributed neural processes
progressively integrate information to orient intelligent behaviour.

Our fMRI findings build on previous knowledge to show that RC is distributed throughout the
brain. Previous lesion and neuroimaging work have demonstrated a key role of frontal (Christoff
et al., 2001; Bunge et al., 2005; Wendelken et al., 2008) and frontoparietal circuits (Vendetti and
Bunge, 2014; Wendelken et al., 2016) in supporting relational processes. However, several studies
have expanded this view by showing that changes in task complexity are supported by local
modulations in brain activity and connectivity in brain network regions beyond the frontal and
parietal cortices (Hearne et al., 2017). For example, Cocchi et al. (Cocchi et al., 2014)
demonstrated that progressively increasing problem complexity also resulted in a proportional
modulation of brain activity and task-based connectivity between core nodes of the cingulo-

opercular network. These observations are in line with network-centric views of cognition and
relational integration (Cole and Schneider, 2007; Morin et al., 2022), positioning frontoparietal
hubs and brain-wide connectivity as central to orchestrating goal-directed cognitive control (Cole
et al., 2013). Our findings extend this work by demonstrating, for the first time, that relational
complexity is mapped in the information representation of frontoparietal, dorsal-attention, and
cingulo-opercular networks. Visual networks also had high model correspondence, likely
reflecting the interaction between the sensory cortex involved in the task and the transmodal
'multiple demand' cortex (Cocchi et al., 2014; Hearne et al., 2017). On the other hand, the default
mode network did not show a strong association with the RC model, suggesting that previously
observed complexity-driven changes in DMN activity and connectivity (Hearne et al., 2015) may
be more related to the engagement of task-positive networks rather than the coding of RC.
Consistent with previous findings we were also able to demonstrate that part of the information
stored in higher-order regions reflected the behavioural effort taken to solve the problems (Chiou
et al., 2024). Despite the high correlation between RC and cognitive effort models, the information
content in the higher-order networks predominantly coded for the dimensionality of the abstraction
as proposed to RC theory, rather than trial-specific puzzle factors associated with cognitive effort.
587
Coherent oscillatory activity is a fundamental element in computational theories of relational
integration (Knowlton et al., 2012; Fries, 2015). Our results suggest that the widespread neural
representations of RC are supported by alpha and beta oscillatory brain rhythms, which emerge
after the first two seconds of stimulus onset. These results complement our fMRI findings by
showing the temporal dynamics supporting the establishment of RC representation in task-relevant
dorsal attention, frontoparietal, and cingulo-opercular networks. RC representation emerged
following the initial computation of the perceived properties of a stimulus (shape, colour; (Cichy
et al., 2014)) and mirrors the timeframe observed to implement task-relevant rules (Hebart et al.,
2018). The involvement of neural activity in the alpha frequency range is consistent with findings
suggesting that frontal and parietal alpha activity support logical reasoning (Brzezicka et al., 2011;
Brzezicka et al., 2017; Heldmann et al., 2024). Accordingly, frontoparietal alpha and beta-rhythms
have been associated with performance on matrix reasoning tasks (Ociepka et al., 2023; Penhale
et al., 2024). Speculatively, within the RC representation alpha-band activity may serve to suppress
irrelevant sensory inputs (Foxe and Snyder, 2011; Gray et al., 2015) or competing relational

602 mappings (Benedek et al., 2014), thereby facilitating the focus on task-relevant information. In

603 contrast, beta-band oscillations are likely to support the sustained activation of task-specific neural

604 activity (Buschman et al., 2012), facilitating the maintenance of relational representations as they

605 are progressively integrated. Other cognitive experiments in particular working memory, attention

606 and rule-switching tasks indicate these high-order cognitive operations decrease alpha and beta

607 power in response to increased demands (Scharinger et al., 2017; Williams et al., 2019; Kaiser et

608 al., 2023). However, this attenuated activity appears to facilitate an increase in frequency-specific

609 synchronisation between brain regions (Sauseng et al., 2005; Palva et al., 2010; Buschman et al.,

610 2012). While our study cannot disentangle the exact contribution of network-specific alpha and

611 beta rhythms to support RC representations, it provides a solid rationale to further investigate these

612 neural correlates.

614 In a final exploratory analysis, we found that individual differences in task performance were

615 inversely related to RC model coding within the beta oscillatory band (EEG dataset) and the

616 frontoparietal and cingulo-opercular networks (fMRI dataset). In other words, better performers

617 produced brain representations that corresponded less to the RC model. The mechanism behind

618 this unintuitive result is unclear, but it would suggest high performers tend to have less clear

619 boundaries between the brain representations of different complexity levels (Binary, Ternary,

620 Quaternary). This result may be related to the idea of neural efficiency (Neubauer and Fink, 2009),

621 suggesting that better performers tend to expend less energy on more difficult tasks. Previous

622 E/MEG studies have also demonstrated a similar trend where reduced beta oscillations are

623 associated with improved spatial working memory performance (Proskovec et al., 2018).

624 Likewise, reduced beta oscillations over the frontal and parietal areas while participants solved

625 reasoning problems were found to be negatively correlated with general intelligence (Ociepka et

626 al., 2023). Overall, these findings are consistent with the proposition that frontoparietal beta

627 rhythms play a key role in establishing stable RC representations necessary to solve the problems

628 ahead.

630 Given the existence of theoretical accounts of relational reasoning (Knowlton et al., 2012), as well

631 as neural network LST solvers (Ito et al., 2024), a key future research direction is to leverage the

632 RSA framework to test specific model-based hypotheses regarding RC. In the version of the LST

we implemented in this study, the puzzles were designed to minimise the loading of working memory demands across complexity levels, reducing multiple processing steps to isolate RC. However, other variations of RC tasks may allow for alternative processing strategies, such as segmentation or chunking, that can overcome trial-specific complexity based on problem attributes (Hartung et al., 2022). This opens up opportunities to explore more nuanced questions of relational integration by examining the trade-offs involved in building complex representations across a diverse range of visuospatial, semantic, and analogical tasks (Halford et al., 1998), and addressing the broader question of whether RC is represented across a domain-general set of problems. A model comparison approach (Schutt et al., 2023), as demonstrated in recent studies (Daws et al., 2020; Chiou et al., 2024), would help to directly contrast different models of reasoning. One insight we gained from this method – when combined with a fusion analysis (Hebart et al., 2018) – was that RC captured the majority of variance shared between EEG and fMRI when contrasted with a cognitive effort model.

In conclusion, our study provides a novel characterisation of the spatial and temporal brain processes underpinning representations of complexity during a relational reasoning task. Our results highlight the role of domain-general functional networks and suggest a key role of alpha and beta oscillatory patterns in the service of human relational reasoning. The current results advance our understanding of the neural mechanisms of reasoning and facilitate the establishment of formal generative models of RC.

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Author contributions

L.J.H. and C.R conceptualised the research goals; L.J.H. supervised the investigation, collected and pre-processed dataset 1 and assisted with the formal data analysis. C.R collected and pre-

processed dataset 2 formally analysed the data and wrote the first draft. All authors reviewed and

edited the manuscript.

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