1 The Neuromusculoskeletal Modeling Pipeline: MATLAB-based Model

2 Personalization and Treatment Optimization Functionality for OpenSim

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5 Abstract

Neuromusculoskeletal injuries including osteoarthritis, stroke, spinal cord injury, and traumatic brain

injury affect roughly 19% of the U.S. adult population. Standardized interventions have produced

suboptimal functional outcomes due to the unique treatment needs of each patient. Strides have been

made to utilize computational models to develop personalized treatments, but researchers and

clinicians have yet to cross the "valley of death" between fundamental research and clinical usefulness.

This article introduces the Neuromusculoskeletal Modeling (NMSM) Pipeline, two MATLAB-based

toolsets that add Model Personalization and Treatment Optimization functionality to OpenSim. The two

toolsets facilitate computational design of individualized treatments for neuromusculoskeletal

impairments through the use of personalized neuromusculoskeletal models and predictive simulation.

The Model Personalization toolset contains four tools for personalizing 1) joint structure models, 2)

muscle-tendon models, 3) neural control models, and 4) foot-ground contact models. The Treatment

Optimization toolset contains three tools for predicting and optimizing a patient's functional outcome

for different treatment options using a patient's personalized neuromusculoskeletal model with direct

collocation optimal control methods. Support for user-defined cost functions and model modification

functions facilitate simulation of a vast number of possible treatments.

An NMSM Pipeline use case is presented for an individual post-stroke with impaired walking

function, where the goal was to predict how the subject's neural control could be changed to improve

walking speed without increasing metabolic cost. First the Model Personalization toolset was used to

develop a personalized neuromusculoskeletal model of the subject starting from a generic OpenSim full-

body model and experimental walking data (video motion capture, ground reaction, and

electromyography) collected from the subject at his self-selected speed. Next the Treatment

Optimization toolset was used with the personalized model to predict how the subject could recruit

existing muscle synergies more effectively to reduce muscle activation disparities between the paretic

and non-paretic legs. The software predicted that the subject could increase his walking speed by 60%

without increasing his metabolic cost per unit time by modifying existing muscle synergy recruitment.

This hypothetical treatment demonstrates how NMSM Pipeline tools could allow researchers working

collaboratively with clinicians to develop personalized neuromusculoskeletal models of individual

patients and to perform predictive simulations for the purpose of designing personalized treatments

that maximize a patient's post-treatment functional outcome.

1. Introduction

Approximately 19% of the U.S. adult population is afflicted by a movement impairment caused by

stroke, osteoarthritis, traumatic brain injury, limb amputation, cerebral palsy, Parkinson's disease, or

spinal cord injury.[1–3] In addition to the physical challenges caused by a movement impairment, these

individuals are more likely to experience increased health care costs, lower work productivity, a higher

risk of developing heart disease or diabetes, a reduction or loss of independence, and a decreased

quality of life.[1,4] At present, treatment of these life-altering impairments typically involves selection of a

standardized treatment based on subjective clinical assessment rather than design of a customized

treatment based on objective evidence-based methods. Consequently, existing treatments for

movement impairments do not address the unique clinical situation and needs of the individual patient

to the extent that they could, and should.

Not surprisingly, the standardized treatment paradigm is often unable to achieve the level of post-

treatment functional recovery that patients desire and expect. The percentage of patients who are

dissatisfied with their functional outcome following a standardized treatment supports this viewpoint.

For those who experience stroke, satisfaction with functional outcome is closely tied to ability to return

to a pre-stroke level of movement function.[5] However, stroke patient satisfaction with mobility

improvements generally declines after hospital discharge,[5] with only 65% of individuals post-stroke

recovering the ability to walk.[6] Even then, they tend to walk at a slow self-selected speed with an

asymmetric gait pattern that is less efficient metabolically than for healthy individuals.[6–8] Furthermore,

20% of stroke survivors remain dependent on others to perform activities of daily living (ADLs).[9] For

those with physician-diagnosed arthritis, roughly 44% have functional limitations that affect their ability

to perform ADLs.[10] For those who receive a total knee replacement (TKR), the best predictor of post-

surgery patient satisfaction is functional outcome.[11] However, 22% of TKR patients are dissatisfied with

their functional outcome one year after surgery,[12] while 16 to 30% are dissatisfied with their ability to

perform specific ADLs.[13] For those who receive a total hip replacement, 7% are dissatisfied with their

functional outcome,[14] with expectations for improved walking and stair climbing ability not being met in

over 30% of patients.[15] For those who receive opening wedge high tibial osteotomy surgery, 22% are

dissatisfied with their outcome, primarily due to unmet expectations for their post-surgery ability to

perform functional activities.[16] For those with cerebral palsy (CP), 33% do not improve walking speed as

a result of multi-level orthopedic surgery,[17] while 21% of parents of children with CP do not feel that

their child's orthopedic surgery was worth the time, effort, pain, and cost.[18] For those with lower limb

amputation, between 12 and 32% cannot perform desired ADLs with their prosthesis, while only 30% to

52% find the same ADLs very easy to perform.[19] Those with upper limb amputation use their prosthesis

primarily for cosmetic rather than functional reasons, with the percentage of individuals who rate their

upper extremity prosthesis as beneficial for performing various ADLs ranging from 5% to only 25%.[20]

These statistics across a myriad of clinical conditions that impair movement highlight the need for a

better treatment design paradigm to help a larger percentage of patients recover their desired amount

of post-treatment function.

One possible way to improve treatment design and thus functional outcomes for individuals with

movement impairments is to employ engineering design optimization methods that utilize physics-

based computational models. Physics-based computational models have an advantage over "black box"

machine learning models since they extrapolate better to situations outside the boundaries of the

training data, which is where optimal solutions often lie. Engineering design optimization methods have

dramatically improved function and reliability of commercial products in numerous industries including

automotive, aerospace, farming, construction, and structural engineering, among others.[21–26] Using

these virtual prototyping methods, engineers can evaluate countless designs – including highly novel

ones – in a time- and cost-efficient manner to determine an optimal design for a given problem, thereby

reducing or eliminating trial-and-error design iterations performed on physical prototypes. Researchers

have already demonstrated the benefits of applying engineering design optimization to two clinical

problems – the design of personalized craniofacial prostheses, and the design of personalized coronary

artery stenting procedures.[27–32]

While a similar computational approach holds promise for designing personalized treatments for

movement impairments, at least three significant challenges must first be overcome for such an

approach to become a reality. First, researchers must be able to personalize the neuromusculoskeletal

computer models used in the computational treatment design process.[33] Published musculoskeletal

modeling studies have typically used scaled generic models rather than models whose relevant

characteristics have been personalized to a subject's movement data.[33] This decision is understandable

given the challenges of collecting the experimental movement (and possibly imaging) data needed for

the model personalization process coupled with the challenges of performing the personalization

process itself for any aspect of a model (e.g., joint functional axes). However, differences between

patients with the same clinical condition are precisely what make the clinical treatment design process

so challenging. Second, researchers must be able to perform the treatment design optimization process

using a patient's personalized neuromusculoskeletal model. Such a process requires performing

repeated predictive simulations of patient function following different implementations of a planned

intervention. To date, the majority of such simulations have been performed using "home brew"

computational software,[34–46] making it difficult for the broader research community to engage in the

process, to repeat studies performed by others, and to transfer knowledge about the process to others.

Third, researchers must have access to computational software that makes the model personalization

and treatment optimization processes easy, repeatable, and transferable. While recent software

advances such as OpenSim Moco[47] have made it possible to perform predictive simulations more easily,

neither OpenSim[48,49] nor Moco[47] provide means to personalize relevant aspects of a patient's

neuromusculoskeletal computer model or to use a personalized model to perform the treatment design

optimization process.

This article introduces the Neuromusculoskeletal Modeling (NMSM) Pipeline, a MATLAB-based

software package that provides researchers and clinicians working together with state-of-the-art

computational tools for designing effective personalized treatments for movement disorders. The

software package is built on the foundation of the OpenSim musculoskeletal modeling software and

adds two toolsets to OpenSim[48,49]. The Model Personalization toolset uses patient movement data and

gradient-based optimization to personalize four subcomponents of a patient's neuromusculoskeletal

computer model: 1) joint structure models, 2) muscle-tendon models, 3) neural control models, and 4)

foot-ground contact models. The Treatment Optimization toolset uses a patient's personalized model

with direct collocation optimal control methods[34,40,47,50–53] to predict how the patient's neural control

and/or anatomy should be changed, or how an external device (e.g., an exoskeleton) or implant should

be designed and/or controlled, to maximize improvement in the patient's post-treatment movement

function. By emphasizing functionality, ease of use, flexibility, and computational speed, the NMSM

Pipeline will hopefully accelerate involvement of the neuromusculoskeletal modeling research

community in the computational design of clinically implementable personalized neurorehabilitation

and surgical interventions.

The remainder of this article is outlined as follows. First, a design overview of the NMSM Pipeline is

presented, including an overview of the philosophy and goals of the software and an introduction to the

two included toolsets. Second, implementation details, design decisions, and important information for

each tool are presented. Third, an example treatment design use case is provided including specifics

about the use of each tool and final results. Fourth, a discussion section is included to provide

information about future work, limitations, and access to the software.

2. Design Overview

2.1 Philosophy and Goals

The goal of the NMSM Pipeline software is to help neuromusculoskeletal modeling researchers

engage in clinical research - and cross the valley of death,[54] thereby moving neuromusculoskeletal

modeling a significant step closer to becoming a clinically useful tool. To achieve this goal, the NMSM

Pipeline uses a personalized medicine approach, where physics- and physiology-based personalized

neuromusculoskeletal computer models constructed from patient movement data are used to design

personalized treatments for movement impairments.[55] Such impairments arise from clinical conditions

like osteoarthritis, stroke, cerebral palsy, spinal cord injury, Parkinson's disease, limb amputation, and

even cancer. Because the open-source OpenSim[48,49] and commercial Anybody[56] software commonly

used for musculoskeletal modeling research lack the ability to personalize neuromusculoskeletal

computer models to patient movement data, these software tools cannot currently be used to optimize

treatments for individual patients. To overcome this critical limitation, the open-source NMSM Pipeline

software uses MATLAB (The MathWorks, Natick MA) to build on the OpenSim foundation and provides

two new toolsets - a Model Personalization toolset that facilitates the creation of personalized

neuromusculoskeletal computer models, and a Treatment Optimization toolset that uses the

personalized models to design personalized treatments that maximize a patient's post-treatment

movement function.

To develop these two new MATLAB-based toolsets, we defined a high-level software design

philosophy. First, the NMSM Pipeline was designed to be both accessible for basic users and extensible

for advanced users so that neuromusculoskeletal modeling researchers of all levels can benefit from it.

Second, modeling and simulation methods were based on laws of physics and principles of physiology

and neuroscience rather than on machine learning, since no training data exist for post-treatment

movement conditions, and machine learning methods do not, in general, extrapolate well outside the

boundaries of the training data. Third, existing OpenSim functionality and model entities were utilized to

the fullest extent possible to avoid duplication. Fourth, NMSM Pipeline functionality was designed to

have the "look and feel" of OpenSim so that those with experience using OpenSim can quickly become

proficient using the Pipeline. Fifth, the NMSM Pipeline was designed to work with any OpenSim model,

providing complete flexibility in the musculoskeletal anatomy and movement situations that can be

modeled and simulated.

To achieve the goal of accessibility for basic users and extensibility for advanced users, we designed

NMSM Pipeline tools to work using XML settings files, similar to OpenSim. This approach allows users to

run each NMSM Pipeline tool with only a single line of code. For basic users, we developed two OpenSim

GUI plugins - one for the Model Personalization toolset with its four tools, and one for the Treatment

Optimization toolset with its three tools, where each toolset appears under the OpenSim "Tools" menu.

The GUI plugin window for each tool allows users to set up tool runs by configuring the most common

settings for each tool (Figure 1), with default values being used automatically for advanced tool settings.

Tool settings selected in the GUI plugin, along with default advanced tool settings, can be exported by

Figure 1: Screenshot of the JMP GUI tool sub-window for adding a JMP task. The GUI tools allow for modifying common settings and creating XML settings files. Advanced settings can be modified directly in the XML file after creation.

the user to an XML settings file that can be read back into the GUI and modified as desired, just as with

OpenSim tools. For advanced users, advanced tool settings are exposed in each tool's XML settings file,

again similar to OpenSim. Advanced users can create an initial XML settings file using the GUI plugin, or

they can start from a pre-existing XML settings file and edit the values of basic and advanced tool

settings using any text editor. For both basic and advanced users, each tool is run from the MATLAB

command line using a tool-specific function that takes a tool-specific XML settings file as an input. Thus,

no "Run" button is provided in any of the GUI plugin tool windows. Tool outputs can be plotted in

MATLAB using included utility or custom functions.

Software engineering principles were used for NMSM Pipeline development to facilitate

extensibility. Namely, atomic functions - functions that complete only a single operation - were used

extensively. All code was written using clear, English-language variable and function names and

organized into logical groupings. GitHub's source control, automated testing framework, and continuous

integration tools were used to maintain this extensive project and its documentation throughout the

development process. These choices make NMSM Pipeline code easy to understand and easy to modify.

Because NMSM Pipeline tools are based on laws of physics and principles of physiology and

neuroscience, we selected computational methods that best facilitate the intended personalized

medicine approach. Gradient-based optimization was used for all tools within the NMSM Pipeline

primarily for computational speed reasons but also for the ability of gradient-based optimizers to find

better solutions than the initial guess, even if the final solution is not the global optimum. For the Model

Personalization toolset, built-in MATLAB optimization algorithms (primarily lsqnonlin and fmincon) were

used exclusively, while for the Treatment Optimization toolset, the open-source IPOPT optimizer[57] was

used within the commercial GPOPS-II direct collocation optimal control software.[51] This approach

eliminates GPOPS-II and direct collocation optimal control from the Model Personalization process,

making model personalization a more reliable and less complex process than it would be if direct

collocation optimal control were required.[40,58,59] The Model Personalization toolset automatically uses

MATLAB's built-in parallel processing capabilities for calculating finite difference derivatives needed by

MATLAB optimization algorithms, while the Treatment Optimization toolset automatically uses parallel

processing only for repeated OpenSim analyses performed through MATLAB via C++ Mex files.

Through the utilization of OpenSim's native models and entities, we included a number of

convenient facilities in the NMSM Pipeline. OpenSim native file types were used for all data interactions

including OpenSim model files (.osim), marker data files (.trc), kinematic motion and ground reaction

data (.mot), time series data (.sto), and XML settings files (.xml). Only one new file type was developed--

the NMSM Pipeline model file type (.osimx) to store personalized model properties that are not included

in native OpenSim models. Similarly, easy-to-use OpenSim GUI tools such as the Scale tool, Inverse

Kinematics (IK) tool, Inverse Dynamics (ID) tool, and Muscle Analysis tool were leveraged as part of the

typical pipeline run-through using experimental movement data. For some NMSM Pipeline tools, groups

of muscles must be identified, and the muscle groups functionality available in OpenSim models was

used for this purpose to avoid the need to store this group information elsewhere.

2.2 NMSM Pipeline Toolsets

The NMSM Pipeline is composed of two toolsets-- a Model Personalization toolset and a Treatment

Optimization toolset. The Model Personalization toolset personalizes four aspects of a scaled generic

OpenSim model using experimental movement data and gradient-based optimization (Figure 2). Those

Figure 2: Overview of the Model Personalization toolset. This toolset creates neuromusculoskeletal models with personalized joint, muscle-tendon, neural control, and ground contact parameters through the use of gradient-based optimization.

four aspects are 1) joint models, 2) muscle-tendon models, 3) neural control models, and 4) ground

contact models. The personalization process is important since personalized rather than generic models

are needed to support model-based treatment design for clinical conditions where patients exhibit

significant heterogeneity (e.g., stroke).[60,61] Furthermore, without a personalization process,

neuromusculoskeletal models do not reliably predict internal muscle and joint contact forces, body

motion, or metabolic cost.[40,62–69] Each stage in the NMSM Pipeline Model Personalization process has

been shown to play an important role in predicting these quantities reliably.[40,62–64,69,70]

The Treatment Optimization toolset uses the subject's personalized neuromusculoskeletal model to

predict their post-treatment movement function using direct collocation optimal control (Figure 3). Over

Figure 3: Overview of the Treatment Optimization toolset. This toolset generates a tracking simulation and two subsequent predictive simulations through the use of direct collocation optimal control.

the past 10 years, musculoskeletal modeling researchers have converged on direct collocation optimal

control as the best method for generating predictive simulations of human movement.[34–

36,36,39,40,47,50,58,71–79] The Treatment Optimization Toolset uses the MATLAB-based GPOPS-II direct

collocation optimal control software[51] to perform predictive simulations of movement for novel

conditions where no experimental data exist. Similar to MATLAB, GPOPS-II is inexpensive for academic

use. The optimal control solver can adjust neural and/or torque control signals along with neural

control, anatomical, internal implant, and/or external device parameters in a patient's personalized

neuromusculoskeletal model to achieve a specified treatment goal (e.g., achieve a desired reduction in

metabolic cost). For any patient, this approach can potentially provide the best treatment prescription,

the best dosage, and an estimate of the patient's capacity for improvement.

Optimization cost function terms for both toolsets were designed to minimize squared errors/values

and utilize a common formulation with physically meaningful cost function parameters. Specifically, cost

function terms utilize a maximum allowable error and, in some cases, a user-provided error center

(Figure 4). For example, if a cost function term seeks to minimize errors between model and

$$\text{Cost} = \left(\frac{\text{Value} - \text{Error Center}}{\text{Maximum Allowable Error}} \right)^2$$

Figure 4: The generic cost function term formulation used throughout the Model Personalization and Treatment Optimization toolsets. The formulation utilizes a maximum allowable error and error center to make the calculated cost physically meaningful. If the difference between the current value and the error center is greater than the maximum allowable error, then the quantity in parentheses (i.e., normalized error) will be greater than 1, and squaring this quantity will amplify the cost (e.g., 1.1^2 = 1.21). In contrast, if the difference between the current value and the error center is less than the maximum allowable errors, then the quantity in parentheses will be less than 1, and squaring this quantity will attenuate the cost (e.g., 0.9^2 = 0.81).

experimental joint moments, and matching to within 2 Nm is acceptable, then the user would set their

cost term error center to 0 and the associated maximum allowable error to 2. Each cost function term

has equal weight with all other cost function terms included in the optimal control problem formulation,

where continuous cost function terms involving time series data (e.g., joint angles, joint moments) are

normalized by final time so that they do not contribute to the total cost more heavily than do terminal

cost function terms involving only a single quantity (e.g., metabolic cost). This method for formulating all

cost function terms allows for contextualized decision-making when determining weights for different

cost function terms.

Neural control models for both toolsets are described using muscle synergies. Muscle synergies

provide a physiologically-relevant low dimensional representation of a large number muscle activations

and can be personalized to represent a specific patient's neural control strategy.[80–87] Each muscle

synergy is composed of a time-varying synergy activation and an associated time-invariant synergy

vector. Each synergy vector contains a weight for each muscle in the model that defines how the

associated synergy activation contributes to the total activation of the muscle. Muscle synergies are

commonly calculated using non-negative matrix factorization,[80,81] and typically between three and six

muscle synergies are required to account for over 95% of the signal variability for common tasks such as

walking, running, and reaching.[88]

3. Implementation Details

3.1 Model Personalization

The Model Personalization toolset calibrates parameter values in an OpenSim neuromusculoskeletal

model so that the model closely reproduces a wide range of experimental movement data. The toolset

consists of four tools and was designed so that the tools can be used largely independently from one

another, though a preferred tool workflow exists. Personalization is likely to be necessary if the

musculoskeletal model is to be used for clinical treatment design purposes.[33] It also improves models for

use in predictive simulations by maximizing the self-consistency of collected experimental data and

easing the task of finding a realistic, dynamically consistent motion.

The four tools of the Model Personalization toolset personalize different anatomical, physiological,

and neurological aspects of a patient's OpenSim model. Joint Model Personalization (JMP) calibrates the

properties of OpenSim constraint-based joint models, Muscle-tendon Model Personalization (MTP)

calibrates the properties of Hill-type muscle-tendon models, Neural Control Model Personalization (NCP)

calibrates the properties of muscle synergy control models, and Ground Contact Model Personalization

(GCP) calibrates the properties of elastic foundation foot-ground contact models. OpenSim models

personalized using the Model Personalization toolset can be used in both the NMSM Pipeline's

Treatment Optimization Toolset and, in the near future, OpenSim Moco. For use with OpenSim Moco,

an NMSM Pipeline .osimx model file must be converted to an OpenSim .osim model file using an

provided MATLAB model conversion utility program.

The Model Personalization toolset requires input data generated using standard OpenSim tools.

First, a generic musculoskeletal model is scaled using the OpenSim Scale Model tool. To facilitate

modeling and simulation of full-body walking motions, we recommend starting with the RCNL2023

OpenSim model (distributed with the NMSM Pipeline software), which is a modified version of the

Rajagopal full-body OpenSim model[89] where the ankle joint kinematic model has been changed to match

van den Bogert et al. (1994)[90] and the knee joint kinematic model changed to eliminate all rotational

offsets while producing the same motion. A scaled generic model is one of the required inputs for the

JMP tool. After personalized joint models are calibrated using the JMP tool, the user must calculate IK

motions and ID loads using the OpenSim Inverse Kinematics and Inverse Dynamics tools, respectively.

The user must then run the Muscle Analysis tool to calculate muscle-tendon lengths and velocities as

well as muscle moment arms if the NMSM Pipeline MTP and NCP tools are to be used. For the JMP tool,

marker files can be manually concatenated to personalize joint parameters using multiple motion trials

(e.g., marker data from isolated ankle, knee, and hip motion trials can be concatenated with marker

data from a walking motion trial to calibrate the functional axes and joint centers of all lower body joints

simultaneously). The MTP and NCP tools accept data from one or more motion trials, and the GCP tool

accepts data from only a single motion trial, ideally the same trial to be used for Treatment

Optimization. If multiple motion trials are used with either the MTP or NCP tools, IK motions, ID loads,

muscle-tendon lengths and velocities, and muscle moment arms need to be calculated for each motion

trial.

3.1.1 Joint Model Personalization

The Joint Model Personalization tool optimizes joint parameters, body scaling, and marker

placement to minimize IK marker distance errors.[90–96]. Reducing inverse kinematics marker distance

errors reduces downstream errors in calculated inverse dynamic joint moments[63], muscle-tendon

lengths and velocities, muscle moment arms, and ultimately muscle activations and forces. These

quantities are used by subsequent Model Personalization tools.

JMP tool inputs are a scaled generic OpenSim model and marker data from one or more motion

trials, where the tool settings file allows the user to specify one or more tasks (Figure 5). The available

Figure 5: Flowchart showing the inputs to and outputs from the JMP tool. The diagram key also applies to Figs. 6 through 9.

design variables include joint locations and orientations in parent and child bodies, body scale factors

applied uniformly, and marker location offsets for each direction independently. The only cost function

term is the sum of the squared marker distance errors normalized by the motion trial duration and

number of markers. No constraints are included in this optimization problem. The output of JMP is a

new OpenSim model with optimized joint parameters, body scale factors, and/or marker placements.

Several important considerations should be kept in mind when using the JMP tool. A JMP run can

be split into multiple tasks, each with its own set of design variables and an associated marker file.

Careful JMP setup is required to avoid obtaining non-anatomical results. Such a result could be found by

personalizing a joint parameter for a coordinate that does not move through sufficient range of motion

(> ~25 degrees) during the motion trial[97]. This issue can be rectified by personalizing the associated joint

parameters with separate tasks using isolated joint motion trials, or by concatenating data from an

isolated joint trial with data from the desired functional trial (e.g., walking). Another cause of non-

anatomic results is selection of joint parameters that produce relative bone motions that are

inconsistent with joint function. For example, the parent frame of the hip joint is often defined to be at

the center of the acetabulum, while the child frame is often defined to be at the center of the femoral

head. Allowing joint parameters to modify the location of the hip joint in either the parent or the child

frame could move the center of the femoral head out of the center of the acetabulum, breaking that

anatomical relationship. In addition, muscle paths and/or relative body sizes may also become non-

anatomical due to inclusion of inappropriate design variables. JMP tool results should be visualized in

the OpenSim GUI and problem formulations modified to achieve an anatomically realistic post-JMP

model.

3.1.2 Muscle-tendon Model Personalization

The Muscle-tendon Model Personalization tool finds an optimal set of subject-specific muscle-

tendon properties and muscle activations from EMG, joint kinematic, and joint moment data by

balancing optimization cost function terms related to muscle properties, similarity of properties among

grouped muscles, and matching of EMG-driven and experimental inverse dynamics joint moments.[66,67,98]

Muscle activation and force predictions are sensitive to optimal muscle fiber length and tendon slack

length.[62,99–101] Therefore, reliable personalization of these parameters is essential for generating reliable

predictions of muscle activations and forces during predictive simulations of movement.

The inputs to the MTP tool are a post-JMP OpenSim model as well as IK motion, ID load, muscle-

tendon length and velocity, and muscle moment arm data from one or more motion trials of interest

(Figure 6). The design variables that can be optimized include activation dynamics and muscle-tendon

length parameters for each muscle.[40,66,102] Cost function terms used by the MTP tool minimize muscle-

Figure 6: Flowchart showing the inputs to and outputs from the MTP tool.

tendon model parameter deviations from initial values, ID joint moment tracking errors, passive muscle

forces, inconsistencies among grouped normalized muscle fiber lengths, inconsistencies among grouped

muscle excitation scale factors, and inconsistencies among grouped electromechanical delays. No

constraints are applied in this optimization problem. The outputs of the MTP tool are a .osimx model file

containing optimized muscle-tendon properties and estimated muscle activations, both for use by other

tools in the NMSM Pipeline.

Several important considerations should be kept in mind when using the MTP tool. Muscle Tendon

Length Initialization is included as an option within the MTP tool and is typically used to find reasonable

reference values for cost function deviation terms involving muscle-tendon length parameters. Muscle

Tendon Length Initialization also estimates the maximum isometric force of each muscle based on

published regression relationships.[103] Since scaling maximum isometric force and muscle excitation at

the same time produces a non-unique muscle force solution, and since muscle excitations are scaled

using EMG scale factor design variables, maximum isometric force is held constant during an MTP tool

run.[62] Synergy Extrapolation (SynX)[104,105] is also included in the MTP tool to estimate the activations of

muscles without experimental EMG data. SynX uses muscle synergy concepts to estimate missing

activations and is more accurate than traditionally used static optimization at predicting missing EMG

signals[106]. A typical use case for SynX is estimating the activations of deep muscles from which EMG data

cannot be easily collected. SynX can use either principal component analysis (PCA) or non-negative

matrix factorization (NMF) to calculate the muscle synergies needed to predict muscle activations

associated with missing EMG data. The MTP tool uses a Hill-type muscle-tendon model with a rigid

tendon and assumes that muscles function primarily on the ascending region of their normalized active

force-length curves.[107] Users can modify cost terms to specify the region of the normalized force-length

curve over which muscles are assumed to operate. Some MTP cost function terms promote similarity in

muscle properties within a group under the assumption that similar muscles, such as the four vastus

muscles, should have similar properties. These muscle groups must be defined within the OpenSim

model.

3.1.3 Neural Control Model Personalization

The Neural Control Model Personalization tool finds muscle synergies that are as consistent as

possible with ID joint moments and, when available, MTP-estimated muscle activations. The NCP tool

fits muscle synergies at the level of muscle activations (i.e., after electromechanical delay and activation

dynamics) for regions of the body where either all muscle activations are available from the MTP tool

(e.g., the right lower extremity) or no muscle activations are available.[108,109] The tool can also be used to

find muscle synergies in multiple regions of the body simultaneously - some with and some without

previously calculated muscle activations. During the NCP optimization process, grouped muscle

properties are maintained and activation-related cost function terms are minimized. Muscle synergies

are typically calculated from muscle activations alone using non-negative matrix factorization, and thus

the muscle activations reconstructed from the resulting synergies will not closely reproduce ID joint

moments when input into a subject's musculoskeletal model. NCP rectifies this issue by optimizing

synergy activations and synergy vectors to be consistent with both ID joint moments and available

muscle activations simultaneously.

The inputs to the NCP tool are a post-JMP OpenSim model as well as data for IK motions, ID loads,

muscle-tendon lengths and velocities, muscle moment arms, and, optionally, MTP-calculated muscle

activations from one or more motion trials of interest (Figure 7). The OpenSim model must contain

Figure 7: Flowchart showing the inputs to and outputs from the NCP tool.

muscle groups that define lists of muscles for which synergy sets are to be fitted (e.g., all right leg

muscles). The design variables for the NCP tool are a set of time-varying synergy activations and an

associated set of time-invariant synergy vectors. The cost function terms for the NCP tool minimize ID

joint moment matching error, MTP muscle activation matching errors, muscle activations,

inconsistencies among grouped normalized muscle fiber lengths, and inconsistencies among grouped

muscle activations. The NCP tool includes a constraint that the sum of the muscle weights in each

synergy vector must equal a constant times the number of muscles described by that synergy. Upon

output, the synergy vectors and synergy activations are normalized such that the largest weight in each

synergy vector is one. The NCP tool produces a set of synergy groups inside a new or pre-existing NMSM

Pipeline model file (.osimx) as well as data files (.sto) containing synergy activations and their associated

synergy vectors.

Several important considerations should be kept in mind when using the NCP tool. Synergy-driven

Tracking Optimization (TO), part of the Treatment Optimization toolset, requires that NCP tool results be

used as the initial guess. NCP results that distribute errors equally between MTP muscle activation

matching and ID joint moment matching will facilitate the process of finding good synergy-driven TO

results. In addition, to facilitate obtaining good NCP results, users should perform their own synergy

analysis on the muscle activations produced by MTP to determine the optimal number of synergies to

use. The number of synergies should be selected to achieve the desired variability accounted for (VAF),

which is often set at 90 or 95%.[40,84,110,111] The NCP tool can be run without having MTP tool results as

inputs through the use of the activation minimization cost function term. Since running the NCP tool

without MTP tool results produces a non-unique solution, the maximum allowable error of the

activation minimization cost function term can be set to achieve a unique solution that contains

activations of expected magnitude. Shared synergy vectors between synergy groups can also be

enforced by the NCP tool. This feature allows for two muscle synergy groups, such as those for right and

left leg muscles, to have nearly identical synergy vectors.

3.1.4 Ground Contact Model Personalization

The Ground Contact Model Personalization tool finds physical properties for elastic foundation foot-

ground contact models that closely reproduce experimental ground reaction forces and moments while

allowing slight changes in foot kinematics. The elastic foundation is composed of a uniform grid of linear

springs with nonlinear damping and friction placed across the bottom of the foot. The tool can

personalize ground contact models for each foot separately, where physical properties will differ

between the two feet, or both feet together, where physical properties will be the same for the two

feet. Currently, the tool works with only a two-segment foot model composed of a hindfoot segment

(including calcaneus, cuboid, navicular, cuneiform, and metatarsal bones) and a toes segment (including

phalange bones). While generic foot-ground contact models can reproduce experimental ground

contact forces accurately, they reproduce experimental ground reaction moments less accurately,

introducing errors into the lower body joint moments generated by predictive simulations of walking.[70]

Personalized foot-ground contact models can overcome this issue by reproducing experimental ground

reaction moments as well.

The inputs to the GCP tool are a post-JMP lower-body or full-body OpenSim model along with IK

motion and associated ground reaction data for a walking trial, where the IK and ground reaction data

must possess the same time increments (Figure 8). The ground reaction data must contain three forces,

Figure 8: Flowchart showing the inputs to and outputs from the GCP tool.

three moments, and a point about which the moments are calculated, which is typically either a time-

invariant point fixed in the laboratory or a time-varying center of pressure. The tool automatically strips

off both feet from the lower-body or full-body OpenSim model and creates a 6 DOF custom joint

connecting each specified hindfoot body to ground. The design variables for the GCP tool are stiffness

coefficients unique to each spring with a nonlinear viscous damping coefficient, a dynamic friction

coefficient, a viscous friction coefficient, and a spring resting length common to all springs. Additional

design variables are B-spline nodal points defining small deviations from experimental foot kinematics

with respect to ground. The cost function terms for the GCP tool include minimization of foot marker

position errors, foot marker velocity errors, hindfoot and toes segment rotational coordinate errors,

hindfoot segment translational coordinate errors, vertical ground reaction force errors, horizontal

ground reaction force errors, ground reaction moment errors, and spring coefficient deviations from

neighboring spring coefficient values. No constraints are present in this optimization problem. The

output of the GCP tool is a new NMSM Pipeline model file (.osimx) containing foot-ground contact

model parameter values.

Several important considerations should be kept in mind when using the GCP tool. The tool can

reproduce all six components of ground reactions with good fidelity. To facilitate reproducing ground

reaction moments, we use the time-varying projection of a midfoot superior marker onto the ground as

the point about which ground reaction moments are calculated. This automatic recalculation of the

ground reaction moments helps keep the moments well-scaled during a GCP run, since the moment arm

of the ground reaction force vector never becomes excessively large. The center of pressure is not used

for joint moment matching since it becomes inaccurate at the transitions into and out of contact due to

division by small vertical ground reaction force values. At this time, the GCP tool requires the use of a

two-segment foot model with the distal toes segment connected to the hindfoot segment via an oblique

pin joint. Before personalization, the GCP tool automatically extracts two-segment OpenSim foot models

from the post-JMP lower-body or full-body OpenSim model and automatically calculates hindfoot

kinematics with respect to ground that are consistent with the input lower-body or full-body kinematics.

Since the foot-ground contact model is sensitive to foot kinematic changes below the measurement

accuracy of a markered motion capture system, the GCP tool allows for small changes to the foot

motion trajectory to facilitate ground reaction matching. Each foot model possesses seven coordinates:

six ground-to-hindfoot coordinates via a 6DOF custom joint and one toes coordinate via a pin joint.

Coordinate deviations are parameterized with B-spline nodes to reduce the number of design variables.

The GCP tool automatically estimates the number of B-spline nodes needed based on a specified

lowpass filter cutoff frequency. Another important feature of the GCP tool is its ability to use a different

time windows for calibrating each foot. This feature facilitates the use of the GCP tool with ground

reaction data obtained from labs possessing only two in-ground force plates. The GCP tool also allows

for symmetric physical properties between contact surfaces on the two feet, and users can modify the

number of springs along each dimension of the grid.

3.2 Treatment Optimization

The Treatment Optimization toolset generates predictive simulations of a patient's post-treatment

movement function by optimizing specified treatment design parameters. The toolset consists of three

tools designed using a "theme and variation" approach, where the tools are intended to be used in a

specific order, with each tool serving a distinct purpose. Each tool uses the GPOPS-II direct collocation

optimal control software for MATLAB[51] and maintains a consistent structure for data inputs, problem

design, cost function terms, constraint terms, and outputs, with variations (Figure 9). The Tracking

Figure 9: Flowchart showing the inputs to and outputs from the tools included in the Treatment Optimization toolset. Since these tools follow a theme and variation approach, various data combinations can be included or excluded based on the goals of the user.

Optimization tool generates "starting point" predictive simulations of patient movement that are

dynamically consistent and closely reproduce all relevant experimental movement data available from

the patient (e.g., joint motion, joint moment, ground reaction, and EMG data). The Verification

Optimization tool starts from the Tracking Optimization solution and verifies that the controls found

produce the correct motion without tracking the motion directly, which ensures that the subsequent

treatment design problem is well formulated before simulated treatments are explored. Finally, the

Design Optimization tool starts from the Verification Optimization solution, applies and (if desired)

optimizes simulated treatments, and predicts the patient's resulting post-treatment movement along

with associated controls and loads. All three tools work with torque controlled, muscle synergy

controlled, and combined torque and muscle synergy controlled problem formulations.

Several important considerations should be kept in mind when working with the Treatment

Optimization toolset. Direct collocation optimal control problems are solved by modifying states and

controls simultaneously to minimize an objective function and fulfill constraints. For Treatment

Optimization, the states consist of joint positions and velocities for selected OpenSim model coordinates

and the controls consist of corresponding joint accelerations (due to the use of an implicit dynamics

formulation[50]), torque controls, synergy controls, or both. All Treatment Optimization tools accept both

a "tracked quantities" and an "initial guess" directory. The tracked quantities directory contains

reference data (e.g., experimental joint positions, joint moments, muscle activation, and ground

reactions) to be tracked by specified cost function terms while the initial guess directory contains data

specifying the initial guess for the problem's states and controls. Treatment Optimization XML settings

files allow for joint position, velocity, and acceleration range scale factors as well as muscle synergy and

torque controller range scale factors. These range scale factors describe the search space of the optimal

control problem by confining the states and controls to be within a certain range relative to their initial

Figure 10: Illustration showing how range scale factors are used to set bounds on the states and controls within GPOPS-II. The range scale factor value is used to set the maximum and minimum searchable spaces for the states and controls as offsets beyond the initial range. In this figure, a range scale factor of 0.5 was used.

range (see Figure 10). After a completed run, all Treatment Optimization tools output the same files to a

user-specified results directory. Specifically, the solution's states and controls, along with IK motions, ID

loads, and ground reactions calculated from the solution's states and controls, are output to the

specified directory. Saved states and controls can then be passed to the next Treatment Optimization

tool as an initial guess to pick up where the previous tool left off.

Because Treatment Optimization tools use implicit dynamics,[40,50] several constraint terms must be

included for successful use of the toolset. One constraint is that the joint acceleration controls must be

the first time derivatives of the joint velocity states, and the joint velocity states must be the first time

derivatives of the joint position states. These constraints are handled internally by GPOPS-II. Another

constraint is that the net joint loads produced by the torque and synergy controls must be consistent

with the model's inverse dynamic loads. This constraint must be handled by the user by including kinetic

consistency constraint terms for all controlled coordinates included in the problem formulation. In

addition, if users want their Treatment Optimization solutions to be dynamically consistent, then the

root segment residual load constraint must be included to ensure that the residual loads acting on the

model's root segment (i.e., the segment connecting the model to ground) are close to zero. In addition,

if the motion of interest is expected to be periodic, such as for walking, running, cycling, or stair-

climbing, joint position and velocity and ground reaction force and moment periodicity constraints can

be used to ensure that a near-periodic motion is found.

3.2.1 Tracking Optimization

The Tracking Optimization tool uses a personalized model to produce a dynamically consistent

movement simulation that closely reproduces all available experimental motion data, including joint

motions, joint moments, ground reaction forces and moments, and muscle activations. To achieve a

dynamically consistent motion, the tool spreads out matching errors between the different

experimental quantities based on user-specified maximum allowable errors. The tool accepts a post-JMP

OpenSim model (.osim file) and personalized NMSM Pipeline model (.osimx file) along with

experimental IK motions, ID loads, ground reactions, muscle-tendon lengths and velocities, muscle

moment arms, and, if using synergy controls, NCP results for the trial of interest. The following cost

function terms are commonly included to achieve a successful Tracking Optimization run: generalized

coordinate tracking, generalized speed tracking, inverse dynamic moment tracking, muscle activation

tracking, external force tracking, and external moment tracking. Common constraint terms include

kinetic consistency, state position periodicity, state velocity periodicity, and root segment residual load

bounding.

Several important considerations should be kept in mind when using the Tracking Optimization tool.

Finding a good result with the Tracking Optimization tool is the biggest challenge in the NMSM Pipeline.

The goal is to trade off errors between tracked experimental data sources by modifying the maximum

allowable error in each cost function term based on the importance of and confidence in the respective

experimental data. Higher quality Model Personalization results and highly consistent tracked

experimental quantities (e.g., tracked muscle activations should closely reproduce tracked ID moments)

make finding a good Tracking Optimization solution easier.

3.2.2 Verification Optimization

The Verification Optimization tool is used to perform a "dry run" Design Optimization without

including any "design elements", the goal being to ensure a good initial guess and to verify the

appropriateness of the optimal control problem formulation. The tool accepts the same inputs as the TO

tool, but in general, the results directory of a TO run is used for both the initial guess and tracked

quantities. The cost function terms for the VO tool include controller tracking and, for uncontrolled

joints, generalized coordinate tracking. Similar to the TO tool, the VO tool includes constraint terms for

kinetic consistency, state position periodicity, state velocity periodicity, and root segment residual load

bounding. If a VO problem is well formulated, it should converge quickly since the initial guess is already

at the optimal solution.

Several important considerations should be kept in mind when using the Verification Optimization

tool. Users must decide whether each coordinate should be controlled or tracked. If controlled, the

coordinate should be assigned the same controller (synergy, torque, or both) as in the TO tool, and the

controls should be tracked by the VO tool. Conversely, if the coordinate does not have a controller or

has a non-essential controller, then the coordinate should be tracked by the VO tool. An example of a

non-essential controller is a torque controller on an upper body joint for a full body gait model with only

lower body muscles. The results of a VO run should closely match the outputs of the TO run used to

define the initial guess and tracked quantities. If the results do not match closely, then a problem

formulation issue is likely present, and users should review their TO and VO settings. Examples of

potential problem formulation issues are having a generalized coordinate that is neither controlled nor

tracked, having a generalized coordinate that is both controlled and tracked, or having a generalized

coordinate that is tracked with a different maximum allowable error than was used by TO. Each of these

situations can produce a VO solution that differs from the TO initial guess. After an adequate VO

solution is found, users can move on to the DO tool by adding a "treatment" to their VO problem

formulation.

3.2.3 Design Optimization

The Design Optimization tool predicts or optimizes how a planned treatment will affect a patient's

post-treatment movement function. The tool accepts the same inputs as the other Treatment

Optimization tools, but typically VO results are used as the initial guess. Similar to VO, DO allows for

controller tracking and generalized coordinate tracking alongside other DO-specific cost function terms.

Similar to TO and VO, DO can use kinetic consistency, state position periodicity, state velocity

periodicity, and root segment residual load constraint terms as well as other constraints to facilitate the

design of a personalized intervention.

Several important considerations should be kept in mind when using the Design Optimization tool.

Unlike the other Treatment Optimization tools, the DO tool allows for both fixed and free final time

problem formulations. For free final time problems, the time vector can be constrained to a user defined

range and tracked control quantities are stretched or compressed in time to match the current time

vector. A number of built-in cost function terms have been included in the DO tool. These terms include

minimizing braking and propulsive impulse errors from target values, metabolic cost per unit of time or

distance[112] errors from a relative target value, whole-body angular momentum error from a target

value, and joint mechanical energy generation or absorption errors from a target values. Two key

features of the DO tool are support for model modification functions and user-defined cost function

terms. By employing model modification functions alongside GPOPS-II's static parameters feature, users

can change the OpenSim musculoskeletal model, modify the neural control model, or adjust parameter

values in an assistive device. Possible model modifications include changing bone geometry (e.g.,

osteotomy parameters), changing muscle-tendon properties (e.g., strengthening muscles or adjusting

optimal muscle fiber lengths), changing neural control properties (e.g., altering synergy vector weights

or synergy activation profiles), modifying ground contact model parameters, optimizing muscle

attachment locations or muscle wrapping surface parameters, redefining joint parameters, and

modifying external device design and/or control parameters. User-defined cost function terms allow

users to write a custom MATLAB function, with a specific function signature, that is added as an

additional cost function term given the iteration's states, controls, and static parameters.

4. Example Application

4.1 Treatment Design Rationale

To demonstrate the capabilities of the NMSM Pipeline, we employed it to investigate a hypothetical treatment to improve walking speed and function for an individual post-stroke. Published studies have hypothesized that time-varying synergy activations originate in the brain while time-invariant synergy vectors reside in the spinal cord.[113,114] If this hypothesis is true, then one might expect a stroke to affect a patient's synergy activations but not synergy vectors.[114] This expectation in turn suggests that an individual post-stroke may have similar synergy vectors between the two legs but lack the ability to recruit one or more of them effectively on the paretic side. Furthermore, published studies have reported that a stroke results in altered neural coordination even on the non-paretic side.[115–117] Taken together, these observations lead to the hypothesis that a stroke may impair recruitment of one or more synergy activations in the paretic leg, resulting in altered recruitment of one or more synergy activations in the non-paretic leg, and that restoration of these impaired and altered synergy activations could result in improved self-selected walking speed and metabolic cost.[117–119]

To investigate this hypothesis, we used the NMSM Pipeline to design a hypothetical treatment that would modify paretic and non-paretic leg synergy activations for an individual post-stroke with the goal of increasing his self-selected walking speed without increasing his metabolic cost. Previously published experimental walking data collected from an individual post-stroke with a self-selected walking speed of 0.5 m/s were used for the investigation.[40] Research has shown that both healthy individuals and individuals post-stroke tend to choose a self-selected walking speed to achieve a desired metabolic cost per unit time.[120] Furthermore, to achieve successful community ambulation (as defined by the walking speed required to cross a typical street before the light changes[121]), individuals should be able to walk at a self-selected speed of 0.8 m/s.[121,122] Thus, the specific goal of the hypothetical treatment was to

increase the subject's self-selected walking speed to 0.8 m/s while maintaining the same metabolic cost

per unit time estimated for the subject's original self-selected walking speed of 0.5 m/s.

4.2 Experimental Data Collection

As described in Meyer et al. (2016),[40] the experimental data used for the present study were

collected from a high-functioning hemiparetic subject with chronic stroke-related walking dysfunction

(sex male, age 79 years, LE Fugl-Meyer Motor Assessment 32/34 pts, right-sided hemiparesis, height 1.7

m, mass 80.5 kg). Experimental data collection was approved by the University of Florida Health Science

Center Institutional Review Board (IRB-01) and the Malcom Randall VA Medical Center Research and

Development Committee, and the subject gave written informed consent prior to participation. Motion

capture (Vicon Corp., Oxford, UK), ground reaction (Bertec Corp., Columbus, OH, USA), and

electromyography (EMG) data (Motion Lab Systems, Baton Rouge, LA, USA) were collected

simultaneously while the subject walked on a split-belt instrumented treadmill with belts tied. The

subject walked at his self-selected speed of 0.5 m/s and fastest comfortable speed of 0.8 m/s. To

facilitate ground contact model personalization, the subject wore Adidas Samba Classic sneakers, which

possess a flat sole with neutral midsole. Motion capture data utilized a full-body marker set with one

marker at each toe tip, three markers on each hindfoot, shank, and thigh, three markers on the pelvis,

and one marker on each acromion, elbow, and wrist (Reinbolt et al., 2005; Fregly et al., 2007). Ground

reaction data from each treadmill force plate included three force and moment components along with

the location of the fixed point used for moment calculations. EMG data included a combination of

surface and fine-wire electrodes collected from 16 muscles on each leg, including deep muscles

adductor longus, iliopsoas, tibialis posterior, extensor digitorum longus, and flexor digitorum longus.

Processing of marker motion, ground reaction, and EMG data followed a previously published

protocol.[40] Marker motion and ground reaction data were filtered at a variable cut-off frequency of 7/tf

Hz, where tf is the period of the gait cycle being analyzed, using a fourth-order zero phase lag

Butterworth filter.[123] EMG data were high-pass filtered at 40 Hz,[66] demeaned, rectified, and low-pass

filtered at a variable cut-off frequency 3.5/tf Hz using a fourth-order zero phase lag Butterworth filter.

Each processed EMG signal was normalized by the maximum value over all walking cycles and then

offset so that the minimum value was zero. For both walking speeds, the single most periodic walking

cycle (heel strike to heel strike for the paretic right leg) was selected for analysis, and all data for this

one cycle were resampled to 101 time points. After resampling, EMG data were padded with 200

milliseconds (18 time points) before the start of the cycle to account for electromechanical delay.

4.3 Model Personalization Process

We utilized all four tools in the Model Personalization toolset to personalize a full-body

neuromusculoskeletal model of the subject being studied. The starting point for the model

personalization process was a scaled RCNL2023 full-body OpenSim model, where scaling was performed

using the OpenSim Model Scaling tool with experimental marker data collected from the subject during

a static standing trial. All subsequent NMSM Pipeline tool runs were performed on a Dell PC workstation

possessing 48 cores.

First, the JMP tool was used to personalize lower body joint parameters and lower body scaling by

minimizing IK marker distance errors. The selected 0.8 m/s gait cycle marker data were used for all JMP

tool tasks. To avoid non-anatomical muscle paths around the hip complex, the left and right hip joint

parameters were not personalized. The left and right knee and ankle joints were personalized, but the

subtalar joint was not personalized because the joint did not move through a sufficient range of motion

to personalize the joint's parameter values accurately. The JMP tool reduced marker distance errors for

the thigh, shank, and foot markers by 48.4% for the gait cycle of interest. Additional JMP results are

included in Table 1 and in the supplementary material. Convergence was achieved after approximately

90 minutes of CPU time.

Marker Distance Errors Before and After Joint Model Personalization

	RMS (mm)		Max (mm)	
	Pre-JMP	Post-JMP	Pre-JMP	Post-JMP
Right Knee	7.5	4.2	18.5	11.8
Right Ankle	6.1	3.3	16.9	9.1
Left Knee	9.5	4.1	26.3	12.8
Left Ankle	6.5	3.2	16.4	10.1

Table 1: RMS and maximum marker distance errors (mm) for the right and left knee and ankle (including
subtalar) joints. Markers included in each joint's JMP marker set included thigh and shank markers for
each knee joint and shank and foot markers for each ankle joint. These markers were used to find the
pre- and post-JMP RMS and maximum marker distance errors.

Second, the MTP tool was used to personalize the properties of all lower body muscles by

minimizing errors in matching inverse dynamic joint moments and changes in initial muscle-tendon

parameter values while also predicting missing EMG signals for deep or "small" muscles (e.g.,

piriformis). Before the MTP tool was run, the OpenSim Inverse Kinematics, Inverse Dynamics, and

Muscle Analysis tools were run from the OpenSim GUI using the selected 0.8 m/s walking cycle data.

Using the outputs of these GUI tools, an NMSM Pipeline utility script processed EMG data, calculated

muscle-tendon velocity from muscle-tendon length data, and automatically organized the trial data into

the directory structure required by the MTP tool. Muscle groups were added to the post-JMP OpenSim

model to group muscles based on normalized fiber length similarity and activation similarity. Muscle-

tendon Length Initialization was used to find initial values for optimal muscle fiber length and tendon

slack length. At that point, muscle-tendon model and activation dynamics parameter values were

personalized. This process was repeated for each leg separately via separate runs of the MTP tool. After

the MTP tool was run for both legs, the left leg was found to match lower body joint moments with an

average root mean square (RMS) error of 3.5 Nm and the right leg with an average RMS error of 2.1 Nm.

Joint-specific moment matching results are included in Table 2 with additional plots available in the

supplementary material. A custom script was used to combine the left and right leg results for use by

the NCP tool. Convergence was achieved after approximately 30 minutes of CPU time.

Lower Body Joint Moment Matching Errors following Muscle-tendon Model Personalization

Joint Coordinate	Hip Flexion	Hip Adduction	Hip Rotation	Knee Angle	Ankle Angle	Subtalar Angle
Right (Nm)	2.9	2.7	3.1	1.7	1.0	1.5
Left (Nm)	5.8	4.3	4.8	2.2	2.4	1.5

Table 2: RMS errors between net joint moments calculated by the OpenSim ID tool and those calculated
by the NMSM Pipeline MTP tool following muscle-tendon model personalization.

Third, the NCP tool was used to calculate lower body muscle synergies (i.e., synergy vectors and

activations) by minimizing errors in matching inverse dynamic joint moments and muscle activations

produced by the MTP tool. Given our treatment design rationale above, we assumed that the subject's

synergy vectors were the same while his synergy activations were different for the two legs. As a result,

the NCP tool was used with the bilateral synergy vector symmetry option enabled. Synergy sets were

defined as muscle groups denoting the right and left legs. A previous synergy analysis performed on the

subject's processed EMG data indicated that six synergies were sufficient to account for the signal

variability even with the added synergy vector symmetry constraint. Muscle Tendon Length Initialization

was not performed as part of this NCP tool run because all muscles had MTP-derived muscle activations

and thus the activation minimization term was not used. The muscle synergies found by the NCP tool

reproduced all lower body joint moments with an average RMSE of 2.2 Nm and all MTP-derived muscle

activations with an average RMSE of 0.034. Additional NCP results are included in Table 3 and in the

supplementary material. Convergence was achieved after approximately 3 hours of CPU time.

Lower Body Joint Moment Matching Errors following Neural Control Model Personalization

Joint Coordinate	Hip Flexion	Hip Adduction	Hip Rotation	Knee Angle	Ankle Angle	Subtalar Angle
Right (Nm)	1.2	2.2	2.9	2.7	1.0	1.5
Left (Nm)	1.6	3.0	3.4	2.8	2.4	1.7

Table 3: RMS errors between net joint moments calculated by the OpenSim ID tool and those calculated
by the NMSM Pipeline NCP tool following neural control model personalization using muscle synergies.

Fourth, the GCP tool was used to personalize foot-ground contact model parameter values by

minimizing errors in matching ground reaction forces, ground reaction moments, and foot kinematics. A

contact element grid size of 5 by 11 was selected to match previous successful investigations.[70] The cost

functions for the three tasks performed by the tool were dominated by terms that emphasized matching

the vertical GRF, vertical and horizontal GRF, and vertical and horizontal GRF as well as ground reaction

moments, respectively, with each task starting from the solution of the previous task to track additional

quantities dependent on the previous quantities. To facilitate smooth ground reaction forces during

Ground Reaction Force/Moment and Foot Position/Orientation Errors following.
Ground Contact Model Personalization

Ground Reaction Forces and Moments	Anterior Force (N)	Vertical Force (N)	Lateral Force (N)	X Moment (Nm)	Y Moment (Nm)	Z Moment (Nm)	
Right	3.5	10.2	0.9	4.6	0.9	2.0	
Left	4.1	7.4	1.3	1.8	1.1	2.1	
Foot Positions and Orientations	X Translation (mm)	Y Translation (mm)	Z Translation (mm)	X Rotation (deg)	Y Rotation (deg)	Z Rotation (deg)	Toe Angle (deg)
Right	5.6	10.1	6.5	0.5	1.1	3.7	1.3
Left	4.9	6.6	4.8	2.1	1.7	2.5	1.2

Table 4: RMS errors between ground reaction forces and moments measured experimentally, and foot
positions and orientations measured experimentally and those calculated by the NMSM Pipeline GCP
tool following ground contact model personalization.

Treatment Optimization, we used the viscous friction coefficient as a design variable and turned off

dynamic friction. The viscous friction model penalizes excessive foot velocity with respect to the ground

during ground contact, which could lead to excessive horizontal GRFs in predictive simulations. The GCP

tool produced a physically realistic distribution of spring stiffness coefficients and matched ground

reaction forces, ground reaction moments, foot positions, and foot orientations with RMSEs of 4.6 N, 2.1

Nm, 6.4 mm, and 1.7 degrees, respectively.[124,125] Additional GCP results are included in Table 4 and in

the supplementary material. Convergence was achieved after approximately 4 hours of CPU time.

4.4 Treatment Optimization Process

After personalizing the subject's neuromusculoskeletal model using all four Model Personalization

tools, we ran all three Treatment Optimization tools to predict how underutilized paretic and non-

paretic leg synergy activations should be upregulated to achieve a 0.8 m/s self-selected walking speed

without increasing metabolic cost per unit time above the subject's 0.5 m/s level.

First, the TO tool was used to generate a dynamically consistent full body walking motion that

closely reproduced the subject's joint motion, joint moment, ground reaction, and muscle activation

data simultaneously using muscle synergy controls for the lower body and joint torque controls for the

back and upper body. Since synergy-driven TO requires an initial guess for synergy vectors and

activations, the TO tool XML settings file was configured such that the initial guess directly was defined

to be the NCP results directory while the tracked quantities directory was defined to be the

preprocessed data directory created after running the JMP tool. Other information, including an NMSM

Pipeline model file (.osimx), the post-JMP RCNL2023 OpenSim model, and the specified output

directory, were also included in the TO tool XML settings file. All lower body joints were controlled by

synergy controllers except for the toes coordinate, which was left uncontrolled, and all other joints were

controlled by torque controllers. Cost function terms tracked joint positions and velocities found by a

post-JMP IK analysis, joint moments found by a post-JMP ID analysis (excluding pelvis residual loads),

muscle activations found by MTP, and external loads consisting of processed experimental ground

reaction data. Constraint terms included bounded kinetic consistency errors (0.01 Nm) for all controlled

joints, root segment residual loads for the pelvis (1 N for forces and 0.1 Nm for moments), and joint

position periodicity errors (0.05 rad for joints below the pelvis and 0.1 rad for joints above it). The

solution produced by the TO tool matched tracked joint positions with an average RMSE of 2.1 degrees,

joint moments with an average RMSE of 5.1 Nm, ground reaction forces with an average RMSE of 25.3

N, ground reaction moments with an average RMSE of 4.0 Nm, and muscle activations with an average

RMSE of 0.038. Additional TO results are included in Table 5 and in the supplementary material.

Convergence was achieved after 305 IPOPT iterations, which required approximately 770 minutes of

CPU time.

Lower Body Tracking Optimization Errors Relative to Experimental Data

	Joint Angles (deg)	Joint Moments (Nm)	Ground Reaction Forces (N)	Ground Reaction Moments (Nm)	Muscle Activations
Right	2.7	4.0	22.8	4.3	0.037
Left	3.1	4.8	27.9	3.7	0.039

Table 5: RMS errors between joint angles, joint moments, ground reaction forces, ground reaction
moments, and muscle activations for the right and left legs obtained from experimental data and
corresponding quantities predicted by the NMSM Pipeline TO tool.

Second, the VO tool was used to verify that tracking the muscle synergy controls and upper body

joint kinematics found by the TO tool reproduced the joint motions, joint moments, and ground

reactions predicted by the TO tool without tracking those quantities explicitly. For the VO run, the

results of the previous TO run were used for both the initial guess and tracked quantities data. Cost

function terms tracked TO-found synergy controls and TO-found torque-controlled joint positions.

Constraint terms included bounded kinetic consistency errors (0.01 Nm) for all controlled joints, root

segment residual loads for the pelvis (1 N for forces and 0.1 Nm for moments), and joint position

periodicity errors (0.05 rad for joints below the pelvis and 0.1 rad for joints above it). The solution

produced by the VO tool matched tracked joint positions with an average RMSE of 0.1 deg, joint

moments with an average RMSE of 0.1 Nm, ground reaction forces with an average RMSE of 0.7 N,

ground reaction moments with an average RMSE of 0.1 Nm, and muscle activations with an average

RMSE of 0.01. Additional MTP results are included in Table 6 and in the supplementary material.

Convergence was achieved after 101 IPOPT iterations, which required approximately 170 minutes of

CPU time. Since the VO results closely matched the TO results, we were confident that the controller

and joint position tracking cost function terms and associated constraint terms selected for the

verification optimization could be used as the basis for the design optimization.

Lower Body Verification Optimization Errors Relative to Tracking Optimization Results

	Joint Angles (deg)	Joint Moments (Nm)	Ground Reaction Forces (N)	Ground Reaction Moments (Nm)	Muscle Activations
Right	0.09	0.06	0.44	0.06	0.01
Left	0.08	0.09	0.97	0.09	0.01

Table 6: RMS errors between joint angles, joint moments, ground reaction forces, ground reaction
moments, and muscle activations for the right and left legs obtained from the NMSM Pipeline TO tool
and corresponding quantities predicted by the NMSM Pipeline VO tool.

Finally, the DO tool was used to explore whether upregulating underutilized synergy activations in

the paretic leg and downregulating overutilized synergy activations in the non-paretic legs could

produce a faster self-selected walking speed of 0.8 m/s while maintaining the same metabolic cost per

unit time calculated for the subject's original self-selected walking speed of 0.5 m/s. The hypothesis in

this problem formulation is that large differences in synergy activation amplitudes between the two legs

are indicative of impaired paretic leg synergy activations that are smaller than desired and

compensatory non-paretic leg synergy activations that are larger than desired. When we evaluated the

synergy activations found by VO for the two legs, we identified four pairs that varied significantly in

amplitude between the left and right sides. Based on this observation, we formulated a DO problem that

sought to bring these four synergy activations with disparate amplitudes in the two legs closer to each

other. Each pair of asymmetric synergy activations contained a "weak" and "strong" side. First, scaled-

up "weak" synergy activations were tracked for each pair to increase their amplitudes. Second, a custom

user-defined cost function was written to reward synergy amplitude similarities between the "weak"

and "strong" synergy activations. A user-defined static parameter was added for each of the four

synergy pairs representing the amplitude scale factor to be applied to the "strong" synergy activation

using a user-defined model modification function. These two terms increased weak synergy activations

and encouraged over-active synergy activations to reduce to more symmetric magnitudes while not

overconstraining the control space. In addition, a cost function term was added to find a solution with a

metabolic cost per unit time that matched the value calculated for the subject's original 0.5 m/s self-

selected walking speed. This value was 90% of the original value calculated for the subject's 0.8 m/s self-

selected walking speed, making a 10% reduction the target value. Cost function terms also tracked VO-

found synergy controls for the two symmetric control pairs and VO-found torque controls. Constraint

terms included bounded kinetic consistency errors (0.01 Nm) for all controlled joints, root segment

residual loads for the pelvis (1 N for forces and 0.1 Nm for moments), and joint position periodicity

errors (0.05 rad for joints below the pelvis and 0.1 rad for joints above it). The VO results were used in

both the initial guess and tracked quantities data directories, and the final time was fixed at the value

determined experimentally for the selected 0.8 m/s walking trial.

The DO predictive simulation produced modified kinematics, synergy activations, and ground

reactions that reduced the subject's metabolic cost per unit time by 9.9% for the selected gait cycle and

achieved closely matching maximum amplitudes for the four modified synergy activations. Final results

are plotted in Figure 11. Convergence was achieved after 489 IPOPT iterations, which required

approximately 730 minutes of CPU time. These DO results suggest that upregulating weak paretic leg

synergy activations while downregulating paired non-paretic leg synergy activations could potentially

allow the modeled subject to increase his self-selected walking speed by 60% without increasing his

metabolic cost per unit time.

Figure 11: Plots showing the final results of the DO tool. Subfigures A) kinematics, B) synergy activations, C) muscle activations, and D) ground reaction forces and moments after VO (blue) and DO (red), respectively.

Discussion

The primary objective of this work was to develop a novel set of easy-to-use computational tools

that facilitate the creation of personalized neuromusculoskeletal models and the subsequent design of

personalized clinical treatments by researchers and clinicians with little to no programming experience.

These tools dramatically reduce the barrier to entry for researchers and clinicians working together who

would like to explore using personalized computational neuromusculoskeletal models to design

personalized treatment approaches. As shown in the example application, the NMSM Pipeline has the

potential to change the way treatments are investigated and applied throughout the

neuromusculoskeletal injury space.

Although the decision to use MATLAB for the NMSM Pipeline facilitates development and ease of

access for users, the decision does create several limitations. C++ and other similar compiled

programming languages generally run significantly faster than interpreted programming languages like

MATLAB. However, they also introduce challenges since few engineering researchers are strong C++

programmers, and system-specific build procedures can often be complicated.[126,127] Due to these

drawbacks, most biomechanics software written in compiled languages can be modified only by

reporting a bug or requesting a feature and waiting for experienced software developers to release a

new version of the software. The NMSM Pipeline actively encourages modifications, bug fixes, and

improvements through open-source easy-to-modify MATLAB toolsets. Other interpreted programming

languages like Python can struggle with package management, virtual environments, and/or

dependency version mismatches that increase barriers to use. MATLAB's native debugging tools,

English-readable error messages, and robust, stable core functions allow for development with

confidence, making the NMSM Pipeline robust to issues common to other interpreted languages.

Our hope is that the NMSM Pipeline's open-source, easy-to-use framework will encourage

investigations by the research community into "best practices" for each of the included tools. With the

availability of seven new tools, each with many optional features, the research community is

encouraged to explore novel approaches to achieving the best results from each tool. Investigations into

changes in task order, data processing/organization, cost function error centers and maximum allowable

errors, among others, will inform the entire research community on the best ways to leverage these

unique tools for successful future research and clinical outcomes.

We are already planning future enhancements to improve the versatility and applicability of the

NMSM Pipeline to a broader range of clinical and research problems. Potential enhancements would

allow greater flexibility and customization during use of the Model Personalization toolset. Support for

compliant tendon muscle models and muscle models that differentiate between fast and slow twitch

fibers in the MTP tool could facilitate muscle-tendon model personalization and simulation for "fast"

activities like running or jumping.[52,128] Support for time-delayed sensory feedback models in the NCP

tool could enable investigation of how spasticity, hyperreflexia, and hypertonia interact with

incoordination and weakness to produce functional impairment in individuals with an upper motor

neuron pathology. Support for multi-segment foot models in the GCP tool could facilitate higher fidelity

simulations of foot biomechanics and better reproduction of ground reaction moments. Other potential

enhancements could facilitate novel use of the Treatment Optimization toolset. User-defined controls,

time-delayed sensory feedback controls, and individual muscle controls could facilitate computational

design of personalized functional electrical stimulation protocols[58] and prediction of how

downregulating overactive reflexes could improve an individual's movement function. Support for user-

defined loads as a function of model states and controls and making it easy to add new states and

controls to a DO problem could facilitate computational design of personalized passive and/or active

exoskeletons, which would be added to a subject's personalized model after TO and VO had been

performed. An enhancement supporting multi-phase optimal control problems, where each phase

simulates a different movement cycle with control information shared across phases, could facilitate

simulating neural feedback mechanisms, neural adaptation, and cycle-to-cycle motion and control

variability. Enhancements supporting the use of closed-chain kinematic models would facilitate

simulation of shoulder models with improved kinematic fidelity for surgical, exoskeleton, and exercise

equipment applications. Support for connecting NMSM Pipeline controls to any type of OpenSim

actuator could allow exploration of alternative optimal control problem formulations that significantly

improve IPOPT convergence rate, especially for TO. Finally, for both toolsets, development of easy-to-

use MATLAB utility functions that automatically process experimental movement data and put it into a

format that can be used directly by NMSM Pipeline tools, without requiring any manual data

manipulation, would make the toolsets accessible to a wider user base.

With all of these potential future enhancements, several limitations and challenges in future NMSM

Pipeline development exist. First, the quality of the personalization results found by the Model

Personalization tools is limited by the quality and quantity of collected experimental data. At this time, it

can be challenging to collect all of the experimental data needed to exercise all seven NMSM Pipeline

tools with a synergy-driven neuromusculoskeletal model. Leveraging markerless motion capture or

inertial measurement units could potentially increase the ability of researchers to collect the movement

data required to perform a high-quality pipeline run-through. For Model Personalization, because

gradient-based optimization techniques are used, solutions may become entrapped in a local minimum,

though the final solution will still be better than the initial guess. The use of muscle activations rather

than excitations for the NCP tool and the Treatment Optimization toolset is another limitation, though

back calculation of muscle excitations from muscle activations could potentially be performed given

estimates of activation dynamics parameter values. Using the OpenSim framework through the

OpenSim MATLAB API prevents the NMSM Pipeline from using automatic differentiation to speed up

optimizations performed during the Model Personalization or Treatment Optimization process.

Computations leveraging the OpenSim MATLAB API are inefficient, and speed limitations inherent to this

framework cannot be overcome.

The NMSM Pipeline's Treatment Optimization toolset has key differences in design and

implementation from the existing OpenSim Moco tool. While Moco is generally the faster software due

to its C++-based implementation, Treatment Optimization leverages the flexibility of MATLAB and

GPOPS-II to facilitate novel features. Current unique features include user-defined functions and the use

of .osimx personalized model components, while future unique features could include support for multi-

phase optimal control problems, as discussed above. Treatment Optimization was designed to be

accessible to both novice and advanced users through intuitive XML settings files, whereas Moco users

typically set up problems through MATLAB or Python scripts. Even so, Moco's implementation facilitates

potential use of C++ automatic differentiation libraries to improve computational speed for gradient

calculations, resulting in more efficient optimizations. Lastly, Moco is free while both MATLAB and

GPOPS-II are commercial products with significant academic discounts. By incorporating NMSM Pipeline

model components into native OpenSim in the future, we plan to give users the option of using their

NMSM Pipeline personalized models in either our Treatment Optimization toolset or OpenSim Moco,

allowing the research community to explore the tradeoffs between these two approaches to developing

predictive simulations.

In conclusion, the NMSM Pipeline represents a significant step forward in the ability to personalize

neuromusculoskeletal computer models to patient movement data and then optimize parameters of

potential treatments using the personalized models. The software assembles over two decades of

biomechanics research into a well-designed and accessible framework that makes previously "high end"

modeling, simulation, and optimization techniques accessible to the entire research community. Our

hope is that by empowering researchers and clinicians working together to explore clinically relevant

questions and to design novel personalized interventions, the NMSM Pipeline will bring

neuromusculoskeletal computer modeling not only to but also across the doorstep of clinical utility.

Declarations

Ethics Approval and Consent to Participate

The de-identified experimental walking data used in this study were collected and disseminated as part

of a previously published study.[40]

Consent for Publication

891   Not applicable.

Availability of Data and Materials

The NMSM Pipeline software, along with all data, models, and settings files described in this article, are

available from the "Neuromusculoskeletal Modeling (NMSM) Pipeline" project on SimTK.org

(https://simtk.org/projects/nmsm). Users are welcome to share feedback and request new functionality

through this project's forum. Documentation including implementation details, examples, and tutorials

is available at https://nmsm.rice.edu.

Further details on the NMSM Pipeline software are provided below:

Project name: Neuromusculoskeletal Modeling Pipeline

Project home page: https://nmsm.rice.edu

Archived version:

Operating systems: Windows, MacOS

Programming language: MATLAB

Other requirements: Version 2023a or higher

License: Apache 2.0

The software has no restrictions for use by non-academics.

Competing Interests

908   The authors declare no competing interests.

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