# Emergence of alternative offspring care patterns from the evolution of parental negotiation strategies

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## Abstract

The evolution of parental cooperation is challenging to explain because caring for offspring is costly, and parents face an evolutionary conflict of interests over how much care each should contribute. Evolutionary game theory suggests that this conflict may be resolved through parental negotiation, where the parents make their care level dependent on the care provided by their partner. However, mathematical negotiation models typically predict a low level of parental cooperation. As these models are not dynamically explicit and tend to neglect stochasticity, we here investigate the evolution of parental negotiation strategies by means of individual-based simulations. Our results differ markedly from earlier analytical predictions. Parental negotiation strategies readily evolve, but replicate simulations result in four alternative care patterns: uniparental care, sex-biased care and egalitarian biparental care with constant or oscillatory care levels. Hence, pronounced sex differences in parental care can evolve even in the absence of sexual selection and uncertainty of paternity. Effective parental cooperation is the most frequent outcome, but in contrast to the earlier models, it is not based on parental compensation but on a tit-for-tat negotiation strategy. Actually, compensation destabilises cooperation and leads to less effective outcomes where one parental sex exploits the other one.

**Keywords:** negotiation rule, parental care, cooperation and conflict, reaction norm, individual-based simulations

## Introduction

Animals exhibit extraordinary variation in how much each parent contributes to caring for their joint offspring[1]. Traditionally, this variation is classified based on the number of caregivers, encompassing biparental, uniparental, and no care. This classification is, however, not the whole story. In some systems, biparental care is relatively egalitarian in that the parents share their workload equally[2, 3], while it is strongly asymmetric in other systems, often in a sex-specific manner[3, 4, 5]. Such differences may arise due to sexual conflict over parental care[6, 7]. While both parents benefit from a higher investment of their partner, it is mainly the partner that has to pay the costs for this investment. Therefore, there is a tension between the need for parental cooperation and the temptation to free-ride on the partner's effort[8, 9]. This antagonistic coevolution between the two sexes ('sexual conflict') has stimulated decades of theoretical and empirical work, attempting to explain how parental care variation and parental sex roles emerge[10, 11, 12, 13, 14, 15, 16].

Many theoretical models make the simplifying assumption that each of the two parents chooses a care strategy that is either fixed or employed only once during a brood care period. Such a strategy, which is assumed to be genetically determined, can be the probability of deserting the nest[10, 17, 18] or the parental effort (in terms of time, energy, and/or resources) devoted to the current brood[12, 13, 14, 15]. The resulting two-player game is then analysed either mathematically (by conducting an ESS analysis[12, 13] or applying a selection gradient approach[14, 15]) or through individual-based evolutionary simulations[16, 18]. This basic approach has been refined by considering 'dynamic' parental games where the parental strategies can change with the time of the season or the parental states[19, 20]. Moreover, the parental game was extended in various ways, allowing the study of the evolutionary interplay of parental care decisions with other factors, such as sexual selection[14, 15, 16, 21] or various sex ratios, such as the operational sex ratio (OSR) or the adult sex ratio (ASR)[14, 15, 22, 23].

All these approaches neglect the possibility that during the brood care period each parent flexibly responds to the behaviour of the other parent. It is well-known from evolutionary game theory that such responsiveness is a game-changer[24, 25]. For example, in the absence of responsive strategies, non-cooperative behaviour is the only evolutionarily stable outcome in the repeated Prisoner's Dilemma game, while cooperation readily evolves if responsive strategies like Tit-for-Tat are also considered[26, 27]. In line with this, John McNamara and colleagues[9, 28] argued that, in organisms with extended periods of biparental care, parental games should be modelled as involving a series of interactions in which the parents negotiate the final outcome. To understand patterns of parental care, models should focus on the evolution of 'negotiation rules' instead of the evolution of specific levels of care[28]. This negotiation rule approach does indeed seem to be more realistic, as there is ample evidence that caregivers respond to each other's behaviour in nature[29, 30, 31, 32, 33].

When analysing the classical parental care game of Houston and Davies[12] from a negotiation perspective, John McNamara and colleagues[28] showed that responsiveness does indeed make

a difference. They concluded that, rather than fostering parental cooperation, the evolutionarily
stable negotiation rule leads to a lower parental provisioning rate than the non-negotiated fixed
level of the Houston-Davies model. The offspring are generally better off with two jointly caring
parents than with a single caregiver, but under some circumstances, negotiation hampers
parental cooperation to such an extent that the offspring would profit from uniparental care[13].
These theoretical results inspired many empirical tests (reviewed in [9, 29, 34, 35]), which led to a
diversity of outcomes, including effective parental cooperation[34, 36, 37]. Several proposals have
been made on reconciling such cooperation with negotiation theory[34, 36, 38]. For example,
Johnstone and colleagues[36, 38] proposed a new type of negotiation model where the negotiation
strategies are solely based on the identity of the parent who last contributed to care. In the most
basal variant of the model[36], the evolved negotiation strategy induces the parents to reciprocate
parental care by taking turns in offspring provisioning over time. Although turn-taking-like
behaviour has been observed in many empirical studies (reviewed in[35, 37]), there is still debate
on whether and how well the observations fit the model predictions[39, 40].

Although incorporating mutual responsiveness in parental care models is a substantial step
forward, negotiation theory is not yet fully solidified. Current models investigating the evolution
of responsive strategies all employ mathematical (or numerical) methods that are based on the
detailed analysis of the two parental fitness functions. Although such analyses are enlightening,
they do often not tell the full story. To keep the mathematical analysis tractable, many
simplifying assumptions must be made (which are not always easily recognisable) that can
strongly affect the model outcome. For example, Johnstone and Hinde [34] showed that
stochasticity and uncertainty can be relevant, quantitatively and qualitatively, for the
evolutionary outcome. Lessells and McNamara [41] noted an inconsistency in the early
negotiation models, as they did not specify the relationship between negotiation and
provisioning. Taylor and Day [42] pointed out another shortcoming of the early analyses: they did
not specify the degree of responsiveness in the negotiation rules. If responsiveness is allowed
to evolve, a continuum of (neutrally stable) negotiation rules arises, rather than a single
evolutionarily stable rule. Interestingly, simulations (whose type and assumptions are not
specified in [42]) indicated that parental cooperation is more prevalent than suggested by the
mathematical analysis.

Here, we propose complementing mathematical theory by studying the evolution of parental
negotiation rules through an individual-based simulation approach. Individual-based
evolutionary simulations consider two timescales: a 'behavioural' timescale, where individuals grow
up, interact with other individuals and produce offspring according to inherited strategies (in our case
negotiation rules), and an 'evolutionary' timescale, where the frequency distribution of these strategies
changes due to the combined action of natural selection, mutation, and genetic drift. Such an
approach has several advantages. First, individual interactions must be specified in detail,
preventing inconsistencies such as those noted by Lessells and McNamara [41]. Second,
individual-based simulations include various kinds of stochasticity (which can be essential for

the evolutionary outcome) in a natural and realistic manner. Third, there is no need to specify
fitness functions when running individual-based simulations. In the past, it has been shown
repeatedly that the specification of such functions is error-prone[11, 43] (see the Supplement for
details). More importantly, when the evolving strategies are multivariate (as in the case of
negotiation strategies), the evolutionary dynamics does not necessarily follow the fitness
gradient; as a consequence, standard mathematical methods may arrive at misleading
conclusions[16]. Fourth, behavioural polymorphisms readily emerge in individual-based models;
such polymorphisms are easily overlooked by mathematical analyses, although they can be
crucial for the evolutionary outcome[16, 44]. Last but not least, even complicated scenarios can
easily be translated into an individual-based evolutionary model, allowing one to tailor the model
to specific empirical systems and research questions[18, 45].

To our knowledge, an individual-based simulation approach has only once been employed to
study the evolution of negotiation rules – in a study by Quiñones and colleagues[45] that
demonstrates that negotiation can be a more effective driver of cooperation than kin selection.
Here, we follow their lead and investigate the evolution of negotiation rules in the context of
parental care. This allows us to address a variety of research questions. Does the evolution of
negotiation rules lead to a well-defined pattern of parental care, or are alternative evolutionary
outcomes possible? Can asymmetric parental sex roles evolve even if the sexes are initially
identical in the model? Can parental cooperation break down completely, resulting in the
replacement of biparental care by uniparental care? What type of care is most effective from the
offspring's perspective? Is, for example, negotiated biparental care less favourable for the
offspring than unnegotiated care as the mathematical models suggest?

## Results

**Model overview.** We consider an individual-based model for the evolution of parental care
strategies.  The individuals in our model can survive for several breeding seasons. Each
individual can only breed once per season. To this end, the adult individuals can form pairs and
produce one clutch of offspring. The survival probability of the offspring increases with the
parents' total food provisioning rate; for the individual parent, the survival probability to the next
season is negatively affected by its own food provisioning rate. Hence, there is a conflict of
interest between the parents: both profit from a high total provisioning rate, but each parent
prefers the other to do most of the provisioning. Our model investigates whether and how the
evolution of parental negotiation strategies can resolve this conflict. The negotiation process of
our model is illustrated in Figure 1. The offspring provisioning phase is subdivided into discrete
time periods. At the start of each period, each parent decides on the provisioning rate for the
next period. This decision is based on an inherited 'behavioural reaction norm,' that is, a rule
telling the parent what provisioning rate to adopt in response to the perceived provisioning rate
of the partner in the previous period (Fig. 1B). As shown in Fig. 1C, the combination of the two
parental reaction norms leads to a sequence of parental provisioning rates that often (but not

always) converges to an equilibrium (Fig. 1D). This iterative process determines the total
provisioning effort of both parents and, consequently, the survival probability of the parents and
their offspring. Each reaction norm is determined by two parameters: a parameter α that
corresponds to the provisioning rate of the partner that elicits half of the maximal provisioning
rate in the next time period and a parameter β that determines the slope of the reaction norm
(Fig. 1B). These two parameters are encoded by genes at an autosomal locus and transmitted
in a Mendelian manner from parents to their offspring (subject to rare mutations). Some
combinations of α and β will correspond to reaction norms (or negotiation rules) that yield their
bearers a higher reproductive success than others. Over evolutionary time, such rules will
spread in the population, eventually leading to a characteristic food provisioning pattern.

Evolution of fixed provisioning rates. As a standard of comparison, we first ran simulations for a
baseline model without negotiation. The baseline model is identical to the negotiation model,
with the exception that the parental provisioning rates (called $F_m$ and $F_f$ for the male and female
parent, respectively) are heritable parameters that are fixed throughout an individual's lifetime
(see Methods). As shown in the Supplement, all simulations rapidly converged to an
evolutionary equilibrium where for our default parameters both parents exhibit a provisioning
rate of about $F_m = F_f = 0.53$ feeds per minute, resulting in a total provisioning rate of $F_m + F_f = 1.06$.
Hence, we observed the evolution of egalitarian biparental care, and there was no indication of
alternative evolutionary outcomes.

Alternative outcomes in the evolution of negotiation strategies. The evolutionary dynamics of the
negotiation model differs markedly from that of the baseline model. Hundreds of replicate
simulations (with identical simulation parameters and identical starting conditions) resulted in six
alternative evolutionary outcomes that are illustrated in Figure 2. As shown in Figure 3, each of
the six evolutionary attractors induces a different provisioning pattern of the two parents. Fig. 3A
classifies the six evolutionary attractors in terms of $(\alpha_m, \beta_m, \alpha_f, \beta_f)$, the evolved values of the
parameters determining the parental behavioural reaction norms (interpreted as parental
negotiation rules) and indicates the relative frequency of each of the six outcomes. Fig. 3B
illustrates how the alternative pairs of evolved negotiation strategies result in distinct
provisioning patterns. We will now briefly describe these outcomes one by one.

(P1) Egalitarian biparental care. This outcome corresponds to the situation where the slopes of
the evolved reaction norms of both parents are positive ($\beta_m > 0$, $\beta_f > 0$). It occurred in 52% of
our simulations. In this case, the negotiation process (represented by the cobweb procedure in
Fig. 1C) results in the rapid convergence of the parental provisioning patterns to the intersection
point of the two reaction norms in the left panel of Fig. 3B(P1). In the simulation shown, this
corresponds to an average provisioning rate of $F_m = 0.58$ feeds per minute for the male and
$F_f = 0.64$ for the female. The actual provisioning rates of a randomly chosen breeding pair
throughout the breeding season fluctuate around these values because the actual number of
feeds is subject to stochasticity.

(P2ab) Sex-biased care. This outcome corresponds to the situation where the slopes of the
parental reaction norms evolve opposite signs, which occurred in 30% of the simulations. When
the evolved reaction norm of the male is increasing while that of the female is decreasing
($\beta_m > 0$, $\beta_f < 0$), the provisioning pattern is female-biased (P2b), as illustrated in Fig. 3B(P2). In
the simulation shown, the negotiation process results in an outcome where females provision at
the maximal rate ($F_f = 1.0$ feeds per minute) while the provisioning rate of males is much lower
(about $F_m = 0.35$ feeds per minute). Hence, an asymmetry in parental behaviour evolves (where
one parental sex is 'exploited' by the other sex) even though our model does not include any
asymmetries between the sexes. The opposite pattern, male-biased care (P2a), occurred as
frequently in our simulations (15%) as female-biased care (P2b). This pattern results if the slope
of the evolved negotiation strategy of the female is positive while that of the male is negative
($\beta_m < 0$, $\beta_f > 0$).

(P3ab) Uniparental care. While in sex-biased care both parents participate in the provisioning of
the offspring, only one parent does all the provisioning in the case of uniparental care. This
outcome evolved in 12% of the simulations (6% resulting in male-only care, P3a, and 6% in
female-only care, P3b). Fig. 3B(P3) shows an example of male-only care, where throughout the
breeding season the male provisions the offspring at the maximal rate ($F_m = 1.0$), while the
provisioning rate of the female is zero ($F_f = 0.0$). Such uniparental care resulted in all
simulations where the slopes of both reaction norms evolved to negative values ($\beta_m < 0$, $\beta_f < 0$),
while the evolved values of $\alpha_m$ and $\alpha_f$ differed considerably. As indicated by Fig. 2C, male-only
care results when $\alpha_m$ is substantially larger than $\alpha_f$ ($\alpha_m \square \alpha_f$), while female-only care
corresponds to the opposite relationship $\alpha_f \square \alpha_m$.

(P4) Oscillatory care. About 6% of our simulations resulted in a pattern where both sexes
alternate between provisioning at maximal and minimal rates in strict synchrony. This pattern of
biparental care results when the slopes of both reaction norms evolve to negative values
($\beta_m < 0$, $\beta_f < 0$) while the evolved values of $\alpha_m$ and $\alpha_f$ are similar ($\alpha_m \approx \alpha_f$).

Efficacy of evolutionary outcomes. All six provisioning patterns described above evolved
regularly, even though they differ in the total care provided to the offspring. In the simulations
shown in Fig. 3B, the total provisioning rate is 1.22 (= 0.58 + 0.64) in the case of (P1), 1.35 (=
0.35 +1.00) in the case of (P2), and 1.00 in the case of (P3) and (P4). In line with this, offspring
survival rates differ considerably between scenarios. In the sex-biased patterns, the sex
provisioning at the maximal rate has considerably higher mortality than the sex that provisions
at a lower rate (P2) or not at all (P3). Accordingly, the adult sex ratio becomes biased in favour
of the less-caring sex, and many members of that sex cannot breed at all in a given season.
Figure 4 illustrates that, as a result, the number of breeding pairs in the population is much
smaller in the case of the sex-biased care patterns (P2) and (P3) than in the unbiased care
patterns (P1) and (P4). Notice that, in comparison to the baseline model (where the total
provisioning rate fluctuated around 1.06), parental provisioning is higher in negotiation equilibria
(P1) and (P2) and lower in (P3) and (P4).

In all simulations, the populations were monomorphic for the evolved reaction norms. In other
words, all members of a given sex employed the same sex-specific reaction norm (with the
possible exception of a few rare mutants). Accordingly, all breeding pairs in the population
showed a very similar provisioning pattern (Figure 4).

**Evolutionary transitions between parental care patterns.** It is well-known that in stochastic
systems with alternative stable states, rapid transitions between attractors will almost inevitably
occur in a long-term perspective[16, 18]. To check for the long-term stability of the provisioning
patterns in our model, we ran 100 simulations for 1 million seasons. In 80% of these long-term
simulations, the provisioning pattern did not change between seasons 40k and 1,000k. However,
evolutionary transitions from one care pattern to a different one occurred in 20% of these
simulations. Figure 5 shows an example of a rapid transition from biparental care to female-
biased care. This example is representative in the sense that, in our model, egalitarian
biparental care is more 'labile' than the other forms of care: in all cases where an evolutionary
transition occurred, it involved a switch from egalitarian care to either sex-biased care or
uniparental care, while the opposite switch was never observed in our long-term simulations.

## Discussion

To our knowledge, this study is the first attempt to investigate the evolution of parental
negotiation strategies via individual-based simulations. In line with analytical models[13, 28, 41, 42],
we show that egalitarian biparental care can evolve, where both parents provision their offspring
at a similar rate. However, egalitarian care with a constant provisioning rate is not the only
evolutionary outcome. For the same parameter setting and initial conditions, almost 50% of the
simulations converged to a qualitatively different evolutionary attractor. Even though the sexes
have identical characteristics in our model, about 30% of the simulations led to sex-biased
biparental care (P2) where either the male or the female provisions the offspring at a much
higher rate than the other parent. More than 10% of the simulations ended up in uniparental
care (P3) where only one of the parents does all the caring. A small percentage of the
simulations ended up in an oscillatory equilibrium (P4), where both parents switch between
periods with maximal and minimal parental effort. This seemingly strange outcome may reflect
synchronised food provisioning in the wild, where parents time nest visits to coincide with each
other's return[46, 47]. In contrast to other individual-based simulation models[16, 18, 44], the evolved
populations were monomorphic, that is, we did not observe systematic individual differences in
negotiation strategies. In line with other models with alternative evolutionary attractors [16, 18, 48],
the evolutionary outcome was 'labile' in the sense that, in a long-term perspective, rapid
transitions between attractors occurred occasionally.

Many empirical studies have arrived at the conclusion that closely related species evolved very
different patterns of parental care (from egalitarian care to sex-biased care to uniparental care)
(e.g., Møller & Thornhill 1998; Remeš et al. 2015) and phylogenetic analyses revealed that
switches from one care pattern to another one are surprisingly common[5, 50, 51]. Traditionally, this

variation has been ascribed to ecological factors such as food abundance [52], predation
pressure[53], ambient temperature [54, 55], or environmental stochasticity [56], to demographic factors
like the sex ratio [57], and to sex differences related to life-history features[5] or sexual selection [49].
In line with such explanations, evolutionary transitions between parental care patterns have
been ascribed to a change in these factors[5, 54, 57, 58]. Our study reveals that a diversity of care
patterns can, in principle, evolve even in the same homogeneous environment and in the
absence of pronounced sex differences in life history and mating patterns. This conclusion
aligns well with recent phylogenetic studies that only find a weak correlation between parental
care patterns and the above-mentioned factors[59] and with earlier simulation studies on a
different type of parental care models[16, 23]. Our model also illustrates that rapid transitions
between parental care patterns can occur spontaneously, without any change in environmental
or organismal conditions. Such transitions have also been reported earlier[16, 18, 23] but, to our
knowledge, never in negotiation models or other models with a multivariate strategy space. As
argued by Long and Weissing (2023), spontaneous transitions between evolutionary attractors
are less strange than they might appear; in fact, one should expect them to occur regularly (on a
long-term perspective) whenever a system has alternative stable states and is subject to
considerable stochasticity.

The focus of most analyses of mathematical parental care models was on finding an
evolutionarily stable equilibrium corresponding to egalitarian biparental care. Various authors
stated that equilibria corresponding to unisexual care might also exist, but, to our knowledge,
the sex-biased negotiation equilibrium P2 has never been found or considered in the
mathematical models. Apparently, the more-caring sex is exploited by the less-caring sex. This
is confirmed by the slopes of the evolved reaction norms, which, in the case of P2, differ in sign
(see Fig. 3). The more-caring sex employs a decreasing reaction norm ($\beta < 0$), indicating a
compensatory negotiation rule ("increase your effort when the partner worked less than
expected and decrease your effort otherwise"). One can imagine that such a rule can be
exploited. In contrast, the less-caring sex employs an increasing reaction norm ($\beta > 0$),
indicating a negotiation rule that resembles a 'tit-for-tat' kind of strategy ("decrease your effort
when your partner did not work hard enough and increase it otherwise"). Notably, the net effect
is that the total level of parental care is higher in the case of sex-biased care (P2) than in the
cases of egalitarian biparental care or uniparental care. However, in the sex-biased equilibrium
P2, the exploitation of one sex ultimately backfires at the population level: the more-caring sex
becomes rarer due to increased mortality, which negatively impacts the mating prospects of the
exploiting sex.

When negotiation models were first introduced, the general expectation was that negotiation
tends to foster cooperation (as in Quiñones et al. 2016 and many economic models[60, 61, 62]). This
expectation is supported by those of our simulations that lead to stable, egalitarian biparental
care (P1), where both parents employ negotiation rules of the tit-for-tat type. In these
simulations, the total care level is lower than in P2 but higher than in the absence of negotiation

(the baseline model). Interestingly, most mathematical studies [13, 28, 41, 42] (but see Johnstone et al.
2014) arrive at the opposite conclusion that the total care level in an evolutionarily stable
negotiation equilibrium is *lower* than in the corresponding model without negotiation (the
Houston-Davies model[12]). In line with the mathematical model studies, our simulations suggest
that in the case of uniparental care (P3), the total care level is lower than in the case of
biparental care, irrespective of whether biparental care is achieved with or without negotiation.
However, we also regularly encountered the oscillatory biparental care equilibrium (P4), where
the total care level does not exceed that of uniparental care.

It is well-known from game theory that stochasticity can be of considerable importance for the
evolutionary outcome [63]. Individual-based evolutionary models automatically include several
forms of stochasticity, such as demographic stochasticity, genetic drift, and the random influx of
mutations, while most mathematical models only consider random mutations (but see [38, 64]). Our
model also includes another form of stochasticity, which arises from incomplete information on
the previous behaviour of the interaction partner. In our model, the negotiation process is an
integral part of the provisioning period (in line with Lessells & McNamara 2012), and the idea is
that in each step, the two parents respond to the effort of their partner in the previous period.
However, this effort may not easily be observable. If both parents are busy collecting food, the
partner may be out of sight much of the time. Moreover, finding food is a stochastic process with
a variable outcome for the same effort. Therefore, the partner's effort can only be deduced
indirectly, for example, from the feeding state of the offspring. In our model, we implemented
this by discriminating between the intended and the realised feeding rate of the partner and
making strategic decisions dependent on the realised rates. In addition, our model assumes that
negotiation decisions are made on a longer time scale (time unit 'one hour') than the time scale
of provisioning events (time unit 'one minute'). The choice of time scale is crucial because it
determines the reliability of the information on which the negotiation decisions are based. If the
time scale is too short (say, after each provisioning event, as in Johnstone et al. 2014), the
partner's feeding rate may reflect stochasticity (good or bad luck in finding food) more than the
partner's effort, leading to a haphazard and jumpy negotiation. If the time scale is too long, it
may take ages until a stable negotiation outcome is reached. In contrast to the more coarse-
grained mathematical models, individual-based simulation models have to include detailed
assumptions on the exact timing of events and the information on which decisions are based.
The necessity of including such detail is one reason why individual-based simulation
approaches are not yet very popular in evolutionary biology. We hope that our study shows that
such approaches are nevertheless a valuable addition to the toolbox of evolutionary theory for
at least three reasons. First, individual-based models include strategically important
stochasticity (e.g., 'trembling hand stochasticity'[63]) in a natural and realistic manner. Second, the
fact that the relationship between abstract strategies and concrete behaviours needs to be
specified in detail prevents inconsistencies that are part of many mathematical (negotiation)
models but are not easily spotted[41] (see the Supplementary Text for details) . Third, individual-
based models are not based on the analysis of a fitness function but are explicitly dynamic, thus

revealing the potential multiplicity of evolutionary outcomes and the existence of outcomes (like
sex-biased care) that are easily overlooked otherwise.

Of course, simulation approaches also have their downside. To get a good overview of the
range of dynamic behaviours within a reasonable time frame, the set of model parameters
needs to be restricted. We consider the focus on a two-parameter family of reaction norms
(characterised by the evolvable parameters $\alpha$ and $\beta$) the most important restriction of our
model, as only increasing or decreasing functions of sigmoidal shape could evolve, thus limiting
the flexibility of parental responses. It is possible that, due to this limitation, other negotiation
outcomes (like parental turn-taking[36]) never evolved. To mitigate the strategic restrictions, a
broader family of reaction norms could be employed (as in Botero et al. 2010[44]). Alternatively,
parental response strategies could be implemented via evolvable neural networks (as in Netz et
al. 2022[48]), which have limitless flexibility if also the network topology is allowed to evolve.

## Conclusions and empirical implications.

In the parental care literature, it is often assumed that sex biases in parental care are the result
of either sex differences in life history, morphology, and physiology or factors like sexual
selection or uncertainty of parentage[65, 66, 67]. Apparently, researchers implicitly assume that
asymmetries between the sexes are required to explain sex biases in parental behaviour. In line
with this, theoreticians have, in models lacking such asymmetries, typically restricted their
analysis to egalitarian evolutionary equilibria. Our study shows that such a restriction is not
warranted. Evolutionary feedback between male and female parental behaviour can lead to the
divergence of male and female strategies, ultimately resulting in asymmetric equilibria such as
sex-biased or uniparental care[16, 18].

Further, classical theoretical and empirical work on parental negotiation often hinges on the idea
that partial compensation (a negative slope β of the reaction norm) is a necessary condition for
the evolutionary stability of biparental care[9, 13, 28, 34]. In contrast, our model shows that
compensation destabilises parental cooperation: when a compensatory strategy evolves in only
one of the sexes, sex-biased care results (P2) where the compensatory sex is exploited by the
other sex; a compensatory strategy in both sexes either results in biparental care of low efficacy
(P4) or uniparental care, which corresponds to the collapse of cooperation (P3). Conversely,
biparental cooperation (P1) persists when a tit-for-tat negotiation rule (i.e. a reaction norm with a
positive slope β) evolves in both sexes. This type of responsive rule aligns with empirical studies
showing 'matching responses'[30, 68, 69] and supports recent theoretical and empirical research on
reciprocal cooperation[35, 36, 38]. If both parents apply a tit-for-tat rule, this has a stabilising effect:
even if one sex temporarily reduces its care contribution (either voluntarily or accidentally), the
system returns to the previous care level within a few interactions. In other words, biparental
care is maintained at an efficacious equilibrium that is stabilised by mutual parental
responsiveness.

The main purpose of our study was the conceptual clarification of the role of negotiation in the
evolution of parental care. However, we hope that the approach taken and the findings made
will open new avenues for empirical research. We welcome additional experimental studies
designed to elucidate the nature of parental norms of reaction (as in [31, 70]), ideally allowing
comparisons between (phylogenetically diverse) species. As we have seen, focusing on sex
differences in parental reaction norms may be particularly important[70, 71]. The emphasis should
not only be on parental compensation[13, 34] but also on tit-for-tat kind of rules[36, 38], allowing to test
whether and to what extent the diversity of parental care patterns found in nature can be
explained by a simple scheme as in Figure 3(A). Most likely, the negotiation rules in natural
systems are more sophisticated than those in our conceptual model. Finding this out may be of
considerable importance for the understanding of parental cooperation. Fortunately, individual-
based models like the one presented here are very flexible and can easily be expanded in
response to new empirical findings.

## Methods

**Intended and perceived provisioning rates.** As illustrated in Fig. 1A, the offspring
provisioning period is subdivided into 100 time periods that we imagine to correspond to one
hour each. Throughout the time period, the two parents have intended provisioning rates of $F_m$
and $F_f$ feeds per minute, respectively. The expected number of feeds per hour (60 minutes) is
therefore $60 \cdot F_m$ for the male parent and $60 \cdot F_f$ for the female parent. As food search is a
stochastic process, we assume that the actual provisioning rates in a given hour, $N_m$ and $N_f$,
are random variables that are drawn from Poisson distributions with means $60 \cdot F_m$ and $60 \cdot F_f$.
Hence, the realised provisioning rates per minute are $\tilde{F}_m = N_m/60$ and $\tilde{F}_f = N_f/60$. We assume
that these realised rates can be perceived by the partner (e.g. on the basis of the feeding state
of the offspring) and form the basis of the partner's decision regarding the intended provisioning
rate in the next time period.

**Behavioural reaction norms.** As illustrated in Fig. 1BC, the parental food provisioning to their
offspring is governed by inherited reaction norms (or negotiation rules). We consider reaction
norms of the form:

406
$$F_{ego}^{t+1} = R(\tilde{F}_{partner}^t) = \left(1 + \exp(-\beta \cdot (\tilde{F}_{partner}^t - \alpha))\right)^{-1}. \qquad (1)$$

In other words, ego's provisioning rate $F_{ego}^{t+1}$ in the next time period is determined by the partner's
perceived provisioning rate $\tilde{F}_{partner}^t$ in the previous time period via a logistic function $R$. The
function $R$ is sigmoidal and ranges between zero and one; it is monotonically increasing if $\beta > 0$
and monotonically decreasing if $\beta < 0$ (see Fig. 1BC). $R$ is characterised by the parameters $\alpha$
and $\beta$, which have the following interpretation: $\alpha$ corresponds to that provisioning rate of the
partner that elicits a provisioning rate of $\frac{1}{2}$ ($F_{ego}^{t+1} = \frac{1}{2}$ if $\tilde{F}_{partner}^t = \alpha$), and $\beta$ is proportional to the
steepest ascent of the function $R$ ($R'(\alpha) = \frac{1}{4}\beta$). The individuals in our model are haploid and
carry four genes with alleles $(\alpha_m, \beta_m, \alpha_f, \beta_f)$, where $\alpha_m$ and $\beta_m$ are expressed if the individual is
a male, whereas $\alpha_f$ and $\beta_f$ are expressed if the individual is a female. Hence, the reaction

norm $R_m$ of the male parent is given by eqn (1), with $\alpha$ and $\beta$ replaced by the male's inherited
values $\alpha_m$ and $\beta_m$, while the reaction norm $R_f$ of the female is obtained from (1) by substituting
the female's inherited values $\alpha_f$ and $\beta_f$.

**Parental provisioning dynamics.** Given the reaction norms $R_m$ and $R_f$ and the intended
provisioning rates in the first time period (which we assume to be $F_m^{t=1} = F_f^{t=1} = \frac{1}{2}$ per minute for
both parents), we can now deduce the provisioning sequence of both parents throughout the
whole provisioning period. Based on the intended provisioning rates $F_m^t$ and $F_f^t$ for time period $t$,
we can first derive the realised provisioning rates $\tilde{F}_m^t$ and $\tilde{F}_f^t$. Using eqn (1), this yields the
intended provisioning rates for the next time period: $F_m^{t+1} = R_m(\tilde{F}_f^t)$ and $F_f^{t+1} = R_f(\tilde{F}_m^t)$. Averaging all
realised provisioning rates yields a measure of the overall provisioning effort of the male and
female parent:

$$E_m = \tfrac{1}{100} \cdot \sum_t \tilde{F}_m^t \text{ and } E_f = \tfrac{1}{100} \cdot \sum_t \tilde{F}_f^t . \qquad (2)$$

**Effects of provisioning effort on parental survival.** We assume that the survival probability to
the next breeding season is for each parent negatively related to the parent's overall
provisioning effort:

$$S_m = S(E_m) = 1 - \tfrac{1}{3} \cdot e^{E_m} \text{ and } S_f = S(E_f) = 1 - \tfrac{1}{3} \cdot e^{E_f} . \qquad (3)$$

As the overall efforts $E_m$ and $E_f$ range between zero and one, the parental survival probabilities
range between $S(0) = \frac{2}{3}$ (in the case of no effort) and $S(1) \approx 0.1$ (in the case of maximal effort).
The parental survival functions in (3) are concave. To examine the robustness of our results, we
also run simulations with the linear function $S(E) = \frac{2}{3} - \frac{17}{30} \cdot E$ and the convex function $S(E) = \frac{2}{3} \cdot e^{-1.5E}$,
which also range between $S(0) = \frac{2}{3}$ and $S(1) \approx 0.1$. The same provisioning patterns evolve at
similar frequencies as the standard scenario when using the linear function (48% Egalitarian
care, 24% sex-biased care, 16% uniparental care and 12% oscillatory care). However,
uniparental care becomes the most prevalent provisioning pattern, with decreased occurrences
of egalitarian care and sex-biased care when using the convex function (32% Egalitarian care,
10% sex-biased care, 50% uniparental care and 8% oscillatory care).

**Effects of provisioning effort on offspring survival.** We assume that the probability $S_{off}$ of an
offspring to survive to adulthood (i.e., to the next breeding season) depends on the sum of the
overall efforts of both parents, $E_{tot} = E_m + E_f$. In our model, it is given by the sigmoidal function

$$S_{off}(E_{tot}) = \frac{A \cdot E_{tot}^2}{E_{tot}^2 + B} . \qquad (4)$$

Our parameter choice of $A = 1.30$ and $B = 1.15$ implies that the survival probability of an offspring
is zero in the absence of parental provisioning ($S_{off}(0) = 0$), 60% if the total effort of both parents
is $E_{tot} = 1.0$ ($S_{off}(1) = 0.6$), and 100% if $E_{tot} = 2.0$ and, hence, maximal ($S_{off}(2) = 1.0$). For a clutch
size of $C$, the expected number of surviving offspring is $S_{off}(E_{tot}) \cdot C$. Here, we assumed $C = 5$ for
all pairs, and the actual number of surviving offspring was drawn from a Poisson distribution
with mean $S_{off}(E_{tot}) \cdot 5$.

**Inheritance of behavioural reaction norms.** When a new offspring is formed, its genotype $(\alpha_m, \beta_m, \alpha_f, \beta_f)$ is formed by drawing each of the four alleles separately from the corresponding alleles of its parents, with a 50% probability from the father and a 50% probability from the mother. Hence, the four genes are not linked, and the same pair of parents can create offspring with $2^4 = 16$ possible genotypes. After assigning the offspring's genotype, mutations with a small effect size can occur. A mutation occurs at each of the four loci with probability $\mu = 0.01$. If a mutation occurs, the mutational step size is drawn from a normal distribution with mean zero and standard deviation $\sigma = 0.1$ and added to the allelic value inherited from one of the parents. Moreover, a new offspring is assigned a sex, where both sexes have the same probability.

**Population dynamics.** We consider a population that, at the start of each breeding season, has a constant size of 500 individuals. Preliminary simulations showed that this population size is large enough for selection to dominate genetic drift. At the same time, it is small enough to run replicate evolutionary simulations over tens of thousands of breeding seasons within a reasonable time frame. A breeding season starts with pair formation, where males and females are matched randomly as long as unmated individuals of both sexes are still available. After pair formation, each pair starts to produce a clutch of offspring and feed their young, as explained above. Each individual only has a single breeding opportunity per season. At the end of the season, all mated adults survive to the next breeding season with a probability given by eqn (3). Unmated individuals have a survival probability of $S(0) = \frac{2}{3}$. The offspring of the season survive and mature with a probability given by eqn (4). All surviving adults are transferred to the next season, while all non-surviving adults are removed from the population and replaced by (randomly drawn) surviving offspring. This ensures that the population size at the start of the season remains constant, but the adult sex ratio may get biased, implying that not all individuals of the most abundant sex can breed in the next season.

**Simulation details.** We initialised the population with 250 males and 250 females that all carried the allele combination $(\alpha_m, \beta_m, \alpha_f, \beta_f) = (\frac{1}{2}, 0, \frac{1}{2}, 0)$. Hence, initially all individuals employ a non-responsive strategy ($\beta = 0$) leading to a provisioning rate of $\frac{1}{2}$ food items per minute throughout the whole provisioning phase. Each simulation was run for at least 40,000 ('40k') seasons, as this time was sufficient to produce evolutionarily stable provisioning patterns. However, we also ran very long simulations (for 10,000k seasons) to check for stability (e.g. Fig. 4). Of all shorter simulations (40k seasons), at least 100 replicate simulations were run to check for consistency in outcomes. At least 50 replicates were run for the ultralong (10,000k) simulations. The simulation code was written in C++ (version 22) and is freely available. Simulation data were analysed and visualised in R-(version 3.3.0+). This theoretical study did not require ethical approval.

**Baseline model.** In the Supplement, we show simulation results of the baseline model where the (intended) parental provisioning rates $F_m$ and $F_f$ do not result from negotiation but are heritable parameters that remain constant throughout an individual's lifetime. The baseline model is identical in all aspects to the negotiation model described above, with one exception.

Instead of harbouring four alleles $(\alpha_m, \beta_m, \alpha_f, \beta_f)$ determining the male and female negotiation
strategy, each individual now carries two alleles $(F_m, F_f)$ determining the male and female
provisioning rate. These alleles are also transmitted to the offspring in a Mendelian manner,
subject to mutations as described above. However, $F_m$ and $F_f$ are restricted to the unit interval.
Therefore, mutations with a negative value were replaced by zero, while mutations above one
were replaced by one.

## References

1.  Royle NJ, Smiseth PT, Kölliker M. *The Evolution of Parental Care*. Oxford University Press (2012).

2.  Remeš V, Freckleton RP, Tökölyi J, Liker A, Székely T. The evolution of parental cooperation in birds. *Proceedings of the National Academy of Sciences* **112**, 13603-13608 (2015).

3.  West H.E.R., Capellini I. Male care and life history traits in mammals. *Nature Communications* **7**, 11854 (2016).

4.  Furness AI, Capellini I. The evolution of parental care diversity in amphibians. *Nature Communications* **10**, 4709 (2019).

5.  Vági B, *et al*. The evolution of exceptional diversity in parental care and fertilization modes in ray-finned fishes. *Evolution*, qpae100 (2024).

6.  Trivers RL. Parental investment and sexual selection. In: *Sexual Selection and the Descent of Man* (ed. Campbell BG). Aldine Press Chicago (1972).

7.  Parker GA. Sexual selection and sexual conflict. In: *Sexual Selection and Reproductive Competiion in Insects* (eds. Blum MS, Blum NA). Accademic Press (1979).

8.  Lessells CM. The evolutionary outcome of sexual conflict. *Philosophical Transactions of the Royal Society B-Biological Sciences* **361**, 301-317 (2006).

9.  Houston AI, Székely T, McNamara JM. Conflict between parents over care. *Trends in Ecology & Evolution* **20**, 33-38 (2005).

10. Maynard Smith J. Parental investment: A prospective analysis. *Animal Behaviour* **25**, 1-9 (1977).

11. Wade MJ, Shuster SM. The evolution of parental care in the context of sexual selection: A critical reassessment of parental investment theory.*The American Naturalist* **160**, 285-292 (2002).

12. Houston AI, Davies NB. The evolution of cooperation and life history in the dunnock, *Prunella modularis*. In Behavioural Ecology*: Ecological Consequences of Adaptive Behaviour*, 471-487 (1985).

13. McNamara JM, Houston AI, Barta Z, Osorno JL. Should young ever be better off with one parent than with two? *Behavioral Ecology* **14**, 301-310 (2003).

14. Kokko H, Jennions MD. Parental investment, sexual selection and sex ratios. *Journal of Evolutionary Biology* **21**, 919-948 (2008).

15. Fromhage L, Jennions MD. Coevolution of parental investment and sexually selected traits drives sex-role divergence. *Nature communications* **7**, 12517-12517 (2016).

545    16.    Long X, Weissing FJ. Transient polymorphisms in parental care strategies drive divergence of sex
546           roles. *Nature Communications* **14**, 6805 (2023).
547

548    17.    Webb JN, Houston AI, McNamara JM, SzéKely T. Multiple patterns of parental care. *Animal
549           Behaviour* **58**, 983-993 (1999).
550

551    18.    Zheng J, Komdeur J, Weissing FJ. Effects of season length and uniparental care efficacy on the
552           evolution of parental care. *Journal of Animal Ecology* **92**, 1719–1729 (2023).
553

554    19.    McNamara JM, Székely T, Webb JN, Houston AI. A dynamic game-theoretic model of parental
555           care. *Journal of Theoretical Biology* **205**, 605-623 (2000).
556

557    20.    Ewald C-O, McNamara J, Houston A. Parental care as a differential game: A dynamic extension
558           of the Houston–Davies game. *Applied Mathematics and Computation* **190**, 1450-1465 (2007).
559

560    21.    Alonzo SH. Sexual selection favours male parental care, when females can choose. *Proceedings
561           of the Royal Society B: Biological Sciences* **279**, 1784-1790 (2012).
562

563    22.    Jennions MD, Fromhage L. Not all sex ratios are equal: the Fisher condition, parental care and
564           sexual selection. *Philosophical Transactions of the Royal Society B: Biological Sciences* **372**,
565           20160312 (2017).
566

567    23.    Long X, Székely T, Komdeur J, Weissing FJ. A life-history perspective on the evolutionary
568           interplay of sex ratios and parental sex roles. *The American Naturalist*, 2022.2011.2023.517539
569           (2024).
570

571    24.    Maynard Smith J. *Evolution and the Theory of Games*. Cambridge University Press (1982).
572

573    25.    McNamara JM, Weissing FJ. Evolutionary game theory. In: *Social Behaviour: Genes, Ecology and
574           Evolution* (eds Székely T, Moore AJ, Komdeur J). Cambridge University Press (2010).
575

576    26.    Axelrod R, Hamilton W. The evolution of cooperation. *Science* **211**, 1390-1396 (1981).
577

578    27.    Van den Berg P, Weissing FJ. The importance of mechanisms for the evolution of cooperation.
579           *Proceedings of the Royal Society B: Biological Sciences* **282**, 20151382 (2015).
580

581    28.    McNamara JM, Gasson CE, Houston AI. Incorporating rules for responding into evolutionary
582           games. *Nature* **401**, 368-371 (1999).
583

584    29.    Harrison F, Barta Z, Cuthill I, Székely T. How is sexual conflict over parental care resolved? A
585           meta-analysis. *Journal of Evolutionary Biology* **22**, 1800-1812 (2009).
586

587    30.    Hinde CA, Kilner RM. Negotiations within the family over the supply of parental care.
588           *Proceedings of the Royal Society B-Biological Sciences* **274**, 53-60 (2007).
589

590    31.    Barbasch TA, *et al*. Negotiations over parental care: a test of alternative hypotheses in the clown
591           anemonefish. *Behavioral Ecology* **32**, 1256-1265 (2021).
592

593  32.    Smiseth PT, Moore AJ. Behavioral dynamics between caring males and females in a beetle with
594         facultative biparental care. *Behavioral Ecology* **15**, 621-628 (2004).
595

596  33.    Lessells CM. Sexual conflict. In: *The Evolution of Parental Care*). Oxford univeristy Press (2012).
597

598  34.    Johnstone RA, Hinde CA. Negotiation over offspring care - how should parents respond to each
599         other's efforts? *Behavioral Ecology* **17**, 818-827 (2006).
600

601  35.    Savage JL, Hinde CA. What Can We Quantify About Carer Behavior? *Frontiers in Ecology and
602         Evolution* **7**, (2019).
603

604  36.    Johnstone RA, Manica A, Fayet AL, Stoddard MC, Rodriguez-Girones MA, Hinde CA. Reciprocity
605         and conditional cooperation between great tit parents. *Behavioral Ecology* **25**, 216-222 (2014).
606

607  37.    Griffith SC. Cooperation and Coordination in Socially Monogamous Birds: Moving Away From a
608         Focus on Sexual Conflict. *Frontiers in Ecology and Evolution* **7**, (2019).
609

610  38.    Johnstone RA, Savage JL. Conditional Cooperation and Turn-Taking in Parental Care. *Frontiers in
611         Ecology and Evolution* **7**, (2019).
612

613  39.    Santema P, Schlicht E, Kempenaers B. Testing the conditional cooperation model: What can we
614         learn from parents taking turns when feeding offspring? *Frontiers in Ecology and Evolution* **7**,
615         (2019).
616

617  40.    Baldan D, Hinde CA, Lessells CM. Turn-taking between provisioning parents: partitioning
618         alternation. *Frontiers in Ecology and Evolution* **7**, (2019).
619

620  41.    Lessells CM, McNamara JM. Sexual conflict over parental investment in repeated bouts:
621         negotiation reduces overall care. *Proceedings of the Royal Society B-Biological Sciences* **279**,
622         1506-1514 (2012).
623

624  42.    Taylor PD, Day T. Stability in negotiation games and the emergence of cooperation. *Proceedings
625         of the Royal Society of London Series B: Biological Sciences* **271**, 669-674 (2004).
626

627  43.    Houston AI, McNamara JM. John Maynard Smith and the importance of consistency in
628         evolutionary game theory. *Biology and Philosophy* **20**, 933-950 (2005).
629

630  44.    Botero CA, Pen I, Komdeur J, Weissing FJ. The evolution of individual variation in communication
631         strategies. *Evolution* **64**, 3123-3133 (2010).
632

633  45.    Quiñones AE, van Doorn GS, Pen I, Weissing FJ, Taborsky M. Negotiation and appeasement can
634         be more effective drivers of sociality than kin selection. *Philosophical Transactions of the Royal
635         Society B: Biological Sciences* **371**, 20150089 (2016).
636

637  46.    Raihani NJ, Nelson-Flower MJ, Moyes K, Browning LE, Ridley AR. Synchronous provisioning
638         increases brood survival in cooperatively breeding pied babblers. *Journal of Animal Ecology* **79**,
639         44-52 (2010).
640

641 47. Mariette MM, Griffith CS. The Adaptive Significance of Provisioning and Foraging Coordination
642 between Breeding Partners. *The American Naturalist* **185**, 270-280 (2015).
643

644 48. Netz C, Hildenbrandt H, Weissing FJ. Complex eco-evolutionary dynamics induced by the
645 coevolution of predator–prey movement strategies. *Evolutionary Ecology* **36**, 1-17 (2022).
646

647 49. Møller AP, Thornhill R. Bilateral symmetry and sexual selection: a meta-analysis. *American*
648 *Naturalist* **151**, 174-192 (1998).
649

650 50. Székely T, Reynolds JD. Evolutionary transitions in parental care in shorebirds. *Proceedings of the*
651 *Royal Society of London Series B: Biological Sciences* **262**, 57-64 (1995).
652

653 51. Balshine S, Kempenaers B, Székely T, Reynolds JD, Goodwin NB, Freckleton RP. Evolutionary
654 transitions in parental care and live bearing in vertebrates. *Philosophical Transactions of the*
655 *Royal Society of London Series B: Biological Sciences* **357**, 269-281 (2002).
656

657 52. Eldegard K, Sonerud GA. Female offspring desertion and male-only care increase with natural
658 and experimental increase in food abundance. *Proceedings of the Royal Society B: Biological*
659 *Sciences* **276**, 1713-1721 (2009).
660

661 53. Pike DA, Clark RW, Manica A, Tseng H-Y, Hsu J-Y, Huang W-S. Surf and turf: predation by egg-
662 eating snakes has led to the evolution of parental care in a terrestrial lizard. *Scientific Reports* **6**,
663 22207 (2016).
664

665 54. Vincze O, *et al.* Local Environment but Not Genetic Differentiation Influences Biparental Care in
666 Ten Plover Populations. *PLOS ONE* **8**, e60998 (2013).
667

668 55. AlRashidi M, Kosztolányi A, Shobrak M, Küpper C, Székely T. Parental cooperation in an extreme
669 hot environment: natural behaviour and experimental evidence. *Animal Behaviour* **82**, 235-243
670 (2011).
671

672 56. Vincze O, *et al.* Parental cooperation in a changing climate: fluctuating environments predict
673 shifts in care division. *Global Ecology and Biogeography* **26**, 347-358 (2017).
674

675 57. Eberhart-Phillips LJ, *et al.* Demographic causes of adult sex ratio variation and their
676 consequences for parental cooperation. *Nature Communications* **9**, 1651 (2018).
677

678 58. Klug H, Bonsall MB, Alonzo SH. The origin of parental care in relation to male and female life
679 history. *Ecol Evol* **3**, 779-791 (2013).
680

681 59. Long X, Liu Y, Liker A, Weissing FJ, Komdeur J, Székely T. Does ecology and life history predict
682 parental cooperation in birds? A comparative analysis. *Behavioral Ecology and Sociobiology* **76**,
683 92 (2022).
684

685 60. Nash J. Two-Person Cooperative Games. *Econometrica* **21**, 128-140 (1953).
686

61. Rahwan I, Ramchurn SD, Jennings NR, McBurney P, Parsons S, Sonenberg LIZ. Argumentation-
based negotiation. *The Knowledge Engineering Review* **18**, 343-375 (2004).

62.   Luce DR, Raiffa H. *Games and Decisions*. John Wiley & Sons (1957).

63.   Selten R. Evolutionary stability in extensive two-person games. *Mathematical Social Sciences* **5**,
269-363 (1983).

64.   Ito K, McNamara JM, Yamauchi A, Higginson AD. The evolution of cooperation by negotiation in
a noisy world. *Journal of Evolutionary Biology* **30**, 603-615 (2017).

65.   McNamara JM, Wolf M. Sexual conflict over parental care promotes the evolution of sex
differences in care and the ability to care. *Proceedings of the Royal Society of London B:*
*Biological Sciences* **282**, (2015).

66.   Barta Z, Houston AI, McNamara JM, Székely T. Sexual Conflict about Parental Care: The Role of
Reserves. . *The American Naturalist* **159**, 687-705 (2002).

67.   Székely T. Sexual Conflict between Parents: Offspring Desertion and Asymmetrical Parental Care.
*Cold Spring Harbor Perspectives in Biology* **6**, (2014).

68.   Hinde CA. Negotiation over offspring care? a positive response to partner-provisioning rate in
great tits. *Behavioral Ecology* **17**, 6-12 (2006).

69.   Meade J, Nam KB, Lee JW, Hatchwell BJ. An experimental test of the information model for
negotiation of biparental care. *PLoS One* **6**, e19684 (2011).

70.   Baldan D*, et al.* Repeatable negotiation rules? Only females show repeatable responses to
partner removal in a brood-provisioning songbird. *Biology Letters* **19**, 20230136 (2023).

71.   Iserbyt A, Farrell S, Eens M, Müller W. Sex-specific negotiation rules in a costly conflict over
parental care. *Animal Behaviour* **100**, 52-58 (2015).

**Figure 1.** Negotiation over parental care in repeated bouts. (A) Two parents invest in a common set of offspring over a discrete number of time periods. At the start of each time period, each parent adjusts its provisioning rate in the new period to their partner's provisioning rate in the previous period. (B) This adjustment is based on heritable behavioural reaction norms (or negotiation rules) that evolve over the generations. In our model, the reaction norms are described by logistic functions, which are determined by two heritable parameters: a parameter α determining the location of the inflexion point and a parameter β determining the slope at the inflexion point. For each sex, two example reaction norms are shown. The solid lines are increasing functions ($\beta > 0$), implying that the provisioning rate elicited by the partner increases with the partner's provisioning rate in the previous time step. The dashed lines illustrate decreasing reaction norms ($\beta < 0$) where a higher provisioning rate by the partner elicits a lower provisioning rate in the next time period. (C) The negotiation process is illustrated by overlaying the solid reaction norms of a male and a female in a single graph (thereby swapping the axes of the female reaction norm in graph B). For any combination of provisioning rates in the previous time period, the light blue arrow indicates the response of the male, while the yellow arrow indicates the response of the female. (D) In the example shown ($\beta > 0$ in both parents), the repeated mutual adjustment of parental provisioning rates converges monotonically to stable sex-specific provisioning rates.

**Figure 2.** Alternative outcomes of the coevolution of male and female negotiation strategies. For 50 replicate simulations, the evolutionary trajectories of the heritable parameters $(\alpha_m, \beta_m)$ and $(\alpha_f, \beta_f)$ that determine the male and female negotiation strategies are shown in four panels where (A) $\beta_m$ is plotted against $\alpha_m$ (B) $\beta_f$ is plotted against $\alpha_f$, (C) $\alpha_f$ is plotted against $\alpha_m$, and (D) $\beta_f$ is plotted against $\beta_m$. All simulations were initialised at $\alpha_m = \alpha_f = 0.5$ and $\beta_m = \beta_f = 0.0$ and run for 40,000 seasons. The initial conditions correspond to a population where males and females provision their offspring at a constant rate of 0.5 and are indicated in the graphs by a black triangle. The evolved state of each simulation after 40,000 seasons is indicated by a solid dot. The 50 trajectories are representative for >1,000 simulations we have run for our model: all converged to six different attractors, which in the panels are indicated by different colours. Each attractor corresponds to a different provisioning pattern (see Figure 3): (P1) egalitarian biparental care (green), (P2a) male-biased care (purple), (P2b) female-biased care (pink), (P3a) male-only care (brown), (P3b) female-only care (yellow) and (P4) oscillatory care (blue).

**(A)**

**(B)**

**Figure 3.** Classification of evolved alternative provisioning patterns. (A) Classification of the six evolutionary attractors in terms of the evolved values $(\alpha_m, \beta_m, \alpha_f, \beta_f)$ that determine the male and female negotiation strategies. (B) The six alternative attractors induce distinct provisioning patterns that are illustrated in panels P1 to P4. Each panel shows one representative simulation. The sub-panels to the left show the evolved behavioural reaction norms of the male (blue) and female (red) parent and a cobweb that indicates the resulting sequence of provisioning rates. Starting at the green dot in the centre of the cobwebs, the yellow dots represent the provisioning rates in the course of the negotiation process. The subpanels to the right show the provisioning patterns of a randomly chosen pair of parents throughout the provisioning period. In (P1), both parents feed their offspring at a similar and roughly constant rate throughout the care period ('egalitarian care'). In (P2), one sex (here: the female) feeds at a maximal rate, while the other sex feeds at a much lower rate ('sex-biased care'). In (P3), one sex (here: the male) feeds again at a maximal rate, but the other sex does not feed the offspring at all ('uniparental care'). In (P4), both sexes oscillate between provisioning at maximal and minimal rates; they do so in synchrony ('oscillatory care').

**Figure 4.** Intrapopulation variation in parental provisioning patterns. For each of the four simulations in Figure 3B, representing the provisioning patterns (P1) to (P4), the provisioning rates (mean ± SD) of all breeding pairs in season 40k are shown (males in blue, females in red). (P1) Egalitarian care, where the males and females of all 230 breeding pairs provision their offspring at similar rates (0.58 and 0.64 feeds/min for the male and female, respectively) with limited variation within and across pairs throughout the season. (P2) Sex-biased care, where all females of the 140 breeding pairs provision at a much higher rate than their male partners. The higher breeding effort of the females results in a higher mortality and, consequently, in a male-biased population sex ratio. For this reason, the number of breeding pairs is much smaller than the maximum of 250. (P3) Uniparental care, where all males provision their offspring at the maximal rate, while all females feed a the minimal rate. Now, the population sex ratio is strongly female-biased. Accordingly, only 140 breeding pairs could be formed. (P4) Oscillatory care, where in all 245 breeding pairs the male and the female both oscillate between the maximal and the minimal provisioning rate. The simulations shown are representative in the sense that all simulations inspected exhibited very little within-population variation in offspring provisioning among breeding pairs.

**Figure 5.** Illustration of a rapid evolutionary switch between parental provisioning patterns. (A) Long-term evolutionary dynamics of the allelic value ($\alpha_m, \beta_m, \alpha_f, \beta_f$) over one million (1000k) seasons. In the first half of the evolutionary trajectory, $\beta_m$ and $\beta_f$ are almost identical and slightly positive, leading to egalitarian parental care (P1). In this evolutionary phase, $\alpha_m$ and $\alpha_f$ differ from each other, but both stay below 1.0. Around season 600k, this pattern changes rapidly: $\beta_f$ becomes negative and $\alpha_m$ increases to much higher values, while $\beta_m$ and $\alpha_f$ more or less stay at their previous values. considerably, leading to a considerable difference between $\alpha_m$ and $\alpha_f$. After season 600k, $\beta_m$ is positive and $\beta_f$ is negative, leading to female-biased care (P2a). (B) Parental provisioning pattern in seasons 600k (egalitarian parental care) and 800k (female-biased parental care).