Improved automated model building for cryo-EM maps using CryFold

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Constructing atomic models from cryogenic electron microscopy (cryo-EM) density maps is essential for interpreting molecular mechanisms. In this study, we present CryFold, an approach for *de novo* model building in cryo-EM that leverages recent advancements in AlphaFold2 [1] to improve the state-of-the-art method ModelAngelo [2]. To incorporate the cryo-EM map information, CryFold replaces the global attention mechanism in AlphaFold2 to local attention, further enhanced by a novel 3D rotary position embedding. It produces more complete models, accelerates the modeling, and reduces the resolution requirement. Applying CryFold to new maps results in accurate differentiation between paralog sequences in noisy regions, detection of previously uncharacterized proteins with unknown functions, precise compartmentalisation of the map for isolation of non-protein components, and improved modeling of conformational changes. In a particular case, a 104-protein complex was modeled within only 5.6 hours, and a minor conformational change of a single protein domain was detected at the periphery when models from two different maps were compared. CryFold stands as an accurate method currently available for model building of proteins in cryo-EM structure determination. CryFold is open-source software available at https://github.com/SBQ-1999/CryFold.

Introduction

With the advent of direct electron detectors, single-particle cryo-EM has become the primary method for resolving biomolecular structures [3-5]. A critical step in cryo-EM structure determination is the construction of atomic models from 3D density maps. The pace of model deposition derived from cryo-EM maps in the Protein Data Bank (PDB) has increased by two orders of magnitude, from 67 in 2012 to ~6000 expected in 2024 [6]. The exponential growth has been driven by advances in automation of data collection and processing [7], accessible software and web platforms empowering broader adoption [8], and community efforts to further democratize and improve cryo-EM methodologies [9], including the use of artificial intelligence (AI).

Previously, model building relied heavily on manual efforts, involving fitting homology models generated by tools like I-TASSER [10] into the density maps using graphic software, such as *Coot* [11] or Isolde [12]. The process of generating a 3D reconstruction involves averaging thousands of non-identical particle projections, resulting in cryo-EM maps that consist of regions with variable resolutions. Consequently, areas with higher flexibility or partial occupancy are more challenging to interpret with precision. For instance, it took around six months to develop modeling and refinement protocols to build a model for the cryo-EM map (EMD-2566, overall resolution 3.2 Å) of the large subunit from the yeast mitoribosome with 13 new proteins [4]. This was the first fully refined cryo-EM model of an asymmetric object that also illustrated cryo-EM's power in resolving structures of large complexes isolated from native sources, where not all protein sequences are known, marking a turning point in structural biology [5]. Today, individual components of complexes are routinely identified directly from the density maps, revealing novel regulatory pathways. In our hands, it led to the description of biochemical connection between biogenesis and fatty acid and iron-sulfur synthesis [13], evolutionary mechanisms for gene transfer from organelles to the nucleus [14], identification of gene splitting [15] and even the discovery of a new type of translational frameshift [16].

The amino-acid sequence can be inferred directly from the side-chain densities, allowing for searches of protein-sequence databases [17]. Tools like *FindMySequence*, which uses main-chain information to fit predicted residue-type probabilities, can query sequence databases of user's choice [18]. However, due to the labor-intensive nature of the process, many deposited PDB structures contain errors, limiting their biological interpretations [19, 20]. This is particularly true when reliable reference structures are unavailable or when dealing with density maps at resolutions lower than 4 Å. As a result, model building becomes a bottleneck, highlighting the necessity of automating this process.

Several methods have been developed to derive atomic structures from cryo-EM
density maps. These can be categorized into two groups: traditional and utilizing deep
learning. Traditional model-building methods include Pathwalking [21, 22], Buccaneer [23],
EM-Fold [24], Rosetta [25], MAINMAST [26], Phenix [27]. In Pathwalking and MAINMAST,
constructing all-atom structures from density maps is treated as a minimization
problem, solved using optimization algorithms. Rosetta and EM-Fold first deduce
fragment structures from the density map and assemble them using Monte Carlo
sampling.

Deep learning-based methods encompass DeepMainmast [28], EMBuild [29], CR-I-
TASSER [30], DeepTracer [31], ModelAngelo [2], Cryo2Struct [32]. These approaches typically
start by applying a deep network to detect the backbone structure from the density map.
They diverge in their subsequent strategies for constructing all-atom models. For
instance, DeepMainmast and EMBuild fit predicted structure models to the backbone
to create all-atom structures. CR-I-TASSER integrates backbone information into I-
TASSER's [10] classical assembly simulations to generate all-atom models. DeepTracer
connects backbone atoms by solving the traveling salesman problem before adding
side-chain atoms for the complete structure. ModelAngelo, regarded as state of the art,
uses predicted amino acid probabilities, refines backbone atoms with a graph-based
network and constructs the all-atom model through Invariant Point Attention, followed
by Hidden Markov Model (HMM)-based sequence correction. Cryo2Struct employs
HMM and Viterbi algorithms to align the input sequences with predicted ones to build
the all-atom structure. By incorporating components of protein structure prediction
framework, current methods have achieved more accurate results in interpreting density
maps [33].

Recently, a breakthrough came from deep learning based structure predictors, such as
AlphaFold2 (AF2) [1], RoseTTAFold [34] and trRosetta [35], which also contributed to the
awarding of the 2024 Nobel Prize in Chemistry. We reasoned that accuracy and the
resolution limit in protein model building, especially for the state-of-the-art method
ModelAngelo, could be further extended by taking advantage of the recent advances.
We thus developed CryFold. Tests on cryo-EM maps of multi protein complexes with
unknown components demonstrate the robustness of CryFold for automated model
building with high speed and accuracy.

Overview of the CryFold approach

CryFold takes as input a cryo-EM density map and the amino acid sequences of the
target proteins, following a two-step process for building atomic structures (Fig. 1). In
the first step, a 3D convolution-based network, specifically a U-Net [36], is employed to

predict the positions of Cα atoms from the density map. Due to GPU memory
limitations, the map is cropped into smaller patches (64×64×64), which are later
combined to reconstruct the original size. The second step generates all-atom structures
using novel transformer network adapted from AF2 [1]. The all-atom positions are post-
processed using a method similar to that used in ModelAngelo [2]. CryFold incorporates
a recycling mechanism, allowing for three iterative refinements of predictions like AF2
[1], and we introduced key modifications in the encoder and decoder to fully exploit the
structural information present in the density map. The encoder, which we call
Cryformer, transforms the density map into the node representation and the edge
representation. The decoder, namely Structure Module, generates all-atom positions
from these improved representations.

Two key differences distinguish the CryFold network (denoted by Cry-Net) from the
AF2 network: an enhanced transformer and the local attention. Cry-Net features an
enhanced transformer that incorporates 3D rotary position embedding (*3D-RoPE*).
Originally, RoPE was used to process 1D sequences [37]. Here we extend it to a node
position encoding in 3D space (see Methods and Supplementary S2.3). 3D-RoPE
effectively encodes the positional information of each node into all attention
calculations, making the attention score to decay with increasing distance between
nodes. This design takes advantage of the spatial constraints inherent in the density
map. The local attention in Cry-Net is realized through the improved edge
representation (see Methods). Instead of an all-against-all approach, Cry-Net employs
an all-against-*k* strategy, where *k* represents the number of spatial neighbors for each
node. This adjustment once again capitalizes on the spatial restraints provided by the
density map, which are usually unavailable in traditional structure prediction. These
features enable efficient training of a deeper network.

The post-processing procedure, adapted from ModelAngelo, is outlined as follows. The
initial all-atom structure is obtained from Cry-Net, and any segments with fewer than
four residues are trimmed (referred to as *model_net*). The amino acid type for each
residue in model_net is assigned as the class with the highest probability output from
Cry-Net. HMM profile is derived from the predicted probability distribution by Cry-
Net and aligned with the input amino acid sequence. The amino acid types of residues
in the Cry-Net structure (prior to trimming) are then corrected according to this
alignment, producing another structure denoted as *model_fix*. Finally, residues that do
not match the input sequence are pruned, producing *model_prune*, the default model
used for assessment unless otherwise specified.

Fig. 1. Overall architecture of CryFold.

Two major steps are employed to build all-atom structure from a cryo-EM density map and the amino acid sequences of the target proteins. In the first step (with purple background), the input density map is fed into a 3D convolution-based network U-Net to predict the Cα atom positions. The map is first cropped continuously into boxes of size 64×64×64, which are then processed by U-Net and combined at the end. The final U-Net output y^{pred} is of the same size to the input map and the value in each voxel is the probability of containing a Cα atom, which is refined by the mean-shift algorithm. In the second step (with green background), all-atom positions are predicted using a local attention network (Cry-Net) from the amino acid sequence and the predicted Cα atom. The initial node and edge representations are first fetched from density map guided by the predicted Cα atom positions. They are then fed into the Cryformer together with the sequence embedding from ESM-2. The updated representations are then decoded into all-atom structure using the Structure Module, followed by a post-processing step. The parameters r, k and c are the numbers of predicted Cα atoms, neighbors considered and channels, respectively.

Quality of the model building and benchmarking

To benchmark CryFold, we first tested it against 177 maps of resolution better than 4 Å from ModelAngelo. The specific metrics for performance evaluation are introduced in Supplementary Information S1. For objective comparison, the ModelAngelo models for these maps were downloaded from the website given in its paper [2]. For new maps,

atomic models were generated locally using the version v0.2.3, which has higher
accuracy to other versions in our tests.

While both CryFold and ModelAngelo perform well when the map resolution is better
than 3 Å (Fig. 2a, indicated by points in the upper right corner), CryFold's advantages
become evident as the map resolution decreases below 3 Å. Notably, with a higher
completeness rate, CryFold also generates more accurate structures, as indicated by Cα
RMSD (0.310 Å vs 0.334 Å) and backbone RMSD (0.338 Å vs 0.375 Å) (Fig. 2e).

Completeness is closely linked to backbone recall and amino acid accuracy. A decline
in either of these metrics results in reduced completeness. To further investigate this
relationship, we calculated backbone recall and amino acid accuracy for the
intermediate models (model_net and model_fix). CryFold achieves a backbone recall
in model_net of 97.17% vs. 94.37% of ModelAngelo (Fig. 2g). If segments less than 4
residues are retained, this parameter increases by 0.87% and 2.0% for CryFold and
ModelAngelo, respectively. The smaller increase for CryFold might reflect that the
structures generated by our network are less fragmented.

Additionally, CryFold exhibits a higher amino acid accuracy before pruning (in both
model_net and model_fix, Fig. 2g), and the two methods show comparable accuracy
after pruning (in model_prune, Fig. 2d). The amino acid accuracy for the model
generated by Cry-Net (model_net) is 73.14%, compared to 58.54% for ModelAngelo.
This indicates that our network possesses a stronger ability to assign amino acid types,
likely due to the enhanced transformer architecture. The HMM-based correction from
ModelAngelo performs well, improving amino acid accuracy in model_fix to 87.09%
for CryFold and 84.67% for ModelAngelo. In summary, CryFold shows high backbone
recall and amino acid accuracy, contributing to the overall completeness.

We also analyzed the accuracy of predicted structures based on the Q-scores [38] of
residues in the deposited structures. The Q-score reflects the consistency between the
map density and the atomic structure, with higher values typically indicating better local
resolution. Fig. 2c plots the backbone RMSD and the completeness of models built by
CryFold and ModelAngelo against the deposited Q-scores. When the Q-score is less
than 0 or greater than 0.6, CryFold models exhibit lower backbone RMSD. For other
Q-score ranges, the RMSDs of both methods are comparable. In terms of completeness,
CryFold outperforms ModelAngelo when the Q-score is below 0.6.

Next, we compared the number of true positives (TPs) in the structures generated by
both methods. A residue is classified as a TP if a corresponding deposited residue exists
within 3 Å. Both methods have 309,401 common TPs, with backbone RMSD values of
0.28 Å and 0.33 Å for CryFold and ModelAngelo, respectively (Fig. 2f). Additionally,
CryFold identifies 31,736 TPs that ModelAngelo misses, contributing to its higher

completeness. These residues generally correspond to lower-resolution areas, as indicated by their lower Q-scores (0.47) and higher backbone RMSD (0.77 Å, Fig. 2e). In contrast, ModelAngelo identifies only 8,980 TPs (with a backbone RMSD of 0.87 Å) that are missed by CryFold. This data reinforces CryFold's advantage in constructing atomic structures for lower-resolution maps/regions.

Fig. 2. Comparison between CryFold and ModelAngelo on the test set of 177 high-resolution maps.

(a) Head-to-head comparison based on the completeness. (b) Violin plots of the backbone recall and the backbone precision. (c) Backbone RMSD and completeness plotted as a function of the Q-scores of the deposited structures. (d) Head-to-head comparison of the amino acid accuracy. (e) Bar plots comparing the average RMSDs of Cα atoms and backbone atoms. The sizes of the sets of true positive residues (*all*, *common*, *exclusive*) are shown in (f). (f) Venn diagram showing the numbers of true positive residues predicted by both methods. (g) Backbone recall and amino acid accuracy for the intermediate models.

CryFold extends the map resolution limit for structure construction

Our tests indicate that CryFold exhibits slightly lower backbone precision compared to ModelAngelo (Fig. 2b), which may stem from CryFold's ability to construct structures in lower-resolution regions (see below), which are often absent in deposited structures and classified as false positives during evaluation. For instance, in the cryo-EM

structure of the *type III-E CRISPR Craspase gRAMP-crRNA complex* (PDB ID: 7Y82, EMD-33678; green cartoon and gray surface in Fig. 3a), residues 1041-1380 are largely absent in both the deposited structure (green cartoon in Fig. 3a) and the ModelAngelo model (magenta cartoon in Fig. 3a). The structures for these regions are modeled by CryFold (blue cartoon in Fig. 3a, b) but classified as false positives, resulting in a lower precision than ModelAngelo (88.8% vs 99.8%). However, these residues are modeled with high confidence (>70, see the next section). We also submitted the domain sequence to AlphaFold3 [39] (AF3) for structure prediction, yielding a high confidence score (AF3 confidence score > 0.8). Structure superimposition indicates that the AF3 model closely resembles the CryFold model (TM-score 0.86, RMSD 2.07 Å; Fig. 3c). This cross-validation supports the correctness of the CryFold model for the missing residues.

The above phenomenon is not isolated, and we have observed it in numerous cases, potentially impacting overall backbone precision. On average, the CryFold models for the 177 maps include approximately 75,000 new residues predicted with high confidence (> 60, see Fig. S1) absent in deposited structures. All structures generated by CryFold are available for download at https://yanglab.qd.sdu.edu.cn/CryFold.

Fig. 3. An example of how CryFold has a more complete model compared to the deposited structure.

(a) The gray surface is the density map EMD-33678 (reported resolution 2.83Å). The green/gray cartoon is the deposited structure (PDB ID: 7Y82); the blue cartoon is the CryFold model, the magenta cartoon is the ModelAngelo model, and the orange cartoon is the AF3 model for the unmodeled regions in the deposited structure. (b) The blue

cartoon is the modeling of the absent residues 1041-1380 in the deposited structure by CryFold and the gray surface is the corresponding density map. (c) An enlarged view of the red box in (a).

Evaluation of residue confidence scores

CryFold provides a reliable estimation of model accuracy through a per-residue confidence score, similar to the confidence scores available in protein structure prediction. This score is derived from the predicted FAPE loss (see Methods). The confidence score ranges from 0 to 100; a higher score indicating lower FAPE loss and a more confident prediction. This score is stored in the B-factor field of the mmCIF file. We analyzed the correlation between the confidence scores of all residues in 177 predicted structures generated by CryFold and their backbone RMSDs (Fig. 4a). Generally, a higher residue confidence score correlates with a lower backbone RMSD. In Fig. 4b and 4c, we illustrate two examples colored by their respective confidence scores. Notably, CryFold assigns lower confidence scores to loop regions, which tend to be more flexible and exhibit lower resolution in density maps.

Fig. 4. Correlation analysis between CryFold confidence score and backbone RMSD.

(a) Confidence score bin size is 6, and the error bars represent the 99% confidence interval of the mean on a per-residue basis. (b-c) CryFold models colored by confidence score for the maps EMD-28080 (b, PDB ID: 8EFD, reported resolution 3. 8Å) and EMD-33678 (c, PDB ID: 7Y82, reported resolution 2.83 Å).

Map masking improves backbone precision

Another factor contributing to CryFold's lower precision is the absence of automatic map masking. Map masking is typically used to exclude regions of low resolution or those unrelated to the structures of interest (e.g., membrane or solvent). We evaluated the impact of map masking on a set of 70 maps from the 177 high-resolution maps, for which both the original and masked maps are available from EMDB [40]. The average backbone precision for structures built by CryFold increased from 86.0% (using the original map) to 90.7% (using the masked map). While most cases show no significant

difference between the original and the masked maps (Fig. S2), some examples
demonstrate improved backbone precision with masked maps. For instance, for the map
EMD-33306, the backbone precision improved from 25.2% to 97.1% after masking
(Fig. S2e). However, map masking can sometimes result in incomplete atomic
structures (Fig. S2f). Nonetheless, our package provides an optional argument to accept
masked maps for expert users.

Benchmarking performance at 4-7 Å resolution maps

Next, we assessed the performance of CryFold at lower resolution range. We tested 104
maps with resolutions of 4-7 Å (Fig. 5a-c). As expected, the accuracy is lower compared
to high-resolution maps. Nevertheless, CryFold builds relatively complete models
(>50% completeness) for approximately 40% of the tested maps. CryFold generally
constructs more complete models than ModelAngelo (backbone recall 43.0% vs.
25.8%; completeness 36.8% vs 23.6%) while maintaining similar accuracy (amino acid
accuracy 86.6% vs. 85.3%; backbone RMSD 0.777 Å vs 0.905 Å). An example is given
in Fig. 6a to illustrate the performance on low-resolution maps.

Figure 5. CryFold ... 104 maps ...
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Running time and GPU memory usage

We evaluated CryFold's running time as a function of protein length on the 177 high-
resolution maps using a single GPU (A100, ~15G memory) (Fig. S3a). The running
time increases linearly with protein length. CryFold can build a structure of
approximately 40,000 residues in about 3.5 hours. CryFold allows users to balance GPU
memory and running time. By default, CryFold processes 300 residues at a time, using
~13 GB of GPU memory. An additional ~1 GB of memory is required for every 100
extra residues. Fig. S3b illustrates the running time for the PDB entry 8FNV (>9,000
residues) under three configurations. Increasing GPU memory by 1.6 times (from 15GB

to 24GB) results in acceleration of the speed by 1.5 times (from 44 minutes to 30 minutes). This linear relationship can be generalized to proteins of any length. In additional tests, the accuracy of predicted models remains consistent with increased crop size. Currently, the software only support single GPU inference, and implementing multiple GPUs functionality in the future might further accelerate protein model building.

Case studies to assess model completeness, protein identification and conformational changes

We showcase the advanced capabilities of CryFold with four complementary examples, each addressing a distinct and challenging aspect of modern macromolecular modeling (Fig. 6). They are introduced below in details.

1) *Handling low-resolution regions within maps.* An illustrative low-resolution example is provided in Fig. 6a, comparing models generated by CryFold and ModelAngelo. The case involves an open state of *kainate receptor GluK2* (PDB ID: 9B36) with 4.3 Å resolution. CryFold successfully constructs structures for 81.2% of the residues, achieving 0.45 Å backbone RMSD. In contrast, ModelAngelo constructs structures for 72.6% residues, achieving 0.53 Å backbone RMSD. Due to the lower resolution in the peripheral regions of the density map, ModelAngelo encountered difficulties during modeling. However, CryFold constructed relatively complete atomic models for these regions (Fig. 6a). In addition, CryFold takes less time than ModelAngelo for the modeling (0.28h vs 0.81h). This example clearly demonstrates CryFold's superior modeling capability and efficiency for handling low-resolution regions within maps.

2) *Resolving compositional heterogeneity by identifying closely related isoforms within a noisy map.* To illustrate CryFold's precision in distinguishing closely related sequences, we selected a challenging case from photosynthesis involving light harvesting. This process is mediated by pigment-protein light-harvesting complexes (Lhc) which function as antennas around catalytic reaction centers, converting photons into chemical energy [41]. These Lhc proteins have been conserved across eukaryotic photosynthetic organisms for billions of years [42]. In the structure of a plant photosystem, the antenna consists of four Lhca proteins [43, 44]. However, wild-type plants have been reported to contain additional isoforms with higher energy chlorophylls [45], and studies suggest extra Lhca dimers [46], supported by *in vitro* reconstitution [47, 48]. We purified photosystem I from a marine angiosperm in the Mediterranean and reconstructed its 3D structure. No reference protein database was used for this modeling. Compared to canonical models from pea and maize [49, 50], we observed an additional Lhca regulatory

dimer with unknown sequences (Fig. 6b). These unidentified chains are located in a
region with 3.0-4.0 Å resolution (Fig. 6c). Despite the short length (~200 residues) and
high similarity (>75% identity) with other isoforms, CryFold generated an atomic
model for these new chains without any reference protein database. This enabled us to
match the sequences within genomic data and identify them among a family of over ten
highly similar proteins. Specifically, these chains were identified as Lhca1 and Lhca4
isoforms. Furthermore, this performance also underscores CryFold's ability to segment
cryo-EM maps, focusing only on protein regions even with multiple cofactors present,
as well as noisy density (Fig. 6c,d). Specifically, the map region for the two newly
identified proteins includes more than 40 non-protein cofactors such as chlorophyll a,
chlorophyll b, lutein, violaxanthin, and β-carotene, as well as various lipids distributed
on different sides of the heterodimer that dominate the cryo-EM density (Fig. 6d). The
calculation took 1.3 hours on an A800 GPU.

3) *Detecting new proteins in multi-component complexes*. Another challenge in protein
modeling for complex organisms is determining the identity of previously
uncharacterized proteins directly from the cryo-EM map. CryFold is able to address
this challenge iteratively without extra model training. Specifically, an initial set of
sequences, which can be completely random or part of the sequences related to the
density map, can be fed into CryFold. The HMM profiles generated by CryFold are
then compared with the sequences in the sequence database related to the density map
(e.g., can be easily download from the UniProt database by organism information, or
just use the whole UniProt database if nothing is known). Successfully matched
sequences are added into the initial sequence set. CryFold is run again with the updated
set of sequences. This iterative process continues until no new sequences are identified.
The final set of sequences represents all sequences related to the density map. Once the
sequence database is prepared, this process becomes fully automated and requires no
manual intervention. This enables for the automatic search of sequences within the
density map from a vast sequence database, thereby constructing atomic models. The
prerequisite for this process to work is that the provided sequence database must
encompass all protein sequences in the density map. Given the rapid development of
the genome sequencing projects, this assumption is not difficult to meet. We can use
this function to identify unknown or missing subunits that human experts failed to build.

We tested CryFold's ability to tackle this using an unpublished reconstruction of
another photosynthetic complex with multiple chains from a brown alga. In this
example, CryFold identified and modeled 22 proteins, six of which had not been
previously characterized (Fig. 6e). Additionally, two universally conserved chains
exhibited fully resolved extensions of 71 and 99 residues, effectively doubling the
original size of each protein in the core complex; indicating potential functional

relevance (Fig. 6f). None of the newly modeled sections had not been identified before,
nor had the new chains been predicted to be part of the complex. CryFold's ability to
detect new proteins and structural extensions within intricate cryo-EM data
demonstrates its efficiency, with calculations taking only 1.1 hours on an A800 GPU.

4) *Capturing minor conformational changes in a mega-Dalton complex.* Finally, we
explored CryFold's sensitivity to subtle conformational changes. We used a
mitochondrial supercomplex functioning as a respirasome, with a mass of 1.8 MDa, in
which only one protein displayed a slight rotation [16]. First, CryFold generated an atomic
model from the map of the native source, constructing the 104-protein complex in 5.6
hours, with half of the chains being species-specific (Fig. 6g). Compared to
ModelAngelo, CryFold provided higher completeness in lower resolution regions of
the map (Fig. S4). To further assess CryFold's precision, we classified two maps and
found a subtle 15 Å movement in a single peripheral domain of a protein. This minor
motion was resolved in two conformations within the 261 × 296 Å supercomplex. The
resolution in the area of this conformational shift is 3.0-4.0 Å. CryFold's ability to
capture such minor structural variations demonstrates its effectiveness for investigating
dynamic biological particles and targeting structural regulation.

Fig. 6. **Capabilities of CryFold with four complementary examples.**
(a) Modelling at low-resolution regions showing comparison between the deposited
model PDB ID: 9B36 (grey cartoon, left), the CryFold model (blue cartoon, middle),
and the ModelAngelo model (purple cartoon, right) with corresponding closeup views.
The density map EMD-44129 (reported resolution 4.29 Å) is shown in transparent. (b)
Detection of isoforms from a noisy map is shown with a plant Photosystem I, where
CryFold modelled two additional proteins (right) compared to the maize complex (left,

PDB: 5ZJI). (c) CryFold identified two specific isoforms in the noisy map region with 3.0-4.0 Å resolution (transparent surface) from ten candidates with over 75% sequence identity. (d) The same map region colored by local resolution, showing the ability of CryFold to segment the density, as a major fraction is contributed by various cofactors. (e) Identification of six new proteins (green) in a 22-protein photosystem complex, shown with their corresponding map densities. (f) Two substantially extended proteins identified by CryFold in the same complex (right) compared to the canonical models (left). (g) The CryFold model of the mitochondrial respirasome II2-III$_2$ -IV2 [16] (grey) with 52 out of 104 proteins that were not reported in other complexes (red). Six of these proteins are shown with their densities and compared with the ModelAngelo in Fig. S4. (h) Two distinct conformations (blue and yellow in close-up views) of a single protein (RIP1) in the 104-protein supercomplex modelled by CryFold in two classes.

Ablating CryFold components to assess drivers of performance

To investigate the contributions of different components to CryFold, we conducted ablation experiments on the 177 high-resolution maps. Four configurations of its network, Cry-Net, were assessed: the default version (18-layer Cryformer), a version without node and edge attention, a version without sequence input, and a version without 3D rotary position embedding (3D-RoPE). These experiments evaluate the impact of network depth, sequence information, and 3D-RoPE on performance. Metrics included amino acid accuracy and all-atom RMSD, calculated against the deposited structures (Fig. 7). The default model achieved 0.506 Å all-atom RMSD and 73.1% amino acid accuracy. The RMSD increased slightly for shallower networks and the version without sequence input, while amino acid accuracy dropped significantly, especially for the version lacking sequence input. The configuration without 3D-RoPE exhibited the most substantial differences, with an increased all-atom RMSD of 0.341 Å and a 26.4% decrease in amino acid accuracy. Notably, the loss curve for the ablation experiment without 3D-RoPE displayed oscillations during training (Fig. S5), suggesting that this encoding is crucial for the effective training of Cry-Net.

Fig. 7. Results of ablation study.

The experiments are conducted on 177 high-resolution maps. (a) is the all-atom RMSD. (b) is the amino acid accuracy. The mean is indicated by the center point. The error bar is calculated based on the 95% percentile interval.

Conclusion

In this study, we demonstrate the advanced capabilities of CryFold in addressing complex challenges in macromolecular modeling. CryFold increases the accuracy and completeness of automated built protein models while reducing execution time, and the requirement for map resolution through a local attention-based deep neural network. Tests on large complexes show identification of previously unknown proteins that could not be revealed by other automated tools. For most tested maps, it constructs models with over 80% completeness, and previously missing residues could be modeled. Through specific examples, we illustrate CryFold's applications in addressing challenging tasks of modern macromolecular modeling. They include: successfully resolving low-resolution map regions, identifying closely related isoforms within noisy maps, detecting novel proteins in multi-component complexes even without a well-established protein database, and capturing subtle conformational changes within large protein assemblies. CryFold also goes beyond simple structural modeling by segmenting maps with multiple cofactors. Together, these results underscore CryFold's ability to tackle a variety of complex challenges in macromolecular modeling in a more time-effecient manner. The versatility, cost-efficiency and precision, mark CryFold as a valuable tool for high-throughput macromolecular modeling and functional analysis of dynamic biological assemblies.

Methods

Training and test data

Training set and validation set. In order to train our method and compare with ModelAngelo[2], we constructed the training dataset with the same setting used in ModelAngelo. Specifically, the training set consists of 6422 EMDB [40] cryo-EM density maps released before April 1, 2022 with resolution better than 4Å and paired structures in PDB [6]. The full training set was used to train an initial model. The model was used to filter the training dataset based on the precision (>0.5) of the predicted Cα atoms. After filtering, there are 5731 remaining map-model pairs, of which 10% are randomly selected for validation and 90% for training.

High-resolution test set. The test dataset we used consists of 177 high-resolution (better than 4 Å) maps from ModelAngelo[2] (released between April 1, 2022 and February 9, 2023). Besides, we applied our method to 2 large cryo-EM density maps to build atomic structures.

Low-resolution test set. To test the performance of CryFold on low-resolution maps, we collected another set of maps with lower resolution. We first obtained 135 maps with resolutions 4-7 Å, which were released between January 1, 2024 and June 1, 2024 (about two years after the training data). Among these maps, ModelAngelo failed to build atomic structures for 31 maps (the program did not respond for a long time or encountered errors during the process). Therefore, the final low-resolution test dataset consists of 104 maps with resolutions 4-7 Å. The number of residues in these maps ranges from 250 to 17520 (3461 residues on average).

CryFold algorithm

CryFold builds the atomic structure from the cryo-EM density map and amino acid sequence information through two major steps (see Fig. 1). The first step predicts the Cα atom positions using U-Net[36]; The second step builds all-atom positions using an enhanced transformer network Cry-Net. They are described in details below.

Step 1: Predict the Cα atom positions using U-Net

We train a 3D convolutional neural network to predict the Cα atom positions of all residues in the density map, which are represented by the Cα atoms coordinates. The convolutional neural network adopts the U-Net architecture[36]. A detailed architecture can be found in the supporting Fig. S6. The input to the network is the cropped density map, with each box size being 64×64×64. The shapes of the network outputs (i.e., y^{pred} and $\hat{y}^{pred}$ in Fig. 1) are the same as the original map but the value in each voxel (i.e.,

each cube 1×1×1) is the probability of containing a Cα atom (obtained through a sigmoid layer). The difference between y^{pred} and $\hat{y}^{pred}$ is that their corresponding labels are slightly different; the label for the former is a hard label, while the label for the latter is a soft label. Here, y^{pred} is used as the final output of the U-Net.

The loss function for U-Net[36] consists of the cross-entropy loss (*CE*) and L_2 distance loss (L_2) as follows:

$$Loss_1 = CE(y^{pred}, y^{true}) + L_2(\hat{y}^{pred}, \hat{y}^{true}) \tag{1}$$

where y^{pred} and $\hat{y}^{pred}$ are both predicted probability density maps for Cα atoms. y^{true} represents the map labeled by the positions of the real Cα atoms, in which a value of 1/0 indicates the presence/absence of a Cα atom; $\hat{y}^{true}$ represents the simulated Cα probability density map, which is calculated the deposited Cα atom coordinates as follows[51]:

$$\hat{y}^{true}(x) = \max\left\{ e^{-\frac{\|x-t\|^2}{d_0^2}}, \forall t \in J \right\} \tag{2}$$

where x is a grid point, t represents the coordinates of the Cα atoms, and J represents the set of all Cα atoms in the deposited structure; d_0 represents a normalization factor (3 Å here). If the distance from the grid point x to the nearest Cα atom is d_0, the probability value for the grid point will be $1/e$. We combine both losses, aiming for the network to learn rich information from the density map.

The Cα atom coordinates predicted above are refined through the mean-shift algorithm[26, 52]. The initial Cα atom coordinates with a probability value above 0.6 are selected first. Then the coordinates for each of the selected Cα atom are updated as the weighted linear sum of its neighboring Cα atoms within 1.7Å (including itself). After this update, the neighboring Cα atoms are removed because the Van der Waals radius of a carbon atom is 1.7Å. Such refinement is necessary because the real coordinates are continuous while the predicted ones from the density maps are discrete. After the refinement, we obtain a set of predicted Cα atoms (the total number of Cα atoms is denoted by r).

Step 2: Build all-atom positions using Cry-Net

Inspired by AlpahFold2, we designed a transformer network to build all-atom positions using a transformer network (named Cry-Net) from the input density map, the input sequences and the predicted Cα atoms. Cry-Net consists of two transformer-based modules. The first one is called Cryformer (see the lower panel of Fig. 1, and Fig. S7a) and the second one is called Structure Module (see the lower panel of Fig. 1, and Fig. S8). Cry-Net iteratively updates two key representations of the protein structure: *node*

535 *representation* and *edge representation* (correspond to the single representation and the

536 pair representation in AF2, respectively), which are introduced below.

Node representation. The node representation ($r \times c$, r is the number of predicted Cα

atoms, c is the number of channels) is constructed from the predicted Cα atoms and the

density map as follows. A cubic box with size $17 \times 17 \times 17$ Å^3 centered at each of the r

predicted Cα atoms is cropped from the density map first. Then to extract information

from the density map and reduce the dimensionality, a convolutional neural network

(CNN) is used to convert the density map in each cubic box into c channels. The

architecture of this CNN is the same as the encoder module in U-Net[36] (*i.e.*, Fig. S6a).

Edge representation. The edge representation ($k \times r \times c$) is constructed similarly,

measuring the relationship between neighboring nodes (k is the number of nearest

neighbors considered). For each edge, a rectangular box with size $3 \times 3 \times 12$ Å^3 is cropped

from the density map. The Cα atom is located at the center of the bottom box (*i.e.*, the

3×3 square) and the direction of the box is the same as the edge vector. Finally, another

convolutional neural network (with kernel size $3 \times 3 \times 1$) is used to convert the density

map in each rectangular box into c channels.

Note that the above representations are different with the ones used in AF2. The

representations here are constructed from the density map guided by the predicted Cα

atoms (inspired by ModelAngelo); rather than from multiple sequence alignment

(MSA) and homologous templates in AF2. In addition, the edge representation (called

pair representation in AF2) is a square matrix ($r \times r$) in AF2; while a non-square matrix

($k \times r$) here. This is because the density map already provides rich structure information

and we only need to consider the k-nearest neighbors rather than all nodes.

The input and output of Cry-Net in the n-th iteration are defined by the following

equation:

$$g\left(T^{(n)}, V, S\right) = (T^{(n+1)}, \alpha^{(n+1)}, A^{(n+1)}, P^{(n+1)}, E^{(n+1)}, M^{(n+1)}) \tag{3}$$

where $T^{(n)} \in \tilde{\ }^{r \times 3 \times 4}$ is the backbone frame (N, Cα, C) at the n-th step, V is the density map,

$S \in \tilde{\ }^{r \times 1280}$ is the sequence embedding from the protein language model ESM-2[53],

$\alpha \in \tilde{\ }^{r \times 7 \times 2}$ is the sine and cosine encoding of the three backbone and up to four side-chain

torsion angles, $A \in \tilde{\ }^{r \times 20}$ is the probability vector for the 20 types of amino acids, $P \in \tilde{\ }^{r}$

is the confidence score of each node, $E \in \tilde{\ }^{r \times k}$ is a binary vector indicating whether each

node is sequentially adjacent to its k nearest neighbors or not, and $M \in \tilde{\ }^{r}$ is the

probability of a node being a true residue.

Cryformer. The Cryformer module consists of a total of 18 blocks with non-shared

weights, as shown in Fig. S7a. The key difference between Cryformer and the

Evoformer in AF2 is the concentration on local attention rather than global attention.

This is reflected by the number of neighbors considered (i.e., the parameter k).
Evoformer will be equivalent to Cryformer when k equals to the total number of nodes
(i.e., $k=r$). The key components of Cryformer are described below.

Sequence attention. This layer incorporates the protein sequence information into the
node features with a gated cross-attention mechanism (see Supplementary Information
S2.2, Algorithm S1). The node representations are queries, and the sequence
embeddings from a pre-trained protein language model (*i.e.*, ESM-2[53]) are keys and
values.

Node attention. As shown in Fig. S7b, the node attention updates the representation of
a given node based on self-attention on the node and its k nearest neighbors, with the
information of edge representations serving as bias. As the depth of this network
increases, it can collect information from more nodes, resulting a larger receptive field.
It is worth noting that this node attention will be equivalent to the row-wise gated self-
attention in AF2 when k equals to r.

Transition and outer product. Inspired by AlphaFold3[39], The transition layer uses the
SwiGLU[54] instead of ReLU[55] to update the node and edge features. It uses the non-
linear activation function to enrich the representation of the two types of features. The
outer product layer updates the edge features based on the node features. It incorporates
the node features of two adjacent nodes into the edge features.

Edge attention. As shown in Fig. S7c, the edge attention updates the edge representation
through self-attention mechanism. The information of edge ij is aggregated from the
information of all edges connected to node i and all edges connected to node j. The edge
attention can be seen as a special type of the node attention, according to the Whitney
graph isomorphism theorem (Fig. S9). In addition, it is worth mentioning that when
$k=r$, the edge attention is equivalent to applying AF2's row and column attentions
simultaneously.

3D Rotary Position Embedding (3D-RoPE). 3D-RoPE is not an independent
component. Originally, RoPE[37] was used to process 1D sequences. We extend it to a
node position encoding in 3D space. It is inserted into the node attention as a
multiplicative positional encoding. It elegantly encodes the position information of
each node into the attention calculations. The attention score will decay when the
distance between two nodes increases. Please refer to the Supplementary Information
S2.3 for more detailed description about 3D-RoPE.

Amino acid probability for each node. In order to generate all-atom positions, we try to
assign each node to one of the 20 possible amino acids. This is done by using the
information from the density map of each node (i.e., the original node representation),
the information from neighboring nodes (i.e., the updated node representation) and the

sequence information (obtained from the sequence attention in Cryformer). A separate

MLP is trained to generate the amino acid probability vectors for all nodes (i.e., A in

Eq. 3, Fig. S10). Ablation experiments indicate that removing the information of

neighboring nodes (i.e., no node attention and edge attention) or removing the sequence

information will affect the subsequent determination of amino acid identity.

Structure Module. The Structure Module here (see Fig. S8) is largely similar to the

one in AF2 but with a few key differences (detailed below). It predicts the backbone

frame (i.e., T in Eq. 3) as well as the backbone and side-chain torsion angles (i.e., α in

Eq. 3), using the updated node and edge representations from Cryformer. The Structure

Module consists of 7 blocks with shared weights. Two types of attention mechanisms

are used in this module (see Supplementary Information S2.2 and Algorithm S2).

The first one is a self-attention mechanism applied to the node features (similar to the

node attention in Cryformer). Given the constraints from the density map, the attention

is restricted to each node and its k nearest neighbors (rather than all other nodes in AF2).

In addition, the position information between nodes is introduced into the attention

mechanism using 3D-RoPE, ensuring that the attention score incorporates position

information.

The second type of attention is the Invariant Point Attention (IPA) from AF2. It is

conducted on the backbone frames and is invariant under global Euclidean

transformations. Like the first type of attention, the attention is restricted to a node and

its k neighboring nodes (rather than all others in AF2).

Cry-Net will be run iteratively to improve its output. During training, 0-2 rounds of

iterations are performed. Only the backbone frame is iterated. During inference, two

rounds of iterations are performed. The reason for choosing $n=2$ here is to keep a

balance between computational cost and performance. No significant improvement in

the network output was observed when more rounds of iterations are performed.

Finally, all-atom positions for each node are then generated using the predicted

backbone frame, the backbone and side-chain torsion angles, as well as the predicted

amino acid type (the amino acid type with the maximum probability). This calculation

is done using the function frames_and_literature_positions_to_atom14_pos in the script

of AF2.

The predicted all-atom positions are postprocessed to connect the unordered nodes into

chains of amino acid sequences. This is done by using the heuristic algorithm in

ModelAngelo[2]. Intuitively, it connects nodes by minimizing the total length of peptide

bond, based on the fact that the C-N distance in a peptide bond is less than 1.4 Å.

Profile-sequence-based alignments between the predicted sequence profiles (i.e., A in

Eq. 3) and the input sequences are further employed to correct the sequence assignment.

Inspired by AF2, recycling is also used here by replacing the predicted Cα atoms in the

first step by the ones from the postprocessed structure. Three rounds of recycling are

used in this work.

The loss function for Cry-Net. The loss function here can be written as:

$$Loss_2 = L_{\text{multi}} + L_{\text{single}} \tag{4}$$

$$L_{\text{multi}} = L_{\text{C}\alpha} + 1.3L_{\text{FAPE}} + 0.025L_{\text{pFAPE}} + L_{\text{existence}} \tag{5}$$

$$L_{\text{single}} = L_{\text{atom}} + L_{\text{torsion}} + L_{\text{attention}} + 2L_{\text{violation}} + 0.3L_{\text{aa}} + L_{\text{edge}} \tag{6}$$

where the overall $Loss_2$ can be divided into L_{single} (single-step loss) and L_{multi} (multi-step

loss). The single-step loss is the final loss output after passing through 7 structure

modules, while the multi-step loss is calculated 7 times within the 7 structure modules

and averaged. They are described in detail below.

L_{atom} is the all-atom RMSD. It calculates the RMSD loss of all atoms on the main chain

and side chain, which can be written as:

$$L_{\text{atom}} = \frac{1}{r} \sum_{i=1}^{r} \sqrt{\frac{1}{3n_i} \sum_{j=1}^{n_i} \sum_{d=1}^{3} \left(\left[x_{ij}^{pred} \right]_d - \left[x_{ij}^{true} \right]_d \right)^2} \tag{7}$$

where r represents the total number of residues, n_i represents the number of atoms in

the i-th residue, x_{ij} represents the atomic coordinates of the j-th atom in the i-th residue,

and d represents the d-th dimension of the 3D coordinates.

L_{torsion} is the L$_2$ distance between the torsion angles of the network output (i.e., α in Eq.

3) and the torsion angles of the deposited model. It is the same as the torsion angle loss

defined in AF2.

$L_{\text{attention}}$ is the classification loss when the nodes attend to the amino acids in the

sequence. The calculation of this loss is the focal loss[56]. The purpose of this loss is to

ensure that each node can correctly match each amino acid in the sequence.

$L_{\text{violation}}$ penalizes unreasonable bond angles and bond lengths in the model. It imposes

certain constraints on the model's output to ensure that the model's output has ideal

bond angles and lengths. The definition of this loss is the same as AF2.

L_{aa} represents the amino acid classification loss. This loss calculates the focal loss by

comparing the twenty-dimensional amino acid probability vector (i.e., A in Eq. 3) and

the one-hot vector corresponding to the amino acid identity in the deposited structure.

The main purpose of this loss is to assign an amino acid identity to each node.

L_{edge} represents the edge classification loss. The edge classification is based on whether

there is a connection between two nodes in the sequence. If there is a connection, we

want them to be classified as neighbors. Specifically, this loss calculates the focal loss
between E in Eq. 3 and the classification corresponding to the edge.

$L_{C\alpha}$ is only the RMSD loss of Cα atoms. Its definition is similar to the all-atom RMSD
(i.e., $n_i=1$ in Eq. 7).

L_{FAPE} comes from AF2, which plays a role in updating the backbone frame. It can be
written as:

683
$$d_{ij} = \sqrt{\left\| T_i^{-1} \circ \vec{t}_j - (T_i^{True})^{-1} \circ \vec{t}_j^{\,true} \right\|^2 + \varepsilon} \tag{8}$$

684
$$L_{FAPE} = \frac{1}{Z} \underset{\substack{i \in \{frames\} \\ j \in \{atoms\}}}{mean} (\min(d_{clamp}, d_{ij})) \tag{9}$$

where T_i represents the i-th backbone frame (i.e., T in Eq. 3). t_j represents the
coordinates of the j-th Cα atom. Both d_{clamp} and Z are taken as 10 Å here.

L_{pFAPE} is a simple regression loss. It calculates the mean squared error (MSE) loss
between the predicted FAPE loss for each residue (i.e., P in Eq. 3) and the actual FAPE
loss (i.e., Eq. 9). It is worth noting that in the post-processing, P will be normalized to
a confidence score between 0 and 100 as the final confidence score.

$L_{existence}$ represents the residue existence loss. Each residue can be classified into two
classes: artificially added (see Supplementary Information S2.4) and naturally
occurring. This loss calculates the focal loss between M in Eq. 3 and the corresponding
one-hot vector of the residue class.

Data and software availability

697 The CryFold package is available at https://yanglab.qd.sdu.edu.cn/CryFold/ and
698 https://github.com/SBQ-1999/CryFold/

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Supplementary Information

S1. Evaluation metrics

We used the same set of evaluation metrics defined by ModelAngelo[1], including
backbone recall, backbone precision, backbone RMSD, Cα RMSD, amino acid
accuracy, and *completeness*.

● *Backbone recall* is the fraction of deposited residues (represented by Cα atoms) that
have a predicted residue (represented by Cα atom) within 3 Å.

● *Backbone precision* is the fraction of predicted residues (represented by Cα atoms)
that have a deposited residue (represented by Cα atom) within 3 Å.

The remaining subsequent metrics involve the matching between deposited residues
and predicted residues, and only consider the deposited residues that have a predicted
residue within 3 Å. We first calculate the distances between the Cα atoms in predicted
structure and the Cα atoms in deposited structure. The Hungarian Matching Algorithm[2]
is then used to match the predicted residues with the deposited residues such that the
total distance is minimized. The metrics can be defined based on the matched residue
pairs.

● *Cα RMSD* is the root-mean-square deviation (RMSD) between the Cα atoms of the
matched residue pairs.

● *Backbone RMSD* is similar to the former but includes all four main-chain atoms
(Cα, C, O, and N).

● *Amino acid accuracy* is the fraction of residue pairs that share identical amino acid
types (i.e., p/m) .

● *Completeness* is the fraction of all deposited residues (including those unmatched
residues) that have a matched predicted residue with the same amino acid identity
(i.e., p/n). It is worth noting that *Completeness ≈ Backbone recall × Amino acid*
accuracy.

Where p represents the number of matched residues that have the same amino acid
identity, m represents the total number of matched residues, and n represents the total
number of residues in the deposited structure.

S2 Architectural details

S2.1 U-Net

The encoder of the U-Net [3] architecture adopts a bottleneck structure [4], which is the same as the CNN module of Cry-Net. The decoder uses the Res2Net architecture [5, 6], as shown in Figure S5. The use of bottleneck for downsampling aims to preserve as much spatial information as possible, while the use of Res2net for upsampling aims to extract as much semantic information as possible. The spatial information and semantic information are then combined to predict the probability map of Cα atoms.

S2.2 Sequence attention and IPA

The Sequence Attention and IPA modules are only briefly mentioned in the main text. In this section, they will be presented in the form of pseudocode.

Algorithm S1: Sequence attention
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1 **def** Seq-attention($\{s_i\}, \{e_j\}, N_{head} = 8, c = 48$):

    // Input projections

2    $s_i \leftarrow \text{LayerNorm}(s_i)$;

3    $q_i^h = \text{LinearNoBias}(s_i)$ $q_i^h \in \mathbb{R}^c, h \in \{1, ..., N_{head}\}$;

4    $k_j^h, v_j^h = \text{LinearNoBias}(e_j)$ $k_j^h, v_j^h \in \mathbb{R}^c, h \in \{1, ..., N_{head}\}$;

5    $g_i^h = \text{sigmoid}(\text{Linear}(s_i))$ $g_i^h \in \mathbb{R}^c$;

    // Cross attention

6    $a_{ij}^h = \text{softmax}_j \left(\frac{1}{\sqrt{c}} q_i^{h\top} k_j^h \right)$;

7    $o_i^h = g_i^h \odot \sum_j a_{ij}^h v_j^h$;

    // Output projections

8    $\widetilde{s}_i = \text{Linear}(\text{concat}_h(o_i^h))$;

9 **return** $\{\widetilde{s}_i\}$

In this algorithm, the input s_i represents the node representation of the *i*-th node, and the input e_j represents the ESM-2 [7] embedding representation of the *j*-th amino acid in the sequence. The output $\tilde{s}_i$ is the updated node representation of the *i*-th node.

Algorithm S2: Local invariant point attention with rope
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def IPA($\{s_j\}, \{z_{ij}\}, \{T_j\}, \{x_j\}, N_{head} = 10, c = 48, N_{query\ points} = 4, N_{point\ values} = 8$):

$q_j^h, k_j^h, v_j^h = \text{LinearNoBias}(s_j)$ $q_i^h, k_j^h, v_j^h \in \mathbb{R}^c, h \in \{1, ..., N_{head}\}$;

$\vec{q}_j^{hp}, \vec{k}_j^{hp} = \text{LinearNoBias}(s_j)$ $\vec{q}_j^{hp}, \vec{k}_j^{hp} \in \mathbb{R}^3, p \in \{1, ..., N_{\text{query points}}\}$;

$\vec{v}_j^{hp} = \text{LinearNoBias}(s_j)$ $\vec{v}_j^{hp} \in \mathbb{R}^3, p \in \{1, ..., N_{\text{point values}}\}$;

$b_{ij}^h = \text{LinearNoBias}(z_{ij})$;

$w_C = 0.1\sqrt{\frac{2}{N_{\text{query points}}}}$;

$w_L = \sqrt{\frac{1}{3}}$;

$\widetilde{q}_j^h, \widetilde{k}_j^h = \text{Rope}(q_j^h, k_j^h, x_j)$;

$a_{ij}^h = \underset{1 \leqslant i \leqslant k}{softmax}\ w_L \left(\frac{1}{\sqrt{c}} \widetilde{q}_j^{h\top} \widetilde{k}_{j_i}^h + b_{ij}^h \right) - \frac{\gamma^h w_C}{2} \sum_p \left\| T_j \circ \vec{q}_j^{hp} - T_{j_i} \circ \vec{k}_{j_i}^{hp} \right\|^2$;

$\widetilde{o}_j^h = \sum_i a_{ij}^h z_{ij}$;

$o_j^h = \sum_i a_{ij}^h v_{j_i}^h$;

$\vec{o}_j^{hp} = T_j^{-1} \sum_i a_{ij}^h (T_{j_i} \circ \vec{v}_{j_i}^{hp})$;

$\widetilde{s}_j = \text{Linear}(\text{concat}(\widetilde{o}_j^h, o_j^h, \vec{o}_j^{hp}, \left\| \vec{o}_j^{hp} \right\|))$;

return $\{\widetilde{s}_j\}$

In this algorithm, the input s_j represents the node representation of the j-th node, z_{ij}
represents the edge representation between the j-th node and its i-th neighbor, T_j
represents the backbone frame of the j-th node, and x_j represents the position (i.e., the
coordinates of the Cα atom) of the j-th node. The output $\tilde{s}_j$ is the updated node
representation of the j-th node. The highlighted text here outlines the main differences
between the IPA module in this work and the one in AF2 [8]: The difference in the
coefficients. The attention used here is a local form and includes positional encoding
(3D-RoPE).

S2.3 3D Rotary Position Embedding (3D-RoPE)

3D-RoPE is used in the node-attention and IPA modules of the Cry-Net. To describe
this in detail, let's first introduce the 1D rotary position encoding [9]:
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$$R_m = \begin{pmatrix} \cos m\theta_0 & -\sin m\theta_0 & 0 & 0 & ... & 0 & 0 \\ \sin m\theta_0 & \cos m\theta_0 & 0 & 0 & ... & 0 & 0 \\ 0 & 0 & \cos m\theta_1 & -\sin m\theta_1 & ... & 0 & 0 \\ 0 & 0 & \sin m\theta_1 & \cos m\theta_1 & ... & 0 & 0 \\ ... & ... & ... & ... & ... & ... & ... \\ 0 & 0 & 0 & 0 & ... & \cos m\theta_{d/2-1} & -\sin m\theta_{d/2-1} \\ 0 & 0 & 0 & 0 & ... & \sin m\theta_{d/2-1} & \cos m\theta_{d/2-1} \end{pmatrix} \tag{S1}$$

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$$\tilde{q}_m^T \tilde{k}_n = (R_m q_m)^T (R_n k_n) = q_m^T (R_m^T R_n) k_n = q_m^T R_{m-n} k_n \tag{S2}$$

910 where q and k represent the query vector and the key vector used in the attention
911 mechanism, respectively. They are both d-dimensional vectors. The above formula is
912 to introduce the positions m and n of the sequence into the attention mechanism using
913 the multiplicative position encoding. We extend this process to 3D space:

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$$R_{(x,y,z)} = \begin{pmatrix} R_x & 0 & 0 \\ 0 & R_y & 0 \\ 0 & 0 & R_z \end{pmatrix} \tag{S3}$$

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$$\tilde{q}_m^T \tilde{k}_n = (R_{(x_m, y_m, z_m)} q_m)^T (R_{(x_n, y_n, z_n)} k_n) = q_m^T R_{(x_m - x_n, y_m - y_n, z_m - z_n)} k_n \tag{S4}$$

Here, we assume that the dimensions of the query and key vectors are both multiples
of three, and (x, y, z) represents the position of each node (i.e., the coordinates of the
Cα atoms). The 3D position encoding has richer connotations compared to the 1D
position encoding, as it not only considers the distance information between nodes but
also the directional information between nodes. Furthermore, this attention mechanism
can actually be applied along the three coordinate axes:

$$q_m = \begin{pmatrix} q_m^x \\ q_m^y \\ q_m^z \end{pmatrix}, k_n = \begin{pmatrix} k_n^x \\ k_n^y \\ k_n^z \end{pmatrix} \tag{S5}$$

$$\tilde{q}_m^T \tilde{k}_n = q_m^T R_{(x_m-x_n, y_m-y_n, z_m-z_n)} k_n$$
$$= q_m^{x\,T} R_{x_m-x_n} k_n^x + q_m^{y\,T} R_{y_m-y_n} k_n^y + q_m^{z\,T} R_{z_m-z_n} k_n^z \tag{S6}$$

The first one-third of the dimensions in the query and key vectors represent the
information along the *x*-axis, the middle one-third represent the information along the
y-axis, and the last one-third represent the information along the *z*-axis. From this
perspective, the 3D-RoPE attention can be seen as the sum of three 1D-RoPE attentions
in different directions (*x*, *y*, *z*). The 3D-RoPE attention is realized by the inner product
calculation. In the 3D world, the inner product has a clear physical meaning, such as
representing the work done:

$$W = \vec{F} \bullet \vec{s} = (\vec{F_x} + \vec{F_y} + \vec{F_z}) \bullet (\vec{s_x} + \vec{s_y} + \vec{s_z})$$
$$= \vec{F_x} \bullet \vec{s_x} + \vec{F_y} \bullet \vec{s_y} + \vec{F_z} \bullet \vec{s_z} = W_x + W_y + W_z \tag{S7}$$

The total work W is the inner product of the force $\vec{F}$ and the displacement $\vec{s}$. From
another perspective, the total work W can be decomposed into the work done along the
three coordinate axes. This has an analogy with the 3D-RoPE attention.

If we interpret the 3D-RoPE attention as the interaction between residues, then based
on the long-term decay property of the 1D-RoPE[9], the 3D-RoPE, which can be seen as
the sum of three 1D RoPE, will also exhibit long-range decay. In this way, the 3D
attention between residues will weaken as the distance increases, which nicely captures
the mechanism of the inter-residue interactions.

S2.4 Cry-Net training
For the convenience of narration, we restate the Eq. 3 from the main text here. The input
and output of Cry-Net in each the *n*-th iteration are defined by the following equation:
$$g\left(T^{(n)}, V, S\right) = (T^{(n+1)}, \alpha^{(n+1)}, A^{(n+1)}, P^{(n+1)}, E^{(n+1)}, M^{(n+1)})$$

The frame T can be defined as (R, t), where $R \in \tilde{}^{r \times 3 \times 3}$ and $t \in \tilde{}^{r \times 3 \times 1}$. At the beginning of
the training, $t^{(0)}$ is initialized as the Cα atomic coordinates of the training data after
adding Gaussian noise $e_i \sim N\left(0, \frac{1}{\sqrt{3}}\right)$ along each dimension, and the rotation matrix $R^{(0)}$
is randomly initialized [1].

During the training process, a Cα atom is randomly selected from each PDB [10] data
sample, and the 200 nearest residues in the spatial region are cropped. Inspired by
ModelAngelo, 10% of the residues are randomly replaced with peptide chains of length
2-5. The purpose of this is to simulate the potential redundancy in the Cα atom

coordinates output by U-Net, i.e., there may be no corresponding residue with deposited
structure around the output nodes. In this case, the output M of the network is used to
determine whether the nodes output by U-Net are redundant or not.

Fig. S1. The distribution of confidence scores of the CryFold models for the 177
maps.

TPs: true positives, FPs: false positives. Note that the FPs are possible to be
misjudgments, as illustrated by the example in Figure 3f.

Fig. S2. The impact of map masking.

(a) Head-to-head comparison of the model backbone precision. (b) Head-to-head
comparison of the model completeness. (c)/(d) Head-to-head comparison of the model
backbone precision/completeness between CryFold and ModelAngelo by inputting
masked maps. (e) Appropriate masking can screen out regions unrelated to the
deposited structure protein. The gray surface is the density map. The green cartoon
represents the deposited structure. The purple/blue cartoon is the CryFold model
constructed using the masked/raw map. (f) Inappropriate masking can lead to incorrect
atomic model. The coloring scheme is the same as in (e).

Fig. S3. Computational efficiency of CryFold.

(a) Running time for building 177 maps using CryFold and ModelAngelo. (b) Running time for an example protein (EMD-29327, PDB ID: 8FNV) under different memory configurations (15GB, 19GB, 24GB). To eliminate the effects of randomness, each configuration was run six times.

Fig. S4. Modelling evaluation by the CryFold and ModelAngelo in low-resolution regions.

Six protein models of the mitochondrial respirasome II2-III$_2$-IV2 [11] are compared and shown with their corresponding densities. Termini are indicated for each protein.

985　**Fig. S5. The curves of loss function under four different configurations**.

Fig. S6. Architecture of U-net.

(a) Encoder module and the downsampling module are integrated together, and a
bottleneck architecture[4] is adopted. (b) Decoder module adopts the Res2Net
architecture [5, 6].

Fig. S7. Architectural details of the encoder network.

(a) Cryformer module. (b) node attention layer. (c) edge attention layer.

Fig. S8. Architectural details of the decoder network Structure Module.

This module is similar to the structure module in AF2 [8]. The difference is that the input

here includes additional node position information (i.e., the Cα positions). The updated

node representations are passed through separate MLPs to output *T, α, P, M* in Eq. 3.

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Fig. S9. Relationship between node attention and edge attention.

A graph (a) can be converted into a line graph (b), and vice versa. According to the
Whitney graph isomorphism theorem, except for a very small number of special cases,
the line graph uniquely determines the original graph. These two types of graphs have
a certain duality. The edge attention to the edge *ij* of the graph on the left is equivalent
to the node-attention to the *ij* node of the line graph on the right.

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Fig. S10. Detailed information for the Cryformer Module.

The original node representation and the updated node representation are concatenated
and passed through a separate MLP to predict the probability vector over the 20 types
of amino acids for each node (i.e., *A* in Eq. 3). The original edge representation and the
updated edge representation are concatenated and passed through another separate MLP
to predict the edge connectivity (i.e., *E* in Eq. 3).

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Supplementary References

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