Patches: A Representation Learning framework for Decoding Shared and Condition-Specific Transcriptional Programs in Wound Healing

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Abstract

Single-cell genomics enables the study of cell states and cell state transitions across biological conditions like aging, drug treatment, or injury. However, existing computational methods often struggle to simultaneously disentangle shared and condition-specific transcriptional patterns, particularly in experimental designs with missing data, unmatched cell populations, or complex attribute combinations. To address these challenges, *Patches* identifies universal transcriptomic features alongside condition-dependent variations in scRNA-seq data. Using conditional subspace learning, Patches enables robust integration, cross-condition prediction, and biologically interpretable representations of gene expression. Unlike prior methods, Patches excels in experimental designs with multiple attributes, such as age, treatment, and temporal dynamics, distinguishing general cellular mechanisms from condition-dependent changes. We applied *Patches* to both simulated data and real transcriptomic datasets from skin injury models, focusing on the effects of aging and drug treatment. *Patches* revealed shared wound healing patterns and condition-specific changes in cell behavior and extracellular matrix remodeling. These insights deepen our understanding of tissue repair and can identify potential biomarkers for therapeutic interventions, particularly in contexts where the experimental design is complicated by missing or difficult-to-collect data.

Introduction

All living organisms have the remarkable ability to repair themselves in response to injury. Healing efficiently and successfully is essential to preserving the integrity of tissues and organs. A central biological process, wound healing involves the complex, coordinated actions of numerous intracellular and intercellular components. These include the activation and regulation of different cell types, such as fibroblasts, keratinocytes, and immune cells, as well as the interplay of signaling molecules[1, 2, 3]. Single-cell RNA sequencing (scRNA-seq) provides a detailed view of the transcriptional dynamics during tissue repair, particularly in murine skin wounds [4, 5, 6, 7, 8]. These recent studies have highlighted the heterogeneity of cell populations involved in the process, identifying distinct wound healing processes linked to physiological changes like aging [4], and demonstrating unique contributions of epithelial [5],[9], mesenchymal [6, 7], and immune cells [8] at the injury site.

However, despite advances in data collection, much of the current work focuses on selecting individual genes based on prior characterization, limiting our ability to uncover novel regulatory programs. As a result, a systematic understanding of the molecular changes of diverse skin cell lineages during the healing process remains incomplete [10, 11]. This gap highlights the need for new computational tools capable of de-novo discovery of cell-specific gene programs from complex scRNA-seq wound datasets, enabling an unbiased exploration of the molecular mechanisms underlying repair mechanisms.

Traditionally, scRNA-seq analysis methods have focused on static snapshots of cellular states, which do not adequately capture the dynamic nature of injury response and result in missing or incomplete data. Indeed, the biological complexity

and physiological variability of skin tissue repair poses unique challenges[11, 12]. High dropout rates in scRNA-seq, coupled with destructive experimental designs, result in incomplete data and biases that obscure transcriptional dynamics across conditions and timepoints. Furthermore, conditions such as aging, drug treatment, or disease can alter these trajectories in ways that are not fully understood. Many gene programs are shared across conditions, making it statistically challenging to disentangle common mechanisms from those that are condition-specific. Addressing these challenges requires new models capable of integrating longitudinal data, accurately capturing shared patterns, and isolating differences unique to each condition.

A wide range of statistical machine learning methods have been developed to annotate [13, 14, 15], integrate [13, 14, 16, 17], and interpret [18, 19, 20] scRNA-seq data. These approaches differ in their statistical focus: a) whether they are generative on non-generative, b) whether they can capture shared versus condition-specific gene expression patterns in multi-condition datasets, and c) whether they are interpretable. In particular, non-generative approaches have provided pipelines for unsupervised clustering [13, 14, 15], uncovering gene expression programs through matrix factorization techniques [18, 19] and understanding cell-cell interaction [21, 22, 23]. Generative models use probabilistic frameworks to represent scRNA-seq data as nonlinear transformations of samples from a lower-dimensional latent space. Unlike non-generative models, the latent representations learnt by generative models have proven particularly useful in modeling complex biological and technical variation [17, 24, 25, 26, 27]. Additionally, generative models have also been used to integrate data from multiple modalities [28, 29] or conditions [26, 30, 31, 32]. In doing so, these tools focus on either modeling shared signals across all conditions [17, 25, 27] or on modeling conditional information – discrete (e.g., cell type labels [26, 30, 31, 33]) or continuous (e.g., for visualization [24, 32]). However, these methods do not quantify the trade-off between the information shared across all conditions and that is specific to each individual condition. Only a few studies have addressed this challenge [34, 35, 36, 37] particularly when integrating multi-modal data, such as morphology and gene expression [34, 35] or gene expression and chromatin accessibility [36, 37]. These approaches generally require matched cells across modalities, which limits their applicability to destructive and complex experimental designs where the focus is on capturing temporal variation. Still, generative models, with their capacity to capture nonlinear relationships, hold significant promise for unraveling the intricate dynamics of wound healing. However, the expressivity of these models usually comes at the expense of interpretability offered by non-generative approaches. Recent work has focused on either altering the generative process by incorporating linearity to enable interpretability [20] or employing linear models in the learned representation space [38]. Specifically, the former approach can be used in tandem with conditional generative model formulations to enable interpretability in complex contexts. Taken together, these considerations highlight the need for interpretable generative models specifically designed to decouple shared and condition-specific effects, enabling the study of intricate processes such as wound healing.

To this end, we introduce *Patches*, a deep representation learning framework designed to model gene expression data from complex, multi-condition experimental designs. Similar to existing generative models such as scVI [17, 25, 27], *Patches* maps a cell's gene expression profile to a low-dimensional latent representation via learnable, nonlinear transformations. However, unlike these approaches, *Patches* leverages conditional subspace learning [39, 40] to disentangle shared and condition-specific transcriptomic patterns. This enables the identification of both common and distinct gene expression features across conditions such as age, treatment type, or temporal profile. This flexible latent space, also allows the generation of transcriptomic data for previously unseen condition combinations by simply modifying the condition labels during generation.

By applying *Patches* to both simulated and real datasets, we show it can uncover new insights into the molecular dynamics of wound repair. Specifically, we apply *Patches* to single-cell data from skin injury experiments, demonstrating its ability to capture both universal and condition-dependent dynamics in the contexts of aging and drug treatment. In aging, *Patches* identifies subtle changes in immune cell behavior and extracellular matrix (ECM) remodeling that distinguish young and aged responses to injury. Similarly, in a drug treatment context, *Patches* captures transcriptional changes associated with wound healing dynamics under verteporfin treatment, revealing potential pathways for therapeutic intervention. These results highlight the potential of *Patches* to provide insights into complex cellular processes and inform experimental designs in challenging multi-condition settings.

Results

Patches

Overview. *Patches* takes as input a collection of observations or gene expression profiles obtained from multiple conditions (Fig. 1A) referred to as 'groups' – for example, age, treatment or injury stage. Each group is characterized by a unique set of categories or attributes – for example, 'young' or 'old' represent the attributes of the group 'age'. Extending

existing variational autoencoder (VAE) architectures [17] by incorporating concepts from multi-modal learning [41] and information theory [39, 40], *Patches* models a gene expression profile $\mathbf{x}_n$ as a sample from a distribution conditional on a latent representation ρ_n – the cell's 'latent identity'. The latent identity ρ_n is decomposed into two components: $\mathbf{z}_n$ and $\mathbf{w}_n$. This decomposition reflects the interaction between the cell's intrinsic state and the experimental conditions or attributes under which it was observed. The shared latent variable $\mathbf{z}_n$ captures condition-independent features of the cell, remaining invariant across different combinations of experimental attributes. Conversely, $\mathbf{w_n}$ encodes group and attribute-specific information that varies according to experimental factors such as age, treatment, or temporal stage (Fig. 1B). This positions *Patches* as a middle ground between unsupervised methods like [17], which focus on learning shared latent spaces, and supervised approaches like [26], which emphasize condition-specific representations. In contrast to these methods, *Patches* jointly learns both shared (common) and condition-specific embeddings (Fig. 1C). *Patches* also enforces information-theoretic constraints [39, 40] to ensure that the shared embeddings remain disentangled from condition-specific attributes. In detail, the group specific latent representations $\mathbf{w}_n$ are obtained by concatenating latent representations corresponding to individual group combinations $\mathbf{y}_n = (\zeta_n^1, \zeta_n^2, \dots \zeta_n^C)$ (Fig. 2A). Here, C denotes the number of groups represented in the experimental design, for example $C = 3$ when the groups considered are the cell type identity, the age of the sample – whether it is from an old or young mouse – and the wound healing stage (*Methods*). Following previous work, the gene expression x_{ng} of a gene g and cell n is modeled using a zero-inflated negative binomial (ZINB) $p(x_{ng} \mid \rho_n, \ell_n)$ [17, 42, 43, 44]. Here, ℓ_n is a cell-specific library size factor and the parameter ρ_n is drawn from a multivariate normal distribution with mean and covariance parameterized by a non-linear function of the latent identities $\mathbf{z}_n$ and $\mathbf{w}_n$ (Fig. 2A). Finally, while *Patches* inherits the inherent opacity of VAE-based models in its learned representations, it addresses this limitation through an interpretable decoder design. By utilizing a single linear layer [20], *Patches* learns interpretable coefficients that connect original data features, such as gene expression values, to condition-specific attributes. These interpretable coefficients provide a direct explanation of how specific genes contribute to observed differences across experimental conditions (*Methods*). This dual capability of disentangling shared and condition-specific signals while offering interpretable insights makes *Patches* a robust and versatile tool for analyzing complex scRNA-seq datasets.

Illustrative examples

As proof of concept, we applied *Patches* to two synthetic datasets, comparing its performance with other generative modeling approaches and highlighting its capacity to separate universal patterns from those tied to specific experimental conditions (*Methods*).

Synthetic attribute separation model. We first simulated a toy dataset of $n = 8,000$ data points, each represented by a G-dimensional feature vector $x_n \in \mathbb{R}^G$, with $G = 30$ (Fig. 2B). The dataset was designed to mimic an experimental setup with two condition groups, ζ^1 and ζ^2, each defined by two attributes. The labels, $\mathbf{y}_n = [\zeta_n^1, \zeta_n^2]$, were obtained by concatenating the one-hot encoded attributes of each group, resulting in four possible configurations: $[1, 0, 1, 0]$, $[1, 0, 0, 1]$, $[0, 1, 1, 0]$, and $[0, 1, 0, 1]$ (*Methods*). We simulated $2,000$ points from each configuration as follows. We sampled latent representations $(\mathbf{z}_n, \mathbf{w}_n^1, \mathbf{w}_n^2)$ consisting of three concatenated vectors: a shared component $\mathbf{z}_n \in \mathbb{R}^{10}$ and two condition-specific components, $\mathbf{w}_n^1 \in \mathbb{R}^{10}$ and $\mathbf{w}_n^2 \in \mathbb{R}^{10}$. The shared component $\mathbf{z}_n$ was sampled from a multivariate normal distribution with mean $\mathbf{0}_{10}$ and covariance $0.5\,\mathbb{I}_{10}$, where $\mathbf{b}_{10}$ denotes a vector of size 10 with entries all equal to a constant value b. The conditional latent component $\mathbf{w}_n^1$ was drawn from a multivariate normal distribution with covariance $0.5\,\mathbb{I}_{10}$ and mean $\mathbf{1.15}_{10}$ (resp. $\mathbf{0}_{10}$) for $\zeta^1 = [0, 1]$ (resp. $\zeta^1 = [1, 0]$). Similarly, $\mathbf{w}_n^2$ was drawn conditionally from a multivariate normal distribution with covariance $0.5\,\mathbb{I}_{10}$ and mean $-\mathbf{1.15}_{10}$ (resp. $\mathbf{0}_{10}$) for $\zeta^2 = [0, 1]$ (resp. $\zeta^2 = [1, 0]$). Then, the observations $\mathbf{x}_n$ were conditionally sampled given latent representations $(\mathbf{z}_n, \mathbf{w}_n^1, \mathbf{w}_n^2)$ from a multivariate normal distribution with mean $A\,[\mathbf{z}_n, \mathbf{w}_n^1, \mathbf{w}_n^2]$ and covariance $0.5\,\mathbb{I}_{30}$, with A the identity matrix, corresponding to a linear, non-compressive decoder.

We found that *Patches* correctly decomposed each simulated synthetic profile into attribute specific components and a shared component (Fig. 2B). Specifically, each data point was projected together with points that were originally clustered in the conditional space (left) and onto a shared cluster in the condition-agnostic or common space (right). In this synthetic scenario, scANVI [26] captures only attribute-specific representations, while scVI [17] biases these representations toward a shared component, failing to accurately model either joint or common behavior. In contrast, Patches effectively disentangles shared and condition-specific variation.

Supervised Swiss roll. We also applied *Patches* to a popular machine learning toy-data set, the *Swiss roll* [45]. This synthetic dataset is often used to illustrate nonlinear structures in high-dimensional data: it represents a 2D plane curved into a 3D spiral, where local relationships between points are preserved, but global distances can be misleading due to the nonlinearity of the embedding (Fig. 2C). VAEs have been previously used on the Swiss roll to show their capacity in learning nonlinear data, 'unrolling' the Swiss roll into flattened latent representations [39]. We generated $n = 10,000$

points in the shape of a Swiss roll (each point has coordinate features X, Y, Z), using an existing implementation [45, 46]. We sliced the Swiss roll structure along the Y-axis into two equal parts at $Y = 10$, and labeled the points based on their slice of origin. The resulting supervised Swiss roll dataset contained a single binary condition ($C = 1, K = 2$) representing the two slices. We trained *Patches* on this labeled dataset using latent dimensions $d_{\mathbf{z}} = 2$ and $d_{w^k} = 1$ (*Methods*), where each latent dimension w^k corresponds to one of the slices. We analyzed two configurations of *Patches*: one with a nonlinear decoder and another with a linear decoder.

As expected, the nonlinear decoder outperformed the linear decoder in reconstruction performance, successfully capturing the full surface of the Swiss roll (Fig. 2C). In contrast, the linear decoder struggled to reconstruct large portions of the data (Fig. 2D). However, the linear decoder compensated for its limited expressivity with greater interpretability. Unlike the black-box nature of the nonlinear decoder, the linear decoder's weights provide insights into the relationship between the original data features and their labels (Fig. 2E). Specifically, the decoder coefficients for the latent dimensions w^1 and w^2 clearly distinguish whether a slice is located in the front or back of the Swiss roll based on the Y-coordinate, when viewed from a fixed angle. Further, the model did not wrongly associate any of the other dimensions (X, Z) with labels (Fig. 2E). Notably, both the linear and non-linear configurations of *Patches* learned latent representations that reflect the underlying properties of the data-generating mechanism (Fig. 2F,G). Particularly, the shared latent components captured the global structure of the Swiss roll (Fig.2F,G; left panels), while the condition-specific components accurately represent the binary Y-conditions (Fig.2F,G; middle panels). Finally, the information-theoretic constraint encouraged the latent spaces to remain disjoint, ensuring a clear separation of shared and condition-specific variations (Fig.2F,G; right panels).

Taken together, these results suggest that both versions of Patches learn informative latent representations that disentangle conditional variation from common signals. However, their distinct strengths make them suitable for different tasks. The nonlinear decoder's reconstruction performance makes it a good candidate for applications like transfer learning or imputation. These tasks require inferring missing data or generating synthetic data for scenarios where collection is difficult. In contrast, the linear decoder offers greater interpretability. Hence, it is better suited for hypothesis generation, where understanding and acting on the signal is key. For example, it can identify gene programs that are condition-agnostic (e.g., metabolic processes essential for normal function) or condition-specific (e.g., wound-healing pathways activated in response to injury or hypoxia-induced signaling during low oxygen conditions).

Patches learns shared and attribute-specific representations in wound healing studies

Next, we demonstrated the performance of *Patches* on two datasets with multi-group experimental designs. The first dataset investigates the impact of aging on wound healing dynamics [4], while the second explores the effects of drug treatment [47]. These datasets included labels capturing contextual conditions, such as experimental timepoints or treatments, as well as intrinsic identities, such as cell types.

Aging. We first applied *Patches* to the wound healing dataset consisting of $26,966$ cells collected across three timepoints (0DPW, 4DPW, 7DPW) from young (7-week-old) and aged (88-week-old) mice [4]. In addition to gene expression profiles, the model was provided conditional information on time post-injury, age, and cell type annotations. *Patches* learned both common (z) and condition-specific (w) representations for each cell (Fig. 3A). In the conditional latent space, UMAP visualizations revealed distinct clusters corresponding to each combination of attributes (e.g., 4DPW young fibroblasts), consistent with the behavior observed in simulations. The common representations (z) effectively integrated data across conditions, aligning cells from different groups, underlying gene expression programs which are common to the wound healing process regardless of age. We further visualized the first two principal components or PCs obtained from the latent gene expression profiles corresponding to shared and condition specific signals, respectively (Fig. 3A, last column). This confirmed that attribute separation occurred exclusively in the conditional latent space.

Drug treatment. To further evaluate the performance of *Patches*, we analyzed a dataset examining the effect of drug treatment on wound healing [47]. This dataset posed a specific challenge common to many multi-conditional datasets: a significant imbalance in the number of cells per condition (cell type, wound healing stage, drug treatment). After preprocessing, the dataset consisted of $2,284$ cells collected at three timepoints (POD7, POD14, POD30) from either PBS (control) or verteporfin treated mice. As before, for each cell, the model was provided with the time post-injury, treatment, and cell type labels alongside the corresponding gene expression profiles. Despite the low observation count, *Patches* successfully learned common (z) and condition-specific (w) representations for each observation (Fig. 3B). Unlike in the aging dataset, the low observation count resulted in more sparsely populated clusters in the conditional space, each corresponding to a unique combination of attributes (e.g., POD7 verteporfin treated fibroblasts). Notably, as with similar methods [17, 20], the low dataset size required an increase in the number of training iterations to achieve convergence, as parameter updates depend on dataset size. This observation aligns with previous studies tackling low-sample scenarios (*Methods*).

Quantifying the attribute-specific representations learned by *Patches*

In both the aging study [4] and the drug treatment study [47], *Patches* learned latent representations that could be qualitatively associated with attributes through UMAP visualizations (Fig. 3). However, visualization alone does not provide a quantitative measure of performance, nor does it explain how these representations reflect the underlying biological attributes. To address this, we further investigated the latent representations learned by *Patches*. Motivated by the results from the simulated Swiss roll example, we evaluated the representations in both linear and nonlinear scenarios. Specifically, we examined *Patches*'s interpretability module and quantified the latent space separability between attribute-specific representations. These were benchmarked against latent spaces learned by previously proposed generative models.

***Patches* recovers cell type markers.** To test its capacity for extracting interpretable signals, we applied *Patches* with a linear decoder to real scRNA-seq wound healing datasets. [4, 47]. Alongside gene expression data, we incorporated auxiliary annotations, including time and age labels for the aging dataset, time and treatment labels for the drug treatment dataset, and cell type information. After model training, we derived attribute-specific scores for each gene using the learned coefficients from the linear decoder (*Methods*).

We analyzed cell type-specific scores, focusing on the top 20 genes for the three predominant cell types in each dataset. In the aging dataset, these included fibroblasts, keratinocytes, and macrophages (Fig. 4A), while in the drug treatment dataset, they comprised macrophages, fibroblasts, and T cells (Fig. 4B). *Patches* accurately linked key marker genes to their respective cell types. For instance, fibroblast markers such as *Dcn, Col1a1, Col1a2,* and *Col3a1* were identified (Fig. 4A,B; top row), along with keratinocyte markers, including *Krt14* and related *Krt* genes (Fig.4A, middle row). For macrophages, *Lyz2* and *Cd14* were recovered (Fig.4A, bottom row; Fig.4B, middle row), while T cell markers included *Nkg7* and *Ccl5* (Fig. 4B, bottom row). Interestingly, *Patches* also identified genes not explicitly used during annotation. For example, *AW112010*, a long non-coding RNA previously shown to promote the differentiation of inflammatory T cells [48], achieved the highest specificity score for T cells (Fig. 4B, bottom row). This highlights *Patches*'s ability to reveal biologically meaningful signals beyond known markers.

Attribute-specific representations show clear separation and interpretability. To assess the ability of *Patches* to separate conditional clusters, we compared its learned latent representations with those generated by two widely used generative models: scVI [17] and scANVI [26]. For each condition group across both datasets, we calculated separability scores based on the encoded observations within the latent spaces of each model (Fig. 4C). We considered four metrics: K-nearest neighbor, classification accuracy (KNN), normalized conditional Average Silhouette Width (cASW), K-Means Adjusted Rand Index (K-Means ARI), and K-Means Normalized Mutual Information (K-Means NMI) [49, 45] (*Methods*). A higher KNN score indicates that points with the same attribute are closely positioned in the latent space. Normalized cASW scores reflect cluster compactness and distinctness, with moderate values indicating overlap. K-Means-based metrics convey correspondence between original data attributes and their organization in the latent space. Importantly, as K must match the number of attributes for each condition group (*Methods*), achieving a high score requires exactly matching cluster structures between two clusterings.

For cell type annotations, scVI achieved the highest separability scores among the tested models when evaluated using K-Means-based metrics. This is likely because scVI does not incorporate labels during training, instead prioritizing the largest axis of variation when structuring the latent space. As a result, it preserves global cluster structures related to cell types. On the other hand, *Patches* is designed to arrange the conditional latent representations into clusters which reflect combinations of attributes, rather than preserving the global structure for any specific axis of variation (Fig. 3, second last column). This results in greater variability across scores for K-Means-based metrics (Fig 4C). However, cells of the same type are still situated closely in the conditional latent space of *Patches*. KNN and cASW scores seem to reflect this, as conditional representations of *Patches* achieve scores similar to scVI (Fig. 4C, right panels).

For condition-specific attributes, scVI showed lower separability scores, comparable to the values observed for the common representations of *Patches* (Fig. 4C, left and middle panels). Additionally, common representations always attain the lowest separability scores across comparisons, highlighting the desired mixing behavior for attributes (Fig. 3, second column). In contrast, for scANVI, the KNN and cASW scores indicated that condition-specific labels were positioned closely together in the latent space, resembling the behavior of the conditional representations learned by Patches. (Fig. 4C, left and middle panels). This is expected, because both scANVI and *Patches* have access to condition-specific labels, and are designed to organize their respective latent spaces to maximize separability with respect to combinations of attributes.

Overall, *Patches* effectively models variation across different data attributes. Owing to the additional structuring of its latent space [39] (*Methods*), Patches achieved better separation of latent clusters, leading to higher separability scores.

Patches achieves competitive reconstruction and transfer accuracy in scRNA-seq data

We next assessed the ability of *Patches* to disentangle conditional information while generating realistic gene expression profiles through its decoder. In addition to reconstruction tasks, we tested the model's capacity to 'transfer' gene expression patterns across timepoints, a key challenge in datasets with dynamic conditions.

We split the datasets into training and test subsets and evaluated the reconstruction accuracy across all cells and the three major cell types by proportion. *Patches* achieved reconstruction scores comparable to scVI, which does not incorporate conditional labels, and outperformed scANVI across all comparisons (Fig. 5A). Notably, in the Vu dataset, scANVI performed relatively well for fibroblasts, likely due to their dominance as the majority cell type.

We further tested the model's ability to 'transfer' gene expression patterns across consecutive timepoints. Starting with observations from the first timepoints (0 DPW for Vu, POD7 for Mascharak), we used *Patches* to transfer these expression profiles to the second sets of timepoints (4 DPW for Vu, POD14 for Mascharak). As proportions of cell types are different across groups, we performed the transfers per cell type for the three major cell types in each dataset. The objective was to understand how these observations might appear if collected at the second timepoint. While *Patches* and scANVI provide internal mechanisms to facilitate transfer between conditions, scVI was not originally designed for this purpose. To address this, we introduced an augmented version of scVI with oracle information (denoted as Oracle-scVI, *Benchmarks*). In this setup, scVI was provided with the statistical distance between the source (gene expression from the first timepoint) and the target (gene expression from the subsequent timepoint) in latent space. Although Oracle-scVI introduces bias toward the target condition, it serves as an upper-performance bound for this task. Comparing the three approaches, *Patches* implemented transfer through label change with high accuracy, achieving performance comparable to Oracle-scVI (Fig. 5B). In contrast, scANVI performed poorly across all cell types, with its best performance observed for T cells in the Mascharak dataset.

To quantify how well the models reproduced biological variation, we compared the mean and variance of reconstructed gene log-counts to the original log-counts. Consistent with the reconstruction accuracy results, Patches and scVI effectively recapitulated gene-level variability, outperforming scANVI (Fig. 5C). The weaker performance of scANVI may stem from its reliance on a single one-hot encoded label to represent multiple condition groups, a strategy that does not scale effectively for datasets with many conditions which might combinatorially overlap.

Patches identifies key genes and pathways driving tissue repair and aging dynamics

Next, we explored how the latent representations learned by *Patches* contribute to separating cells according to their attributes. To this end, we first extracted the first PC from both common and conditional latent representations across the wound healing datasets considered. Then, for each gene, we computed alignment scores (R^2) by correlating the obtained PC values with the original transcript counts, which are shown on the Y-axis in Fig. 6, Panel A. Simultaneously, we performed differential gene expression tests using the normalized count matrix, grouping observations by condition-specific attributes (e.g., age and time for the Vu dataset [4]; treatment and time for the Mascharak [47]). The resulting significance scores ($-log10$ adjusted P-values) are plotted on the X-axis). As expected, the common latent representations do not encode condition-specific information, reflected by the lower correlation between alignment scores and differential expression significance, as well as the low separability score (quantified using the Average Silhouette Width).

The scores resulting from the conditional latent representation, can be interpreted in two way.. First, they can be indicative of a direct influence of condition on expression. Namely, if a group-specific change (e.g., age or treatment) directly drives gene expression, we would observe higher R^2 values for the linear fit in the alignment-differential expression plots. This indicates that variations in gene expression align closely with condition-specific latent changes, as observed for aging fibroblasts in the Vu dataset. Second, the scores can be indicative of a nonlinear or indirect relationships. Namely, in cases where values are lower, the condition-specific changes are not directly captured by differential expression analysis. This suggests a more complex, potentially nonlinear relationship between latent representations and expression values.

We found several genes with high alignment scores that were associated with wound healing and aging phenotypes in a cell-type-specific manner. In fibroblasts, key genes such as *Gsn*, *Oxtr*, *Ebf1*, *Il1r2*, and *Gas6* exhibited strong associations with processes central to tissue repair and regeneration. *Gsn* plays a critical role in actin cytoskeletal remodeling, enabling fibroblast migration during wound healing [50]. *Oxtr* is involved in tissue regeneration and homeostasis [51], while *Ebf1* regulates cell differentiation [52], and *Gas6* promotes fibroblast survival and tissue repair via TAM receptor signaling, with a notable role in age-dependent fibrosis [53].

Similarly, aging effects were prominent in keratinocyte populations. Here, the highest-scoring genes included *Krt15*, *Lef1*,

Clec2d, *Sult5a1*, and *Gm47283*. *Krt15*, a marker of keratinocyte stem cells, and *Lef1*, a regulator of the Wnt pathway, suggest impairments in stem cell maintenance and regenerative capacity [54, 55]. *Clec2d* reflects immune modulation and aging dependent inflammation [56], while *Sult5a1* indicates altered metabolic and hormone processing [57]. The uncharacterized *Gm47283* may implicate RNA-based regulatory mechanisms. Together, these findings demonstrate *Patches*'s ability to identify genes linked to critical pathways involved in tissue repair, stem cell exhaustion, immune dysregulation, and age-related metabolic changes across fibroblast and keratinocyte populations.

Finally, we incorporated a linear decoder into *Patches* to derive interpretable contributions of individual genes to the latent representations [20]. Using this computational framework, we analyzed the two major cell types in the Vu dataset — fibroblasts and keratinocytes. Group-conditional scores were computed for each gene, capturing linear relationships between condition specific attributes (e.g., cell type, age, time) and gene expression levels (*Methods*). Genes were ranked by attribute and the top 10% of genes were selected for downstream analyses, including gene ontology (GO) enrichment analyses [58] (Fig. 6). We found gene programs associated with ECM organization were more enriched in fibroblasts rather than in keratinocytes in the aged groups. Conversely, gene programs specific to keratinocytes showed a larger contribution to intermediate filament organization programs, further supporting the fact that aging significantly impacts intermediate filament organization during tissue repair[59].

To assess the impact of modeling choices on gene specific interpretability scores, we examined three variants of the linear decoder making up *Patches*'s interpretability module. In addition to a standard linear decoder architecture [20], we also considered an extension with an explicit intercept term, and a model incorporating both an intercept and an $\mathcal{L}_1$ sparsity penalty on the conditional coefficients (*Methods*; *Interpretability module*). We compared the top 10% of genes from the ranked lists generated by each implementation. Across the three decoder variants, Patches consistently identified top-scoring genes in a cell-type and age-specific manner, highlighting their biological relevance to wound healing and aging processes (Fig. 6C). In fibroblasts, the intersection of top genes for aged samples included *Gzmc*, *Scube3*, *Cilp*, *Smoc1*, and *Apoe*. In particular, *Scube3* has been linked to ECM organization and growth factor signaling [60], and both *Cilp* and *Smoc1* are ECM-associated proteins, with *Cilp* implicated in age-related fibrosis [61, 62] and *Smoc1* promoting fibroblast migration and repair [63]. Notably, *Apoe* is a key regulator of lipid metabolism and inflammation, both of which are altered in aging fibroblasts [64]. In young fibroblasts, top genes included *Gas6*, *Gsn*, *Il1r2*, *Hbb-bt*, and *Cilp*. Among them, *Hbb-bt*, a hemoglobin beta subunit, may reflect metabolic activity associated with fibroblast responses [65]. The consistent appearance of *Cilp* across both age groups underscores its importance in ECM regulation and tissue remodeling.

In keratinocytes, *Fabp5*, *Krt25*, *Krt35*, *Tchh*, and *Slc30a1* were identified as top genes for aged samples across algorithmic variants. Notably, *Krt25* and *Krt35* are keratin genes associated with cytoskeletal stability, which are reflecting age-related changes in keratinocyte structure and function [66, 67], while *Tchh* (trichohyalin) is involved in keratinocyte differentiation [68], and *Slc30a1* encodes a zinc transporter linked to cellular stress responses and proliferation [69]. For young mice, Patches identified *Slc27a1*, *Tgfa*, *Col1a2*, *Terf2ip*, and *Calml3*. *Slc27a1*, a fatty acid transporter, and *Tgfa*, a growth factor involved in epidermal proliferation, are involved in active lipid metabolism and regeneration processes in younger cells [70, 71]. Similarly, *Col1a2*, a collagen gene, underscores ECM production and tissue integrity [72], while *Calml3* is linked to calcium signaling, which plays a role in keratinocyte differentiation and proliferation [73].

Computationally, adding the intercept term to the standard approach resulted in minimal changes to the ranked gene lists. However, introducing the sparsity term in the loss function altered the lists to varying degrees, depending on the condition-specific attributes (Fig. 6C). This observation suggests that many genes may contribute nonlinearly to the attribute-specific representations. Alternatively, it highlights the need to carefully document and scrutinize non-trivial modeling choices, as such choices can strongly influence the interpretability and reproducibility of generative models applied to scRNA-seq data [74].

Discussion

Here we introduce *Patches*, a generative deep learning framework designed to learn both shared and condition-specific gene expression representations from experiments with observations collected across multiple conditions. In the context of wound healing, this approach provides a powerful tool for understanding the impact of cell type, age, or treatment. Specifically, *Patches* enables both qualitative and quantitative analyses of single-cell datasets in complex experimental designs involving multiple conditional labels, providing researchers with deeper insights into the cellular dynamics of wound healing. *Patches* leads to visualizations that separate gene expression signals into common and distinct nonlinear patterns, complementing existing dimensionality reduction techniques. This separation is achieved through information-theoretic priors, which promote disentangled representations. Furthermore, *Patches* can handle data collected from experiments involving combinatorial condition groups, where not all the cells are observed across all the groups. Finally, its inter-

pretable design facilitates an understanding of how individual genes contribute to the learned data representations. Using Patches, we identified several unique age-related changes, including notable alterations in cellular pathways, extracellular matrix components, and gene expression patterns. Among these, a novel observation was the alteration of *Apoe*, a key regulator of lipid metabolism and inflammation, in aging fibroblasts. This finding may provide a mechanistic explanation for the altered lipid homeostasis, increased inflammatory signaling, and functional decline observed in aged fibroblast populations [75, 4, 76].

Despite its strengths, *Patches* presents computational challenges, including longer training times compared to simpler models like scVI. This is partly due to the use of adversarial discriminators and the additional training epochs required to ensure disentangled latent representations. Furthermore, while the linear decoder enables interpretability, its expressivity may limit performance in complex generative tasks such as cross-condition imputation. Nonetheless, this trade-off is offset by its ability to generate biologically interpretable insights.

A promising future application for *Patches* is the cross-species comparison of wound healing dynamics. Direct studies of wound healing in humans are limited by ethical and practical constraints, yet substantial single-cell transcriptomic datasets from unwounded human tissues are readily available. *Patches* could bridge this gap by leveraging transcriptomic patterns from unwounded human samples and integrating data from animal models, where wounding can be experimentally induced. This approach could provide critical insights into the conserved and divergent mechanisms underlying wound healing across species. Such cross-species predictive analyses hold significant potential for improving the translation of findings from model organisms to human biology, paving the way for the development of targeted and more effective therapeutic strategies for wound healing. Further extending *Patches* to accommodate additional data modalities, such as spatial transcriptomics or chromatin accessibility data, could further enhance its utility in studying dynamic biological processes. Lastly, improving scalability and computational efficiency would enable broader adoption in large-scale studies.

The ability to disentangle shared and condition-specific transcriptomic patterns makes *Patches* a valuable tool for investigating multi-condition biological systems. Its application extends beyond wound healing, with potential use cases in developmental biology, aging research, and response to therapeutic interventions. As datasets become increasingly complex and multifaceted, *Patches* provides a critical framework for extracting interpretable insights, driving discoveries in systems biology and translational research.

Methods

Overview of *Patches*

Patches is a representation learning framework which extends traditional VAE models in various important ways. First, *Patches* incorporates a hierarchical latent space to improve visualization and generative accuracy. Moereover, the underlying latent variables are organized into common and conditional components. Information theoretical constraints ensure the separation between common and condition-specific latent representations. Finally, *Patches* allows interpretability through incorporating a linear decoder [20] to identify gene expression signatures driving both common and condition specific cell states. In detail, our framework integrates and extends several key concepts from computational biology and machine learning into a unified approach:

Deep Generative Models. Deep generative models, such as scVI [17] and its extensions [26, 32, 28, 29], have demonstrated success in generating highly realistic gene expression profiles.

Latent Space Structuring. Organizing the latent space can significantly enhance model performance. Hierarchical structuring of the latent space improves visualizations [24], while conditioning the latent space on discrete categories (e.g., chemical interventions or cell types) enables learning gene expression patterns specific to attributes in the data[26, 35, 77, 31].

Challenges in Disentangled Representations. Learning conditional disentangled latent representations is inherently challenging [39, 40]. In some cases, it may even be theoretically unattainable [78]. Most importantly, organizing the latent space only as a mixture of conditions can overlook important biological factors. For instance, in wound healing studies, gene expression signatures may be present irrespective of whether the cells originate from old or young mice, alongside age-specific signatures. Previous work has shown the benefits of incorporating both common and conditional latent representations in generative [34] and non-generative models [36]. However, these models necessitate explicit cross-modality alignment, which is impractical when observing complex scenarios like wound healing in both young and old mice simultaneously.

Regularization for Disentanglement. To ensure the disentanglement and the identifiability of common and conditional latent representations, additional regularization is necessary. This can be achieved through imposing various constraints [39, 40, 79].

Improving Interpretability. End-to-end deep learning models often suffer from poor interpretability. This can be enhanced by incorporating linear decoding layers [20].

Generative model

Notation and setup. In the following, n indexes the N cells and g indexes the G genes in a given study. The corresponding gene expression values are denoted by x_{ng} for each cell n and gene g. We encode observation labels through a two-level hierarchy consisting of C condition groups each with S_i attributes, where $i = 1, 2, \ldots C$ indexes the C classes. For example, 'age' represents a class or a condition group, and 'young' or 'old' represent its $S_{age} = 2$ attributes. The total number of attributes is denoted by K, where $K = S_1 + S_2 + \ldots + S_C$, and each attributes is indexed by k. The label information about the observation n is encoded in a binary vector $\mathbf{y}_n \in \{0,1\}^K$. This binary vector is a concatenation of C one-hot encodings, unit vectors $\zeta_n^i \in \{0,1\}^{S_i}$, one for each class $i = 1, 2, \ldots C$.

As an example, consider observations collected from a dataset with two annotated cell types (fibroblasts and keratinocytes) across three different timepoints (t_1, t_2, t_3) and from mice of different ages (young and old). This sample can be represented with a binary encoding consisting of three condition groups: cell type ($S_{Cell\ Type} = 2$), timepoint ($S_{Time} = 3$) and age ($S_{Age} = 2$). In this case, let $\mathbf{y}_n = [1, 0, 1, 0, 0, 1, 0]$ represent a fibroblast collected from an uninjured, young mouse. This is concatenation of three unit vectors $\zeta_n^1 = [1, 0]$ for the cell type, $\zeta_n^2 = [1, 0, 0]$ for the timepoint and $\zeta_n^3 = [1, 0]$ for the age. Note that a sample with the label encoding $\mathbf{y}_n = [1, 0, 1, 1, 0, 1, 0]$ would be inadmissible since it would imply that the data comes from two timepoints simultaneously.

Model. Each gene expression count x_{ng} is generated using a hierarchy of latent variables informed by the label encodings $\mathbf{y}_n$ under which the cell n was collected, as follows:

$$\mathbf{z}_n \sim \text{Normal}(\mathbf{0}_{d_z}, I_{d_z})$$

$$\mathbf{w}_n = \bigoplus_{k=1}^{K} \mathbf{w}_n^k, \ \mathbf{w}_n^k \sim p(\mathbf{w}_n^k \mid y_n^k) = \begin{cases} \text{Normal}(\mathbf{m}_{d_{w^k}}, I_{d_{w^k}}) & \text{if } y_n^k = 1 \\ \text{Normal}(\mathbf{0}_{d_{w^k}}, 0.1\, I_{d_{w^k}}) & \text{otherwise} \end{cases}$$

$$\rho_n \sim \text{Normal}(f_{\rho_\mu}(\mathbf{z}_n, \mathbf{w}_n), \ f_{\rho_\sigma}(\mathbf{z}_n, \mathbf{w}_n)).$$

Here, $\mathbf{m}$ is a constant vector of size d_{w^k} that controls the separation between common and conditional latent variables. The latent variable $\mathbf{z}_n$ has a standard multivariate normal prior and reflects the portion of the cell's identity that is independent of its conditional labels $\mathbf{y}_n = [y_n^k]_{k=1}^K \in \{0,1\}^K$. On the other hand, each $\mathbf{w}_n^k$ is drawn from one of two multivariate normal distributions, depending on whether the y_n^k governing the corresponding $\mathbf{w}_n^k$ is 1 or 0. Intuitively, this provides a mechanism to turn the corresponding conditional subspace $\mathbf{w}_n^k$ 'on' or 'off' through the value of y_n^k. Then, for a cell n, $\mathbf{w}_n$ is defined as the concatenation ($\bigoplus$) of all such $\mathbf{w}_n^k$. The functions f_{ρ_μ} and f_{ρ_σ} are used to generate a cell's latent representation ρ_n using its conditional latent representation $\mathbf{w}_n$ and common latent representation $\mathbf{z}_n$. The final gene expression profiles are generated following other related latent variables accounting for common technicalities in generative models for single cell RNA-seq data [43, 17, 26]:

$$\ell_n \sim \text{LogNormal}(\ell_\mu, \ell_\sigma^2)$$

$$\nu_{ng} \sim \text{Gamma}(Softmax(f_\nu^g(\rho_n)), \theta^g)$$

$$\gamma_{ng} \sim \text{Poisson}(\ell_n \nu_{ng})$$

$$h_{ng} \sim \text{Bernoulli}(f_h^g(\rho_n))$$

$$x_{ng} = \begin{cases} \gamma_{ng} & \text{if } h_{ng} = 0 \\ 0 & \text{otherwise,} \end{cases}$$

where ℓ_n are cell-specific scaling factors centered around the observed log-library size and $\theta \in \mathbb{R}_+^G$ are gene-wise inverse dispersions. The layers f_ν and f_h map the latent representations back into the gene space while accounting for dropouts [43, 17, 26]. The resulting distribution of the gene counts is ZINB, where the zero-inflation probabilities for each gene are encoded by f_h.

Inference and optimization

The posterior distribution of the model latent variable given gene expression profiles $\mathbf{x}_n \in \mathbb{R}_+^G$ and their corresponding sample attributes $\mathbf{y}_n$, that is $p_\phi(\mathbf{w}_n, \mathbf{z}_n, \rho_n, \ell_n \mid \mathbf{x}_n, \mathbf{y}_n)$, is intractable [17, 26, 80]. We compute an approximation via stochastic variational inference [17]. In detail, the resulting variational distribution $q_\phi(\mathbf{w}_n, \mathbf{z}_n, \rho_n, \ell_n \mid \mathbf{x}_n, \mathbf{y}_n)$ is factorized into neural networks with parameters ϕ:

$$q_\phi(\mathbf{w}_n, \mathbf{z}_n, \rho_n, \ell_n \mid \mathbf{x}_n, \mathbf{y}_n) = q_\phi(\rho_n \mid \mathbf{x}_n)\, q_\phi(\ell_n \mid \mathbf{x}_n)\, q_\phi(\mathbf{w}_n \mid \rho_n, \mathbf{y}_n)\, q_\phi(\mathbf{z}_n \mid \rho_n),$$

where, for simplicity, we drop the batch indicators s_n. Similarly to [17], $p(x_{ng} \mid \rho_n, \ell_n)$ has a closed form density, following a ZINB distribution. Hence, inference over the random variables ν_{ng}, h_{ng} and γ_{ng} is not needed. Applying Jensen's inequality to the approximate posterior, we obtain the variational lower bound which constitutes the first part of our objective:

$$\mathcal{L}_{ELBO} = \underbrace{-\mathbb{E}_{q_\phi(\mathbf{w},\mathbf{z},\rho,\ell\mid\mathbf{x},\mathbf{y})}\log p(\mathbf{x} \mid \rho, \ell)}_{\text{Reconstruction}} + \underbrace{\mathbb{E}_{q_\phi(\mathbf{w}\mid\rho,\mathbf{y})q_\phi(\mathbf{z}\mid\rho)}[KL(q_\phi(\rho \mid \mathbf{x}) \parallel p(\rho \mid \mathbf{w}, \mathbf{z}))]}_{\rho}$$
$$+ \underbrace{\mathbb{E}_{q_\phi(\rho\mid\mathbf{x})}[KL(q_\phi(\mathbf{w} \mid \rho, \mathbf{y}) \parallel p(\mathbf{w} \mid \mathbf{y}))]}_{\mathbf{w}} + \underbrace{\mathbb{E}_{q_\phi(\rho\mid\mathbf{x})}[KL(q_\phi(\mathbf{z} \mid \rho) \parallel p(\mathbf{z}))]}_{z} + \underbrace{KL(q_\phi(\ell \mid \mathbf{x}) \parallel p(l))}_{\ell}.$$

This variational objective encodes the assumption that the common latent representations $\mathbf{z}$ are independent of the conditional labels $\mathbf{y}$. However, in practice, minimizing this objective does not necessarily lead to solutions that satisfy the independence condition [39]. Additional constraints are necessary to ensure that all information correlated with $\mathbf{y}$ is removed from $\mathbf{z}$. To do so, we employ an information-theoretic strategy and introduce a condition-dependent discriminator loss:

$$\mathcal{L}_D = \sum_{i=1}^{C} \beta_i \mathbb{E}_{q_\phi(\mathbf{z}\mid\rho)}[D_{\delta_i}(\zeta^i \mid \mathbf{z})],$$

where the parameters β_i weigh the importance of individual conditions and δ_i are the parameters of the neural networks corresponding to the discriminators of each condition ζ^i. During training, the discriminators try to maximize their accuracy of predicting the correct attribute for the corresponding condition class (e.g, predicting 'early' for the condition class 'healing stage') only from the common latent representations $\mathbf{z}$ of the given sample:

$$\min_{[\delta_i]_{i=1}^C} \mathcal{L}_D.$$

Minimizing this objective would result in representations $\mathbf{z}$ that are suboptimal: They would retain as much information about the conditional labels $\mathbf{y}$ as possible, making them difficult to distinguish from condition-specific representations $\mathbf{w}$. Since we seek the opposite, our final objective actively penalizes the representations that are favorable for the discriminator loss:

$$\min_{\phi} \mathcal{L}_{ELBO} - \mathcal{L}_D.$$

Cross-condition transfer

Patches is designed to allow switching between any condition by treating each condition group as a separate entity in the label encoding $\mathbf{y}_n$. Cross-condition transfer for a cell $\mathbf{x}_n$ with target conditional label $\mathbf{y}_t$ using a trained instance of *Patches* is performed in three steps:

1. Encode $\mathbf{x}_n$ into the shared latent space $\mathbf{z}_n$.

2. For the conditional identity, either (1) sample a $\mathbf{w}_t$ using $\mathbf{y}_t$, or (2) construct any $\mathbf{w}_t$ of choice [39].

3. Decode the transferred gene expression using the concatenated representation $[\mathbf{z}_n, \mathbf{w}_t]$.

Step 2 provides substantial flexibility in defining $\mathbf{w}_t$, in that any custom $\mathbf{w}_t \in \mathbb{R}^{d_w}$ can be provided during transfer. Alternatively, multiple $\mathbf{w}_t$ instances can be sampled to explore a range of possible generation outcomes [39]. For our experiments, however, we sample a single $\mathbf{w}_t$ using $\mathbf{y}_t$ to minimize time spent with computations.

Interpretability module

Patches can optionally be run using a linear decoder for the generative step, which allows it to associate the expression pattern of each gene g with condition attributes y_n^k [20]. Notably, the intermediate variable ρ is not considered in this option, and the function f_ν^g is linear. This option should not be used for cross-condition prediction, as the linear decoder may limit expressivity when generating gene expressions.

Let $[\mathbf{z}, \mathbf{w}] \in \mathbb{R}^{d_z + d_w}$ be the concatenation of latent representations, $\alpha \in \mathbb{R}^g$ be the optional intercept term (that does not appear in the standard linear decoder implementation in [20]) and $\Lambda \in \mathbb{R}^g \times \mathbb{R}^{d_z + d_w}$ be a matrix. The lines that changes for the generative model can be rewritten as:

$$\nu_{ng} \sim \text{Gamma}(Softmax([\mathbf{z}, \mathbf{w}] \cdot \Lambda^T + \alpha)^g, \, \theta^g)$$
$$h_{ng} \sim \text{Bernoulli}(f_h^g([\mathbf{z}, \mathbf{w}])).$$

By construction, Λ is a concatenation of two sub-matrices $\lambda_z \in \mathbb{R}^G \times \mathbb{R}^{d_z}, \lambda_w \in \mathbb{R}^G \times \mathbb{R}^{d_w}$ along the columns, which correspond to the common and conditional weights per gene specifically. Additionally, λ_w itself is a concatenation of K sub-matrices of the form $\lambda_{w^k} \in \mathbb{R}^G \times \mathbb{R}^{d_{w^k}}$ along the columns. The conditional sparsity penalty is an $\mathcal{L}_1$ loss on the conditional coefficients λ_w defined as:

$$\mathcal{L}_{CondSparsity} = \tau . \sum_{i=1}^{G} \sum_{j=1}^{d_w} (\lambda_w)_{i,j} \, ,$$

where we chose $\tau = 1e - 4$ for our experiments. To have a single continuous value per gene that we can treat as an attribute specific score, we report the sum of weights over attribute dimensions d_{w^k}.

Architecture and hyperparameters

Architecture *Patches* uses neural networks to parameterize many of its components: all the encoders used for the approximate variational posterior $(q(\mathbf{w}, \mathbf{z}, \rho, \ell \mid \mathbf{x}, \mathbf{y}))$, the generative functions $(f_{\rho_\mu}, f_{\rho_\sigma}, f_\nu, f_h)$, and the discriminators $(D_{\delta_i}(\zeta^i \mid \mathbf{z}))$. In detail:

- The encoders for the approximate variatonal posterior and the generative functions are neural networks with $n_{hidden} = 2$ hidden layers. Each hidden layer is a fully-connected layer of $d_{hidden} = 128$ neurons, followed by a *BatchNorm1d* layer of the same size and then a *ReLU* activation.

  - The inputs for the encoders are determined by the variables being conditioned on (*Inference and optimization*). The outputs, similarly, correspond to the parameters for the outcome variable distributions. If the parameters are required to be non-negative, the outputs are passed through an additional *Softplus* layer.

  - The input for $f_{\rho_\mu}, f_{\rho_\sigma}$ is the concatenation of latent representations $\mathbf{z} \bigoplus \mathbf{w}$ in this order. The input for f_ν, f_h is the latent representation of the cell identity ρ. The outputs of $f_{\rho_\mu}, f_{\rho_\sigma}$ are respectively the mean and variance for the reparameterized cell identity ρ. The outputs of f_ν are passed through an additional *Softmax* layer (as in [17]) to encode the mean gene expression proportions irrespective of total counts. The outputs of f_h represents the log-odds for the probability of a technical dropout event for each gene.

  - For all neural networks, the inputs are passed through hidden layers, and then a final fully-connected layer.

- The discriminators $D_{\delta_i}(\zeta^i \mid \mathbf{z})$ are neural networks formulated in the same fashion with the same hyperparameters. The input representations $\mathbf{z}$ are passed through the hidden layers, and then a final fully-connected layer. The discriminator output represents log-odds for the probability of belonging to the condition ζ^i.

Training procedure. During training, the model receives as input the gene expression $\mathbf{x}_n = [\mathbf{x}_{ng}]_{g=1}^G$ of a cell n, along with its label encoding $\mathbf{y}_n = [\zeta_n^i]_{i=1}^C = [y_n^k]_{k=1}^K \in \{0, 1\}^K$. These inputs are passed through an encoder $q(\rho_n, l_n \mid \mathbf{x}_n)$, which parameterizes cell identity ρ_n, independent of library size, and a value ℓ_n corresponding to the library size of the cell. The cell identity ρ_n is then decoupled into two components: a common representation $\mathbf{z}_n$, which is agnostic to the encoding $[y^k]_{k=1}^K$, and a conditional representation $\mathbf{w}_n = [\mathbf{w}_n^k]_{k=1}^K$. To enforce the independence between $\mathbf{z}_n$ and $\mathbf{y}_n$, discriminators $D(\zeta_n^i \mid \mathbf{z}_n)$ attempt to predict the cell's conditions ζ_n^i based on its latent representation $\mathbf{z}_n$. The latent representations are further used by the decoders $f_{\rho_\mu}, f_{\rho_\sigma}$ to generate reconstructed cell profiles ρ_n', which are then mapped back to the original gene expression space by the decoders f_ν, f_h and the encoded library size ℓ_n.

Implementation details and hyperparameters. *Patches* was implemented using the Pyro probabilistic programming framework [81]. For all real datasets, we used latent dimensions of $d_z = 10$ for condition-agnostic representations z, and $d_{w^k} = 2$ for each attribute-specific representation $\mathbf{w}^k$. The total latent dimension was set as $d_\rho = d_z + d_w$. In detail, for the Vu dataset [4], this corresponds to attribute-specific representations with dimensions $d_w^{Age} = 4, d_w^{Timepoint} = 6$ and $d_w^{Cell\ Type} = 20$. Similarly, for the Mascharak dataset [47] we learned attribute-specific representations with sizes: $d_w^{Treatment} = 4, d_w^{Timepoint} = 6$ and $d_w^{Cell\ Type} = 18$. All the fully connected layers of the neural networks were initialized using Kaiming initialization [82], while the *BatchNorm* layers followed PyTorch default settings with scaling initialized to a vector of $\mathbf{1}$ and biases to a vector of $\mathbf{0}$ [83]. The multivariate normal distributions of each $\mathbf{w}^k$ were parameterized by a constant vector $\mathbf{m}$ set to $\mathbf{3}$, in line with [39]. To ensure consistent scaling, we normalized the loss function by the number of genes g and the mini-batch size d_b. Optimization was performed using the Adam optimizer with parameters $\gamma = 0.001$, $\epsilon = 0.01$ and $\beta_1, \beta_2 = [0.9, 0.999]$. All models were trained for 2000 epochs on the Vu dataset, and for 20000 epochs on the Mascharak dataset.

Illustrative examples

This section provides a detailed explanation of the methods used to implement the simulations that generated the results presented in Fig. 2B-G.

Synthetic attribute separation model. We considered the dataset $\mathcal{D} = \{\mathbf{x}_n, \mathbf{y}_n\}_{n=1}^N$ for $N = 8,000$ where $\mathbf{x}_n \in \mathbb{R}^{30}$ and $\mathbf{y_n} = [\zeta_n^1, \zeta_n^2]$ for conditional groups $\zeta_n^i \in \{[1,0],[0,1]\}$. The total number of sampled points was distributed equally across different possible combinations of ζ_n^i. Each data point $\mathbf{x}_n$ was constructed through the following procedure:

$$\mathbf{z}_n \sim \text{Normal}(\mathbf{0}_{10}, 0.5\,\mathbb{I}_{10})$$

$$\mathbf{w}_n^1 \sim p(\mathbf{w}_n^1 \mid \zeta_n^1) = \begin{cases} \text{Normal}(\mathbf{1.15}_{10}, 0.5\,\mathbb{I}_{10}) & \text{if } \zeta_n^1 = [0,1] \\ \text{Normal}(\mathbf{0}_{10}, 0.5\,\mathbb{I}_{10}) & \text{if } \zeta_n^1 = [1,0] \end{cases}$$

$$\mathbf{w}_n^2 \sim p(\mathbf{w}_n^2 \mid \zeta_n^2) = \begin{cases} \text{Normal}(-\mathbf{1.15}_{10}, 0.5\,\mathbb{I}_{10}) & \text{if } \zeta_n^2 = [0,1] \\ \text{Normal}(\mathbf{0}_{10}, 0.5\,\mathbb{I}_{10}) & \text{if } \zeta_n^2 = [1,0] \end{cases}$$

$$\mathbf{x}_n \sim \text{Normal}\left(A\,[\mathbf{z}_n, \mathbf{w}_n^1, \mathbf{w}_n^2], 0.5\,\mathbb{I}_{30}\right),$$

where $\mathbf{b}_{10}$ denotes a 10-dimensional vector with all entries being equal to the constant value b, and $\mathbb{I}_{10}$ is the 10×10 identity matrix, A is a 30×30 identity matrix, and $[\mathbf{z}_n, \mathbf{w}_n^1, \mathbf{w}_n^2]$ denotes the concatenation of the latent vectors.

Swiss roll. We used the previously implemented `make_swiss_roll_dataset` function [45, 46] to generate $N = 10,000$ points situated on a Swiss roll in three dimensions (X, Y, Z). Following point generation, we sliced the roll from the midpoint along the Y-axis – at $Y = 10$ – and assigned labels to points to reflect their slice of origin. This resulted in a dataset with a single condition group having two attributes. $\mathcal{D} = \{\mathbf{x}_n, \mathbf{y_n}\}_{n=1}^N$ where $\mathbf{x_n} \in \mathbb{R}^3$ and $\mathbf{y_n} = \zeta_n \in \{[1,0],[0,1]\}$.

Datasets

We used publicly available single-cell datasets representing various wound healing contexts. These datasets included samples exposed to distinct temporal, chemical, or pathological conditions. We follow a similar approach for every dataset to preprocess and annotate the raw objects prior to runnning the models.

Vu dataset. The Vu dataset [4] contains data for $N = 26,966$ cells after preprocessing, with samples collected from 10 seven-week-old and six 88-week-old wild-type female mice. Each sample corresponds to data from single mouse and one of three conditions: unwounded (UW), four days post-wounding (4DPW), or seven days post-wounding (7DPW). We only consider the samples from v3 sequencing runs to limit the influence of chemistry-related batch effects. As per the original analysis conducted, we keep cells with at least 200 and at most 5000 non-zero genes and with less than 15% of gene counts arising from mitochondrial genes. We use the standard `scanpy` analysis pipeline [14, 84], assign broad cell type labels based on the output of the `rank_genes_groups` function, and finally validate the cell type labels assigned by comparing with markers from previous literature.

Mascharak dataset. The Mascharak dataset [47] consists of $N = 2,284$ cells after preprocessing. Samples were obtained from mice treated with a PBS control or with verteporfin at five key timepoints (UW, 2DPW, 7DPW, 14DPW, 30DPW). As UW cells are not treated with any substance, we did not choose to include these cells in the final dataset

considered. Since antibody counts for demultiplexing were missing from cells belonging to the 2DPW timepoint in the raw data, we instead only use the cells from 7DPW, 14DPW and 30DPW. For demultiplexing, we use the implementation of `hashsolo` [85] provided in [14]. After matching the sample metadata, we apply the standard `scanpy` analysis pipeline [14] to assign broad cell type labels based on the output of the `rank_genes_groups` function, and validate these cell types by comparing with markers from previous literature.

Data processing. Gene expression count matrices were analyzed with the `scanpy` [14] Python package (version 1.10.0). Separate samples belonging to each dataset were merged into a single `anndata` [86] object prior to preprocessing. After preprocessing and before running the models, for any group of cells considered, we retain the top $g = 3,000$ highly variable genes. Specifically, we obtain these genes using the `highly_variable_genes` function provided through `scanpy` with default parameters.

Benchmarks

Patches is uniquely designed to (a) learn both shared, condition-agnostic representations and condition-specific representations, and (b) transfer information across different combinations of conditions. While these capabilities are specific to *Patches*, we extended existing methods with oracle-like features for comparison, allowing us to comprehensively evaluate the performance of our framework.

Oracle-scVI. The original scVI framework [17] provides a biologically informative latent space, but is not inherently designed for condition transfer. To enable this, we define an attribute manipulation function [39, 30]. Let $\mathbf{y}_s$, $\mathbf{y}_t$ represent the source and target conditions, and μ_s, μ_t represent the means of latent representations for cells collected under these conditions. Switching a cell $\mathbf{x}_n$ from the source to the target condition is defined as:

$$\text{Switch}(\mathbf{x}_n)_{s \to t} = \text{Decode}(\text{Encode}(\mathbf{x}_n) - \mu_s + \mu_t)$$

In this process, the cell's gene expression profile is encoded, transformed via arithmetic in the latent space to enable condition transfer, and decoded to reflect the new condition.

scANVI. A semi-supervised version of scVI, scANVI, allows learning latent representations informed by user-specified cell annotations [26]. However, as scANVI is not inherently designed for condition transfer, we adapted it by making the model fully supervised with respect to one hot encodings of attribute combinations $\mathbf{y}_n^1$. This allows us to define a function for switching between these conditions [39]. In detail, letting $\mathbf{y}_s^1$, $\mathbf{y}_t^1$ represent the one-hot encoded source and target conditions, switching between conditions for a cell $\mathbf{x}_n$ can be expressed as:

$$\text{Switch}(\mathbf{x}_n, \mathbf{y}_s^1, \mathbf{y}_t^1)_{s \to t} = \text{Decode}(\text{Encode}(\mathbf{x}_n, \mathbf{y}_s^1), \mathbf{y}_t^1)$$

This way, we encode the cell using its source condition and switch the label to the target condition during decoding.

Evaluation metrics

We categorized the metrics into two main groups focused on: (1) mixing and separability, and (2) generative accuracy. Mixing and separability metrics quantify the extent to which conditional effects are captured by the models. These metrics were calculated using latent representations – z for scVI [17], z for scANVI [26] and z, w for *Patches*. These metrics were used to evaluate representations for each condition group separately.

Generative accuracy metrics assess the models' ability to accurately reconstruct or transfer gene expressions of observations across conditions, reflecting model performance. For these metrics, evaluations were conducted on the generated data within the original gene space g.

Mixing and separability of conditional effects
1. *Normalized Condition Average Silhouette Width (cASW)*
The silhouette score is a measure of how similar a data point is to its own cluster (within-cluster similarity) compared to other clusters (inter-cluster dissimilarity). To calculate the average silhouette scores across attributes for a given condition group ζ^i, we adapt the implementation detailed in [49] - specifically the `silhouette` function - which serves as a wrapper to the original implementation in [45]. The outputted score is a continuous value in the range $[0, 1]$ where values close to 0 indicate non-cluster structure, values around 0.5 indicate overlapping labels and scores closer to 1 indicates compact, distinct clusters.

2. *KNN Classification Accuracy (KNN)*

Using latent representations of cells and euclidean distance as the distance metric, we train a KNN classifier for a given condition group ζ_i on the latent representations to predict the attributes of each observation. Given attribute labels, the classifier assigns the attribute label of the most common attribute among each observation's closest $k = 30$ neighbors. We calculate the accuracy score of this classifier, which is the number of correct predictions divided by the number of all predictions. The outputted score is a continuous value in the range $[0, 1]$, and is expected to be high if the clusters are more compact, with neighborhoods of each cell belonging to the same label.

3-4. *K-Means (3) Normalized Mutual Information and (4) Adjusted Rand Index*

Normalized Mutual Information (NMI) and Adjusted Rand Index (ARI) both measure the similarity of two clusterings. For a given condition group ζ^i, the original clusterings are naturally present in the data, which are given by the attributes for each observation. We obtain an additional clustering using latent representations by running K-means with default hyperparameters and $K = S_i$ determined by the number of attributes for the given ζ^i. Using the two clusterings, we calculate the NMI and ARI through implementations provided in [45] - specifically through the use of `normalized_mutual_info_score` and `adjusted_rand_score` functions. The outputted scores are in the range $[0, 1]$ for NMI and $[-0.5, 1]$ for ARI (even though negative values were not observed), where a higher score indicates greater similarity between clusterings.

Generative accuracy - Aggregate metrics

Metrics in this section are applied to normalized pseudobulk gene expression profiles [87, 88], which generalize the analysis to cases where a one-to-one correspondence between generated and ground truth cells is unavailable. To create a pseudobulk gene expression profile $x^{\mathcal{P}} \in \mathbb{R}^G$ for a group of cells $\mathbf{x} \in \mathbb{R}^{N \times G}$, we first compute the total gene expression across all cells in the group. The resulting vector is then scaled to a pre-defined library size ℓ as follows:

$$x_{Bulk} = \sum_{n=1}^{N} \mathbf{x}_n \ ,$$

$$x^{\mathcal{P}} = \ell \times \frac{x_{Bulk}}{\sum_{g=1}^{G} x_{Bulk}} \ .$$

For all applications, we use a default value $\ell = 1e4$. In Fig. 5A, we analyze pseudobulk profiles for all cells as well as for specific cell types, comparing these with the pseudobulk profiles derived from reconstructed cells. In Fig. 5B we analyze pseudobulk profiles of cell types from the target timepoint. We compare these with transferred profiles of cells mapped from the source timepoint. For simplicity, we use $x \in \mathbb{R}^G$ to represent the ground-truth pseudobulk gene expression profile and $x' \in \mathbb{R}^G$ for the pseudobulk profile generated by the model.

1. *Root Mean Squared Error (RMSE)*

The Root mean squared error (RMSE) is a commonly used metric to assess the closeness of two vectors. We report the RMSE between ground truth and generated pseudobulk gene expression profiles. We define RMSE as:

$$RMSE = \sqrt{\frac{1}{G} \sum_{g=1}^{G} (x_g - x'_g)^2}$$

2. *Pearson Correlation*

Similar to RMSE, Pearson correlation is a widely used metric for comparing gene expression values. Bounded between -1 and 1, it is often preferred over RMSE because of its interpretability. We compute the Pearson correlation coefficient as:

$$r = \frac{\sum_{g=1}^{G} (x_g - \bar{x})(x'_g - \bar{x}')}{\sqrt{\sum_{g=1}^{G} (x_g - \bar{x})^2} \sqrt{\sum_{g=1}^{G} (x'_g - \bar{x}')^2}}$$

Generative accuracy - Point cloud metrics

The metrics in this section are directly applicable to point clouds and, therefore, do not require any matching. This allows them to be used directly with generated observations without additional processing, unlike approaches such as generating pseudobulk expression profiles. In this context, we denote $P \in \mathbb{R}^{N_1 \times G}$ as the point cloud for observations and $P' \in \mathbb{R}^{N_2 \times G}$ as the point cloud generated by the model, with respective sizes N_1, N_2. For reconstruction tasks, we have

$N_1 = N_2$; however, in transfer tasks, this equality does not necessarily hold. Indeed, for the real datasets considered in this study, it is always the case that $N_1 \neq N_2$.

1. *Chamfer Discrepancy (CD)*

Chamfer discrepancy (CD) is a metric that quantifies the difference between two point clouds. In our case, these point clouds correspond to observations P and generated profiles P'. CD is defined as:

$$d_{CD}(P, P') = \frac{1}{n_1} \sum_{p \in P} \min_{p' \in P'} d(p, p') + \frac{1}{n_2} \sum_{p' \in P'} \min_{p \in P} d(p, p'),$$

where $d(p, q)$ is the Euclidean distance between points p, q. Each summand iterates over all points in a single point cloud, picks the closest points (supports) from the other cloud, and calculates the sum of distances divided by the number of points. This metric takes values in the range $[0, \infty)$, with lower values indicating higher similarity. However, it is important to note that Chamfer Discrepancy (CD) may lack robustness in certain scenarios. For instance, point clouds with significant differences can sometimes yield low CD values due to the metric being disproportionately influenced by sparsely located points near the boundaries of the point clouds[89, 90].

2. *2-Sliced Wasserstein Distance (SW_2)*

2-Sliced Wasserstein Distance (SW_2) is another metric used to quantify the difference between two point clouds. We use the implementation provided in [91], where for two probability measures μ, ν corresponding to observations P and generated points P' respectively, the SW_2 is calculated for as:

$$SW_2(\mu, \nu) = \mathbb{E}_{\theta \sim \mathcal{U}(\mathbb{S}^{G-1})} [W_2^2(\theta_{\#}\mu, \theta_{\#}\nu)]^{\frac{1}{2}}$$

where W_2^2 is the 2-Wasserstein distance [89], while $\theta_{\#}\mu$ and $\theta_{\#}\nu$ stand for the pushforwards of the projections $P \mapsto \langle \theta, P \rangle, P' \mapsto \langle \theta, P' \rangle$ respectively.

Reproducibility, applicability, robustness, and scalability of *Patches*

Reproducibility and applicability. In addition to providing the code used in the study, we offer a high-level workflow API built over *anndata* [86] and a low-level developer API. These both facilitate the reproducibility of our results and streamline the application of conditional generative models to other datasets. We showcase the usage of these APIs through various tutorials, most of which aim to reproduce the behaviour of *Patches* using the simulated and real scRNA-seq datasets featured in this study.

Robustness. To ensure the robustness of the generative results, we perform multiple repetitions of training and evaluation. Specifically, we repeat the training process for each benchmark 5 times with different random seeds and repeat the generative processes 10 times across each evaluation before reporting the average performance for a single training process. Tables in Figure 5A,B report the averages of these mean values across 5 training repetitions. For the interpretability module, we investigate 3 distinct model configurations for each data setup: (1) using the standard implementation in [20], (2) incorporating an intercept to the standard implementation and (3) adding an additional $\mathcal{L}_1$ term to the loss function for conditional sparsity.

Scalability. In the tutorial, for the Vu dataset, a single pass through the training set – $21,573$ cells – requires approximately 14.23 seconds for *Patches*, 1.82 seconds for scVI and 3 seconds for scANVI. The memory usage is 1342 MiB (~ 1.4 GB) when training with default hyperparameters (*Implementation details and hyperparameters*). All experiments were conducted using a single H100 GPU. Notably, *Patches* generally demands more training epochs to achieve convergence than the base scVI model, owing to its complex training procedure.

Analysis of common and cross-condition gene expression modules

Here, we outline the details for comparing the attribute-specific scores derived from the interpretability module of *Patches* with other commonly used quantitative and qualitative approaches for analyzing scRNA-seq datasets.

Differential gene expression analysis. For Figure 6A, we obtain significance values for genes using the `rank_genes_groups` function implemented in [14] with default parameters. We perform differential expression testing for each gene by grouping the observations across attributes through the `groupby` parameter, and report the $-log10$ adjusted P-values as significance scores. For rare cases where the adjusted P-value is 0 due to precision

constraints, we set the value to 10^{-300}.

Gene ontology enrichment analysis. GO enrichment analysis was conducted using the `enrichr` wrapper provided in [92, 58] using the gene set `GO_Biological_Process_2023` for mouse. Attribute specific scores obtained from the interpretability module were ranked, and the union of top 10% genes across all attributes were used to construct the input gene list for enrichment testing. Significantly enriched (adjusted P-value < 0.05) GO terms were ranked and manually curated to remove redundancy.

Data availability

Raw data files for the Vu dataset [4] can be accessed through the Gene Expression Omnibus (GEO), under the accession number GSE188432. Raw files for the Mascharak [47] dataset can be found under the accession number GSE186527. Additionally, we provide the exact *anndata* objects used in this study through the implemented package.

Code availability

Implementation of *Patches*, as well as the code base that can be used to reproduce results and apply the models considered in this study to other datasets can be found at: `https://github.com/Computational-Morphogenomics-Group/Ladder/tree/patches`. Documentation and tutorials on how to apply the models to new datasets will be made publicly available under `https://ladder.readthedocs.io/`.

Author contributions

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Visualization: OB, BD
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Figures

Figure 1: **Overview of *Patches* for multi-condition experimental designs: A**, Graphical illustration of datasets compatible with *Patches*, with observations from different time, age or cell type attributes. **B**, Illustration of how *Patches* models multi-condition data, disentangling condition-specific and condition-agnostic (common) representations. The condition-specific representation captures the expression components that vary across attribute labels, while the common representation reflects shared features across all conditions. **C**, Comparison of *Patches* with existing models: in contrast to scVI, which learns representations in a condition agnostic fashion, and to scANVI, which learns conditional-representations one condition at the time, *Patches* employs a mix of both approaches, obtaining both conditional and common representations, which are then disentangled using information-theoretical or adversarial priors.

Figure 2: **A proof of concept for *Patches* using synthetic examples.** Given observations with conditional labels as input, *Patches* obtains condition specific and common representations. **A**, Graphical model for *Patches*: the adversarial discriminators $D(\zeta^i \mid \mathbf{z})$ and all the approximate distributions are implemented via neural networks. **B**, UMAP embeddings of the original observations and their corresponding latent representations for the synthetic attribute separation model, demonstrating the ability of *Patches* to separate attributes. **C, D**, Reconstruction of the Swiss roll by *Patches* with nonlinear (**C**) and linear (**D**) decoders, showing differences in reconstruction quality. **E**, The linear decoder in *Patches* learns coefficients that indicate the contribution of each variable in the original data space (columns) to the latent space (rows). **F,G** Latent representations of the Swiss roll data for linear (**F**) and nonlinear **G** decoders, highlighting the separation of common and condition-specific components. Legends in the top right of the panels indicate axes.

Figure 3: **Application of *Patches* to wound healing datasets**. **A, B**, Visualization results for gene expression profiles from aged and young mice, collected from 0 (unwounded), 4 and 7 days post wounding conditions (**A**) [4] and for gene expression profiles collected from mice 7, 14 or 30 post operative days (POD), treated with either PBS (control) or Verteporfin **B** [47]. Cells were colored by condition groups across rows, corresponding to cell types (**A, B**) time (**A, B**), age (**A**) and treatment (**B**). The first three columns show UMAP embeddings of: the original gene expression profiles (first), the common latent representations (second) and the conditional latent representations (third). The fourth column shows the values of the first two principal components, with the first and second inner columns corresponding to common latent representations, and the third and fourth inner columns corresponding to conditional latent representations.

Figure 4: **Quantification of the attribute specific representations of *Patches*.** *Patches* can distinguish attribute-specific effects in real datasets. **A**, **B**, Top 20 marker genes associated with the provided cell type label annotations for the 3 major cell types in the Vu (**A**) and Mascharak (**B**) datasets, obtained from the linear decoder of *Patches*. Violin plots show gene expression distributions across all annotated cell types. **C**, Separability scores for the latent representations obtained by running scVI, scANVI and *Patches* on the Vu (top row) and Mascharak (bottom row) datasets. KNN, K-Means NMI, K-means ARI and cASW scores for models were calculated separately for each condition group within each dataset - a higher score indicates higher separability.

Figure 5: ***Patches* performs competitively in generative tasks.** Comparison of generative accuracy metrics (RMSE, Correlation, 2-SWD and CD) for scVI, scANVI and *Patches*. Darker colors indicate better performance. **A**, Reconstruction accuracy on held out cells for the benchmarked models for all cells and the three major cell types for the Vu (top row) and Mascharak (bottom row) datasets. **B**, Transfer accuracy for the benchmarked approaches calculated after transferring held out cells of the 3 major cell types from the first (0DPW for Vu, POD7 for Mascharak) to the subsequent timepoint (4DPW for Vu, POD14 for Mascharak) for the Vu (top row) and Mascharak (bottom row) datasets. **C**, Comparison of *Patches* (left), scVI (middle) and scANVI (right) in recapitulating the true and reconstructed log-mean and log-variance for each gene across the Vu (top row) and Mascharak (bottom row) datasets.

Figure 6: **Extracting condition-specific interpretations with *Patches*. A**, Alignment R^2 values from conditional and common representations (Y-axis) plotted against differential gene expression significances obtained by comparing expression of genes across condition labels (X-axis) for the 3 major cell types (columns) of the Vu (top row) and Mascharak (bottom row) datasets. **B**, Sankey diagram of the top 10 significantly enriched GOs for the top 10% ($n = 300$) genes in fibroblasts (left) and keratinocytes (right) of the Vu dataset. Genes appearing in the top 10% across multiple attributes were labeled with the top scoring attribute, but shown connected to other attributes through links. Link bandwiths between GOs and attributes represent the flow of attribute scores. **C**, Venn diagrams of top 10% genes for each attribute in the Vu dataset by applying linear decoders with different statistical architectural choices (intercept, sparsity) for fibroblasts (left) and keratinocytes (right).