1 **Tracking changes in stability of North Sea Atlantic cod in 40 years**
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17 **Abstract**
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Tracking changes in the stability of low-abundance populations is vital for conservation.
While the stability of natural populations is often assessed based on linear dynamics, many
exhibit state-dependent dynamics, such as the iconic Atlantic cod in the North Sea (*Gadus*
morhua). This fish population experienced an abrupt decline in the year 2000 and has not
shown a clear sign of recovery despite relaxed fishing pressure. To understand the
mechanisms behind the recovery dynamics, we used a dynamical systems approach to
reconstruct the state space of the population from yearly abundance data of age groups
between 1982-2021. Specifically, we estimated yearly interaction matrices of age groups and
derived yearly population stability, defined as the rate of recovery to or departure from the
current state after a small perturbation to the matrix. We found that since the abrupt decline in
abundance of North Sea cod in the year 2000, the population continued to fluctuate closer to
the transition threshold; some age groups experienced weaker self-regulation; and age-1
group became more sensitive to perturbations than older groups. These results provide
important information on North Sea cod's resilience and capacity to buffer natural and
anthropogenic impacts.

34
35 **Keywords**
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37 Age-specific abundance, non-linear dynamics, empirical dynamical modelling, interaction
38 Jacobians, population stability, recovery dynamics
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41 **Introduction**
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To date, many marine populations are experiencing delayed rebuilding and uncertainties in
recovery (Neubauer et al. 2013, Britten et al. 2017, Duarte et al. 2020). Understanding these
populations' stability, defined as the capacity of the populations to persist or maintain their
present state in the face of disturbance, may provide explanations for their recovery
dynamics. The stability of a fish population is often evaluated by the distance or rate of
recovery to fixed biological reference points (e.g., Neubauer et al. 2013, Trochta et al. 2020).
These reference points are determined by assessments of populations' state based on linear

dynamics. However, population dynamics are shaped by deterministic and stochastic forces
(Bjørnstad and Grenfell 2001), and some marine fishes exhibit nonlinear dynamics with
varying equilibrium points over time (Anderson et al. 2008, Glaser et al. 2014) and regime
shift-like dynamics (Blöcker et al. 2023).
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The mismatch between linear methods and nonlinear dynamics of natural systems motivates
recent advances to estimate stability as how the system's state departs from or recovers to the
current state when slightly perturbed, without having to identify a reference or equilibrium
point (Bjørnstad and Grenfell 2001, Ushio et al. 2018, Cenci and Saavedra 2019, Grziwotz et
al. 2023). Particularly, empirical dynamic modeling, a statistical approach which is based on
nonlinear dynamical systems (Takens 1981), has been used to estimate the stability of natural
communities (Cenci and Saavedra 2019, Chang et al. 2021, Zhao et al. 2023), evaluate
species interactions (Ushio et al. 2018), and rank species' relative sensitivity to perturbations
(Medeiros et al. 2022, Medeiros and Saavedra 2023). These properties are derived from
reconstructed species interactions network within communities. However, whether empirical
dynamic modeling can also estimate the stability of structured natural populations from
interactions between age or size groups, remains unknown.
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The interactions between age or size groups of a marine fish population fundamentally shape
the dynamics and stability of the population (Hsieh et al. 2010, Hidalgo et al. 2011, Ciannelli
et al. 2013, Wang et al. 2020). The most common interactions are growth, as positive
influence from one age to the next; reproduction, as positive links from mature adult to young
juveniles; cannibalism, as negative links from larger to smaller fish; and competition for food
and habitats, as negative links from one age to another; self-regulation, as negative links
within the same age groups. The interactions between age or size groups are strongly
dependent on population abundance. At low abundance, adult reproduction is likely
insufficient to sustain recruitment. If juvenile survival is further impacted by fishing pressure,
growth within the life cycle is disrupted, resulting in fewer adults. In addition, all of the
interactions change over time in the face of disturbances. Thus, the stability derived from
age/size group interactions is not a stationary property yet changes with time.
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Observing the change in the stability of a population through time provides potential
explanations on how a natural population's abundance or biomass changes in response to
perturbation. In addition, the interactions between age/size groups and the sensitivity of age
groups to perturbations provide additional information to better understand the recovery
dynamics. This is particularly relevant to exploited fishes as fisheries are often age/size-
selective (Rouyer et al. 2011, Hidalgo et al. 2011), and also to understand the recovery
dynamics and mechanisms of depleted stocks.
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Atlantic cod in the North Sea is an iconic example of fish experiencing delayed recovery. As
a target commodity of one of the world's oldest fisheries, North Sea cod have profoundly
shaped the history, economy, and culture of Western Europe since the 16th century (Goodlad
2022). This population has experienced several abrupt changes in abundance and biomass for
the past decades, with the most recent abrupt decline in 2000 (Blöcker et al. 2022), mainly
due to substantial loss of juveniles (ICES 2024). Despite fishing pressure starting to decline
in the same year, there was a lack of significant recovery. It remains unclear whether and how
the stability of the population has changed, particularly before and after the events of abrupt
decline in abundance and relaxed fishing pressure in 2000.

In this work, we used empirical dynamic modeling to study whether the failure in recover of
Atlantic cod since 2000 is related to its stability and states of age groups. Using abundance
time series of six age groups, we first recovered the trajectory of the population (manifold) in
a reconstructed state space with six dimensions of age groups. We then estimated the pair-
wise age group interactions at each time point based on locally-weighted linear regressions
on the manifold (Sugihara et al. 2012). From these reconstructed interaction matrices, or the
time-varying Jacobians which informs the local stability of the system, we extracted the
dominant eigenvalues as a proxy of population stability. These eigenvalues describes the rate
at which the system recovers to or diverges from its current state, after slightly perturbing the
interaction networks (Ushio et al. 2018). We also extracted the dominant eigenvector of each
age group from the interaction matrices to evaluate the relative sensitivity of an age group to
perturbation in the age group interaction network at each time point (Medeiros et al. 2022).

We addressed the following questions: comparing two periods of 1982-2000 (before abrupt
abundance decline) and 2001-2021 (after abrupt abundance decline), (1) how did the stability
of the North Sea cod population differ? (2) what were the differences in the interactions
among age groups? (3) what were the differences in the relative sensitivity of each age group
to perturbations contributing to the population stability? We hypothesized that North Sea cod
exhibited different stability patterns between the two periods. We further hypothesized
several changes at the second period: due to the sharp decline in the population abundance,
self-regulations within age groups were weakened. In addition, due to extreme low
abundance of adults, reproduction success was reduced, resulting in higher sensitivity of
younger groups to perturbations in the age group interaction network. In contrast, declines in
the survival rate of younger groups impaired the growth in the life cycle, leading to less
sensitivity of older groups to perturbations in the network.

Methods
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124 **1. Data of time series of North Sea Atlantic cod abundance**
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We obtained the winter abundance time series data (from January to March) between 1983-
2022 of Atlantic cod in the North Sea, from the International Bottom Trawl Survey (IBTS) of
the International Council for the Exploration of the Sea (ICES) (https://data.ices.dk). The data
is catch per unit effort (CPUE), measured as the number of fish trawled adjusted to one hour
of hauling and per survey rectangle (1° longitude by 0.5° latitude) for each age group across
the North Sea. To calculate the abundance for each age group in the entire North Sea, we
summed the CPUE data from all rectangles. We used change point analysis (Pélissié et al. 2024),
to detected the year when an abrupt shift in the total abundance occurred over the study period.
Estimated yearly fishing mortality for age-2 to age-4 groups was compiled from the ICES stock
assessment report (ICES 2020).

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137 **2. Analytical framework**
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139 Empirical dynamic modeling (EDM) is a nonlinear statistical approach based on state space
140 reconstruction (Takens 1981). Unlike traditional models that rely on predefined equations,
141 EDM reconstructs the underlying dynamical system directly from observed time series data.
142 In this framework, the state of a dynamical system is depicted as a specific location within a
143 multivariate coordinate space, referred to as "state space", where the axes represent causally
    linked variables or lagged terms of a variable. The system's state evolves over time following

its intrinsic dynamic rules, thereby forming a trajectory. The ensemble of these trajectories
constitutes a geometric structure known as an attractor manifold, which elucidates the
relationships between variables over time (Sugihara et al. 2012).

In this study, we used the following methods of empirical dynamical modelling to address
each of our research questions: (1) simplex projection (Sugihara and May 1990) to determine
the optimal embedding dimension for each age group, (2) S-map (Sugihara 1994) to quantify
the nonlinearity of the population, (3) MDR S-map (Chang et al. 2021) to identify
interactions between age groups. We then (4) derived the absolute value of the dominant
eigenvalue of the interaction matrix (Ushio et al. 2018) estimated from the MDR S-map as a
proxy of population stability, and finally (5) used the eigenvector ranking method (Medeiros
et al. 2022) to identify the relative sensitivity of each age group to perturbations.
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Step 1: Determine the optimal embedding dimension for each age group

We first used simplex projection (Sugihara and May 1990) to determine the optimal
embedding dimension for each age group. This step is crucial for reconstructing the state
space of a dynamical system. The embedding dimension refers to the optimal number of state
variables, or the optimal number of time lags of a state variable, needed to reconstruct the
manifold in the state space.

For each age group, we divided the time series into a library set and a prediction set. Within
the library set, we created state-space reconstructions for different embedding dimensions
ranging from 2 to 10. For each state-space reconstruction, we constructed simplexes, which
are geometric polygons formed from neighboring points around a given point. These
simplexes were then used to predict the future states of the system. Specifically, for each
point in the state space, the future state was predicted based on the weighted average of the
future states of the points that form the simplex. The weights were inversely related to the
distances from the points to the vertex of the simplex.

To evaluate the prediction skill for each embedding dimension, we compared the predicted
states to the observed states in the prediction set using root mean square error (RMSE). The
embedding dimension with the best prediction skill, indicated by the lowest RMSE, was
identified as the optimal embedding dimension.

Step 2: Identify the nonlinearity of the population

We used the S-map method to evaluate the nonlinearity, or state dependency of the
population (Sugihara 1994, Hsieh et al. 2005). For each age group, we first reconstructed the
state space using the abundance time series data of different time lags, where the number of
time series was determined by the optimal embedding dimension identified in the previous
step. In the S-map approach, a locally weighted linear regression model is fitted for each
point in the state space, where closer points have a greater influence on the fit.

The weighting of neighboring points is controlled by a tuning parameter, θ, which determines
the degree of state dependency. When $\theta = 0$, all neighbors are equally weighted, resulting in a
linear model. When θ is greater than 0, closer neighbors are given exponentially more weight,

enabling the model to capture more local and potentially nonlinear dynamics. The fitted local
linear models are then used to make predictions for the system's future states.

We ran the S-map with various values of θ, ranging from 0 to 8, and determined the optimal θ
based on the best forecast skill, identified by the minimum mean absolute error (MAE). If the
prediction skill improves as θ increases from 0, the target age group is deemed nonlinear.
Conversely, if the best predictive skill occurs at θ = 0, the target age group's dynamics is
linear.

We followed the analytical procedure outlined in (Clark and Luis 2019) to assess the
significance of nonlinearity for each age group. We first calculated ΔMAE, which is the
difference between MAE at θ = 0 and the minimum MAE. Next, we generated 1,000 null
models using phase-randomized surrogates, which preserves the basic statistical properties of
the time series such as autocorrelation. We then compared the ΔMAE from the original time
series with the null distribution of ΔMAE. The dynamics is considered significantly nonlinear
if ΔMAE is higher than the 95th percentile of the null distribution.

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Step 3: Construct an interaction matrix of age groups for each year

We quantified the strength and the direction of interaction between each pair of age groups
through time by adapting the Multiview Distance Regularized S-map method (MDR S-map)
(Chang et al. 2021). This approach is developed to study species interactions within a
community, by reconstructing multiple low-dimensional state spaces with the optimal
embedding dimension to determine neighborhood relationships among data points. These
distances are then ensembled to determine the weights used in the multivariate S-map. The
interaction Jacobian elements in the Jacobian interaction matrix of each time point indicate
pairwise interaction strengths and directions.

In this study, we used six age groups to reconstruct the low-dimensional state space, with
maximum embedding dimension of six. The interaction strength of age group i at year t on
age group j in the following year is approximated as the interaction Jacobian $(\partial A_{j(t+1)} / \partial A_{i(t)})$,
where $A_{i(t)}$ is the abundance of age i at year t. We compiled all the pairwise interaction
Jacobians between the six age groups to generate a 6 x 6 discrete-time Jacobian matrix that is
interpreted as the interaction network of our six age groups. For self-interactions, defined as
the change of any age group influences on itself $(\partial A_{i(t+1)} / \partial A_{i(t)})$, we subtract the value of
interaction Jacobian by 1 (Miki et al. 2024).

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219 **Step 4: Compute the population stability at each year**
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From the interaction matrix of age groups of each year, we derived the absolute value of the
dominant eigenvalue (|DEV|) to indicate the population's stability of that year (after Ushio et
al. 2018), known as the local Lyaponov stability. This proxy implies that when given a small
perturbation at a given time to the interaction matrix, how fast the population returns to or
departs from the current state, without having to identify whether the state is at equilibrium.

When |DEV| equals to 1, the population is at a transition threshold between stable and unstable
states. When |DEV| is below 1, the population is stable as it tends to recover to the current
trajectory from disturbances. The lower the value, the more stable the population is at that

moment. Conversely, when |DEV| is higher than 1, the population is unstable, as it tends to
depart from the current trajectory after a small disturbance. The higher the value, the more
unstable the population is at that moment.

Step 5: Quantify the relative sensitivity of age groups to perturbations

To determine the relative sensitivity of age groups to perturbations, we adopted the
eigenvector ranking method (Medeiros et al. 2022), originally developed to rank the relative
sensitivity of different species within a community. In this method, the relative sensitivity is
indicated by the absolute dominant eigenvector of each species, derived from time-varying
Jacobian interaction matrix reconstructed using S-map. The principle lies in when given
small perturbations to the interaction network, the distribution of abundance of a species
expands or contracts approximately along the direction of the dominant eigenvector at a rate
specified by the dominant eigenvalue (Medeiros et al. 2022). That is, the absolute value of the
eigenvector of a species determines how much perturbed abundance would differ from the
unperturbed abundance at the next time point. For a sensitive species, the perturbed
abundance would have a large difference between perturbed and unperturbed abundance.

We applied this method by constructing the interaction matrix from six age groups with MDR
S-map. To compare the relative sensitivity between age groups for a given year, we
standardized the dominant eigenvector of each age by dividing the square root of the sum of
square of all six eigenvectors of that year. Then, we used the absolute values to infer the
relative sensitivity of age groups to perturbations. The original method used ranking rather
than the absolute value of eigenvector due to the uncertainty of interaction Jacobian
approximation (Medeiros et al. 2022). Therefore, we produced another result using the
ranking of the absolute dominant eigenvector, which was compared with the result using
absolute value.

Results

We first examined the changes in abundance of Atlantic cod in the North Sea over the study
period from 1982 to 2021. Using change point analysis, we detected an abrupt decline in the
total abundance in the year 2000, with a drop of more than 60% of the total abundance (**Fig
1a-b**). This decline was mainly attributed to the decrease in the abundance of age groups 1
and 2. Fishing mortality for age 2-4 groups increased from 1982 to 2000, and started to
decline since (**Fig S1**). However, despite relaxed fishing pressure, North Sea cod did not
show significant recovery in the following 20 years.

Next, using S-map, we found that North Sea cod exhibits nonlinear (disequilibrium)
dynamics (**Fig S2**). This justified the need to use a nonlinear approach to estimate the
stability of this population. To estimate time-varying stability of North Sea cod, we used
MDR-Smap to estimate the age group interaction Jacobian of each year, and derived the
absolute value of the dominant eigenvalue (|DEV|) as a population stability index. We found
that throughout the study period, the population fluctuated between stable and unstable states
(**Fig. 1c**). The mean |DEV| between the periods of 1983-2000 and 2001-2021 did not differ;
yet during the second period, the fluctuations have become less pronounced (mean ± standard
deviation for 1982-2000: 092±0.23; for 2001-2021: 093±0.16). Particularly, after year 2008,

the population fluctuated close to the transition threshold ($|DEV| = 1$), imply that the
population is approaching a transition.

We further compared the mean interaction strength of each age group pair between 1983-
2000 and 2001-2021. The interaction strength of each age group pair and year were extracted
from the corresponding Jacobian elements of the interaction matrix of that year. We averaged
these yearly values to generate mean interaction strengths within each period. Overall, the
strongest interaction in the network was the self-interaction link (how change in abundance of
one age influences itself) (**Fig 2, S3**). The mean strengths of these links across periods were
either very strong ($|jacobian|>0.9$) or strong ($0.6 < |jacobian| <0.9$). The second dominant
interaction link in the network was the growth link (how change in one age influences the
next age). The mean strengths of these links were either strong or medium ($0.3 < |jacobian|$
<0.6). There was also a strong positive link from age-2 to age-1 group. All the other links
were weak ($|jacobian|<0.3$).

The major change in the age group interaction network between the two periods was that the
self-interaction link within age-1, age-2, and age-4 groups decreased, while the link within
age-6$^+$ group increased (**Fig 2, S3**). In addition, the growth link from age-1 to age-2 group
decreased. Conversely, the positive link from age-2 to age-1 increased.

Finally, we adopted the eigenvector ranking method to investigate the relative sensitivity of
age groups. Comparing the distribution of these values between each age group within
periods of 1983-2000 and 2001-2021 indicates that, before 2000, the relative sensitivity of
different age groups was similar, although younger groups appeared to have slightly higher
sensitivity (**Fig. 3**). In contrast, after 2000, the relative sensitivity of age-1 group to
perturbations was much higher than other age groups, while the contribution of adult age
groups (i.e. age ≥ 4 years) dropped. Using the rankings rather than the absolute values of the
dominant eigenvector of the Jacobian interaction matrix showed comparable results (**Fig S4**).
This implies that the contribution to stability was shared by the different age classes before
2000, while after 2000, the stability was mainly associated with the high sensitivity of the
age-1 group.

Figures
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Fig 1 Changes in the abundance and stability of the North Sea cod population over time.
(a) Black line indicates the abundance of the total population, and colored lines indicate
abundances of age groups. Dotted vertical line indicates the year 2000, when the abundance
of the population declined sharply, and fishing pressure started to decline in the same year.
(b) Sum of yearly abundance for each age group within the period 1982-2000 and 2001-2021.
The abundance of age groups 1 and 2 declined sharply from the first to the second period.
The ratio above each bar indicates the percent abundance within each period (**c**) Black line
indicates yearly population stability, computed as the absolute value of the dominant
eigenvalue (DEV) from yearly Jacobian interaction matrix of age groups. The dotted black
horizontal line indicates DEV = 1, when the population is at a transition period. A population
is considered stable when DEV < 1 and unstable when DEV > 1. The red line indicates five-
year rolling mean of stability. The mean and standard deviation of yearly stability values
within each period are indicated. The mean DEV does not differ between 1982-2000 and
2001-2021; yet since year 2008, the population fluctuated closer to DEV = 1.
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330 **Fig 2 Interactions between age groups for the two time periods: 1982–2000 and 2001–**
331 **2021.** The thickness of the arrows indicates the mean interaction strength, calculated as the
332 average of yearly values for 1982–2000 (a) and 2021–2020 (b). Interaction strength is
333 quantified as the absolute value of interaction Jacobian estimated from the MDR-Smap
334 method. Here, we classified the interaction strength into four categories.

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Fig 3 Distribution of the yearly relative sensitivity to perturbation of each age group for two periods 1983-2000 and 2001-2021. Each point represents the relative sensitivity of an age group compared to other age groups in a given year. The distribution of yearly relative sensitivity for each age group is summarized using boxplots and violin plots for the first period (a) and the second period (b). The relative sensitivity of each age group was computed as the absolute value of the leading eigenvector for each age group, standardized by the square root of the sum of squares of all six eigenvectors for a given year.

Discussion

Despite reduced fishing pressure on many fisheries in recent decades, more than half of the assessed marine fish populations worldwide still need rebuilding (Worm et al. 2009). While fixed biological reference points are needed to estimate recovery and support management measures, exploited fish populations can exhibit nonlinear dynamics without fixed equilibrium (Glaser et al. 2014). This highlights the importance of accounting for state-dependent dynamics when evaluating the stability of these populations. In this work, we applied a dynamical systems method to investigate North Sea cod, an iconic fish population that suffered from an abrupt decline in 2000 and showed minimal recovery since, despite reduced fishing pressure. We analyzed and compared two time periods, 1982–2000 and 2001–2021, to evaluate (1) population stability, (2) interactions among age groups, and (3) the relative sensitivity of each age group to perturbations.

We found that the stability pattern of the North Sea cod appears to be different between the two periods. During the first period, the population strongly fluctuated between stable and unstable states (crossing frequently the transition threshold of |DEV| = 1, **Fig. 1c**). However, during the second period, particularly after 2008, the population mainly stayed at the stable zone (|DEV| < 1) and very close to the threshold (**Fig 1c**). Although it is hard to conclude if the cod population's stability increased or decreased between the two periods, it seems that the change of the stability pattern followed the abrupt decline in abundance in year 2000.

One might argue that the low abundance during the second period could be the reason for the North Sea cod's stability pattern, which stayed at the stable zone but close to the transition threshold. However, theoretical models show that even low-equilibrium states could be associated with high stability far away from the transition threshold (Dakos et al. 2017). Instead, such pattern of stability remaining close to yet below the transition implies several possibilities. In the best scenario, the population is going to cross the threshold and shift to a new state with higher abundance, as a sign of recovery. Alternatively, the population may shift to an attractor associated with lower abundance, implying further dampening of the population dynamics. Still, the population may move away from the threshold to a higher level of stability, meaning that the population will be "locked in" to its current low abundance state. Our method does not allow us to predict the direction and probability of change, yet the sign of North Sea cod approaching a transition threshold since year 2008 implies a change may occur, requiring attentions from fisheries management. Our finding can also complement other work focusing on forecasting, for example early warning signals (Clements et al. 2019, Grziwotz et al. 2023).

We found some clear differences in the age group interactions between the two periods, which may explain the recovery dynamics of this population. Particularly, after year 2000, the

self-interaction strengths within both age-1 and age-2 groups decreased, while positive links
from age-2 to age-1 group increased (**Fig. 2**). We speculated that these results were related to
a positive density-dependent effect, where the sharp decline in juvenile's abundance
potentially reduces cannibalism and competition, leading to relaxed self-regulation to
promoted survival of the juveniles (Hilborn et al. 2014, Perälä et al. 2022). In addition, the
self-interaction link within age-4 group also decreased during the second period. This has
important implications to population dynamics, because these older spawners can potentially
contribute to larger and higher-quality eggs, promoting reproduction success. On the other
hand, the growth interaction, defined as the positive links from one age to the next, were as
strong as self-interaction links (**Fig. 2**). However, the strength of most growth interactions did
not differ between the two periods. This suggests that even though relaxed self-regulation of
age-1, age-2, and age-4 groups may have promoted their survival and abundance, these
effects did not propagate to increase the strengh of growth toward the next age groups. This
may explain why the North Sea cod has been trapped in the low-abundance state since year
2000.
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In addition to age group interactions, we identified a major change in the relative sensitivity
to perturbations among age groups between the two periods: age-1 group became much more
sensitive to perturbations than older groups at the second period (**Fig. 3**). It is important to
note that the sensitivity of age groups in this study is quantified as how sensitive the
abundance of any age group depends on small perturbations in abundance of other age groups
in the interaction network. In the context of a life cycle within a fish population, the
abundance of juveniles mainly depends on the reproduction success of adults (with minor
impact of cannibalism), while the abundance of adults relies the growth of younger groups.
Based on these assumptions, the increased sensitivity of the age-1 group after year 2000 was
potentially due to impaired reproduction from adult cod with their extremely low abundance.
Another possible explanation is that age-1 group may have become more vulnerability to
environmental forcings due to eroded demography, as documented in some exploited fishes
(Anderson et al. 2008, Hsieh et al. 2010, Hidalgo et al. 2012). On the other hand, while age-
1group became more sensitive to perturbations during the second period, the older groups
became much less sensitive to perturbations (**Fig 3**). If our assumptions remain true, this
result implies that the capacity to grow from one age to the next were impaired in the life
cycle of this population, beginning from the sharp decline of age-1 group since year 2000.
Indeed, we found that the strength of growth from age-1 to age-2 group was reduced since
year 2000 (**Fig 2**), while the growth from age-2 onward did not change; yet the low
abundance of age-1 group may have had a cascading effect on the entire growth chain. In
summary, we speculated that during the second period, failures in reproduction from mature
cod may have led to high sensitivity of age-1 group, while impaired growth chain may have
led to reduced sensitivity of older age groups; these changes led to the population to be
trapped in a low-abundance state until present.
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This study has several limitations. First, we assessed the stability of the entire North Sea cod
population, although recent evidence suggests it may comprise multiple subpopulations with
potential mixing (Holmes et al. 2014). Additionally, our analysis was based on yearly winter
data, as data from other seasons are shorter and less continuous. Winter is the season when
mature cod undertake spawning migrations and aggregate spatially more than in other
seasons (Neat et al. 2014). This spatial restructuring likely influences interactions among
adults and between adults and juveniles. Another key limitation involves the data
requirements for empirical dynamic modeling. At least 35 data points are typically needed to
reliably reconstruct the state space (Sugihara et al. 2012), and the accuracy improves with

longer, less noisy time series (Chang et al. 2017). This issue of the length of time series also
affects other state-dependent approaches for assessing population stability, such as locally
linear autoregressive state-space models for nonlinear dynamics (Ives and Dakos 2012),
lagged time series reconstructions (Grziwotz et al. 2023), or stability proxies like the trace
derived from interaction matrices (Cenci and Saavedra 2019). In this work, our time series
was relatively short with 40 time points. We are therefore aware of potential process and
observation errors when estimating |DEV| (Chang et al. 2021).

Future research can compare the available approaches to provide a comprehensive
understanding of the stability of natural populations. Beyond the standard approach of
estimating maximum sustainable yield in fisheries sciences (Lotze et al. 2011) and
aforementioned state-dependent methods, several other techniques exist for quantifying the
stability of marine fish populations. These include detecting abrupt shifts (Pélissié et al.
2024), identifying regime shifts (Blöcker et al. 2022), analyzing variations in time series
(Hsieh et al. 2006), and detecting early warning signals (Clements et al. 2019). Each method
defines stability differently with unique assumptions. A further systematic comparison of
these methods could help clarify their applicability and improve the understanding of natural
population dynamics across taxa and regions.

Finally, our approach of measuring population stability based on nonlinear dynamics, along
with aforementioned methods in detecting regime shifts and early warning signals (e.g.,
Clements et al. 2019, Möllmann et al. 2021, Pélissié et al. 2024), may be considered to
complement fisheries management advice with biological reference points obtained from
state-of-the-art fisheries stock assessment methods and management strategy evaluations.
These methods provide important information of the state of the populations beyond biomass-
based sustainable indicators, and are more related with their resilience and capacities to
buffer natural and anthropogenic impacts.

Conclusion
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Tracking changes in the stability of low-abundance populations is critical for understanding
the mechanisms behind recovery dynamics. Using an analytical framework based on
dynamical systems, we find that since the abrupt decline in abundance of North Sea cod in
the year 2000, the population fluctuated closer to the transition threshold; some age groups
experienced weaker self-regulation; and age-1 group became more sensitive to perturbations
than older groups. We speculate that despite positive density-dependent effects to promote the
survival of some age groups, impaired reproductive success from adults and reduced capacity
to grow from one age to another resulted in a low-abundance state of cod since year 2000
without a strong sign of recovery. Our findings also demonstrate that the population appears
to approach a transition since year 2008, yet is it unknown whether the abundance of the
population is going to increase, decrease, or whether the age structure of the population will
change. In any case, more attention in managing and preserving this population is important.
Currently, commercial catches of the North Sea cod are predominantly composed of juveniles
under three years old, with bycatch and discard rates estimated at 23% by weight of the total
catch in 2023 (ICES 2024). Given the high sensitivity of juveniles to perturbations and their
strong dependence on the recruitment of adults, it is critical to protect the entire population
from overfishing and to preserve their habitats to ensure the sustainability of the population.
The recovery of North Sea cod is also facing challenges in the rising ocean temperatures,
increasing frequency and intensity of extreme events (IPCC 2023), and the potential
irreversibility of regime shifts in the North Sea (Sguotti et al. 2022). Beyond Atlantic cod in

the North Sea, several other exploited fish populations in this region also exhibited regime-shift dynamics (Blöcker et al. 2023). Our analytical framework is broadly applicable to other natural populations across taxa and regions with biomass or abundance time series for size, age, or life stages within the populations. More importantly, it enables the estimation of within-population interactions and sensitivities to perturbations, providing valuable insights to understanding recovery dynamics and informing conservation efforts.

Code and data availability

All the data used this study were downloaded from open-access online databases as mentioned above. We used "rEDM" package (https://cran.r-project.org/src/contrib/Archive/rEDM, version 1.2.3) to perform all the analysis. The MDR S-map was performed using functions provided in Chang et al. (2021). All statistical analyses were performed in R 4.3.1. Data and codes for reproducing the results are deposited in Dryad https://datadryad.org/stash/share/J51GkKEfPNjlyiVhSccjYz-qDbtnx3O_1wbaK7CjXL4.

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