Signaling of trans-saccadic prediction error by foveal neurons of the monkey superior colliculus

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33   **Abstract**
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Across saccades, neurons in retinotopically organized visual representations experience
drastically different images, but visual percepts remain stable. Here we investigated whether
such stability can be mediated, in part, via prediction-error signaling by neurons processing
post-saccadic visual images. We specifically recorded from foveal superior colliculus (SC)
neurons when a visual image only overlapped with their response fields (RF's) after foveating
saccades but not pre-saccadically. When we rapidly changed the target features intra-
saccadically, the foveal neurons' post-saccadic visual reafferent responses were elevated,
even though the neurons did not directly sample the pre-saccadic extrafoveal target
features. This effect did not occur in the absence of saccades, and it also scaled with the
extent of the introduced intra-saccadic image feature discrepancies. These results suggest
that foveal SC neurons may signal a trans-saccadic prediction error when the foveated image
stimulating them is inconsistent with that expected from pre-saccadic extrafoveal
representations, a potential perceptual stability mechanism.
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Introduction

Sensory systems benefit from spatial and temporal continuity of incoming information streams. Often, such continuity is disrupted, whether through exogenous environmental factors or through self-movement. One example such disruption occurs every time we generate a rapid eye movement. Across saccades, which we typically use to foveate relevant extrafoveal image patches, retinotopic representations of foveal visual inputs can experience drastically different images. For example, when viewing a painting like the Mona Lisa, we might generate a saccade from a foveated image patch containing the model's eye to one containing her mouth. In this case, the pre-saccadic extrafoveal image of the mouth is rapidly translated to become the post-saccadic foveal image; thus, the pre- and post-saccadic foveal visual images are decidedly different from each other. Despite that, our percept of the portrait remains seamless.

The question of perceptual stability across saccades has intrigued scientists for many decades [1-8]. Among the theories invoked for such stability are ones utilizing a form of prediction (meant in the phenomenological sense) of the visual consequences of eye movements [3,9]. Conceptually, such prediction may be thought of as a template matching between newly incoming foveal visual information and the expected appearance, obtained a priori, of the post-saccadic foveal image [3,9]. Such matching could arise, for example, by relaying a pre-saccadic extrafoveal preview of the eye movement's target [10] to neurons processing the newly foveated visual evidence. Here, we searched for a neural correlate of such a process in the visual responses of foveal superior colliculus (SC) neurons. We specifically asked whether these neurons' post-saccadic reafferent responses (after target foveation) are sensitive to the pre-saccadic extrafoveal image appearance, even when such extrafoveal visual input never activated the neurons' classic response fields (RF's) pre-saccadically. If so, then this would suggest a potential trans-saccadic dispatching of extrafoveal pre-saccadic visual information to the foveal SC.

The SC is particularly attractive for exploring hallmarks of extrafoveal-to-foveal trans-saccadic integration. First, SC neurons exhibit sufficiently varied feature tuning properties [11], allowing us to investigate reafferent visual responses for different image manipulations. Importantly, such feature tuning endows extrafoveal SC neurons with integrated evidence about the extrafoveal appearance of saccade targets [11]; while likely not enough to process very fine details [11-13], this integrated evidence can provide a sufficient [13-15] pre-saccadic preview. Second, the SC possesses a putative mechanism for relaying exactly such an extrafoveal preview to the rest of the visual system (including foveal representations) at the time of saccades [16-19]. In particular, SC motor bursts, time-locked to saccade onset [20], embed within them a representation of the visual properties of the extrafoveal saccade target [16,17,19]. Thus, whether through intra- or extra-collicular connections, SC foveal representations [21] can be "informed" about extrafoveal saccade target appearance, despite not being directly visually-stimulated by the saccade target pre-saccadically. Finally, the SC signals salience [22-25]; hence, trans-saccadic integration by foveal SC neurons would be functionally useful to signal failures of image stability. In other words, potential inconsistencies between experienced versus expected foveal images constitute salient events worthy of flagging, so detecting them is desirable.

Here, we show that foveal SC neurons are indeed sensitive to the pre-saccadic extrafoveal
target appearance, despite never being stimulated by the extrafoveal targets before the eye
movements. We also show that such sensitivity is contingent upon saccade generation,
depends on extrafoveal target visibility, and scales with the extent of sensory conflict
experienced between pre-saccadic extrafoveal and post-saccadic foveal image appearances.
We suggest that the SC is endowed with mechanisms for signaling salient events in the
temporal domain [26-28], such as happens trans-saccadically, and not just in the image-based
one [22-25].

Results

Foveal superior colliculus neurons detect unexpected trans-saccadic stimulus
changes

We recorded from foveal SC neurons while monkeys generated visually-guided saccades to
extrafoveal images containing different spatial frequency textures[12,13,16,29] (Methods). In our
basic condition, the saccade target was a circular patch containing one of two possible
spatial frequencies, and it appeared either to the right or left of fixation (Methods). A
saccade "go" signal was provided a few hundred milliseconds later, after which the monkeys
foveated the circular patch (Fig. 1a). The patch itself never moved on the display, but it was
rapidly translated on the retina by saccades, eventually entering the RF's of our recorded
foveal SC neurons and visually stimulating them.

We employed a strict selection of neurons to include in our analyses (Methods). Specifically,
we ensured that the neurons were not visually-stimulated by the saccade target except after
eye movement generation. Thus, we only accepted neurons with foveal RF's that were not
visually-driven (before the saccades) by the extrafoveal image patch (RF's were estimated
through a mapping task run before our main paradigm; Methods). Fig. 1b shows an example
such RF, with the white circle indicating the size of the saccade-target image patch (were the
eye to be perfectly aligned with the patch's center). In the actual experiment, this patch was
centered at an eccentricity of 8 deg before the saccade, and was thus far from the neuron's
RF; however, the same patch was large enough to clearly visually drive the neuron after the
eye movement has ended (i.e. after the patch was retinally translated towards the fovea by
the saccade). We confirmed these two points by measuring the neuron's activity after
extrafoveal stimulus onset and also upon saccade generation. In the former case, there were
no visually-evoked bursts (Fig. 1c shows the neuron's activity when extrafoveal image
patches containing two different spatial frequency textures appeared; Methods). If anything,
there was a transient reduction in baseline activity, particularly for the high spatial frequency
texture. Such transient reduction has been observed before upon extrafoveal stimulus onset
(for examples, see ref. [30]), and it can aid in subsequent winner-take-all processes needed to
recruit the extrafoveal saccade-related motor bursts [31]. Upon saccade generation, the
neuron now exhibited a visual reafferent response caused by translating the saccade-target
image into its RF (Fig. 1d). Importantly, by employing two different spatial frequencies, we
ensured that this response was visual in nature, because it depended on the visual

appearance of the foveated saccade target [29]. For example, the reafferent response of the
neuron of Fig. 1b, c was earlier and stronger for the low spatial frequency texture, as might
be expected [29] (Fig. 1d).

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Figure 1 Testing for trans-saccadic prediction error signaling by foveal SC neurons. (a) Monkeys generated a
delayed, visually-guided saccade towards an extrafoveal target. We used a delayed paradigm to make sure that
there was a stable visual image upon saccade generation. In some trials, the saccade target was unchanged
throughout the whole trial (high spatial frequency grating embedded within a circular patch for this shown
example). In other trials, we detected saccade onset and immediately flipped the saccade target to another
feature (from a low to a high spatial frequency texture in the shown example; Methods). **(b)** We only selected
foveal SC neurons with response fields (RF's) not extending towards the pre-saccadic extrafoveal stimulus
location. In this example, the RF was almost entirely contained within <2 deg eccentricity. Each black dot is a
stimulus onset location during RF mapping, and the white circle (3 deg radius) shows the extent of the saccade
target if it was perfectly foveated post-saccadically. The target covered the RF post-saccadically but not pre-
saccadically. The z-axis indicates the visual response strength of the neuron at each stimulus location (Methods).
(c) Activity of the same example neuron when the extrafoveal stimulus appeared. There was no visual response,
confirming that the pre-saccadic stimulus did not drive the neuron. The faint lines show eye position traces (the
monkey was still fixating the central fixation spot). **(d)** After saccades, the neuron exhibited a visual reafferent
response to the image feature entering its RF. Note how the neuron completely paused intra-saccadically and
only responded after the new visual evidence entered its RF (there was additionally a pre-saccadic transient
elevation before the pause due to the release of fixation, which we do not focus on in this study). Note also that
the neuron was visually-tuned to the low spatial frequency [12,29]. The faint lines indicate eye position traces,
showing how the neural modulations were time-locked to saccade onset. Error bars denote SEM, and numbers
of trials are evident from the rasters.

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Having established that our neurons were not visually stimulated by the pre-saccadic
extrafoveal stimuli (Fig. S1), we next analyzed the situation in which there was an image
mismatch between the experienced post-saccadic visual stimulus and the pre-saccadic
(extrafoveal) target image. For each saccade to a given image feature (low or high spatial
frequency), we had two conditions: no change in the image feature across the saccade

(control), or an instantaneous intra-saccadic change (to the other spatial frequency;
Methods). For example, if the pre-saccadic image had a high spatial frequency texture, then,
during the saccade, we flipped it to the low spatial frequency texture. Thus, the foveal
neurons experienced a visual feature different from that expected from the extrafoveal pre-
saccadic feature, but these neurons were never directly stimulated by the extrafoveal
feature pre-saccadically. We used instantaneous eye position to detect saccade onset and
updated the display accordingly (either fictively in the control condition or actually;
Methods). This allowed us to compare the visual reafferent response for the same image
feature in the fovea (e.g. landing on a low spatial frequency), but either when the
extrafoveal pre-saccadic image was the same (low spatial frequency) or different (high
spatial frequency).
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Figure 2a shows example radial eye speed traces for rightward saccades from the same
session of the example neuron of Fig. 1. Here, we aligned all traces to the end of the
stimulus update on trials in which the saccade target flipped from containing a high to a low
spatial frequency texture during the saccade (similar results were obtained for the other
image flip condition). As can be seen, the stimulus update was intra-saccadic, and the eye
speed by the end of the stimulus change was systematically higher than ~100 deg/s. Thus,
given that the gratings were vertically oriented and the saccades were predominantly
horizontal, this ensured substantial blurring of both spatial frequencies on the retina by the
ongoing eye movements (and during the image change). In Fig. 2b, we plotted the visual
reafferent response of the same example neuron of Fig. 1, but now aligned to the time of
intra-saccadic stimulus update completion in all trials. In both shown conditions, we were
measuring the neuron's visual reafferent response for the same post-saccadic foveal
stimulus (low spatial frequency); the only difference is that, in one case (blue), the
extrafoveal pre-saccadic image was the same (control; low-to-low spatial frequency from
pre-saccadic to post-saccadic image appearances); in the other (yellow), it was different
(high-to-low spatial frequency change). The neuron's visual reafferent response was elevated
when there was a mismatch in the pre-saccadic image, even though the foveated visual
feature was the same as in the control condition. This was the case even though the
extrafoveal image location was outside of the neuron's RF before the saccade (Fig. 1).
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The same observation was also made when the post-saccadic foveal visual image feature
was the high spatial frequency (Fig. 2c). Again, the neuron's reafferent response was
elevated (relative to control) when there was a mismatch with the pre-saccadic extrafoveal
saccade-target appearance (i.e. when the pre-saccadic image was a low spatial frequency).
Note that there was no other change in the firing patterns of the neuron in Fig. 2b, c, for
example in the reafferent response timing on stimulus change trials. This suggests that we
were not observing a simple superposition of the original reafferent response and an
additional sensory drive by the stimulus flip event; rather, there was a modulation of the
otherwise-normal reafferent response, as if it was more salient than expected. Thus, this
example foveal SC neuron signaled a trans-saccadic change in the saccade-target
appearance, even though it did not "see" the saccade target pre-saccadically.
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Figure 2 Signaling of trans-saccadic prediction error by the foveal SC. (a) Radial eye speed traces from the same session as in Fig. 1b-d when the monkey was generating foveating saccades. Here, we aligned the traces to the end of the stimulus update event (on trials in which the pre-saccadic extrafoveal texture was of high spatial frequency and the post-saccadic foveal feature was a low spatial frequency texture). Eye speed was consistently >100 deg/s during stimulus updates (also see Fig. S2). **(b)** Relative to control (blue; same data as in Fig. 1), the initial reafferent response of the neuron was elevated (yellow). This happened even though the neuron was not stimulated by the pre-saccadic extrafoveal stimulus (Fig. 1). **(c)** Similar observations when the foveated image feature contained a high spatial frequency; in this case, the control condition also contained a high spatial frequency pre-saccadically. Thus, the neuron's visual reafferent response was systematically elevated when the experienced post-saccadic visual feature was different from that expected based on the pre-saccadic extrafoveal target appearance; this was despite the lack of visual stimulation of the neuron pre-saccadically by the extrafoveal saccade target (Fig. 1). Error bars denote SEM, and numbers of trials in each condition are evident from the individual traces and rasters.

Across neurons and sessions, we confirmed that all of our stimulus updates were intra-saccadic (Fig. S2). At the level of reafferent responses, there was a systematic elevation of their magnitudes, for each spatial frequency, if the pre-saccadic image contained a different feature from that experienced foveally after the saccade. This result can be seen in Fig. 3a, b. For each neuron, we measured the strength of the visual reafferent response (peak firing rate in a prescribed interval after the end of the real or fictive stimulus update; Methods). We did this twice: once when the pre-saccadic extrafoveal visual image was the same as that stimulating the foveal RF after the saccade (control), and once when the pre-saccadic extrafoveal image was of a different spatial frequency (intra-saccadic image change). We then plotted the two values against each other. Figure 3a shows the condition when the foveated stimulus had a low spatial frequency texture; the reafferent response to this texture was elevated if it was inconsistent with the extrafoveal pre-saccadic texture's spatial frequency (p=4.91x10^{-8}; Wilcoxon signed-rank test). Figure 3b shows the results from the same neurons when the foveated stimulus was a high spatial frequency and the extrafoveal stimulus in the image flip condition was a low spatial frequency (p=0.0031; Wilcoxon signed-rank test). In both cases, the reafferent response expected from a particular visual feature in

the RF (low or high spatial frequency) was systematically elevated when the visual feature was unexpected based on the extrafoveal pre-saccadic feature. This is a hallmark of prediction-error signaling.

Figure 3 Consistency of trans-saccadic error signaling by foveal SC neurons. (a) Reafferent response strength (Methods) on trials with an intra-saccadic spatial frequency change versus reafferent response strength on control trials. In both cases, the foveated image feature was the low spatial frequency texture within the circular patch of the saccade target. There was a systematic elevation of reafferent response strengths across the population when there was a visual feature inconsistency across saccades. **(b)** Similar results for the case in which the foveated texture had a high spatial frequency. **(c, d)** Neural modulation indices (Methods) for the results in **a**, **b**. For both foveated image features, there was a systematic elevation of foveal neuron visual reafferent response strength when the experienced post-saccadic image was inconsistent with that expected from the pre-saccadic target appearance. In each panel, the solid vertical line indicates the mean of the distribution, and the dashed vertical line indicates the median.

We also created a neural modulation index for each foveated image spatial frequency. This index was calculated by subtracting the reafferent response strength on the control condition from that in the image flip condition and then dividing by the sum of response strengths (Methods). Again, there was a systematic elevation of reafferent response strengths when the experienced post-saccadic foveal visual image feature was not consistent with that expected from the pre-saccadic extrafoveal visual appearance of the saccade target. Statistically, comparing population modulation indices to zero revealed significant elevations for both the low ($p=1.47 \times 10^{-7}$; Wilcoxon signed-rank test) and high ($p=0.0119$; Wilcoxon signed-rank test) spatial frequency foveated targets. Thus, foveal SC neurons

290 signaled the occurrence of intra-saccadic stimulus changes, a kind of prediction error from
291 the expected pre-saccadic extrafoveal target image appearance.
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We also considered the possibility of systematic differences in landing positions across pre-
saccadic target spatial frequencies and sessions. These did indeed exist (due to expected
variances in saccades), but the retinotopic positions of the foveated image patches were
always encompassing our neurons' RF hotspot locations (Fig. S3a). Moreover, variations in
landing positions by the saccades across conditions (thus causing variations in foveated
retinotopic image positions relative to the foveal RF's) would not be expected to always
systematically elevate reafferent visual responses; rather, they might equally likely also
diminish responses if the eye landing position resulted in a sub-optimal visual stimulation of
the RF by the image patch. This was clearly not the case in our data (Fig. 3).
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Therefore, our results so far indicate that, even though our foveal SC neurons were not
directly visually stimulated pre-saccadically by the extrafoveal saccade targets, they were
still, nonetheless, sensitive to these targets' pre-saccadic appearances: intra-saccadically
introduced conflicts in post-saccadic target appearances resulted in elevated reafferent
response magnitudes. Such elevation, under prediction error situations, is a hallmark of
predictive coding in a variety of brain areas [7,8,32-35].
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311 *Independence of trans-saccadic error signaling from neuron preference*
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We next checked whether an individual neuron's preference for a particular foveated image
feature dictated whether the neuron was sensitive to a conflict with pre-saccadic image
features. We assessed neuron preference from the control conditions of Figs. 1-3: we
measured the reafferent response strength when foveating a low spatial frequency (that was
unchanged across the saccade) and compared it to the case when the saccade landed on a
high spatial frequency (again with no intra-saccadic change). In our database, 30/81 neurons
(37.04%) had numerically stronger visual reafferent responses when the foveated image
feature was a high spatial frequency, whereas 51/81 neurons (62.96%) responded more
strongly for the low spatial frequency patch. This is consistent with SC neurons generally
preferring low spatial frequencies [12,29] (Fig. 4a). Next, we plotted the results of Fig. 3a, b
against each other. Specifically, we measured, for each neuron, the difference in reafferent
response strength between the low-to-high image flip condition and the corresponding
control scenario (high-to-high), and we plotted it against the difference between the high-to-
low image flip condition and the corresponding control condition (Fig. 4b). There was no
correlation between the two measures (r = 0.0062; p = 0.956), suggesting that we were not
merely observing a single, universal sensitivity (per neuron) for just any intra-saccadic image
update. Moreover, when we colored the neurons according to whether they preferred high
or low spatial frequencies in Fig. 4a, we found that neurons from both groups could signal a
trans-saccadic inconsistency in foveated image appearance (by elevated reafferent response
strengths; Fig. 4b), and for both types of spatial frequency changes. For example, 38/51
neurons (74.5%) preferring the low spatial frequency had an elevated reafferent response
when the pre-saccadic image was of a high spatial frequency. For the neurons preferring the
high spatial frequency, 17/30 neurons (56.7%) signaled a trans-saccadic inconsistency by
elevating their reafferent response strengths (even though this proportion was less than for

neurons preferring the low spatial frequency, the trend was still in the same direction). Thus, the results of Fig. 2, 3 were a general property of our population, and could happen regardless of individual neuron preferences for the foveated image features.

Figure 4 Elevations of foveal reafferent response strengths with trans-saccadic image inconsistencies for both neurons preferring low and neurons preferring high spatial frequency textures. (a) We assessed neuron preferences for low or high spatial frequency textures based on their reafferent responses in the control trials. More neurons preferred low spatial frequencies, as might be expected [12,29]. The different colors are used to help in classifying the different neuron groups in **b**. **(b)** For the same neurons, we plotted whether they elevated or decreased their reafferent responses on image-flip trials. Neurons with both preferences in **a** could elevate their reafferent responses with trans-saccadic image inconsistencies. Thus, there was no systematic dependence of the results of Figs. 2-3 on neuron preferences.

In Fig. 4b, there were additional interesting differences in the foveal neurons' abilities to signal intra-saccadic stimulus changes in their reafferent responses. For example, when landing on a low spatial frequency image patch (x-axis), trans-saccadic error signaling seemed to be slightly more systematic than when landing on a high spatial frequency image patch, independent of neuron preferences (79.01% of all neurons elevated their reafferent response strength in the former case, as opposed to 67.9% in the latter, but this difference was not significant; p>0.5; binomial distribution fit). In addition, going from a low spatial frequency pre-saccadic extrafoveal image to a high spatial frequency post-saccadic foveal image had neurons with more marked modulations in either direction (elevations or reductions relative to control; y-axis). These observations might suggest two possibilities. One, it could be that the SC might favor certain types of trans-saccadic image inconsistencies to "flag" by its foveal neurons (such as high-to-low spatial frequency image flips). Alternatively, since high spatial frequencies are significantly less visible and less salient than low spatial frequencies extrafoveally (due to visual acuity and contrast sensitivity functions of the visual system), a flip from high to low spatial frequency may elicit a more robust prediction error signal (on average) than a flip from an already highly salient extrafoveal

373 image feature (low spatial frequency) to a less salient one. In a later experiment described
374 below, we show evidence consistent with this latter possibility.
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377 *Trans-saccadic error signaling does not occur with simulated saccades*
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To check whether a saccade was needed for foveal neurons to signal a trans-saccadic
inconsistency between extrafoveal and foveal visual image appearances, we also ran a
simulated saccade condition. In this condition, the monkeys always maintained gaze fixation,
and we rapidly translated the extrafoveal image patch (initially appearing to the right or left
of fixation at the same eccentricity as in the active saccade task) towards the fovea
(Methods). On some trials, the patch had a fictive image change (control), and, on others, it
had a real one, just like in the saccade task. Naturally, due to our discretized (both spatially
and temporally) display, we could not mimic the exact saccadic eye movement profile, but
we used a similar duration and peak speed of image translations (Methods).
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During maintained fixation, externally translating extrafoveal images into the neurons' foveal
RF's did not elevate the neurons' visual responses to the stimuli on the image flip conditions
relative to control; that is, there was no added spiking when the experienced foveal image
feature was different from the pre-translation extrafoveal one. Consider, for example, Fig.
5a, b, showing the responses of the same neuron of Figs. 1, 2 but in the simulated saccade
condition. First, it should be noted that the neuron's activity was not completely paused
during the image translation phase of the trials (compare Fig. 5a, b to Fig. 2b, c around the
time of the stimulus update event). This is expected: the image translation in this condition
was no different (conceptually) from a stimulus onset event used in many visual
neurophysiology experiments; thus, the neuron just maintained its baseline firing rate until
new sensory evidence entered into its RF. On the other hand, during real saccades,
extrafoveal neurons were bursting and, simultaneously, foveal neurons paused [30,36-38]. More
importantly, the same neuron's response to the afferent sensory input itself (the circular
patch entering it's RF) was the same, for a given spatial frequency, irrespective of the image
flip condition. That is, when the stimulus entering the RF was a low spatial frequency, it did
not matter whether the initial extrafoveal stimulus was a low or high spatial frequency (Fig.
5a). Similarly, when the stimulus entering the RF was a high spatial frequency, it did not
matter whether the extrafoveal stimulus was the same or different (Fig. 5b). We also
assessed this statistically: we measured the peak firing rate in a prescribed interval
(Methods) from (fictive or real) stimulus update time; whether the final foveal stimulus was
of low or high spatial frequency, there was no difference in visual response strength relative
to the corresponding control condition ($p=0.1303$; Wilcoxon rank sum test comparing low-
to-low and high-to-low; and $p=0.1260$; Wilcoxon rank sum test comparing high-to-high and
low-to-high trials). Thus, besides confirming our earlier assertion that our foveal neurons
were not sensitive to extrafoveal image appearance during fixation, these results indicate
that signaling of trans-saccadic extrafoveal-versus-foveal image inconsistencies in Figs. 2-4
above was contingent upon saccade generation.
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Figure 5 Lack of foveal neural response elevations in the absence of real saccadic eye movements. (a, b) Responses of the same example neuron of Figs. 1, 2, but this time in the absence of saccades. The monkey maintained gaze fixation, and we rapidly translated the extrafoveal image patch to the fovea (Methods). This resulted in a visual response to the patch entering the neuron's RF, and there was no prior pause in neural activity because there was no actual saccade generation (compare to Figs. 1, 2). Importantly, whether there was an intra-translation image flip or not, the neuron simply reflected the visual appearance of the final foveal stimulus in its RF. Thus, the neuron was neither sensitive to the pre-translation extrafoveal appearance, nor was it sensitive to an intra-translation image change. **(c-f)** Analyses similar to those in Fig. 3, demonstrating a lack of foveal response elevations in the absence of saccades. Error bars denote SEM, and all conventions are like in Figs. 2, 3 above.

Across the population, we reached similar conclusions. Figure 5c-f shows results of analyses
like those in Fig. 3, but for the present simulated saccade condition. For each foveated image
feature, there were no statistically significant differences between control and image flip
conditions (p=0.44 in Fig. 5c and p=0.055 in Fig. 5d, Wilcoxon signed-rank test in each case;
and p=0.71 in Fig. 5e and p=0.09 in Fig. 5f, Wilcoxon signed-rank test in each case), indicating
that the foveal neurons did not "detect" a change from pre-translation extrafoveal image
appearance like we saw with real saccades. Consistent with this, there was no significant
correlation between the effects of real and simulated saccades in the neurons in which we
ran both conditions within the same session (Fig. S4; r=-0.1034, p=0.4701 for panel **a**; r=-
0.1703, p=0.2323 for panel **b**).

Thus, when foveal SC neurons were visually-stimulated through exogenous means, and not
through self-generated saccades, they expectedly only reflected the instantaneous sensory
evidence entering into their RF's. Signaling of trans-saccadic inconsistencies between
extrafoveal and foveal image appearances by foveal SC neurons was contingent upon
saccade generation.

Extrafoveal stimulus visibility interacts with trans-saccadic error signaling

Because extrafoveal visual acuity is not as good as that in the fovea, including in the SC's
retinotopic visual field representation [21,39], one should not necessarily expect universally
successful signaling of trans-saccadic prediction errors by foveal SC neurons. Specifically, if
the relevant extrafoveal visual feature was only subtly changed intra-saccadically, then trans-
saccadic elevations of foveal SC reafferent responses might be reduced or eliminated: when
extrafoveal visibility is already limited, there is little evidence to allow signaling a trans-
saccadic image mismatches.

To test this, we employed object shape changes; rather than changing the spatial frequency
of the texture inside the saccade target across saccades, we changed only the outline form
encompassing the texture. For either a low or high spatial frequency texture, the pre-
saccadic extrafoveal target was a circle, and the post-saccadic foveal target was now a
square. These trials were interleaved with all of the other trials of Figs. 1-4 (Methods). We
hypothesized that, with the low spatial frequency texture, extrafoveal target visibility was
dominated by the highly salient texture and not by the outline shape (especially for SC
neurons preferring low spatial frequencies [12]). On the other hand, with the less salient fine
texture, the form (circle versus square) could be better distinguished extrafoveally, and
could, in turn, be sensed by the foveal neurons if it was changed trans-saccadically. Thus, we
expected that trans-saccadic signaling of shape changes (between the pre-saccadic
extrafoveal and post-saccadic foveal image scenarios) would be weakened with the low
spatial frequency texture embedded within the shape.

Figure 6a, b shows the results of the same example neuron of Figs. 1, 2, 5 under these
additional image manipulations. When the shape of the saccade target was changed across
saccades, this change was only detected by the foveal SC neuron when the texture inside the
shape was a high spatial frequency. We also confirmed this statistically. Across trials, the
peak visual reafferent response in the shape-change trials was not different from that in the

control trials for the low spatial frequency texture embedded within the saccade targets
(p=0.7587; Wilcoxon rank sum test; Fig. 6a). However, the reafferent response was elevated
relative to control in the shape-change trials when the embedded texture was of high spatial
frequency (p=2.67x10^{-4}; Wilcoxon rank sum test; Fig. 6b).
482
Such an effect was also present across the population (Fig. 6c-f, using similar formatting to
earlier figures). When the pre- and post-saccadic targets contained within them a low spatial
frequency texture, the median modulation index across the population was 0.0161 (Fig. 6e).
This was lower than the median modulation index seen in Fig. 3c when landing on a low
spatial frequency texture (median 0.0541; p=0.0228; Wilcoxon signed-rank test comparing
the modulation indices in the two conditions). This suggests weakening of trans-saccadic
prediction error signaling when the trans-saccadic change was rendered more subtle (also
see below for further evidence of such scaling effects). Interestingly, when the embedded
texture was of a high spatial frequency, putatively rendering the shape change more visible
due to the lower salience of high spatial frequencies, there was no difference in modulation
indices between the shape-change trials (Fig. 6f) and the spatial-frequency change trials (Fig.
3d; p=0.6530; Wilcoxon signed-rank test comparing the modulation indices in Figs. 3c, 6f).
Once again, these results were not an outcome of variability in saccade landing positions
(Fig. S3b).
497
498 Therefore, trans-saccadic signaling of inconsistencies between experienced and expected
499 foveal visual target appearances by SC neurons may fail when the limits on pre-saccadic
500 extrafoveal preview visibility are reached.
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Figure 6 Generalizability of trans-saccadic error signaling to the case of intra-saccadic outline shape changes.
(a) Visual reafferent responses of the same foveal neuron of Figs. 1, 2, 5. Here, we compared the control condition (blue; same as in Figs. 1, 2) of landing on a circular target containing a low spatial frequency texture to the one in which only the outline form was changed (but the foveated texture unaltered). There was no elevation of reafferent response strength by the intra-saccadic image change. We hypothesize that the salient low spatial frequency texture dominated the pre-saccadic visibility of the extrafoveal target, rendering the shape harder to discern pre-saccadically. **(b)** Consistent with this, when the embedded texture was a high spatial frequency, and thus putatively less salient, a trans-saccadic shape mismatch was successfully detected by the neuron. **(c, d)** Same as in Fig. 3a, b, but for the shape-change manipulation. Across the population, there was a significant elevation in both cases (p=0.0025 in **c** and p=0.0056 in **d**; Wilcoxon signed-rank test). **(e, f)** For the neural modulation indices, there was also a positive population index in both cases (p=0.03 in **e** and p=0.0016 in **f**; Wilcoxon signed-rank test). However, as mentioned in the text, the modulation indices in **e** were significantly weaker than those in Fig. 3c, suggesting a weaker effect of the shape changes when the embedded textures were of low spatial frequency. All conventions are similar to those in Figs. 2, 3.

Scaling of error signaling by combined image conflicts

Finally, our shape-change experiments allowed us to next test combined image manipulations. On intra-saccadic image flip trials, we now flipped both the spatial frequency and the encompassing outline form at the same time. This way, we could ask whether signaling of trans-saccadic prediction errors by foveal SC neurons may be viewed as just an "event detector" of any trans-saccadic image inconsistency, or whether the signaling strength might scale with the magnitude of the feature changes generated by the intra-saccadic image flips. From the comparisons made between the neural modulation indices of Figs. 3, 6, we had reason to believe that trans-saccadic prediction error signaling by foveal SC neurons is more than just a simple event detection process.

At the individual neuron level, consistent with the differences between the Fig. 3 and Fig. 6 population results, we did indeed notice that the modulation of reafferent response strengths on combined feature change trials could be significantly stronger than its modulation on individual feature change trials. For example, Fig. 7 shows the results of the same neuron as in Figs. 1, 2, 5, 6 above, but now with both a shape and spatial frequency change across saccades. When saccades landed on a low spatial frequency texture (plus a changed shape; Fig. 7a), there was an elevated reafferent response relative to control, and this elevation was larger in magnitude than that observed on either the spatial-frequency (Fig. 2b) or shape (Fig. 6a) change trials alone: the difference in peak reafferent response from control was 26.82 spikes/s in the combined change trials, whereas it was 16.11 and 1.02 spikes/s in Fig. 2b and Fig. 6a, respectively. When the saccades landed on a high spatial frequency target instead, and again in the combined change trials (Fig. 7b), the reafferent response elevation was larger than that observed on the shape-only trials (Fig. 6b; 38.74 versus 19.01 spikes/s), and also more robust than that observed for the spatial frequency trials alone (Fig. 2c; 38.74 versus 27.06 spiks/s). Thus, combining multiple intra-saccadically altered image features strengthened the elevations of reafferent response magnitudes caused by inconsistencies between the pre- and post-saccadic visual image appearances.

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Figure 7 Scaling of trans-saccadic prediction error signaling by foveal SC neurons with combined intra-saccadic
feature changes. (a, b) Results from the same example neuron of Figs. 1, 2, 5, 6. Here, relative to the same control
trials of Figs. 1, 2, we checked reafferent responses when both the outline shape and the embedded spatial
frequency texture within it were altered intra-saccadically. Both when landing on a low (**a**) or high (**b**) spatial
frequency texture, the reafferent responses of the neuron were elevated more strongly than either for only the
spatial frequency (Fig. 2) or for only the shape (Fig. 6 changes) change trials. **(c, d)** Consistent trans-saccadic error
elevations in foveal neuron reafferent responses were observed across the population (p=0.0033 for **c** and
p=6.22x10^{-5} for **d**; Wilcoxon signed-rank test). **(e, f)** Similarly, population modulation indices were also positive
(p=0.0023 for **e** and p=6.6x10^{-5} for **f**; Wilcoxon signed-rank test). Error bars denote SEM, and all conventions are
the same as in earlier figures.
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Next, after confirming that the combined image feature inconsistencies still caused trans-
saccadic error signaling in our population (Fig. 7c-f), we tested to what extent the neural
modulation indices on combined (shape plus spatial frequency) image trials approached the
sum of the neural modulation indices obtained in the individual image manipulations
separately. Specifically, our control trials were the same for both types of experiments, since
these control conditions constituted only circular saccade targets and a single spatial
frequency (Methods). Thus, on trials with only spatial frequency flips or only shape flips, the
control condition that we were comparing to was the same. This allowed us to compute
neural modulation indices on the trials with combined image changes and see whether they
approached the sum of the individual modulation indices.

For each neuron, we plotted, on the x-axis, the sum of neural modulation indices obtained
from the modulation indices of the individual image manipulations (shown in Figs. 3 and 6).
Then, on the y-axis, we plotted the actual (measured) neural modulation indices obtained
from the combined image manipulations (Fig. 7e, f). There was indeed a clear positive
correlation, both when landing on a low (Fig. 8a; r=0.6632; p<0.000001) and high (Fig. 8b;
r=0.8521; p<0.000001) spatial frequency texture. Therefore, signaling of trans-saccadic
prediction error by foveal SC neurons does scale (albeit sub-additively when landing on a low
spatial frequency texture) with the amount of feature conflicts experienced by the neurons.

We should also emphasize here that we additionally ran the simulated saccade experiments,
on the same neurons as in Fig. 5, with the shape-only and combined (shape plus spatial
frequency) change experiments. In both cases, we did not observe systematic elevations in
sensory responses to the afferent signals received by the translating images into the
neurons' RF's. This can be seen in Fig. S5.

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Figure 8 Scaling of trans-saccadic error signaling in the foveal SC by combined intra-saccadic image changes.
(a, b) When landing on either a low (**a**) or high (**b**) spatial frequency texture, we computed on the x-axis the sum
of modulation indices obtained from the experimental trials with only spatial frequency intra-saccadic changes
(Fig. 3) and only shape changes (Fig. 6). Then, on the y-axis, we calculated the actual measured modulation
indices from the trials containing both spatial frequency and shape intra-saccadic image updates. In both cases,
there was a clear positive correlation, suggesting a scaling of prediction error signaling effects in the foveal SC
with the magnitude of feature inconsistencies across saccades (correlation coefficients are indicated in each
panel; p<0.000001 in each case).

Discussion

In this study, we investigated the activity of foveal SC neurons [21] as these neurons were visually stimulated by saccade-induced translations of extrafoveal visual stimuli into their RF's. We tested the hypothesis that foveal SC neurons can receive, trans-saccadically, an expected appearance of the foveated saccade target (based on this target's pre-saccadic visual features). We picked only neurons that were not visually stimulated by the extrafoveal saccade target. Then, during the saccade, we altered the target's appearance, such that the post-saccadic foveated image feature (now visually driving the neurons) was different from that expected from the pre-saccadic visual property. We found that visual reafferent responses were systematically elevated if there was a trans-saccadic mismatch in saccade target appearance. This elevation did not happen with simulated saccades, and it also scaled with the extent of feature mismatches that we introduced across saccades.

We interpret our results within the framework of predictive coding [7,8,32,33]. In this framework, neural responses would be elevated under so-called prediction error situations. In our case, a stable saccade target across saccades is the most expected sensory consequence of eye movements (that is, having no prediction error). This is because the real world is generally stable across rapid eye movements [40,41], despite translations of its image on the retina. Thus, experiencing a different foveal image from that expected based on the pre-saccadic extrafoveal saccade-target appearance constitutes a trans-saccadic prediction error; accordingly, the visual environment can be interpreted as having been unstable across the saccade.

Consistent with our interpretation, some of the oldest ideas about perceptual stability in the face of eye movements have revolved around concepts of "template matching": a pre-movement template (or prediction) is formed, and post-saccadic perceptual stability is established when a post-movement image matches the pre-emptively formed template [3,9]. Neurobiologically, changes in visual RF shapes and locations do indeed occur peri-saccadically [42-49]. In sensory-motor areas, such as frontal eye field (FEF), lateral intraparietal area (LIP), and SC, these RF changes have long been termed "predictive remapping" [42,43,49]. However, while the exact details of spatial updating continue to be under scrutiny [45,47,48,50,51], such spatial updating remains significantly and conceptually different from our focus here: how is visual sensation of a stably present visual object in the environment handled when an eye movement brings this object inside a given neuron's RF?

One aspect of this question was already addressed previously by Crapse and Sommer [33]. These authors recorded from extrafoveal FEF neurons. They presented a visual stimulus that was stable and brought into the visual RF of an FEF neuron by a saccade. When the stimulus remained stable across the saccade, the visual reafferent response to the stimulus (as it entered into the RF of the recorded neuron) was not as strong as when the same stimulus was experimentally translated intra-saccadically (such that it still occupied the same post-saccadic RF location). Thus, the recorded FEF neuron "signaled" (by elevating its firing rate) a deviation from the "predicted" location of a stable stimulus, even though the stimulus was outside its RF pre-saccadically; the neuron, therefore, detected the unexpected intra-saccadic change in stimulus position. We do not know of such effects in the SC, and certainly

not with visual features other than spatial location. Thus, we attempted to fill this gap here,
and we also used target features, rather than location, as the manipulation of interest for us.
Importantly, we additionally did this in the foveal visual processing domain, which is, in any
case, one of the most important aspects of active visual scanning by saccadic eye
movements. Our results, in this sense, support the recent experiments demonstrating that
foveal perception is influenced, right before saccade onset, by extrafoveal saccade target
appearance [52,53].

Our choice to study the SC was also motivated by additional factors. For example, besides
integrating visual evidence from the entire visual system [11], the SC issues saccade motor
commands [20]. Importantly, at the time of saccade generation, such integrated visual
evidence gets curiously reactivated in the SC, exactly when predictions might be relayed to
foveal visual representations according to our framework: SC saccade-related motor bursts
embed within them a sensory representation of the saccade target's visual properties [16,19].
Thus, our foveal neurons might receive such evidence from the extrafoveal motor bursts of
the SC. It would be interesting in the future to explore whether such information transfer
happens intra-collicularly or through loops outside of the SC, especially because it is also
known that an influence in the reverse direction (from the fovea to the periphery)
additionally occurs [54]. This could be done, for example, by reversibly inactivating the
extrafoveal SC representation and checking whether trans-saccadic error signal by foveal
neurons would survive.

We also think that the SC is interesting to study because of its importance for signaling
salience. Classically, such salience has been described in the image domain. That is, when
spatiotemporal movies are played to the retina, then the SC can signal salient "locations" in
retinotopic images at specific time snapshots [22-25]. However, salience can also be
represented in the temporal domain. For example, our results indicate that foveal SC
neurons can signal salient post-saccadic events highlighting a "failure" of expected visual
scene stability as seen by the very same neurons. Thus, the same retinotopic location
responds differently at different times. We believe that this idea can also extend to non-
saccadic situations. For example, if there are known temporal contingencies in the
environment with certain types of stimuli, then we can expect that SC neurons can still be
sensitive to violations in these contingencies even in the absence of saccades. This can
happen, say, if certain object motions follow strict or systematic physical rules to their
sequencing, such as in the case of biological motion. If the SC does indeed behave as a
temporal salience detector for detecting violations in temporal contiguity across saccades,
then this can be part of a larger framework for building invariant object detection in the
cortex [55,56].

We now turn to potential limitations of our study and its interpretations. For one, it could be
argued that our elevated reafferent responses reflect a relief from adaptation. That is, in the
control trials, the pre-saccadic image was the same as the post-saccadic one, whereas it was
different on the image-flip trials. However, because the SC is retinotopic, adaptation in our
experiments would have been specific to the extrafoveal neurons that saw the pre-saccadic
stimulus and not to our recorded foveal neurons. It is not clear at all why foveal SC neurons
should reflect the adaptation state of extrafoveal ones. More importantly, if this was indeed
the case, then this in itself would constitute a trans-saccadic transfer of information from the

extrafoveal to the foveal SC. This would be directly consistent with our interpretation that
foveal SC may receive information about the state of extrafoveal scene appearances before
saccades.
701
Our simulated saccades were also not direct replicas of real saccadic trajectories. Thus, it
might be argued that our simulated saccades were not "sufficient" to cause elevated
responses in image-flip trials. However, our experience with these types of simulated
saccades from earlier experiments is that they often lead to stronger, rather than weaker,
modulations [57]. Also, the fact that we did not see pauses in activity before the visual
responses (Fig. 5) supports our view that the neurons were not stimulated before the image
translations, and that they simply passively received new stimuli entering their RF's. Thus, it
is not too surprising that they might not detect a pre-translation image difference.
710
It would also be interesting in the future to have a perceptual readout from our paradigm.
That is, here, we did not query whether the monkeys experienced perceptual instability or
not. This would be important to establish, along with causal manipulations of SC activity, in
order to establish whether prediction error signaling has direct influences on perceptual
experience. Given the role of the SC in attention [58], we suspect that our neural modulations
would be relevant for altering behavior. For example, we could inactivate the extrafoveal SC
and ask whether trans-saccadic error signaling by foveal SC neurons would survive, and
whether perceptual readouts can also be affected.
719
Finally, we think that SC neurons with large RF's can potentially contribute to the transfer of
information from the extrafoveal neurons at the time of saccade onset [16] to the foveal
neurons post-saccadically, exactly for realizing prediction error signaling. In our analyses, we
strictly excluded such neurons (Methods). However, we had plenty of such excluded neurons
with subtle elevations in their activity at extrafoveal stimulus onset. That is, their peri-foveal
RF's extended out to be marginally driven by extrafoveal stimulus onset. When we analyzed
those excluded neurons like we did in this study, we found that they had trans-saccadic
modulations that were not too different from those reported here (for example, like the
reafferent responses of Figs. 1, 2). Thus, intermediate RF's spanning both pre- and post-
saccadic visual representations could be critical for the mechanisms explaining our results,
and they could exist through wide-field synaptic connections in the SC [59].
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Competing interests statement

737 The authors declare no competing interests.

Data availability statement

742 Data is provided within the manuscript and all figures.

Acknowledgements

747 We were funded by the Deutsche Forschungsgemeinschaft (DFG; German Research
748 Foundation) through the Special Priority Programme: "SPP 2411 Sensing LOOPS: cortico-
749 subcortical interactions for adaptive sensing" (project numbers: 520617944 and 520283985,
750 HA 6749/11-1). We were also funded by the DFG project BO5681/1-1.

Methods

Experimental animals and ethical approvals

We collected data from two adult, male rhesus macaque (macaca mulatta) monkeys (A and M), aged 8-9 years.

The animals were prepared previously for behavioral and neurophysiological procedures. They each had a head holder for stabilization of head position during the experiments, scleral search coils for eye tracking, and a recording chamber with craniotomy for access to the superior colliculus (SC).

All experiments were approved by ethical committees at the regional governmental offices of Tübingen (Regierungspräsidium Tübingen), under licenses CIN 3/13 and CIN 4/19G, and the experiments complied with all guidelines and regulations.

Laboratory setup

The experiments were conducted using the same setup as in our earlier studies [13]. Specifically, we used a custom-built modification to PLDAPS [60], which employed the PsychToolbox [61-63] for display control. The system synchronized with the OmniPlex system from Plexon for data acquisition and storage. We used a linearized and calibrated CRT display monitor with a refresh rate of 85 Hz and ~34 pixels/deg resolution. The monkeys sat ~72 cm from the display, and experiments were conducted with a gray background on the display (having 26.11 cd/m^2 luminance). White stimuli (for example, for a fixation spot) had a luminance of 79.9 cd/m^2. We tracked eye movements using the magnetic induction technique [64,65], and we recorded neural activity using 16- or 24-channel V-Probes from Plexon.

Experimental procedures

For response field (RF) mapping, we employed a fixation task. The monkeys maintained fixation on a central fixation spot (black), and we then presented a small white spot at pseudorandom locations across trials [66]. The fixation and target spots were each ~10.8 x 10.8 min arc in size. We mapped RF's to ensure that there were no visual responses to the extrafoveal visual stimulus onset in the main tasks (e.g. Fig. 1b).

For the main saccade task, the monkeys fixated a central (white) fixation spot of the same dimensions as above. After 300-700 ms from foveating the fixation spot, we presented the extrafoveal stimulus. This stimulus appeared at 8 or 10 deg to the right or left of the fixation spot in all sessions except two; for these two sessions, we placed the stimulus at +/- 5.5 deg horizontally and -4.7 deg vertically, or +/- 4.6 deg horizontally and +4.4 deg vertically. This placement was dictated by other unrelated experiments that we were simultaneously performing during these two sessions in the primary visual cortex. The extrafoveal stimulus was a circle of 3 deg radius. Inside, there could be a vertical sine wave texture of high contrast (100%), having either 1 cycle/deg (cpd) or 4 cycles/deg (cpd) spatial frequency. We called the former the low spatial frequency texture and the latter the high spatial frequency

799 texture. After a delay period of 500-1000 ms, we removed the fixation spot, instructing the
800 monkeys to generate a saccade towards the extrafoveal stimulus.
801
When eye position exited a virtual window surrounding the fixation spot, the computer
flagged a saccade detection event. This triggered a stimulus update on the very next
graphics display frame update. In control trials, the initial shape was always a circle (with
either low or high spatial frequency embedded within it), and the display update event was
fictive. That is, the stimulus was unchanged in this case (of course, the display itself was
always being refreshed from frame to frame, as expected from such display technology).
Such control trials constituted 50% of all trials within a session. The remaining trials were
split among the different intra-saccadic change conditions. In one case, the initial stimulus
was a circle and the final stimulus was still a circle, but containing the other spatial
frequency. That is, if the initial circle encompassed 1 cpd, then the changed stimulus had 4
cpd. These spatial-frequency change trials constituted 16.67% of all trials. In another case,
the initial shape was a circle containing either the low or spatial frequency texture, and the
final shape was a square (6x6 deg in size) with the same texture. These shape-change trials
constituted 16.67% of all trials in a session. Finally, there were trials with a circle initial
shape; the final shape was a square (6x6 deg) containing a different spatial frequency (shape
plus spatial frequency trials). These constituted 16.67% of all trials in the session. Note that
the stimulus never moved in any of the trials. It was the eye that was moving and causing
the stimulus to move towards the fovea on the retina. After the foveating saccade to the
extrafoveal stimulus, the monkeys maintained fixation for another 500 ms before being
rewarded with juice droplets. We collected 322-1440 trials of this task per session.
822
In some sessions, we also ran a simulated saccade version of the above paradigm. Here, the
monkey always maintained fixation. Instead of a go signal to generate a saccade (removal of
the fixation spot), we simply translated the extrafoveal stimulus towards the center of the
display. The translation proceeded as follows: the target at the initial 8 deg eccentricity was
translated to 5.5 deg in the first frame (i.e. 2.5 deg in 11.76 ms), and then to 1.5 deg in the
second frame (i.e. a shift of 4 deg in 11.76 ms), and finally to the final central position in the
next frame (i.e. a shift of 1.5 deg in 11.76 ms). Thus, the simulated saccades had an
accelerating and decelerating profile with a peak speed of 340 deg/s, which is similar to our
real saccades' peak speeds (e.g. Fig. 2a). Image-change trials involved changing the relevant
image feature in the first frame of the translation. The experiment was otherwise the same
as the real saccade version. We did not run the simulated saccade experiment during the
two sessions in which the saccade target was at an oblique position relative to the fixation
spot. We collected 647-841 trials of this task per session.
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Data analysis
839 We detected all microsaccades and saccades using our established methods [67,68]. In the
840 saccade task, we only accepted trials in which saccades landed within a radius of <2deg from
841 the center of the saccade target. This ensured that the saccade target activated our foveal
842 neurons post-saccadically (Fig. S3).
843
We sorted neurons offline using Kilosort [69]. In total, we had 249 neurons in our database.
However, we excluded neurons in which there was an elevation (however small) in firing

rates after extrafoveal stimulus onset in our main task (relative to pre-stimulus firing rates).
This is because we wanted to exclude any remote possibility that our foveal neurons were
visually-stimulated by the pre-saccadic extrafoveal stimulus. We also confirmed this with our
RF mapping task, as well as by measuring post-stimulus activity in our accepted neurons (Fig.
S1). We also excluded neurons in which the average firing rate in the interval 0-100 ms from
fictive stimulus update time (i.e. in control trials) was less than 5 spikes/s, to ensure that we
had a proper post-saccadic visual response to analyze. This left us with 81 neurons that we
included in the final database.
854
855 To check for intra-saccadic stimulus updates, we collected all saccades and related their
856 parameters (onset, peak velocity, and end times) to the time after stimulus update
857 completion. We also measured eye speed at the time of stimulus update completion.
858
To measure reafferent response strength, we calculated the peak firing rate in the interval
after the end of stimulus updates. For low spatial frequency foveated targets, the interval
was 0-120 ms from real or fictive stimulus update; for high spatial frequency foveated
targets, it was 0-150 ms. The two different intervals reflected the fact that responses were
delayed for high spatial frequency foveated stimuli [12,29]. For the simulated saccade version of
the task, we used the same measurement intervals relative to the stimulus update times.
Note that in all cases, we focused only on the initial reafferent response and not also later
modulations in firing rate that could happen. This is because such later modulations
coincided with potential catch-up saccades, which (due to their small size) were expected to
significantly alter foveal SC activity.
869
870 Our modulation indices were calculated for each neuron as follows: firing rate on the intra-
871 saccadic change condition of interest minus firing rate on the corresponding control
872 condition, divided by the sum of the firing rates.
873
874 We performed statistical analyses in two ways. First, across neurons, we measured the firing
875 rate on the intra-saccadic change of interest and the firing rate on the corresponding control
876 condition. We then performed a Wilcoxon signed-rank test across neurons. Second, we
877 checked whether the population modulation indices were different from zero using a
878 Wilcoxon signed-rank test.
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Supplementary figures

Figure S1 Lack of visually-evoked bursts in the foveal neurons at the time of extrafoveal stimulus onsets. (a) For all neurons included in our main analyses of Figs. 1-4, 6-8, we measured neural activity 50-150 ms after extrafoveal stimulus onset (during maintained gaze fixation), and we compared it to pre-stimulus activity. Here, the appearing stimulus was a circular patch containing a low spatial frequency texture. There was a reduction in activity, rather than visual bursts. **(b)** Similar observations for the case in which the extrafoveal stimulus had a high spatial frequency texture embedded within it.

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Figure S2 Confirmation of intra-saccadic stimulus updates. (a) For all trials containing a real or fictive image
update (from the basic paradigm of spatial frequency changes and circular outline shapes of the saccade targets),
we measured (also across all sessions) the times of saccade onset, saccade peak velocity, and saccade end
relative to when the image flip event was completed. We always had intra-saccadic image updates in our
experiments. **(b)** Importantly, the eye speed was always high by the end of the image update. Here, for each
session, we calculated the average eye speed by the end of the image update event, and we plotted a histogram
across sessions. For the great majority of sessions, the image speeds on the retina by the end of intra-saccadic
image updates were >150 deg/s. For the two sessions with speeds of ~50 deg/s, the saccade targets were placed
a bit closer to the fovea (thus having smaller saccades) because the sessions involved other experiments involving
the primary visual cortex (we thus tailored the target locations to the cortical neurons explored during the same
sessions for other purposes). However, eye speed was still relatively large during these outlier sessions.
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Figure S3 Confirmation of post-saccadic visual stimulation of our foveal neurons by the saccade targets. **(a)** Across trials and sessions from our basic paradigm, we plotted the retinotopic position of the saccade-target patch (circles) upon saccade end. There was variability due to variability in saccade metrics. However, the foveated image patches were always encompassing our recorded foveal neurons (green spots indicating the foveal RF hotspot locations). Thus, we always had robust visual reafferent responses. Note also that such jitter in saccade landing should have weakened reafferent responses in some cases, rather than strengthened them, because it could cause visual stimulation at sub-optimal RF positions. This suggests that our main results (dominated by elevated reafferent responses) are not explained by jitter in saccade landing positions. **(b)** Similar observations from the shape-change trials (Methods) of our paradigm. Here, the foveated stimulus had a square outline instead of a circular one.

Figure S4 Lack of relationship between the modulation indices associated with real versus simulated saccades.
(a) For a low spatial frequency foveated patch after either real or simulated saccades, we plotted the modulation indices from Fig. 5e on the x-axis (for simulated saccades) and those from Fig. 3c on the y-axis (for real saccades). The shown neurons are those for which we ran both conditions together in the same session. In the simulated saccade case (x-axis), the modulation indices straddled zero; however, in the real saccade case (y-axis), the modulation indices were largely positive. Thus, there was no correlation between the two situations (p=0.4701).
(b) Similar observations for a high spatial frequency foveated image (p=0.2323).

Figure S5 Confirmation that shape-change and shape plus spatial frequency changes had much weaker effects on foveal SC neurons during simulated saccades than during our main experimental manipulations with real saccades. (a, b) Population results like in Fig. 5c, d, but now for the shape change trials and a low (**a**) or high (**b**) spatial frequency post-translation texture. There were weaker differences in visual response strength relative to control than with real saccades. **(c, d)** Similar observations for the shape plus spatial frequency change trials. **(e, f)** Neural modulation indices for **a**, **b** (p=0.8 and 0.049 for **e** and **f**, respectively; Wilcoxon signed-rank test). **(g, h)** Neural modulation indices for **c**, **d** (p=0.22 and 0.40 for **g** and **h**, respectively; Wilcoxon signed-rank test).