Haptic Force Feedback Enhances *De Novo* Learning of Arm Kinematics and Dynamics

Abbreviated title: Haptic Feedback Enhances *De Novo* Learning

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Conflict of Interest

The authors declare that they have no financial, personal, or professional interests that could be construed to have influenced the paper.

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Significance Statement (106/120)

Humans can learn to control arbitrary extensions of the body. However, the factors that influence such De Novo motor learning remain unclear. Here, we demonstrate that haptic force feedback from a simulated endpoint mass enhances the acquisition

of a novel kinematic and dynamic mapping, using a virtual arm. Participants who trained with haptic feedback showed greater adaptation to curl fields and more accurate trajectory control. These results suggest that haptic input facilitates the formation of more efficient internal models during novel sensorimotor learning. Beyond theoretical insights, these findings have practical implications for the use of haptic feedback in rehabilitation training and complex machinery control.

Abstract (227/250)

The human motor system exhibits remarkable plasticity. Not only can we master complex skills, but we can also learn to control artificial effectors. Here, we examine whether haptic force feedback from a simulated endpoint mass facilitates the De Novo learning of novel kinematic and dynamic mappings. We investigate this using a virtual 2D planar arm controlled via a bimanual robotic manipulandum. Human participants moved two handles constrained to 1D channels, with handle positions specifying shoulder and elbow joint angles. Across two days, they performed center-out and out-back movements under two experimental conditions. On Day 1, one half of the participants practiced with a purely kinematic arm, whereas the other half received continuous haptic feedback from an endpoint mass. Initially, intrinsic hand movements were often sequential, but participants rapidly adopted more coordinated control strategies, and trajectories became straighter with practice. Notably, the haptic feedback group exhibited significantly greater improvements in virtual arm control. On Day 2, we introduced a velocity-dependent curl field to both groups. The curl field initially resulted in curved, loopy paths, but participants gradually compensated, consistent with internal-model formation. Prior exposure to haptic feedback conferred a superior capacity to adapt to the novel dynamics, as evidenced by straighter trajectories and smaller directional biases throughout curl-field exposure. These findings suggest haptic feedback enhances sensorimotor learning, possibly by engaging distributed neural networks involved in motor skill acquisition.

Introduction (599/650)

Humans can master intricate motor skills, from rudimentary tool use to the operation of complex machinery (Savion-Lemieux and Penhune, 2005; Reis et al., 2009; Shmuelof et al., 2012; Krakauer et al., 2019). Nevertheless, many motor control studies have examined relatively simple adaptations to altered task dynamics or visual feedback, often interpreted as recalibrations of the motor system. Many motor learning studies use veridical feedback from point-to-point movement tasks, often without kinematic transformations, and draw conclusions based on steady state performance. For example, numerous studies have investigated both visuomotor adaptation (Krakauer et al., 2000, 2005; Bock et al., 2001; Goedert and Willingham, 2002) and dynamic learning tasks have been examined either directly (Lackner and Dizio, 1994; Shadmehr and Mussa-Ivaldi, 1994; Brashers-Krug et al., 1996; Gandolfo et al., 1996) or across different unimanual contexts (Howard et al., 2012, 2013; Sarwary et al., 2015) and different bimanual contexts (Nozaki et al., 2006; Howard et al., 2010, 2024; Gippert et al., 2023; Orschiedt and Franklin, 2023).

Simultaneous visuomotor and dynamic adaptations have also been investigated. For
instance, participants can learn visuomotor rotations, viscous curl fields, or their
combination within the same session (Flanagan et al., 1999), and evidence suggests
that separate yet coexisting kinematic and dynamic internal models can be formed
(Krakauer et al., 1999). There has also been compelling research into more complex
adaptations, such as nonlinear visuomotor transformations involving movement in
altered visual space (Flanagan and Rao, 1995), mirror reversal compensations
(Lillicrap et al., 2013), rotational adaptations (Telgen et al., 2014), and sensorimotor
transformations (Pouget et al., 1991; Pouget and Snyder, 2000). More complex
remapping has been investigated using finger motions to control the joint angles of a
simulated planar two-link arm, demonstrating relevance for prosthetic control
(Danziger et al., 2009; Danziger and Mussa-Ivaldi, 2012). These studies have
highlighted the pivotal role of visual feedback (Danziger and Mussa-Ivaldi, 2012),
in learning to control virtual objects through finger movements (Liu et al., 2011).

Skill acquisition that requires entirely new mappings, rather than incrementally
adjusting existing ones, is often referred to as De Novo learning (Sternad, 2018; Yang
et al., 2021; Haith et al., 2022). Such paradigms shift the focus to the mechanisms by
which the motor system builds novel sensorimotor transformations capable of
supporting arbitrary task spaces. Thus, whereas adaptation tasks may primarily
involve updating parameters within an existing internal model, De Novo learning
requires establishing entirely new sensorimotor mappings without reliance on prior
control structures. Empirical evidence suggests that early phases of De Novo learning
are characterized by increased motor variability. There is also a reliance on cognitive
strategies, and the gradual formation of stable control policies through trial-and-error
exploratory learning (Yang et al., 2021; Haith et al., 2022).

Here, we investigate De Novo learning of kinematic and dynamic relationships using
a virtual two-dimensional planar arm with and without haptic feedback during learning.
The arm was implemented using a bimanual robotic manipulandum. Participants
controlled the simulated arm by moving two robotic handles backward and forward
through two distinct one-dimensional channels. These hand movements directly
controlled the angles of the shoulder and elbow joints, thereby determining the position
of the end-effector. Participants were tasked with performing center-out and out-back
movements, allowing us to chart how practice improves their performance over time.

We examined two conditions: training either with or without an endpoint mass attached
to the virtual arm's end-effector, to assess how exposure to different dynamics
influences learning of novel kinematics and dynamics. In both scenarios, after
participants became proficient at controlling the 2D arm, we evaluated their adaptation
to the introduction of additional novel task dynamics, specifically a velocity-dependent
curl field.

Materials and Methods

Participants

We recruited 16 healthy, right-handed human participants from a similar age range
and educational background, and randomly allocated each participant to one of two

experiments. All participants provided written informed consent, and the protocol was
approved by the University of Plymouth's local ethics committee. All participants
completed the Edinburgh Handedness Inventory (Oldfield, 1971) and the Quick
Physical Activity Rating (QPAR) assessment (Galvin et al., 2020).

Experiment 1 (Kinematic Arm Task) comprised eight participants (4 female, 4 male;
mean ± SD age 20.8 ± 1.4 years; QPAR 40.9 ± 19.4).

Experiment 2 (Endpoint Mass task) included eight participants (3 female, 5 male;
mean ± SD age 21.9 ± 3.2 years; QPAR 46.3 ± 16.3).

To avoid experimental bias, participants were kept naïve to the hypotheses of the
study.

Experimental Setup

All experiments were conducted using two identical custom-built, back-drivable vBOT
planar robotic manipulanda (Fig. 1A, B), which exhibit low mass at their handles
(Howard et al., 2009). Handle position was sampled with optical encoders at 500 Hz,
and planar forces were updated by torque motors at the same rate. A planar virtual
reality projection system was used to overlay images of targets, the end-effector
cursor, and the 2D arm configuration in the plane of the vBOTs' movements.
Participants were prevented from viewing their arms directly and were seated in front
of the apparatus holding one robot handle in each hand.

Two-joint Revolute Arm Simulation

We modeled a planar, two-joint (shoulder –elbow) revolute arm (Fig. 1C) with a
workspace origin at point (0, 0). The shoulder joint was located at coordinates (−12,
−2) cm, while both arm links were 12 cm in length and depicted as yellow lines 2 mm
wide. The shoulder and elbow joints were drawn as yellow circles with a radius of 0.5
cm. The end-effector position, located at the endpoint of the second arm segment,
was drawn as a red circle with a radius of 0.5 cm. The default arm configuration was
purely kinematic and exhibited no intrinsic dynamics. Dynamics were added when
required by the experimental conditions.

Participants controlled the arm by moving the left and right handles on the vBOT
manipulandum, which caused the arm to rotate around its shoulder and elbow joints,
thereby controlling the location of its end effector. To accentuate the novelty of the
mapping, handle positions and joint angles were deliberately decoupled from natural
endpoint motion. Consequently, the arm movement directional mapping, represented
by the parameter dir_{slider}, was set to –1, such that outward movements of the handles
tended to generate inward movement of the cursor.

Mechanical Channels

179 The movement of the two vBOT handles was restricted to linear channels along the y-
180 axis, with a length (*chanLen*) of 30 cm. To spatially separate the hands, the left and

181 right channels were offset laterally by ±10 cm, yielding central handle positions of (-
182 10, 0) cm and (+10, 0) cm, respectively.
183
184 Simulated mechanical channels constrained hand motion to a single degree of
185 freedom in the direction of the y-axis (Scheidt et al., 2000), with a wall stiffness of k_{chan}
186 = 4,000 N/m and a damping coefficient b_{chan} = 30 N.s/m. The channels were
187 implemented according to the following equation, which relates the forces experienced
188 at a given handle $[F_{xh} \quad F_{yh}]^T$ to its position $[x_h \quad y_h]^T$ and velocity $[\dot{x}_h \quad \dot{y}_h]^T$:
189

$$\begin{bmatrix} F_{xh} \\ F_{yh} \end{bmatrix} = k_{chan} \begin{bmatrix} -1 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} x_h \\ y_h \end{bmatrix} + b_{chan} \begin{bmatrix} -1 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \dot{x}_h \\ \dot{y}_h \end{bmatrix}$$

(1)

Control of the Simulated Arm

193
194 The y-position (y) of each handle was linearly mapped to the corresponding joint angle
195 (θ):
196

$$\theta = \theta_{min} + (\theta_{max} - \theta_{min}) \frac{\left(dir_{slider} \cdot y + \frac{\text{chanLen}}{2} \right)}{\text{chanLen}}$$

(2)

199 The y-location of the left handle y_{h1} was mapped to a joint angle θ_1 in the range
200 of $\theta_{min} = 0$ radians and $\theta_{max} = \pi$ radians:

$$\theta_1 = \frac{(15 - y_{h1})}{30} \pi$$

(3)

202
203 The y-location of the right handle y_{h2} was mapped to a joint angle θ_2, between the
204 range of $\theta_{min} = -\pi$ radians and $\theta_{max} = 0$ radians:
205

$$\theta_2 = \frac{(15 - y_{h2})}{30} \pi - \pi$$

(4)

207
208 Differentiating equations (2) and (3) results in a mapping between the handles' y-
209 velocities and the corresponding joint angular velocities:

$$\begin{bmatrix} \dot{\theta}_1 \\ \dot{\theta}_2 \end{bmatrix} = -\frac{\pi}{30} \begin{bmatrix} \dot{y}_{h1} \\ \dot{y}_{h2} \end{bmatrix}$$

(5)

Simulating Forward Kinematics

213
214 Forward kinematics of the 2D arm is necessary to calculate the endpoint position and
215 calculate and display its configuration. By trigonometric analysis (Fig. 1C), the
216 positions of the elbow and end effector in Cartesian coordinates can be expressed
217 using matrix equations:

218
$$\begin{bmatrix} x_{elbow} \\ y_{elbow} \end{bmatrix} = \begin{bmatrix} l_1 \cos(\theta_1) \\ l_1 \sin(\theta_1) \end{bmatrix} + \begin{bmatrix} x_{shoulder} \\ y_{shoulder} \end{bmatrix} \tag{6}$$

220
$$\begin{bmatrix} x_{end} \\ y_{end} \end{bmatrix} = \begin{bmatrix} l_1 \cos(\theta_1) + l_2 \cos(\theta_1 + \theta_2) \\ l_1 \sin(\theta_1) + l_2 \sin(\theta_1 + \theta_2) \end{bmatrix} + \begin{bmatrix} x_{shoulder} \\ y_{shoulder} \end{bmatrix} \tag{7}$$

221
222 Differential kinematics of the 2D arm are needed to relate handle velocities to endpoint
223 velocities and to map endpoint forces back to vBOT handle forces. The Jacobian
224 matrix of the 2D arm is given as:
225

226
$$J = \begin{bmatrix} \dfrac{\partial x_{end}}{\partial \theta_1} & \dfrac{\partial x_{end}}{\partial \theta_2} \\ \dfrac{\partial y_{end}}{\partial \theta_1} & \dfrac{\partial y_{end}}{\partial \theta_2} \end{bmatrix} = \begin{bmatrix} -l_1 \sin(\theta_1) - l_2 \sin(\theta_1 + \theta_2) & -l_2 \sin(\theta_1 + \theta_2) \\ l_1 \cos(\theta_1) + l_2 \cos(\theta_1 + \theta_2) & l_2 \cos(\theta_1 + \theta_2) \end{bmatrix} \tag{8}$$

227
228 The relationship between the handle velocities and the extrinsic endpoint velocity is
229 given by:

230
$$\begin{bmatrix} \dot{x}_{end} \\ \dot{y}_{end} \end{bmatrix} = J \begin{bmatrix} \dot{\theta}_1 \\ \dot{\theta}_2 \end{bmatrix} = -\frac{\pi}{30} J \begin{bmatrix} \dot{y}_{h1} \\ \dot{y}_{h2} \end{bmatrix} \tag{9}$$

232 **Task Force Feedback**

233
234 Although the arm itself was modeled as a purely kinematic structure with no intrinsic
235 dynamics, different endpoint dynamics were simulated by relating the load at the
236 endpoint back to the y-direction forces experienced by the participants at the control
237 handles. The relationship between the virtual arm endpoint force
238 vector $[F_{xend} \quad F_{yend}]^T$ and the joint torque vector $[\tau_1 \quad \tau_2]^T$ is given by:
239

240
$$\begin{bmatrix} \tau_1 \\ \tau_2 \end{bmatrix} = J^T \begin{bmatrix} F_{xend} \\ F_{yend} \end{bmatrix} \tag{10}$$

241
242 Where J^T is the transpose of the arm's Jacobian matrix. The torques $[\tau_1 \quad \tau_2]^T$ at the
243 arm joints are mapped to corresponding y-direction forces $[F_{h1} \quad F_{h2}]^T$ applied at the
244 vBOT handles by accounting for the mechanical advantage relationship between the
245 handle displacement and the joint rotational angles. This yields the following
246 conversion formula:
247

248
$$\begin{bmatrix} F_{h1} \\ F_{h2} \end{bmatrix} = dir_{slider} \frac{(\theta_{max} - \theta_{min})}{chanLen} \begin{bmatrix} \tau_1 \\ \tau_2 \end{bmatrix} \tag{11}$$

249
250 Substituting in the expression for joint torques, and numeric values, this leads to the
251 final expression for the force along the y-axis at the handle in terms of endpoint force:
252

$$253 \qquad \begin{bmatrix} F_{h1} \\ F_{h2} \end{bmatrix} = -\frac{\pi}{30} J^T \begin{bmatrix} F_{xend} \\ F_{yend} \end{bmatrix} \qquad (12)$$

Endpoint Dynamics Simulation

In the null-field condition, when the arm endpoint was unloaded, no endpoint forces
were present or experienced at the control handles during arm movement. When
endpoint dynamics were introduced, namely, a viscous curl field, added mass, or the
combination of both, the endpoint forces arising from these dynamics were mapped
back to the handles and experienced by the participants as they moved the arm around
the workspace.

Endpoint Curl Field Simulation

266 In curl field endpoint trials, a velocity-dependent curl field (Gandolfo et al., 1996) was
267 implemented using the relationship between arm endpoint velocity and the endpoint
268 force:

$$270 \qquad \begin{bmatrix} F_{xend} \\ F_{yend} \end{bmatrix} = b_{curl} \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} \dot{x}_{end} \\ \dot{y}_{end} \end{bmatrix} \qquad (13)$$

The curl field constant b_{curl} was set to ±16 N.s/m, where the sign determined the
direction of curl field (clockwise or counterclockwise). In each experiment, the curl field
direction was counterbalanced across all eight participants to minimize directional
bias. Each participant experienced only a single curl field direction.

The endpoint velocity used in Equation (13) was calculated from the handle velocities
using Equation (9). The corresponding forces experienced in the y-direction at the
handles were then calculated using Equation (12). The total 2D force applied to the
vBOT handles corresponds to the sum of the channel force component and the force
feedback component arising from the effect of the curl field.

Simulating Endpoint Mass

285 To achieve a stable simulation, a moving mass was modeled as connected to the
286 endpoint of the virtual arm by a strong spring. In addition, viscous damping was
287 included in the simulation to improve stability,

289 At the start of the simulation, the spring was set to its rest length, and the mass position
290 was initialized at the current endpoint of the arm.

$$292 \qquad \begin{bmatrix} x_m \\ y_m \end{bmatrix} = \begin{bmatrix} x_{end} \\ y_{end} \end{bmatrix} \qquad (14)$$

294 We set the velocity of the mass and its initial acceleration to zero.

$$296 \qquad \begin{bmatrix} v_{xm} \\ v_{ym} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix} \qquad\qquad (15)$$

$$298 \qquad \begin{bmatrix} a_{xm} \\ a_{ym} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix} \qquad\qquad (16)$$

300 We also set the force acting on the mass to zero.

$$302 \qquad \begin{bmatrix} F_{xm} \\ F_{ym} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix} \qquad\qquad (17)$$

304 In the main vBOT simulation update loop, running at the nominal frequency of 1 kHz,
305 the real-time simulation of the arm and endpoint mass is then carried out. At each time
306 step, Euler integration was used to update mass position.

$$308 \qquad \begin{bmatrix} x_m \\ y_m \end{bmatrix} = \begin{bmatrix} x_m \\ y_m \end{bmatrix} + \begin{bmatrix} v_{xm} \\ v_{ym} \end{bmatrix} \Delta t \qquad\qquad (18)$$

310 Where Δt is the timestep since the previous update (nominally 1 ms). We then estimate
311 acceleration of the mass using the equation:

$$313 \qquad \begin{bmatrix} a_m \\ a_m \end{bmatrix} = \frac{1}{m} \begin{bmatrix} F_{xm} \\ F_{ym} \end{bmatrix} \qquad\qquad (19)$$

315 Where m is the mass at the point (2 kg) and $[F_{xm} \quad F_{ym}]^T$ is the force acting on the
316 mass. We use Euler integration of the acceleration of the mass to calculate mass
317 velocity:

$$319 \qquad \begin{bmatrix} v_{xm} \\ v_{ym} \end{bmatrix} = \begin{bmatrix} v_{xm} \\ v_{ym} \end{bmatrix} + \begin{bmatrix} a_{xm} \\ a_{ym} \end{bmatrix} \Delta t \qquad\qquad (20)$$

321 The force acting on the mass was then estimated by consideration of the extension of
322 the spring, with spring constant k_{mass} = 2000 N/m, connecting the endpoint mass to
323 the endpoint of the arm:

$$325 \qquad \begin{bmatrix} F_{xm} \\ F_{ym} \end{bmatrix} = -k_{mass} \left(\begin{bmatrix} x_m \\ y_m \end{bmatrix} - \begin{bmatrix} x_{end} \\ y_{end} \end{bmatrix} \right) \qquad\qquad (21)$$

327 An additional viscous damping term was applied to the endpoint to improve stability:

$$329 \qquad \begin{bmatrix} F_{xdamp} \\ F_{ydamp} \end{bmatrix} = -b_{end} \begin{bmatrix} \dot{x}_{end} \\ \dot{y}_{end} \end{bmatrix} \qquad\qquad (22)$$

331 Where damping viscosity b_{end} = 10 N.s/m. The mass force (Equation 21) and damping
332 force (Equation 22) were summed together and the corresponding forces experienced
333 in the y-direction at the handles were then calculated using Equation (12). Again, the

334   total 2D force applied to the vBOT handles corresponds to the sum of the channel
335   force component and the force feedback endpoint components.
336

Simultaneous Endpoint Mass and Curl Field

339   In trials with both endpoint mass and a curl field present, we first calculate the endpoint
340   mass and curl field components as described previously. The vBOT applies an overall
341   2D force to its handles by summing the force-feedback components from the curl field
342   and the endpoint mass, along with the additional channel forces that restrict handle
343   movement to the y-direction.
344

Experimental Protocol

Participants executed center-out and out-back reaching movements with the endpoint
of the two-dimensional (2D) planar arm. Each center-out movement began at a central
'home' position (radius: 1.0 cm, pink) and ended at one of eight peripheral targets
randomly selected without replacement (radius: 1.0 cm, pink), evenly spaced (0°, 45°,
90°, 135°, 180°, 225°, 270°, and 315°) on a 10 cm-radius circle centered at (0, 0). The
home start position was in the mid-sagittal plane, approximately 30 cm below eye level
and 30 cm in front of the participant's chest. An out-back movement then followed,
which involved reaching back from the previous center-out target to the central home
start position.
356

At the beginning of each trial, the manipulanda automatically positioned the handles
so the endpoint of the virtual arm was at the home location. Participants were required
to keep the cursor within the central starting position and maintain cursor speed below
0.1 cm/s. After a 0.5 s delay, a target appeared at a location (randomly selected
without replacement), the arm became visible, and a tone indicated that the participant
should move out to the target.
363

Each block comprised 17 trials: 8 outward and 8 inward movements with the simulated
arm visible. In addition, there was one outward movement where the arm was not
visible. The outward movements constituted a typical center-out task, enabling
comparison of behaviors with other such studies in the literature. The inward (out-
back) movement provided further coverage of the operating space using movements
in the opposite direction. A trial terminated when the cursor was within 0.5 cm of the
target and cursor speed dropped below 0.01 cm/s.
371

An outward catch trial movement to a randomly selected target from one of the four
cardinal directions (0°, 90°, 180°, or 270°) was also included in each block of 17 trials.
In this catch trial, both the arm and the endpoint cursor location were invisible, allowing
assessment of feedforward control. Since catch trials are made without visual
indication of cursor position, catch trial termination only occurred when cursor
movement speed dropped below 0.01 cm/s. This is because accurate movement to a
catch target was difficult and was often not achieved.
379

380   Participants were required to complete a trial movement within 10 s, otherwise, the
381   trial was aborted. During each trial, the handle positions and velocities, as well as the
382   virtual arm's endpoint location and velocity, were recorded.

Experiments

We conducted two independent experiments, each comprising eight randomly assigned participants, to investigate the learning and control of a virtual planar (2D) arm. Each participant completed two sessions of 2,380 trials on separate days (see Fig. 1H).

Kinematic Arm Task Experiment 1.

This experiment examined De Novo acquisition of kinematic control of a two-dimensional arm operating without endpoint mass. On Day 1, participants executed point-to-point reaches, in a null-field environment.

Day 2 began with a brief re-exposure to the null field, comprising the first 20% of trials (n = 476), to re-establish baseline performance. A velocity-dependent viscous curl field was then imposed for most of the session (n = 1,870). The resulting endpoint forces were computed as joint torques via the Jacobian transpose and subsequently transformed into linear forces at the handles, enabling participants to perceive the perturbation directly. In the final two blocks (n = 34 trials) the curl field was removed to assess washout after-effects of the prior dynamic exposure.

Endpoint Mass Arm Task Experiment 2.

Experiment 2 was similar to Experiment 1, but introduced a constant 2 kg endpoint mass, thereby providing continuous haptic load feedback. The actuation forces generated by moving the mass were related to the virtual arm joint torques and subsequently mapped to forces at the control handles.

409
Figure 1. Experimental Setup and Task Design. **A:** Control of a virtual 2D arm was conducted using the vBOT robotic manipulandum. **B:** The left and right handle y-positions determine the arm joint angles. The handles are constrained to linear channels. **C:** Plan view of the simulated planar two-joint revolute arm. The lower link has a length L_1, and the upper link has a length L_2. The position of the end effector is affected by both link angles θ_1 and θ_2. **D:** Angles θ_1 and θ_2 are controlled by moving the robotic handles in two separate channel trials. Moving the left handle (controlling θ_1) up decreases the angle, while moving it down increases the angle. Similarly,

moving the right handle (controlling θ_2) up decreases the angle, and moving it down
increases it. **E:** Workspace of the simulated 2D arm is shown in black. A center-out
and out-back task, home position and targets fit within the workspace. **F:** Curl field
trials. Participants performed outward and inward movements toward a displayed
yellow target. After completing the training, they were exposed to two distinct
directional curl fields. Half of the participants experienced clockwise (CW) curl fields
during outward movements and inward movements. The other half experienced
counterclockwise (CCW) curl fields during outward and inward movements. This
design counterbalanced the exposure to each field type across participants. **G:**
Channel trials. These only used a single adaptation movement direction to a target
point (0°, 90°, 180°, or 270°). **H:** Training and testing trial schedule for the experiment.
Each block contains 17 trials: 8 cursor-visible center-out movements to a target, 8
cursor-visible out-back movements to the home position, and 1 invisible-cursor center-
out catch movement to one of four targets. **I**. Location of informative trajectory
observation points: First Null Block, Final Null Block, First Curl Block, Final Curl Block,
and First Washout Block.

Data Analysis

435
436 The experimental data were processed offline using MATLAB R2024a.

Hand Trajectory Plots

438 Hand trajectory plots provide an intuitive visualization of participants' movement
439 behavior throughout the experiment. They illustrate naïve control early in training, the
440 progressive refinement that accompanies exposure to external dynamics (e.g.,
441 viscous curl fields), and the re-emergence of baseline patterns once those forces are
442 removed, thereby revealing learning, adaptation, and de-adaptation in a single display.

443
444 In both experiments, several key phases are critical to understanding participants'
445 motor performance and adaptation. These include the first and final blocks of null-field
446 trials (baseline establishment and improvement), the first and final blocks of curl-field
447 exposure (early and late adaptation), and the first washout block (de-adaptation).

448
449 Hand trajectory plots allow direct comparison of movements during outward and
450 inward paths and provide insight into both extrinsic trajectories (hand paths in
451 Cartesian space) and intrinsic trajectories (joint space paths). Additionally, catch trials,
452 in which the target is shown but no visual feedback of the arm is provided, are included
453 to assess predictive adaptation to the control of the novel kinematics.

454
Trajectory quantification: Several measures were calculated to quantify the movement
trajectory of each individual trial. First, the movement start, and end points were
determined in both time and space. A movement was considered to have started when
the center of the extrinsic cursor location left the center of the starting target circle
(radius: 0.5 cm) and was traveling at a speed greater than 0.01 cm/s. A movement
was considered to have stopped when the center of the extrinsic cursor reached the
extrinsic target circle (radius: 0.5 cm).

Performance Metrics

We quantified kinematic accuracy with four complementary deviation metrics.

Extrinsic Absolute Maximum Perpendicular Error (AMPE): For each trial we took the absolute value of the maximum perpendicular deviation of the 2D arm endpoint trajectory from the ideal straight-line joining the start cursor location and the target cursor location in extrinsic space. This measure ensures that positive and negative deviations over trials do not cancel out and gives an overall indication of how well participants were able to move in a straight trajectory from the starting point to the target, making it a suitable metric to quantify how well participants could control the virtual arm.

Extrinsic Signed Maximum Perpendicular Error (SMPE): We also retained the signed maximum deviation of the 2D arm endpoint trajectory from a straight-line path, between the starting cursor location and the target cursor location in extrinsic space, was calculated. This measure preserved the direction of the maximum deviation from a straight-line trajectory. Consequently, the effects of random fluctuations are minimized, since contributions from positive and negative deviations cancel out in the averaging procedure. Consequently, the group-mean SMPE is a clearer indicator of systematic bias in the trajectories. As such, since its introduction, this is typically the preferred metric used to assess deviation from a straight line in curl field adaptation experiments (Smith et al., 2006).

Movement Duration: Difference between movement onset and termination times.

Movement Length: To estimate the extrinsic movement path length, we computed the sum of the distances between adjacent (x, y) cursor trajectory positions, calculated using the Pythagorean theorem, from the start to the end movement locations.

Mean ± SE over Trials and Participants

The average values of each trajectory metric were first computed across all trials within a given set of blocks. The mean $\pm$ standard errors (SE) of the resulting average values were then calculated across all participants.

Statistics

Statistical analyses were conducted in JASP (JASP Team, Version 0.19.1, 2024). A Mauchly's test was applied to check for sphericity wherever applicable. In cases where the Mauchly's test was significant, the degrees of freedom were adjusted using a Greenhouse-Geisser correction. The α-level was set to 0.05 in all tests. We report omega squared as the effect size (ω^2).

Each of the two experiments was conducted with different participants, resulting in a total of two sets of AMPE, SMPE, path length and movement duration data. For each of these two datasets in isolation, we first performed repeated measures ANOVAs to

examine differences in AMPE, SMPE, path length and duration data at various critical
phases within each experimental condition.

To evaluate the four metrics within each experimental condition, we compared the
mean of each metric over two blocks for the initial null phase, the final null phase, the
initial curl field exposure phase, the final curl field exposure phase, and the washout
phase. This comparison was conducted using a repeated-measures ANOVA, with
phase as a repeated-measures factor (5 levels). When a significant main effect was
observed, we proceeded with post-hoc comparisons using the Holm-Bonferroni
correction.

To compare results across experiments for the four metrics, we compared the mean
of each metric over ten blocks using an ANOVA between the final null phase, the initial
curl field exposure phase, and the final curl field exposure phase. In this analysis,
experimental condition (2 levels) was considered the factor. Post-hoc comparisons
were conducted with the Holm-Bonferroni correction if a significant main effect was
detected

Results

The Kinematic Arm Task Experiment 1 involved first learning how to control a virtual
revolute arm using a purely arbitrary kinematic mapping between hand movements
and its joint angles. It then investigated the effect of an endpoint curl field. Each
participant performed two sets of 2,380 trials, with each set on a separate day. On Day
1, the arm was controlled with a purely kinematic mapping from hand positions to joint
angles. On Day 2, the first 20% of trials maintained this kinematic mapping. For the
remainder, the endpoint was simulated moving through a viscous curl field and
participants experienced corresponding joint torques as reaction forces at their hands.

We recorded and subsequently analyzed the behavior of participants as they learned
the novel kinematics and dynamics of the simulated 2D arm. This process was
undertaken for both experiments, Experiment 1 – Kinematic Arm Task and Experiment
2 – Endpoint Mass Task. See Fig. 1H for the location of the critical informative phases
in the experiments discussed below.

Trajectory Plots Kinematic Arm Task Experiment 1

We first examined the representative hand trajectories during the initial null phase for
a single participant. Fig. 2A shows the extrinsic and intrinsic outward-movement
trajectories for the first null block for a typical participant. The extrinsic paths were
highly erratic as participants searched for the target location, and the corresponding
intrinsic movement trajectories show typical segmented, independent hand
movements typical of early learning. By the final null block, the participant exhibited
straighter extrinsic paths, as shown in Fig. 2B. The previously independent hand
movements were replaced by simultaneous, continuous intrinsic motions.

We then examined outward movement trajectory trends across participants. Fig. 2C
plots the mean ± SE extrinsic trajectories across the participants in the clockwise (CW)

condition, and Fig. 2D shows the corresponding trajectories in the counterclockwise
(CCW) condition. In the initial null block, trajectories deviated substantially from
straight-line paths. However, by the end of the null phase, their outward paths to the
targets became consistently much straighter. Upon introducing a curl field,
participants' trajectories became systematically curved, as the curl field pushed them
away from their straight paths. By the end of the curl field exposure phase, participants
exhibited adaptation to the curl field, straightening their hand trajectories. This
adaptation process resembles typical curl field adaptation. In the final washout phase,
the curl field was removed, and pronounced after-effects were observed. These after-
effects manifested as deviations from the intended path, in the direction opposite to
the original curl field force.
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We examined the mean ± SE speed profiles across all extrinsic movements over the
same experimental phases, as shown in Fig. 2E. Initially, movements were slow and
exhibited a similarly low speed across the movement trajectory. By the end of the null
phase, the speed profile more closely resembled that of a minimum-jerk extrinsic point-
to-point movement, exhibiting a characteristic peak. However, there was still some
asymmetry in the speed profile. The introduction of the curl field slowed down the
movements and skewed the profile toward lower speeds as well, although the shape
of the speed profile became more symmetric and faster by the end of adaptation to
the curl fields. In the washout phase, the after-effect led to a somewhat more erratic
speed profile.
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Catch trials, performed without visual feedback, assessed feedforward control of the
virtual arm. We examined the catch trial trajectories made by participants at the start
of the experiment, at the end of the null exposure phase, and at the end of curl field
exposure. The raw trajectories are presented in Fig. 2F, as each participant behaved
differently, and average plots would obscure their individual characteristics. Initially,
the movements were often made in inappropriate directions and of inappropriate
length. By the end of the null training, movement directions and lengths had improved,
although there was still inaccuracy in most of the trajectories. At the end of curl field
training, by which time participants had the most experience learning to control the
virtual arm, the directions and lengths of the catch movements had improved further.
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Figure 2. Trajectory plots for Experiment 1 – Kinematic Arm Task. **A:** Representative
extrinsic and intrinsic trajectories from the first null trials of an individual participant. **B:**
Representative extrinsic and intrinsic trajectories from the final null trials of the same
participant. **C:** Mean ± SE extrinsic outward path trajectories for the clockwise (CW)
curl field condition during the initial null block, final null block, initial curl block, final curl
block, and washout phase blocks. **D:** Corresponding mean ± SE extrinsic outward path
trajectories for the counterclockwise (CCW) curl field condition. **E:** Corresponding
mean ± SE extrinsic speed profiles across CW and CCW trials. **F:** Extrinsic catch trial
trajectories from the first 8 null blocks, the final 8 null blocks, and the final 8 curl blocks.
Trajectories to the 0°, 90°, 180°, and 270° targets are plotted in red, green, blue, and
black, respectively.
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Trajectory Plots Endpoint Mass Task Experiment 2

Fig. 3 shows trajectory plots from Experiment 2 (Endpoint Mass Task), which closely parallel those in Figure 2 from Experiment 1 (Kinematic Arm Task).

Fig. 3A displays the outward extrinsic and intrinsic trajectories during the initial null phase for a typical participant. As in Experiment 1, extrinsic paths were initially erratic, whereas intrinsic movements showed segmented, independent control of both inputs.

Fig. 3B shows the final null block, where extrinsic trajectories became straighter and intrinsic hand movements continuous and coordinated.

Fig. 3C and Fig. 3D show the mean ± SE extrinsic outward trajectories across participants in the clockwise (CW) and counterclockwise (CCW) conditions, respectively. Movements initially deviated significantly from the straight-line paths but straightened by the end of the null phase. Introduction of the curl field led to systematic curvature, which diminished with adaptation. Upon washout, typical after-effects emerged, showing curvature opposite to the field direction.

Fig. 3E presents mean ± SE speed profiles for extrinsic movements. Early movements were slow with flat-topped profiles; by the end of the null phase, a clear single peak resembling minimum-jerk profile emerged, though still somewhat asymmetric. The curl field initially reduced peak speed and skewed the profile, but symmetry and peak velocity improved by the end of exposure. Washout produced more variable speed profiles.

Fig. 3F shows catch trial trajectories from individual participants at the start, end of null training, and end of curl field training. As in Experiment 1, early catch movements were often misdirected or poorly scaled. With training, both direction and movement length improved, reflecting better feedforward control of the virtual arm.

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Figure 3. Trajectory plots for Experiment 2 – Endpoint Mass Task. **A:** Representative
extrinsic and intrinsic trajectories from the first null trials of an individual participant. **B:**
Representative extrinsic and intrinsic trajectories from the final null trials of the same
participant. **C:** Mean ± SE extrinsic outward path trajectories for the CW curl field
condition. **D:** Mean ± SE extrinsic outward path trajectories for the CCW curl field
condition. **E:** Mean ± SE extrinsic speed profiles across CW and CCW trials. **F:**
Extrinsic catch trial trajectories for the first 8 null blocks, the final 8 null blocks, and the
final 8 curl blocks. Trajectories to the 0°, 90°, 180°, and 270° targets are plotted in red,
green, blue, and black, respectively.
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Examining Effects within Experiments

We quantified movement trajectory quality with four metrics, AMPE, SMPE, movement duration, and path length, first averaging values across pairs of trial blocks (32 trials per pair). The mean ± SE values of each metric across participants are plotted in Fig. 4. Since experiments ran over two separate sessions, we noted a slight discontinuity in metrics at the start of the second session.

To check for significance within each experimental condition, we compared the metrics at critical stages. At the start of the experiment (initial null phase), at the end of the arm control training phase (final null phase), at the onset of curl field exposure (initial curl phase), at the end of curl field exposure (final curl phase), and finally during the curl field washout (washout phase).

Movement Metrics Plots Experiment 1

The AMPE values are plotted in Fig. 4A in blue. Repeated measures ANOVAs indicated that AMPE showed significant variations between the initial null, final null, initial curl, final curl, and washout phases. Post-hoc comparisons further tested the significant differences between these phases. In this experimental condition ($F = 11.366$; $p < 0.001$; $\omega^2 = 0.463$), AMPE was high at the initial null phase, but it was significantly reduced by the final null phase ($p_{bonf} = 0.027$). Upon introduction of the curl field in the initial curl phase, it significantly increased ($p_{bonf} < 0.001$). By the final curl phase, AMPE significantly decreased ($p_{bonf} = 0.043$). At the washout phase, AMPE showed a significant difference compared to the final curl phase ($p_{bonf} = 0.047$).

The SMPE values are plotted in Fig. 4B in blue. Repeated measures ANOVAs indicated that SMPE showed significant variations between the initial null, final null, initial curl, final curl, and washout phases. Post-hoc comparisons further tested the significant differences between these phases. In the experimental condition ($F = 26.061$; $p < 0.001$; $\omega^2 = 0.617$), SMPE was highest at the initial null phase, but did not significantly decrease by the final null phase ($p_{bonf} = 1.0$). Upon introduction of the curl field in the initial curl phase, it significantly increased ($p_{bonf} < 0.001$). By the final curl phase, SMPE significantly decreased in a fashion typical of that seen in normal curl field exposure experiments ($p_{bonf} = 0.049$). SMPE at the washout phase showed a significant difference compared to the final curl phase ($p_{bonf} = 0.002$).

The movement duration is plotted in Fig. 4C in blue. Repeated measures ANOVAs indicated that movement duration showed significant variations between the initial null, final null, initial curl, final curl, and washout phases. Post-hoc comparisons further tested the significant differences between these phases. In the experimental condition ($F = 30.213$; $p < 0.001$; $\omega^2 = 0.728$). Movement duration was high at the initial null phase, but was significantly reduced by the final null phase ($p_{bonf} = 0.006$). Upon introduction of the curl field in the initial curl phase, it significantly increased ($p_{bonf} = 0.009$). By the final curl phase, movement duration significantly decreased ($p_{bonf} = 0.029$). Movement duration at the washout phase showed no significant difference compared to the final curl phase ($p_{bonf} = 0.639$).

Extrinsic path length is shown in Fig. 4D in blue. Repeated measures ANOVAs
indicated that path length showed significant variations between the initial null, final
null, initial curl, final curl, and washout phases. Post-hoc comparisons further tested
the significant differences between these phases. In the experimental condition (F =
11.269; p < 0.001; ω^2 = 0.466), path length was high at the initial null phase, but it did
not significantly reduce by the final null phase (p_{bonf} = 0.061). Upon introduction of the
curl field in the initial curl phase, it significantly increased (p_{bonf} < 0.001). By the final
curl phase, path length significantly decreased (p_{bonf} = 0.008). Path length at the
washout phase showed a significant difference compared to the final curl phase (p_{bonf}
= 0.044).

Movement Metrics Plots Experiment 2

Fig. 4A green plot shows the AMPE. Repeated measures ANOVAs indicated that
AMPE showed significant variations between the initial null, final null, initial curl, final
curl, and washout phases. Post-hoc comparisons further tested the significant
differences between these phases. In the experimental condition (F = 23.674; p <
0.001; ω^2 = 0.629), AMPE was high at the initial null phase, but it significantly reduced
by the final null phase (p_{bonf} = 0.014). Upon introduction of the curl field in the initial
curl phase, it significantly increased (p_{bonf} < 0.001). By the final curl phase, AMPE
significantly decreased (p_{bonf} = 0.004). AMPE at the washout phase showed a
significant difference compared to the final curl phase (p_{bonf} = 0.004).

Fig. 4B green plot shows the SMPE. Repeated measures ANOVAs indicated that
SMPE showed significant variations between the initial null, final null, initial curl, final
curl, and washout phases. Post-hoc comparisons further tested the significant
differences between these phases. In the experimental condition (F = 14.013; p <
0.001; ω^2 = 0.504), SMPE was highest at the initial null phase, but did not significantly
reduce by the final null phase (p_{bonf} = 1.000). Upon introduction of the curl field in the
initial curl phase, it significantly increased (p_{bonf} = 0.003). By the final curl phase,
SMPE significantly decreased (p_{bonf} = 0.013). SMPE at the washout phase showed a
significant difference compared to the final curl phase (p_{bonf} < 0.001).

The movement duration is plotted in Fig. 4C in green. Repeated measures ANOVAs
indicated that movement duration showed significant variations between the initial null,
final null, initial curl, final curl, and washout phases. Post-hoc comparisons further
tested the significant differences between these phases. In the experimental condition
(F = 166.581; p < 0.001; ω^2 = 0.923), Duration was high at the initial null phase, but it
significantly reduced by the final null phase (p_{bonf} < 0.001). Upon introduction of the
curl field in the initial curl phase, it significantly increased (**p_{bonf} = 0.016**). By the final
curl phase, movement duration significantly decreased (p_{bonf} < 0.001). Movement
duration at the washout phase showed a significant difference compared to the final
curl phase (p_{bonf} = 0.031).

Fig. 4D green plot displays movement path length. Repeated measures ANOVAs
indicated that path length showed significant variations between the initial null, final
null, initial curl, final curl, and washout phases. Post-hoc comparisons further tested
the significant differences between these phases. In the experimental condition (F =

23.558; p < 0.001; ω^2 = 0.647), path length was high at the initial null phase, but it did
significantly reduce by the final null phase (p_{bonf} = 0.013). Upon introduction of the curl
field in the initial curl phase, it significantly increased (p_{bonf} < 0.001). By the final curl
phase, path length significantly decreased (p_{bonf} = 0.009). Path length at the washout
phase showed a significant difference compared to the final curl phase (p_{bonf} = 0.020).
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Comparison of Metrics Across Experiments

To compare the two experimental conditions, we plotted the four metrics AMPE,
SMPE, duration and path length against block pairs, as shown in Fig. 4. In addition,
we ran ANOVAs to compare metrics computed over 10 blocks (160 trials) at the end
of the kinematic learning, at the start curl field exposure, and at the final curl field
exposure phases between Kinematic Arm Experiment 1 and the Endpoint Mass
Experiment 2.
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Fig. 4A shows AMPE decreases in both experimental conditions. The final null phase
showed a significant variation across experimental conditions (F = 4.778; p =0.046; ω^2
= 0.191). The first curl phase showed a significant variation across experimental
conditions (F = 15.405; p =0.002; ω^2 = 0.474). Post-hoc comparisons revealed a
significant difference (p =0.002). The final curl phase showed a significant variation
across experimental conditions (F = 8.492; p = 0.011; ω^2 = 0.319). Throughout training,
the use of an endpoint mass consistently results in lower AMPE values than those
observed in the kinematic arm condition. Notably, at the end of the null field phase,
AMPE had decreased to a lower value in the mass condition. When the curl field was
introduced, AMPE rose again in both experimental conditions. However, the kinematic
arm condition showed a consistently higher AMPE compared to the mass condition.

Fig. 4B shows the trajectory SMPE plotted against pairs of trial blocks. The final null
phase showed no significant variation across experimental conditions (F = 0.176; p =
0.681; ω^2 = 0.000). The first curl phase showed a significant variation across
experimental conditions (F = 32.405; p < 0.001; ω^2 = 0.662). Post-hoc comparisons
revealed a significant difference (p < 0.001). The final curl phases showed a significant
variation across experimental conditions (F = 9.015; p = 0.010; ω^2 = 0.334).

When no curl field is present, the SMPE value indicates little bias in movement
trajectories. Consequently, in both training conditions, with and without the endpoint
mass, the SMPE values remained close to the zero baseline. However, upon
introduction of the curl field, there is a dramatic increase in SMPE in both conditions.
In the kinematic arm condition, this value exhibited a slower decay and maintained a
large offset bias. In contrast, the endpoint mass condition shows a rapid decay in
SMPE, returning closer to the baseline value. In both conditions, expected washout
effects were observed, with SMPE values changing sign, indicating that predictive
compensation to the novel curl field dynamics had developed.

Fig. 4C shows the movement duration across pairs of trial blocks over the
experiments. The final null phase showed a significant variation across experimental
conditions (F = 18.603; p < 0.001; ω^2 = 0.524). The first curl phase showed a significant
variation across experimental conditions (F = 6.952; p = 0.020; ω^2 = 0.271). The final

curl phase showed no significant variation across experimental conditions (F = 2.218;
p = 0.159; ω^2 = 0.071). Thus, movement durations were generally shorter in the
kinematic arm condition, suggesting participants moved more slowly when performing
the endpoint mass task.

Fig. 4D shows the extrinsic trajectory length over trial block pairs, for both experiments.
The final null phase showed no significant variations across experimental conditions
(F = 1.171; p =0.441; ω^2 = 0.070). The first curl phase showed no significant variation
across experimental conditions (F = 0.965; p = 0.512; ω^2 = 0.000). The final curl phase
showed no significant variation across experimental conditions (F = 0.830; p = 0.591;
ω^2 = 0.000).

To summarize the main results, by the end of the kinematic learning phase, training
with haptic feedback (endpoint mass condition) produced significantly straighter
movements as indicated by lower AMPE values. In addition, the endpoint mass
condition led to straighter movements at the onset of curl field exposure and greater
adaptation by the end of the curl field exposure phase. This was reflected in both
AMPE and SMPE measurements. The duration of movements was significantly longer
in the endpoint mass condition; however, the path length did not differ significantly.
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Figure 4. Comparison of movement metrics between Experiment 1 – Kinematic Arm
(blue) and Experiment 2 – Endpoint Mass Task (green). **A:** Mean ± SE extrinsic
absolute maximum perpendicular error (AMPE) shown over the experiments. **B:** Mean
± SE extrinsic signed maximum perpendicular error (SMPE) over the experiments. **C:**
Mean ± SE trial duration over the experiments. **D:** Mean ± SE extrinsic path length
over the experiments.

Discussion (1500/1500)

Summary

This study demonstrates that augmenting practice with haptic force feedback from a
simulated endpoint mass facilitates the De Novo learning of arm kinematics and
dynamics in a virtual 2D environment. Although both groups of participants initially
exhibited similar learning trajectories, those who trained with the simulated mass
ultimately achieved greater inter-limb coordination and straighter movement paths in
extrinsic space over time.

In the Kinematic Task (Experiment 1), participants initially moved their hands sequentially, briefly arresting one hand before advancing the other. However, they soon adopted simultaneous bimanual movements and extrinsic trajectories progressively straightened with practice. Upon introduction of a curl field, trajectories initially showed pronounced curvature, but these straightened with continued exposure, similar to typical behavior observed in curl field learning. However, observation of the SMPE suggested that adaptation was incomplete by the end of the curl field exposure.

The Endpoint Mass Task (Experiment 2), which added a 2 kg endpoint mass, displayed parallel trends. Early movements again featured independent hand control, but the simulated inertia induced noticeable overshoot. As training progressed, participants quickly adopted simultaneous movements and gradually learned to control the arm to perform point-to-point movements, again resulting in straighter extrinsic trajectories with practice. Upon introduction of the curl field, loopy trajectories were again observed, though to a lesser extent than in Experiment 1, and the SMPE was considerably lower. The systematic bias seen in Experiment 1 was absent and SMPE values had nearly returned to baseline by the end of curl field exposure.

Crucially, when exposed to a novel dynamic perturbation (curl field), robust adaptation emerged exclusively in the force-feedback group, likely due to prior exposure to endpoint force control, which reduced trajectory biases. These findings suggest that experiencing physical forces during training enriches internal models used for motor control, enabling more robust generalization to new dynamic contexts. This has important implications for the design of training protocols in rehabilitation, robotics, and skilled tool use, where incorporating force feedback could accelerate and enhance motor learning.

Stereotypical Behaviors

Human point-to-point reaching movements exhibit stereotyped kinematic regularities. Work examining hand movements has consistently shown that participants exhibit specific invariant features (Morasso, 1981; Atkeson, 1989; Flanagan and Rao, 1995; Burdet and Milner, 1998; Sailer et al., 2005). These include (i) bell-shaped velocity profiles (Flash and Hogan, 1985), (ii) distinct acceleration and deceleration phases (Soechting and Lacquaniti, 1981; Gottlieb, 1998), and (iii) trajectories that are predominantly straight (Abend et al., 1982), although slight curvature may be observed depending on workspace geometry (Atkeson and Hollerbach, 1985; Boessenkool et al., 1998).

We observed comparable characteristics in extrinsic trajectories of the virtual arm endpoint: paths progressively straightened with practice, and the corresponding speed profiles became increasingly symmetric and bell-shaped. The former phenomenon has also been previously reported in brain–machine interface (BMI) tasks when visual feedback of movement is available (Danziger and Mussa-Ivaldi, 2012).

Another aspect of our experiments reveals how participants explored the novel kinematics during the early stages of De Novo learning. In developmental robotics, exploratory behaviors such as babbling have been used to develop transformations

between coordinate frames (Fiala, 1994), and to learn control policies (Demiris and
Dearden, 2005). Extending this idea, goal babbling has been proposed as a method
for learning the inverse kinematics of robotic arms (Rolf et al., 2010; Rolf and Steil,
2014), where exploration is directed toward achieving desired outcomes. Similarly,
goal-directed feedback has been shown to facilitate skill learning in humans (Rohde
et al., 2019). In our study, participants appeared to engage in a form of goal-directed
exploration, using feedback to iteratively refine their understanding of the novel
kinematic transformations.
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Haptic Feedback and Networks in the Brain

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Proprioceptive acuity training has been shown to enhance motor learning (Wong et
al., 2012). Haptic feedback likely facilitates De Novo motor learning by providing rich
proprioceptive and tactile information. This may enhance the engagement of
distributed neural networks, including the cerebellum for predictive modeling and
internal model formation (Shadmehr and Krakauer, 2008; Izawa and Shadmehr,
2011), the somatosensory and parietal cortices for integrating haptic input and
updating limb representations (Wolpert et al., 1998; Diedrichsen et al., 2005), and
motor areas for encoding novel dynamics and motor skill acquisition (Sanes and
Donoghue, 2000; Galea et al., 2011). Importantly, De Novo learning appears to recruit
a broader set of neural circuits compared to traditional adaptation tasks, reflecting the
need to construct entirely new control policies rather than merely modifying existing
ones.
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While cerebellar circuits are heavily implicated in adaptation through the computation
of sensory prediction errors (Tseng et al., 2007; Izawa and Shadmehr, 2011), De Novo
learning engages additional regions such as the basal ganglia and prefrontal cortex
(Doyon et al., 2009; Hardwick et al., 2013; Dhawale et al., 2017). The basal ganglia
support reinforcement learning processes that help select successful movement
strategies, whereas the prefrontal cortex facilitates the maintenance and flexible
updating of new sensorimotor mappings, particularly during the exploratory phases of
learning (Taylor and Ivry, 2014; Haith and Krakauer, 2018). As learning progresses,
gradual reorganization within sensorimotor areas, including the primary motor cortex
(M1) and premotor regions, consolidates novel control policies into more automatic
motor programs (Mawase et al., 2018; Yokoi and Diedrichsen, 2019). Together, the
engagement of this distributed network underscores the complexity of De Novo skill
acquisition and highlights the interplay between error-driven, reinforcement-based,
and strategic processes necessary for building new action-outcome associations.
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De Novo Learning

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The relative ease with which we can learn novel tasks, even those involving almost
arbitrary kinematics and dynamics, suggests that the motor system inherently
possesses the ability to perform system identification and develop adaptive control
strategies. This capability is not confined to the kinematics and dynamics of our own
bodies. We are also proficient at learning how to use extensions of our bodies, learning
how to use simple tools such as hammers, spanners, and screwdrivers. Moreover, we
can attain mastery over more complex systems, such as driving a car or operating an

excavator. The latter example closely resembles the scenario investigated in this
study, namely learning to control a novel arm.

When encountering a new motor task with an unfamiliar muscle-to-movement
mapping, predictive motor commands cannot be generated due to the absence of prior
knowledge. Consequently, exploration of muscle activity space becomes essential to
learning this relationship. Notably, this situation resembles the developmental
challenges faced by infants in learning goal-directed reaching (von Hofsten, 1984;
Konczak et al., 1995; Konczak and Dichgans, 1997) and how it relates to our novel
arm task. Learning requires the ability to evaluate actions, and improvement heavily
relies on visual feedback, with haptic feedback also playing a valuable role.

Motor skill acquisition (Schmidt, 1975; Newell, 1991) involves the improvement of
movement and task performance through practice (Willingham, 1998). This process
ranges from simple adaptation to changes in kinematics or dynamics. Early research
quantified the nature of arm kinematics and dynamics (Atkeson, 1989). Subsequent
studies have furthered our understanding of how the motor system learns to navigate
unfamiliar environments. For instance, research on De Novo learning has investigated
how individuals adapt their motor skills to map and manipulate new spatial contexts
(Mosier et al., 2005). In that study, participants learned to control a cursor through
coordinated movements and developed a mental representation of Euclidean space
for remapping hand movements. Training with terminal visual feedback resulted in
smoother cursor trajectories and reduced unnecessary movements in non-critical
degrees of freedom. Notably, full visual feedback accelerated the learning process.

A study using a novel visuomotor task investigated the mapping between isometric
bimanual actions and the control of a cursor in 3D. Participants exhibited distinct
stages in their behaviors (Sailer et al., 2005). Notably, studies have shown how
patients adapt to using artificial limbs (Maimon-Mor et al., 2021). Electromyogram
signals have enabled control of cursor movements (Radhakrishnan et al., 2008) or a
virtual mass (Berger et al., 2013). Neural signals have similarly been used for cursor
control (Oby et al., 2019), and the operation of prosthetic devices (Ganguly and
Carmena, 2009).

Brain–Machine Interfaces (BMIs) are often studied as a means to control prosthetic
limbs (Casadio et al., 2012) and have broadened the scope of research from simple
adaptations to more substantial changes in dynamics and vision, as well as to enhance
our understanding of neural representations (Orsborn et al., 2014; Sadtler et al., 2014).

Although not investigated here, De Novo learning has also been examined in tasks
beyond point-to-point movements, including continuous tracking under rotation and
mirror reversal of visual feedback (Yang et al., 2021). Subsequent studies investigated
the influence of noise and the estimation of sensitivity derivatives in De Novo learning
(Dal'Bello and Izawa, 2022).

A comprehensive study of long-term De Novo bimanual learning was also undertaken,
highlighting the long timescale needed to achieve baseline performance (Haith et al.,
2022). Over time, the process of learning De Novo control becomes habitual (Yang et
al., 2022). More recently, neural network models (specifically recurrent neural
networks, RNNs) have been investigated to examine De Novo learning (Chang et al.,

2024), providing a new modeling paradigm to investigate and explain human
sensorimotor control.

Author Contributions

970 ISH conceived, designed, and implemented the current study. LAH conducted data
971 collection. Data analysis was carried out by ISH. The initial draft of the manuscript was
972 written by ISH. Both authors (ISH and LAH) reviewed and edited the manuscript.

Competing Interest Statement

975 The authors declare that they have no financial, personal, or professional interests
976 that could be construed to have influenced the paper.

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