PEtab Select: specification standard and supporting software for automated model selection

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Abstract

A central question in mathematical modeling of biological systems is determining which processes are most relevant and how they can be described. There are often competing

hypotheses, which yield different models. Model comparison requires parameter optimization and sampling methods. Yet, standards for the specification of model selection problems and the swift evaluation of a broad spectrum of approaches are not available.

PEtab Select addresses this challenge by providing a concise, standardized specification of model selection and its associated calibration problems through a new file format standard and software package. The standard facilitates the compact representation of even very large model selection problems; in one example, billions of model alternatives. PEtab Select builds on the PEtab standard for the specification of parameter estimation problems, and enables the use of state-of-the-art modelling and calibration workflows utilizing COPASI, Data2Dynamics, PEtab.jl, and pyPESTO. PEtab Select supports common model selection criteria (e.g., Akaike and Bayesian information criteria) and can be easily extended to use others. To ensure flexibility, PEtab Select implements several model space exploration approaches, including basic brute-force, forward, and backward selection, and also advanced, flexible selection methods.

PEtab Select introduces the first standardization of model selection tasks, filling a critical gap in existing computational pipelines. It constitutes an essential contribution to FAIR research software in systems biology by promoting interoperability and reusability in model selection.

Author summary

Model selection is a crucial step in mathematical modeling, guiding the choice of components to include in a model. PEtab Select automates this process across diverse modeling frameworks and programming languages via (1) a new interoperable, language-agnostic standard for specifying large-scale model selection problems, and (2) a comprehensive software package that implements these selection methods. Developed through a community effort, PEtab Select has been integrated into multiple modeling frameworks and is accessible to users of COPASI, Julia, MATLAB, and Python.

Introduction

In systems biology, mechanistic models are employed for various purposes, including explaining and predicting process dynamics, guiding experimental design, and evaluating hypotheses [1, 2]. However, developing these models typically requires translating biological assumptions into mathematical formulations, a process that is subject to two primary sources of error. Firstly, the underlying biological hypotheses may be incomplete or inaccurate. Secondly, the conversion of these hypotheses into mathematical expressions may be faulty. In both instances, model selection techniques are valuable because they quantify the capacity of competing hypotheses—or their mathematical representations—to account for observed data [3].

Nowadays, there are several advanced workflows for the iterative development of mechanistic models for biological processes, which cover tasks such as model definition, simulation, parameterization, and uncertainty quantification. Model definition can be performed using standards like the Systems Biology Markup Language (SBML) [4], an Extensible Markup Language (XML)-based format capable of encoding biochemical reaction networks, which can be compiled to ordinary differential equations. Model simulation, parameterization, and uncertainty quantification can be specified using the Simulation Experiment Description Markup Language (SED-ML) [5] and the Parameter Estimation tables (PEtab) standard [6]. While SED-ML is an XML-based format, PEtab involves tab-separated value (TSV) files and YAML Ain't Markup Language (YAML) files. PEtab provides a flexible definition of measurement data, experimental conditions, observation models, and the parameters (including their priors) to be estimated. An ecosystem of software tools supports these formats, enabling seamless integration across diverse computing platforms and programming languages.

Some of these software tools also support model selection using information criteria (e.g., the Akaike Information Criterion (AIC) [7], corrected AIC (AICc) [8], or the Bayesian Information Criterion (BIC) [9]), Bayes factors [10], statistical tests including likelihood ratio tests [11], or cross-validation [12]. In fact, there are also software tools that allow for the selection of relevant features and the improvement of parameter identifiability through model reduction [13–17], facilitate model reduction for improved identifiability [18], or enable multi-model inference [19]. The most versatile tools appear

to be Data2Dynamics (D2D) [20], dMod [21], pyPESTO [22], and BioModel Selection   32
System 2 (BMSS2) [23]. However, none of these software tools provide comprehensive   33
support for all methods, and the specification of model selection problems is often   34
limited.   35

To address this critical gap, we introduce the PEtab Select standard, for the   36
encoding of model selection problems in systems biology. The standard has been   37
developed in a community effort and expands upon the widely adopted SBML [4]   38
standard for describing mechanistic models and PEtab [6] for specifying parameter   39
estimation problems. By providing a flexible encoding scheme for model selection, the   40
standard allows for a compact description of thousands of candidate models using only a   41
few lines, thereby facilitating large-scale comparative analyses. Crucially, the standard   42
retains compatibility with existing workflows by building on recognized community   43
standards, eliminating the need for researchers to adopt entirely new toolchains.   44

Alongside the standard, we also provide a reference PEtab Select software package,   45
which integrates seamlessly into established modeling workflows. The package can   46
interface with popular PEtab-compatible systems biology model calibrators — such as   47
Data2Dynamics [20], PEtab.jl [24], pyPESTO [22], and COPASI [25] via   48
BasiCO [26] — leveraging the strengths of each. Implementing a truly general solution   49
for model selection poses significant challenges, given the need for interoperable file   50
formats and libraries compatible with diverse programming languages. The package   51
addresses these challenges by building on community-endorsed standards and providing   52
efficient built-in algorithms for model selection, including brute force, forward selection,   53
backward selection, and FAMoS [27], the latter of which is designed for large model   54
spaces. The subsequent sections detail the PEtab Select standard and package, and   55
discuss how they can be readily combined with pre-existing calibration workflows to   56
streamline model selection tasks (Fig. 1).   57

Design and implementation   58

In this section, we outline the aims of PEtab Select and describe how they are fulfilled   59
by the proposed new PEtab Select file format standard (hereby, standard) and   60
accompanying PEtab Select reference software package (hereby, package), alongside   61

Fig 1. Model selection workflow with PEtab Select (1) The user defines the
model selection **problem**, including the model space and the mathematical description
of the set of possible process components, in the **standard**. (2) The user runs model
selection via a **calibration tool** by sending the PEtab Select problem to the PEtab
Select **package**, which initiates iterations of model selection. (2a) The package provides
model candidates to the calibration tool based on the problem specification and the
available calibration results. (2b) The calibration tool calibrates the proposed candidate
models and sends the calibration results to the package. Iterations of (2a) and (2b)
continue until the package sends a termination signal to indicate the end of model
selection. The results are provided in the PEtab Select model format and include all
calibrated models with their calibration results. (3) The package can be used to perform
subsequent analyses and visualizations of the results.

pre-existing software for calibrating models (hereby, calibration tools). Subsequently, we ₆₂

detail the design and implementation of PEtab Select, which builds on the SBML and ₆₃

PEtab standards to ensure broad compatibility with existing workflows. ₆₄

Scope

The model selection process begins by defining a set of admissible candidate models $\mathcal{M}$. In many cases, this set can be derived from a single, overarching "superset model" that encodes all processes under consideration; specific processes may then be removed or deactivated to yield distinct candidate models. When the range of competing hypotheses is broad, there may be multiple superset models, each reflecting different conceptual assumptions or alternative sets of biological processes. For each of the candidate models in $\mathcal{M}$ there exists a corresponding parameter estimation problem that needs to be solved to compute the selection criteria. Importantly, to ensure the comparability of the values of the selection criteria, all estimation problems have to use the same dataset (and transformations of the dataset are not allowed). Model selection methods iterate over the set of admissible models until a stopping condition is met (e.g., no further improvement is achieved).

The PEtab Select ecosystem addresses these steps comprehensively. PEtab Select allows for (1) defining the model selection problem in the standard in terms of mathematical models and corresponding parameter estimation problems, (2) using a compatible calibration tool to fit the candidate models according to one of the model selection methods implemented in the package, and (3) receiving the final selection results in the standard format, and analyzing them with the package (Fig. 1).

The PEtab Select standard

The standard is an extension to the existing **PEtab** standard, utilizing the same TSV and YAML-based structure while introducing additional configuration options for model selection. Indeed, the standard preserves the core PEtab specification, which defines a parameter estimation problem through tables of model parameters, experimental conditions, observables, and measurement data. Building on this, the standard adds a new layer dedicated to specifying the model space and relevant selection details (e.g., the subset of processes or reactions that can be toggled, the selection method to apply, and the selection criterion to use). This design ensures that existing PEtab workflows remain valid, while enabling that large and complex model spaces can be described in a concise manner (see Fig. 3 for an example). The standard file formats are designed to

be easy for both humans and machines to read and write, facilitating collaborative development and straightforward integration into broader systems biology pipelines.

Model space (TSV) The model space is the set of models to perform model selection on. In the standard, this can be defined as any combination of single models and superset models, from which multiple models are derived.

An example of defining a model space based on two superset models is given in Fig. 2. Each superset model has an associated mathematical model and parameter estimation problem specified in the `model_subspace_petab_yaml` column. The set of submodels is constructed by customizing the superset model with all combinations of *plausible parameter values* in the additional table columns; for this specific example, subspaces `supersetA_models` and `supersetB_models` encode 16 (Fig. 2d) and 8 models, respectively.

The model space table is flexible to support a variety of use cases. A subspace with a single model can be specified by single numerical values or "`estimate`" in the *Plausible parameter values* columns, as opposed to semicolon-delimited lists. In this way, subspace `supersetB_models` could have alternatively been specified as 8 rows of single-model subspaces in the table. When dealing with multiple superset models that have different parameters (e.g., `k_3` is in `problem1.yaml` but not `problem2.yaml`), users may opt to use one model space table per superset model, to avoid sparsity or dummy parameters.

Note that for the example superset models in Fig. 2b and c, processes are turned "off" by setting parameters to 0, which is not always the case. For example, a fold-change effect parameter might be turned off by setting it to 1.

Model files (YAML) Given mathematical models, parameter estimation problems, and the model space, the package can run model selection methods. As the methods require calibrated models, the package sends the uncalibrated models to a calibration tool, which calibrate the models and then send the results back to the package (step 2 in Fig. 1).

The standard model file format is used to transmit all model information at different steps of the workflow (Fig. 1): in step 1, the initial models of a method; in step 2, the models communicated between the package and calibration tools; and, in step 3, the

(a) The PEtab Select model space table.

Model subspace metadata		Plausible parameter values			
model_subspace_id	model_subspace_petab_yaml	k_1	k_2	k_3	k_4
supersetA_models	problem1.yaml	0;estimate	0;estimate	0;estimate	1.5;2.5
supersetB_models	problem2.yaml	0;estimate	0;estimate	0	0;estimate

(b) The superset model for the subspace `supersetA_models`.

(c) The superset model for the subspace `supersetB_models`.

(d) All models in the subspace `supersetB_models`.

Fig 2. Example model space. (a) The model space table encodes model subspaces as rows. Each model subspace has an ID and an associated superset PEtab problem, which includes the mathematical model. This superset problem is customized into single models according to the remaining columns, which contain semicolon-delimited lists of values that parameters (column headers) can take in the subspace. (b,c) Each subspace is associated with a superset model, where all possible parameters are estimated. (d) Based on a superset model, candidate models are encoded by turning (estimation of unknown) parameters on or off.

results, such as all calibrated models or the best model. The information in the standard model file format includes: the properties (e.g. model subspace ID and estimated parameter IDs) that uniquely identify this model; the PEtab problem; and calibration results, such as the AIC value.

In a typical workflow, the model files (or equivalent Python objects) during steps 2 and 3 are automatically produced by the package and the PEtab-compatible calibration tool. The user can optionally specify initial models in step 1 manually, as done in test case 0009 of the PEtab Select test suite, or use the PEtab Select software package to generate initial model(s).

Model selection problem file (YAML)   As in PEtab, the standard uses a single YAML-based model selection "problem" file to combine all files of the model selection

problem, such that compatible tools can load the model selection problem from a single ¹³⁶
file. The standard problem file also contains settings, including the model selection ¹³⁷
method to use, and the criterion by which models will be compared. ¹³⁸

The PEtab Select package ¹³⁹

The primary purpose of the package is to extend state-of-the-art calibration workflows, ¹⁴⁰
by providing an API that calibration tools can use to enable model selection capabilities. ¹⁴¹
The package performs all model selection functions except for model calibration, which ¹⁴²
is performed by the calibration tool. Hence, users can choose their preferred compatible ¹⁴³
calibration tool that contains the features they need. ¹⁴⁴

Intended usage   For this primary purpose, the user might never interact with the ¹⁴⁵
package directly, rather indirectly via their preferred calibration tool. Hence, within this ¹⁴⁶
primary workflow (Fig. 1), users supply their specification files (model, PEtab, and ¹⁴⁷
PEtab Select files) to their calibration tool, then initiate model selection. Iterations of ¹⁴⁸
the chosen model selection algorithm are then coordinated manually by the user and/or ¹⁴⁹
automatically by the calibration tool, until the model selection problem is solved. ¹⁵⁰
Results are made available as calibrated models in the standard model format, that are ¹⁵¹
stored in memory or on disk. ¹⁵²

Calibration tools   For a tool to perform model selection with PEtab Select, the tool ¹⁵³
needs to be able to calibrate PEtab problems and implement the package API. The ¹⁵⁴
package is written in Python 3 and the API is available via Python or the command ¹⁵⁵
line, such that calibration tools written in different languages can easily integrate PEtab ¹⁵⁶
Select. A test suite with several model selection problems is available to ensure the ¹⁵⁷
compatibility of calibration tools with the package. ¹⁵⁸
    We have worked with the developers of different state-of-the-art pipelines to ¹⁵⁹
integrate PEtab Select, such that users who are already familiar with one of the ¹⁶⁰
pipelines can easily add model selection to their workflow. Currently, PEtab Select is ¹⁶¹
supported by COPASI [25] via BasiCO (Python) [26], Data2Dynamics ¹⁶²
(MATLAB) [1, 20], PEtab.jl (Julia) [24], and pyPESTO (Python) [22]. ¹⁶³

Other features The package provides several other features to enable flexible model   164
selection. This includes automated summaries of the model selection run, custom or   165
automated selection of initial models, limits on the number of models calibrated in any   166
iteration, restarting of model selection runs with previous model selection results, and   167
object-oriented programming such that other methods and selection criteria can be   168
easily implemented.   169

Model selection methods   170

Model selection methods can be broadly classified as global or local. In each algorithm,   171
models are calibrated and compared by a model selection criterion. In this section, bold   172
terms are methods and features that are available in the package.   173

Global methods   To guarantee that the best model in the model space is identified, a   174
global method is required. An example is the **brute-force** method, where every model   175
is calibrated. However, if a model space is generated from a superset model with n 176
components, then there are potentially 2^n plausible models in the model space. The   177
brute-force method would therefore involve 2^n model calibrations, which may be   178
computationally-infeasible.   179

Local methods   To mitigate this, local methods such as stepwise regression can be   180
employed. Local methods do not guarantee that the best model is found, but instead   181
explore the model space efficiently to find good models. An example stepwise regression   182
method is the **forward** method, which proceeds in iterations and begins with an initial   183
(first predecessor) model. In each iteration, all models with one additional estimated   184
parameter, compared to the predecessor model, are calibrated. The best of these models   185
is then selected as the predecessor model for the next iteration. Iterations proceed until   186
the models in the current iteration do not improve on the current predecessor model,   187
and then this predecessor model is selected as the best model. The **backward** method   188
is similar but proceeds in the reverse direction, calibrating models with one fewer   189
estimated parameters than the predecessor model.   190

The **FAMoS** method is an advanced local stepwise regression method that uses   191
metaheuristics to change the local method employed over iterations [27]. Each FAMoS   192

iteration involves the full run of all iterations of a simple method, such as the forward or ₁₉₃
backward method, or the **lateral** method, wherein simultaneous forward and backward ₁₉₄
changes are applied that keep the number of estimated parameters the same as the ₁₉₅
predecessor model. Between FAMoS iterations, a method switching scheme is employed ₁₉₆
to switch between local methods, based on the recent history of employed methods. For ₁₉₇
example, if the previous method was the backward method, and the current method is ₁₉₈
the forward method, then the next method is the lateral method. In PEtab Select, this ₁₉₉
method switching scheme is fully customizable. The FAMoS method also supports a ₂₀₀
"jump to most distant" local method. Full details of the FAMoS method are provided in ₂₀₁
Gabel et al. (2019) [27]. ₂₀₂

Model selection criteria   All methods involve model comparisons according to a ₂₀₃
model selection criterion, in order to select the best or good models. Typically, these ₂₀₄
criteria try to simultaneously maximize both model goodness-of-fit and model ₂₀₅
parsimony. This involves a trade-off, since less parsimonious models tend to provide a ₂₀₆
better goodness-of-fit due to overfitting. Examples of such criteria include the **Akaike** ₂₀₇
information criterion (AIC) [7], **corrected AIC** (AICc) [8], **Bayesian information** ₂₀₈
criterion (BIC) [9]. The choice of criteria is nontrivial, with both philosophical and ₂₀₉
problem-dependent aspects. The AIC tends to select larger models for larger datasets, ₂₁₀
which may be undesirable. The AICc adds a small sample size correction factor to the ₂₁₁
AIC to mitigate overfitting, but this correction factor is derived for univariate linear ₂₁₂
models with Gaussian-distributed residuals, and hence may perform poorly with other ₂₁₃
models. The BIC is designed to select a model with a similar dimension as the ₂₁₄
data-generating process but uses a Taylor-series approximation of the log-likelihood and, ₂₁₅
like the AIC, is an asymptotic result that may perform poorly on smaller datasets. ₂₁₆

FAIR data principles ₂₁₇

The FAIR data principles [28] provide guidance on achieving human-out-of-the-loop ₂₁₈
re-usability, through the implementation of many principles that enable machine ₂₁₉
actionability. While the principles of findable and accessible data are out-of-scope here, ₂₂₀
PEtab Select implements several of the principles for interoperability and re-usability: ₂₂₁
the standard involves machine-readable file formats including YAML and TSV; the ₂₂₂

controlled vocabulary of keywords in the standard is documented and schemas for the ²²³

standard YAML-based file formats are provided in the widely-adopted JSON Schema ²²⁴

format; the standard provides sufficient information to fully reproduce a model selection ²²⁵

problem, and the package enables reproduction with several calibration tools; and, we ²²⁶

utilize community standards where possible, by supporting the use of SBML and PEtab. ²²⁷

The model selection results are also covered by the standard, such that they can be ²²⁸

analyzed in a consistent manner, independent of the framework that produced them. ²²⁹

For example, the package provides several plotting methods for results generated with ²³⁰

any of the supported calibration tools. ²³¹

Results ²³²

PEtab Select enables model selection in existing workflows, each ²³³ with unique tool-specific features ²³⁴

To assess the interoperability of PEtab Select with different software suites, we tested ²³⁵

its functionality in four PEtab-compatible tools: BasiCO (built on COPASI), ²³⁶

Data2Dynamics, PEtab.jl, and pyPESTO. Each tool successfully passed the tests in the ²³⁷

test suite, confirming that they can parse and execute model selection tasks defined in ²³⁸

the PEtab Select standard. While the software tools have a broad spectrum of ²³⁹

overlapping features, there are a few distinctive characteristics. ²⁴⁰

BasiCO (COPASI) provides the possibility of custom evaluation functions in place ²⁴¹

of the standard information criteria. Moreover, its programmable interface enables ²⁴²

model-specific optimizer settings, so callbacks or post-processing steps can be ²⁴³

incorporated into the model selection workflow. This flexibility allows users to adjust ²⁴⁴

parameters on a per-model basis or to visualize results automatically after each ²⁴⁵

calibration step. ²⁴⁶

Data2Dynamics supports transferring parameter estimates from one calibrated ²⁴⁷

model to another, potentially reducing computation time when new models are ²⁴⁸

introduced. Additionally, users can define custom calibration routines to adjust the ²⁴⁹

workflow before, during, or after parameter fitting. For example, the number of ²⁵⁰

multi-starts in an optimizer can be dynamically set based on the size of the parameter ²⁵¹

space, or diagnostic plots can be automatically generated to assess calibration quality. ₂₅₂

PEtab.jl integrates with the Julia SciML ecosystem, tapping into highly efficient ₂₅₃
ODE solvers provided by `DifferentialEquations.jl` [29] and automatic ₂₅₄
differentiation routines [30]. These capabilities enable rapid prototyping of novel ₂₅₅
approaches and runtime-efficient parameter estimation [24]. ₂₅₆

pyPESTO supports ensemble-based approaches, for instance, using ₂₅₇
Akaike-weighted ensembles to combine the results from multiple candidate models. Its ₂₅₈
ready-to-use post-processing tools also facilitate structured output of calibration results ₂₅₉
and automated generation of diagnostic figures, streamlining the analysis of potentially ₂₆₀
large model spaces. ₂₆₁

PEtab Select enables reproducible model selection across workflows

To assess the comparability of results across workflows, we consider an exemplary model ₂₆₄
selection problem from the work of Blasi et al. (2016) [13] that studied the acetylation ₂₆₅
of the histone H4 protein. It features a superset model where dynamics are governed by ₂₆₆
a reaction network with 16 state variables and 32 motif-specific reactions (Fig. 3a). ₂₆₇
Each reaction describes the conversion of one biochemical species into another. The rate ₂₆₈
constant of each motif-specific reaction is either the shared basal parameter or a ₂₆₉
motif-specific parameter. The model selection problem is to determine which reactions ₂₇₀
are sufficiently explained by the shared basal parameter, and which reactions require a ₂₇₁
motif-specific parameter instead. This model selection problem differs from the original ₂₇₂
publication in that we omit the additional 11 "site-specific" models in the original ₂₇₃
publication, which add a negligible computational cost and are not amongst the best ₂₇₄
models. Our model selection problem of 32 plausible motif-specific parameters therefore ₂₇₅
involves a model space of $2^{32} \approx 4.3$ billion plausible models. ₂₇₆

To concisely specify the model space with PEtab Select, the reaction rate constant ₂₇₇
for each reaction is formulated as the product of the shared basal parameter and the ₂₇₈
motif-specific parameter. The model selection problem then becomes whether to ₂₇₉
estimate motif-specific parameters, or to remove them by fixing them to 1. The ₂₈₀
corresponding PEtab Select model space table is shown in Fig. 3b. Details of the ₂₈₁

(a) Published best model, taken from Blasi et al. (2016).

(b) PEtab Select model space table for the Blasi et al. (2016) model selection problem.

Model subspace metadata		Plausible parameter values		
model_subspace_id	model_subspace_petab_yaml	a_0ac_k05	a_0ac_k08	...
M	petab_problem.yaml	1;estimate	1;estimate	...

Fig 3. The Blasi et al. (2016) [13] model selection problem in PEtab Select.
(a) The reaction network for the published best model. The histone chemical species can undergo acetylation reactions at four different positions (5, 8, 12, and 16). Nodes are acetylation states (motifs) of the histone, and arrows are acetylation reactions. The model selection problem involves two different possibilities for the rate constant of each reaction; it is either: the shared basal rate constant (the value is fixed to 1), or an estimated motif-specific rate constant (the value is estimated). The model selection problem is to identify the reactions with motif-specific rate constants, and the published best model contains seven (solid arrows). (b) There are 32 reactions, and therefore 32 independent hypotheses for motif-specific rate constants. Only two parameterized hypotheses (`a_0ac_k05` and `a_0ac_k08`) are shown here for brevity, with the remaining 30 parameters represented by the ellipses. This two-row, 34-column table encodes the full model space of $\approx$ 4.3 billion models.

parameter estimation problem are specified by a single PEtab problem for the superset model (located at `petab_problem.yaml`), which is automatically customized by the package to represent the models that are visited during the search. The problem files and all technical details of the experiments in this section are provided in the Zenodo repository.

In the original publication, all $\approx$ 4.3 billion models were calibrated then compared, and they found that a model with 7 motif-specific parameters is the best (Fig. 3a and [13], Supplemental Information, Table S1).

We used the FAMoS algorithm [27] initialized with 100 unique initial models that were randomly sampled from the model space; i.e., we repeated the algorithm 100 times,

(a) An initial model.

(b) Model sizes across all 100 searches.

(c) Waterfall plot of the 100 search results.

Fig 4. Multi-start FAMoS searches solve the Blasi et al. (2016) model selection problem. (a) The initial model that was used to assess reproducibility with all calibration tools, visualized as in Fig. 3a. (b) The sizes of models before and after model selection. The published best model had seven motif-specific rate constants. (c) The criterion of the selected model from each of the 100 FAMoS searches.

starting at different points in the model space (different initial sets of parameters). These initial models had a greater number of motif-specific parameters (with mean ≈ 16) (Fig. 4b) compared to the 7 in the published best model (Fig. 3a).

This first experiment with 100 FAMoS searches is to determine whether PEtab Select can find the same published best model, and was conducted using only pyPESTO as the calibration tool. The best model across the 100 searches matched the published best model, and the FAMoS algorithm found it three times in the 100 repeats (Fig. 4c). In total, there were 83,125 ($\approx 0.00194\%$ of 2^{32}) model calibrations across all model starts. As the model starts were run independently without sharing results, some models were calibrated multiple times. However, PEtab Select supports user-provided calibration results, which means these duplicate calibrations can be avoided. The number of unique model calibrations was 58,858, which is $\approx 0.00137\%$ of the model

	Iteration													
	1	2	3	4	5	6	7	8	9	10	11	12	13	14
Local search method	→	→	←	←	←	←	←	←	←	←	←	←	→	⇌
Candidate models (#)	17	16	16	15	14	13	12	11	10	9	8	7	23	168
Criterion (ΔAICc)	•	•	•	•	•	•	•	•	•	•	•	•	•	•
New model selected	✔	✗	✔	✔	✔	✔	✔	✔	✔	✔	✔	✗	✗	✗
Selected parameters (#)	16	16	15	14	13	12	11	10	9	8	7	7	7	7
Change in selected parameters. θ_i: added. θ_i: removed. $\varnothing$: no change.														
BasiCO (COPASI)	θ_6	$\varnothing$	θ_{12}	θ_{26}	θ_{22}	θ_{20}	θ_9	θ_8	θ_{10}	θ_{25}	θ_{13}	$\varnothing$	$\varnothing$	$\varnothing$
Data2Dynamics	θ_6	$\varnothing$	θ_{12}	θ_{26}	θ_{22}	θ_{20}	θ_9	θ_8	θ_{10}	θ_{25}	θ_{13}	$\varnothing$	$\varnothing$	$\varnothing$
PEtab.jl	θ_6	$\varnothing$	θ_{26}	θ_9	θ_{22}	θ_{20}	θ_{12}	θ_8	θ_{10}	θ_{25}	θ_{13}	$\varnothing$	$\varnothing$	$\varnothing$
pyPESTO	θ_6	$\varnothing$	θ_{10}	θ_{22}	θ_9	θ_{20}	θ_{12}	θ_{26}	θ_8	θ_{25}	θ_{13}	$\varnothing$	$\varnothing$	$\varnothing$
Same model across tools	✔	✔	✗	✗	✗	✗	✗	✗	✔	✔	✔	✔	✔	✔

Fig 5. Reproducibility of model selection across calibration tools. Local search methods are the forward ($\rightarrow$), backward ($\leftarrow$), and lateral ($\rightleftharpoons$) methods. All calibration tools reproduced the same criterion value in each iteration, within 0.01 ΔAICc. The only difference between tools in each iteration is in the change in selected parameters. θ_i is the ith motif-specific parameter; see the Zenodo repository for details.

space. In total, the 83,125 model calibrations took 655.8 CPU hours. Extrapolating to the full model space, this saved $\frac{2^{32}}{83125} \cdot \frac{655.8}{24 \cdot 365} = 3868$ CPU years; hence, FAMoS rendered the standardized PEtab Select approach computationally feasible, meaning that tailoring the simulation and optimization routines to the problem, as was done in the original publication, is not necessary.

To assess reproducibility of model selection results generated with PEtab Select across all calibration tools, we chose one of the three searches that selected the best model (Fig. 3a) in the first experiment, then ran model selection with the initial model of the chosen search (Fig. 4a) with each calibration tool (Fig. 5). In the first experiment where only pyPESTO was used, the chosen search involved 339 model calibrations. The subsequent experiments with COPASI (BasiCO), Data2Dynamics and PEtab.jl reproduced the same sequence of local search methods and calibrated similar sets of 339 models. Importantly, the same best model (Fig. 3a) was found with each of the calibration tools.

Model selection for the considered problem is inherently challenging. The search space is vast and populated by many candidate models whose information criterion values differ only within numerical precision, so minute floating-point variations render the ranking effectively non-deterministic across machines. Indeed, classical forward and

backward selection mostly failed to arrive at the optimal solution. By contrast, the FAMoS algorithm [27] reproducibly converged on models with markedly better criterion scores. Although the reproduced single FAMoS search (with 339 model calibrations) takes slightly different trajectories through the model space on repeated executions within and between calibration tools (Fig. 5, calibration tool rows), each trajectory delivers the same overall improvement within simulator and optimizer tolerances (Fig. 5, row "Criterion (ΔAICc)"), with negligible differences (< 0.01) in criterion across calibration tools.

Discussion

We present PEtab Select for (1) the concise specification, and (2) the efficient, reproducible solution, of model selection problems, which we achieve with a new file format standard and software package. Currently, users can perform model selection with PEtab Select via COPASI (BasiCO), Data2Dynamics, PEtab.jl, and pyPESTO. We demonstrate the feasibility of this approach on a published model selection problem with $\approx 2^{32}$ models, by reproducing the result with each of these calibration tools.

There are several useful directions in which PEtab Select can be improved. Currently, PEtab Select only provides support for the SBML mathematical model format, as this is the only model format supported by PEtab. However, PEtab Select has no direct dependency on the model format. Hence, this is expected to improve with the next version of PEtab, which will support non-SBML model formats. Another improvement would be to implement calibration tool-specific features in the package directly, thereby making them available to all calibration tools. For example, the termination of a model selection iteration as soon as a better model is found. In this way, the PEtab Select design could provide opportunities to enable model selection features in multiple calibration frameworks, from single implementations. Additionally, thanks to the general API available via Python or the command-line, users can readily implement model selection for unsupported calibration tools, model formats other than SBML, and problem formats other than PEtab; however, dummy PEtab files are required. An example of this is provided in the documentation for the package.

In addition to the implementation aspects, several opportunities for the improvement

of model selection methodology were identified when working with the problem $\quad$ 352
published by Blasi et al. (2016) [13]. On one hand, the analysis revealed that $\quad$ 353
reproducibility could be boosted by developing tailored strategies for handling the case $\quad$ 354
that multiple models are equivalent in best criterion value (up to numerical noise). If $\quad$ 355
performing a backward search, one possibility is to branch the backward search into $\quad$ 356
multiple backward searches, one per equivalent model. On the other hand, a further $\quad$ 357
improvement of search algorithms would be beneficial, in particular for large model $\quad$ 358
spaces, e.g., an automatic tuning of metaheuristics in the FAMoS method across runs. $\quad$ 359
However, when drawing conclusions from model selection results, all plausible models $\quad$ 360
should be considered, to account for uncertainty in model structure. $\quad$ 361

In summary, PEtab Select establishes, for the first time, a unified standard and $\quad$ 362
reference implementation for large-scale, reproducible model selection. By decoupling $\quad$ 363
the description of a model selection task from the calibration engine that solves it, the $\quad$ 364
framework enables researchers to tackle search spaces of billions of candidates in $\quad$ 365
whichever environment—COPASI, Data2Dynamics, pyPESTO, PEtab.jl, or future $\quad$ 366
tools—best suits their workflows. This interoperability not only accelerates day-to-day $\quad$ 367
practice but also lowers the barrier for methodological innovation, allowing new $\quad$ 368
inference algorithms to be benchmarked immediately on realistic problems. We $\quad$ 369
therefore expect PEtab Select to become a cornerstone for transparent, comparable, and $\quad$ 370
scalable model selection across the life and physical sciences. $\quad$ 371

Availability, reproducibility and supporting information $\quad$ 372

Code, data, and specific package versions for reproducing the reported results is $\quad$ 373
available at Zenodo (`https://doi.org/10.5281/zenodo.17185040`). Code for the $\quad$ 374
PEtab Select package is maintained at GitHub $\quad$ 375
(`https://github.com/PEtab-dev/petab_select/`), and documentation is hosted at $\quad$ 376
ReadTheDocs (`https://petab-select.readthedocs.io/`). $\quad$ 377

Acknowledgments

The authors are grateful to the many people who have provided feedback and contributions to the standard, package, and other aspects of PEtab Select, including participants of the HARMONY and COMBINE conferences (`https://co.mbine.org`).

This work was supported by the TRA Life and Health (University of Bonn) as part of the Excellence Strategy of the federal and state governments, the Deutsche Forschungsgemeinschaft (DFG, German Research Foundation) under Germany's Excellence Strategy (project IDs 390685813 - EXC 2047 and 390873048 - EXC 2151) and through Metaflammation (project ID 432325352 – SFB 1454), the German Federal Ministry of Education and Research (BMBF) within the e:Med funding scheme (junior research alliance PeriNAA, grant no. 01ZX1916A), the Horizon Europe - ERC Consolidator Grant 2023 (grant agreement no. 101126146), the Federal Ministry of Education and Research (grant no. 031L0293C), and by the University of Bonn via the Schlegel professorship to JH. FTB was supported by LIBIS, and de.NBI, the German Network for Bioinformatics Infrastructure (W-de.NBI-016). MC and SP were supported by the Swedish Research Council (VR2017-05117 and VR2023-04319) and the Swedish Foundation for Strategic Research (FFL15-0238). The work of NN, JT, CK, and HB has been funded by the Deutsche Forschungsgemeinschaft (DFG, German Research Foundation) – Project-ID 499552394 – SFB 1597 Small Data.

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