Accurate prediction of protein stability changes from single mutations
using self-distillation and antisymmetric constraint strategies

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Abstract

Computational approaches for accurately predicting protein stability changes upon residue
mutations are crucial for protein engineering and design. Sequence-based methods are easier to
apply to large-scale proteins since they do not rely on high-quantity structures. However, existing
sequence-based approaches struggle to capture structural changes, resulting in lower
performance compared to structure-based methods. In this study, we propose DPStab, a
sequence-based deep learning solution that accurately predicts protein stability changes upon
single residue mutations. DPStab transfers a protein large language model as a core component
and incorporates a cross-attention mechanism to capture the contact changes around mutated
positions for $\Delta\Delta G$ and ΔT_m prediction. To address data imbalance and the antisymmetric nature of
mutation effects, DPStab employs a self-distillation inference strategy under the supervision of an
antisymmetric constraint. Benchmarking demonstrates that DPStab achieves state-of-the-art
performance in both $\Delta\Delta G$ and ΔT_m prediction. Practical evaluations confirm DPStab's capability in
accurately ranking protein stability on large-scale datasets and effectively identifying critical
structural contacts impacting stability. More experiments on extensive cDNA display proteolysis
data demonstrate the significant contributions of self-distillation and antisymmetric constraint
strategies.

Significance Statement

Single amino acid mutations significantly influence protein stability, thereby affecting biological
function and potential therapeutic uses. Accurately predicting how mutations affect protein
stability is fundamental to protein engineering and therapeutic design. However, current
sequence-based computational methods fail to capture the structural context changes around
mutated residues. To overcome this, we propose DPStab, a sequence-based deep learning
approach that combines a protein language model and a cross-attention mechanism with self-
distillation and antisymmetric strategies. DPStab effectively captures residue contact changes
and predicts stability changes without structural data. Sufficient experiments demonstrate that
DPStab significantly outperforms existing methods, providing a fast and practical tool for
enhancing protein engineering and biomedical research.

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32 **Main Text**

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34 **Introduction**

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Proteins exhibit a variety of functions in nature, including catalyzing chemical reactions, mediating
intercellular signaling, and facilitating transcriptional transport, with their stability serving as a
fundamental prerequisite for these processes (1, 2). Protein stability is highly correlated with its
sequence and structure, which is easily altered by residue mutations (3, 4). Introducing specific
residue mutations to enhance protein stability has become a widely used strategy, particularly in
industrial applications (5, 6). However, a brute-force mutation strategy is both time-consuming
and costly. Accurately predicting protein stability changes upon residue mutations can reveal
crucial insights into the relationships between protein sequence, structure, folding, and function,
serving as invaluable prior knowledge for guiding protein design (7).
Gibbs free energy (ΔG) is the difference between the folded and unfolded states, denoted as
$\Delta G = G_{folded} - G_{unfolded}$, and T_m represents the melting temperature of proteins, which are two
commonly used metrics to measure protein stability. Correspondingly, Gibbs free energy changes
($\Delta\Delta G$) and melting temperature changes (ΔT_m) reflect protein stability changes. These properties
are antisymmetric, which means $\Delta\Delta G_{x\rightarrow y} = -\Delta\Delta G_{y\rightarrow x}$ and $\Delta T_{m,x\rightarrow y} = -\Delta T_{m,y\rightarrow x}$. In this study, both
higher $\Delta\Delta G$ and ΔT_m denote the mutation more stable.

To accurately predict $\Delta\Delta G$ and ΔT_m, numerous predictors centered on the geometric potential energy of protein structures have been proposed, such as FoldX (8), EvoEF (9, 10), STRUM (11), and Korpm (12). These computational methods rely on protein structures, rendering them limited when high-quality experimental or predicted structures are not available. Additionally, machine learning methods, like DDGun (13, 14) and MutateEverything (15), have also been proposed for $\Delta\Delta G$ prediction from sequences. Notably, a few deep learning approaches (16, 17) integrate protein sequence and structure information to predict $\Delta\Delta G$ and ΔT_m, which achieve an improvement compared to other methods and provide new sights for incorporating sequence and structure information through deep learning. However, these methods require the native or predicted protein structures, which prevents them from performing end-to-end prediction directly from sequence. Meanwhile, the imbalance of protein stability data presents a significant challenge for existing methods, where the number of stabilizing mutations is considerably less than that of destabilizing mutations. This phenomenon can easily impact these approaches, leading to results with distinct preferences (18).

Protein large language models (pLLMs) (19–21), owing to their self-supervised training on vast amounts of unlabeled protein data, exhibit remarkable generalization capabilities and have achieved robust performance across numerous downstream tasks (2, 19). Recently, some efforts have attempted to use pLLMs to predict protein stability changes (22, 23). For instance, ThermoMPNN (23) extracts the learnable features from a structure-based pLLM, ProteinMPNN (24), and leverages transfer learning from the mega-scale data used in ProteinMPNN to the protein stability data. In contrast, PROSTATA (22) adopts a sequence-based pLLM, ESM2 (20), as the backbone and uses different regression heads to predict protein stability changes. However, most existing pLLMs and structure modeling methods take a single protein as input during their pre-training process, which makes it hard to distinguish the single mutation effects. Consequently, it is essential to capture the contact changes around the mutation sites, even though the structural backbone may not change significantly before or after the mutation. Additionally, distillation on existing LLMs shows great potential to further enhance the performance of LLMs for specific downstream tasks (25) and has made much progress in various areas (26), such as DeepSeek (27), providing new perspectives to transfer LLMs. Here, we propose DPStab, a protein sequence-based deep learning method for accurate protein stability change prediction. DPStab can capture residue features, infer contact maps, and incorporate neighbors around the mutated positions with the architecture of pLLM. Notably, we propose a self-distillation inference strategy and introduce an antisymmetric constraint to further improve its performance. Comprehensive benchmarks and analyses demonstrate DPStab to be the state-of-the-art method for both $\Delta\Delta G$ and ΔT_m prediction.

Results

DPStab consists of three modules (Figure 1a): (1) a sequential encoder transferred from ESM2 for extracting evolutionary information from sequence and conformational information from contact maps (Figure 1b). (2) a neighboring encoder that crosses the information between sequence and structure, with weighted attention to neighboring residues, which includes the long-range interaction (Figure 1c). (3) a feature transition module that incorporates the representations of the wild-type and mutated proteins, along with environmental factors (e.g., pH and temperature), to predict stability changes ($\Delta\Delta G$ or ΔT_m). Notably, temperature is used only for $\Delta\Delta G$ prediction (Figure 1d).

Additionally, at the inference stage, we propose a self-distillation strategy to enrich the training data (Figure 1e) and incorporate a constraint to align DPStab with the antisymmetric nature of mutations. Specifically, multiple DPStab models are first trained on the direct and symmetrical training data. These trained models act as teachers to produce pseudo-labels for test data, which will be fed back to generate better student models with the original training set and independent validation set. Meanwhile, a contrastive loss is applied to make DPStab produce opposite outputs

104   for direct and inverse mutations. Further details of each module can be found in the "Methods"
105   section.
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DPStab outperforms existing methods overall in $\Delta\Delta G$ and ΔT_m prediction. To evaluate the
overall performance of DPStab in $\Delta\Delta G$ prediction, we compare it against seven structure-based
(8, 13, 14, 16, 23, 28, 29) and three sequence-based (13–15, 22) approaches. To ensure a fair
comparison, we utilize a manually curated independent test dataset, S461 (12), containing
proteins sharing a low sequence identity with those in the training set. S461 is also used as a
benchmark set in previous studies (16, 17). Four regression metrics - Spearman correlation
coefficient (SCC), Pearson's correlation coefficient (PCC), root mean square error (RMSE) and
mean absolute error (MAE) - as well as three multi-class classification metrics: accuracy (ACC),
Matthews correlation coefficient (MCC) and Cohen's kappa score (κ) are used to evaluate the
performance of these methods. Higher SCC, PCC, ACC, MCC and κ values indicate superior
performance, whereas lower RMSE and MAE values correspond to smaller prediction errors (see
"Methods" for more details).
Table 1 presents the performance of various methods on the S461 dataset in these metrics.
DPStab outperforms all other approaches. It achieves a smaller error range, with an RMSE below
0.93 kcal/mol and an MAE below 0.68 kcal/mol, while the best performance of other methods
corresponds to an RMSE of 0.98 kcal/mol and an MAE of 0.72 kcal/mol, respectively (details can
be seen in Supplementary Table S1). In terms of rank correlations, the predictions of DPStab
exhibit greater consistency with experimental results. Compared to other methods, DPStab
improves from 0.83 to 0.86 in SCC and from 0.82 to 0.84 in PCC. In Figure 2a, we further
compare the absolute errors of individual mutations predicted by DPStab against several control
methods. The median of absolute errors of DPStab is significantly lower than other sequence-
based and structure-based approaches, where the corresponding P-values confirm the statistical
significance of these improvements.
In certain scenarios such as soluble protein design, classifying mutations rather than predicting
exact $\Delta\Delta G$ values is more practically useful (30–32). To establish a classification task, we
categorize mutations into three classes: destabilizing ($\Delta\Delta G$ < -0.5 kcal/mol), stabilizing ($\Delta\Delta G$ > -
0.5 kcal/mol) and neutral. DPStab achieves a significantly higher ACC than other methods (Table
1). Among the 922 mutations (comprising 461 direct and 461 inverse mutations), DPStab
correctly predicts the mutation classes for 684 cases (Figure 2b). Additionally, DPStab achieves
the highest MCC and κ (both > 0.61), whereas the second-best method, GeoDDG-3D, achieves
only 0.51 (Figure 2c), highlighting its superior performance in mutation classification.
Furthermore, we compare DPStab with GeoDTm-AF2 and GeoDTm-3D (16) on ΔT_m prediction.
Interestingly, DPStab achieves a comparable SCC to GeoDTm-AF2 and GeoDTm-3D while
significantly outperforming them in terms of PCC, RMSE and MAE (Table 2 and Supplementary
Table S2). For classification, we similarly categorized mutations into three groups: destabilizing
(ΔT_m < -2 ℃), stabilizing (ΔT_m > 2 ℃), and neutral. DPStab achieves an ACC of 0.56, surpassing
the 0.52 for GeoDTm-AF2 and 0.53 for GeoDTm-3D (Table 2). Moreover, the evaluation on
Cohen's kappa score and MCC confirms the better performance of DPStab relative to the two
GeoDTm models (Figure 2d). Overall, our data indicates that DPStab achieves a stronger or
comparable performance for both $\Delta\Delta G$ and ΔT_m prediction.
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DPStab provides accurate guidance on individual proteins. We further evaluate DPStab's
performance on individual proteins to investigate its capability for protein engineering. We
independently evaluate its performance on individual proteins. Accordingly, there are 388
mutations from 15 proteins used here; each protein has at least 6 mutations. DPStab exhibits
substantial improvements in SCC, PCC, and ACC, compared to GeoDDG-3D (Figure 3a).
Specifically, it achieves remarkable median improvements of 9.1% (0.88 versus 0.81) in SCC,
7.5% (0.86 versus 0.80) in PCC, and 19.4% (0.80 versus 0.67) in ACC. Regarding error ranges,
DPStab surpasses GeoDDG-3D across most proteins (Figure 3b). A similar conclusion can also
be obtained for ΔT_m prediction (Supplementary Figure S1). Collectively, these results highlight the

advantages of DPStab in $\Delta\Delta G$ and ΔT_m at protein-level, which provides strong guidance for
protein engineering.
We further investigate protein 2PTL-A, which is a clear sample of DPStab outperforming
GeoDDG-3D (Figure 3b). Figure 3c presents a head-to-head comparison of DPStab and
GeoDDG-3D for $\Delta\Delta G$ prediction on all known mutations of 2PTL-A, which indicate that DPStab
achieves higher R^2 correlation values with an improvement of 9% over GeoDDG-3D, as well as
SCC (increase 11%) and PCC (increase 5%). These demonstrate that DPStab can provide a
more reliable rank list for mutations of 2PTL-A. To explore the reason for the DPStab boost, we
analyze the representation similarities of these mutations from our model and ESM2 that are also
used in GeoDDG-3D. In the original ESM2 model, these mutations have high similarities and are
hard to distinguish for $\Delta\Delta G$ prediction, while in DPStab, the correlation between representation
similarities and $\Delta\Delta G$ is significantly improved (Figure 3d).
DPStab is not only able to identify positive mutations but also predict negative mutations. We
provide two specific mutations here. The first one is 2PTL-A (Figure 3e) and its mutation A34G
(Figure 3f), which is provided in the manually curated test dataset and leads to a decreased
stability (-2.1 kcal/mol). Notably, DPStab accurately predicts this mutation (-1.2 kcal/mol), while
GeoDDG-3D considers A34G a neutral mutation with a prediction of -0.3 kcal/mol. To investigate
the underlying reasons for their stability changes, we analyze the structural alterations induced by
this mutation via FoldX. Specifically, Glycine (Gly, G) lacks a C_β atom, which may decrease the
Solvent Accessible Surface Area (SASA) and backbone flexibility, leading to local structural
instability. Secondly, Gly has a smaller molecular volume compared to Alanine (Ala, A), resulting
in fewer interactions with surrounding residues. Consequently, it loses interactions with Y50 and
the hydrophobic residue F36, reducing hydrophobic interactions and further contributing to
structural destabilization (see Figure 3f).
Similarly, Figure 3g and Figure 3h illustrate another mutation H51A of protein 1O6X-A. In wild-
type protein, Histidine (His, H) at position 51 generates two hydrogen bonds with W40 and T49,
respectively. However, after the mutation H51A, the volume of the residue A51 reduces
significantly, which does not interact with E14 and K41, resulting in the area being hollow and
unstable. More importantly, due to the disappearance of the phenyl ring, the hydrogen bond
between A51 and T49 is lost, which is detrimental to structural stability. Consequently, the
mutation H51A will reduce protein stability ($\Delta\Delta G$ = -0.7 kcal/mol), and DPStab detects it
accurately with a prediction of -0.8 kcal/mol. In contrast, GeoDDG-3D considers this mutation
stable with a prediction of 0.6 kcal/mol. All evidence demonstrates that DPStab can effectively
predict protein stability changes upon single mutations.
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DPStab achieves high ranking accuracy in large-scale DMS data. We further test the
scalability of DPStab on deep mutational scanning (DMS) data (33) that has been used in
GeoDDG-3D. As DMS data is not equivalent to $\Delta\Delta G$, we use Kendall rank correlation coefficient
to measure the correlation between two ranks (34). In the self-distillation stage, we randomly
extract 10% (2000) mutations to enrich our data to avoid introducing much noise. DPStab
improves SCC and Kendall by 13% and 15%, respectively (Figure 4a). In terms of individual
proteins, this advantage is more pronounced. DPStab gets better predictions for most proteins,
improving median SCC (0.72 versus 0.64 in Figure 4b) and Kendall (0.53 versus 0.46 in Figure
4c) significantly on individual proteins. And the corresponding scatter plots in Figure 4b and 4c
demonstrate that DPStab outperforms GeoDDG-3D on most proteins, indicating that DPStab can
rank multiple associated mutations in a single protein in most cases.
Furthermore, for each protein, we measure the accuracy of top-k predicted mutations. Figure 4d
shows the results for k from 1 to 60. DPStab is maintained and does not diminish as k increases,
which represents that its predictions for top-ranked mutations are more reliable. On the other
hand, we statistically compare the true $\Delta\Delta G$ values corresponding to the top-k ratio of mutations
predicted by different methods, where higher $\Delta\Delta G$ values suggest that the methods are more
likely to accurately provide higher $\Delta\Delta G$ values, i.e., stabilizing mutations (32). DPStab continues
to excel across different ratios (Figure 4e), indicating that its top-ranked predictions generally

exhibit higher ground-truth $\Delta\Delta G$ values and therefore are more likely to correspond to stabilizing
mutations.
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Generalization of self-distillation inference and antisymmetric constraint in DPStab. The
self-distillation inference strategy can enhance training data diversity and further improve the
accuracy of existing trained models. After removing the inference stage, the performance will
reduce in all metrics (Figure 5a). Specifically, for $\Delta\Delta G$ prediction, both SCC and PCC reduce by
3%, and RMSE and MAE correspondingly increase by 6% and 4%. This phenomenon also exists
in ΔT_m (Figure 5b).
To investigate the role of self-distillation more thoughtfully, we collect more protein stability-
related data, which is generated by cDNA display proteolysis for fast measuring folding stability
(35). It infers ΔG of proteins and $\Delta\Delta G$ of mutations from sequencing counts with a Bayesian
model. To validate the accuracy of inferred $\Delta\Delta G$ values, we extract the overlapping mutations in
the inferred data and our training data. The correlation between them achieves 0.85 when
considering $\Delta\Delta G$ between -2 and 1 kcal/mol (Figure 5c). Consequently, we split all mutations into
six groups by protein length and randomly sample three proteins with 450 mutations in each
group (Supplementary Figure S2), resulting in six sampled independent test datasets
(Supplementary Table S3). Then, based on our trained teacher models, we first generate pseudo-
labels for these test datasets and re-train corresponding DPStab models, respectively. As shown
in Figure 5d, SCC and PCC values at the inference stage can be further improved in most cases,
which demonstrates the effectiveness of self-distillation in our model.
Additionally, as can be deduced from the definitional formula of $\Delta\Delta G_{wt\rightarrow mut} = \Delta G_{wt} - \Delta G_{mut}$, direct
and inverse mutations should produce exactly opposite $\Delta\Delta G$ values. Since DPStab does not
employ a fully symmetrical network architecture (i.e., GeoDDG-AF2 and GeoDDG-3D), it may not
produce inverse outputs for symmetric inputs (x_{wild}, x_{mut}) and (x_{mut}, x_{wild}). This limitation also
exists in other methods, such as PROSTATA, ThermoMPNN, and Mutate Everything, which need
to be addressed to make models more robust in practical cases. To mitigate this limitation, we
introduce a constraint loss to guide our model in learning this antisymmetric property. The
absolute value of the sum of predicted results for direct and inverse mutations is used here as an
error evaluation metric $\langle\delta\rangle$. It can be observed that after introducing the antisymmetric constraint,
DPStab exhibits a significant reduction in error and is nearly capable of predicting perfectly
opposite $\Delta\Delta G$ values for direct and inverse mutations, making it more valuable for practical
applications (Figure 5e). Above all, the self-distillation strategy can improve the robustness of our
model, and the antisymmetric constraint makes the predictions more practical.
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246 **Discussion**
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Effective and efficient predicting protein stability changes ($\Delta\Delta G$ and ΔT_m) of mutations is crucial
for protein design and protein engineering. Sequence-based predictors are more easily applicable
to large-scale datasets compared to structure-based approaches. However, existing sequence-
based methods fail to capture structural contact changes, resulting in inferior performance to
structure-based methods. In this study, we develop a sequence-based deep learning method for
predicting protein stability changes from single residue mutations, called DPStab. It leverages a
pLLM to encode residue representations and predict residue contacts. Subsequently, a cross-
attention mechanism is introduced to capture the contact changes around the mutated positions.
Comprehensive and rigorous analyses highlight the significant improvements achieved by
DPStab. Notably, DPStab not only demonstrates strong overall performance, but also shows its
advantages on individual protein level, which is more efficient in practical cases.
Although fine-tuning pLLMs for predicting protein stability changes has already been explored in
previous studies (22, 23), these models still face the limitations of $\Delta\Delta G$ training data, which is very
unbalanced. This can lead to decreased performance of these models when predicting the
independent test set with different data distributions (32). Consequently, we adopt a self-
distillation strategy at inference stage to further improve the generalization of models. This

strategy can generate more data and enrich data distributions, which further improves the
performance of existing models. On the other hand, traditional asymmetrical frameworks cannot
generate inverse outputs for symmetric inputs, except when the wild-type and mutated proteins
share the whole network. However, completely sharing model weights between wild-type and
mutated proteins may make it difficult to learn the difference between these two proteins. To
solve these limitations, we introduce a simple antisymmetric constraint to guide our model to
learn antisymmetric data. Comprehensive ablation studies suggest that the self-distillation
strategy substantially enhances the performance of DPStab, offering new perspectives into
further improving existing protein large language models (pLLMs) for specific downstream tasks.
And contrastive loss can also enable an asymmetric network architecture to better learn the
constraints of antisymmetric data.
Overall, DPStab only takes protein sequences as input and does not rely on high-quality
structural data. It can predict residue contact changes and potentially capture the key residues or
regions involved in important interactions that maintain protein stability, such as $\pi - \pi$ interactions
and hydrogen bonds. In the future, we will consider side-chain changes and introduce more
geometric potential to help models capture structure changes during mutations. Additionally, in
practical protein engineering, optimizing a protein for specific applications often requires multiple
mutations. Consequently, how to design an effective framework to predict stability changes upon
multiple residue mutations is another challenge to be addressed.
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285   **Materials and Methods**
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Datasets. The $\Delta\Delta G$ and ΔT_m training dataset used in this article is derived from the previous
study (16), named S8754 and S4346, respectively, which are collected from the ProThermDB
(36) and ThermoMutDB (37) databases. S8754 consists of 8754 single-point mutations across
301 proteins, along with environmental factors (pH and temperature) and $\Delta\Delta G$ values. S4346
includes 358 proteins with 4346 single residue mutations, along with pH factors and ΔT_m values.
We randomly select 10% of the training data to serve as a validation set to assess whether the
model training is sufficient. Additionally, we use an independent dataset to test the performance
of models in $\Delta\Delta G$ prediction, named S461. This dataset maintains <25% sequence identity with
the proteins in S8754 and each mutation has been manually corrected. Finally, there are 461
single mutations of 48 proteins used in our test dataset. For ΔT_m prediction, we use S571 as test
data. It includes 39 proteins with 571 single mutations, which are all controlled by 25% sequence
identities to the S4346.
Due to the antisymmetric nature of mutations, where $\Delta\Delta G_{wild\rightarrow mut} = -\Delta\Delta G_{mut\rightarrow wild}$, it is necessary
to measure the prediction results of models in antisymmetric consistency. Consequently, we
generate corresponding inverse mutation data ('mutation'→'wild type') from the direct mutation
data ('wild type'→'mutation'), resulting in a maximum of 17235 samples available for training and
922 samples for test. Similarly, there are 8692 samples for ΔT_m training and 1142 samples for
test.
Moreover, we also collect an inferred $\Delta\Delta G$ dataset generated by cDNA display proteolysis (35),
consisting of 389068 single residue mutations across 412 proteins. Based on the length of the
wild-type protein sequences, we randomly select three proteins within each length interval of 7
residues, and further randomly selected 150 mutations per protein to construct the test set.
Totally, there are 6 generated test sets, each containing approximately 450 mutations.
Additionally, to compare DPStab with GeoDDG-3D fairly, another sampled DMS dataset is used,
including 20000 mutations from 73 proteins, where all these proteins have native structures (16).
312
Architecture of sequential encoder. To learn evolutionary and conformational information of
protein sequence, DPStab adopts the same sequential encoder as ESM2 and utilizes the pre-
trained weights of ESM2 as its initial parameters, including one token embedding layer, 33
stacked transformer layers, and one linear regression layer for contact map prediction.
Specifically, the input is a wild type or mutated protein sequence $p = \{r_1, r_2, \ldots, r_L\}$ with L residues,

where $r_i \in \{A, B, \ldots, Y, Z\}$ are the different residue types. It is first fed into a token embedding
layer:

$$Tokens_p = \{\langle CLS \rangle, r_1, r_2, \ldots, r_L, \langle EOS \rangle\} \#(1)$$

$$R_p = \text{Embedding}(Tokens_p) \in \mathbb{R}^{(L+2)\times d} \#(2)$$

320 where $Tokens_p$ is the tokens that represent the protein sequence p, $\langle CLS \rangle$ and $\langle EOS \rangle$ are two
321 additional signs indicating the beginning and end of protein sequences. Then, a trainable
322 embedding matrix is used to generate corresponding representations for each token, denoted as
323 R_p, which is fed into later transformer layers:

$$H_{l+1} = \text{MLP}(\text{SelfAttention}(H_l) + H_l)\#(3)$$

where $H_l \in \mathbb{R}^{(L+2)\times d}$ is the input of $(l+1) - th$ transformer layer $(l = 0, \ldots, n-1)$, and $H_0 = R_p$
initially. $\text{SelfAttention}(\cdot)$ is traditional attention mechanism that generates (Q, K, V) items,
calculates attention scores between different tokens and updates their representations. $\text{MLP}(\cdot)$ is
composed of several linear layers and corresponding activate functions. Through transformer
layers, different attention maps can be obtained from different heads, which are concatenated to
predict contact probabilities between residues:

$$CM = \text{Sigmoid}(\text{Concat}(a_{1,1}, \ldots, a_{i,j}, \ldots, a_{n,h}) \times W_{lr} + b_{lr})\#(4)$$

$$\text{Sigmoid}(x) = \frac{1}{1+e^{-x}}\#(5)$$

330 where $\alpha_{i,j}$ is the attention map from $j - th$ attention heads in $i - th$ transformer layer, $(W_{lr} \in$
331 $\mathbb{R}^{n \times h, 1}, b_{lr} \in \mathbb{R}^1$ is a linear layer, and n, h represent the number of transformer layers and attention
332 heads of each layer, respectively.
333
Architecture of neighboring encoder. Through sequential encoder, DPStab generates the
residue representations H_n and corresponding contact map CM from the target protein sequence
p. Based on these features, DPStab introduces a cross-attention module to extract the
neighboring information of mutated site m $(1 \leq m \leq L)$. Specifically, in the contact map CM, the
top-k neighboring residues with the highest concat probabilities with the mutation site m are
selected:

$$neighbors(m) = \text{topk}(CM[m, :]).index\#(6)$$

340 Subsequently, the representations of these k neighbors (denoted as $H_n[neighbors(m), :] \in \mathbb{R}^{k \times d}$),
341 along with the mutation site $(H_n[m, :] \in \mathbb{R}^{1 \times d})$, are then extracted and used as inputs for the
342 cross-attention module to integrate the neighboring information:

$$\begin{cases} Q = H_n[neighbors(m), :] \times W_Q \\ K = H_n[m, :] \times W_K \qquad\qquad \#(7) \\ V = H_n[neighbors(m), :] \times W_V \end{cases}$$

$$X_{temp} = \text{Softmax}\left(\frac{Q \times K^T}{\sqrt{d}}\right)^T \times V + H_n[neighbors(m), :]\#(8)$$

$$X_{output} = \text{MLP}(X_{temp}) + X_{temp}\#(9)$$

$$X_{neighbors} = \sum_{i=1}^{k} X_{output}[i, :]\#(10)$$

343 where $(Q \in \mathbb{R}^{k \times d}, V \in \mathbb{R}^{k \times d})$ is linearly transferred from the k neighbors and $V \in \mathbb{R}^{1 \times d}$ is from the
344 mutated site. Through this cross-attention mechanism, DPStab can learn the importance of
345 neighbors and integrate their representations adaptively, denoted as $X_{neighbors} \in \mathbb{R}^{1 \times d}$.
346 Additionally, residual operation and $\text{LayerNorm}(\cdot)$ are also employed here to prevent the loss of
347 features.
348
Architecture of feature transition module. Finally, by two previous encoders, DPStab
generates the features of the target protein, mutated site, and corresponding neighbors, denoted
as $H_n[0, :] \in \mathbb{R}^{1 \times d}$ ($\langle CLS \rangle$ token), $H_n[m, :] \in \mathbb{R}^{1 \times d}$, and $X_{neighbors} \in \mathbb{R}^{1 \times d}$, respectively. Hence, the
features of wild-type protein $(H_n^{wild}[0, :], H_n^{wild}[m, :], X_{neighbors}^{wild})$ and mutated protein

$(H_n^{mut}[0,:], H_n^{mut}[m,:], X_{neighbors}^{mut})$ can be obtained separately. Based on these paired features, a
simple feature transition module is applied to learn the difference between the two proteins:

$$X_{wild} = \text{Concat}\left(H_n^{wild}[0,:] \odot W_{wild}, H_n^{wild}[m,:] \odot W_{wild}, X_{neighbors}^{wild} \odot W_{wild}\right) \#(11)$$

$$X_{mut} = \text{Concat}\left(H_n^{mut}[0,:] \odot W_{mut}, H_n^{mut}[m,:] \odot W_{mut}, X_{neighbors}^{mut} \odot W_{mut}\right) \#(12)$$

$$X_{diff} = \text{MLP}(X_{wild} - X_{mut}) \#(13)$$

355 where $W_{wild} \in \mathbb{R}^{1 \times d}$ and $W_{mut} \in \mathbb{R}^{1 \times d}$ are two learnable parameters. After obtaining the difference
356 between wild-type and mutated proteins, environmental parameters are combined to predict ΔG
357 changes ($\Delta\Delta G$) upon single-point mutation:

$$X_{env} = \text{MLP}([ph, temperature]) \#(14)$$

$$\Delta\Delta G_{pred} = \text{MLP}\left(\text{Concat}\left(X_{diff}, X_{env}\right)\right) \#(15)$$

358
Self-distillation strategy and model training. As shown in Figure 1e, the whole process of
DPStab can be divided into two stages, including training and inference. Specifically, the first
stage generates two different trained DPStab models, based on the direct mutations and
symmetrical mutations. To effectively learn the naturally imbalanced distribution dominated by
destabilizing mutations, the first DPStab model is trained on direct training data and optimized
using mean squared error (MSE) loss function:

$$MSELoss = \frac{1}{N}\left(\sum_{i=1}^{N} y_{pred}^i - y_{true}^i\right)^2 \#(16)$$

365 where N is the number of training samples and (y_{pred}^i, y_{true}^i) are the predicted and true $\Delta\Delta G$
366 values, respectively. Then, we train another DPStab model on symmetrical data with MSE loss
367 and an additional antisymmetric constraint:

$$AtSymmConstraint = \sum_{i=1}^{N} \left| y_{pred}^{i,wild \to mut} + y_{pred}^{i,mut \to wild} \right| \#(17)$$

$$Loss = MSELoss + AtSymmConstraint \#(18)$$

where $y_{pred}^{i,wild \to mut}$ is the predicted result of $i-th$ training sample from wild-type protein to mutated
protein, and $y_{pred}^{i,mut \to wild}$ corresponds to the predicted result for the inverse mutation. This loss
function ensures that the model's predictions are consistent with the constraint as much as
possible. Based on these two teacher models, at the inference stage, we first average their
predicted results for test data as pseudo-labels. After incorporating training data and test data
with pseudo-labels, a single dependent DPStab is trained to produce the final predictions. In the
entire training and inference process, the hidden dimension size is set to 1280, AdamW optimizer
is used to optimize models with dynamic decaying learning rates, and the weights of transformer
layers from ESM2 are fixed in the first two epochs. DPStab will stop training if the loss value of
validation data is stable or trending upwards.
All experiments of DPStab are carried out using one NVIDIA Tesla H100 GPU card with 96 GB of
memory. The training process takes around 15 hours with a batch size of 4.
380
381 **Evaluation metrics.** In this study, seven metrics are used to evaluate the performance of models
382 in regression and classification, including Spearman correlation coefficient (SCC), Pearson's
383 correlation coefficient (PCC), root mean square error (RMSE), and mean absolute error (MAE),
384 accuracy (ACC), Matthews correlation coefficient (MCC) and Cohen's kappa score. Specifically,
385 given predicted results Y_{pred} and true labels Y_{true}, SCC is defined as:

$$SCC\left(Y_{pred}, Y_{true}\right) = \frac{Cov\left[Rank\left(Y_{pred}\right), Rank(Y_{true})\right]}{\sigma_{Y_{pred}} \sigma_{Y_{true}}} \#(19)$$

386 where $Rank(\cdot)$ is the rank positions of elements in the sorted order of the original list. Cov
387 denotes the covariance between two lists, and σ is the standard deviation. PCC is similar to SCC
388 but directly calculates the correlation between the original lists:

$$PCC(Y_{pred}, Y_{true}) = \frac{Cov[Y_{pred}, Y_{true}]}{\sigma_{Y_{pred}} \sigma_{Y_{true}}} \#(20)$$

389 where lager SCC and PCC indicate better predictions. RMSE and MAE reflect the error distances
390 between predictions and labels:

$$RMSE(Y_{pred}, Y_{true}) = \sqrt{\frac{1}{N}\left(\sum_{i=1}^{N} y_{pred}^i - y_{true}^i\right)^2} \#(21)$$

$$MAE(Y_{pred}, Y_{true}) = \frac{1}{N}\sum_{i=1}^{N}|y_{pred}^i - y_{true}^i| \#(22)$$

391 Both smaller RMSE and MAE represent better performance. Additional three metrics, ACC, MCC,
392 and Cohen's kappa score (κ) evaluate the multi-class classification abilities of models:

$$ACC = \sum_{c \in C} \frac{tp_c}{N} \#(23)$$

$$MCC = \frac{\sum_c tp_c \times N - \sum_c p_c \times n_c}{\sqrt{(N^2 - \sum_c p_c^2)(N^2 - \sum_c n_c^2)}} \#(24)$$

$$\kappa = 1 - \frac{1 - \sum_c tp_c}{1 - \sum_c p_c \times n_c} \#(25)$$

393 where tp_c denotes the number of true positives for category c, and N represents the number of
394 samples. p_c and n_c represent the number of samples predicted as class c and the number of
395 samples belonging to class c, respectively. Both higher ACC, MCC, and κ values show better
396 performance in multi-class classification.
397
398 **Data and Software Availability.** The data and source code can be downloaded from
399 https://github.com/CSUBioGroup/DPStab.
400
401
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403

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493

      Figures and Tables
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Figure 1. Model architecture of DPStab. **a.** The overview of DPStab. It consists of three modules.
The wild-type protein sequence and mutated protein sequence are fed into the first two modules,
respectively, to generate the features of the whole protein, mutated position, and its neighboring
information. Subsequently, the features of wild-type and mutated proteins are combined in a
feature transition module, with environmental parameters (pH and temperature), to predict the
difference of stability (ΔG or ΔT_m) between two proteins. **b.** The architecture of the sequential
encoder module. **c.** The architecture of the neighboring encoder module. **d.** The details of the
feature transition module. **e.** The details of self-distillation for different test datasets.
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Figure 2. Performance comparison of DPStab. **a.** The violin plot of DPStab and other
representative methods in terms of absolute error. The median values are denoted by the red
lines. The first and third quartiles are indicated by the bounds of the box. The whiskers represent
the 0.8 inter quartile range (IQR). Two-side paired t-tests are conducted between DPStab and
other methods, and the P-values are annotated at the top of the violins. **b.** The detailed
predictions of DPStab. The mutations are divided into three categories with different
thresholds. **c.** The performance of DPStab and other representative methods in terms of MCC
and κ score for   prediction. **d.** The performance of DPStab and other representative methods
in terms of MCC and *κ* score for   prediction.
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Figure 3. Performance comparison and analysis at protein-level. **a.** The performance comparison of DPStab and other methods on 15 individual proteins in terms of SCC, PCC and ACC. **b.** The performance comparison of DPStab and other methods on 15 individual proteins in terms of RMSE and MAE, where each point represents a protein, and the point size indicates the number of mutations. **c.** Comparison of detailed predictions of 2PTL-A by DPStab and other methods in terms of correlation. **d.** The correlation between representation similarity and experimental in original ESM2 and DPStab, where the similarity is calculated by single mutations and wild-type protein 2PTL-A. **e.** Local structure of 2PTL-A near the mutation site Ala34, where the residues with annotations are contacted with the wild-type residue A34. **f.** Local structure of 2PTL-A mutation (A34G) near the mutation site Gly34, where the residues with annotations are contacted with the mutated residue G34. **g.** Local structure of 1O6X-A near the mutation site H51, where the yellow lines indicate the hydrogen bonds, and the residues with annotations are associated with changes before and after the mutation H51A. **h.** Local structure of 2PTL-A mutation (A34V) near the mutation site Val34, where the yellow lines indicate the hydrogen bonds, and the residues with annotations are associated with changes before and after the mutation H51A.

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Figure 4. Benchmarking on large-scale DMS data. **a.** The overall performance comparison on
20000 inferred mutations of DPStab and other tools. **b.** The performance comparison on 73
individual proteins of DPStab and other methods in terms of SCC, where each point in the box
plot or scatter plot represents one protein with corresponding several mutations. **c.** The
performance comparison on 73 individual proteins of DPStab and other methods in terms of
Kendall rank correlation coefficient, where each point in the box plot or scatter plot represents
one protein with corresponding several mutations. **d.** The accuracy of top-k predicted mutations
on 73 individual proteins, where the point indicates the mean accuracy across these proteins and
error bars correspond to its standard deviation (std). **e.** The box plot of true   values
corresponding to the prediction results of top-k proportions, where higher   values represent
the predicted results more stabilizing.
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Figure 5. The role analysis of self-distillation strategies. **a.** The performance comparison of
DPStab and DPStab without self-distillation strategies (inference stage), in correlation coefficient
(left panel, including SCC and PCC), error ranges (right panel, RMSE and MAE) for
prediction. **b.** The performance comparison of DPStab and DPStab without self-distillation
strategies (inference stage), in correlation coefficient (left panel, including SCC and PCC), error
ranges (right panel, RMSE and MAE) for   prediction. **c.** The correlation between experiment
and inferred   from cDNA display proteolysis. **d.** The performance comparison of DPStab
and DPStab without self-distillation strategies (inference stage) on different test groups from
cDNA display proteolysis data. The left panel and right panel indicate SCC and PCC,
respectively. **e.** The antisymmetric error comparison for direct and inverse mutations.
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564 **Table 1.** Overall comparison of $\Delta\Delta G$ prediction on S461 in terms of SCC, PCC, RMSE, MAE, and
565 ACC.

Method	SCC	PCC	RMSE	MAE	ACC
Structure-based					
mCSM[a]	0.394	0.464	1.710	1.307	0.423
FoldX[a]	0.526	0.440	2.003	1.262	0.579
ThermoNet[a]	0.604	0.673	1.270	0.969	0.555
DDGun-3D[a]	0.722	0.755	1.138	0.826	0.629
ThermoMPNN	0.659	0.637	1.344	0.985	0.555
GeoDDG-AF2[b]	0.830	<u>0.824</u>	<u>0.984</u>	0.728	<u>0.662</u>
GeoDDG-3D[b]	<u>0.831</u>	0.805	1.008	<u>0.722</u>	0.672
Sequence-based					
PROSTATA	0.786	0.777	1.206	0.892	0.629
DDGun[a]	0.755	0.752	1.276	0.945	0.637
Mutate Everything	0.539	0.568	1.490	1.091	0.502
DPStab	**0.860**	**0.837**	**0.926**	**0.671**	**0.742**

566 [a] indicates that the raw results are taken from a prior benchmark. [b] refers that the raw results are
567 taken from its original paper.

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570 **Table 2.** Overall comparison of ΔT_m prediction on S571 in terms of SCC, PCC, RMSE, MAE, and
571 ACC.

Method	SCC	PCC	RMSE	MAE	ACC
GeoDTm-AF2[a]	0.536	0.518	8.112	5.546	0.522
GeoDTm-3D[a]	<u>0.547</u>	<u>0.535</u>	<u>8.034</u>	<u>5.308</u>	<u>0.525</u>
DPStab	**0.549**	**0.592**	**7.643**	**5.050**	**0.561**

572 [a] refers that the raw results are taken from its original paper.