Novel binning-based methods for model fitting and data splitting improved machine learning imbalanced data

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Abstract

Machine Learning (ML) models may perform inconsistently on individual classes on nominal outputs or ranges on continuous outputs, collectively referred to here as bins. Models should be assessed through metrics that consider each bin individually, called bin metrics. Inconsistent model performance is often due to model fitting with imbalanced data. Towards improving modelling of imbalanced data, novel model fitting methods are proposed including using bin metrics as loss functions and the use of Epoch sampling. Imbalanced data also poses a challenge for appropriate data splitting. Akin split is a novel method proposed that objectively yields the most appropriate data split(s).

Existing and novel model fitting methods were used to fit models, and the models were assessed by a bin metric in in two case studies. The first case study used synthetically generated datasets with different levels of noise and imbalance. On datasets with noise and greater levels of imbalance, Epoch sampling significantly improved the model performance by up to 23.6% while significantly using less resources (computation and time) by up to 57.7% compared to a standard

23   model fitting method. The second case study used protein-genome interactions data that are often

24   severely right-skewed. Akin split was used to split the data more appropriately than traditional

25   methods. Model fitting methods were tried on two model configurations. The effects of the

26   model fitting methods varied by the model configuration, but all models were significantly

27   improved by up to 57.7% compared to the standard model fitting.

1   Introduction

Machine learning (ML) models are used for their predictive abilities as well as their

learned concepts that ultimately guide and stimulate further exploration. Accordingly, ML

models can have large downstream ramifications. ML entails numerous steps, each with several

tunable parameters. To ensure an appropriate and effective ML model, it is imperative that each

step as well as their tunable parameters are thoughtfully attended to.

ML can be broken into 6 steps: data processing, data splitting, model design, model

fitting, model scoring, and model analysis (**Fig. 1**). Data processing involves processing the data

into observations which are pairs of inputs and outputs. The outputs can be nominal – which

have different classes – or continuous. A ML model processes an input and produces its own

output, known as a prediction. Data splitting entails dividing the observations into at least a

training and a testing set each serving different purposes. Additional sets may also be necessary

(see **Sup. Note 9.1.1)**. Model design involves choosing the ML algorithm and configuring its

tunable non-learnable parameters, known as hyperparameters. Model fitting entails exposing the

training set data to the model to adjust its learnable parameters. Model scoring involves using the

testing set which has not been exposed to the model to assess the model's ability to generalize to

unseen data. Model analysis entails extracting learned concepts which may require simplifying to

human-understandable forms.

Fig. 1. ML involves 6 steps.

Raw data is processed into observations in data processing which are then divided into training

and testing sets in data splitting. The training set is used to fit a model which is constructed in

model design. The fit model is scored using the testing set in model scoring. Predictions can be

made with the fit model and the learned concepts can be retrieved in model analysis.

Flowchart with grey rounded rectangles, yellow rectangles, green rectangles, and red rectangles

denoting data, steps, model, and ML products, respectively. Bolded yellow rectangles denote the

steps that this study focuses on.

This study focuses on and explores 3 steps of ML: model scoring, model fitting, and data

splitting. These steps are significantly challenged by imbalanced data: data where the numbers of

outputs belonging to each of the different classes for nominal outputs or ranges for continuous

outputs – collectively referred to here as bins – is inconsistent. This study improves the 3 steps

by handling the outputs as individual bins instead of an aggregate. Existing methods for model

scoring, model fitting, and data splitting are explored in **Sections 1.1**, **1.2**, **1.3**, respectively.

Novel methods for each step are also introduced in those sections and are described in more

detail in **Section 2**. Existing and novel model fitting and data splitting methods are experimented

in two cases studies. The first case study, **Section 3**, is on synthetically generated data. The

second case study, **Section 4**, is on genomics data, specifically protein-genome interactions.

Code for methods and case studies are provided at https://github.com/Husam94/BinMeths.

70 1.1 Introduction for model scoring methods

ML models are scored by metrics that consider the prediction errors which are the

differences between the predictions and their corresponding actual output. Most of the

commonly used metrics, such as the Mean Squared Error (MSE) and coefficient of determination

(also known as r^2) for regression tasks, consider the prediction errors of all predictions together.

These metrics do not assess the predictions of a model on individual bins. For continuous values,

the number of bins used is arbitrary and the bins are conventionally determined as having equal

ranges, referred to here as histogram bins. These metrics can yield identical scores on the

predictions for two models that score differently on individual bins, exemplified in **Fig. 2**. To

better assess the performance of a model, each bin should be scored individually.

Fig. 2. Models can perform similarly on non-bin metrics but perform differently on

different bins.

A) Predictions versus actuals of two simulated models with different types of prediction error

called "Additive" and "Square Root". Actual models can have predictions that resemble these

prediction errors or can be different.

B) MSE of each histogram bin of the two models, summarized by the mean (Mean Bin MSE)

and Root Mean Squared (RMS Bin MSE).

In some ML tasks, some values are more important than others. In other words, the

importance, often called relevance, of values is not uniform. For example, in fraud detection,

bins with extreme values have more importance than bins with values closer to the mean.

Weights are assigned to values based on their importance, referred to here as relevance weights,

and are used in metrics. For regression tasks, this is known as Utility-based regression and can

involve the binarization of continuous values (Torgo et al., 2013). For simplicity, in this study,

all bins are equally important.

It is preferred that a model performs well on all bins. It is also typically preferred that a

model performs consistently on all bins. The performances on the bins can be summarized as the

mean but this does not account for the consistency (i.e. variation). To summarize the

performances on the bins while accounting for variation for metrics where lower scores are

preferred, the Root Mean Squared (RMS) can be used. Extending the previous example, the

Mean Squared Error (MSE) of each bin, referred to here as the Bin MSE, is determined and

subsequently summarized by the mean (Mean Bin MSE) and the RMS (RMS Bin MSE) (**Fig. 2.**

B). While the Mean Bin MSEs are similar for the two models, the RMS Bin MSEs are different,

indicating that the "Additive" model has more consistent performance than the "Square Root"

model. Metrics that assess the performance on each bin and summarize them (e.g. RMS Bin

MSE) are referred to here as **bin metrics**. Assessing the performance on individual bins for

regression tasks has been done before (albeit rarely) (e.g. Steininger et al., 2021), but bin metrics

is rarely, if ever, done.

Inconsistent model performance on the bins is often due to model fitting with imbalanced

data. Imbalanced data consists of bins with proportionally more observations (i.e. over-

represented) and bins with proportionally less observations (i.e. under-represented). Generally,

over-represented observations have a greater influence on model fitting, resulting in models that

are better fit on over-represented observations than under under-represented observations.

The most prevalent example of imbalanced continuous data is *Tailed* data: data with

continuous outputs that are increasingly rarer away from the mean. Tailed data includes right-

skewed, left-skewed, and bell-shaped distributions, exemplified in **Fig. 3**. By simply predicting

the mean of Tailed data for all observations without fitting to the inputs, models can score

deceptively well on non-bin metrics. This is especially dangerous when these models are used

for predictions and/or learned concepts that drive later studies. Crucially, histogram binning of

Tailed data results in bins away from the mean with increasingly fewer values, often with too

few values for adequate model scoring and data splitting. Thus, different binning methods may

be necessary for Tailed data.

Fig. 3. Tailed data includes data with outputs that are right-skewed, left-skewed, and bell-

shaped.

For each set, 10,000 samples were drawn from truncated normal distributions with means of 0

and standard deviations of 1. Right-skewed, left-skewed, and bell-shaped distributions have

standard deviation bounds of [0, 3], [-3, 0], and [-3, 3], respectively. For each distribution, the

samples are binned into 10 histogram bins and the proportion of samples belonging to each bin

were determined.

1.1.1   Binning methods for Tailed data

Instead of using equal ranges for each bin for Tailed data, ranges that are progressively

larger away from the mean can be used to capture more values. The bin ranges can be

determined by first transforming the output values by a monotonic transformation that

compresses the values away from the mean towards the mean to produce a distribution that better

resembles a uniform distribution. Monotonic transformations, simply called transformations

hereafter, are functions that do not change the relative order of the values. Bin ranges in the

transformation scale are then determined by histogram bins. The transformation is then inversed

on the bin ranges, producing bin ranges in normal scale, referred to here as transformation bins.

This method of determining bins, referred to here as **transformation binning**, is rarely if ever

done.

The transformation bins for Tailed data can be determined by using log-based functions.

For right-skewed values, the log function $(\log(1 + x))$ is used. The right-skewed values are first

translated by their minimum $(x = x + \min(x))$ to avoid applying the log function to negative

numbers. For left-skewed data, the power function (x^q) can be used but the values can be treated

as right-skewed values by reflecting them $(x = -x)$. For bell-shaped distributions, the log-

modules function can be used (John & Draper, 1980). Before applying the log-modules function,

the values should be translated by their mean $(x = x - \bar{x})$ such that the mean is 0.

Importantly, inversing log-based functions to determine bin ranges involves the

exponential function (e^x), producing bin ranges that exponentially increase away from 0. This

can result in bins near 0 having too small of a range that capture too few values. Additionally,

this can result in too many bins spanning too small of a total range and too few bins spanning too

large of a total range, depending on user preferences. To produce bin ranges that are

progressively larger away from 0 but are not exponentially increasing, the tanh function can be

used (**Sup. Eq. 1**, **Sup. Eq. 2**).

There must also be consideration of scaling the values with a scale factor prior to

applying a transformation for transformation binning. Scale factors affect the distribution of

values in the transformed scale, thereby affecting the bin ranges and number of observations in

each bin. Based on user preferences, the minimum and/or maximum bin range proportion as well

as the minimum number of observations in a bin could be considered when determining the scale

factor. The scale factor can be objectively determined to best fulfil user preferences, referred to

here as **objective binning**, but this is rarely, if ever, done. Notably, even with transformation

binning, the number of observations in each bin can be inconsistent.

1.2   Introduction for model fitting methods

The following methods are only applied during model fitting and not model scoring and

can be used individually or in combination. The methods are categorized into three categories.

The first category is using the bin metric that assesses the model performance as the loss function

which are metrics used to guide model fitting. Using the same metric for model fitting and

scoring may guide model fitting towards better scoring. The other two categories of model fitting

methods are output weighting and data balancing.

1.2.1   Output weighting

176   Output weighting methods assign weights to output values to have different influences on

177   the loss function. To address imbalanced data, greater and lesser weights are assigned to under-

178   and over-represented values, respectively. There are two effective output weighting methods:

179   Density-based Weighting (DenseWeights) and reciprocal weighting, exemplified in **Fig. 4**.

Fig. 4. Different output weighting methods assign different weights.

Data for all examples is the Bell-shaped distribution from **Fig. 3**.

DenseWeights are determined with default parameters from Steininger et al., 2021.

DenseWeights assigns weights to continuous outputs based on the complement of a

Kernel Density Estimation (Steininger et al., 2021). DenseWeights was shown to perform well

on a variety of tasks compared to other state-of-the-art model fitting methods.

Reciprocal weighting determines weights of values as the reciprocal of the proportion of

values belonging to their respective bin (**Sup. Eq. 3**). Reciprocal weighting can be used for both

nominal and continuous outputs. Notably, the influence of a value on a bin metric is roughly the

reciprocal of the proportion of values belonging to its bin. Thus, using bin metrics as a loss

function is nearly equivalent to using non-bin metrics with reciprocal weighting. However, this is

not always true for Neural Networks (NNs). NNs are fit to the training data through batches

which are subsets that typically range from 32-1024 observations. The batches are generated by a

random partition of the training set. Using bin metrics as a loss function on batches is nearly

equivalent to using reciprocal weighting based on each batch. Output weights, however, are

determined based on all the training data used in the epoch.

1.2.2 Data balancing

Data balancing methods aim to reduce the imbalance of the number of observations in

each bin. Importantly, data balancing methods require each observation to belong to a single bin,

but observations may have outputs with multiple values thereby belonging to multiple bins. For

observations with multiple output values, the bins can be determined as a combination of bins.

For example, for observations with 2 output values and each value binned into 10 bins, there are

a total of (10*10) 100 combinations of bins. Alternatively, the bins can be determined by

clustering the observations by their multiple output values.

Data balancing methods either resample or create synthetic data. Resampling methods

either sample and/or oversample (i.e. replicate) observations belonging to over- and under-

represented bins, respectively. Synthetic data methods create artificial observations that belong

to under-represented bins based on the observations in a dataset through methods such as k-

nearest neighbors (Branco et al., 2017; Chawla et al., 2002). Oversampling and synthetic data

creation methods expand the dataset which requires more computing resources for storage and

may require more computing resources for modelling. Sampling, however, results in fewer

observations that may require fewer computing resources for modelling. This study only focuses

on sampling for data balancing.

Sampling can be done through weighted random sampling. Observations can be weighted

by methods mentioned in **Section 1.2.1**. Observations are randomly selected using their weights

without replacement until the desired number of total observations is obtained. As this method

relies on randomness, the number of sampled observations in each bin can vary considerably in

different samples especially with a low number of total observations.

Alternatively, the number of samples from each bin can be determined prior to applying

sampling methods. The number of observations in each bin can be that of the bin with the fewest

observations, but this may result in too few total observations to model effectively. Alternatively,

the number of observations in each bin can be based on the equal proportions. For example,

given 10,000 observations and 10 bins, each bin would have ($\frac{10,000}{10}$) 1,000 observations. Still,

under-represented bins are exhausted, resulting in fewer total observations than desired. A novel

method called **Harpoon sampling** (see **Section 2.1**) guarantees the desired number of total

observations while minimizing the variation of the number of observations in each bin,

exemplified in **Fig. 5**.

Fig. 5. Harpoon sampling produces the most balanced proportion of observations in each

bin compared to other sampling methods without replacement.

Data for all examples is the Bell-shaped distribution from **Fig. 3**.

Sampling with different techniques of random weighted sampling (weighted by DenseWeights,

reciprocal weighting), and Harpoon sampling. A sampling proportion of 0.3 is used for all

samples, resulting in 3,000 values. The proportions of samples belonging to each bin of each set

of values are determined.

After the desired number of observations in each bin are determined, observations can be

selected randomly or based on their inputs. The latter involves clustering observations by their

inputs through *k*-nearest neighbors (or similar) for each bin and samples from each cluster which

reduces the redundancy of the inputs of the observations (Bach et al., 2019; Beckmann et al.,

2015). This selection procedure requires additional considerations, computational resources, and

time. The following study only selects observations from each bin randomly.

Importantly, sampling methods, even those based on inputs, involve randomness whereby

different samples can have different observations. Model fitting with different data can

ultimately result in models with substantially different performances. Hence, model fitting with

sampling requires multiple samples as an additional level in model scoring. However, this costs

additional computational resources and time. NNs provide a unique opportunity to absolve the

need for multiple samples. NNs are fit to the training data in cycles, known as epochs. Instead of

sampling the training data before modelling, a novel method called **Epoch sampling** (see

Section 2.1) samples the training data at each epoch thereby introducing new samples at every

epoch.

As mentioned, model fitting methods can be used individually or in combination. When

using output weighting and sampling, output weights are determined after sampling. When using

Epoch Sampling, output weights are determined after sampling within each epoch.

1.3   **Introduction for data splitting methods**

The observations of a dataset should be divided such that each set contains observations

that are independent to the observations of another set and that the output values of the sets have

similar distributions (i.e. identically distributed). Non-independent observations that are spread

across different sets affect both model fitting and scoring which leads to improper model

evaluation, known as data leakage. Moreover, identical distributions are necessary to ensure that

the model is fit and scored on comparable data. Scoring models using data that has a different

distribution than the data used in model fitting is inappropriate. For example, fitting on Tailed

data without any additional model fitting method results in models that better predict values

closer to the mean. Scoring a model by only values close to the mean does not account for its

performance on values away from the mean and vice versa.

The most common method of data splitting is through random sampling, known as

Random split. Non-independent observations must be grouped prior to splitting to ensure they

are allocated to a single set.

Sequential data, such as genomics data, requires additional considerations for

independent data splits. Observations from sequential data are windows (i.e. a sub-sequence) of a

larger sequence (called the references sequence). Overlapping windows are non-independent and

thus must be grouped before splitting. Also, as neighboring windows are likely to be related, it is

suggested that neighboring observations also be confined to a single set.

For data with multiple reference sequences, overlapping and neighboring observations

can be confined to a single set by assigning entire reference sequence(s) to a single set. For

example, genomics data is typically based on a genome that contains multiple chromosomes. The

prevailing practice is to assign all observations belonging to a specific chromosome(s) to a single

set. Typically, the numbers of observations belonging to each reference sequence varies (i.e.

different reference sequences have different numbers of observations belonging to them).

Dividing observations such that each set contains a desired proportion of observations is difficult

to attain, if possible.

To ensure the desired proportion in each set while limiting data leakage of neighboring

interactions, splitting can be done by using larger non-overlapping windows, referred to here as

Window split. This method first sorts the observations by their location on the reference

sequence(s), groups non-independent observations, and uses larger non-overlapping windows

that are of sizes corresponding to the desired proportions of each set to split the observations. For

example, given 100 observations with no overlap that are sorted by their location, and a desired

proportion of observations of 0.7 and 0.3 for the training and testing sets, windows of size 70 and

30 are used, respectively. Different splits can be generated by sliding (i.e. translating) and/or

changing the order of the windows on the ordered list.

The methods mentioned thus far (Random and Window split) do not guarantee that the

sets are identically distributed. A common method for data splitting for identical distributions is

Stratified split which random samples observations based on bins, ensuring each bin is

proportionally distributed among the splits. However, Stratified split does not directly

accommodate outputs with multiple values, requiring each observation to belong to a single bin

which is similar to data balancing methods (see **Section 1.2.2**). More problematic still, Stratified

split does not accommodate for non-independent observations and is not possible for sequential

data when trying to confine neighboring windows.

Akin split is a novel objective data splitting method that produces a data split(s) that

contains sets that are independent, have the most identical output distributions, and have the

desired proportions (see **Section 2.3.1**). More specifically, data splits are generated through

Random or Window split and scored by the identicalness of the output values of its sets through

a novel method called the **Akin score** (see **Section 2.3**) which can directly handle multiple-

output values. The data split(s) with the best Akin score is selected. As Window split can be used

to generate splits, Akin split can be used to split sequential data, such as genomics data,

appropriately and effectively.

2   Novel methods

2.1   Harpoon sampling

Harpoon sampling is a sampling method that determines the number of samples per bin

by iteratively sampling each bin without replacement until a desired number (or proportion of the

original) samples is attained (**Fig. 6**). This method aims to capture all under-represented values

while sampling over-represented values to produce as balanced a distribution as possible without

replacement.

Input:
b: number of bins
$q[1..b]$: array of available samples per bin
n: total number of samples desired
326
327   **Output:**
328          $g[1..b]$: array of samples to draw from each bin
329
330   **Procedure:**
331   Initialize $g[1..b] \leftarrow$ array of zeroes
332   while n > 0:
333   for bin in Shuffle(1 to b):
334   if $q[bin] > 0$:
335                            $g[bin] \leftarrow g[bin] + 1$
336                            $q[bin] \leftarrow q[bin] - 1$
337                            $n \leftarrow n - 1$
338   If $n == 0$:

339	Break
340	return g
341	

Fig. 6. Algorithm of Harpoon sampling.

This algorithm describes the sampling logic used to balance bins while ensuring a fixed total sample size.

2.2   Epoch sampling

Epoch sampling performs sampling in each epoch during NN fitting. As different observations are used in each epoch, Epoch sampling absolves the need for modelling multiple samples as an additional level of model scoring, thereby saving resources and time. It is recommended that Harpoon sampling is the sampling method used in Epoch sampling.

2.3   Akin Score

The Akin Score assesses the similarity of the output distributions of a data split. It is essentially a summary of pairwise comparisons of the proportions of values belonging to each bin of each set. For example, given a data split with 3 sets $\{A, B, C\}$ there are 3 pairwise comparisons $\{(A, B), (A, C), (B, C)\}$.

The output of an observation can be a single value or be multiple values. Multi-value outputs can have dependencies with other output values. For example, values in a sequence are dependent on each other. Output values are grouped by dependency, referred to here as output groups. Values that have no dependencies form groups of 1. For observations with multiple output groups, each pairwise comparison of a set involves pairwise comparisons of each matching output group. For example, for observations with 2 output groups $\{H, J\}$ and 3 sets

$\{A, B, C\}$, the pairwise comparisons become

$\{(A_H, B_H), (A_J, B_J), (A_H, C_H), (A_J, C_J), (B_H, C_H), (B_J, C_J)\}.$

The distribution of each output group is represented as the proportion of values belonging

to each of their bins, referred to here as bin proportions. Notably, the sum of bin proportions is 1.

Bins with lower proportions can be given more influence in later operations by using the

reciprocal of the bin proportions but these values must be divided by the total sum to preserve

the sum as 1.

The similarity of two bin proportions is scored by the Minkowski distance, producing

scores where a lesser score indicates greater similarity. The Minkowski distance can be the

Manhattan Distance or the Euclidean Distance when the order of the norm is 1 and 2,

respectively. Since the sum of the bin proportions is 1, the minimum (0) and maximum of the

Minkowski Distance can be determined and be used in scaling the distance values, producing the

Scaled Minkowski Distance (SMD). Notably, the range of possible values of the SMD is [0,1].

The SMD is determined for each pairwise comparison, resulting in multiple values. The SMDs

are summarized into a single value by the RMS to account for the average and the variation of

the pairwise comparisons.

Notably, the Akin Score assesses the identicalness of the sets of a split regardless of the

number of output values, number of output groups, observation grouping, and the type of output

values (nominal or continuous).

2.3.1   Akin Split

Akin split selects a split(s) from a pool of splits that has the best (i.e. lowest) Akin Score

thereby selecting a split that has the most identical distributions of output values. The splits are

generated by Random or Window Split. Notably, generating and scoring splits is

computationally inexpensive and can be parallelized.

3 Case study: synthetic right-skewed data

Models fit on imbalanced data often results in inconsistent model performance. Existing

and novel model fitting methods are tried towards producing models with more consistent model

performance. The effects of these methods on model performance individually and in

combination are not known prior to modelling and may be dependent on the data that is modeled,

the metrics used for model scoring, and the ML algorithm used.

ML algorithms contain non-learnable tunable parameters, known as hyperparameters,

that must be set before modelling and that substantially influence model performance. The

different possible configurations of hyperparameters are a search space that must be searched for

optimizing model performance. Some ML algorithms, such as NNs, have many hyperparameters

resulting in a search space that may be too large to sufficiently search due to limitations in

computational resources and time. Moreover, the performance of the different configurations of

hyperparameters may depend on the model fitting methods used. Thus, hyperparameters and

model fitting methods may be codependent. The model fitting methods can be searched along

with the hyperparameters, but this further expands a search space that may already be too large

to adequately search.

To reduce the influence of the hyperparameters of a ML algorithm while determining the

effects of the model fitting methods, the following case study generates data and models the data

using the same configuration of a ML algorithm. The effects of the methods are explored on

datasets that vary by amounts of noise and right-skew. In theory, and from experiments that are

not included in this study, the effects of these methods on right-skewed data are similar to other

Tailed data.

3.1 Methods

413 See https://github.com/Husam94/BinMeths/C1-Synth/ for complete details.

3.1.1 Neural networks

416 Inspired by Steininger et al., 2021, a NN with 3 Dense layers each with 10 nodes and

417 ReLU activation functions between the Dense layers was used, referred to here as the Base NN.

418 Batch normalization layers were added between the Dense layers as they are found in most

419 current NN architectures.

3.1.2 Data generation

3.1.2.1 Initial data generation

A 10-feature input was generated by sampling uniform distributions with a range [-1, 1].

A total of 1,000,000 10-feature inputs were generated. A Base NN was randomly initialized by

Kaiming Initialization and produced corresponding outputs from the inputs. The pairs of input-

output are referred to as original data. This procedure was repeated 20 times, generating 20 sets

of original data from 20 different initializations of Base NNs, referred to as synthetic repeats.

The outputs of the synthetic repeats were visually inspected for bell-shaped distributions. Of the

synthetic repeats, 5 were chosen that best resemble bell-shaped distributions for the target and

control values.

3.1.2.2 Noise

434   The following applies to each of the synthetic repeats. Three noise levels were used: $g =$

435    $0, 0.5, 1.0$, corresponding to noise conditions N1, N2, N3, respectively. The noise is applied as

436   the product of three components: the noise level g, the standard deviation of the original outputs

437    $\sigma_{original}$, and samples from a truncated normal distribution. The resulting noisy output values

438   are defined by the following equation:

439
$$y_{noised} = y_{original} + \left(\sigma_{original} * g * \mathrm{TN}(0,1,2)\right)$$

where:

- $y_{original}$ are the original output values

- $\sigma_{original}$ is the standard deviation of the original output

- g is the noise level

- $\mathrm{TN}(0,1,2)$ represents a sample from a truncated normal distribution with mean 0,

standard deviation 1, and bounds of ± 2 standard deviations.

This application of noise ensures that noise is scaled appropriately and bounded to avoid extreme

perturbations. Notably, noise level N1 ($g = 0$) results in no added noise, preserving the original

output values. The different levels of noise are exemplified in exemplified in **Fig. 7**.

Fig. 7. Examples of levels of noise.

Different levels of noise were added ("Noised") to a random sample of 1,000 values of the

outputs of a synthetic repeat ("Original").

3.1.2.3 Right-skew selection

456   The following applies to each level of noise. Different *levels* of right-skewed data were

457   obtained through weighted random sampling. Observations were weighted by a two-part

458   weighting scheme based on the output values. The weighting function is defined as:

459
$$w = \frac{\text{BinProps}(y_{norm}, 1000)}{e^{r*y_{norm}}}$$

460   where:

461   - y_{norm} are the output values after adding noise, clipping, and min-max normalization

462   - $\text{BinProps}(y_{norm}, 1000)$ computes the proportion of samples in each of the 1000

463   histogram bins

464   - r controls the degree of right-skew with values r$r = 0,2,5,8$ corresponding to skew

465   levels R1 through R4

The exponential term $e^{r*y_{norm}}$ increases the weight decay for higher output values, thereby

inducing right-skew. When $r = 0$, the dataset remains balanced (R1). Each skewed dataset

contains 10,000 observations sampled according to these weights, exemplified in **Fig. 8**.

Fig. 8. Examples of levels of right-skew.

Histograms (50 bins) of the output values of the different levels of right-skews generated from

one synthetic repeat.

3.1.2.4 Binning and data splitting

For each dataset, the observations were binned into 10 transformation bins by scaling the

values by a scaling factor and using the tanh function. The scaling factor was objectively

determined as the scaling factor that yielded the lowest variation of the proportions of

observations belonging to each bin and having a maximum bin range less than 0.3x the total

range of output values. The scaling factors determined ranged from 0 to 1.8 depending on the

level of right-skew.

For each dataset, the data was split into training, stoppage (see **Supplementary Note**

9.1.1), and testing sets with proportions of 0.6, 0.2, 0.2, respectively, using Akin split with

Random split as the split generator. Each split is referred to here as a split repeat. Binning and

split information for different right-skew levels for the first synthetic repeat and noise level N1

are provided in **Sup. Table. 1 – Sup. Table. 4**. Datasets with different synthetic repeats, level of

noise, and split repeats have similar binning and splitting for each corresponding level of right-

skew.

3.1.2.5 Output weighting

Output weights were determined by the output values of the observations in the training

set. For experiments that combined output weighting and Epoch sampling, output weights were

determined within each epoch of the sampled training set after Epoch sampling. DenseWeights

were determined using the default parameters described in Steininger et al., 2021. Reciprocal

weights were determined as the reciprocal of the proportion of values in each of the bins.

3.1.3   Model scoring

The objective is consistent model performance within each bin and of all bins. For each

bin, the corresponding predictions are scored by the Root Mean Squared Error (RMSE). The

RMSEs of each bin (Bin RMSEs) are summarized by RMS, yielding the RMS Bin RMSE

(RBR). A lower RBR is preferred.

The learnable parameters of NNs are initialized randomly and are fit using stochastic

methods which can result in substantially varying model performances. Considering computing

budgets, each experimental unit was repeated 15 times, referred to as model repeats. For later

statistical assessment, different sets of model repeats were simulated by bootstrapping the

existing model repeats (Efron & Tibshirani, 1986). Based on computing budgets, 100 bootstrap

sets of model repeats were sampled for each set of model repeats.

Commonly, a single model out of a set of model repeats that best performs on the

stoppage set is used for further assessment. This selection criteria, however, lacks reproducibility

as a different set of model repeats can yield a substantially different best performing model.

Instead of using a single best performing model, the best 3 models were used. The predictions of

the best 3 models were averaged, akin to an average ensemble model, simply referred to as an

ensemble. The ensemble predictions were scored by the RBR, referred to as a bootstrap score.

Each experimental unit had 100 bootstrap scores as there were 100 bootstrap sets of model

repeats.

3.1.3.1 Comparisons of models

A subject experimental unit was compared to a corresponding reference experimental unit by the pairwise comparisons of their bootstrap scores, resulting in (100*100) 10,000 comparisons which simulates repeating the modelling of the two experimental units 10,000 times. Each pair of bootstrap scores were compared by percent relative change, referred to here as the pairwise bootstrap score. Negative pairwise bootstrap scores indicate the subject has a lower RBR than the reference which is preferred. For each level of noise, for each level of right-skew, the pairwise bootstrap scores of synthetic and split repeats were pooled, totaling (3*3*10,000) 90,000 pairwise bootstrap scores.

The mean and the standard error of the pooled pairwise bootstrap scores were determined for each dataset and for each experimental unit. For statistical assessment, the 5th (P_5) and the 95th (P_{95}) percentiles of the pairwise bootstrap scores were determined, simulating a one-sided statistical significance level of 0.05 and a two-sided statistical significance level of 0.1 (Efron & Tibshirani, 1986). If $0 > P_{95}$, percentile, the subject model is significantly better than the reference model. If $0 < P_5$ percentile, the subject model is significantly worse than the reference model. If $P_5 < 0 < P_{95}$, the subject model is not significantly different from the reference model.

3.1.4 Model fitting

All modelling used the Base NN, a batch size of 512, RBR as the stoppage metric, and a patience of 10. The choice of patience was informed by preliminary trials (not included here) which indicated that increasing patience did not yield significant performance improvements and this setting reduced computation resources. Also, all models used the Adam optimizer (Kingma & Ba, 2014), selected for its widespread adoption and proven effectiveness across a broad range

of NN applications. The Adam learning rate used for all experiments was determined as the

learning rate that best reduces the RBR given the standard model fitting method and a budget of

200 epochs (**Sup. Table. 5**).

The *standard* model fitting method uses RMSE as the loss function, no output weighting,

and no sampling. RMSE is chosen as the predictions at bin-level are assessed by RMSE but also

because it and the closely related MSE are among the most widely used loss functions for

regression tasks.

3.2   Results and discussion

549 The objective of this case study is to minimize the RMS Bin RMSE (RBR) on modelling

550 datasets with different levels of noise and right-skew. Towards minimizing the RBR, three

551 different categories of model fitting methods of bin metrics as the loss function, output

552 weighting, and data balancing were tried first individually and then in combination.

3.2.1   Model fitting with different loss functions

Compared to models fit with the standard method which used RMSE as the loss function,

models fit using RBR as the loss function performed significantly better on datasets with noise

(N2 and N3) and right-skew (R2, R3, R4) by up to 23.0% (**Table 1**). On datasets without noise

(N1) and those without right-skew (R1), models fit with either method performed similarly. The

models fit with RBR as the loss function were not significantly worse than those fit with the

standard method for any of the datasets. Using RBR as the loss function on any datasets yielded

models that performed as good if not better than those fit using the standard method. Notably,

since the RBR is used as the evaluating metric, it was expected that using RBR as the loss

function yields models that perform better on the RBR than using RMSE as the loss function.

Table 1. Models fit with RBR as the loss function performed better than those fit with

RMSE on datasets with greater levels of right-skew and noise.

Mean pairwise bootstrap scores comparing models fit with different loss functions ("Loss

Func.") to models fit with RMSE as the loss function.

The "Shuffled RMSE" refers to models fit with RMSE as the loss function but with the outputs

in the training and validation sets shuffled, serving as a negative control.

See **Sup. Table. 6** for full bootstrap statistics.

Negative values indicate that models fit using the subject configuration performed better than

models fit using the reference configuration. Bolded values indicate that the models fit using the

subject configuration are significantly better or worse than models fit using the reference

configuration.

"Noise ID" and "Right ID" refer to noise level and right-skew level of the dataset, respectively.

Dark to light color scale visualize values from -25 to 0.

Noise ID	N1				N2				N3			
Right ID	R1	R2	R3	R4	R1	R2	R3	R4	R1	R2	R3	R4
Loss Function												
RMSE	0.7	1.1	0.8	0.8	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
RBR	-1.5	12.5	27.7	20.4	0.3	**-5.0**	**-15.4**	**-15.2**	0.0	**-13.1**	**-23.0**	**-19.2**
Shuffled RMSE	**748.0**	**956.5**	**819.1**	**516.4**	**66.3**	**91.4**	**65.2**	**35.1**	**21.2**	**30.1**	**17.1**	**6.7**

579   ### 3.2.2 Model fitting with different output weighting methods

580   Compared to models fit with the standard method which does not use output weighting,

models fit with reciprocal weighting for output weighting performed similar to those fit with

RBR as the loss function (**Table 2**). They performed significantly better than those fit with the

standard method on datasets with noise and right-skew by up to 22.6% and were not significantly

worse for any of the datasets. Models fit with DenseWeights also performed significantly better

than those fit with the standard method on datasets with noise and right-skew by up to 17.5%.

However, models fit with DenseWeights were significantly worse than those fit with the standard

method on datasets with noise and without right-skew (R1) by up to 9.1%.

Table 2. Models fit with reciprocal weighting performed better than those fit without

output weighting on datasets with greater levels of right-skew and noise.

Mean pairwise bootstrap scores comparing models fit without output weighting ("None") or with

output weighting methods of DenseWeights ("DenseW") or reciprocal weighting ("Recip.") to

models fit without output weighting.

See **Sup. Table. 7** for full bootstrap statistics.

See **Table 1** for additional descriptions.

Noise ID	N1				N2				N3			
Right ID	**R1**	**R2**	**R3**	**R4**	**R1**	**R2**	**R3**	**R4**	**R1**	**R2**	**R3**	**R4**
Weighting												
None	0.7	1.1	0.8	0.8	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
DenseW	27.9	10.8	2.7	7.0	**9.1**	**-4.3**	-12.7	-12.7	**5.1**	-12.6	-17.5	-15.2
Recip.	-0.5	11.9	24.6	23.3	0.1	**-5.2**	-15.0	-14.2	0.0	-13.0	-22.6	-19.4

3.2.3 Model fitting with different sampling proportions

Sampling with different proportions – none (1.0), 0.8, 0.4, 0.2, 0.1, 0.05, 0.025, and 0.01

– was tried using Epoch sampling with Harpoon sampling (**Table 3**). These proportions follow a

roughly geometric progression, decreasing by approximately a factor of 2 at each step. This

design was chosen to systematically explore the effects of increasingly aggressive sampling on

model performance. Harpoon sampling is used instead of random or weighted random sampling

as it was previously shown to best yield the most balanced distributions (**Fig. 5**).

Compared to models fit with the standard method which does not use sampling, models

fit with a sampling proportion of 0.4 or less performed significantly better on datasets with noise

and greater right-skew (R3, R4), by up to 23.6%. Models fit with sampling proportions of 0.8

and 0.4 performed similarly to those fit with the standard method on datasets without noise.

Conversely, in general, using a sampling proportion of less than 0.4 yielded models that

performed significantly worse than the standard method on datasets without noise by up to

176.9%. On datasets with noise and right-skew, models fit with a sampling proportion of 0.1

performed the best on average.

Table 3. Models fit with sampling generally performed better than models fit without

sampling on datasets with noise and right-skew.

Mean pairwise bootstrap scores comparing models fit without sampling ("None") or with

different sampling proportions ("Samp. Prop.") ranging from 0.8 to 0.01 to models fit without

sampling.

See **Sup. Table. 8** for additional bootstrap statistics.

See **Table 1** for additional descriptions.

Noise ID	N1				N2				N3			
Right ID	R1	R2	R3	R4	R1	R2	R3	R4	R1	R2	R3	R4
Samp. Prop.												
None	0.7	1.1	0.8	0.8	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.8	6.8	6.7	1.4	6.4	0.2	-2.1	-4.8	**-4.8**	-0.2	**-5.8**	**-5.3**	**-6.1**
0.4	**23.2**	24.5	19.2	19.4	0.7	**-4.8**	-12.8	-11.8	0.0	-12.8	-16.6	-15.8
0.2	**38.8**	**45.1**	**34.0**	25.8	2.0	-4.5	-15.9	-15.2	0.1	-13.2	-21.5	-18.1
0.1	**69.6**	**72.4**	**53.7**	47.7	**3.1**	-3.4	-15.8	-15.5	0.5	-12.9	-23.6	-20.1
0.05	**113.1**	**111.0**	**98.1**	92.6	**5.3**	-1.0	-13.5	-12.8	1.2	-12.3	-22.9	-19.7
0.025	**135.6**	**142.7**	**121.0**	111.7	**7.7**	0.8	-11.7	-12.5	**1.8**	-11.4	-22.8	-19.8
0.01	**167.9**	**176.9**	**162.9**	138.8	**12.1**	4.5	-10.4	-10.6	**3.1**	-10.2	-22.5	-19.8

3.2.4 Model fitting with different combinations of methods

The most effective methods from each category (RBR as the loss function, reciprocal weighting for output weighting, and sampling with a proportion of 0.1) were tried in combination towards further improving model performance (**Table 4**). The methods applied in combination were similarly effective to the methods applied individually but their effects were chiefly dependent on the sampling proportion. Generally, compared to models fit with the standard method (RMSE as the loss function, without output weighting, and without sampling), the models fit with the different combinations of methods performed significantly better on datasets with noise and right-skew by up to 23.6%. On datasets without noise, all combinations with sampling yielded models that were significantly worse than those that were fit with the standard method by up to 72.4%.

Table 4. Models fit with combinations of model fitting methods generally performed similarly on datasets with noise and right-skew.

Mean pairwise bootstrap scores comparing models fit with combinations of RMSE or RBR as the loss function, without output weighting ("None") or with reciprocal weighting (Recip.), and without sampling ("1.0") or with a sampling proportion of 0.1 to models fit with RMSE as the loss function, without output weighting, and without sampling. The combinations are denoted as (loss function, output weighting, sampling proportion).

See **Sup. Table. 9** for additional statistics.

See **Table 1** for additional descriptions.

Noise ID	N1				N2				N3			
Right ID	R1	R2	R3	R4	R1	R2	R3	R4	R1	R2	R3	R4

Combination												
(RMSE, None, 1.0)	0.7	1.1	0.8	0.8	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
(RMSE, None, 0.1)	**69.6**	**72.4**	**53.7**	**47.7**	**3.1**	**-3.4**	-15.8	-15.5	0.5	-12.9	-23.6	-20.1
(RMSE, Recip., 1.0)	-0.5	11.9	24.6	23.3	0.1	**-5.2**	-15.0	-14.2	0.0	-13.0	-22.6	-19.4
(RMSE, Recip., 0.1)	**61.3**	**71.8**	**58.3**	**50.2**	**3.4**	**-3.0**	-15.1	-14.1	0.6	-13.0	-23.3	-19.9
(RBR, None, 1.0)	-1.5	12.5	27.7	20.4	0.3	**-5.0**	-15.4	-15.2	0.0	-13.1	-23.0	-19.2
(RBR, None, 0.1)	**67.5**	**69.8**	**53.2**	**44.9**	**3.4**	-3.1	-15.0	-14.0	0.6	-12.9	-23.4	-20.0
(RBR, Recip., 1.0)	0.6	15.8	26.1	14.2	0.2	**-4.9**	-15.9	-15.2	0.0	-13.0	-23.0	-19.5
(RBR, Recip., 0.1)	**64.3**	**66.0**	**55.5**	**47.8**	**3.2**	-3.4	-14.9	-14.0	0.5	-12.8	-23.5	-20.1

The methods with sampling may use less resources (computation and time) for NN model

fitting than those without. Sampling uses fewer observations of the training set in each epoch

thereby reducing the resources used per epoch. However, the effect of sampling to the total

number of epochs needed for model fitting is not clear. Notably, each epoch involves evaluating

the model by the stoppage set which is not sampled – it is the same regardless of sampling the

training set. Accounting for the proportion of sampling of the training set and the unsampled

stoppage set, the resources used by the different combinations of methods were compared to

those used by the standard method (**Table 5**). Model fitting with combinations of methods that

used a sampling proportion of 0.1 used significantly fewer resources than model fitting using the

standard method for all datasets except for datasets with noise and right-skew R2, by up to

57.7%. Conversely, model fitting with combinations of methods that did not use sampling used

similar (i.e. not statistically different) amounts of resources than model fitting with the standard

method.

Table 5. Models fit with sampling used substantially less resources than those fit without

sampling.

Mean *resource* pairwise bootstrap scores comparing models fit with combinations of RMSE or

RBR as the loss function, without output weighting ("None") or reciprocal weighting (Recip.),

and without sampling ("1.0") or sampling with a proportion of 0.1 to models fit with RMSE as

the loss function without output weighting and without sampling.

Resource pairwise bootstrap scores are the same as pairwise bootstrap scores except instead of

using RBR of the average predictions of a bootstrap ensemble, resources are calculated as the

sum of the epochs used by the bootstrap ensemble * (sampling prop. * training set prop. +

stoppage set prop.) / (training set prop + stoppage set proportion). Negative values indicate the

subject used less computational resources than the reference.

See **Sup. Table. 10** for additional bootstrap statistics.

See **Table 4** for additional descriptions.

	N1				N2				N3			
	R1	R2	R3	R4	R1	R2	R3	R4	R1	R2	R3	R4
Combination												
(RMSE, None, 1.0)	0.4	0.5	0.7	0.6	0.5	0.4	0.4	0.5	0.4	0.5	0.7	1.0
(RMSE, None, 0.1)	-49.6	-43.4	-42.0	-44.2	-32.6	-12.5	-33.4	-52.3	-26.0	-14.5	-45.7	-39.4
(RMSE, Recip., 1.0)	3.8	4.6	7.7	3.8	2.1	24.1	-8.8	-23.3	2.3	9.2	-23.7	-15.8
(RMSE, Recip., 0.1)	-46.0	-45.3	-41.7	-45.1	-33.0	-11.1	-37.3	-54.7	-24.9	-15.9	-46.8	-43.5
(RBR, None, 1.0)	2.7	2.8	0.9	1.4	-4.2	22.8	-4.8	-23.5	3.8	9.4	-20.1	-4.8
(RBR, None, 0.1)	-47.9	-43.3	-40.0	-41.6	-32.1	-11.0	-37.8	-56.5	-25.9	-14.1	-47.4	-44.4
(RBR, Recip., 1.0)	0.5	2.5	2.7	5.7	-2.6	**27.4**	-2.2	-18.2	2.6	10.3	-21.3	-7.6
(RBR, Recip., 0.1)	-48.1	-42.8	-40.1	-45.9	-32.7	-10.3	-36.5	-57.7	-23.9	-12.6	-47.4	-42.0

As explored, on datasets with noise and greater right-skew, methods with sampling

yielded similarly performing models than methods without sampling while using significantly

and substantially less resources. Most often, the configuration of hyperparameters of a model for

effective modelling is not known prior, requiring a hyperparameter search. While the

combinations of methods presented are recommended to be searched alongside the

hyperparameters, the hyperparameter search space is often already too large to adequately

search. For modelling Tailed datasets with noise, sampling can be used to fit models in

hyperparameter search to save computing resources while presumably producing models that

perform similarly to those that are fit without sampling. This is beneficial for modelling tasks

that have large models, large datasets, and/or limited computing resources. The savings in

resources can be used towards more hyperparameter search (i.e. trying more hyperparameter

configurations), potentially finding hyperparameter configurations that may ultimately yield even

better performing models. Therefore, sampling is recommended in a hyperparameter search on

datasets with noise and greater levels of skew. It is still recommended to further optimize the

model fitting method after a hyperparameter search.

There are two specific caveats of this case study concerning the noise and the NN used.

The noise was injected additively (i.e. additive noise) but noise can be in different forms (e.g.

multiplicative noise). The methods tried may have different effects on different forms of noise.

Moreover, a single configuration of a NN was used. Although the same NN was used to generate

and model the data, the methods may behave differently to different NN configurations.

Likewise, a single configuration of optimizer and batch size was used for the experiments. The

methods tried may have different effects with different NN configurations including the

optimizer and batchsize. Together, these caveats are further impetus for experimentation with all

model fitting methods for each specific modelling task.

696   4   Case study: YY1-genome interactions

The interactions of proteins with DNA of the genome, referred to here as protein-genome

interactions (PGIs), are central to genomics as they are principal components of gene regulation.

The frequency and strength, collectively referred to here as the intensity, of an interaction of a

protein to a location in the genome can depend on the underlying DNA sequence as well as the

surrounding environment which includes histone post-translational modifications (histone PTMs)

(Guertin & Lis, 2010; Slattery et al., 2014; Wang et al., 2012). Successful modelling of PGIs

using DNA sequence and the surrounding environment may yield deeper biological insights that

are not possible by other methods.

Most proteins that interact with their respective genome only substantially interact with a

relatively few locations of the genome and interact with progressively greater intensity to

progressively fewer locations in the genome. Together, the intensities of PGIs are often severely

right-skewed. Early works discretize PGIs using an arbitrary threshold, but this procedure

discounts the differences in intensities which are biologically rooted and therefore should be

taken into account (Toneyan et al., 2022). While PGIs have been modelled before, data was

typically split by chromosome and the models were scored by non-bin metrics that are

ineffective for sequential and Tailed data, respectively. The following case study is an example

of modelling PGIs and assesses existing and novel methods for appropriate data splitting and

consistent model performance.

Yin Yang 1 (YY1) is a DNA sequence-specific transcription factor (a protein that affects

gene transcription) implicated in human diseases such as cancer and has a significant role in

development, specifically neurogenesis (Verheul et al., 2020). The PGIs of YY1 in human

cancer cells are modelled using the human genome DNA sequence and 11 histone PTMs.

The PGIs of YY1 are modelled using a NN called Oyster (Abdulnabi & Westwood,

2025b). There are two major variants of Oyster: Exact and non-Exact. Exact Oyster facilitates

model analysis whereas non-Exact may provide performance benefits. While the previous case

study used different datasets but a single model configuration, the following case study uses a

single dataset but compares the model fitting methods with configurations of Exact and non-

Exact Oysters. Model analysis of Exact Oysters modelling YY1-genome interactions is

conducted in the (Abdulnabi & Westwood, 2025b).

4.1　Methods

728　　　See https://github.com/Husam94/BinMeths/C2-YY1/ for complete details.

4.1.1　Data processing

4.1.1.1　Initial data processing

PGIs are captured through Chromatin Immunoprecipitation (ChIP) followed by DNA

sequencing. Single-end high-throughput sequencing alignment files of ChIP of YY1 and 11

histone PTMs in human cancer cell line K562 were obtained from the Encyclopedia of DNA

Elements (ENCODE), each having 2-3 repeats and a corresponding control with 3 repeats

(ENCODE Project Consortium, 2012) (**Sup. Table. 11**). MACS version 3 (MACS3) was used to

estimate the fragment length of the single-end reads for each alignment file (Zhang et al., 2008).

The alignments were converted to scores that map over the genome and the resolution was

reduced to 50 nucleotides (nts). Only scores in autosomal chromosomes (chr 1-22) were used.

Scores in blacklist regions (Amemiya et al., 2019) were zeroed. For each set of repeats, the

scores of the repeats were scaled relative to the average total scores and were then merged

through averaging.

The variation of a score is best explained by a Gamma distribution, explored in

(Abdulnabi & Westwood, 2025a). The scores of the ChIP repeats were scaled by the scores of

their corresponding control. The ratio of two Gamma distributions is a Beta Prime distribution.

The control-scaled scores, referred to as YY1 scores hereafter, are determined as the mode of

Beta Prime distribution with an α of the ChIP score and a β of the control score.

Windows of size 500 for genomic DNA sequence, 2000 for histone PTM signals, and 50

for YY1 signals were used for modelling. The output of each observation is a single value of

YY1 score over 50 nts. Only relatively few of the possible locations on the genome, referred to

here as sites, outside of the blacklist regions and in autosomal chromosomes can be used for

modelling due to computing budgets. Sites selected should have as balanced of a distribution of

YY1 values as possible but also be as diverse as possible for effective modelling.

ChIP experiments typically result in mound-shaped scores at locations where proteins

interact with the genome. MACS3 was used to determine the YY1 peaks (i.e. locations of the

genome of significant enrichment) with a q-value of 0.001. YY1 scores extend roughly ±1000

nts from the center of the peaks (**Sup. Fig. 1**). Towards diverse sites, the sites containing the

highest local values of YY1 score within ±1000 nts and having control scores greater than 0.5

corresponding to both YY1 and histone PTM ChIP were determined, totaling 113,540 sites.

YY1 scores belonging to the sites were binned by 10,000 histogram bins. Considering

computing budgets and towards a balanced distribution of YY1 scores, 20,000 sites were

sampled based on their histogram bins using Harpoon Sampling, referred to here as center sites.

Towards models that are robust to translational shifts, additional sites shifted ± 150 nts from each

of the center sites were also included, totaling 60,000 sites.

4.1.1.2 Binning, split generation, and output weighting

The YY1 scores are extremely right-skewed and very noisy (**Fig. 9**). YY1 scores for the

selected sites were binned by only using those belonging to center sites to ensure diverse sites in

later bins. They were binned by using the max-scaled YY1 score and using the tanh function and

a scaling factor of 2.497 which was determined to produce the bins with the lowest variation

with a minimum of 50 observations belong to each bin or a max range of 0.45x the total range,

whichever was fulfilled first (**Sup. Table. 12**).

Fig. 9. YY1 scores of selected sites extremely right-skewed and noisy.

A) Histogram (50 bins) of YY1 scores selected for modelling.

B) Scatter plot of YY1 Score and *simulated standard deviation*. For each site, for each of the

ChIP and control scores, a Gamma distribution with an α of the score was sampled 3 times and

averaged, referred to as simulated scores, mimicking the experiment. For each site, the YY1

score was determined as the Beta Prime mode with α of the simulated ChIP score and a β of the

simulated control score, referred to as the simulated YY1 score. This procedure was repeated 100

times, producing 100 simulated YY1 scores for each site. The standard deviation was determined

for the set of simulated YY1 scores, referred to as the simulated standard deviation.

786   The split for modelling was generated using Akin split with Window split as the split

787 generator. Proportions of 0.55, 0.15, 0.15, and 0.15 were used for the training, stoppage,

788 evaluation, and testing sets (see **Supplementary Note 9.1.1**).

789   Output weights were determined as described in **Section 3.1.2.5**.

791 **4.1.2 Model scoring and model fitting**

792   Methods used for model scoring and model comparisons are the same as the ones used

793 for the previous case study (see **Section 3.1.3**) except for two modifications. First, the Mean

794 Deviation Error (MDE) is used instead of the RMSE as it better assesses predictions for

795 measurements with measurement variation (Abdulnabi & Westwood, 2025a). More specifically,

796 the Deviation Error accounts for each YY1 score to have measurement variation that is explained

797 by a Beta Prime distribution. The RMS of the MDE of each bin is referred to as RBM. Second,

798 there is only a single dataset with a single data split and the evaluation set was used to score and

799 compare the experimental units instead of the testing set which is used to assess the final selected

800 model in (Abdulnabi & Westwood, 2025b).

801   All modelling used a NN, RBM as the stoppage metric, a patience of 10, and the Adam

802 optimizer. As with the previous case study, the choice of patience was determined based on trials

803 with other patience values (not included here) and considering computing budgets. The *standard*

804 model fitting method used MDE as the loss function without output weighting and without

805 sampling.

807 **4.1.3 Oyster models**

Configurations of hyperparameters for the Exact Oyster and the non-Exact Oyster

models, including the learning rate for the Adam optimizer and the batch size, were searched.

More specifically, for each type of Oyster, 200 configurations were randomly selected from a

search space that was based on computing budgets and other experiments not included here, see

(Abdulnabi & Westwood, 2025b). All configurations used RBM as the loss function and

sampling with a proportion of 0.1 as it is assumed to save resources without impairing

performance for data with greater levels of noise and right-skew, as seen in the previous case

study.

For each type of Oyster, the top 10 scoring configurations were repeated 10 times. The

configuration with the lowest mean pairwise bootstrap scores (see **Section 3.1.3**) was used for

further experiments (see (Abdulnabi & Westwood, 2025b) for model configurations).

4.2   Results and discussion

The total proportion of sites belonging to each chromosome and the distribution of values

in the bins for each chromosome is not consistent (**Sup. Table. 13**). Even more concerning, some

chromosomes do not have any sites belonging to one or more bins (i.e. the proportions of sites

belonging to one or more bins is 0). It is not clear which chromosome(s) and/or which part(s) of

the chromosome(s) should be used for each division of the data split to obtain the desired

proportions and to have identical distributions. Thus, splitting by chromosome is not an adequate

data splitting method. Akin split worked well to obtain a data split with the desired proportions

and identical distributions (**Sup. Table. 14**). Hence, Akin split is a more appropriate and

effective data splitting method than splitting by chromosome.

The objective of this case study is to minimize the RBM (see **Section 4.1.2** for details)

and three different categories of model fitting methods of bin metrics as a loss function, output

weighting, and sampling were first tried individually and then in combination.

The effectiveness of the model fitting methods applied individually varied and were

dependent on the model. Compared to fitting with MDE (see **Section 4.1.2** for details) as the loss

function, fitting with RBM as the loss function significantly improved the performance of the

Exact model by 54.7% but did not significantly affect the performance of the non-Exact model

(**Table 6**). Since the models were evaluated on the RBM, it was expected that using RBM as the

loss function yielded models that better performed on the RBM than models fit with MDE as the

loss function. Compared to fitting without sample weighting, fitting with reciprocal weighting

significantly improved the performance of the Exact model by 56.4% but did not significantly

affect the performance of the non-Exact model (**Table 7**). Fitting with DenseWeights did not

significantly affect the performance of both models. Compared to fitting without sampling,

sampling proportions of 0.8, 0.4, 0.2, 0.025, and 0.01 significantly improved the performance of

the non-Exact model by up to 39.2% (**Table 8**). Intriguingly, sampling proportions of 0.1 and

0.05 did not significantly affect non-Exact model performance although sampling proportions of

0.2 and 0.025 had. Conversely, the model performance of the non-Exact model was significantly

improved by a sampling proportion of 0.05 by 25.2%. Of the methods applied individually, the

fitting with RBM as the loss function, reciprocal weighting for output weighting, and sampling

proportions of 0.2 and 0.05 for Exact and non-Exact models, respectively, were the best model

fitting methods applied individually.

Table 6. Fitting with RBM as the loss function yielded better performing Exact models but

similar performing non-Exact models compared to fitting with the standard method.

Mean pairwise bootstrap scores comparing Oyster models that were fit with different loss

functions to models fit with MDE as the loss function.

The "Shuffled MDE" refers to models fit with MDE as the loss function but with the outputs in

the training and validation sets shuffled, serving as a negative control.

See **Sup. Table. 15** for full bootstrap statistics.

See **Table 1** for additional descriptions.

Oyster	Exact	non-Exact
Loss Function		
MDE	0.2	1.2
RBM	**-54.7**	-2.9
Shuffled MDE	**322.5**	**592.6**

Table 7. Fitting with reciprocal weighting yielded better performing Exact Oyster models

but similar performing non-Exact models.

Mean pairwise bootstrap scores comparing Oyster models that were fit without output weighting

("None") or with output weighting methods of DenseWeights ("Dense") or reciprocal weighting

("Recip.") to models fit without output weighting.

See **Sup. Table. 16** for full bootstrap statistics.

See **Table 1** for additional descriptions.

Oyster	Exact	non-Exact
Weighting		
None	0.2	1.2
DenseW	**-20.7**	-12.4
Recip.	**-56.4**	11.4

868
Table 8. Fitting with sampling proportion of 0.2 and 0.05 best improved the performance of

the Exact and non-Exact models, respectively.

Mean pairwise bootstrap scores comparing Oyster models that were fit without sampling

("None") or with different sampling proportions ("Samp. Prop.") ranging from 0.8 to 0.01 to

models fit without sampling.

See **Sup. Table. 17** for additional bootstrap statistics.

See **Table 1** for additional descriptions.

Oyster	Exact	non-Exact
Samp. Prop.		
None	0.2	1.2
0.8	**-23.7**	-8.4
0.4	**-29.7**	3.6
0.2	**-39.2**	-19.1
0.1	-24.6	-24.4
0.05	14.1	**-25.2**
0.025	**-38.5**	-22.0
0.01	**-18.1**	-14.0

The most effective methods from each category were tried in combination towards

further improving model performance (**Table 9**). Fitting with RBM as the loss function, with

reciprocal weighting, and with sampling best improved the Exact model by 57.7%. Conversely,

fitting with RBM as the loss function, without reciprocal weighting, and with sampling best

improved the non-Exact model by 32.4%.

Table 9. Using combinations of methods did not further improve the performance of any

model.

Mean pairwise bootstrap scores comparing Oyster models fit with combinations of RMSE or

RBR as the loss function, without output weighting ("None") or with reciprocal weighting

(Recip.), and without sampling ("False") or sampling proportions ("True") of 0.05, 0.025, or

0.05 for Exact, non-Exact A, and non-Exact B models, respectively, to models fit with RMSE as

the loss function, without output weighting, and without sampling. The combinations are denoted

as (loss function, output weighting, sampling proportion).

See **Sup. Table. 18** for additional bootstrap statistics.

See **Table 1** for additional descriptions.

Oyster Combination	Exact	non-Exact
('MDE', 'None', False)	0.2	1.2
('MDE', 'None', True)	-39.2	-25.2
('MDE', 'Recip.', False)	-56.4	11.4
('MDE', 'Recip.', True)	-56.2	-29.3
('RBM', 'None', False)	-54.7	-2.9
('RBM', 'None', True)	-55.8	-32.4
('RBM', 'Recip.', False)	-47.3	57.8
('RBM', 'Recip.', True)	-57.7	-28.8

There were model fitting methods that significantly improved the performance of both

models. Furthermore, the effects of the model fitting methods on model performance was

dependent on the model configuration. The optimal model fitting methods for the model

configurations were different. Together, these results further highlight the benefits and

importance of experimenting and optimizing with the model fitting methods for each individual

model configuration.

5   General discussion

There were model fitting methods that substantially and significantly improved the modelling performance compared to the standard method for both case studies. The effects of the methods on model performance were dependent on the data, specifically the amount of noise and skew, best exemplified in the first case study. In general, the methods were more effective on datasets with noise and skew. Model fitting methods with sampling impaired model performance for datasets without noise and datasets without skew. Still, the model fitting methods with sampling substantially reduced the resources used. For datasets with noise and greater levels of skew, sampling is recommended to be used for hyperparameter search to save resources or enable more search without (presumably) impairing performance. Furthermore, the effects of the methods were also dependent on the model configuration used, best exemplified in the second case study.

There is no general prescription of model fitting methods (or combinations thereof); different methods should be tried for each modelling task. Both case studies explored the methods through a stepwise procedure which first tried the methods individually and then tried the best methods in combination. There may be a combination(s) involving non-best methods that perform better than the combinations explored. An optimal combination of methods is better determined through Random search or an optimization algorithm. As the effects of the combination of methods are dependent on the model configuration used, it is ideal to search the combination of methods along with the model configurations.

There are two major caveats of the case studies presented concerning the metric and the distributions of the data used. First, both case studies assessed the models by the RBR. It is expected that the effects of these methods are dependent on the metric used. As such, the effects

of the methods are expected to be different when assessing the models with different metrics.

Second, both case studies only used right-skewed data. Still, it is expected, both in theory and

from experimentation not included here, that the methods are similarly effective to similar levels

of other Tailed data (left-skewed or bell-shaped data). It is also expected that these methods are

effective for imbalanced data in general, including nominal data.

All methods presented in this study including bin metrics, transformation binning, model

fitting methods, and Akin split, should be used towards appropriate and effective modelling.

Surely, these methods can be used to improve existing works. These methods can be especially

beneficial for works that extract the learned concepts of the models to use them to guide future

exploration which is common practice in genomics ML. Improved models may yield different

and more accurate learned concepts, ultimately better guiding future explorations.

6   Acknowledgements

7   Author contributions

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1003

9   Supplementary

1005

9.1   Notes

1007

9.1.1   Additional sets for ML

Neural Network (NNs) are fit in cycles called epochs wherein the NN is exposed to each

observation of the training set once. The number of epochs can be specified prior to modelling

but the optimal number of epochs is not known prior. Models fit with too few epochs are often

underfit, but models fit with too many epochs are often overfit to the training set and do not

generalize well to unseen data (e.g. the testing set). An additional set can be used to assess the

model at every epoch for its ability to generalize, called the stoppage set (commonly known as a

validation set but renamed for clarity). The performance on the stoppage set deteriorates when

the model becomes overfit, indicating that model fitting should be terminated. While the model

is not exposed to this data directly, it dictates model fitting and thus is separate to the testing set.

There are several tunable parameters concerned with the ML algorithm and/or the model

fitting process, known as hyperparameters. Different configurations of hyperparameters should

be tried towards obtaining the best model possible. The testing set needs to be completely unused

in this process. An additional set is used to evaluate the model during hyperparameter search,

called an evaluation set.

1023

1024   **9.2   Equations**

1025   **Sup. Eq. 1.** tanh function.

1026
$$\tanh(x) = \frac{2}{1 + e^{-\alpha x}} - 1$$

1027

1028   **Sup. Eq. 2.** Inverse tanh function.

1029
$$\tanh^{-1}(x) = -\frac{\log\left(\left(\frac{2}{(x+1)}\right) - 1\right)}{2}$$

1030

1031   **Sup. Eq. 3.** Reciprocal weighting for each bin.

1032
$$p = \text{proportion of values belonging to a bin} = \frac{\text{number of values belonging to a bin}}{\text{total number of values}}$$

1033

1034 $$\text{Reciprocal Weighting } (p) = \frac{1}{p}, p > 0$$

1035

1036 **9.3 Figures**

1037

1038

1039 **Sup. Fig. 1.** YY1 score over YY1 peaks ± 2000 nts from the center.

1040 Peaks were filtered to be outside of Blacklist regions and within autosomal chromosomes.

1041

1042 **9.4 Tables**

1043 All tables in **BinMeths.Sup.Tables.xlsx**.

1044

1045 **9.4.1 Synthetic Tailed data case study**

1046 **Sup. Table. 1.** Tanh Binning and splits for synthetic repeat 1, noise level NA, and right-

1047 skew level RA. "Prop." and "Stop." refer to proportion and stoppage, respectively. Select

1048 columns are white-grey-black color scaled to visualize low to high values for each

1049 respective column.

1050

1051   **Sup. Table. 2.** Tanh Binning and splits for synthetic repeat 1, noise level NA, and right-

1052   skew level RB. Refer to **Sup. Table. 1** for full explanation.

1053

1054   **Sup. Table. 3.** Tanh Binning and splits for synthetic repeat 1, noise level NA, and right-

1055   skew level RC. Refer to **Sup. Table. 1** for full explanation.

1056

1057   **Sup. Table. 4.** Tanh Binning and splits for synthetic repeat 1, noise level NA, and right-

1058   skew level RD. Refer to **Sup. Table. 1** for full explanation.

1059
1060   **Sup. Table. 5.** Mean pairwise bootstrap scores comparing models fit with Adam learning

1061   rates from 0.0003 to 0.01 to models fit with an Adam learning rate of 0.0001.

1062   Bolded values indicate the subject is significantly better or worse than the reference if

1063   negative or positive, respectively.

1064   Dark to light color scale visualize values from -25 to 0.

1065

1066   **Sup. Table. 6.** Statistics of pairwise bootstrap scores comparing models fit with different

1067   loss functions to models fit with RMSE as the loss function.

1068   "SE", "Conf. Int.", and "Sig." refer to standard error, confidence interval, and

1069   significance, respectively. Bolded rows indicate rows that are significant. Dark to light

1070   color scale visualize mean from -25 to 0.

1071

1072   **Sup. Table. 7.** Statistics of pairwise bootstrap scores comparing models fit without

1073   output weighting ("None") or with output weighting methods of DenseWeights

1074   ("Dense") or reciprocal weighting ("Recip.") to models fit without output weighting.

1075   See **Sup. Table. 6** for additional descriptions.

1076

1077   **Sup. Table. 8.** Statistics of pairwise bootstrap scores comparing models fit without

1078   sampling ("None") or with different sampling proportions ranging from 0.8 to 0.01 to

1079   models fit without sampling.

1080   See **Sup. Table. 6** for additional descriptions.

1081

Sup. Table. 9. Statistics of pairwise bootstrap scores comparing models fit with

combinations of RMSE or RBR as the loss function, without output weighting ("None")

or with reciprocal weighting (Recip.), and without sampling ("None") or with a sampling

proportion of 0.1 to models fit with RMSE as the loss function, without output weighting,

and without sampling.

See **Sup. Table. 6** for additional descriptions.

1088

Sup. Table. 10. Statistics of resource pairwise bootstrap scores comparing models fit

with combinations of RMSE or RBR as the loss function, without output weighting

("None") or reciprocal weighting (Recip.), and without sampling ("None") or sampling

with a proportion of 0.1 to models fit with RBR as the loss function without output

weighting and without sampling. The combinations are denoted as (loss function, output

weighting, sampling proportion).

See **Table 5** for description of resource pairwise bootstrap scores.

See **Sup. Table. 6** for additional descriptions.

1097

9.4.2 YY1-genome interactions case study

Sup. Table. 11. Files obtained from ENCODE. "predictd" column is the predicted fragment length determined using MACS to extend single-end reads.

Sup. Table. 12. Tanh Binning of YY1 values. Refer to **Sup. Table. 1** for full explanation.

Sup. Table. 13. Chromosomes differ in the number and distributions of observations belonging to them.

Proportions of observations of each chromosome belonging to each bin. The Total column indicates the total proportion of observations belonging to the chromosome. Light-dark color scale visualize low to high values for each respective column. Red shading indicates a 0 value.

Sup. Table. 14. Akin Split produces a split with the desired proportion and similar distributions.

Proportions of observations of each set belonging to each bin.

See **Sup. Table. 13** for additional descriptions.

Sup. Table. 15. Statistics of pairwise bootstrap scores comparing Oyster models fit with different loss functions to models fit with MDE as the loss function.

See **Sup. Table. 6** for additional descriptions.

1121   **Sup. Table. 16.** Statistics of pairwise bootstrap scores comparing Oyster models fit

1122   without output weighting ("None") or with output weighting methods of DenseWeights

1123   ("Dense") or reciprocal weighting ("Recip.") to models fit without output weighting.

1124   See **Sup. Table. 6** for additional descriptions.

1125

1126   **Sup. Table. 17.** Statistics of pairwise bootstrap scores comparing Oyster models fit

1127   without sampling ("None") or with different sampling proportions ranging from 0.8 to

1128   0.01 to models fit without sampling.

1129   See **Sup. Table. 6** for additional descriptions.

1130

Sup. Table. 18. Statistics of pairwise bootstrap scores comparing Oyster models fit with

combinations of MDE or RBM as the loss function, without output weighting ("None")

or with reciprocal weighting (Recip.), and without sampling ("FALSE") or sampling

proportions ("True") of 0.2 or 0.05 for Exact and non-Exact models, respectively, to

models fit with MDE as the loss function, without output weighting, and without

sampling. The combinations are denoted as (loss function, output weighting, sampling

proportion).

See **Sup. Table. 6** for additional descriptions.