Emergence of active turbulence limits chemotaxis-induced collective
condensation of bacteria.

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Abstract

Collective bacterial condensation arises from positive feedback between the ability of bacteria to generate chemical gradients and their chemotactic ability to track those gradients, resulting in the spontaneous formation of local cell accumulations. Here, by following the bacterial condensation dynamics in uniform acidic environments, we show that condensation is critically constrained by the spontaneous emergence of correlated bacterial swimming. Under the unique conditions prevailing within the condensate— characterized by sharp cell-density gradients and the absence of physical boundaries— correlated bacterial motion leads to vortex-like cell motion with an additional substantial radial component directed down the cell-density gradient. Correlated bacterial motion leads, in turn, to local fluid motion that tends to broaden the condensate and expels non-chemotactic bacteria. However, when cells are embedded in a porous environment, correlated motion is suppressed, allowing spontaneous condensation to proceed further and form exceptionally dense bacterial accumulations. Overall, these findings highlight a previously unrecognized interplay between self-generated bacterial condensation and correlated swimming.

Significance statement

Self-induced condensation and active turbulence are two prominent forms of collective bacterial behaviors. However, their interplay has not been experimentally studied. Here, we show that collective bacterial condensation gives rise to correlated swimming, which in turn fundamentally limits further condensation. Furthermore, we demonstrate that in dilute porous environments—common in natural bacterial habitats—correlated swimming is strongly suppressed, enabling the spontaneous formation of extremely dense cell condensates. These condensates may serve as a basis for the development of more structured bacterial communities.

Introduction

Motile bacteria navigate their environment by tracking chemical gradients toward regions they deem favorable (1-4). This behavior, termed chemotaxis, influences many aspects of bacterial ecology (5, 6) and human health (7-9). Even in spatially uniform environments, bacteria can collectively follow self-generated gradients, allowing them to accelerate their expansion into resource-rich regions (10, 11), or, alternatively, condense into focal points by either secreting beneficial (attractant) effectors (12, 13) or neutralizing harmful (repellent) effectors (14). Notably, in contrast to the inherently dynamic bacterial distributions triggered by external chemoeffector release (15) or in expanding bacterial bands (16), bacterial condensation can lead to sharp but quasi-static bacterial accumulation (14). Condensation relies on positive feedback between self-generated gradients and the chemotactic responses of the bacteria to those gradients (Fig. 1A) that, in principle, can lead to a divergence in the local cell density (17). From studies of low cell-density, transient condensations, it was suggested that a fundamental limit on such cell condensation arises from the fact that chemotaxis itself is a non-local behavior (18). However, the fundamental constraints on stable, high-density bacterial condensations remain unclear. Here, we show that at high cell-density, stable condensation is, in fact, limited by the dynamic emergence of correlated bacterial swimming.

Escherichia coli (E. coli) cells, a model for studying chemotaxis behaviors, use rotating helical filaments (flagella) that bundle at the back of the cell and propel it forward. However, during stochastic episodes of counter-rotation the bundle comes apart, causing random reorientation of the cell. These two swimming modes—forward swimming ('run') and random reorientation ('tumble')—together generate an active random walk (19). The typical run length (~10–30 μm) defines a fundamental characteristic length scale. In the presence of effector gradients, the probability of

tumbling is modulated to bias the random walk toward beneficial effectors and away

from harmful ones. In particular, bacteria can migrate towards neutral pH (20, 21), which

along with their ability to neutralize the environment, can lead to their spontaneous, self-

induced, condensation (14). Notably, this behavior is readily apparent only under

conditions that the bacterial suspension is coupled to larger, cell-free environment that

keeps the pH level within the dynamic range of efficient sensory detection, but also

prevents oxygen depletion, allowing cells to remain motile.

On the other hand, at high cell density, bacteria tend to exhibit correlated motion

(22, 23), which may lead to turbulent-like motion often termed 'active turbulence' (24-26).

This behavior arises from direct steric interactions between cells and long-range

hydrodynamic interactions mediated by the fluid. With notable exceptions (27, 28),

correlated bacterial swimming has mostly been studied in uniformly distributed

populations confined by physical boundaries. In contrast, bacterial condensation leads

to highly non-uniform cell distributions in the absence of explicit physical boundaries.

However, the interplay between bacterial condensation and correlated swimming is

poorly understood. Numerical studies have suggested that dilute self-attracting run-and-

tumble particles with rather weak chemotactic strength aggregate less efficiently when

self-induced fluid motion is considered (29). In addition, experiments have suggested

that cell alignment may constrain the angular rotation of individuals and thus reduce their

chemotactic efficiency in uniform cell density and shallow effector gradients (25).

However, other experiments with notable cell-density gradient have shown that the

tendency of cells to align may, in fact, enhance their taxis efficiency toward a local

source (30). Thus, how correlated, collective swimming of bacteria may influence their

condensation remains unclear.

Here, we investigate the limits of bacterial condensation using the low-pH setup

under conditions where oxygen deprivation or effector-saturation is not the primary

limiting factor. We show that stable bacterial condensation in liquid is sharply

constrained by the emergence of correlated bacterial swimming during cell

accumulation. This correlated bacterial swimming gives rise to substantial turbulent fluid

motion, with averaged velocity characterized by vortex-like motion with an added velocity

component in the outward direction aligned with the downward cell-density gradient.

This fluid motion effectively exerts outward physical forces on the cells that counter the

inward chemotaxis force. Interestingly, the alignment of the collective motion with the

cell-density gradient was maintained even in ring-shaped condensates (appeared at very

high cell densities), in which case, the bacterial behavior in the outer region of the ring

remained as before, but at the inner region the radial velocity and vortex direction

reversed. Finally, we show that in porous environments, bacterial correlated motion is

diminished without significantly affecting the chemotactic performance of cells.

Consequently, bacterial condensation is considerably enhanced, approaching the low

cell-density limit but with much higher cell densities.

Results

Bacterial condensation is constrained by the emergence of correlated swimming.

To test the constraints on bacterial condensation in a controlled environment, we used

the setup illustrated in Fig. 1B (see ref. (14)). In this setup, free-swimming cells are

confined within a shallow liquid layer (typically 120 µm thick), sandwiched between glass

and a much larger hydrogel, which establishes a uniformly low-pH environment (pH 5.2).

Under these conditions, bacteria tend to collectively condense due to inherent feedback

between the ability of the bacteria to neutralize their local pH and their chemotactic

ability to swim towards neutral pH (14). While cells cannot penetrate the dense hydrogel

mesh (3 % agarose), protons and oxygen readily diffuse across the bacterial layer and

into the gel, preventing their rapid depletion inside the bacterial condensate and thereby

enabling quasi-stable, high-density cell condensation (14), as demonstrated in Fig. 1B

(right plot).

By following the peak cell-density (ρ_{max}) and the width at half-maximum (W) of

the cell distribution we identified two distinct temporal phases of the condensation

(Fig. 1C). Initially, in phase 1, the peak cell-density ρ_{max} increased while the width W

decreased, reflecting strong bacterial condensation. Then, beyond a critical time point

(t_{sat}), in phase 2, the width W abruptly plateaued while ρ_{max} continued to rise, reflecting

continued cell accumulation without further narrowing of the condensate. These trends

are further demonstrated in Fig. 1D, where the width of the condensation is plotted

against the maximum cell density for several repetitions. Notably, the saturated

condensate width was substantially larger than the low-cell-density limit previously

reported in ref. (18). The spatial profile of the bacterial accumulation also reflected this

dynamical transition (Fig. 1D, inset). By normalizing each profile by ρ_{max} and the width

by W, the profiles collapsed onto a single curve in each phase, but these cumulative

curves were distinct between the two phases.

The dynamic transition described in Fig. 1D, was clearly associated with the

appearance of significant density fluctuations within the condensate (Fig. 1E). Initially

(phase 1), the bacterial condensate was smooth and stable (Fig. S1). However, beyond

the critical time point (t_{sat}), pronounced spatial non-uniformity developed, with clear cell-

density fluctuations on a scale of approximately 20-100 μm, characterizing correlated

bacterial swimming (Fig. 1E, see also Supplementary Movie 1). Analysis of these

dynamic and seemingly-chaotic swimming patterns using particle image velocimetry

(PIV; see Materials and Methods) revealed that, on-average (~ 30 sec), cell motion is

characterized by a vortex-like clockwise rotation of the entire condensate as well as a

radial component (Fig. 1E). Interestingly, the emergence of the cell-density fluctuations

and correlated swimming coincided with the dynamic transition at t_{sat} (Fig. 1E).

Fluid motion associated with the bacterial correlated swimming. To characterize

the potential fluid-motion related to the bacterial correlated swimming, we embedded

passive green fluorescent beads (1 µm in diameter) within the bacterial population,

which in this case expressed red fluorescent proteins (Fig. 2). The beads' motion was

analyzed by particle tracking (Materials and Methods). Typically, trajectories included

periods of local motion interrupted by approximately directional movements, termed 'jets'

(Fig. 2A). To elucidate the effect of the bacterial motion on the beads, we evaluated for

each jet the ratio $Pe = \upsilon \cdot L / D_{beads}$ (Péclet number), where υ and L are the characteristic

velocity and length of the jet, respectively, and D_{beads} is the diffusion constant of the

beads. This Pe characterizes the time required for a bead to traverse a typical distance

by fluid flow compared to the typical diffusion time associated with the same distance.

The cumulative distribution of Pe is shown in Fig. 2A (right plot) for trajectories within

(green) or outside (blue) the condensate region. Clearly, the beads' motion was

substantially expedited within the condensate.

Turbulent-like fluid motion can potentially also modulate the effector (H^+)

distribution. To evaluate the potential significance of this effect, we evaluated the Pe

parameter for the protons ($D_{protons} \sim 10^3 \cdot D_{beads}$), assuming protons follow the local fluid

motion. Fig. 2B presents the cumulative number of jets per bead, integrated over a

diffusion time of a proton from the condensate center to its edge $t_D = W^2 / 4 D_{H+}$, where W

is the width of the condensate. These data show that, on average, each bead

experiences at least one substantial jet with $Pe > 0.5$ over the time t_D. We therefore

conclude that, while cell-induced fluid motion can influence the effector distribution, it is

most likely not dominant.

As with the bacterial collective motion, averaging the beads' motion in time

(90 sec) reveals a vortex like fluid flow in the condensate (Fig. 2C–D). The spatial

distributions of the velocity components are shown in Fig. 2C, and the corresponding

profile of the angular velocity is shown in Fig. 2D, revealing a coordinated vortex like

motion. Notably, in addition to the tangential velocity contributing to vorticity, the flow

field exhibited a substantial outward radial component peaking at ~ 0.85 µm·s^{-1} near its

half-width and extended throughout the condensate. This outward radial velocity is

comparable to *E. coli's* chemotactic drift velocity (19, 25). Additionally, we noted that

above the condensed cells, which tended to occupy the lower-half region of the fluid

layer (~ 60 µm), the tracer beads exhibit an inward flow (Fig. 2E; Supplementary

Movie 2). Thus, the fluid motion in the vicinity of the condensate exhibited a three-

dimensional toroidal pattern (Fig. 2F).

Correlated swimming leads to expulsion of non-chemotactic cells. Given the

observed fluid motion, and particularly the outward radial component, we tested its effect

on the cells within the condensate. To this end, we repeated the condensation

experiments using a mixture of chemotactic (wild-type, red-labeled) and low density non-

chemotactic cells (*ΔcheY ΔcheZ* cells; green-labeled). Because non-chemotactic cells

are not subjected to the inward chemotactic force, we expected them to be more

sensitive to influence by the fluid motion. We found that as the wild-type cells

condensed, the non-chemotactic cells were expelled from the condensate (Fig. 3).

Additional run-and-tumble but non-chemotactic strain was tested (31), also showing

significant depletion, see Fig. S2 and related text. We expect this outward force to act

also on chemotactic cells; however, in their case, this force is balanced by an inward

chemotactic force that drives condensation. Still, such an outward force can be

expected to influence the width of the condensate.

Porous environments suppress correlated swimming and enhance condensation.

Porous media is expected to dampen fluid flows due to the added drag with the porous

scaffold (32) and potentially inhibit correlations between bacteria. For example, porous

media have been suggested to inhibit bioconvection (33). Thus, to further test the effect

of correlated swimming on bacterial condensation, we conducted experiments in which

cells were immersed in a thin porous environment formed by a dilute agarose hydrogel

(0.08%) instead of liquid (Fig. 4A). The rest of the setup was unchanged. Using the

channel chemotaxis assay described in ref. (21), we verified that the bacterial

chemotaxis performance in this porous environment was comparable to that in liquid

(Fig. S3). Moreover, by introducing opposing chemoeffectors at one end of the channel,

we triggered low cell-density accumulation. The agarose hydrogel had no detectable

effect on the cell-diffusion-driven broadening of this accumulation (Fig. S3).

In contrast, the porous environment had a dramatic effect on bacterial

condensation and correlated swimming (Fig. 4). Although the condensation proceeded

at a rate similar to that in liquid, it saturated in hydrogel only when the width of the

condensate approached the low-density limit of ~180 µm (18) (Fig. 4A-B).

Correspondingly the cell density in these tightly condensed bacterial populations

became extremely high. As in liquid, also in porous environment, the shape of the

bacterial condensate was modified when it reached its limit (Fig. S4). Finally, the

saturated condensates were also more compact in the vertical direction, spanning only

~30 µm. Overall, in porous environments, the bacterial population spontaneously

condensed to its fundamental limit, reaching a cell volume fraction of 0.5-0.7 (Fig. S5),

while the cell population remained largely dynamic (Supplementary Video 3).

The enhanced condensation observed in porous environments was indeed

associated with a suppression of correlated swimming and associated fluid motion (Fig.

S6 and Fig. 4C). Furthermore, when we repeated the experiments with mixed

populations of chemotactic and non-chemotactic cells in the hydrogel environment, we

found that, despite the strong condensation of the chemotactic cells, the expulsion of the

non-chemotactic cells was significantly weaker (Fig. 4D). Taken together, these results

further support the notion that bacterial condensation in liquid media is limited by the

emergence of correlated swimming, rather than merely the high cell density.

Ring-like condensation and the potential role of oxygen-taxis. To test the

condensation at still higher cell densities, we repeated the experiments while increasing

the initial (uniform) cell density (Fig. 5). Since only one condensate is formed in the well

diameters used here (see also ref. (14)), we expect the overall cell density in the

condensate to increase accordingly. Yet, we find that in both liquid and porous media,

following the initial condensation, once enough cells accumulate, the peak density

ceases to increase while the condensate broadens and turns into a ring (Fig. 5). A likely

cause for such ring formation are the expected oxygen gradients, formed around the

condensate, promoting cell dispersion by oxygen-taxis (aerotaxis) (34). Compared with

the liquid medium, ring formation occurred at much higher cell density in the porous

environment but at significantly lower total number of cells (Fig. 5A). This difference

may result from the fact that turbulent swimming in liquid weakens the net inward force

and can be more easily be dominated by aerotaxis. Additionally, in liquid, aeration of the

condensate by bacteria-mediated convection may support the accumulation of higher

cell numbers prior to ring formation.

245   Interestingly, we found that in liquid, following ring formation, the vorticity

reverses between the inner and outer regions of the 'aerotaxis' ring (Fig. 5C). This

includes both the radial and tangential velocities. We note, however, that the reversals

of both velocities are consistent with them being determined relative to bacterial density

gradient: the collective motion flows radially down the cell density gradient and tends to

exhibit also a rightward lateral deflection in both cases (illustrated in Fig. 5C).

Simplified model for condensate broadening. To test whether the observed cell-

induced fluid motion (Fig. 2) can indeed lead to repulsion of non-chemotactic cells

(Fig. 3) and broaden the condensation of wild-type cells, we used Keller-Segel type

chemotaxis model (35) that describes the bacterial condensation in such acidic

environment (14, 36):

$$\frac{\partial \rho}{\partial t} = \vec{\nabla} \cdot \left(D \vec{\nabla} \rho - \rho \vec{v}_D \right) \quad (1)$$

$$\frac{\partial c}{\partial t} = D_c \nabla^2 c - r_H \rho c \quad (2)$$

Here, D is the active diffusion of the cells, v_D is their drift velocity, D_c is the effective

proton diffusion coefficient, and r_H is the proton-removal rate. Note that bacteria are not

growing in these experiments. Following ref. (37), the chemotaxis-induced drift velocity

was modeled as $\vec{v}_D = \beta \vec{\nabla} \ln \left(c + K_{off} / c + K_{on} \right)$ where K_{on} and K_{off} are the effective

dissociation constants for the chemoreceptors in the ON or OFF states, and β is the

chemotaxis coefficient. The proton-removal rate was given the empirical form $r_H = \gamma c^{1/2}$

(14). The cell density dynamics was assumed to be two dimensional and radially-

symmetric, occupying the top layer of a three-dimensional proton field. See Supp. Text

for details and parameters used. This model accurately describes the shape of

condensates in phase 1 (Fig. 6A). However, it predicts much sharper condensation and

a different shape than those observed experimentally in phase 2 (Fig. 6B, dashed blue

line).

Thus, considering the random fluid motion at short time scales with the added

outward averaged drift component observed in Fig. 2, we suggest that bacteria

subjected to such fluid motion experience not only the inward-pointing chemotactic force,

but also an additional radial drift. Since this radial velocity was found to be proportional

to the cell-density gradient (Figs. 2C, 5C, and S7), we added a drift velocity of the form:

$$\vec{U} = -\eta \cdot \vec{\nabla}(\rho / \rho_0) \quad (3)$$

with $\eta = 10^{-7}$ cm^{2}s^{-1} and ρ_0 the initial (uniform) cell density ($\rho_0 \sim 0.7 \cdot 10^6$ cells·mm^2).

Indeed, adding this fluid-induced velocity component to the model can strictly limit the

condensation and account for the broadening and shape of mature condensates during

phase 2 (Fig. 6A-B, black lines). Notably, adding the drift velocity ($\vec{U}$) from the beginning

of the simulation resulted in a gradual transition between phase 1 and phase 2, which

does not agree with the sharp transition observed in the experiments (Figs. 1C and 6B).

However, adding this velocity only above a certain threshold cell density clearly account

for the observed transition (Fig. 6B). This is consistent with the emergence of the

correlated motion only above a certain cell density (Fig. 1). The added drift velocity ($\vec{U}$),

can also account for the expulsion of non-chemotactic cells from the condensate (Fig.

6C, see also Fig. 3 and Supp. Text).

Finally, we also considered the potential influence of correlated swimming on the

chemotaxis efficiency (25, 38). First we note that for such influence to limit

condensation, it must reduce chemotaxis efficiency. To incorporate this into the model,

we allowed the chemotactic coefficient (β) to depend on the local cell-density according

to the findings in ref. (25) (Fig. S8). Clearly, such an effect can also contribute to limiting

the condensation (Fig. 5B, orange line). Yet, it would not lead to repulsion of non-

chemotactic cells.

The overall relationship between the initial cell density and condensation is

summarized in Fig. 6D. When the initial cell density is below approximately

$0.4 \cdot 10^6$ cells/mm^2, no condensation is observed (14, 36). At higher densities, the initially

uniform distribution becomes unstable, and condensation emerges. In the absence

corelated swimming, the bacteria can condense until the local cell density becomes

sufficient to raise the local pH beyond the sensory dynamic range of the cells (blue line,

see also ref. (14)). However, because correlated swimming readily emerges, bacterial

condensation is severely restricted (simulations: dark-gray line; data: red circles). In

contrast, in porous media, condensation proceeds further (gray circles), though still

limited below the value set by the dynamic range (blue line), likely due to the non-local

nature of bacterial gradient sensing (see ref. (18)). At even higher cell densities,

condensation becomes limited by ring formation, likely due to aerotaxis (Fig. 5).

Discussion

Chemotaxis-mediated condensation and correlated swimming are two prominent

collective behaviors exhibited by motile bacteria. Here, we reveal an intrinsic interplay

between these behaviors. We show that bacterial condensation is fundamentally

constrained by the emergence of correlated swimming (Fig. 1), and, on the other hand,

that bacterial condensates lead to a distinct form of correlated swimming under

conditions of stable but sharp cell-density gradients and the absence of physical

boundaries confining the cell population (Figs. 1–3). Furthermore, we find that

correlated swimming is suppressed in porous environments, enabling exceptionally

robust bacterial condensation with extremely high cell density (Fig. 4).

The dynamics of bacterial condensation in liquid exhibit two phases (Fig. 1C-D):

initially, the condensate narrows while cell density increases; then, quite abruptly, the

width plateaus while cell density continues to rise. Notably, this transition coincides with

the emergence of correlated bacterial swimming (Fig. 1E), which strictly prevents further

narrowing of the condensate, and while additional cells can join the condensate, its width

remains fixed. Previous experiments demonstrated bacterial expulsion from a local

vortex generated by rotating magnetic microspheres at 2–40 Hz (27). Here, we show

that non-chemotactic bacteria are forced out of the condensate (Fig. 3), which exhibits

much weaker vorticity (~ 10^{-3} Hz). Notably, this expulsion force is diminished in a porous

environment, where cell density in the condensate is approximately 10-fold higher but

correlated swimming is absent (Fig. 4). This suggests that expulsion of non-chemotactic

cells from the condensate is not merely due to accumulation of the chemotactic cells.

Rather, this expulsion is consistent with the observed outward fluid flow generated by

correlated swimming in liquid. These forces, in turn, lead to segregation of the bacterial

communities into chemotactic and non-chemotactic subpopulations (Fig. 3).

The fluid motion in the vicinity of the condensate exhibited a three-dimensional

toroidal pattern (Fig. 2F). Such motion patterns seem somewhat similar to the patterns

observed in bioconvection (33, 39). Bioconvection occurs due to instability formed by

upward bacterial taxis and a downward gravitational force, which becomes dominant

once bacteria reach high enough cell-density. More complex behavior has been

observed when metallic particles were also driven up and down by the applied voltage of

the sample (40). In contrast, in the system described here, the condensate is overall

stable near the bottom surface and the fluid motion arises due to random but correlated

swimming of the bacteria combined with the large cell density gradients imposed by the

chemotactically driven condensation.

Advection of chemotactic effectors by the turbulent-like fluid motion may

contribute to limiting condensation by also limiting the buildup of steep effector gradients

(Fig. 2B). We find that within a time period corresponding to the diffusion time across

the condensate, each probe particle typically experiences at least one significant event

that enhances its motion beyond simple diffusion ($Pe > 0.5$). This suggests that while

advection might not dominate over diffusion, it is not negligible. Finally, a direct

influence of correlated-swimming on chemotaxis efficiency, as suggested in ref. (25),

may also contribute to limiting bacterial condensation (Fig. 5B). However, given the

strong effector and cell-density gradients within the condensates, the extent of this effect

is not clear.

In general, but with a notable exceptions (28, 41), correlated bacterial swimming

has been studied in uniform cell populations confined by well-defined lateral boundaries,

either solid (42) or at liquid–air or liquid–oil interfaces (42-45). In such settings, the

bacterial swimming patterns the bacterial behavior near the lateral physical boundaries

may play an important role in the observed behaviors (43, 46). In contrast, bacterial

condensation leads to stable and highly non-uniform bacterial distribution driven by self-

induced chemoeffector gradients in the absence of lateral boundaries. Under these

conditions, we find a clear radial velocity, in both the cells' correlated motion and

associated fluid motion, that generically aligns with the bacterial density gradient

(Figs. 1,2, 5 and S7). This alignment is consistent with the fact that correlated swimming

is enhanced at high cell densities (28) but fades as cells spread to down the density

gradient.

In small wells spanning less than few tens of microns, active turbulence was

shown to exhibit vortex-like motion with a random direction, whereas in larger wells,

chaotic motion was observed without coherent vorticity (47). In contrast, the correlated

swimming observed here is consistently characterized by time-averaged clockwise

vorticity of the entire condensate (~ 600 µm), as viewed from the glass side (Figs. 1–2).

At higher cell densities, when the condensate develops a ring-like structure (most likely

due to aerotaxis), the vorticity reverses between the inner and outer regions of the ring

(Fig. 5C). However, since the radial velocity also reverses across the ring, a global

rightward swimming tendency is maintained. Notably, this rightward swimming tendency

is consistent with the circular motion observed when non-interacting individual cells swim

near glass surfaces (< 1 µM; Fig. S9) (48). However, bacterial condensates extend

farther from the surface (up to 60 µm) and are far denser. Thus, it seems that the

interaction with the glass surface might not be enough to cause strong vorticity but it

may still introduce a clockwise bias to the otherwise chaotic motion.

Correlated bacterial swimming was clearly supressed in porous environments

leading to extremely dense cell condensates (Fig. 4), which may further promote the

formation of structured bacterial communities. Notably, experiments conducted in

mucin-containing media at neutral pH still exhibit correlated swimming, albeit with larger

vortex size (49). Interestingly, however, low-density agarose hydrogel more closely

resembles mucin-containing media at low pH (50), which may be more relevant to

certain physiological conditions than neutral pH.

Materials and Methods

Strains and plasmids. We used *E. coli* MG1655 (VF6 (31, 51)) and its derivatives

harboring deletion of *cheY* and *cheZ* (MK3) or deletions of all chemoreceptors and a

dysfunctional *cheZ* gene (non-chemotactic run-and-tumble cells (AVE4 (31)). Cells

expressed also a fluorescent mGFP (75 µM IPTG) or mCherry (5 mM) from a pTrc99a

vector (pSA11).

Cell growth and motility medium. Cells were grown over night in Tryptone Broth (TB,

tryptone extract 10 g/l and 5 g/l NaCl) supplemented with Ampicillin, diluted 100-fold into

fresh medium with IPTG, and allowed to grow at 33.5 °C with shaking. Cells were

harvested at an OD_{600} of 0.5 by centrifugation and gently washed twice in motility

medium and resuspended in motility medium with final cell concentration of OD_{600} 0.4

(unless otherwise mentioned). The motility medium (0.1 mM potassium phosphate,

0.94 mM lactic acid, 85.5 mM sodium chloride, 0.1 mM EDTA, and 1 µM methionine)

titrated to the desired pH with NaOH. Notably, this medium supports long-term bacterial

motility but not cell proliferation. Experiments in porous medium (Fig. 4) were done

gently mixing the cell suspension with agarose hydrogel at 37 °C to a final agarose

concentration of 0.08%.

The condensation setup. The setup used here is schematically illustrated in Fig. 1a.

For more details see ref. (14). An agarose gel (3% in motility medium) was casted in a

cylindrical chamber made from grade-2 titanium (6 mm height, 10.7mm diameter) and

sealed at the top with a mold with a thin cylindrical protrusion (~120 μm high, and radius

of ~ 3 or 5 mm), which will form the bacterial layer; fabricated using a resin printer

(Elegoo Mars 3). After the agarose solidified, the mold and the bottom cover were

removed and the agarose was dialyzed overnight in motility buffer and a second time, for

an additional 4 h, in a fresh motility buffer just before the experiment (final dialysis ratio

of 10^4:1). Bacterial cells were then introduced into the shallow well, suspended in either

liquid or soft agarose (0.08%), and the bottom and top of the chamber were covered with

BSA-treated glass coverslips (1% bovine serum albumin in double-distilled water for 30

minutes) and secured in position. Experiments were performed at room temperature (24

°C).

Fluorescence microscopy. The bacterial distribution was followed by using a Nikon Ti

microscope equipped with a 20× (0.5 NA) or 4× (0.2 NA) objective, a decoded controlled

stage and a 'perfect-focus' system. Large images were obtained by stitching smaller

images (approximately 2mm× 2mm each) with 20% overlap using a built-in function in

NIS Elements software (Nikon). The bacterial distribution inside the well was extracted

from the images by removing the measured background intensity and normalizing to the

average intensity within each well. Radial averaging was done by measuring the

fluorescence intensity around the center of focal points (Radial Profile Angle plugin for

ImageJ).

Cell density estimates. Due to inhomogeneity of the cell distribution in the vertical

direction (see Fig. 2F), cell distributions are shown in cells/mm^2. Calibration of OD_{600} to

cells/mm^3 was done by plating serial dilution of cells after growth (OD_{600} 0.5), yielding

OD_{600} 0.5 ≈ 7.2·10^9 cfu/mm³. Surface density was then estimated by multiplying the cell

density (ρ_{3D}), averaged over the vertical direction (z), by the well height (h): $\rho = h\langle\rho_{3D}\rangle_z$.

Non-uniformity estimates. To determine the non-uniformity of the cell distribution

within condensates from still images, where temporal averaging is unavailable, a smooth

radially-averaged version of each image was subtracted from the original ones. A high-

pass filter was then applied to remove residual, large-scale intensity fluctuations (0-140

μm). Non-uniformity was then measured as the difference between the standard

deviation of the intensity within a disk around the condensate center (600 μm diameter)

and away from it.

Fluorescent spheres. In the experiments presented in Fig. 2, we used green

fluorescent spheres (beads) with a 1μm diameter (FluoSpheres, ThermoFisher

Scientific). Before use, spheres were thoroughly washed in motility medium to which

Tween-20 (0.01%) was added. The spheres were then added to a cell suspension,

which also contained Tween-20 (0.01%). The added Tween-20 prevented self-

aggregation of the fluorescent spheres but had no detectable effect on the bacterial

condensation.

Particle image velocimetry (PIV). To capture velocity fields, time-lapse fluorescent

images (2-10 frames per second) were captured and analyzed by PIV using PIVLab(52).

To analyze the collective motion of cells, a filtering procedure was first applied to remove

the large-scale bacterial condensation (see Non-uniformity estimates) and a nearest-

neighbors smoothing scheme was applied to remove residual noise. PIV analysis

proceeded using multipass FTT window deformation (4 passes) with the final

interrogation window being 16-18 pixels (64–72 μm). To avoid false detection, only

vectors with a correlation coefficient larger than 0.5 were kept. The PIV parameters

were chosen to balance between the resolution of the extracted velocity field and the

signal-to-noise ratio; changing them did not modify the results significantly. To analyze

the motion of the fluorescent beads, an initial mask was applied to ensure only particles

within the focal plane were analyzed. This was possible since beads within the focal

plane seem smaller and brighter than beads in other planes (see SI Video 3). Despite

the BSA treatment, beads slowly adhered to the glass coverslip. By subtracting the

median image from the time lapse, only non-adhered beads were analyzed. Analysis

then proceeded in PIVLab as described for the bacteria.

Particle tracking and detection of jets. Time lapse images (2 frames per second) of

the fluorescent beads were masked to ensure only particles within the focal plane are

analyzed (see Particle image velocimetry (PIV)). Tracking was then performed using the

TrackMate plugin for ImageJ. Detected tracks were exported and analyzed separately.

Each track was smoothed using a Savgol-Golay filter (5 frames window) and velocities

were estimated numerically. Jets were detected as temporal peaks in the velocity

magnitude with a mean prominence of more than 0.5 μm/s. The length of each track (L)

and it's mean velocity (v) were captured. If neighboring beads, less than L apart,

exhibited a jet in the same direction ($\Delta\theta < 0.15$), their jets were considered as correlated;

the velocity of such jets were averaged over and considered as one. Due to the low

density of beads, such events were rare (7 of the 2362 detected jets).

Numerical solution of the model. Solutions and parameters were based on (14) and

full details can be found in the Supp. Text. Briefly, the dynamics of cells was modeled in

2D assuming radial symmetry and the dynamics of protons was modeled in 3D

assuming cylindrical symmetry. Proton uptake in the bacterial layer was accounted for

by imposing absorbing boundary conditions for the protons at the bacterial layer

interface. Numerical solutions were obtained by calculating spatial derivatives with 2nd

order accuracy and using a 4th order Runge-Kutta method for time integration.

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Figure 1. Bacterial condensation is constrained by correlated swimming. **(A)** Schematic of bacterial condensation in acidic environments (see ref. 14). On the one hand, by neutralizing free protons in their vicinity, cells generate pH gradients in an otherwise uniform acidic environment. On the other hand, cells are chemotactically attracted toward neutral pH. These behaviors form reinforcing feedback that derives condensation. **(B)** The experimental setup consists of a thin liquid layer (~ 120 µM thick and 5 mm diameter) with GFP-expressing, free-swimming bacteria, molded in a 3% agarose gel. Both the liquid layer and the surrounding gel initially formed a uniform acidic environment (pH 5.2), and the bacterial condensation dynamic was monitored using fluorescence microscopy. A typical condensate at steady state is shown on the right (2 h after initiation, scale bar - 300 µm) along with the radially averaged cell-density. The width at half maximum (w) and peak cell density (ρ_{max}) are marked. **(C)** A typical condensation dynamic is shown, characterized by the width (w) and peak cell density (ρ_{max}). The abrupt saturation of the condensate's width is marked by t_{sat}. **(D)** The width of the condensate (w) is plotted against peak cell density for 7 independent experiments. Solid gray line reparents power-law slope of -2/3. Dashed lines mark the width of saturated condensates (dark gray) and the corresponding value measured at low cell density (light gray, (18)). *Inset* – normalized cell density profiles observed at different time points for 3 independent experiments: profiles were labeled red for $t < t_{sat}$ and green for $t > t_{sat}$. Profiles at $t \sim t_{sat}$ (within 5 min) are not shown. Density was normalized by subtracting the baseline and dividing by the peak density; the radial coordinate was normalized by $w/2$. **(E)** Collective swimming emerges at $t \sim t_{sat}$. A typical filtered fluorescence image (top-left) highlighting the emerging non-uniformity (see Materials and Methods), and the corresponding time-averaged (30 s) velocity field obtained by particle image velocimetry (PIV; top-right; grey arrows are a guide to the eye). See also SI Video 1. Fluorescence intensity of the non-uniformity (Δ) within condensates ($r \leq 300$ µm) is shown over time (lower plot; 4 independent experiments. see Materials and Methods); inset – Δ divided by the square root of the peak intensity (I_{peak}). Note that the onset of this non-uniformity occurs at $t \sim t_{sat}$.

Figure 2. Fluid motion within the condensate. Fluid motion was assessed by tracking green fluorescent beads (1 μm diameter) mixed with the bacterial cells (red-labeled). (**A**) Motion of beads in the condensate plane. Image shows the traces of individual beads tracked over 50 sec using particle tracking analysis (Materials and Methods). The dashed white circle indicates the condensate width (~ 550 μm). A typical trace is highlighted on the right, illustrating intermittent motion composed of periods of local random motion (gray symbols) and periods of directed motion, termed 'jets' (green symbols). The length (L) and average speed (v) of each jet were used to calculate $Pe = v \cdot L/D_{beads}$, with D = $5 \cdot 10^{-9}$ cm^2 s^{-1}. The cumulative distribution of this parameter is shown in the right plot for beads within or outside the condensate, clearly demonstrating enhanced motion within the condensate. (**B**) Comparison of the beads motion to proton diffusion, using D_{H+} = $5 \cdot 10^{-6}$ cm^2 s^{-1}. Beads traces (90 sec long) were analyzed. Plotted is the number of jets per bead whose Pe value exceeds a given threshold (Pe_0) during the diffusion time across the condensate $t_D \sim w^2/4D_{H+}$. (**C**) Time-averaged velocity field (90 sec) in the condensate plane, extracted using PIV (Materials and Methods). Profiles of the radial and tangential velocity components are shown on the right alongside the corresponding (normalized) cell density profile. The red arrow marks the condensate width (w) (**D**) The angular velocity profile, revealing correlated vortex-like motion. (**E**) Measured velocity field above the condensate showing a radially-inward flow. (**F**) Schematic summarizing the inferred fluid flow in the vicinity of the condensate (see also Supplementary Video 2).

Figure 3. Correlated swimming forces non-chemotactic cells out of the condensate. Cell-density profiles of chemotactic cells (red line) and non-chemotactic, smooth-swimming cells (green symbols) in a mature condensate. Profiles were normalized to the background density and divided by a factor of 3000 (red) and 1 (green). The chemotactic and non-chemotactic bacteria, labeled in red and green fluorescence, were initially mixed in a 100:1 ratio, respectively, and applied to the setup shown in Fig. 1B (Materials and Methods; 3 independent experiments).

Figure 4. Bacterial condensation in porous media. Experiments similar to those described in Fig. 1 were performed except that cell were suspended in a porous medium (0.08% agarose hydrogel) rather than liquid medium. **(A)** Representative mature condensates in porous (gray) or liquid (blue) media. Typical fluorescence image of the condensate in porous medium (scale bar 300 μm) and a schematic description of the revised setup are also shown. The layers dimensions are similar to those in Fig. 1, with 3 mm diameter. **(B)** The condensation dynamics (width versus time) in porous medium (left plot, black symbols). The saturation width value in liquid is marked with dashed blue line. *Inset* – The saturation width values in porous medium for 17 different experiments are plotted against the saturated peak cell density. The saturation width at low cell-density (ref. (18)) is marked with gray dashed lines. Gray region shows a linear fit to the data. **(C)** Fluid flow in the plane of a condensate in porous medium (analyzed by PIV; see Materials and Methods). The velocity field (right) and the radial and tangential velocities (left) were averaged over 30 s. **(D)** Expulsion of non-chemotactic cells from the condensate for experiments done in liquid (from Fig. 3) or porous media.

Figure 5. Condensation at still higher cell number. (A) The maximal cell density is plotted against the total number of cells in the condensate for experiments with the cells in liquid (red symbols) or porous medium (blue symbols). Notably, this maximal cell density falls at high cell numbers—controlled by the initial (uniform) cell density—due to formation of ring-shaped cell distribution, shown in (B) for cells in porous medium and (C) for liquid. **(B)** Evolution of the condensate profile in porous medium. A snapshot image at 50 min is also shown demonstrating the ring formation (scale bar – 150 μm). **(C)** A snapshot image of a mature condensate at high cell number in liquid. The bacterial time-averaged velocity fields (extracted using PIV) are overlaid on the image (red arrows), and demonstrated on the right (green arrows). The profile of time-averaged radial and tangential velocities is shown below the image, along with the cell density gradient; note that both velocities reverses across the ring. This reversal is also schematically described on the right.

Figure 6. Simplified model for condensate broadening by collective motion. (A) Measured condensate profiles of 3 independent experiments in liquid medium (markers) compared with numerical solutions of the Keller-Segel type model in phase 1 (right) and phase 2 (left). Dashed blue line represents the basic model ($\eta = 0$), which saturate only due to the limited sensory dynamic range of the cells. Expulsion force was modeled by adding drift velocity $\vec{U} = -\eta \vec{\nabla}(\rho/\rho_0)$ (black line; $\eta = 1.7 \cdot 10^{-7}$ cm^2 s^{-1}). Alternatively, following ref. 25, the chemotaxis efficiency was allowed to depend on the local cell-density (orange line). (B) Condensation dynamics. Condensate width plotted against t-t$_{sat}$ for 4 independent experiments (gray symbols) along with the simulated width of the different models (as labeled). To simulate the emergence of correlated motion above ρ_c, a sigmodal function was used $(1 + \exp(-(k/\rho_0)(\rho_{max} - \rho_c)))$ with $k = 3$ and $\rho_c = 25\rho_0$ (~$17 \cdot 10^6$ cells·mm^{-2}). (C) Expulsion of non-chemotactic cells (ρ_{NC}) by condensating wild-type cells (ρ_{WT}). Data from Fig. 3 of ρ_{NC} is replotted along with the distribution predicted by the model: $\rho_{NC} = \exp\left(-\frac{\eta}{D_{NC}} \frac{\rho_{WT}(r)}{\rho_0}\right)$ with D$_{NC}$ = 2.5·10^{-6} cm^{2}s^{-1}, η = 1.7·10^{-7} cm^{2}s^{-1} and $\rho_{WT}(r)$ taken from the experimental data in (A). (D) Summary of the saturated condensation (defined here as 1/W) as a function of the initial cell density. Data from various experiments is shown as empty circles and simulations are shown as lined (as labeled). The 'aerotaxis' line marks the density above which aerotaxis rings become dominant. The low-density limit (18) is plotted as a dashed gray line ('non-locality'). In the 'no condensation' region the initially-uniform cell distribution is stable (14, 36). See Text and Supp. Text for details.