Distinct System-Level Computations Underlie Perceptual Variation Across the Visual Field

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Abstract

Human visual perception for basic dimensions varies with eccentricity and polar angle, influencing daily activities such as reading, searching and scene perception. We investigated whether and how system-level computations that transform visual input into perception underlie these heterogeneities. Using the equivalent noise method and perceptual template model, we estimated gain, internal noise, and nonlinearity for orientation discrimination across eccentricity (fovea, parafovea and perifovea) and around polar angle. Participants discriminated the orientation of Gabors embedded in dynamic white noise and showed the expected variations across eccentricity and around polar angle. Importantly, visual performance declined with eccentricity due to decreased gain and nonlinearity and increased internal noise. Observers with stronger eccentricity effects showed greater gain decrease. Only gain varied with polar angle—higher along the horizontal than vertical meridian, and lower than upper vertical meridian—paralleling performance asymmetries. This dissociation aligns with known variations in neuronal count and tuning, suggesting that neural correlations and neural noise contribute to these system-level computations. By revealing distinct system-level computations underlying the eccentricity effect and polar angle asymmetries, our findings link perceptual heterogeneity across the visual field and neural architecture and provide insights into how the human brain encodes information under neural constraints.

Significance Statement

Human visual performance varies across eccentricity–distance from gaze–and around polar angle –circular dimension. Retinal factors and cortical surface area account for eccentricity, but only partially for polar angle variations. Here, we show that system-level computations—how signal are amplified and how noisy the system is—distinctly underlie these perceptual variations. Decline across eccentricity stems from both reduced gain and nonlinearity and elevated internal noise, whereas variation around polar angle arises solely from gain difference. This dissociation implies fundamental differences in information processing along two axes of the visual field. Our results provide a computational link between behavior and its neural bases and highlight the importance of considering both eccentricity and polar angle in modeling and understanding human perception.

Main Text

Introduction

Visual performance declines with eccentricity[1–3] and varies systematically around polar angle at isoeccentric locations. Performance is superior along the horizontal than vertical meridian— horizontal-vertical anisotropy (HVA)—and along the lower than upper vertical meridian—vertical meridian asymmetry (VMA) (**Fig. 1A**; review[3]). These polar angle asymmetries are ubiquitous across multiple visual functions, from early vision, such as contrast sensitivity (e.g[4–8]) and acuity (e.g[8,9]), to mid-level vision, such as texture segmentation[10] and crowding[11], and high-level vision, such as visual short-term memory[12] and face perception[13]. Their magnitude is equivalent to doubling[14,15] or tripling[7] eccentricity, and they persist under both binocular or monocular viewing[9,14]. These variations were amplified at more peripheral locations[7,14,16–18] increase at higher spatial frequencies[4,14,15], and remain robust even in the presence of attention[4,10,14,19,20]. Here, we investigate the computations by which the visual system gives that to this pervasive and resilient pattern of performance across the visual field.

Both the eccentricity effect and polar angle asymmetries are related to better optical quality[21], higher density of cones[22,23] and midget retinal ganglion cells[24,25] and larger surface area in primary visual cortex (V1) (eccentricity[26–31]; HVA/VMA[28–30,32]). Importantly, V1 surface area correlates with contrast sensitivity around polar angle[32], indicating a link between cortical anatomy and visual perception at the level of individual observer.

However, retinal and cortical factors are insufficient to account for polar angle asymmetries. An
encoding model simulating orientation discrimination based on spatial variations in both optical
and retinal factors explained only 10% of VMA and 40% of HVA performance[33,34]. Furthermore,
M-scaling the stimulus size as per a well-established cortical magnification factor eliminates
contrast sensitivity differences across eccentricity (e.g[7,35]), but not around polar angle[7].

Here, we investigated whether system-level computations reflecting the pooled activity of
neuronal populations activated by the stimulated visual field play a critical role. We examined
three computations that limit visual performance in a noisy environment: gain —the system's
ability to amplify the signal[36–38] (or modeled as efficiency[39]), nonlinearity—how the system
transforms inputs in a nonlinear fashion[40,41], and internal noise—the variability intrinsic to the
visual system, independent of external stimulation[40–42]. Both gain and nonlinearity are template
properties reflecting the system's ability to extract task-relevant information from stimuli. We used
the equivalent noise method to probe these system-level computations by introducing external
noise (e.g[40–45]) and infer the three computations by observing how performance changes (**Fig.**
1B). We constructed threshold-versus-noise curves at different locations to capture how
performance is jointly influenced by external noise and system-level computations.

The perceptual template model quantifies the three system-level computations (**Fig. 1C**). We
used a simplified version of the original model developed by Lu and Dosher (e.g[40,41,43]), which
retains its explanatory power. First, the noisy stimulus is filtered through a perceptual template
tuned to the signal's orientation and spatial frequency (SF). This step is scaled by the gain
parameter, such that better template-signal alignment yields higher gain. Then, the template-
matched output is passed through a nonlinear transformation, typically a power function. Next,
this transformed signal is corrupted by additive internal noise. Finally, a decision is made based
on the noisy signal.

These neural computations have been linked to neurophysiological properties. Higher gain
reflects stronger template alignment, which may depend on smaller receptive fields and sharper
SF tuning[46], thereby supporting higher sensitivity. Neurons have intrinsic variability due to factors
such as fluctuations in firing rate and membrane potential[47]. At the system level, internal noise is
shaped by neural correlations: when neural activity is more correlated among neurons, their noise
is less likely to cancel out through averaging, leading to greater internal noise at the system
level[48,49]. Nonlinearity is shaped by both retinal and cortical processes, including synaptic
rectification[50] and divisive normalization[51].

Each computation influences performance in distinct ways (**Fig. 1D**). When gain differs between
two locations, the system's ability to filter both signal and noise changes proportionally, resulting
in a vertical shift of the threshold-versus-noise curve without altering its shape. Differences in
internal noise impact performance the most at lower external noise levels, where internal noise
dominates. As external noise becomes more dominant, performance at higher external noise
becomes indistinguishable across locations. Finally, nonlinearity determines the curvature of the
function.

To investigate how these system-level computations shape visual field heterogeneity, we
assessed whether they vary throughout the visual field. Previous studies have shown that internal
noise increases across eccentricity[52–54]. Neuroimaging studies have shown that the size of
surface area decreases with eccentricity (e.g[26,27,31]). These studies averaged data around polar
angle; thus, it is unknown whether polar angle modulates these computations. Based on the
anatomical evidence that the decline of cone and retinal ganglion cell density[22–25] and cortical
surface area[28] across eccentricity is steeper along the vertical than horizontal meridian, as well as
behavioral findings that the eccentricity effect is more prominent along the vertical than horizontal
meridian (e.g[5,16,55,56]) and a robust HVA (e.g[6,8]), we hypothesize that the eccentricity effect as well

as the gain and internal noise underlying this effect will vary more along the vertical than
horizontal meridian.

It is unknown whether gain and internal noise also vary around polar angle. Anatomical and
neuroimaging measurements, including cone and retinal ganglion density[22,23], as well as V1
cortical surface area[28–32], population receptive field size[28,31], and BOLD signal amplitude[11,57],
contribute to the behavioral polar angle asymmetries[33,34]. Accordingly, both gain and internal
noise may vary around polar angle. However, magnifying stimulus size only reduced variation
around polar angle, suggesting that differences in V1 cortical surface area do not fully explain
polar angle asymmetries[7]. Here, we explored whether in addition to retinal and cortical
differences, polar angle asymmetries also reflect differences in gain and internal noise, or
whether the underlying computations differ from those underlying the eccentricity effect. We also
assessed nonlinearity across eccentricity and around polar angle, as it reflects how the visual
system amplifies or compresses neural responses and plays a critical role in shaping the
threshold-versus-noise curve.

Second, we examined whether variations in gain, internal noise, and nonlinearity across locations
contribute to performance heterogeneity. Specifically, we asked whether the magnitude of
variation in system-level computations—quantified by a location difference index—predicts
corresponding differences in performance. By quantifying the impact of each computation on
performance[54], this analysis provides further evidence that system-level computations play a
mechanistic role in shaping visual perception throughout the visual field.

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122   **Results**
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Observers performed an orientation discrimination task at nine visual field locations: fovea, four
cardinal meridians (left and right horizontal meridian and upper and lower vertical meridian) at 4º
and 8º eccentricity (**Fig. 2A**). The target signal was a tilted Gabor embedded in dynamic white
noise with a SF of either 4 or 6 cpd. We varied the contrast of Gabor and noise across trials to
map contrast threshold as a function of external noise, location and SF (**Fig. 2B**). We estimated
three parameters—gain, additive internal noise, and nonlinearity—by fitting the perceptual
template model to threshold-versus-noise curves at each location (**Fig. 2C**). Finally, we assessed
how each parameter varies across eccentricity and around polar angle, and contributes to
location differences of performance.

Visual field heterogeneities in the absence of external noise

We first verified the visual field heterogeneity—the eccentricity effect and polar angle
asymmetries—in absence of external noise and examined how SF modulated their magnitudes.
Fig. 3 shows threshold-versus-noise curves for each location group at 4 and 6 cpd. Only
thresholds estimated at 75% accuracy are shown, for illustration purposes. We focused on
thresholds estimated at external noise equal to 0, referred to as *performance*. We fit linear mixed-
effects models to performance and conducted Type III ANOVAs to examine interactions between
location (eccentricity/meridian/specific location) and SF (4 and 6 cpd) and their main effects
(Materials and Methods, equation (9)).

We observed an interaction between eccentricity and SF along both the horizontal meridian ($F_{(2,}$
$_{45.7)}$ = 7.277 [1.623, 9.959], p_{obs} = 0.002, $\eta^2_{partial}$ = 0.241 [0.067, 0.303]; **Fig. 3A**) and the vertical
meridian ($F_{(2, 45.7)}$ = 29.089 [10.615, 30.430], p_{obs} < 0.001, $\eta^2_{partial}$ = 0.560 [0.318, 0.570]; **Fig.**
3B). Post-hoc pairwise comparisons revealed that performance decreased with eccentricity along
both meridians and both SFs (all eccentricity pairs had p_{emp} < 0.001). This decrement was more

pronounced for 6 than 4 cpd and for vertical than horizontal meridian (averaged Cohen's *d*:
Vertical-6 cpd > Vertical-4 cpd > Horizontal-6 cpd > Horizontal-4 cpd). These results confirm the
well-established eccentricity effect, in which a decline in performance is more pronounced at
higher SFs and along the vertical than the horizontal meridian.

We then compared performance between the horizontal and vertical meridian (**Fig. 3C-a**) and
examined the modulation of eccentricity (4º and 8º) and SF (4 and 6 cpd) (Materials and
Methods, equation (10)). We found a three-way interaction among meridian, eccentricity and SF
($F(1,64.7) = 6.728$ [0.178, 10.399], $p_{obs} = 0.012$, $\eta^2_{partial} = 0.094$ [0.003, 0.139]). Post-hoc
analyses revealed that performance was higher at the horizontal than the vertical meridian for all
four SF x eccentricity combinations, confirming a HVA in performance. The largest HVA was
observed at 6 cpd x 8º eccentricity ($t(65.0) = 14.030$ [7.869, 14.100], $p_{emp} < 0.001$, Cohen's $d =$
17.702), followed by 4 cpd x 8º (4 cpd; $t(65.0) = 5.890$ [3.060, 7.730], $p_{emp} < 0.001$, Cohen's $d =$
8.122). The asymmetries at 4º eccentricity were smaller but still statistically significant for both 4
cpd ($t(65.0) = 3.010$ [1.410, 10.399], $p_{emp} < 0.001$, Cohen's $d = 5.907$) and 6 cpd ($t(65.0) = 5.090$
[3.060, 5.390], $p_{emp} < 0.001$, Cohen's $d = 5.225$). In sum, the performance HVA was robust and
stronger at further eccentricity and higher SF.

Along the vertical meridian (**Fig. 3D-a**), the three-way interaction (location x eccentricity x SF)
was not significant ($p_{obs} > 0.1$). Location interacted with eccentricity ($F(1,64.6) = 4.400$ [0.945,
9.634], $p_{obs} = 0.040$, $\eta^2_{partial} = 0.064$ [0.014, 0.130]) but not with SF ($p_{obs} > 0.1$), indicating that
performance variation along the vertical meridian was modulated by eccentricity, but not by SF.
Post-hoc analysis showed that performance was better at lower than upper vertical meridian at
both 4º ($t(65.0) = 1.300$ [0.139, 1.890], $p_{emp} = 0.044$, Cohen's $d = 2.258$) and 8º eccentricity
($t(65.0) = 4.270$ [2.469, 5.060], $p_{emp} < 0.001$, Cohen's $d = 5.806$), confirming a VMA in
performance.

Together, we observed robust eccentricity effects and polar angle asymmetries in performance.
Effects are more pronounced at the higher SF and farther eccentricities.

Gain, additive noise and nonlinearity vary throughout the visual field

To examine how computations underlie the observed visual field heterogeneity, we first assessed
whether and how each parameter varied throughout the visual field. We fitted linear mixed-effects
models (Materials and Methods, equation (11-12)) to each parameter and conducted Type III
ANOVAs to test interactions between locations and SF and their main effects. Matching between
a parameter's variation pattern with typical visual field performance patterns—eccentricity effect,
HVA and VMA—suggests that the corresponding computation underlies these visual field
heterogeneities.

Gain, additive noise and nonlinearity vary across eccentricity

When eccentricity increases from fovea to 4º, at 4 cpd the curve differs at lower external noise
levels but converges at higher levels (**Fig. 3A**), indicating increased internal noise at parafoveal
locations (**Fig. 1D**, *middle*). As eccentricity increases further to 8º eccentricity, performance
decreased across all levels of external noise, suggesting a reduction in gain at peripheral
locations (**Fig. 1D**, *left*). Based on these qualitative differences, we quantitatively compared gain
and internal noise across the visual field. For gain, along the horizontal meridian (**Fig. 4A**),
eccentricity interacted with SF ($F(2, 57.0) = 6.032$ [0.509, 9.016], $p_{obs} = 0.004$, $\eta^2_{partial} = 0.175$
[0.018, 0.264]). Post-hoc pairwise comparisons showed that for 6 cpd, 8º eccentricity had lower
gain than both fovea ($t(46.7) = 3.220$ [0.799, 3.830], $p_{emp} = 0.048$, Cohen's $d = 3.248$) and 4º
eccentricity ($t(46.7) = 4.680$ [1.430, 4.620], $p_{emp} = 0.036$, Cohen's $d = 4.400$); but for 4 cpd, gain

was similar across eccentricity. For additive internal noise (**Fig. 4B**), there was a main effect of
eccentricity ($F(2, 45.1) = 34.842$ [10.783, 38.066], $p_{obs} < 0.001$, $\eta^2_{partial} = 0.607$ [0.307, 0.623]):
fovea was lower than 4º ($t(46.3) = -5.310$ [-5.991, -2.350], $p_{emp} = 0.006$, Cohen's $d = -4.380$),
which in turn was lower than 8º eccentricity ($t(46.3) = -2.920$ [-3.540, -1.110], $p_{emp} < 0.001$,
Cohen's $d = -3.611$). Lastly, nonlinearity (**Fig. 4C**) also varied with eccentricity along the
horizontal meridian ($F(2, 46.6) = 11.916$ [1.653, 14.295], $p_{obs} < 0.001$, $\eta^2_{partial}= 0.338$ [0.065,
0.379]), being higher at the fovea than 8º eccentricity ($t(46.3) = 4.870$ [1.640, 5.221], $p_{emp} =$
0.006, Cohen's $d = 3.523$).

A similar pattern emerged at the vertical meridian (**Fig. 4D-F**). For gain, eccentricity interacted
with SF ($F(2, 57.0) = 11.098$ [0.657, 10.210], $p_{obs} < 0.001$, $\eta^2_{partial} = 0.280$ [0.028, 0.297]; **Fig.
4D)**. At 6 cpd, Gain was lowest at 8º eccentricity and lower than at 4º ($t(46.7) = 8.720$ [3.229,
8.011], $p_{emp} < 0.001$, Cohen's $d = 7.123$) and at the fovea ($t(46.7) = 9.870$ [3.449, 8.752], $p_{emp} <$
0.001, Cohen's $d = 8.542$). Moreover, at 4 cpd, gain was lower at 8º than 4º eccentricity ($t(46.7) =$
5.990 [1.339, 7.720], $p_{emp} = 0.024$, Cohen's $d = 3.418$). Additive noise increased with eccentricity
(**Fig. 4E**), ($F(2, 45.3) = 48.393$ [13.872, 46.819], $p_{obs} < 0.001$, $\eta^2_{partial} = 0.681$ [0.361, 0.673])
without interacting with SF ($p_{obs} > 0.1$). Additive noise was lower at the fovea than at 4º ($t(46.2) =$
-6.130 [-6.780, -2.569], $p_{emp} = 0.024$, Cohen's $d = -4.343$), which in turn was lower than at 8º
eccentricity ($t(46.2) = -3.590$ [-4.120, -1.000], $p_{emp} = 0.006$, Cohen's $d = -3.215$). Similarly,
nonlinearity varied across eccentricity ($F(2, 47.0) = 6.787$ [0.745, 11.888], $p_{obs} = 0.023$, $\eta^2_{partial} =$
0.224 [0.030, 0.337]; **Fig. 4F**), being higher at the fovea than 8º eccentricity ($t(46.4) = 3.600$
[0.930, 4.580], $p_{emp} = 0.024$, Cohen's $d = 2.883$). Overall, the effect size of gain, but not of internal
noise or nonlinearity, was higher along the vertical than the horizontal meridian, indicating a more
pronounced gain decline across eccentricity along the vertical meridian.

In sum, gain decreased with eccentricity from fovea to 8º, and more so from 4º to 8º—with this
effect being the most pronounced along the vertical meridian and for 6 cpd. Additive noise
increased with eccentricity, and nonlinearity was higher at fovea than 8º eccentricity, similarly
along both meridians.

Gain, but not internal noise or nonlinearity, varies around polar angle

We next assessed whether gain differed between horizontal and vertical meridian and whether
this was modulated by eccentricity and SF (**Fig. 5A**). There was no three-way interaction ($p_{obs} >$
0.1), but meridian interacted with eccentricity ($F(1, 56.9) = 13.960$ [1.503, 25.598], $p_{obs} < 0.001$,
$\eta^2_{partial} = 0.197$ [0.022, 0.290]; **Fig. 5A-a**) and SF ($F(1, 56.9) = 4.430$ [0.006, 8.976], $p_{obs} = 0.040$,
$\eta^2_{partial} = 0.072$ [0, 0.123] **Fig. 5A-b**). Post-hoc analyses showed that gain was higher at the
horizontal than the vertical meridian at 8º eccentricity ($t(65.5) = 6.130$ [1.870, 6.560], $p_{emp} <$
0.001, Cohen's $d = 4.297$) but not at 4º ($p_{emp} > 0.1$), consistent with the HVA pattern for
performance. Similarly, gain reflected the HVA pattern at 6 cpd ($t(65.5) = 5.370$ [1.560, 4.650],
$p_{emp} = 0.008$, Cohen's $d = 4.649$), but not at 4 cpd ($p_{emp} > 0.1$). In sum, gain showed a pattern
consistent with HVA, with stronger effects at greater eccentricities and higher SF. Neither additive
noise (**Fig. 5B**) nor nonlinearity (**Fig. 5C**) differed between horizontal and vertical meridian ($p_{obs} >$
0.1) at any eccentricity or SF. Note that the lower additive noise at 4º than 8º eccentricity (**Fig.
5B**) was already captured by the eccentricity difference (**Fig. 4B**). These findings suggest that
HVA arises specifically from variation in gain.

We next examined whether gain differed between the lower and upper vertical meridian (**Fig. 5D**).
Location interacted with SF ($F(1, 76.0) = 6.469$ [0.071, 12.967], $p_{obs} = 0.013$, $\eta^2_{partial} = 0.078$
[0.001, 0.165] **Fig. 5D-a**), and gain was higher at lower than upper vertical meridian at 4 cpd
($t(65.5) = 4.410$ [1.280, 5.580], $p_{emp} < 0.001$, Cohen's $d = 3.374$), but not at 6 cpd ($p_{emp} > 0.1$).

This result means that VMA for gain was stronger at 4 than 6 cpd. The lack of VMA at a higher
SF is because for some observers, gain at 6 cpd (particularly at 8° eccentricity) was near the floor
level (close to 1), limiting any differences. There was no three-way interaction or interaction
between location and eccentricity ($p_{obs} > 0.1$). Neither additive noise (**Fig. 5E**) nor nonlinearity
(**Fig. 5F**) differed between the upper and lower vertical meridian ($p_{obs} > 0.1$). Together, these
findings indicate that differences in gain, rather than in internal noise or nonlinearity, may underlie
VMA.

In sum, gain alone consistently varies around polar angle, indicating that it is related to both HVA
and VMA. These location-based effects are more pronounced at higher SFs. Distinct from the
eccentricity effect, additive noise and nonlinearity did not vary around polar angle.

Contribution: Gain, but not additive noise or nonlinearity, contributes to eccentricity effect

We examined the extent to which each system-level parameter—gain, additive internal noise, and
nonlinearity—contributed to visual field asymmetries. First, we identified the direction in which
each parameter modulated performance. Using linear mixed-effects models (Materials and
Methods, equation (13)), we assessed the relation between performance and each parameter
across seven locations in the visual field: the fovea, the horizontal meridian and the upper and
lower vertical meridians at both 4° and 8° eccentricities.

As shown in **Fig. 6A-C**, locations with higher performance were associated with higher gain
(slope = 0.090 [0.047, 0.130], $p_{emp} < 0.001$, conditional R-squared=0.75 [0.67, 0.80]; **Fig. 6A**) and
lower additive noise (slope = -0.029 [-.042, -0.008], $p_{emp} < 0.05$, conditional R-squared=0.77
[0.70, 0.81]; **Fig. 6B**). Nonlinearity showed no significant relation with performance (slope = -
0.019 [-0.043, 0.02], $p_{emp} = 0.082$, conditional R-squared = 0.79 [0.72, 0.82]; **Fig. 6C**). These
findings confirm our hypothesis that stronger gain and lower internal noise improve performance,
whereas nonlinearity has no effect.

The direction of each modulation informs the directionality of parameter contribution to location-
based performance differences: Parameters that enhance performance should vary across
locations in line with performance variation, whereas parameters that impair performance should
vary in the opposite direction. We examined whether and how these location differences of each
parameter are proportional to the heterogeneity in the expected direction (equation (14)).
Location variation was indexed by the difference between two locations divided by their sum,
providing a normalized measure. In **Fig. 6D,** we plot location difference indices for each
parameter against those for performance.

For gain, the only significant correlation was between the fovea and 8° along the horizontal
meridian (slope = 0.164 [0.020,0.412], $p_{emp,\ right-tailed} = 0.038$, conditional R-squared = 0.75 [0.48,
0.93], **Fig. 6D-a**). The effect was driven by the positive correlation at 6 cpd ($p_{emp,\ right-tailed} = 0.030$).
No correlations were observed for the other eccentricity pairs (**Fig. 6D-b and c)**, or for internal
noise and nonlinearity (all $p_{emp} > 0.1$, **Fig. 6D-e-i**), despite their variations across eccentricities.
These results suggest that gain, particularly at higher SF, is the primary factor underlying the
eccentricity effect along the horizontal meridian.

In contrast, no correlation with polar angle differences was significant ($ps_{emp}>.1$), meaning that
although gain varies around polar angle, it does not contribute to polar angle asymmetries as
much as to the eccentricity effect.

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Discussion

Using the equivalent noise method and perceptual template modeling, we mapped contrast sensitivity across the visual field and identified distinct computations that underlie performance variations across eccentricity –which have been examined primarily along the horizontal meridian or collapsed across polar angle (review[3])– and around polar angle. With increasing eccentricity, all three computations varied: gain and nonlinearity decreased, whereas internal noise increased. Gain variations across eccentricity were stronger along the vertical than horizontal meridian, consistent with visual performance (e.g[5,16,55,58]), and they were also stronger at higher SFs, in line with previous studies[5,59,60]. Moreover, gain predicted contrast sensitivity differences between fovea and 8⁰, indicating that gain is a key driver of the eccentricity effect. In contrast, around polar angle, neither internal noise nor nonlinearity varied, only gain did—being higher along the horizontal than the vertical meridian and at the lower than the upper vertical meridian—mirroring the HVA and VMA in performance. Together, these findings indicate that polar angle asymmetries arise from a distinct computational profile.

We found that the eccentricity effect and the HVA were more robust at 6 cpd than at 4 cpd. These findings are consistent with previous studies (eccentricity effect[5,59,60]; HVA[4,5,9,15,55]). A parallel pattern emerged for gain: the eccentricity effect and HVA were stronger at 6 cpd. This shared SF dependence reveals a qualitative link between performance and underlying computations, which likely reflect neural constraints: peripheral neurons prefer lower SFs in both humans[61,62] and non-human primates[46,63,64]. Higher SFs place greater demands on spatial resolution, taxing locations with lower resolving power and thereby amplifying performance differences across eccentricity— and potentially around polar angle as well. The distinctions in underlying computations for eccentricity effect and polar angle asymmetries are consistent with a recent study, which using reverse correlation and a noisy-observer model, showed higher sensitivity to signal orientation and SFs and lower internal noise at the fovea than the parafovea[54]. In contrast, only orientation sensitivity varies around polar angle, mirroring performance[65]. The gain —an overall measure of how much the signal is amplified (current study) — and featural representation —the sensitivity profile to different features[54,65]— provide complementary descriptions of how the system enhances relevant input. Moreover, internal noise estimates obtained using the perceptual template model in the current study, and those derived from a noisy-observer model [54,65], quantify the same system-level property and together offer a more complete account of internal variability across the visual field.

These distinctions in underlying computations may reflect the interplay of four neurophysiological factors: (1) the number of neurons co-activated by visual stimuli, (2) the tuning properties of individual neurons (e.g., sensitivity and selectivity for visual features), (3) the intrinsic neural noise of individual neurons (e.g., firing variability and dendritic noise[47]), which contributes to system-level internal noise, and (4) correlations in activity across neurons[48,49]. By linking behavioral results to model-derived system-level computations, our results provide inferences about how these neurophysiological properties vary throughout the visual field.

Across eccentricity, the decrease in gain is consistent with two neurophysiological factors: First, as eccentricity increases, the cortical surface area stimulated by a given visual input decreases (e.g[26–31]), and thus, assuming uniform cortical density[66], fewer neurons are recruited. Second, fewer neurons are tuned to high SFs at peripheral than central locations[46,61,63,64] and receptive fields become larger[67]. Pooling from fewer and less well-tuned neurons likely result in weaker signal amplification and thus lower gain.

Whereas gain was substantially reduced from the fovea to the perifovea, it did not differ between the fovea and the parafovea. This result may seem surprising given the known decline in spatial resolution with eccentricity, but it may reflect an interaction between broader neural tuning and increased neural correlation. The increase in neural correlation at the parafovea can be attributed to a lower proportion of orientation-selective neurons[68] and fewer parvocellular neurons[69], which

exhibit broader selectivity for SF[70], than in the fovea. Together, these factors would offset the
tuning advantage at the fovea, resulting in similar gain as at the parafovea. However, as
eccentricity increases towards the perifovea, tuning continues to decrease while correlations
remain high, resulting in a substantial drop in gain, consistent with our observations. The increase
in internal noise with eccentricity may reflect a tradeoff between neural noise and neural
correlation: The more correlated the neurons' activity, the less likely their noise is to average
out[48,49]. Although direct measurements of intrinsic noise across eccentricity are lacking, even if
the noise of single neurons remains constant, increased neural correlation from fovea to
periphery will result in greater system-level internal noise. This connection between higher neural
correlation and higher internal noise is supported by findings that attention is associated with both
lower neural correlations[71,72] and reduced internal noise (e.g[40]).

The present study also provides the first assessment of nonlinearity across eccentricity. Here,
nonlinearity —which reflects the system's sensitivity to amplified signals (modeled by the power
function in the perceptual template model)— exceeded 1 at all locations. Importantly, models
without a nonlinear component, including the linear amplifier model[42] and variants of perceptual
template models[40,43], failed to account for our data. These results underscore the need to
consider nonlinear computations to explain visual performance. Further research is needed to
determine whether this enhanced foveal nonlinearity shares neural mechanisms with the higher
gain and lower additive noise observed at central locations.

Around polar angle, only gain varied and reflected both the HVA and VMA. Higher gain at better-
performing locations may arise from greater cortical surface area[28–32,57,73]—implying more
neurons, smaller population receptive field sizes[28,31], and a preference for higher SFs[61,62,65]. This
observed gain variation constrains hypotheses about how neural correlations vary around polar
angle: robust gain variation around polar angle suggests that better-performing locations not only
have superior tuning but also exhibit weaker neural correlations.

This interpretation on neural correlation, in turn, informs the observed invariance in internal noise
around polar angle. As discussed in the eccentricity section, such invariance may reflect a
tradeoff between neural correlation and neural noise. Thus, better-performing locations with
weaker neural correlations —as suggested by our gain results—should have higher intrinsic
neural noise. Although it may seem counterintuitive that neurons at better-performing locations
could have higher neural noise, increased neural noise can be advantageous, e.g., it can facilitate
the detection of subthreshold signals[74]. Future studies should map both neural correlations and
neural noise across the visual field to characterize their interplay.

In sum, the observed gain variation across both eccentricity and polar angle likely results from an
interplay of three factors at better-performing locations: a greater number of neurons, preference
for higher SFs, and stronger neural correlations. In contrast, variation in internal noise across
eccentricity —and its invariance around polar angle— may be jointly influenced by neural
correlations and intrinsic neural noise, which our results suggest varying across the visual field.
The relative impact of these neural factors remains an empirical question. A perceptual template
model with population coding showed that neural correlations have a greater impact on
performance than mere amplification or sharpening of tuning functions[75].

Our findings may help explain why M-scaling eliminates eccentricity effects but not polar angle
asymmetries in contrast sensitivity[7]. While M-scaling normalizes the cortical surface area
stimulated, it may not equate other neurophysiological properties. For example, increasing
stimulus size and thus the number of neurons reduces neural correlation[48,76] and may diversify
tuning profiles, further lowering such correlations. This reduction in neural correlation in the
perifoveal region likely decreases system-level internal noise and therefore eliminates the
eccentricity effect. In contrast, because internal noise appears uniform around polar angle, polar

angle asymmetries—which are primarily driven by gain variations—may persist despite M-
scaling.

It has been proposed that asymmetries between the upper and lower hemifields may relate to
functional specialization, where the upper visual field primarily processes distant objects and the
lower visual field processes near objects[77]. Polar angle asymmetries in contrast sensitivity[4–8] and
acuity[8,9] decrease gradually with angular distance from the cardinal meridians, suggesting that
whereas the near-versus-far specialization contributes to meridional asymmetries, it cannot fully
account for the polar angle variations. We therefore hypothesize that gain-related polar angle
asymmetries progressively diminish along non-cardinal meridians and disappear along the
intercardinal meridians.

Previous studies have revealed ontogenetic and phylogenetic factors in these visual field
asymmetries. Ontogenetically, children show an HVA both behaviorally[78] and in cortical surface
area[31] but lack a behavioral[78] or cortical[31] VMA. The HVA progressively strengthens through
adolescence, whereas the VMA emerges and becomes as pronounced as that of adults in late
adolescence[79]. Phylogenetically, non-human primates show the typical HVA but an inverted VMA
in visual performance. Evolutionary differences in locomotion, navigation, and tool use, which
result in distinct visuomotor interactions at specific visual field locations, may contribute to
shaping the organization of the visual field[80].

In conclusion, by linking our novel behavioral data to underlying system-level computations, this
study provides insights into the neurophysiological architecture of the visual field and generates
novel, testable hypotheses. We found that visual field heterogeneities arise from distinct system-
level computations. The eccentricity effect is driven by a combination of reduced gain and
nonlinearity alongside increased additive noise, consistent with changes in cortical magnification
and receptive field properties. Polar angle asymmetries are associated with differences in gain,
but not in internal noise or nonlinearity. Together, these findings highlight a fundamental
distinction in how the visual system implements computations across eccentricity versus and
around polar angle, advancing our understanding of visual processing throughout the visual field.

409
Materials and Methods

Observers

Twelve observers (9 females; age mean=26.44; SD=3.24) participated in this experiment. All
observers except two authors (S.X. and Q.C.) were naïve to the study's purpose. All observers
had normal or corrected-to-normal vision and provided written informed consent. The
experimental methods complied with the Helsinki Declaration and were approved by the
Institutional Review Board for Human observers at New York University.

Apparatus

All experimental stimuli were generated using MATLAB 2020b (MathWorks) and the
Psychophysics Toolbox[81], and displayed on a gamma-calibrated CRT monitor (40 cm by 30 cm,
1,280 by 960 pixels, 100 Hz, 26 cd/m^{-2} background luminance). Each pixel extends 0.03 x 0.03
dva squared. The display was calibrated using a Photo Research (Chatsworth, CA) PR650
Spectracolorimeter to generate linear lookup tables for this experiment. The display resolution
was 32 pixels per degree of visual angle. An EyeLink 1000 eye-tracker was positioned in front of
observers to track gaze position. Observers were seated in a dark room with their head stabilized
using a chin rest 57 cm from the display monitor.

Stimuli

The stimulus presented in each trial consisted of a target, sandwiched between two streaks of
dynamic noise patches. The target was a Gabor patch—a sinusoidal grating modulated by a
Gaussian envelope—with luminance ( ) defined at each pixel position (and , relative to the
patch's center) (**Fig. 2A**, *inset*):

[Equation 1]

$$L(x, y) = C \cos(2\pi f(x' + \phi)) \exp\left(-\frac{x^2 + y^2}{2\sigma_{env}^2}\right)$$

$$x' = x \sin\theta + y \cos\theta$$

and range from -48 to 48 pixels (diameter=3 dva). represents linear contrast, either
sampled from a staircase procedure or picked at a fixed value (Procedure). denotes SF (0.125
or 0.1875 cycles per pixel, equivalent to 4 and 6 cpd). denotes orientation in radians, either
counterclockwise (/4) or clockwise (- /4) with equal probability on each trial. denotes the
phase which was randomized on each trial. specifies the Gaussian envelope size (=32
pixels, or 1 dva, one-third of the grating size).

The Gabor was embedded in dynamic noise, which were generated independently on each frame
by sampling pixels from a Gaussian distribution with standard deviation (   ) and centered at 0
(hence, the RMS contrast of the noise patch equals   ) (**Fig. 2A**, *inset*):

[Equation 2]

$$N_t(x, y) \sim \mathcal{N}(0, \sigma_{ext}^2)$$

On each trial,   could be one of nine possible values (0, 0.0275, 0.055, 0.0825, 0.11, 0.165,
0.22, 0.33, 0.44).

The possible stimulus locations were indicated by placeholder (**Fig. 2A**, *first display*): one at the
fovea, and four along the horizontal (Left: 0º; right: 180º) and vertical meridians (upper: 90º;
lower: 270º) at either 4° (parafovea) or 8° (perifovea) eccentricity. Each placeholder consisted of
four corners (line length=0.75°).

Procedure

Fig. 2A shows the trial sequence. Each trial began with all placeholders and a fixation dot
(radius=0.1º of visual angle) at the center of a gray background. A streak of dynamic white noise
was then presented at each location for a total duration of 630 ms. On each trial, a target Gabor
was presented for 30 ms at one of the possible locations, 300 ms after the onset of the dynamic
white noise, while other locations were only filled with noise. The streak of dynamic white noise
persisted for 300 ms following target offset. The target location was marked by a boldened
placeholder at the onset of the target Gabor, and until the observer's response, eliminating
location uncertainty.

Target location, orientation, and external noise levels were randomly selected on each trial. The
Gabor SF (4 or 6 cpd) was constant within each experimental session. Observers performed an
orientation discrimination task, pressing one of two keys to indicate whether the Gabor was tilted
counterclockwise or clockwise (±45º). Task difficulty varied with stimulus parameters—Gabor
visibility increased, hence tasks got easier, with higher contrast and lower noise standard
deviation . Observers received auditory feedback after making a response: a high pitch for
correct and a low pitch for incorrect responses. Their average accuracy was displayed at the end
of each block.

We collected data to estimate contrast thresholds in two steps. First, at each noise level and
location, we conducted a titration procedure using four interleaved staircases (two 1-up-2-down
and two 1-up-3-down) starting from different contrast levels, with 40 trials per staircase. Second,
based on Weibull fitting, we collected 30 to 40 additional trials at selected Gabor contrast levels—
both within the dynamic range and at anchoring levels. We interleaved external noise and
locations for all observers. Each observer completed 12,600 trials across approximately eight
one-hour sessions for each SF. Nine observers were tested with both 4 cpd and 6 cpd stimuli,
three were tested only at 6 cpd. They completed 25,200 trials in approximately 16 sessions.
Stimuli generation and response recording were conducted with MATLAB. Data analysis and
visualization were conducted in both MATLAB and R (R Core Team, 2024; RStudio
v2024.12.1+563).

Eye-tracking

We monitored the gaze position of the right eye in real-time during each trial using an SR
Research Eyelink 1000 Desktop Mount eye tracker at a sampling rate of 1000 Hz. Stimulus
presentation was contingent on maintaining central fixation from the onset until the offset of the
dynamic white noise. Trials were terminated and re-queued to the end of the block if observers'
gaze deviated more than 1.5º of visual angle from the fixation center.

Estimate contrast thresholds

For each noise level and location, we constructed psychometric functions by fitting a Weibull
function to trials tested at varying Gabor contrast and corresponding binary responses (**Fig. 2B**).
Trials collected through titration were binned into 10 bins based on percentile. Following titration,
we collected additional trials at 2 to 3 fixed signal contrast levels per noise condition. These
contrast levels were manually selected based on preliminary titration fits to improve the
robustness of the psychometric function fitting.

[Equation 3]

$$f(C) = \lambda + (1 - \lambda - \gamma)\left(1 - e^{-\left(\frac{C}{\alpha}\right)^{\beta}}\right)$$

denotes accuracy as a function of Gabor contrast for each bin. , , and represent the
function's threshold at 75% accuracy, steepness, lapse rate, and chance performance,
respectively. Model parameters were estimated using constrained nonlinear optimization via
MATLAB's fmincon() function. Parameter bounds were set as follows: thresh (\alpha) ranging
from 1% to 100%, steepness ( ) from 0.01 to 100, guess rate ( ) from 0.45 to 0.55, and lapse
rate (lambda) from 0 to 0.1, in 100 steps.

To balance the trade-off between trial count and fitting quality, we added "stabilizer" trials at low
contrast levels (50 trials each at 0.01% and 0.1% Gabor contrast, enforcing 50% accuracy). At
these low contrast levels, all observers were expected to perform at chance level, assuming no
bias in reporting leftward or rightward orientation. The stabilizer trials were used only for fitting
purposes and their trial counts were not included in the TvN fitting weights.

Perceptual template model characterizes TvN curves

505　For each observer, we fitted a simplified version of the perceptual template model[40,41] to contrast
506　thresholds (　) as a function of external noise levels (　) at a given performance level (　)
507　(**Fig. 2C**):

508　[Equation 4]

509
$$C_{\tau,d'}^{\text{pred}} = \left\{ \frac{d'^2 \left(\sigma_{\text{ext}}^{2\gamma} + \sigma_{\text{add}}^2 \right)}{\beta^{2\gamma}} \right\}^{\frac{1}{2\gamma}}$$

The model includes three key free parameters:　(gain), a scaling factor reflecting how well the
observer's template matches the signal;　(additive noise), the standard deviation of a
Gaussian noise component independent of the stimulus strength;　(nonlinearity), describing how
the template-matched output is amplified. Note that the original full model also included a
multiplicative noise parameter (　) which reflects how internal noise scales with signal
contrast[41]. By doing a model comparison we found that the reduced model excluding
multiplicative noise outperformed the full model (p < 0.05, Bonferroni-corrected) (see Model
Comparison below). Therefore, we proceeded with the more parsimonious three-parameter
model (**Fig. 2C**).

Model Comparison

520　We evaluated the need to include all four parameters for the perceptual template model by
521　conducting a nested model comparison between the full model and 15 reduced models, each
522　systematically excluding one or more parameters. The full model devised and tested by Lu and
523　Dosher is:

524　[Equation 5]

525
$$C_{\tau,d'}^{\text{pred}} = \left\{ \frac{d'^2 \left[\left(1 + N_{\text{mul}}^2 \right) \sigma_{\text{ext}}^{2\gamma} + \sigma_{\text{add}}^2 \right]}{\beta^{2\gamma} - N_{\text{mul}}^2 \beta^{2\gamma} d'^2 / 2} \right\}^{\frac{1}{2\gamma}}$$

When excluded from fitting, multiplicative (　) and additive (　) internal noise were fixed at 0,
and gain (　) and nonlinearity (　) were fixed at 1. We fitted each candidate model to the seven
locations we tested (fovea, horizontal meridian, upper and lower vertical meridian at 4º and 8º
eccentricity). We first excluded models that failed to account for the data (indicated by negative
R-squared), which occurred when gain and/or additive noise were omitted. For the remaining four
models that included both gain and additive noise, we quantified their goodness of fit by the
Bayesian Information Criterion (BIC):

[Equation 6]

$$\text{BIC} = n \log \left(\frac{\text{RSS}}{n} \right) + k \log(n)$$

RSS is the sum of squared residuals specified above,   is the number of data, and   is the
number of parameters. Lower BIC scores indicate better model fits while penalizing overfitting.
We fitted the full set of perceptual template models to each location group independently for each
observer, allowing all parameters to vary freely across locations within each location group. Delta
BIC was calculated by subtracting the minimum BIC score from each candidate model's BIC
score. Finally, we fitted linear mixed-effects models to delta BIC values to evaluate the fixed
effect of model type with random effects specified across observers:

[Equation 7]

$$\Delta \text{BIC}_{\text{nested}} = 1 + \text{Model}_{\text{nested}} + (1|\text{Subj})$$

The reduced model excluding multiplicative noise outperformed the full model ($p < 0.05$,
Bonferroni-corrected). Therefore, we proceeded with the more parsimonious three-parameter
model.

When fitting the perceptual template model, additive noise was calculated in log10 units because
they are in contrast units. Model fitting was implemented by MATLAB's fmincon() function, which
minimized the sum of squared residuals (RSS) between the measured and predicted thresholds.
Prior to squaring, residuals were calculated on log contrast values and weighted by the number of
trials per noise level (   ).

[Equation 8]

$$\text{RSS} = \sum_{N} \left(n_{N} \left(\log C_{N}^{\text{meas}} - \log C_{N}^{\text{pred}} \right) \right)^{2}$$

Parameter bounds were decided according to the literature[9,41]: multiplicative noise (   ) was
constrained between 0 to   ‾   (to ensure a positive denominator in equation (4)), additive
noise (   ) ranged from 10^-8 to 1 in log steps, gain ( ) was bounded between 0 to 5, and
nonlinearity ( ) ranged from 0 to 5.

To constrain model estimation[40,41], we obtained thresholds (   ) at three performance levels
=0.77, 1.05, 1.35, where   , corresponding to 65%, 70% and 75% accuracy ( ),
respectively. Only thresholds at 75% correct were shown as TvN functions (**Fig. 3**). This
approach was originally intended to constrain the model by ruling out substantial reductions in
internal multiplicative noise as a plausible mechanism of performance variation[43]. Although we
ultimately adopted a simpler version of the model that does not require this constraint anymore,
we retained the method for consistency with prior literature.

To examine visual field heterogeneity (eccentricity effect, HVA, and VMA), we grouped locations
according to the effect of interest (see Statistical Analysis-Location groups below), then fitted
perceptual template models to all locations within each location group.

Statistical Analysis

Location groups

At each noise level, we derived thresholds for eccentricity and meridian by combining data across locations. To represent the horizontal meridian at each eccentricity, we collapsed trials from the left and right locations and fit a single psychometric function. Thresholds for the vertical meridian were computed as the mean of the upper and lower vertical meridian. Thresholds for each eccentricity were computed as the means across the horizontal and vertical meridian.

We grouped visual field locations to systematically examine the eccentricity effect, HVA, and VMA. To assess the eccentricity effect, we compared thresholds at the fovea, 4º, and 8º along the horizontal and vertical meridians separately (i.e., three locations in each group), allowing us to examine whether the meridian modulates eccentricity-related changes. To evaluate polar angle asymmetries, we compared thresholds between the horizontal and vertical meridians (for HVA) and between the lower and upper vertical meridians (for VMA) at 4º and 8º eccentricities, with four locations included in each group. In addition, we defined four supplementary groups to isolate each asymmetry at individual eccentricities, enabling follow-up analyses when needed. Within each group, we fit the perceptual template model to thresholds across external noise levels to estimate the underlying system-level computations. Grouping was essential to isolate location-specific computations without conflating repeated measures. Some locations appeared in multiple groups (e.g., the fovea appeared in both eccentricity groups), leading to multiple parameter estimates per location. One-way ANOVAs confirmed that these estimates did not differ across groups (all ps > 0.1), and all were retained for further analysis.

Linear mixed-effects model

We used linear mixed-effects models for three sets of analyses: (1) verifying the eccentricity effect and polar angle asymmetries, (2) determining the optimal parameter configuration of the perceptual template model, and (3) analyzing the spatial pattern of computations. This approach was chosen for two reasons. First, linear mixed-effects models handle unbalanced datasets effectively, which was optimal given our mixed design: a between-observer factor (nine observers were tested at both 4 and 6 cpd, and an addition of three people were tested only at 6 cpd) and a within-observer factor (three thresholds were derived per location x noise per observer). Second, linear mixed-effects models account for random effects by including observer-specific intercepts, capturing individual variability across conditions.

All analyses were conducted in RStudio (v2024.12.1+563) using R. Linear mixed-effects models were fitted using the lmer() function from the lmerTest package, with maximum likelihood estimation and degrees of freedom calculated using the Satterthwaite approximation, which improves accuracy under unequal sample sizes and the inclusion of random effects. We used the anova() function to perform Type III ANOVA tests for assessing main effects and interactions, and the emmeans package for post-hoc comparisons with Bonferroni corrections. Model fit was evaluated using conditional R-squared values, which reflect both fixed and random effects.

Visual field heterogeneity for performance

Before examining the computations, we first verified that eccentricity effects and polar angle asymmetries were robust for contrast threshold in the absence of external noise, consistent with previous studies. We defined "performance" as the intercept threshold—the threshold measured without external noise— the standard metric in studies without external noise. To align with conventional performance definitions, where higher values indicate better performance, we took the absolute value of log-transformed thresholds. We assessed how performance varied across visual field locations within each location group and whether SF modulated these variations.

614   To verify eccentricity effects, we separately modeled performance within each location group
615   using linear mixed-effects models, with fixed effects for eccentricity, SF, and their interaction:

616   [Equation 9]

$$\text{Perf} = 1 + \text{Eccentricity} * \text{SF} + (1|\text{Subj})$$

618   To verify HVA and VMA, we fit separate linear mixed-effects models for each asymmetry. For
619   HVA, we tested the fixed effects of *meridian* (horizontal vs. Vertical meridian), eccentricity (4^0 and
620   8^0) and SF and their interactions. For VMA, we modeled the fixed effects of *location* (lower vs.
621   upper vertical meridian), eccentricity and SF, and interactions among these factors.

622   [Equation 10]

$$\text{Perf} = 1 + \text{Location} * \text{SF} * \text{Eccentricity} + (1|\text{Subj})$$

Variation and contribution

We investigated how these parameters underlie visual field heterogeneity throughout the visual
field (eccentricity effect, HVA, and VMA) by examining the variation and contribution of neural
computations.

First, to analyze how each computation varies across locations and how these variations interact
with SF, we fitted a linear mixed-effects model to each parameter. To assess variation across
eccentricity, similar to equation (6), the model assesses the interaction between eccentricity (4^0
and 8^0) and SF (4 and 6 cpd):

[Equation 11]

$$\text{Gain} = 1 + \text{Eccentricity} * \text{SF} + (1|\text{Subj})$$

634   To assess variation around polar angle, similar to equation (7), the model assesses the
635   interaction among location (meridian for HVA and location for VMA), SF and eccentricity:

636   [Equation 12]

$$\text{Gain} = 1 + \text{Location} * \text{SF} * \text{Eccentricity} + (1|\text{Subj})$$

638   Both models had random intercepts for observers. Regression slopes were constrained to be
639   constant, enabling assessment of overall trends.

640   Then, we examined how each parameter modulates performance. We analyzed the fixed effect of
641   each parameter. Using gain as an example:

642   [Equation 13]

$$\text{Perf} = 1 + \text{Gain} + (1|\text{Subj} * \text{SF})$$

This model includes a random intercept for each location- SF combination. Hence, any observed
fixed effect cannot be attributed to differences across locations or SFs. We chose not to include
random slopes because this analysis aims to estimate the overall fixed effect across locations
and SF. The model was fitted to the seven locations that cover the isoeccentric locations at the
tested eccentricity range.

After determining whether each parameter enhanced or impaired performance, we assessed the
independent contribution of each parameter to each performance heterogeneity. First, we
quantified the extent of asymmetry for both performance and parameters using a location
difference index (LDI)—the arithmetic difference between two locations divided by their sum. This
index provides a normalized measure of location variation. By design, the first of the two values in
the LDI calculation was always taken from the location with higher performance. For example,
when comparing the fovea and 8º, both the numerator and denominator of the LDI were
computed as the difference between fovea and 8º. We then fitted linear mixed-effects models to
LDI values of each parameter (e.g., gain) and that of performance, and the resulting fixed effects
indicate contribution of each parameter.

For gain and additive noise, we computed one-tailed empirical p-values (see Bootstrapping
section for definition) because the directionality of their contribution to performance heterogeneity
could be inferred from the directionality of their modulation on performance. Specifically, if better-
performing locations have higher gain, then gain is assumed to enhance performance. In this
case, both the performance LDI and gain LDI would be positive, and a stronger difference in
performance would correspond to a larger difference in gain—resulting in a positive correlation.
Conversely, if a parameter impairs performance (e.g., additive noise), a negative correlation
would be expected. If a parameter does not modulate performance (e.g., nonlinearity), we
evaluated the two-tailed empirical p-value.

[Equation 14]

$$\mathrm{LDI}_{\mathrm{Perf}} = 1 + \mathrm{LDI}_{\mathrm{Gain}} + (1|\mathrm{SF}) + (1|\mathrm{Subj})$$

Bootstrapping

To derive confidence intervals and assess statistical significance, we performed bootstrapping
beginning at the level of threshold estimation. In each iteration, we resampled trials with
replacement at each location and noise level separately. Psychometric functions were then fitted
to the resampled data to estimate contrast thresholds at each noise level. These thresholds were
subsequently fitted with the perceptual template model within each location group to estimate the
three model parameters. Finally, statistical analyses were performed across observers to assess
modulation, variation, and contribution effects. Both the resampling and the two-stage model
fitting were conducted independently for each observer. This procedure was repeated 1,000
times. We reported the observed statistics for all tests (F-values, t-values, effect sizes, slopes)
and p-values (p_{obs}) from the non-bootstrapped data, along with 95% confidence intervals
(excluding p-values) from the bootstrap distribution. For pairwise comparisons and correlation
analyses, empirical two-tailed p-values (p_{emp}) were computed as twice the smaller proportion of
bootstrapped differences (and slopes) greater or less than zero, and empirical Cohen's d was
computed as the median of the bootstrapped differences divided by the standard deviation of
those differences. For correlation analyses assessing contribution effects, the choice between
one-tailed and two-tailed empirical p-values depended on the parameter's modulation effect: if the
parameter significantly modulated performance in a specific direction, a one-tailed p-value was
used; otherwise, a two-tailed p-value was applied.

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Figures and Tables

Figure 1. Schematics of key concepts. **(A)** A schematic of visual field heterogeneity in
performance. The size of the dot indicates performance (bigger dots = better performance). From
left to right we illustrate the eccentricity effect (fovea is better than farther eccentricities),
horizontal-vertical anisotropy (HVA, the horizontal is better than the vertical meridian), and
vertical-meridian asymmetry (VMA, the lower is better than the upper vertical meridian). **(B)** The
equivalent noise method infers neural computations by mapping performance (e.g., contrast
threshold) as a function of external noise and observing how performance is altered by both
external (dark green) and internal (orange) noise. The performance decrease with higher external
noise levels is captured by the threshold-vs-noise (TvN) curve. **(C)** The Perceptual Template
Model (PTM) includes three system-level computations—gain, additive internal noise and
nonlinearity. A noisy stimulus is filtered by a perceptual template, and its contrast is scaled by a
gain parameter, transformed nonlinearly, and corrupted by internal noise before decision-making.
(D) Proposed computations influence performance in distinct ways. Differences in gain scale the
entire curve without altering its shape, reflecting proportional changes in how the system filters
both signal and noise; Changes in internal noise primarily affect thresholds at low external noise
levels, where internal variability dominates. As external noise increases, performance converges
across locations. Nonlinearity determines the curvature of the function: higher nonlinearity results
in a more curved (nonlinear) function.

A **Orientation discrimination task**

B **Map contrast thresholds**

C **Estimate system-level computations**

Figure 2. Stimulus, procedure, and model fitting. **(A)** Orientation discrimination task. Observers
saw a streak of dynamic white noise presented at nine locations (fovea, four polar angle at 4º and
8º eccentricity) both before and after seeing a Gabor signal presented at one location. They
reported whether the Gabor was tilted clockwise or counterclockwise and received feedback. The
signal location, noise contrast and signal contrast varied across trials. The Gabor SF varied
across sessions (4 and 6 cpd, counterbalanced). Eye fixation was enforced by an eye tracker. **(B)**
To derive contrast thresholds at each location and each noise level, we fitted a Weibull function to
accuracy as a function of Gabor contrast (binned into 10 bins) for each noise level (indicated by
lines of different shades) and estimated threshold (indicated by the dots of different shades at x-
axis). **(C)** We fitted the perceptual template model to the thresholds across external noise to
derive the three computations: gain, additive internal noise and nonlinearity. The solid dots
indicate the threshold estimated in **(B)**.
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Figure 3. Threshold-vs-noise curves and performance throughout the visual field. Each panel
plots thresh-vs-noise curve for each location group to visualize one of the three visual field
heterogeneities: eccentricity effect along the horizontal **(A)** and vertical meridian **(B)**, HVA **(C)** and
VMA **(D)**. Dots and error bars represent group-averaged contrast thresholds (±1 SEM) across
nine levels of external noise. Many error bars are smaller than the symbols. Shaded bands are
PTM model predictions (±1 SEM). Colors denote visual field locations, indicated by icons in each
panel, and corresponding R^2 values for PTM fitting are shown alongside. Dot shapes indicate
SF (circles=4 cpd, triangles=6 cpd), plotted separately in the left and right panels within each
dashed cell. **(A, B)** Threshold-vs-noise curves at the fovea, and at 4º and 8º eccentricity along the
horizontal **(A)** and vertical **(B)** meridian. To examine eccentricity effects, we compared
performance—defined as the absolute value of the log contrast threshold at zero external noise—
between each pair of eccentricities (fovea vs. 4º, fovea vs. 8º, and 4º vs. 8º). Vertical comparison
lines indicate the pairs tested; asterisks denote Bonferroni-corrected *p*-values (***p < .001, **p <
.01, *p < .05, ns, *p*>.1). **(C)** Threshold-vs-noise curves at the horizontal and vertical meridians at
both 4º and 8º eccentricity. Subpanel (a) plots performance as a function of meridian ×
eccentricity, separately for 4 and 6 cpd, illustrating how both eccentricity and SF modulate the
HVA. Group means (±1 SEM) are plotted as colored dots; individual subjects' performance
(median of 1,000 bootstraps) is shown in grey lines. We focused on comparisons between
horizontal and vertical meridian, indicated by horizontal comparison lines. Asterisks denote
significance levels from post-hoc pairwise tests. **(D)** Threshold-vs-noise curves at the lower and
upper vertical meridians at 4º and 8º eccentricity. Subpanel **(a)** shows performance collapsed
across SF as a function of meridian × eccentricity, revealing eccentricity-dependent modulation of
the VMA. Formatting follows that of **(C)**.

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Figure 4. Gain, additive noise and nonlinearity vary across eccentricity. Each panel shows group
means (±1 SEM) of estimated model parameters—gain **(A, D)**, additive noise **(B, E)**, and
nonlinearity **(C, F)**—as a function of eccentricity along the horizontal (top row) and vertical
(bottom row) meridian. Grey lines represent individual subject data (median of 1,000 bootstraps).
Asterisks above horizontal comparison lines indicate Bonferroni-corrected post-hoc significance
levels (***p < .001, *p < .05, ns p > .1). Parameters that showed a significant interaction between
eccentricity and SF (e.g., gain in panels **A** and **D**) are plotted separately for 4 and 6 cpd.
Parameters showing only a main effect of eccentricity without such interaction are collapsed
across SFs (additive noise in panels B and E, and nonlinearity in panels **C** and **F**).

Figure 5. Gain **(A and D)**, but not internal noise **(B and E)** or nonlinearity **(C and F)**, varies
around polar angle. We plot estimated parameters as a function of location × eccentricity pairs,
separately for 4 and 6 cpd. To highlight post hoc comparisons from significant two-way
interactions for gain **(A and D)**, we collapsed across SF to illustrate the modulation effect by
eccentricity (panels **A-a** and **B-a**), given a significant meridian/location × eccentricity interaction.
Similarly, we collapsed across eccentricity to illustrate the modulation effect by SF (panels **A-b**
and **B-b**), given a significant meridian/location × SF interaction. Figure format follows that of **Fig.**
4.

Figure 6. Gain contributes to performance differences between the fovea and 8⁰ eccentricity. **(A-C)** Each panel shows estimated gain **(A)**, additive internal noise **(B)**, and nonlinearity **(C)** as a function of performance across locations and SFs. Each data point represents an individual location × SF combination (color-coded by location, shape-coded by SF). Colored regression lines show predictions from linear mixed-effects models. Medians of bootstrapped slopes and empirical *p*-values (p_{emp}) are reported in the figure. Performance improves with increasing gain **(A)** and decreasing internal noise **(B)**, while nonlinearity shows no relationship with performance **(C)**. **(D)** Quantify the contribution of each computation. Each panel plots the location difference index (LDI) of a parameter against the LDI of performance. Shapes denote individual observer data at 4 cpd (circles) and 6 cpd (triangles). Regression lines reflect linear mixed-effects model predictions for each SF. Median of bootstrapped regression slopes and empirical one-tailed *p*-values are shown in each panel. Subpanels **(a-c)** show gain results across three eccentricity pairs (fovea vs. 8⁰, fovea vs. 4⁰ and 4⁰ vs. 8⁰) along the horizontal meridian. A significant positive correlation appears only for the fovea vs. 8⁰ pair **(D-a)**, especially at 6 cpd, indicating that gain differences contribute to the eccentricity effect. Subpanels **(d-f)** show additive internal noise, which shows no significant correlations with performance for any eccentricity pair. Subpanels **(g-i)** shows nonlinearity, which similarly shows no significant correlation with performance across eccentricity pairs.