Sequence-to-graph alignment based copy number calling using a network flow formulation

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Abstract. Variation of sequence copy number (CN) between individuals can be associated with phenotypical differences. Consequently, CN calling is an important step for disease association and identification, as well as for genome assembly validation. Traditionally, CN calling is done by mapping sequencing reads to a linear reference genome and estimating the CN from the observed read depth. This approach, however, is significantly hampered by sequences and rearrangements not present in a linear reference genome; at the same time simple CN prediction for individual graph nodes does not make use of the graph topology and can lead to inconsistent results. To address these issues, we propose Floco, a method for CN calling with respect to a genome graph using a network flow formulation. Given a graph and alignments against that graph, we calculate raw CN probabilities for every graph node based on the Negative Binomial distribution and the base pair coverage across the node, and then use integer linear programming to compute the CN flow through the whole graph. We tested this approach on 15 aligned datasets, involving three different graphs, as well as HiFi and ONT sequencing reads and linear assemblies split into reads. These results demonstrate that the addition of the network flow formulation increases the accuracy of CN predictions by up to 43% when compared with read depth based estimation alone. Additionally, we observed that concordance between predictions from the three different sequence sources was able to reach 93.2%. Floco fills a gap in CN calling tools specifically designed for genome graphs.

Introduction

Genome sequences often contain copy number (CN) variable segments. This variation can produce impacting differences in terms of molecular behavior, which can ultimately be associated with phenotypical differences [1–4]. For example, CN changes at the *STRC* locus are known to cause hearing loss in humans [2] and a duplication of two exons in the *Dock2* gene have been associated with striking immune phenotypes in mice [4]. Variation in CN can be observed either within the same sequence or haplotype, or alternatively between sequences or haplotypes. Consequently, CN calling is an important step for disease association and identification, as well as in population genetics. It also appears as a task in genome assembly workflows to determine how often each node in an assembly graph is present in the underlying genome.

Traditionally, CN calling is done by mapping sequencing reads to a linear reference and then estimating the CN in the sequenced sample either from the observed read depth [5–7], by using information from paired-ends and split-read alignments [8, 9], or by combining both approaches [10]. Although these approaches work well within their context, there are inherent problems with using a single linear reference, the biggest of them being the bias against sequences and genomic rearrangements not represented in the linear reference. Moreover, any single reference genome is bound to include numerous unreliable paralogous sequence variants (PSVs)—polymorphic positions where repeat copies differ in the reference genome, but not necessarily in the examined individual, leading to biased read mapping and subsequent CN estimation [11, 12].

In recent years, hundreds of high quality diploid human whole genome assemblies became available, giving rise to several pangenome references [13–16]. Pangenomes reduce the reference bias by using a larger and more diverse set of sequences as reference, increasing the representativity. CN calling can then be done on a bigger set of sequences by using graphs, one of the most common data structures for representing pangenomes, together with sequence-to-graph alignments of sequencing reads. Graphs contain more sequences, some of them completely missing in the linear reference, which then become available for CN estimation. Additionally, graphs also contain non-reference edges between sequences that are not observed next to each other in a linear reference, allowing for a more sensitive read placement, and correspondingly more sensitive CN analysis. The usage of graphs does not change the fundamental reasoning, which is the same as for coverage-based approaches on linear references, where the observed read depth is used to estimate CN, but in this case for each of the graph nodes.

However, using a graph also raises new challenges, in this particular case, the CN consistency across the graph is not guaranteed. That is, CN values are only consistent across the graph if the individual nodes' CN can be translated into walks through the graph. Several factors can cause erroneous coverage values, including sequencing errors, misalignments and misassemblies, which in turn will negatively impact the coverage-based CN assignments and potentially make them inconsistent across the graph.

To address this problem, we propose Floco, a method for CN calling with respect to a graph (pan)genome using a network flow formulation. Medvedev and Brudno [17] proposed a method to model DNA double strandedness in the context of genome assembly. They developed a framework that, given a set of sequencing reads, builds a bidirected overlap graph from those reads, and estimates read copy counts using a convex min-cost flow formulation. Here, we also use a similar flow-based formulation that, in our case, models node coverages resulting from sequence-to-graph alignments with a negative binomial distribution. In this way, CN assignments are made more consistent throughout the graph compared to estimating CN individually for each node, overcoming incorrect assignments originating from coverage-related noise.

Method

Overview. Floco calls individual node CN on genome graphs. As input, it takes a graph (in GFA format) and alignments (in GAF format) against the same graph (Fig. 1a). It then computes the individual base

pair coverage for every node and uses them to calculate node CN probabilities (Fig. 1b). The CN probabilities are then provided to our network flow formulation (Fig. 1c), together with some other constraints (Fig. 1d), which we then solve using Integer Linear Programming (ILP). With this method, Floco is able to correct wrong CN assignments made exclusively from coverage-based information (Fig. 1e).

Figure 1. Method overview. a, Genome graph and reads aligned against the graph. Reads are aligned to multiple nodes and are shown with different colors. **b**, Table with log CN probabilities per node based on the observed read depth. **c**, Flow network definition and estimated CN. Each connected pair of nodes are linked by two opposite-directed edges. In addition, each node end has one incoming edge from the supersource (denoted by *s*, edge in blue) and one outgoing edge to the supersink (denoted by *t*, edge in red). **d**, Individual node constraints for the flow network: incoming flow on one node end equals to the outgoing flow on the opposite node end; and the sum of incoming/outgoing flow equals to the CN of the node. **e**, strangepg [18] visualization of the CN predictions on a subgraph before and after applying the flow network. On the left side, CN predictions are inconsistent, with an interruption in the path at the bottom of the panel, where all nodes have CN=0 (orange); as well as two diploid nodes (light blue), located in the middle of the image. On the right side, a consistent walk through the graph can be achieved by using nodes with CN=1 (purple).

Network flow solved with Integer Linear Programming. In order to get our final CN estimations for each node, we use a network flow formulation solved using Integer Linear Programming (ILP) [19]. Minimum cost flow [20] through a graph is a well known problem in computer science. Such flow can be found using a system of linear equations, where f_{uv} represents flow between nodes u and v, both belonging to a set of nodes V and connected by an edge e from a set of edges E. The incoming flow through one side of the node v equals to the outgoing flow through the opposite side: $\sum_{e \in E_{vL}^-} f_e = \sum_{e \in E_{vR}^+} f_e$, where E_{vL}^- and E_{vR}^+ are the sets of edges entering the node v from the left and leaving it from the right, respectively (Fig. 1d). Flow through each edge e is linearly penalized through costs ξ_e. With additional constraints on the node/edge capacity, as well as on the total required flow, the problem is then defined as the minimization of the total cost of the flow from a source s to a sink t: $\sum_{e \in E} f_e \cdot \xi_e \rightarrow \min$.

With regards to the CN flow, we adapt the minimum cost flow formulation into a maximum probability flow on a bidirected graph, where each edge e has integer flow f_e and each node v has associated probabilities p_{vc} (Equation 2) as well as a range of possible CNs C_v. CN is encoded with a non-negative

integer variable x_v that is connected to CN probabilities via a piecewise linear (PWL) function $g(x_v; p_v)$, where $g(x_v = c; p_v)$ is set to $\log p_{vc}$. We also extend the concept of source and sink to a supersource s and a supersink t, each of them connected to both ends of every node $v \in V$ through a directed edge, with s and t having only outgoing and incoming edges, respectively. The usage of such edges is subject to a "cheap" cost if the node has no other edges connected to the same node end (-25 by default); or "expensive" cost otherwise (-10^5 by default). Corresponding values are stored in the edge costs ξ_e.

Table 1. Table of notation.

Notation	Description
$v, u \in V$	Graph nodes
$i, j \in \{L, R\}$	Left and right node end
$e \in E$	Graph edges, $e = (u, i, v, j)$
E_{vi}^-, E_{vi}^+	Incoming/outgoing edges from (v, i)
f_e	Flow through edge e
ξ_e	Cost of traversing the edge e
s and t	Supersource and supersink
$b \in B_v$	Bins for the node v
m	Bin size
k_v	Node v coverage
C_v	Possible copy numbers at node v
p_{vc}	Probability of CN c at node v
x_v	Integer variable for node v CN
$g(x; p)$	PWL function, connecting x_v and p_{vc}
d_e	Number of reads covering edge e
l_e	Overlap size of the edge e

In addition, we apply a cost on the usage of edges supported by few reads. Specifically, we examine the number of reads d_e supporting the edge e, i.e., the number of reads consecutively passing both of the edge nodes; and compare d with the expected number of reads $E[d_e]$ given the edge length l_e (size of the overlap between the two nodes). We have observed that read length values follow a skew normal distribution (SN) [21] (Suppl. Fig. 1), and calculated $E[d_e]$ as $S_{\text{SN}}(l_e) \cdot \mu_1$, where $S(l)$ is the SN survival function of the edge length (expected number of reads longer than l_e) and μ_1 is the expected read depth for nodes of length 1, defined later. Edge e remains free whenever $d_e \geq E[d_e]/4$, otherwise we set edge cost ξ_e to the "cheap" superedge penalty. In summary, CN flow is formulated as the following maximization problem:

$$
\begin{aligned}
\text{Maximize} \quad & \sum_{v \in V} g(x_v; p_v) + \sum_{e \in E} f_e \cdot \xi_e, \\
\text{Subject to} \quad & x_v = \sum_{e \in E_{vL}^- \cup E_{vR}^-} f_e \qquad \forall v \in V, \\
& \sum_{e \in E_{vL}^-} f_e = \sum_{e \in E_{vR}^+} f_e \quad \text{and} \quad \sum_{e \in E_{vR}^-} f_e = \sum_{e \in E_{vL}^+} f_e \qquad \forall v \in V, \\
& x_v \in \mathbb{Z}_{\geq 0}, \quad f_e \in \mathbb{Z}_{\geq 0}.
\end{aligned}
\tag{1}
$$

Finally, Floco employs Gurobi ILP solver [22] to find the most likely set of CNs x.

Node coverage computation and background read depth. As nodes in the overlap graphs contain redundant sequence, which could influence observation independence, Floco first clips nodes in a procedure similar, but less strict than graph bluntification [23] (see Suppl. Methods). We then define node coverage as the sum read depth across all retained positions in the node, obtained by summing up alignment sizes between reads and clipped nodes for all primary alignments in the input GAF file. Fully clipped nodes are not considered for the coverage computation, and their CN is estimated purely based on the flow. In addition, we split all nodes longer than m (100 bp by default) into bins of that size. Bin coverages are defined and calculated analogous to the node coverages.

In previous studies, negative binomial (NB) has been used to model the total number of reads overlapping a single genomic position or a fixed-size bin [11, 24]. In contrast, we defined coverage as the sum read depth over all base pairs in a given node or bin as it provides a better ability to capture reads, stopping or starting within a node/bin, as well as allows for variable length nodes shorter than the bin

size m. Nevertheless, we empirically observed that node/bin coverage can also be explained by the NB distribution (Suppl. Fig. 2a). This way, when bin coverage for nodes with CN=1 follows $NB(r, q)$, bin coverage at CN=c follows $NB(cr, q)$ due to the additive characteristics of the NB distribution. At CN=0 a node should not be covered by any reads, nevertheless, non-zero coverage can be observed due to read alignment errors. We model that using discretized exponential distribution as it has a lower tail than NB distribution with small r. To connect NB and exponential parameters, we set exponential mean to $\varepsilon \cdot \text{mean(NB)}$, resulting in $\lambda = \frac{q}{\varepsilon r(1-q)}$, where ε represents putative read aligner error rate (default: 0.02).

To estimate NB parameters, we examine bin coverage across nodes with at least 10 bins as longer nodes are expected to have better read alignments. Next, we discard outliers as well as potentially uncovered nodes by first removing nodes where all bin coverages are under m (effectively, no single read passes through the whole bin) and then removing the top and bottom 3% of the nodes based on their mean bin coverage. After node filtering we estimate coverage parameters using the maximum likelihood method by numerically optimizing the total log-likelihood of the retained bin coverages under a weighted mixture of distributions for CNs from 0 to $c_{\max} = \max\{3, c_{\text{def}} + 1\}$, where c_{def} is the expected CN for most nodes in the graph. Floco automatically tests several possible values of c_{def} (default: 1 and 2) and selects the one that produces the highest log-likelihood. In addition, we allow users to manually set c_{def} due to the fact that in certain cases a graph consisting of mostly CN=1 nodes is almost indistinguishable from a graph containing mostly CN=2 nodes. Optimization is performed using the bounded Nelder-Mead method [25, 26] on the following variables: CN=1 distribution mean and variance; and ratios of node CNs. For better conversion, CN ratios are normalized to sum to one during the likelihood calculation instead of numerical optimization using one less ratio variable.

Node coverage probabilities. Computed background read depth distribution with mean $\hat{\mu}$ and standard deviation $\hat{\sigma}$ describes a coverage for a bin of size m and CN=1. To extend this definition to variable size nodes, we empirically observed that the distribution of mean and standard deviation proportionally depend on the bin size: $\mu_{m'} = \frac{m'\hat{\mu}}{m}$ and $\sigma_{m'} = \frac{m'\hat{\sigma}}{m}$ (Suppl. Fig. 2b). This allows us to define read depth distribution $NB(r_v, q_v)$ for any node v with CN=1 using NB method of moments. As above, we define probability of observing read coverage k_v at CN $c > 0$ as $P(k_v \mid c_v{=}c) = P_{NB}(k_v; cr_v, q_v)$ and use the exponential distribution for CN=0. To improve predictive power of large nodes and preserve independence of observations, we randomly subsample node bins so that on average each read appears in exactly one bin (rate = m / mean read length). Whenever less than two bins remain per node, we use node coverage for calculating CN probabilities, otherwise we redefine coverage probability as the product of all bin coverage probabilities: $P(k_v \mid c) = \prod_{b \in B_v} P(k_b \mid c)$, where B_v is the set of retained node bins.

Afterwards, we use Bayes' theorem with equal priors to define bin or node CN probabilities based on the observed coverage k_v:

$$p_{vc} = P(c \mid k_v) = \frac{P(k_v \mid c_v = c)}{\prod_{c' \in C_v} P(k_v \mid c_v = c')}. \tag{2}$$

To define the set of possible CNs C_v for node v we start from normalized and rounded coverage $\left\lceil \frac{k_v}{\mu_v} \right\rfloor$ and extend the set to the left and right until log-difference between best and current probability $\log P(k_v \mid c_{\text{best}}) - \log P(k_v \mid c)$ does not get too large (over 4 expensive superedges).

Results

To evaluate Floco and demonstrate its utility, we focus on two applications: The first application is *assembly graphs quality control (QC)*, where we align reads from a sample against its own assembly graph. In this case, we expect all nodes to have CN>0, given they were derived from reads from that same sample, while nodes with CN=0 indicate errors. CN calling on assembly graphs also has applications for phasing workflows [27, 28], but here we restrict our attention to QC.

The second application is *CN calling using a pangenome reference*, where we align reads to a pangenome graph. When aligning reads from a sample that was used during graph construction (in-sample), the expected outcome is that all nodes originated from that sequence are covered and all others are not. When aligning a sample that was not included in graph construction (out-of-sample), we expect this sample to carry segments with CN not observed by samples in the pangenome reference, which would result in nodes with CN=0 or CN>2.

In our evaluations, we contrast the CN assignment *before* and *after* using the network flow. That is, *before flow* corresponds to using the same negative binomial formulation to assign a maximum likelihood CN to each node separately without considering the graph connectivity, where *after flow* corresponds to the full Floco approach.

Data description. We used three graphs for evaluation (Suppl. Table 1): For the assembly QC use case, we used two Verkko [28] assembly graphs, one from a diploid human HG01114 [16] (4k nodes and 3.4k edges) and the other one from a tetraploid potato [29] (20k nodes and 27k edges). For the pangenome use case, we used the minigraph [30] pangenome graph from the Human Pangenome Reference Consortium (HPRC) [15], which contains 90 haplotypes, being the most fragmented of the graphs (671k nodes and 965k edges).

Table 2. Sample–graph pairs used for Floco evaluation. First column shows the sample–graph pair, where the graph is abbreviated as either 'pang' (HPRC pangenome) or 'asm' (assembly graph). The last column ("in-sample") defines whether the sample was used for the graph construction.

Pair	Species	Graph	In-sample
CHM13-pang	*Homo sapiens*	HPRC	Yes
HG01258-pang	*Homo sapiens*	HPRC	Yes
HG01114-pang	*Homo sapiens*	HPRC	No
HG01114-asm	*Homo sapiens*	HG01114	Yes
Altus-asm	*Solanum tuberosum*	Altus	Yes

Furthermore, we used the following sequencing and synthetic data (Suppl. Table 2), aligned to the graphs using GraphAligner [31] (Suppl. Methods). First, we aligned HG01114 and Altus sequencing data to the corresponding assembly graphs. Next, we aligned three samples to the HPRC pangenome graph: haploid CHM13, which was used as the graph's backbone sequence; HG01258, which was added to the graph during its construction (in-sample); and HG01114, which is not present in the graph (out-of-sample). We use suffixes 'asm' (assembly graph) and 'pang' (HPRC pangenome) to indicate which graph was used. This way, we consider five sample–graph pairs: HG01114-asm, Altus-asm, CHM13-pang, HG01258-pang, and HG01114-pang (Table 2). For each sample we used PacBio High Fidelity (HiFi) and Oxford Nanopore (ONT) reads, as well as their own linear assemblies, "chopped" into groups of fixed-size reads (see Suppl. Methods).

Floco accurately calls copy number for CHM13. CHM13 was used as a backbone when constructing the HPRC graph [15] and mapping CHM13 reads to the HPRC graph (CHM13-pang) hence constitutes an in-sample setting. For the ground truth CN set, we defined all nodes belonging to CHM13 (identified by the SN tag in the rGFA file) as having CN=1 (314k nodes), whereas all other nodes were assigned CN=0 (357k nodes). We then compared the CN predictions from the CHM13-pang chopped assembly, HiFi and ONT alignments against the ground truth, both before and after applying the network flow. Additionally, we evaluated the effect of read depth on CN prediction accuracy by downsampling sequencing data to coverages from 1× to 30×.

First, we observed that Floco achieved almost perfect accuracy on the chopped assembly (Fig. 2, Suppl. Fig. 3), accurately predicting CNs for 99.7% (99.6% before flow) of the nodes, and achieving

Figure 2. Copy number calling accuracy for the CHM13 sequencing data and HPRC pangenome graph.
Each subpanel shows prediction evaluation before and after CN flow, calculated for the PacBio HiFi (blue),
Oxford Nanopore (red) and the chopped assembly (yellow) datasets, subsampled to coverages between 1 and
30 (shown with different transparency levels). Left and right groups of panels show values calculated based on
the number of nodes and the sequence length, respectively. Accuracy is either measured directly (fraction of
nodes/sequence length matching with the CHM13 path in the graph); or through corresponding precision and
recall. Y-axis is clipped at the bottom at 0.35 for accuracy and recall and at 0.85 for precision.

perfect precision (error $<4 \cdot 10^{-5}$). When translated into the sum of node lengths, around 1.9% of the
total sequence was predicted to have CN=0 instead of CN=1, driven primarily by the missing read
alignments. Even then, using the network flow allowed to correctly predict CNs for additional 619 Mb
compared to CN predictions before the flow. So while a limited amount of residual errors remain, this
demonstrates that Floco effectively leverage the graph topology to derive CN assignments.

At 30× coverage, Floco accurately predicted CNs for 98.1% of the total sequence for both the ONT and
HiFi data, trailing behind assembly-based CN predictions by just 0.007–0.016 percentage points. At the
same time, CN predictions without the network flow achieved 97.5% (ONT) and 97.2% (HiFi) accuracy,
0.6 and 0.9 percentage points behind the flow-based accuracy values. In terms of the number of nodes,
improvement was even greater: 0.8 percentage points (98.8→99.6%) for ONT and 4.1 percentage points
(95.2%→99.3%) for HiFi sequencing data (Fig. 2).

At smaller coverage it becomes more difficult to both accurately estimate background read depth, as
well as to distinguish sequence, unsupported by chance, from sequence truly missing from the sample
genome. Consequently, network flow, which effectively aggregates signal from nearby nodes, achieves a
greater edge over CN predictions for individual nodes. At 1× coverage data, ONT-based CN predictions
showed 53.4% and 96.9% accuracy (total length) before and after the network flow, while HiFi-based
accuracy marked 64.6 and 97.6%, respectively, which represents approximately a 15-fold reduction in
error rate in both cases. In contrast to other cases, some CN=0 nodes were assigned CN=1 (node-

Figure 3. Concordance between copy number predictions for different sequencing technologies. Each of the four panels contain an extended UpSet plot, which shows the number of nodes and sum length of the nodes for each combination of CN predictions (orange for 0; purple for 1; light blue for larger values) based on the chopped assembly, PacBio HiFi and Oxford Nanopore (ONT) reads. Columns are sorted by sum length, 11th and later columns are groupped together ("other"). Right side of each panel shows the total number of nodes and their sum length for each CN group and each sequencing technology. Concordance is calculated for **a**, HG01114 human data and **b**, potato Altus data mapped to their corresponding assembly graphs; as well as **c**, in-sample HG01258 and **d**, out-of-sample HG01114 data mapped to the HPRC pangenome. Chopped assembly is removed from the panel **b** due to the low resolution of the corresponding linear haplotype-resolved assembly.

based precision = 97.5–97.8%), however, this mostly affected short nodes (median length ≈70 bp for both sequencing technologies), and did not notably influence precision, weighted by the sequence length.

Concordance between technologies. Obtaining ground truth CN values is a more difficult problem for other samples and graphs, even in the presence of linear assemblies. We therefore focused our analysis on comparing Floco CN predictions for three different alignment sources: independently generated HiFi and ONT sequencing datasets, as well as sample linear assemblies, chopped into reads.

In the human assembly graph case, for HG01114-asm (Fig. 3a, Suppl. Fig. 4a), Floco predicted the same CN values for all three data sources across 3,956 Mb (93.2% of total sequence in the graph), corresponding to 73.5% of the informative nodes, which contained unique sequence following graph preprocessing (Suppl. Methods). Individually, both HiFi and ONT CN predictions matched the chopped assembly across 96.5% and 96.0% of the total sequence, respectively; as well as matched each other by 93.8% (83.8% nodes). However, we observed that discordances are often caused by Floco selecting one or the other of two alternative paths through a bubble, where both arms have almost identical sequences and very similar read depth (Suppl. Fig. 5). Consequently, while difficult to measure, Floco concordance in terms of the actual sequence content is likely to be significantly higher than the raw sequence length concordance. We also note that such bubble structures (Suppl. Fig. 5) exist only in places where the assembly tool was not able to resolve them; that is, they by construction reflect loci with ambiguity, accumulation of systematic sequencing errors, or artifacts introduced by the assembly algorithm.

In the tetraploid potato assembly graph case, Altus-asm (Fig. 3b), we excluded assembly-based predictions, because of low assembly quality (see Suppl. Fig. 4b). For the two sequencing datasets, Floco

predicted the same CNs across 92.9% of the sequence (71.4% informative nodes), HiFi and ONT-based CN predictions, reaching concordance levels similar to HG01114-asm.

Next, for the HPRC pangenome graph, we examined in-sample HG01258-pang and out-of-sample HG01114-pang alignments. In both cases, ONT better matched the chopped assembly, with 89.3 and 90.6% of concordant sequence, respectively, compared to HiFi data with 80.7 and 81.4% of concordant sequence. This can be explained by the prevalence of CN=1 sequence at the expense of higher CN in the HiFi-based predictions (Fig. 3c–d, Suppl. Fig. 4c–d). Nevertheless, in terms of the node-based concordance, Floco showed similar values for both technologies: 81.4% (HiFi) and 75.6% (ONT) for HG01258-pang compared to 81.6% and 81.7% for HG01114-pang. Predicted node CNs had high correlation between the two sequencing datasets: r=0.833 and 0.899 for HG01258 and HG01114, respectively. Even though HG01258 was used for the HPRC graph construction, its ONT data has lower coverage (7× compared to 26× for HG01114, see Suppl. Table 3), which could explain lower prediction concordance. Additionally, we looked at the concordance for in-sample CHM13-pang, where the concordance between the three sources reached 99.9% of concordant sequence (99.4% of informative nodes) (Suppl. Fig 3).

Assembly graph quality control. With Floco, we are able to flag potentially misassembled nodes with CN=0, even though some of them have observed coverage. For example, when aligning HiFi reads from HG01114 against its assembly graph (HG01114-asm), we get 33.9 Mb of sequence with CN=0, corresponding to 1,825 informative nodes. Most of these nodes belong to very small components of the graph, where alignment is harder to perform. There are, however, some cases in the bigger components (Suppl. Fig. 6), where bubbles are erroneously created, leading to three possible paths through a given locus, when at most two would be the expected for a diploid individual. We have manually examined some of these examples and found that all of them appear to be indeed misassembled nodes, where the sequence content of the node is represented in the alternative paths, either exactly or with very high sequence similarity.

Additionally, we examined CN predictions based on the HG01114 ONT read alignments to the HG01114 assembly graph, and observed the same pattern, although the number of CN=0 nodes was slightly higher in that case (2,208), corresponding to a total of 91.2 Mb of sequence. The difference between the two sequencing technologies is explained by the larger number of CN=0 nodes in smaller components. This is likely due to the fact ONT reads have a higher error rate than HiFi reads, introducing additional noise in the alignment process. We also note that small nodes in these (otherwise high quality) assembly graphs typically represent either errors or low complexity sequence.

Runtime and peak memory usage. Floco CN calling on assembly graphs (HG01114-asm and Altus-asm) is extremely lightweight, and can easily be executed on a laptop; with one-threaded runtime varying between 8 and 22 minutes (Suppl. Table 3) and peak memory not exceeding 3.1Gb. As pangenome graphs are more convoluted, Floco required more time (ranging from 40 minutes to just under 3 hours), with peak memory not exceeding 53Gb for real sequencing data. In any run, Floco CN calling took a fraction of time needed to align reads to the graph, as GraphAligner required between 14 and 100 hours, depending on sequencing coverage, for both graph types, and consumed between 8 and 35Gb.

Furthermore, we evaluated the impact of varying coverage on the Floco computational resources usage. Starting from 33× (HiFi) and 112× (ONT) coverage for CHM13-pang, we downsampled the alignments and measured Floco runtime and memory consumption. As Figure 4a shows, running time weakly grew with coverage for both sequencing technologies (Pearson's r=0.83–0.86), with CN calling taking between 79 and 100 minutes for the HiFi data and between 89 and 131 minutes for the ONT data. At the same time, memory usage did not depend on the underlying coverage, with Floco consuming 33.4–35.1Gb in all cases (Fig. 4b).

Figure 4. Computational resource usage per sequencing coverage. Floco runtime (**a**) and peak memory usage (**b**) were measured for the ONT (red triangles, coverage between 1 and 112) and HiFi data (blue circles, coverage between 1 and 33).

Discussion

We presented a new method, Floco, to call CN on genome graphs using graph-aligned reads. Floco combines techniques for read-depth based CN estimation [5–7, 10] and network flow formulations introduced in the context of genome assembly [17], addressing a need in the tool ecosystem for working with genome graphs. Even though the proposed flow formulation involves piecewise linear node weights in addition to linear edge weights, the problem can be reduced to the regular min-cost network flow problem, which can be solved in polynomial time [17, 20]. Floco uses integer linear programming solver Gurobi [22] to find the optimal flow, which leads to fast runtime on all evaluated datasets. We therefore did not attempt to use specialized flow solvers.

We demonstrate the advantage of using the network flow approach by comparing CN predictions before applying the flow, i.e. using read depth information only, and after applying the flow to correct inconsistencies and overcome misalignments and sequencing errors. Results show a clear gain when adding the network flow formulation on top of the read depth based approach (Fig. 2), especially regarding accuracy and precision.

We also demonstrate that Floco is robust with respect to the choice of input data, as shown by the concordance observed between the predictions made from different sources (Fig. 3). Given the varying characteristics of each source, with ONT reads being much longer than HiFi reads and assembly pieces; while having, on the other hand, a higher error rate; differences in final results are expected. Nevertheless, we still achieved high levels of concordance for at least two out of three sources, reaching values above 92.9% of the total sequence length for both assembly cases, and 80.7—90.6% for the pangenome cases. The difference between species might be explained by the lower quality of both the Altus graph and its linear assembly, as well as the fact that it represents an autotetraploid organism.

Floco is fast and has low memory requirements (Fig. 4, Suppl. Table 3). Computational resource usage can be reduced further by tweaking input parameters, specifically the "expensive" superedge penalty (see Method), which allows to control a trade-off between speed and accuracy. Additionally, ILP solving time can be decreased by using multiple threads (values shown in this study were all ran with a single thread). Time and memory consumption are mostly influenced by the graph complexity, namely the number of nodes and edges, which translate into more variables for the ILP (see Method).

For the analysis performed here, we have used only long reads. Theoretically, the tool should work with any type of reads, but it is dependent on the input alignments of the reads to the graph, which are more challenging to obtain for short reads. While Floco is a generic tool designed to work on as many graphs as possible, the performance in practice and interpretability of results depends on the

input graphs. Especially when quantifying CNs relative to a pangenome reference, the quality of results will depend on whether copy-number-variable segments are represented as their own nodes. As future work, we envision to add functionality to call CN changes that occur within single nodes.

There are not yet community-curated benchmark sets for CN calling on graphs. Here, we have created our own benchmarks by using publicly available resources. One open challenge consists in comparing CN calls on graphs to CN calls with respect to a linear reference genome. Such a comparison would require a transfer of CN predictions from a graph to a linear reference, involving copy-number-variable regions as well as sequence missing from the reference. This operation is not only difficult to define and develop, but would likely introduce its own discordance. We therefore did not include comparisons to CN callers for linear references. We show that further challenges for the evaluation stem from cases of high sequence identity across different genomic paths through the graph, which can lead to underestimated concordance values.

Our method supports multiple use cases. On the one hand, predicting CNs by aligning a linear assembly against the individual's assembly graph can be used as quality control for the graph itself (Suppl. Fig. 6). On the other hand, Floco fills an important gap for genotyping classes of genomic variation with variable CN, like segmental duplications, which are becoming more tractable given the advances on assembly methods. This use of Floco has applications for downstream association studies to discover correlations between CN states and phenotypes.

In summary, we have presented a method, implemented in the general-purpose tool Floco, that fills a gap in CN calling tools specific to genome graphs, offering an accurate and robust strategy with multiple applications.

Data Availability

The HPRC graph used for the benchmarking of Floco can be found at `s3-us-west-2.amazonaws.com/human-pangenomics/pangenomes/freeze/freeze1/minigraph/hprc-v1.0-minigraph-chm13.gfa.gz`. The Altus tetraploid assembly graph can be found at `zenodo.org/records/17599056`. The HG01114 assembly graph was produced under the scope of HGSVC3 [16]. CHM13 linear assembly can be found in the European Nucleotide Archive with the accession number PRJNA559484, and the reads can be found at `github.com/marbl/CHM13/blob/master/Sequencing_data.md` (HiFi Data and Guppy 5.0.7). Data for HG01258 can be found at `s3-us-west-2.amazonaws.com/human-pangenomics/index.html?prefix=working/HPRC/HG01258`. HG01114 reads can be found in the European Nucleotide Archive with accession number SAMEA115605425. The sequencing reads for Altus are available via the NCBI BioProject under accession number PRJNA778192 (HiFi) and PRJNA1049180 (ONT).

Code Availability

Floco is implemented in the Python programming language. The source code is freely available under the terms of the MIT license at `github.com/hugocarmaga/floco` along with installation and usage instructions. Benchmarking scripts are available at `github.com/hugocarmaga/floco-benchmarking`.

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References

[1] Brownstein, C. A. *et al.* RCL1 copy number variants are associated with a range of neuropsychiatric phenotypes. *Mol. Psychiatry* **26**, 1706–1718 (2021).

[2] Shearer, A. E. *et al.* Copy number variants are a common cause of non-syndromic hearing loss. *Genome Med.* **6**, 37 (2014).

[3] Mueller, M. *et al.* Genomic pathology of SLE-associated copy-number variation at the FCGR2C/FCGR3B/FCGR2B locus. *Am. J. Hum. Genet.* **92**, 28–40 (2013).

[4] Mahajan, V. S. *et al.* Striking immune phenotypes in gene-targeted mice are driven by a copy-number variant originating from a commercially available C57BL/6 strain. *Cell Rep.* **15**, 1901–1909 (2016).

[5] Abyzov, A., Urban, A. E., Snyder, M. & Gerstein, M. CNVnator: an approach to discover, genotype, and characterize typical and atypical CNVs from family and population genome sequencing. *Genome Res.* **21**, 974–984 (2011).

[6] Talevich, E., Shain, A. H., Botton, T. & Bastian, B. C. CNVkit: Genome-wide copy number detection and visualization from targeted DNA sequencing. *PLoS Comput. Biol.* **12**, e1004873 (2016).

[7] Boeva, V. *et al.* Control-free calling of copy number alterations in deep-sequencing data using GC-content normalization. *Bioinformatics* **27**, 268–269 (2011).

[8] Rausch, T. *et al.* DELLY: structural variant discovery by integrated paired-end and split-read analysis. *Bioinformatics* **28**, i333–i339 (2012).

[9] Chen, X. *et al.* Manta: rapid detection of structural variants and indels for germline and cancer sequencing applications. *Bioinformatics* **32**, 1220–1222 (2016).

[10] Layer, R. M., Chiang, C., Quinlan, A. R. & Hall, I. M. LUMPY: a probabilistic framework for structural variant discovery. *Genome Biol.* **15**, R84 (2014).

[11] Prodanov, T. & Bansal, V. Robust and accurate estimation of paralog-specific copy number for duplicated genes using whole-genome sequencing. *Nat. Commun.* **13**, 3221 (2022).

[12] Prodanov, T. & Bansal, V. A multilocus approach for accurate variant calling in low-copy repeats using whole-genome sequencing. *Bioinformatics* **39**, i279–i287 (2023).

[13] Ebert, P. *et al.* Haplotype-resolved diverse human genomes and integrated analysis of structural variation. *Science* **372**, eabf7117 (2021).

[14] Wang, T. *et al.* The Human Pangenome Project: a global resource to map genomic diversity. *Nature* **604**, 437–446 (2022).

[15] Liao, W.-W. *et al.* A draft human pangenome reference. *Nature* **617**, 312–324 (2023).

[16] Logsdon, G. A. *et al.* Complex genetic variation in nearly complete human genomes. *Nature* **644**, 430–441 (2025).

[17] Medvedev, P. & Brudno, M. Maximum likelihood genome assembly. *J. Comput. Biol.* **16**, 1101–1116 (2009).

[18] Bonnet, K. & Marschall, T. strangepg. https://github.com/qwx9/strangepg.

[19] Nemhauser, G. L. and Wolsey, L. A. *Integer and Combinatorial Optimization* (1988).

[20] Ahuja, R. K., Magnanti, T. L. & Orlin, J. B. *Network Flows: Theory, Algorithms, and Applications* (Prentice Hall, 1993).

[21] O'hagan, A. & Leonard, T. Bayes estimation subject to uncertainty about parameter constraints. *Biometrika* **63**, 201–203 (1976).

[22] Gurobi Optimization, LLC. Gurobi optimizer reference manual (2024).

[23] Eizenga, J. M., Lorig-Roach, R., Meredith, M. M. & Paten, B. Walk-preserving transformation of overlapped sequence graphs into blunt sequence graphs with GetBlunted. In *Lecture Notes in Computer Science*, Lecture notes in computer science, 169–177 (Springer International Publishing, Cham, 2021).

[24] Anders, S. & Huber, W. Differential expression analysis for sequence count data. *Genome Biol.* **11**, R106 (2010).

[25] Gao, F. & Han, L. Implementing the nelder-mead simplex algorithm with adaptive parameters. *Comput. Optim. Appl.* **51**, 259–277 (2012).

[26] Nelder, J. A. & Mead, R. A simplex method for function minimization. *The Computer Journal* **7**, 308–313 (1965).

[27] Henglin, M. *et al.* Graphasing: phasing diploid genome assembly graphs with single-cell strand sequencing. *Genome Biol.* **25**, 1–26 (2024).

[28] Rautiainen, M. *et al.* Telomere-to-telomere assembly of diploid chromosomes with verkko. *Nat. Biotechnol.* **41**, 1474–1482 (2023).

[29] Serra Mari, R. *et al.* Haplotype-resolved assembly of a tetraploid potato genome using long reads and low-depth offspring data. *Genome Biol.* **25**, 26 (2024).

[30] Li, H., Feng, X. & Chu, C. The design and construction of reference pangenome graphs with minigraph. *Genome Biol.* **21**, 265 (2020).

[31] Rautiainen, M. & Marschall, T. GraphAligner: rapid and versatile sequence-to-graph alignment. *Genome Biol.* **21**, 253 (2020).