Noise-driven cell differentiation and the emergence of spatiotemporal patterns

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Abstract   One of the major transitions in evolution is the step from unicellularity into the brave new world of multicellularity. To understand this feat, one has to fathom two main characteristics of multicellular organisms: differentiation and self-organization. Any explanation concerning this major transition should involve mechanisms that can simultaneously explain the marvelous intricacies manifest in the aforementioned characteristics, and an account of the evolution of such traits. Here we propose a noise-driven differentiation (NDD) model. The reliance on noise, in place of a more mechanistic approach, makes the NDD model a more suitable approach to explain differentiation and self-organization. Furthermore, our model sheds some light on the possible evolutionary origins of these biological innovations. To test the NDD model, we utilize a model of cell aggregation. The behavior of this model of cell aggregation is in concert with the NDD model.

Introduction

The traditional idea of a living cell where every organelle, every reaction, and every interaction is part of a clock-like order has long been shattered by the understanding that biological systems usually struggle to function in noisy environments. One might consider life to be an uphill battle against pandemonium, where disarray is the norm and spheres of order – i.e., biological systems – are rarities that are unlikely to appear in the first place. In this view, noise is a nuisance that natural selection always attempts to eliminate. It is for the same reason that selection cannot increase the fidelity of replication beyond a certain threshold; the biological cost of increasing fidelity simply becomes too high at that point (*Kimura, 1967*).

A different view has recently gained some grounds (*Balázsi et al., 2011*; *Chalancon et al., 2012*; *Huang, 2009*; *Losick and Desplan, 2008*). In this view, biological systems that regulate and utilize the noise can have higher fitness under certain circumstances. Had biological systems been utterly deterministic, adaptation – i.e., the emergence of a new phenotype or a change in the gene expression pattern to utilize a new food source – would have been impossible without the emergence of new mutations. In reality, noise in the cell can result in beneficial non-genetic diversity in oth-

erwise genetically homogenous populations – e.g., cyanobacteria (**Wolk, 1996**) and yeast (**Paliwal et al., 2007**). But what mechanism can account for the presence of phenotypic diversity amongst daughter cells that are genetic clones of each other? Is it possible for a stochastic mechanism to explain the non-genetic diversity? Even if such stochastic explanation were offered, how could this explanation possibly account for the ordered spatiotemporal patterns in spatially-extended cell population?

The model of cell differentiation proposed in this work, henceforth referred to as the noise-driven differentiation (NDD) model, accounts for the peculiarities of this biological phenomenon by weaving noise into an explanation of cellular behaviors at the time of differentiation. While on the surface, this approach might seem lofty and even radical, the model discussed in this paper is parsimonious when it comes to the mechanisms requisite for its operation. The NDD model rests on 8 components (Table 1). Some can be regarded as facts, based on reliable empirical evidence from biological systems (components #1 and #2), while others are more accurately described as assumptions (components #$3 - 8$).

There is a plethora of phenomena within a cell that can contribute to its intrinsic noise – e.g., transcription regulation, transcription factor binding to the DNA, RNA processing in eukaryotes, translation, post-translational modifications, protein complex formation, protein and RNA degradation, etc. Single-cell level measurements of gene expression further cements the notion that cells are intrinsically noisy when it comes translating its genotype into phenotype (**Sanchez and Golding, 2013**). The displacement of the division plane relative to the middle of the cell can result in an unequal distribution of cell content between the daughter cells, even if molecules are homogeneously distributed within the cell. In fact, the central role of asymmetric cell division in the diversification of cells, from *Drosophila* to mammals has been known for many years (**Jan and Jan, 1998**; **Betschinger and Knoblich, 2017**).The components #$1 - 2$ is an acknowledgement of the role stochasticity in living systems based on these observation.

Thus far, two types of solutions to the problem of cell differentiation have been proposed: the first category consists of models that rely on cell-cell communication (reviewed in **Wolpert** (**2011**)) and the second category relies on asymmetric cell division (reviewed in (**Rudel and Sommer, 2003**)). The research project within the confines of the former category is mainly a quest to find the building blocks of the apparatus that makes the specific kind of cell-cell communication needed for cell differentiation. The latter category, on the other hand, presumes the asymmetric cell division to result in differentiation. Hitherto unknown and often complicated mechanisms have been proposed to explain the asymmetric distribution of fate-determining factors during cell division (**Morrison and Kimble, 2006**; **Clevers, 2005**). Both categories are quintessentially mechanistic in nature, since they rely on mechanical interactions at the cellular level. While we agree with the importance of the asymmetric cell division, it seems to us that a stochastic model of differentiation, like the NDD model, negates the need for new mechanisms. In this model, we adopt the view that stochastic processes result in differentiated cells due to the distribution of key proteins, instead of cells differentiating by receiving signals after they are born (component #3).

The component #4 is based on the idea that characteristics of a cell can be changed by a switch (Not a very recent idea, e.g., **Novick and Weiner** (**1957**)). The notion that cell fate is determined by a switch is best illustrated by the now famous case of the λ phage. The process by which the phage decides to integrate into the host's genome – i.e., lysogenic – or to replicate copies of itself in the cell until it bursts open – i.e., lytic – can be explained by a stochastic switch which makes that portentous decision in a probabilistic fashion, while taking into account the presence of certain key factors (**Ptashne, 2004**). One can assume that the bias of this switch is determined by the interactions of its building blocks (component #5). For example, upon infecting bacterial cells, λ phage

Figure 1. The phase-portrait diagram for the NDD model (based on Eq 1). In a bistable switch, two attractors (red semicircles) and, consequently, two phenotypes are available: A and B. The likelihood of a switch choosing state A over B depends on the number of the transcription factor associated with state A (TF_X) relative to the number of the transcription factor associated with state B (TF_Y), as well as the noise in its environment. The parameters used to generate this and the following figure are as follows: $n = 2$, $\beta = 0.1$, protein half-life $= 10$min, and protein dissociation constant $= 10$. Unless noted otherwise, these parameters are used in all the subsequent figures.

Table 1. The components of the NDD model.

#	Component	Justification
1	Noise, resulting from a plentitude of sources, is an inseparable part of a living cell.	Based on the observed effect of noise on the processes in living cells, from microbes to mice (e.g., see (*Kepler and Elston, 2001*; *Ozbudak et al., 2002*; *Elowitz et al., 2002*; *Maamar et al., 2007*; *Chang et al., 2008*)).
2	Stochastic partitioning of cytoplasm during cell division and the random distribution of molecules in the cytoplasm determine the cytoplasmic contents of the daughter cells.	Variation in the position of cell-division plane is a biological fact (reviewed in *Margolin* (*2000*); *Monahan et al.* (*2014*); *Pickett-Heaps et al.* (*1999*); *Wu and Tzanakakis* (*2012*); *Bradshaw and Losick* (*2015*)), and its effect on the diversification of cells is well-known (e.g., see *Jan and Jan* (*1998*); *Betschinger and Knoblich* (*2017*)).
3	The fate of a cell is determined when it is born.	Based on the assumption that cell-fate-determining factors are in small numbers in a cell and the stochastic distribution of these factors during cell division determines the fate of the newly-born daughter cells.
4	Cell fate is determined by a switch.	Genetic switches have been observed in a variety of taxa (reviewed in *Balázsi et al.* (*2011*)), and has been proposed as a model to account for cell differentiation (e.g., see *Perez-Carrasco et al.* (*2016*)).
5	The interaction between the building blocks of the switch determines its bias.	Our assumption based on our knowledge of well-known genetic switches, such as λ phage (see *Cortes et al.* (*2018*)).
6	All the information needed to construct the switch is genetic.	We assume that, while stochasticity is what drives the decision made by the switch, the information necessary to construct the switch is encoded in the genetic content of a cell.
7	The robustness of the switch is the result of a complex network of interactions.	Our assumption based on *Sharifi-Zarchi et al.* (*2015*).
8	Cell fate is influenced by its location and its environment.*	We assume the the switch determining cell fate should, in addition to being swayed by the intrinsic factors, be influenced by its neighbors.

* This component is necessary for the ordered spatiotemporal patterns in cell population.

proceeds to lyse the host, but as the concentration of CII protein increases, so does the likelihood of the reactions suppressing the activation of *pR* and *pL* promoters, relevant to the onset of the lytic trajectory, which in turn, tilts the scale away from lysis towards lysogeny (*Cortes et al., 2018*). We propose that phenotypic diversity arises from the effect of the noise on a genetic circuit that exhibits a switch-like behavior (component #6). The notion that different phenotypes are produced from the same genotype as a consequence of noise is widely observed in nature (reviewed in (*Vogt,*

2015))

How robust can a fate-determining toggle switch in the face of new mutations? *Sharifi-Zarchi*
et al. (*2015*) took advantage of the gene expression profiles of 442 mouse embryonic cells to con-
struct a network of key transcription factors (TFs). While a regulatory circuit with two TFs could
explain differentiation, They reasoned that such a simple switch is susceptible to mutations. To
construct a robust switch, they built a circuit with two clusters of TFs with correlated expressions.
Expectedly, the alternative switch, which involved more interactions, was much more robust. We
would expect different levels of robustness for a switch, given its biological importance in evolution
(component #7).

The components #1-7 are sufficient to generate a population of cells with different proportions
of two phenotypes (Fig 1). While this kind of fate determination is adequate vis-à-vis primitive cells
with no organization, it does not allow the emergence of multicellularity. An additional compo-
nent is necessary to explain this major transition from mere phenotypic differentiation to ordered
spatiotemporal patterns in the body of a multicellular organism. For self-organization to occur,
we assume that the toggle switch determining cell fate should, in addition to being swayed by the
intrinsic factors, be influenced by its neighbors (component #8).

To test the general veracity of the NDD model, we used a simple model of cell aggregation. In
this model, a simple switch is defined that can switch between phenotypes, A and B.

Results

120 The overall behavior of the cell aggregation model demonstrates the principles of our framework –
121 that is, the stochasticity results in phenotypic heterogeneity as the population grows in size (movie
122 S1). To further illustrate how each source of noise affects the cell differentiation, we focused on
123 each source separately in the simulations.

The stochastic positioning of division plane and the stochastic distribution of key proteins affect differentiation

One source of intrinsic stochasticity stems from the random positioning of the division plane. This
factor would disproportionately influence the number of molecules that exist in low numbers
within cytoplasm. In this work, it has been postulated that the determinants of cell fate are low
in numbers and thus, greatly affected by stochasticity.

To demonstrate this phenomenon, the position of the division plane was allowed to vary with
respect to the mid plane of the cell. Starting from a cell with phenotype A, in which the protein
X is dominant, the population heterogeneity –i.e.,emergence of phenotype B– was traced over 12
generations. The results are shown in Fig 2. When the division plane is situated in the middle of
the cell, and the TFs are relatively abundant, very few cells differentiate. As the variance in the cell-
division plane increases, so does the proportion of B cells. This phenomenon is dependent on the
number of proteins, since such bias is more pronounced when the number of proteins is relatively
low. In fact, with large numbers of TFs in a cell, it will be more likely for its daughters to have almost
the same density of TFs as their mother. Thus, they will be in the same domain as the mother in the
phase space, and their fates will be identical to hers. This can be seen clearly in the lower curves in
Fig 2. However, for low copy numbers of TFs, the difference between TF numbers in two daughter
cells becomes more prominent and can even lead to different cell fates. Therefore, it is possible
to have heterogeneity in the population in the absence of any other noise, i.e., cells with low TF
numbers are heterogeneous even with no variance in division-plane displacement (Fig 2a). Adding
spatial fluctuation to the distribution of TFs within a cell increases the chance of differentiation,

since in this case, in addition to the noise from the positioning of division plane, the key proteins
are stochastically distributed as well (Fig 2b).

Signaling can create spatial order

In the cell aggregation model, B cell can release signals in the environment. These signals diffuse
at a slow rate and, consequently, have a very short radius of influence. The absorption of these
signals by other cells in the population affects the number of proteins involved in the switch –
that is, switching to the phenotype B during cell division becomes more likely (Fig 3). When this
environmental signaling is added to the population, the cells organize in a non-random fashion, a
stark contrast to the random heterogeneity observed before (Movie S2).

Fig 4 represents a visual understanding of the results from the NDD model. It shows the bac-
terial community in a 2-dimensional simulation area after more than 8 generations. In Fig 4a, the
variance in the stochastic positioning of the division plane increases from left to right. It can be
seen that the heterogeneity in the population increases as well by the presence of new pheno-
types (cells in orange). In Fig 4b, development of an organized community as a result of signaling
molecules is apparent (group of orange cells). The organization observed will increase over time
and the community of orange cells will develop (Movie S3).

Discussion

Molecular processes in the cell are noisy events that result in varying degrees of heterogeneity.
Taming this inherent noise is vital for the emergence and the continuation of life. In fact, life can
be characterized as a system with the capacity to control noise. The phenotype of a cell is gener-
ally stable, but during cell division, this cell can produce daughter cells with different phenotypes
via symmetric or asymmetric cell division. The resulting non-genetic phenotypic diversity is a way
to achieve adaptation in a fluctuating environment by producing phenotypically diverse offspring
without any need for genetic change. Given the variety of sources of noise, the cell fate determina-
tion can be a stochastic process. One can imagine a few genes involved in cell fate determination,
where the noise in the cell affects the proportion of daughter cells born with a certain pheno-
type. The ability to change the phenotypic proportion of daughter cells via a stochastic mechanism,
which is also tunable, is a superb strategy to outcompete rivals bereft of such gift.

Given the prominence of noise in living cell, we argue that the NDD model can provide a satis-
factory explanation of how organization can emerge from noise. Proposing a stochastic model of
cell differentiation is not an entirely novel concept, e.g., see *Suzuki et al.* (*2011*); *Yamagishi et al.*
(*2016*) as examples of an impressive body of work produced by Kunihiko Kaneko and his colleagues
on this subject and *Kupiec* (*1997*); *Paldi* (*2003*) as similar proposals regarding the possible role of
stochasticity in generating phenotypic diversity. We argue that our approach differs from theirs
and similar ideas in certain important aspects: firstly, our model assumes that cell fate is deter-
mined when the cell is born, and secondly, that stochastic fluctuations in the cell, and the effect
of signals from neighboring cells in the multicellular case, drive the phenotype of the cell towards
one attractor rather than another during cell division. This approach is in keeping with the recent
emphasis on the importance and the prevalence of noise in biological functions, specifically cell
fate (*Balázsi et al., 2011*; *Huang, 2009*; *Kittisopikul and Süel, 2010*). The model of cell aggregation
used in this study allowed us to test all the components of the NDD model, barring components #6
and #7, which demand through investigations of their own. This model of cell aggregation provides
us with a relatively realistic depiction of the process that results in phenotypic differentiation in a
population. We believe that, with few changes, the NDD model can be applied to other biological
systems as well.

Figure 2. The stochastic positioning of the division plane and the random distribution of TFs in the cytoplasm, as intrinsic sources of noise, affect the none-genetic phenotypic diversity (component #2). The phenotypic diversity is represented by the proportion of cells with the phenotype B relative to the total number of cells in the population. In panel (a), the only source of noise is the stochastic positioning of the division plane, while panel (b) shows the phenotypic diversity as a result of both sources of noise. In each panel, the curves indicate different amounts of protein X in the mother cell; from top to bottom, respectively, $X = 10, 15, 20, 25, 35, 45, 55, 100$. The results are average over 100 replications. Error bars are 95%CI.

Figure 3. Adding signaling to the cell aggregation model results in higher none-genetic phenotypic diversity, compared to populations without signaling (as shown in Fig 4). The phenotypic diversity is represented by the proportion of cells with the phenotype B relative to the total number of cells in the population. The curves indicate different amounts of protein X in the mother cell; from top to bottom, respectively, $X = 10, 35, 55, 100$. It fascinating to notice how the lowest number of TFs ($X = 10$) results in total differentiation. The efficacy of signaling is defined as follows: if in the position of a cell with phenotype A, the signal concentration exceeds the mean signal concentration, then this cell would have more chance of becoming a B cell. The results are average over 100 replications. Error bars are 95%CI.

(a)

(b)

Low $\Longrightarrow$ High

Figure 4. Population heterogeneity as a result of the noise in: (a) the number of TFs in the daughter cells or (b) the secretion of signals from the B cells. Both the number of TFs in (a) and the efficacy of singling in (b) increases from left to right in this figure. The blue circles represent the A cells and the orange ones represent the B cells. Each aggregation is the final state of a single run of the stochastic model with the given parameters. The amount of protein X in the initial cell in each simulation was 35. The radius of the area of aggregation is $100\mu m$.

The ability of the cells to differentiate into different types was the crucial step that enabled the
ancient solitary cells to leave the primordial soup behind and evolve into the vast array of special-
ized cells we see today. As *Queller and Strassmann* (*2009*) point out, there are different shades
of organismality –i.e., the ability for components to work together with little conflict among them–,
each shade resulting from the affinity of the members of the system to cooperate versus the temp-
tation to cheat. We can sidestep the problem of conflict since in prokaryotic multicellularity, e.g.,
biofilm, and in most truly multicellular eukaryotes, the cells are highly related, thus lowering the
probability of cheating (*Ostrowski and Shaulsky, 2009*). Without tangible levels of conflict, multi-
cellularity as a trait becomes patently advantageous. In their seminal work, Maynard Smith and
Szathmáry (*Maynard Smith and Szathmáry, 1995*) considered two possible mechanisms to account
for the emergence of cell differentiation: one relies on the presence of determinants that prohibit
the stem cell to differentiate, and the other postulates the cell-cell contact as a mechanism that
determines cell fate. While these suggestions account for how the multicellularity might be sus-
tained, they do not explain how this major evolutionary transition could have occurred in the first
place.

It is easier for cell differentiation to evolve via the emergence of a switch, rather than the less
plausible path that involves the evolution of a clockwork mechanism. According to the NDD model,
the emergence of early stages of multicellularity only requires the evolution of a suitable switch –
the rest of the necessary ingredients needed for the transition into self-organization is provided
by the stochastic elements affecting the switch. The major transition from unicellularity to mul-
ticellularity –i.e., from phenotypic diversity in a population to from an ordered and stable spatial
heterogeneity– only requires one more step: the evolved switch should be simply affected by the
signal(s) released by its neighbors (components #8). The spatial information received in this way
would bias the switch such that the population-level organization is retained. It is tempting to pos-
tulate a connection between the cell-differentiation switch, postulated in the NDD model, and the
toggle switch used in quorum sensing in bacteria (*Hooshangi and Bentley, 2011*). Quorum sensing
enables bacteria to regulate their phenotypes apropos of their neighbors and is more robust in a
dense community (*Schluter et al., 2016*). It seems plausible to consider this type community-based
phenotypic regulation as a precursor to similar switch-based mechanisms for cell differentiation
in multicellular organisms.

In their criticism of a noise-driven alternative to their model, *Suzuki et al.* (*2011*) considered it
unlikely for a noise-driven model to maintain the exact levels of stochasticity needed to produce
the desired proportion of differentiated cells to stem cells. In our view, this conclusion follows
from a non-evolutionary perspective, since it is easy to imagine negative selection keeping a ge-
netic switch just sensitive enough to result in a correct differentiation pattern vis-à-vis the biologi-
cal fitness. Furthermore, if a switch is robust (component #7), then it will be able maintain its bias
in the face of new mutations. *Suzuki et al.* (*2011*) also point out that a noise-driven model can
only produce reversible differentiation. While the NDD model as described here only explains the
phenotypic differentiation in prokaryotes, which is indeed reversible, it seems that changing the
bi-stable switch to a tri-stable one could remedy this issue and explain the irreversibility of differ-
entiation observed in eukaryotes, as it should increase the strength of attractors (*Ghaffarizadeh*
et al., 2014).

One of the quintessential aspects of the discussed model is its population-level perspective.
Population-level thinking is one of the main points of the evolutionary theory, and bringing it to
explain a cellular phenomenon can lead us to reap valuable insights. While a population of cells has,
on average, certain properties relevant to differentiation, e.g., the mean number of key proteins,
the average position of cell division plane, and etc., these average values do not tell the whole story.
Instead, the variance in these values, i.e., the non-genetic variation present amongst individuals, is

the key to understand differentiation (as observed in studies such as in *Chang et al.* (*2008*); *Moussy et al.* (*2017*)). This noise in the population is essentially the fuel that propels cellular differentiation, be it in the reversible differentiation in prokaryotes or the more complicated irreversible ones in higher organisms. We believe that this population-level vintage point is the necessary tool to understand this otherwise mind-boggling biological process. Without this perspective, the task of explaining such a seemingly fine-tuned process devolves into an attempt to come up with complex cellular interactions that would make climbing this improbable biological mountain feasible.

The NDD model can be used wherever there is cell division and differentiation. The differentiating cell can be a prokaryotic one, able to divide into daughter cells with dissimilar, and reversible, phenotypes or a eukaryotic cell undergoing irreversible differentiation, without the need for one or a few complicated mechanisms. The transition from single cells into the brave new world of multicellular entities could have been the result of a mechanism very much akin to the NDD model. Such transition is possible because the bias of the switch can be affected by the neighboring cells. The NDD model paints a simple and elegant picture of differentiation and organization, from prokaryotes to eukaryotes. Our model is the logical extension of earlier ideas describing the role of stochasticity in phenotypic variation and the switch-like behavior of genetic circuits vis-à-vis differentiation and multicellularity (e.g., see *Nanjundiah* (*2016*)).

Materials and methods

In the cell aggregation model, the population is made up of cells, where each cell is a circular particle defined by its state variables – e.g., spatial position, size, and phenotype. The simulation geometry is a $L \times L$ square and no flux boundaries. It is assumed that the relative amount of two key transcription factors, X and Y, controls the cell types; hence, in this model, a cell can have two phenotypes, A and B, as shown in Fig 1. The dominance of protein X leads to phenotype A and the dominance of protein Y results in phenotype B. In fact, a positive feedback loop influences the decision-making process. Two negatively coupled repressors mutually inhibit the expression of the gene that encodes the other repressor- i.e., a toggle switch (component #4). The rate of this mutual repression is represented in the form of a Hill function (*Gardner et al., 2000*). This positive feedback loop results in two stable steady states, hence implies non-linear approaches. Nonlinear differential equations govern the changes in the number of the repressor proteins, X and Y (Fig 1);

$$
\frac{dX}{dt} = \frac{\beta}{1 + Y^n} - X \quad ,
$$
$$
\frac{dY}{dt} = \frac{\beta}{1 + X^n} - Y \quad .
\tag{1}
$$

Here, β is the effective rate of protein synthesis and n is the Hill coefficient, which represents the degree of competence. The number of repressors are represented in the unit of their dissociation constants and time is rescaled by degradation rate of proteins (*Gardner et al., 2000*; *Carson and Cobelli, 2000*; *Elowitz and Stanislas, 2000*). Biologically-reasonable values were chosen for the parameters used in our simulation such that Eq 1 would be bi-stable (following (*Gardner et al., 2000*)). This bistable regulatory network has two attractors corresponding to its stable steady states. Based on the amount of proteins at the cell division time, the cell can be in the domain of each attractors, which determines its fate. Depending on the intensity of inhibitory effects of TFs (through the values of constants in the Hill function (*Gardner et al., 2000*)), the two domains of attractors could be equal or not (component #5). Fig 5 shows an example of such behavior in our cell aggregation model. Movie S1 shows the changes in the distribution of TFs in cells around their attractors during the emergence of generation 12.

Figure 5. As cells grow, they stochastically explore the phase-plane around their attractor (as depicted in Fig 1) – i.e., over time the values for transcription factors X (a) and Y (b) for each cell fluctuate around the attractor that was determined when the cell was born. These fluctuations can result in a cell moving away from its original attractor towards the other attractor, such that it will be more likely for its daughters to have phenotypes different from their parent (the blue and orange trajectories). Results are based on 512 cells that descended from a single cell in the cell aggregation model. The trajectories follow the TFs counts during their lifespan.

Population growth algorithm

Simulation starts with a single cell with phenotype A. Each iteration in the simulation can be divided into four steps:

1. *Cell growth*: In this step, cells grow linearly in size. Simultaneously, the cytoplasmic content of each cell fluctuates in a stochastic fashion (component #1). The repressor proteins inside the cytoplasm interact with each other and their numbers, X and Y, are updated; however, because of their low copy numbers, instead of deterministic equations (Eq 1), their fluctuations are captured by the Gillespie algorithm (*Gillespie, 1977*) as a stochastic dynamics for discrete values. According to this algorithm, a probability of occurrence will be assigned to every biochemical reaction in the system. Every protein (X or Y) is produced with a probability according to the first term on the right hand sides of the Eq 1. As the number of protein X increases, it further represses the production of protein Y and vice versa. Every protein degrades according to its number. In every step of the Gillespie algorithm, one of the above reactions occurs and the time will be updated. The process continues until the number of proteins reaches a steady state.

2. *Cell division*: Even after the number of proteins in a cell reaches the steady state, the cell continues to grow. The growth stops only after the cell reaches a critical size. At this point the cell divides into two daughter cells. The content of the mother cell is distributed among her daughters according to a uniform distribution. In reality and in the presence of active transportation, one can still expect a uniform distribution of molecules in the cytoplasm (*Huh and Paulsson, 2011*), making this assumption biologically reasonable. The position at which cell division occurs is randomly chosen based on a normal distribution (component #2). At the time of birth, the phenotype of each newborn cell is determined based on the cytoplasmic contents (number of key proteins, X, and Y at the time of birth) inherited from the mother cell (component #3). During the cell growth, the number of each protein has a stochastic trajectory in the domain of its attractor and finally it will reach its steady state. In this model, phenotypic change is reversible, meaning that the phenotype can change between the two possible states over generations. Since in our simulations, daughter cells have similar volumes, we consider the number of proteins distributed between them, and not their concentrations.

3. *Relaxation*: After a cell divides, the cells push each other outwards to make room for the new daughter cells (*Kreft et al., 2001*). Simulation proceeds by repeating the steps #1-3. It is worth noting that, without considering self-organization, the process described above would result in a disordered blob of cells.

4. *Self-organization*: To involve the self-organization phenomenon in the process of cell maturation (component #8), cells secrete some signaling molecules, with concentration C_s, which affects the propensities in the Gillespie algorithm and, consequently, the production of proteins. The signaling molecules diffuse in the medium according to the following reaction-diffusion equation:

$$\frac{\partial C_s}{\partial t} = D_s \nabla^2 C_s + k_{sp} C_B - k_{sc} \frac{C_s}{K_s + C_s}(C_A + C_B) - k_{sd} C_s \quad . \tag{2}$$

Here, k_{sp}, k_{sc} and k_{sd} represent, respectively, the rate of production, consumption and decay of the signaling molecules and D_s is the diffusion coefficient of the signaling molecules. C_A and C_B respectively show the number of cells with phenotype A and B at each point of the medium. In our simulations, we used $D_s = 10^{-11} m^2/s$, $k_{sp} = 0.01 kg^{-1} s^{-1}$, $k_{sc} = 0.0001 kg^{-1} s^{-1}$, $k_{sd} = 0.01 s^{-1}$, and $K_s = 0.01 m^{-3}$.

In these simulations, the secreting cells are those with phenotype B; hence, the production of signaling molecules is proportional to the amount of B cells. Since both phenotypes consume these molecules, the consumption depends on the number of both A and B cells. When B cells emerge, they secret signaling molecules, which diffuse in their environment. The

₃₃₆ minimum effective concentration of the signaling molecules at any location determines if a
₃₃₇ cell at that location is affected by the signal, which would decrease the production of protein
₃₃₈ X and augment the production of protein Y. Consequently, their surrounding cells would
₃₃₉ have less chance of producing protein X and their offspring is less likely to be in the domain
₃₄₀ of attraction of protein X.

Code availability

The software used to run all simulations was Matlab 2016 and the scripts are available at https://github.com/hasafdari/Noise_Driven_Cell_Differentiation (doi: https://doi.org/10.5281/zenodo.1227287).

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Author contribution

MS designed research; RT and BG contributed to the initial idea; AK wrote the manuscript; HS and CP contributed to the methods section; MS and AK contributed to the introduction and the discussion; HS analyzed the data; HS and AK visualized the results. All authors read and approved the final manuscript.

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Appendix 1

Movies

Movie S1: The change in the distribution of TFs within cells just before they they divide. Parameters used are the same as Fig 1.

Movie S2 and Movie S3 show 3-dimensional simulations of a community of cells in a layer. Simulation performed in a $L \times L \times h$ cube and starts with one cell at the centre. The cells grow in volume; after reaching a critical volume they divide and the same as two dimensional case, their cytoplasmic content distributes between the two daughter cells.

Movie S2: The emergence of heterogeneity in the population of cells as a result of the presence of noise in the process of cell growth and division. The average amount of TFs in each cell at steady state is 25. The simulation started by one cell and continues over 13 generations, $L = 130 \mu m$ and $h = 1.33 \mu m$. Since there is a single layer of cells, h corresponds to the diameter of a single cell.

Movie S3: The formation of a spatial organization as a result of the secretion of signaling molecules, which diffuse in their environment and affect the differentiation of the cells. The average amount of TFs in each cell at steady state = 25. The simulation started by one cell and continues over 13 generations, $L = 130 \mu m$ and $h = 1.33 \mu m$.

Appendix 1 Figure 1. The final frame of Movie S1

Appendix 1 Figure 2. The final frame of Movie S2

Appendix 1 Figure 3. The final frame of Movie S3