On the deformability of an empirical fitness landscape by microbial evolution

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Abstract
A fitness landscape is a map between the genotype and its reproductive success in a given environment. The topography of fitness landscapes largely governs adaptive dynamics, constraining evolutionary trajectories and the predictability of evolution. Theory suggests that this topography can be "deformed" by mutations that produce substantial changes to the environment. In spite of its importance, the deformability of fitness landscapes has not been systematically studied beyond abstract models, and little is known about its reach and consequences in empirical systems. Here we have systematically characterized the deformability of the genome-wide metabolic fitness landscape of the bacterium *E. coli*. Deformability is quantified by the non-commutativity of epistatic interactions, which we experimentally demonstrate in mutant strains on the path to an evolutionary innovation. Our analysis shows that the deformation of fitness landscapes by metabolic mutations rarely affects evolutionary trajectories in the short-range. However, mutations with large environmental effects leave these as a "legacy", producing long-range landscape deformations in distant regions of the genotype space that affect the fitness of later descendants. Our methods and results provide the basis for an integration between adaptive and eco-evolutionary dynamics with complex genetics and genomics.

30 Introduction

31 When a new genotype appears in a population its reproductive success is largely governed
32 by the environment. Although it is often thought of as an external driver of natural
33 selection, the environment can also be shaped by the population itself, for instance through
34 its metabolic activity, or through interactions with the abiotic habitat or other species (F.
35 John Odling-Smee, Kevin N. Laland, Marcus W. Feldman, 2003; Laland et al., 2014;
36 Lewontin, 1983). These population-driven environmental changes can in turn modify the
37 fitness effects of future mutations, closing in an "eco-evolutionary" feedback loop (Post and
38 Palkovacs, 2009). Eco-evolutionary feedbacks are well documented in natural (Hendry,
39 2016) and experimental populations (Jones et al., 2009), and at all scales of biological
40 organization: from the cellular scale, e.g. in the evolution of cancer (Basanta and Anderson,
41 2017) and microbial populations (Sanchez and Gore, 2013), to the organismal scale in
42 animal (Matthews et al., 2016) and plant evolution (terHorst and Zee, 2016).

43 The one-to-one "map" between each genotype and its adaptive value in a given
44 environment is known as the fitness landscape (Wright, 1932). Since populations actively
45 modify their environment, new mutations can in principle have environmental as well as
46 fitness effects. Thus, evolving populations may reshape or "deform" the fitness landscapes
47 on which they are adapting (Kauffman and Johnsen, 1991). Though they are often used only
48 metaphorically to depict or visualize adaptation, fitness landscapes are a major
49 determinant of evolution. In particular, the topography of a fitness landscape (i.e. the
50 location of fitness peaks and valleys and their connectivity) plays a pivotal role, as it
51 governs the accessibility of evolutionary trajectories (Hartl, 2014; Poelwijk et al., 2007;
52 Weinreich et al., 2006); the role of population structure on evolution (Nahum et al., 2015);
53 the degree of evolutionary convergence among populations (Van Cleve and Weissman,
54 2015); the expected role of drift, selection, and sex in the evolutionary process
55 (Moradigaravand and Engelstädter, 2012; Rozen et al., 2008); the discovery of evolutionary
56 innovations (Barve and Wagner, 2013); and the predictability of evolution (de Visser and
57 Krug, 2014), a subject of growing importance for the management of pathogens and cancer
58 treatment (Barber et al., 2015; Lässig et al., 2017; Luksza and Lässig, 2014;
59 Nourmohammad et al., 2013; Zhao et al., 2016). Given the critical role it plays in adaptation,
60 if populations do indeed change the topography of their fitness landscapes as they evolve, it
61 is imperative to understand precisely how. Do mutations that alter the environment
62 generally deform the fitness of every other subsequent mutation, or just a subset of them?
63 If the latter, where are those "deformations" localized in the genotype space, and how
64 strong are they? All of these questions remain open as the deformability (or "rubberness")
65 of fitness landscapes has never been systematically studied beyond abstract theoretical
66 models (Kauffman and Johnsen, 1991).

67 Substantial experimental evidence suggests that microbial fitness landscapes are likely to
68 exhibit deformability (Friesen et al., 2004; Gac and Doebeli, 2010; Good et al., 2017; Paquin
69 and Adams, 1983; Rosenzweig et al., 1994), making microbes an ideal system with which to
70 address this issue. Microbial metabolism leads to large-scale environmental construction
71 through the uptake and release of metabolites (Good et al., 2017; Rosenzweig et al., 1994).
72 Which nutrients are uptaken, which byproducts are produced and released, and in what
73 amounts, are all governed by the structure of the metabolic network and, therefore, by the
74 genotype (Paczia et al., 2012; Quandt et al., 2015). Therefore, new mutations that change
75 the metabolic network can also change the patterns of metabolic uptake and secretion,
76 altering the environment and potentially also the fitness of future mutations (Rosenzweig
77 et al., 1994). Microbial physiology and growth can be explicitly simulated using genome-
78 scale metabolic models (Lewis et al., 2010; O'Brien et al., 2015; Orth et al., 2011). Due to
79 their excellent predictive capabilities (Orth et al., 2011) and ability to easily and rapidly
80 screen millions of genotypes, these genome-wide metabolic models have been successfully
81 used to systematically explore the genotype space (Matias Rodrigues and Wagner, 2009).
82 Recent advances in dynamic metabolic modeling make it possible to explicitly simulate the
83 growth of microbial communities and their environmental feedbacks with evolution
84 (Harcombe et al., 2014; Mahadevan et al., 2002), making genome-wide dynamic metabolic
85 modeling of microbial genotypes a promising method to examine the deformability of
86 fitness landscapes (Fig. 1A).

87 Here we have used such an approach, as well as experiments with the bacterium *E. coli*, to
88 show that fitness landscape deformability can profoundly alter the definition of epistasis,
89 which becomes dependent on the order in which mutations occur. By systematically
90 screening the *in silico* metabolic fitness landscape of *E. coli*, we are able to offer a precise
91 view of how deformability by eco-evolutionary feedbacks plays out over short and long
92 mutational ranges.

93 ## Results

94 **Non-commutative epistasis characterizes fitness landscape deformability.** To
95 investigate the effect of metabolic secretions on the fitness landscape, we used dynamic
96 Flux Balance Analysis (dFBA) to determine the distribution of fitness and environmental
97 effects of new mutations in the local mutational neighborhood of a recently curated,
98 genome-scale metabolic model of *E. coli* (Orth et al., 2011). Our screen included all possible
99 single addition and deletion mutants (Methods), whose growth was simulated on anaerobic
100 glucose media until saturation was reached. Of all non-essential mutations, 147 (3.3%)
101 affected growth rate, either positively or negatively (Fig. 1B). All of these mutations also
102 altered the chemical composition of the environment (see Fig. 1C for a representative
103 subset; Fig. S1 for the full set, Methods), and the magnitude of the environmental and

104   fitness effects were strongly correlated (Pearson's ρ = 0.61, P<10^{-6}, Fig. S2). This suggests

105   that as new mutations fix in the population, the extracellular environment will change,

106   which in turn could alter the fitness effects of new mutations thus deforming the fitness

107   landscape.

108   We explored the extent of fitness landscape deformability in a dataset that consisted of ~

109   10^7 single and double mutants, representing the entire second-order metabolic mutational

110   neighborhood of *E. coli*. The fitness of each mutant was determined in competition with its

111   immediate ancestor as $F_M = \log([X'_M/X_M]/[X'_A/X_A])$(Lenski et al., 1991; Travisano and

112   Lenski, 1996); where X_A and X_M represent initial densities of ancestor and mutant, and X'_A

113   and X'_M their final densities after 10 hours of competition, respectively (see Methods). All

114   competitions were performed at an initial mutant frequency of 0.01. Using this measure,

115   the fitness of two mutations is expected to combine additively when they act independently

116   (Fig 1D). As shown in Fig. 1E, when two mutations without an environmental effect interact

117   with one another, epistasis (ε) will cause the fitness of the double mutant to deviate from

118   additivity. This is the usual definition of epistasis in the literature, and epistasis is, as usual,

119   invariant with respect to the order in which mutations occur (Poelwijk et al., 2007). In

120   contrast, when at least one of the single mutants has an environmental effect, the double

121   mutant experiences a different extracellular environment depending on which of the two

122   single mutants is its immediate ancestor. For example, a double mutant could crossfeed on

123   one of its possible single-mutant ancestors, but not on the other (Fig. 1F). The result is a

124   gene-by-environment-by-gene (G×E×G) interaction in which the magnitude of epistasis

125   depends on the order in which mutations occur. In other words, epistasis becomes non-

126   commutative. The value of that non-commutative fitness shift (δ) characterizes the

127   deformation of a two-step mutational trajectory(Fig. 1F).

128   **Deformability in the path to an evolutionary innovation in *E. coli*.** To experimentally

129   validate this concept and assess the potential relevance of landscape deformability in

130   experimental evolution, we studied two mutations on the path to the evolutionary

131   innovation of strong aerobic growth on citrate (Cit^{++}) in the Ara-3 population of the *E. coli*

132   Long-Term Evolution Experiment (LTEE)(Blount et al., 2008). The two principal mutations

133   underlying this phenotype are known to have profound ecological consequences,

134   suggesting that non-commutative epistasis may be present (Fig. 2A). The first mutation is a

135   tandem amplification overlapping the citrate fermentation operon, *cit*, which occurred after

136   31,000 generations. This amplification caused aerobic expression of the CitT transporter,

137   producing a weak citrate growth phenotype (Cit$^+$)(Blount et al., 2012). CitT is an antiporter

138   that imports citrate, which is present in large amounts in the LTEE's DM25 growth medium,

139   while exporting intracellular C_4-dicarboxylate TCA intermediates, including succinate and

140   malate (Quandt et al., 2015), thereby increasing their concentration in the extracellular

141   environment. A subsequent mutation causes high level, constitutive expression of DctA, a

142 proton-driven dicarboxylic acid transporter. This mutation refines the Cit$^+$ trait to Cit^{++} by
143 allowing recovery of the C_4-dicarboxylates released into the medium by both the progenitor
144 and the double mutant itself during growth on citrate (Quandt et al., 2014) (Fig. 2A). We
145 reasoned that these mutations together enable the exploitation of environments built by
146 progenitor strains, producing a stronger increase in fitness than expected in the absence of
147 environmental construction (Fig. 2B). In contrast, had the DctA mutation occurred prior to
148 the CitT-activating duplication, it would have conferred no fitness benefit, and would not
149 have produced any changes in the environment relative to the ancestral strain (Fig. 2B).

150 We tested this prediction by performing competitive fitness assays with different
151 combinations of a spontaneous Cit$^-$ mutant and *dctA$^-$* knockout strains derived from ZDB89,
152 a 35,000 generation Cit^{++} clone that possesses both the DctA-activating and CitT-activating
153 mutations (see Methods). Competitions were carried out with equal volumes of each
154 combination of competitors, and relative fitness determined using colony counts obtained
155 after 0 and 24 hours of growth (Lenski et al., 1991). In parallel, we used dynamic FBA
156 modeling to simulate these competitions, relying solely on known parameters from the
157 experiments, as well as published parameters pertaining to the physiology of *E. coli* (Gallet
158 et al., 2017; Harcombe et al., 2014)(see Methods). Confirming our expectations, dynamic
159 FBA predicts strong non-commutative epistasis (δ =1.50) (Fig. 2C). This is confirmed by the
160 experimental results (δ=1.78±0.15) (Fig. 2D). The agreement between the empirically
161 calibrated computational model and the experiments is not only qualitative but
162 quantitative: with no fitting parameters, dynamic FBA is predictive of the outcome of the
163 experimental pairwise competitions, explaining 52% of the variance in colony counts from
164 all experiments (N=120; Fig. S3).

165 **Short-range deformability in *E. coli* is weak and rare.** Although the above examples
166 demonstrate the potential presence of fitness landscape deformability, its pervasiveness in
167 empirical fitness landscapes remains unclear. To shed light onto this question, we screened
168 the entire second order mutational neighborhood of *E. coli* using our computational model
169 (Fig. 3A). In Fig. 3B we represent all pairs of mutations that exhibit deformability as nodes
170 in a network that are connected if their non-commutative fitness shift (δ) is larger than 1%
171 of the fitness effects (F_{MAX}). These represent only a small subset (203/3343, or 6.1%) of all
172 epistatic interactions, which for the most part are not altered by the environmental effects
173 of mutations.

174 Non-commutative interactions also tend to be unevenly distributed: most of the mutations
175 do not deform the fitness of any other mutation, and only 15 of them (0.3% of all), deform
176 the fitness of 5 or more other mutations (Fig. 3B-C). These few highly connected "hubs" on
177 the network tend to be the mutations with the strongest environmental effects (Fig. S4;
178 Pearson's correlation = 0.79, P<10^{-6}). Non-commutative epistatic effects also tend to be

179   small in magnitude (Fig. 3D); only 1.6% (55/3343) of epistatic pairs have a non-
180   commutative epistatic shift larger than 10% of the total fitness increase ($\delta/F_{MAX} > 0.1$, Fig.
181   3D). This reveals that deformability of the local mutational neighborhood of the *E. coli*
182   metabolic landscape is both generally weak, rare, and highly anisotropic (i.e. non
183   homogenous), with deformations limited to localized directions in genotype space.

184   **Long-range deformability of the *E. coli* metabolic fitness landscape.** The low
185   deformability of the local mutational neighborhood could be explained by the strong
186   genetic similarity between the mutants and the ancestral genotype: genotypically close
187   descendants will rarely be able to use metabolites that are discarded by their immediate
188   ancestors. By the same logic, one may predict that over longer mutational distances
189   metabolic differences might accumulate that enable the use of extracellular metabolites
190   that are left as a "legacy" by previous mutations. Thus, we hypothesize that changes to the
191   extracellular environment produced by a given mutation will primarily deform the fitness
192   landscape at distant positions on the genotype space.

193   To test this hypothesis, we set out to introduce a mutation with a strong environmental
194   effect and measure the deformation it causes at different distances in the genotype space.
195   We chose the ACKr mutation (the deletion of the acetate kinase gene), which as shown in
196   Fig. 1C modifies the environment by releasing large amounts of lactate at the expense of
197   lower secretions of formate, acetate and ethanol. To quantify the deformation introduced
198   by this mutation, we compared the fitness of thousands genotypes at increasing mutational
199   distances from the ancestor, in competition with either the ancestor *E. coli* model (A) or the
200   ACKr mutant (M) (Fig. 4A). The results are shown in Fig. 4B-C. Consistent with our
201   hypothesis, we found that the fitness landscape deformation introduced by ACKr is
202   negligible at short genotypic distances from it (e.g. 16 mutations or less), but it becomes
203   stronger at longer distances. Fifteen other mutants (M) in addition to ACKr were also
204   tested, with similar results (Fig. S5). Furthermore, by comparing the growth rate of
205   thousands of genotypes in the environments constructed by A and M, we found that
206   increasingly distant genotypes become increasingly sensitive to the differences between
207   both environments. This explains the observed pattern of deformation as a function of
208   genotypic distance (Fig. 4D, Fig S5).

209   Discussion

210   Darwin was perhaps the first to recognize that the environment experienced by a
211   population can also be shaped by the population itself (Darwin, 1881). Long neglected, this
212   concept was revived by Lewontin (Lewontin, 1978, 1983), and has gained added
213   momentum in recent years as the important role played by eco-evolutionary feedbacks in
214   both ecology and evolution has become better appreciated (Laland et al., 2014; Post and

215   Palkovacs, 2009; Rudman et al., 2018). Due to technical limitations, experimental studies of
216   eco-evolutionary feedbacks and the adaptive dynamics models that seek to explain them
217   often lack explicit, genome-wide representations of the adaptive landscape, in particular
218   with regard to complex traits and gene-gene interactions (Rudman et al., 2018). The exact
219   state of the environment, which is intrinsically complex and multi-dimensional (Lawrence
220   et al., 2012) , is also rarely measured experimentally or explicitly included in eco-
221   evolutionary models. In return, and in spite of early abstract models of species coevolution,
222   which introduced the idea of fitness landscape deformability (also referred to as
223   "rubberness", ((Kauffman and Johnsen, 1991; Solé and Sardanyés, 2014)), and the many
224   examples of the importance in co-evolutionary arms races and other forms of coevolution
225   (Morran et al., 2011; Stern and Sorek, 2011; Strauss et al., 2005), genotype-fitness maps
226   have largely ignored the effects of eco-evolutionary feedbacks. This is particularly
227   important in light of the argument, made by many authors, that the deformability of fitness
228   landscapes (or its consequences, in the form of frequency dependent selection) would
229   erode their practical and conceptual utility (Doebeli et al., 2017; Moran, 1964; Schuster,
230   2012).

231   The work presented above seeks to reconcile both perspectives on empirical grounds.
232   Encouragingly, our results show that fitness landscapes may retain their local properties
233   even in the presence of mutations that significantly alter the environment. By
234   systematically mapping an empirical fitness landscape, we have found that ignoring
235   deformability and assuming a "rigid" (i.e. non-deformable) landscape is a good
236   approximation over short genotypic distances. This is because closely related genotypes are
237   unlikely to differ from one another in their physiological response to the built environment.
238   In contrast, over longer mutational distances, landscapes are likely to be affected by
239   environmental construction, an effect that is shaped by complex genetic interactions. This
240   suggests a new, ecologically-mediated mechanism by which historical contingency may
241   shape downstream evolution even in clonal populations. In summary, our work suggests
242   that depending on the resolution, fitness landscapes can behave as either a fixed externally
243   determined topography on which adaptation proceeds, or become a dynamic property of
244   the populations adapting on them (Doebeli et al., 2017; Moran, 1964).

245   Our results indicate that simulating cellular adaptive dynamics with an explicit and
246   biologically realistic representation of the genotype-phenotype map is within reach. Such
247   an approach will shed light into the role played by dynamic niche construction on cellular
248   evolution. We believe that it will also create multiple opportunities to incorporate genomics
249   into the study of eco-evolutionary dynamics, and thus reveal the genetic, biochemical and
250   environmental constraints that simultaneously govern the ecology and evolution of cellular
251   populations.

252 Acknowledgments

264 METHODS

265 **Reconstruction of a prokaryotic genotype space.** All *in silico* explorations of genotype
266 space in this work took as a reference the *E. coli* model iJO1366 and consisted of both gene
267 additions or deletions. Gene deletions were performed by constraining both upper and
268 lower bounds of the reaction to zero. Gene additions were performed from a set of all
269 known prokaryotic reactions. We used the BiGG database (King et al., 2016) to compile a
270 dataset of all known reactions found across prokaryotic species. Conflicts in reaction
271 directionality were resolved as follows i) if a reactions is found in the well benchmark *E.*
272 *coli* iJO1366 model, use the properties given by this model, ii) if a reaction conflicts in
273 directionality, only accept directions found across all models (e.g. if there is one model
274 where a given reaction is irreversible, we set it as irreversible). We used this dataset to
275 create a "universal" metabolic model that included all reactions found in *E. coli* iJO1366 as
276 well as a set of all potential novel reactions. We removed reactions that would lead to
277 erroneous energy-generating cycles using the ModelFit algorithm (Fritzemeier et al., 2017).
278 The algorithm was constrained to conserve reactions present in the original *E. coli* model.
279 Removing any futile cycles from this "universal" model ensures that there will not be any
280 futile cycles in any subset. The resulting network contains 4999 metabolic reactions and
281 585 nutrient uptake or sink reactions, of which 2758 and 255 were not found in the
282 original *E. coli* model.

283 ***In silico* simulation of growth through metabolic modeling.** Dynamic Flux Balance
284 Analysis simulations were performed using the COMETS package ("Computation of
285 Microbial Ecosystems in Time and Space", (Harcombe et al., 2014)) and the gurobi
286 optimizer software. For computationally intensive simulations, we used the High
287 Performance Facility at Yale University. For standard (non dynamic) FBA simulations, we
288 used the COBRApy python package (Ebrahim et al., 2013). Both Dynamic and Standard FBA
289 optimizations were done using the parsimonious algorithm, in which a first optimization is

290   done to maximize biomass yield, and a second one fixes this yield and minimizes total
291   fluxes throughout the network (Lewis et al., 2010). Unless otherwise stated, the default V_{max}
292   was set in dynamic FBA simulations to 10 mmol×gr^{-1}×hr^{-1} for all uptake reactions. Inorganic
293   ions and gases where kept at high concentrations and where kept undepleted throughout
294   the simulation (i.e lower bound : -1000 mmol×gr^{-1}×hr^{-1}, amount of metabolite: 1000
295   mmol). This was done to constrain our analysis to situations where growth is limited only
296   by uptake of carbon sources. The unbounded nutrients are: ca2_e, cbl1_e, cl_e, co2_e,
297   cobalt2_e, cu2_e, fe2_e, fe3_e, h_e, h2o_e, k_e, mg2_e, mn2_e, mobd_e, na1_e, nh4_e, ni2_e,
298   pi_e, sel_e, slnt_e, so4_e, tungs_e, zn2_e. For the citrate simulation to avoid oxygen, nitrogen
299   or proton limitation uptake was unconstrained by setting the vmax to 1000 mmol×gr^{-1}×hr^{-1}.
300   Analysis of results was performed using GNU R language (R Core Team, 2017).

301   **Fitness, environmental effects and deformability measurements.** To measure fitness,
302   we use here (in both experiments and simulations) the Malthusian fitness measure that
303   allows for a quantitative comparison across environments (Wagner, 2010). Fitness of
304   mutant M relative to ancestor A is therefore given as $F_M = \log([X'_M/X_M]/[X'_A/X_A])$, where X
305   and X' represent initial and final densities. For a pair of mutations, deformability can be
306   then measured as $\delta_{ij} = F_{ij}^{(i)} + F_i^{(A)} - (F_{ij}^{(j)} + F_j^{(A)})$, where $F_x^{(y)}$ represents the fitness of genotype
307   *x* in competition with genotype *y*. To compute environmental effects of mutations, the
308   difference in secretion profile of mutants (as shown in Fig. 1C and Fig. S1) is computed for a
309   given released molecule as sign(D) * (log(D)+1) where D is the amount released by the
310   mutant minus that secreted by Ancestral *E. coli*. This log-modulus transformation (John and
311   Draper, 1980) is applied to help visualization of the generally small differences in released
312   amount, which can be either positive or negative. To measure environmental effect of a
313   mutation (as used in Fig. S2 and Fig. S4) , we use the Euclidean distance in the profile of
314   released metabolic byproducts between a mutant and the *E. coli* ancestor using standard
315   Flux Balance Analysis (Ebrahim et al., 2013).

316   **Simulation of the fitness landscape of *E.coli* citrate utilization.** Starting with *E.coli*
317   model iJO1366 we constructed metabolic models of the four mutants necessary to predict
318   the fitness landscape involved in the evolution of aerobic citrate utilization in the Ara3
319   population of the LTEE. Unlike the LTEE ancestral strain REL606 (and *E. coli* generally),
320   which possess the necessary genes for citrate utilization but do not express them in aerobic
321   conditions, iJO1366 is able utilize both citrate and succinate if these reactions are
322   unbounded (as FBA optimizes precisely regulation). Thus, the ancestral phenotype was
323   recreated by knocking out three reactions CITt7pp (*citT*), SUCCt2_2pp (*dctA*) and
324   SUCCt2_3pp (*dcuA* or *dcuB*). The reactions encoded by the first two genes (*citT* and *dctA*)
325   are known to be involved in the evolution of citrate utilization in the LTEE whereas *dcuA*
326   and *dcuB* are involved in dicarboxylate uptake in anaerobic conditions and are inactive in
327   aerobiosis (Six et al., 1994). This triple knockout represents the pre-citrate *E. coli* ancestor
328   strain. The addition of CITt7pp simulates the promoter capture and consequent aerobic
329   expression of CitT. Similarly, the addition of SUCCt2_2pp is equivalent to the first mutation
330   (aerobic expression of *dctA*). We used dynamic FBA to predict the fitness landscape of these
331   two mutations, calibrating the simulations to reflect the the experimental conditions. This
332   involved i) setting the *in silico* media to reflect DM25 minimal glucose media (0.139mM
333   glucose, 1.7mM citrate). Aerobic condition was simulated by keeping oxygen (o2_e)

334 undepleted. ii) using published parameters pertaining to the physiology of *E. coli*
335 (Harcombe et al., 2014) and iii) estimating the initial biomasses of each mutant prior to
336 competition. Initial biomass for citrate simulations was determined using initial plate
337 counts from pairwise competitions experiments (see also Fig. S3). We assume that average
338 cell dry mass is $3.9 * 10^{-13}$ g which is the empirically measured cell dry mass of REL606 the
339 ancestral strain used in the LTEE (Gallet et al., 2017)

340 ***E. coli* Long-Term Evolution Experiment.** Briefly, twelve populations of *E. coli* B were
341 founded in 1988 from clone REL606. The populations were initially identical, save for half
342 having a mutation that permitted growth on arabinose. (See below.) These have since been
343 evolved in DM25 minimal glucose medium under conditions of daily, 100-fold serial
344 transfer, and incubation at 37°C with 120 rpm orbital shaking. Samples of each population
345 are frozen every 500 generations [38]. DM25 is Davis-Mingioli broth supplemented with 25
346 mg/L glucose. (Per liter: 7g potassium phosphate dibasic trihydrate, 2g potassium
347 phosphate monobasic anhydrous, 1g ammonium sulfate, 0.5g sodium citrate, 0.01%
348 magnesium sulfate, and 0.01% thiamine.)

349 **Isolation and Preparation of Test Strains.** ZDB89 is a Cit^{++} clone isolated from the Ara-3
350 population sample frozen for generation 35,000 during the LTEE. Cit$^-$ revertants arise
351 spontaneously from Cit$^+$ and Cit^{++} clones due to recombination-mediated collapse of the
352 tandem cit amplification to the ancestral genotype at that locus. We isolated a Cit$^-$ revertant,
353 ZDB757, by first passaging ZDB89 in a glucose-only medium for five days. This passaging
354 does not constitute a selection, but nonetheless enriches for Cit$^-$ revertants by eliminating
355 the selective penalty for losing the ability to grow on citrate. Passage cultures were spread
356 on LB plates, and Cit$^-$ mutants screened for by patching colonies to LB and Minimal Citrate
357 (MC) plates to identify clones that no longer grew on citrate. The Cit$^-$ phenotype was
358 confirmed by streaking on Christensen's Citrate Agar. Recombineering with the pKO3
359 suicide plasmid (Link et al., 1997) was used to delete the *dctA* gene from ZDB89 and
360 ZDB757, producing the Cit$^+$ *dctA$^-$* and Cit$^-$ *dctA$^-$* constructs, ZDB912 and ZDB904,
361 respectively. To permit differentiation of competitors during fitness assays, we isolated Ara$^+$
362 revertants of each of the aforementioned clones and constructs. Briefly, Ara$^-$ strains lack the
363 ability to use arabinose, and form red colonies on Tetrazolium Arabinose (TA) plates, while
364 Ara$^+$ revertants are mutants with restored ability to grow on arabinose, and form white
365 colonies on TA. The ancestral strain of the Ara-3 population and its descendants are Ara$^-$.
366 We isolated Ara$^+$ revertants by plating clone or construct cultures on Minimal Arabinose
367 (MA) plates. Revertants were competed against their Ara$^-$ parents to verify marker state
368 neutrality. Clones, constructs, and revertants are listed in Supplementary Table 1.
369 Derivation of constructs and revertants are shown in Supplementary Figure S7.

370 **Experimental fitness Assays**. Fitness was assayed in pairwise competitions. Competitors
371 with opposite Ara marker states were inoculated from frozen stocks into 10 mL LB broth,
372 and incubated overnight at 37°C with 120 rpm orbital shaking to permit revival and
373 elimination of traces of glycerol cryoprotectant. To precondition the competitors, each
374 competitor revival culture was then diluted 100-fold in 0.85% saline, and 100 L of the
375 diluted culture used to inoculate 9.9 mL DM25 with ten-fold replication. These culture were
376 grown for 24 hours at 37°C with 120 rpm orbital shaking, after which they were

377   transferred via 100-fold dilution into 9.9 mL volumes of fresh DM25, and grown for another
378   24 hours under the same conditions. Ten competition cultures were prepared for each
379   competitor pairing by inoculating each 9.9 mL DM25 with 50 L of each preconditioned
380   competitor. A single replicate preconditioning culture of each competitor for each
381   competition was inoculated so that each competition was inoculated from a single
382   preconditioned culture of the competitors. Upon inoculation with the competitors, 100 L of
383   a 100-fold dilution of each was spread on TA to permit enumeration of the initial frequency
384   of each competitor. 100 L of a 1000-fold dilution was also plated for each competition
385   including at least one Cit⁺ or Cit⁺⁺ competitor. Colonies were counted following 48 hours of
386   plate incubation at 37°C. Following 24 hours incubation under the same conditions used for
387   preconditioning, 100 L of 10,000-fold dilutions of each competition were plated on TA to
388   permit final enumeration of the competitors. 100,000-fold dilutions were also plated for
389   competitions including at least one Cit⁺ or Cit⁺⁺ competitor.

390   **Exploration of deformability in the local mutational neighborhood of *E. coli*.** To
391   systematically analyze the local mutational neighborhood of *E.coli* we construct a set of
392   metabolic models consisting of every viable single and double mutation, considering both
393   additions and deletions from our universal reaction set and using as a reference the *E. coli*
394   iJO1366 model (4389 and 9636050 genotypes, respectively). We removed from the final
395   analysis essential genes, as well as those genes leading to artifacts (H_2 or CO_2 limitation).
396   We used dynamic flux balance analysis to simulate competition assays of each mutant with
397   its immediate ancestor. The simulations assayed co-culture growth during 10hr, a period
398   during which glucose was never exhausted, i.e. growth remained exponential, to simplify
399   the interpretation of the results. All simulations were done with the mutant starting at low
400   frequency (1%, 10^{-10} gr. dry cell weight, for 9.9×10^{-9} gr. for the ancestor) in anaerobic
401   glucose minimal media (unless otherwise stated, see detailed parameters in supplement
402   and supplementary tables ST2-ST4).

403   **Simulation of long-range fitness landscape deformation.** In order to explore the long-
404   range effects of landscape deformation, we started from a one-step mutation from ancestor
405   *E. coli* model and performed random walks in genotype space by sampling 1024 mutations
406   (without replacement) among both deletions and additions. To speed-up simulations, the
407   sampling procedure ignored all reactions that were essential in a minimal model built by
408   sequentially removing reactions while possible, following (Pál et al., 2006)). At regular
409   intervals, fitness was measured as before in competition with the mutant and the ancestor
410   (wild-type) using dynamic flux balance analysis (COMETS (Harcombe et al., 2014)). To
411   determine the growth rates of genotype in ancestral vs mutant environments we repeated
412   this procedure except at each step, growth rate was measured in the environment provided
413   by the mutant and the ancestor using standard flux balance analysis (COBRApy (Ebrahim et
414   al., 2013)). These environments were simulated by setting uptake rates for each secreted
415   metabolites to the excretion rate of the respective ancestor.

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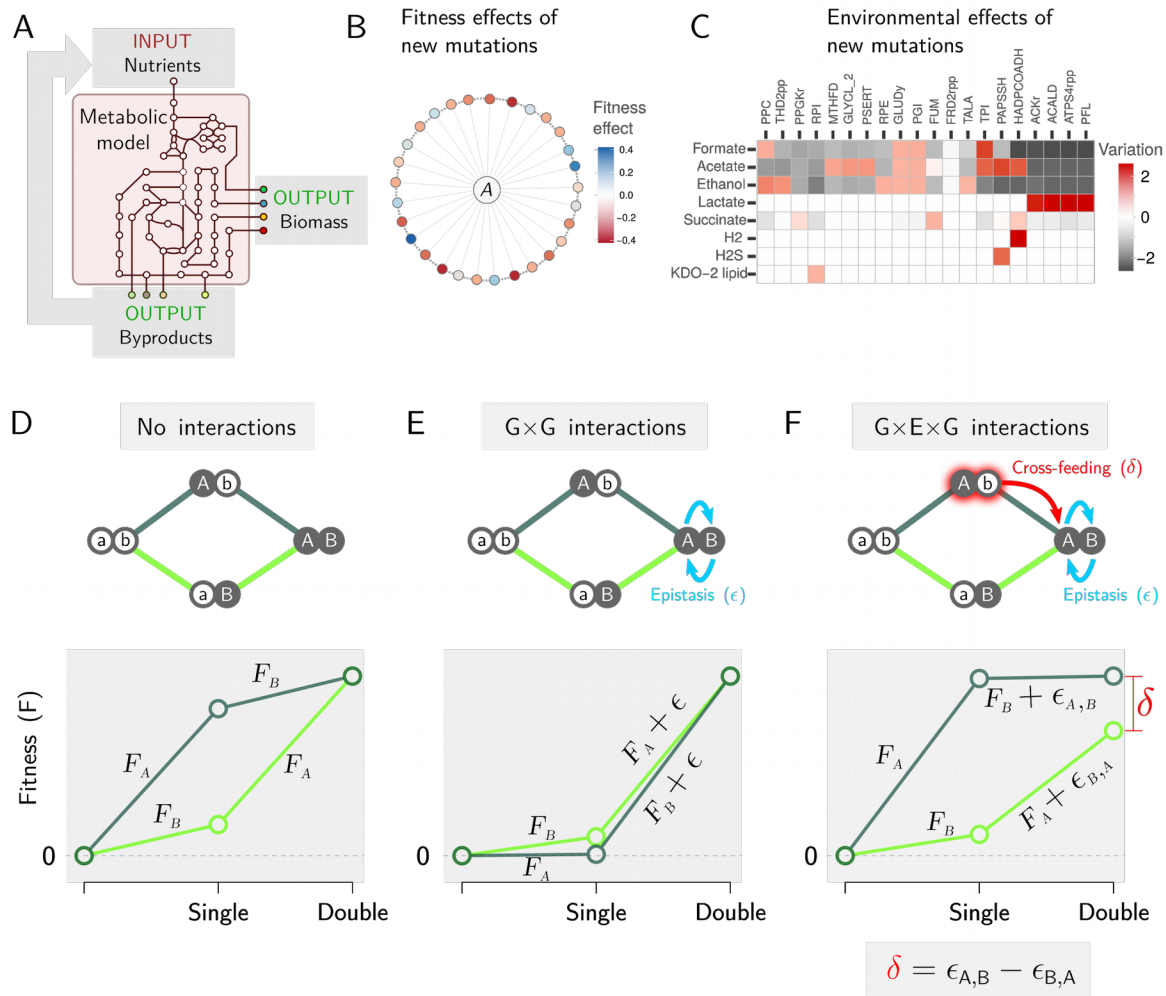558 Combinations Design. Trends Cancer Res. *2*, 144–158.

559 **FIGURES**

560 **Fig. 1. Measuring deformability in the *E. coli* metabolic fitness landscape. A** . Schematic
561 depiction of dynamic Flux Balance Analysis (dFBA) simulations. Given an input in the form of
562 nutrients, metabolic fluxes through an explicit and empirically curated metabolic model are
563 optimized to maximize the biomass growth yield. The optimal metabolic fluxes produce metabolic
564 byproducts that are released to the external environment, becoming part of it and of future inputs.
565 **B.** A small subset of genotypes differing from our *E. coli* metabolic model in a single mutation (an
566 added or deleted reaction), colored according to its effect on fitness in competition with the
567 ancestor (A). **C.** Environmental effects of a subset of mutants, expressed as the variation in the
568 profile of secreted metabolites compared to ancestral *E. coli* genotype (computed as log-modulus
569 transformed difference in the amount of a given secreted molecule; see Methods). Mutant names
570 given as reaction names in BIGG database notation. **D.** Two loci fitness landscape in the absence of
571 gene-gene interactions, where the fitness of each mutation is the same in both the ancestral and the
572 other mutant's genetic backgrounds. Fitness of each genotype was calculated in direct competition
573 with its immediate ancestor. Mutations A and B correspond to the addition of GLYCL_2 (in BiGG
574 database notation) glycine cleavage system) and AIRCr (phosphoribosylaminoimidazole

575   carboxylase) respectively. **E.** Two-loci fitness landscape with gene-gene interactions giving rise to
576   epistasis ($\boldsymbol{\varepsilon}$). Mutations A and B were respectively SO3R (sulfite reductase) and PAPSSH
577   (phosphoadenylylsulfatase), simulated in a constant environment. **F.** Two-loci fitness landscape
578   where one of the mutants transforms the environment, leading to cross-feeding towards the double
579   mutant. Mutations A and B correspond to the addition of PAPSSH and HADPCOADH (3-
580   hydroxyadipyl-CoA dehydrogenase), simulated in conditions where environmental construction
581   was allowed. In addition to regular epistasis, this leads to a non-commutative epistatic shift ($\boldsymbol{\delta}$).
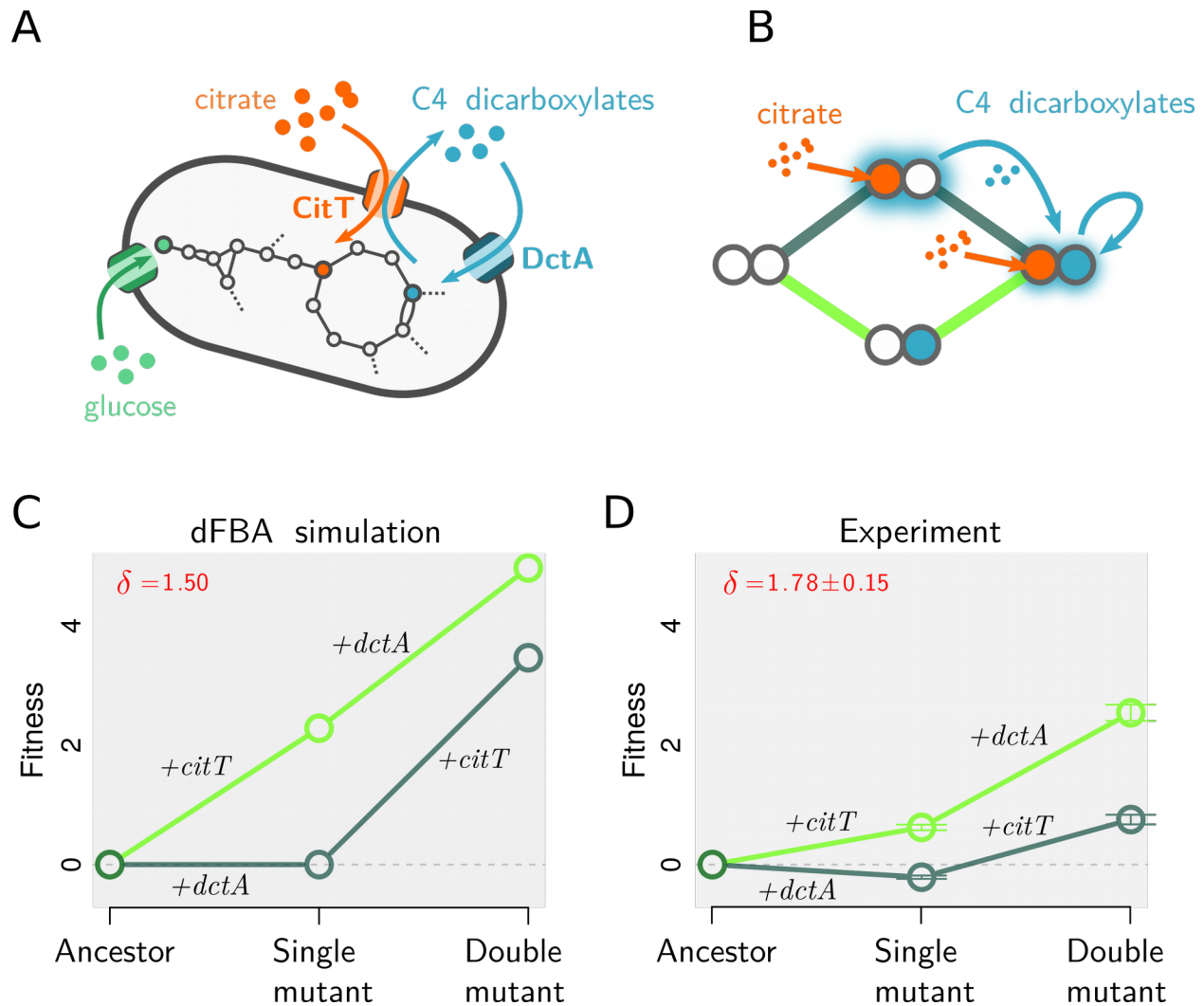
Fig. 2. Non-commutative epistasis in the evolution of aerobic citrate use in *E. coli*. A. Function of the two transporters involved in the innovation of strong aerobic growth on citrate (Cit^{++}) in *E. coli*. CitT is an antiporter that exchanges extracellular citrate for internal C$_4$-dicarboxylates (e.g. succinate, fumarate, malate). DctA is a carboxylic acid transporter that imports C$_4$-dicarboxylates from the extracellular space into the cytoplasm. **B.** The two possible mutational trajectories leading to the Cit^{++} trait. If the mutation leading to expression of *citT* (+*citT*) occurs first, it will transform the environment leading to cross-feeding towards the double mutant. This should not occur if the *dctA* overexpression mutation (+*dctA*) occurs first. Simulated (**C**) and experimentally measured (**D**) fitness landscapes in the DM25 medium used in the LTEE (see Methods). Experimentally obtained values are reported as mean ± SEM (N=10).
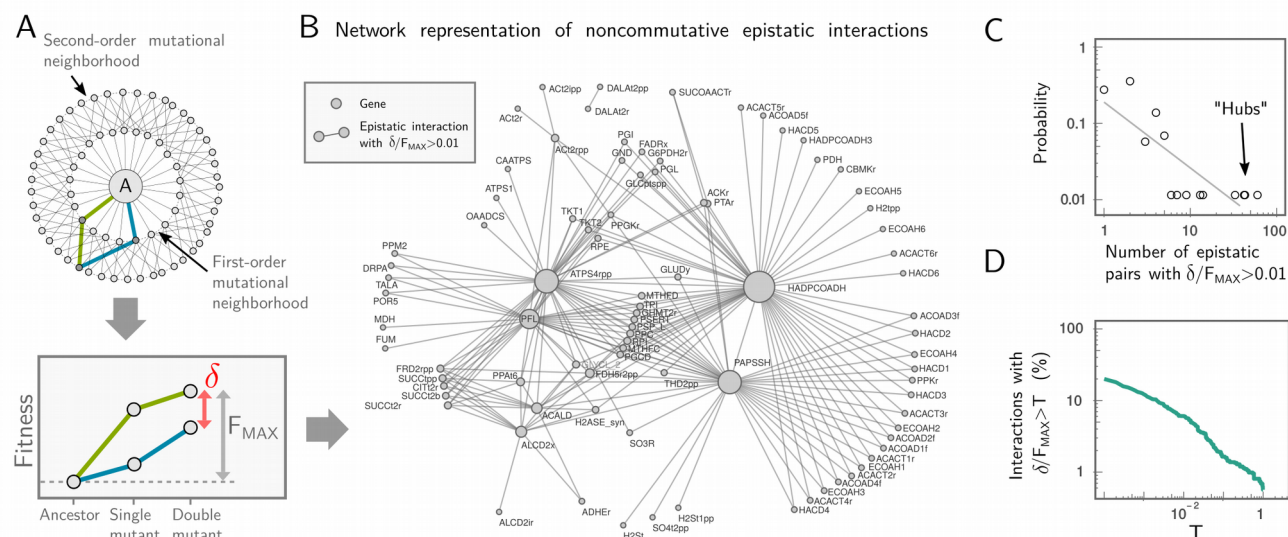
Fig. 3. Short-range deformability in *E. coli* is rare, weak, and directional. A Systematic exploration of the second-degree mutational neighborhood of *E. coli*. We used our model to exhaustively simulate every possible mutational trajectories starting from the "ancestral"(A) metabolism and ending in each double-mutant, including all nonessential reaction deletions and additions. Non-commutative epistasis (δ) was measured for each pair of mutants, and normalized by F_{MAX}, i.e. the maximal cumulative fitness effect of the double mutant: $F_{MAX} = \max[\ |F_i^{(A)} + F_{ij}^{(i)}|, |F_j^{(A)} + F_{ij}^{(j)}|\ ]$, where e.g. $F_x^{(y)}$ denotes the fitness of mutant x when invading its immediate ancestor y at low frequency (see also Methods for simulation details). **B.** Network representation of all non-commutative epistatic pairs. Nodes represent single mutations, and two nodes are joined by edges if $\delta/F_{MAX} > 0.01$ for that epistatic pair. Node names represent reaction names from BIGG database. **C.** Distribution of deformability for each gene in the network, measured as the number of other genes with which it has a non-commutative epistatic interaction. **D.** Strength of all non-commutative epistatic interactions. Percentage of epistatic pairs with $\delta/F_{MAX} > T$ as a function of T.

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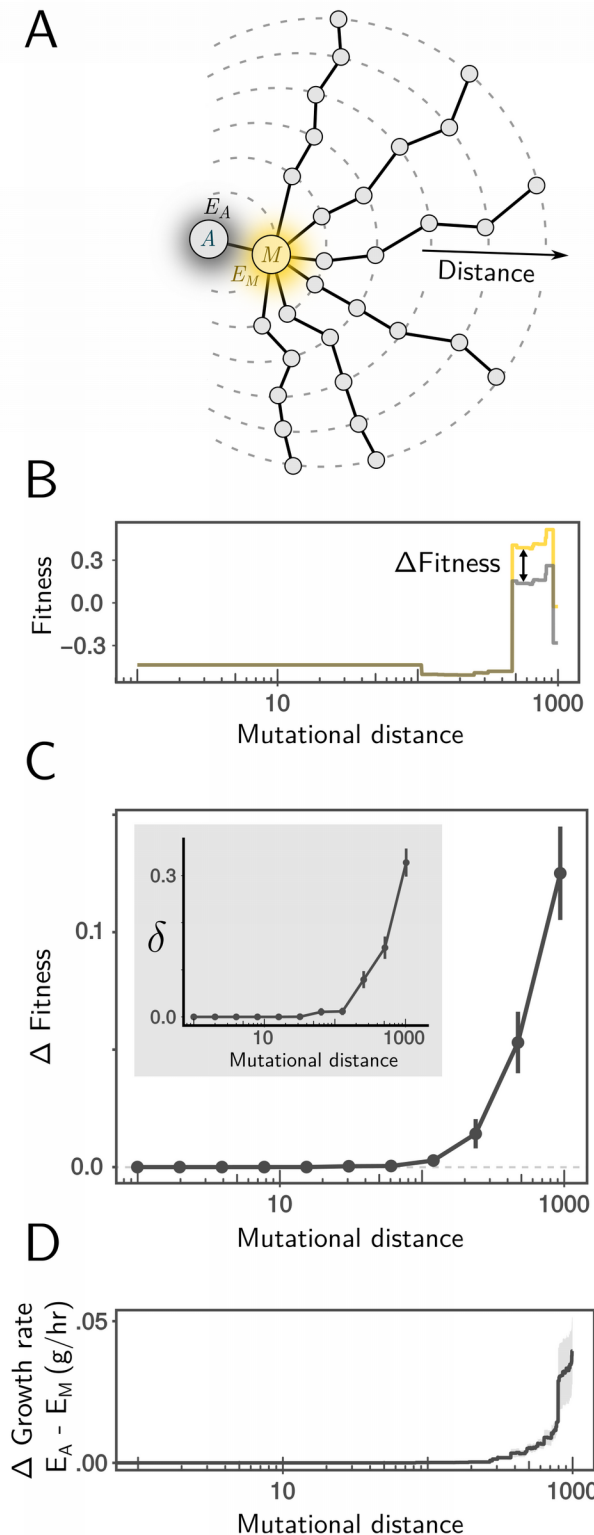618
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Fig. 4. Long-range deformability of the *E. coli* metabolic fitness landscape. A. We performed random walks (length = 1000 mutations) in genotype space starting from a *E. coli* ancestor (A; gray) and first passing through a mutant (M; orange) with large environmental effect. **B-C.** Fitness of mutants along these random walk was measured in competition with A (gray), and in the environment it generates (E_A), as well as in competition with M (orange) in the environment it generates (E_M). In **B** we show the result for a single example random walk. Note that fitness in competition with M is shifted by the difference in fitness between M and A so all observed differences in fitness (ΔFitness) are due to deformation. In **C** we plot the average ΔFitness at increasing mutational distances from A in over N=100 random walks (error bars represent SEM; N=100). The non-commutative epistasis δ exhibits a similar trend as ΔFitness (inset). **D.** Average difference (absolute value) in growth rate between environments E_M and E_A (in grams of dry cell weight × hr^{-1}) at varying genotype distances (gray line, shading represents SEM; N=100).