The Influence Of Social Behavior On Selection and Spread of Virulent Pathogen Strains

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1   Abstract

Virulence measures the degree of harm inflicted by a pathogen on its host, and mathematical models including features of pathogens such as virulence have long been studied in an effort to better understand disease dynamics. Interventions like social distancing or vaccination have proven effective in reducing the size of epidemics and in some cases eliminating a disease from a population. Such interventions depend partly for their success on social processes that respond adaptively to disease dynamics, but mathematical models of virulence evolution typically assume that human behaviour is fixed. Here, our objective is to model the influence of social behaviour on the competition between pathogen strains with differing virulence. We couple a compartmental Susceptible-Infectious-Recovered model for a resident pathogen strain and a mutant strain with higher virulence, with a differential equation of a population where individuals learn to adopt protective behaviour from others according to the prevalence of infection of the two strains and the perceived severity of the respective strains in the population. We perform invasion analysis, time series analysis and phase plane analysis to show that perceived severities of pathogen strains and the efficacy of infection control against them can greatly impact the invasion of more virulent strain. We demonstrate that adaptive social behaviour enables invasion of the mutant strain under plausible epidemiological scenarios, even when the mutant strain has a lower basic reproductive number than the resident strain. Surprisingly, in some situations, increasing the perceived severity of the resident strain can facilitate invasion of the more virulent mutant strain. Our results demonstrate that for certain applications, it may be necessary to include adaptive social behaviour in models of the emergence of virulent pathogens, so that the models can better assist public health efforts

to control infectious diseases.

2 Introduction

Modern approaches to developing a theory of the spread of infectious diseases can be traced to 1927 when Kermack and McKendrick developed an integro-differential equation model now widely described as the SIR (Susceptible-Infected-Recovered) model [1]. The model tracks changes in the number of individuals susceptible to an infection $S(t)$, the number of infected individuals $I(t)$, and (implicitly) the number of recovered individuals $R(t)$. SIR models are useful in cases where individuals recover from a disease and gain life long immunity (e.g. measles). For other diseases, individuals become immediately susceptible again upon recovery (e.g. Influenza) and therefore they would be better analyzed with an SIS model (Susceptible-Infected-Susceptible). There also exist diseases that place individuals in an exposed class where they are infected but not immediately infectious (e.g. Tuberculosis) and could be modeled through an SEIR system (Susceptible-Exposed-Infectious-Recovered) or SEIS (Susceptible-Exposed-Infectious-Susceptible). Several frameworks were designed to study the spread of infectious diseases. Some prominent examples include: partial differential equations [2], network models [3], metapopulation models [4], and stochastic models [5]. A universal conception to all types of models is the basic reproductive number $\mathcal{R}_0$ [6] (the number of secondary infections generated by one infectious individual during their infectivity period in an otherwise susceptible population). $\mathcal{R}_0$ has traditionally been used to determine whether a particular disease invades a population and becomes endemic or dies out.

Parasites (including viruses, helminths, protozoa, bacteria, *etc*) vary widely in terms of how much they harm their host [7]. Virulence of a parasite can be defined as the rate at which it induces host mortality [8]. Virulence is often positively correlated with death of the host due to infection [9]. It was initially believed that hosts and parasites co-evolved to a state of commensalism (whereby parasites benefit from their host without harming them) [10, 11] but this hypothesis was later challenged [12]. Studies have shown that, while hosts evolve, parasites evolve to maximize their evolutionary fitness [13]. One of the most common hypotheses is that a trade-off exists for between-host transmission and virulence. To increase its probability of transmission, the parasite must replicate within the host. This replication, on the other hand, must be controlled because otherwise it might lead to the host's death and therefore prevent transmission. However, other trade-offs have been suggested, such as between transmission rate and host recovery rate [14]. Moreover, complicated host life cycles imply that many other types of trade-offs are also possible [15], and the presence of multiple trade-offs may complicate the relationship between transmission rate and virulence [16].

Pathogens evolve through natural selection operating on mutation and recombination [17]. Several models

have been developed to study the evolution and epidemiology of multiple species of parasites in a population or different strains of the same species [18]. Some models focus on between-host competition while some others on within-host competition [19]. Bull suggested in the 1990s that coupling inter-host and intra-host dynamics in models may be desirable [20]. Models linking between-host transmission dynamics to within-host pathogen growth and immune response are now becoming commonplace [19, 21, 22, 23, 24]. One such approach is to link host viral load (which is a necessary condition of virulence) to the between-host transmission rate. Other factors influencing virulence include mode of transmission and network connectivity.

In mathematical models, virulence is often treated as a fixed model parameter expressing the excess mortality rate caused by the pathogen. For instance, virulence has been assumed to depend on the intrinsic reproductive rate of the parasite [25]. Other research expresses expresses the transmission rate β and the recovery rate μ in terms of a parameter ν that represents virulence [26]. When the impact of human behaviour is discussed in such models, it is discussed in terms of hypothesized effects of human behaviour on the value of the fixed parameter representing virulence. In general, these models do not treat human behaviour as a dynamic variable that can evolve in response to transmission dynamics and influence the evolution of virulence. (A few exceptions exist, including work that allows virulence to be a function of the number of infected hosts, thus capturing a situation where the magnitude of the epidemics affects the ability of health care services to host patients [27].) However, as human responses to both endemic and emerging infectious diseases show, human behaviour can have a significant influence on how infections get transmitted. For instance, an early and well-documented example shows how the residents of the village of Eyam, England quarantined themselves to prevent the spread of plague to neighbouring villages [28]. Individuals moved to less populated areas during the Spanish Influenza pandemic in the early 20th century [29]. More recently, masks became widely used during the outbreak of the Severe Acute Respiratory Syndrome (SARS) at the beginning of the 21st century [30], and it has been shown pathogen virulence in Marek's disease can evolve in response to how vaccines are used [31].

Theoretical models of the effect of human behaviour on the spread (but not necessarily evolution) of infectious diseases are increasingly popular and tend to be either compartmental epidemic models or network simulation models [32, 33, 34, 35, 36, 37, 38]. Bagnoli *et al* [39] found that under certain conditions, a disease can be driven extinct by reducing the fraction of the infected neighbours of an individual. Zanette *et al* [40] showed that if susceptible individuals decide to break their links with infected agents and reconnect at a later time, then the infection is suppressed. Gross [41] also shows that rewiring of edges in a network (and thus social interaction) can greatly influence the spread of infectious diseases. Of the compartmental models, we focus on those that have used concepts from evolutionary game theory such as imitation dynamics [42] to describe the evolution of behaviour and its interplay with the epidemics. An example of imitation dynamics

concerns, as described in detail in [43], the effect of vaccination on the spread of infectious diseases. Each individual in the population picks one strategy and adopts it: "to vaccinate" or "not to vaccinate". The proportion of vaccinators is modelled using an ordinary differential equation and is coupled with a standard SIR model. An important aspect of behavioural models is to couple them with epidemiological processes such as transmission. This coupling creates a feedback loop between behaviour and spread of the disease. In their paper [44], Murall *et al* discuss the influence of Human PapillomaVirus (HPV) vaccines on the evolution of virulence. Their findings show that vaccination favours an increase in virulence. A Human Immunodeficiency Virus (HIV) virulence model by Massad *et al* [45] shows that reducing the number of sexual partners could possibly drive HIV to be a more benign pathogen, although subsequent work with more detailed models has suggested this evolutionary outcome may not be feasible [46].

Given that adaptive social behaviour is important in many aspects of infection transmission, we hypothesize that adaptive social behaviour can also influence selection between pathogen strains with differing virulence in ways that cannot be captured by assuming it to be represented by a fixed parameter. Our objective in this paper was to explore how behaviour and virulence influence one another, in a coupled behaviour-disease differential equation model. This approach can help us understand the effects specific social dimensions, such as level of concern for a strain or the rate of social learning, on the coupled dynamics of pathogen strain emergence and human behaviour in a situation where virulence imposes evolutionary trade-offs and is strain-specific. Instead of considering long-term evolutionary processes with repeated rounds of mutation and selection, we focus on the case of invasion of a single mutant strain with a large phenotypical difference compared to the resident strain. In the next section, we describe a model without adaptive social behaviour as well as a model that includes it, and in the following Results section we will compare their dynamics.

3 Model

We compare dynamics of a two-strain compartmental epidemic model in the presence and absence of adaptive social behaviour. Individuals are born susceptible (S). They may be infected either by a resident strain (I_1) or a mutant strain (I_2). For simplicity, we assume that co-infection and super-infection are not possible. Infected individuals can either recover (R) or die from infection. We furthermore assume that recovery from either strain offers permanent immunity to both strains. The system of differential equations representing the SI_1I_2R model in the absence of adaptive social behaviour (we will refer to this as the "uncoupled model" throughout) is given by

$$\frac{dS}{dt} = \mu - \delta S - \beta_1 S I_1 - \beta_2 S I_2,$$
$$\frac{dI_1}{dt} = \beta_1 S I_1 - (\gamma_1 + \delta + \nu_1)I_1,$$
$$\frac{dI_2}{dt} = \beta_2 S I_2 - (\gamma_2 + \delta + \nu_2)I_2, \qquad (1)$$
$$\frac{dR}{dt} = \gamma_1 I_1 + \gamma_2 I_2 - \delta R,$$

where β_1 (β_2) represents the transmission rate of the resident (mutant) strain; γ_1 (γ_2) represents the recovery rate from the resident (mutant) strain; ν_1 (ν_2) represents the death rate from the resident (mutant) strain due to infection (virulence); μ is a birth rate and δ is the background death rate. All variables represent the number of individuals with the given infection status (for instance, S is the number of susceptible individuals). Since R does not appear in the other equations, we can omit R from the analysis.

The system of differential equations in the presence of adaptive human behaviour couples the SI_1I_2R epidemic spread with a differential equation for human behaviour ("coupled model"). Each individual in the population can choose to accept or reject behaviours that reduce infection risk (e.g. washing hands, wearing a mask, social distancing), and individuals imitate successful strategies observed in others. Let x represent the proportion of individuals accepting preventive behaviour (we will call these "protectors"). Individuals sample others in the population at rate κ, representing social learning. The choice is based on the perceived severity ω_1 (resp. ω_2) from the resident (resp. mutant) strain, where ω_1 (resp. ω_2) can be quantified as the probability that an infection by the resident (resp. mutant) strain results in a severe case of disease. The more severe cases the population observes, the more attractive preventive behaviour becomes: we assume that individuals respond to the total number of severe cases $\omega_1 I_1 + \omega_2 I_2$ they observe at a given time. Preventive behaviour is not always completely effective. We introduce efficacy of infection control ϵ_1 (ϵ_2) against the resident (mutant) strain. The efficacy of infection control influences the transmission process. The more effective infection control is against a strain, the less likely it will be transmitted.

More formally, the preceding imitation dynamic (or equivalently, replicator dynamic) assumes that each individual samples others as a fixed rate, and if another person is found to be playing a different strategy but is receiving a higher payoff, the individual switches to their strategy with a probability proportional to the expected gain in payoff [47]. These assumptions give rise to a differential equation of the form $dx/dt = kx(1 - x)\Delta U$ where k is the sampling rate and ΔU is the payoff difference between the two strategies. This equation is derived elsewhere and is used in other socio-ecological and socio-epidemiological models [43, 48, 49, 50]. The augmented system of differential equations representing the coupled social-epidemiological SI_1I_2RX model with adaptive human behaviour is therefore given by:

$$\frac{dS}{dt} = \mu - \delta S - \beta_1(1 - \epsilon_1 x)SI_1 - \beta_2(1 - \epsilon_2 x)SI_2.$$

$$\frac{dI_1}{dt} = \beta_1(1 - \epsilon_1 x)SI_1 - (\gamma_1 + \delta + \nu_1)I_1.$$

$$\frac{dI_2}{dt} = \beta_2(1 - \epsilon_2 x)SI_2 - (\gamma_2 + \delta + \nu_2)I_2. \tag{2}$$

$$\frac{dR}{dt} = \gamma_1 I_1 + \gamma_2 I_2 - \delta R.$$

$$\frac{dx}{dt} = \kappa x(1 - x)(w_1 I_1 + w_2 I_2 - 1).$$

We apply the restrictions $\epsilon_i \in [0, 1]$ and $\omega_i \geq 0$.

Baseline parameter values are summarized in Table 1. We chose parameter values to represent an emerging infectious disease with a relatively low basic reproduction number and an acute-self limited infection natural history, as might occur for viral infections such as ebola or influenza. Recruitment is assumed to occur due to births and immigration at a constant rate μ, while the per capita death rate due to all causes other than the infection is δ. The values of μ and δ are obtained as the reciprocal of an average human lifespan of 50 years. Note that $\gamma_i + \nu_i$ is the reciprocal of the average time spent in the infected class before the individual recovers or dies from infection. Since we are assuming that strain 2 is more virulent, $\nu_2 - \nu_1 = 0.05$/day can be considered as the excess death rate due to infection from the more virulent strain 2. We assume $\beta_1 = \beta_2$ and therefore $\mathcal{R}_{0,2} \approx 1.6 < \mathcal{R}_{0,1} \approx 2$. Hence, all else being equal, the more virulent strain has a lower reproductive number and is therefore at a disadvantage to invade. We note that R does not appear in the other equations and hence could be omitted.

We identify all equilibria of the uncoupled and coupled systems and determine their local stability properties. We study conditions under which the mutant strain successfully invades. Due to the analytical complexity of the coupled model, we rely primarily on numerical simulations. We used MATLAB to run our simulations and generate parameter planes (ODE45, ODE23tb, and ODE15s). We also wrote MATLAB code to analyze the stable regions of all equilibria versus a combination of parameters of interest. Model code appears in Supplementary Appendix 1.

 # 4 Results

 ## 4.1 Invasion analysis: SI_1I_2R model

The SI_1I_2R model has 3 equilibria. One equilibrium is disease free and is stable when

$$\max\left\{\mathcal{R}_{0,1}, \mathcal{R}_{0,2}\right\} < 1.$$

$\mathcal{R}_{0,1}$ (resp. $\mathcal{R}_{0,2}$) is the basic reproductive number of the resident (mutant) strain, where $R_{0,i}$ is given by

$$\mathcal{R}_{0,i} = \frac{\beta_i}{\gamma_i + \delta + \nu_i}.$$

 The other two equilibria are endemic. Assuming that basic reproductive numbers are not equal, strains can
 not co-exist and the strain with the higher basic reproductive number always invades.

 ## 4.2 Invasion analysis: SI_1I_2RX model

 In contrast, the addition of a dynamic social variable $x(t)$ generates 9 equilibria for the SI_1I_2RX model. Two
 equilibria are disease free and the other equilibria are endemic. One of the 7 endemic equilibria represents a
 state of coexistence of both strains (which can occur even if basic reproductive numbers are not the same).
 The analytical expression and stability criteria for the equilibrium with co-existing strains are difficult to
 compute and therefore, we analyze it numerically. Conditions for existence or stability of all boundary
 equilibria can be found in Table 2.

If both basic reproductive numbers are less than 1, then the system is disease-free and social behaviour is not relevant. Assume, on the other hand, that $1 < \mathcal{R}_{0,2} < \mathcal{R}_{0,1}$ (as in our baseline parameter values, Table 1). This corresponds to a scenario where the resident strain is more transmissible than the mutant strain. As already noted the mutant strain can not invade in the absence of adaptive social behaviour (SI_1I_2R model). However, in the presence of adaptive social behaviour, we can derive necessary and sufficient conditions for the mutant strain to invade when $1 < \mathcal{R}_{0,2} < \mathcal{R}_{0,1}$:

$$\omega_2 > \frac{\beta_2}{\delta}\frac{1}{\mathcal{R}_{0,2} - \frac{1}{1-\epsilon_2}}, \qquad \epsilon_1 > 1 - \frac{\mathcal{R}_{0,2}}{\mathcal{R}_{0,1}}(1-\epsilon_2).$$

 These results show that a high level of perceived severity from the mutant strain is a necessary condition
 for invasion. However, it has to be coupled with a sufficiently high efficacy of infection control against the
 resident strain (with $\epsilon_1 > \epsilon_2$). A high efficacy of infection control against the resident strain will effectively

reduce its transmission and therefore creating a larger pool of susceptible individuals for the mutant strain. The two conditions must be met simultaneously to provide a necessary and sufficient condition for invasion. The condition that $\epsilon_1 > \epsilon_2$ could easily be met in a real population if the two strains differ in their model of transmission, and the population has more experience with controlling the resident strain than with the new mutant strain. Moreover, a high value of ω_2 could easily be met in a real population due to spreading panic about a new and more virulent strain that public health does not yet know how to best control.

We also consider necessary and sufficient conditions for failure of invasion of the mutant strain:

$$\omega_1 > \frac{\beta_1}{\delta} \frac{1}{\mathcal{R}_{0,1} - \frac{1}{1-\epsilon_1}}, \qquad \epsilon_2 > 1 - \frac{\mathcal{R}_{0,1}}{\mathcal{R}_{0,2}}(1-\epsilon_1), \qquad \omega_2 < \frac{\beta_2}{\delta} \frac{1}{\mathcal{R}_{0,2} - 1}.$$

Invasion fails when perceived severity of the mutant strain is low enough but also that of the resident strain high enough. Note the difference between invasion and failure to invade. Here, we require conditions on both perceived severities. As predicted, if the efficacy of infection control against the mutant strain is high enough (relative to that of the resident strain) then invasion fails. Again, all three conditions must be met jointly. Together, they create a necessary and sufficient condition for the failure of invasion.

Finally assume that $\mathcal{R}_{0,1} < \mathcal{R}_{0,2}$ (this scenario is not discussed at length in this paper). In the absence of social behaviour, the mutant strain is bound to invade. However, we derive necessary and sufficient conditions for the failure of invasion when social behaviour is added to the system:

$$\omega_1 > \frac{\beta_1}{\delta} \frac{1}{\mathcal{R}_{0,1} - \frac{1}{1-\epsilon_1}}, \qquad \epsilon_2 > 1 - \frac{\mathcal{R}_{0,1}}{\mathcal{R}_{0,2}}(1-\epsilon_1).$$

Note the difference between this case and the case when $\mathcal{R}_{0,1} < \mathcal{R}_{0,2}$: there is no conditioning on ω_2. If the mutant strain has a higher fitness, it does not matter how severely it is perceived. It will fail to invade provided that the perceived severity of the resident strain is high enough and that efficacy of infection control against the mutant strain is high enough relative to the resident strain (with $\epsilon_2 > \epsilon_1$). Once again we require both inequalities to be satisfied and together they provide necessary and sufficient condition for the mutant strain to fail invasion.

We finally turn our attention to the invasion of the mutant strain when it is more transmissible. The invasion is conditional: necessary and sufficient conditions for the invasion of the mutant strain are:

$$\omega_1 < \frac{\beta_1}{\delta} \frac{1}{\mathcal{R}_{0,1} - 1}, \qquad \epsilon_1 > 1 - \frac{\mathcal{R}_{0,2}}{\mathcal{R}_{0,1}}(1-\epsilon_2).$$

In this scenario, a low perceived severity of the resident strain will allow invasion of the mutant strain provided that the efficacy of infection control against the resident strain is high enough.

The addition of adaptive social behaviour to the epidemic model introduced four new parameters, and it is clear that the model permits conditions for the mutant strain to invade on account of behaviour, even when the mutant strain has a lower basic reproductive ratio, as long as certain conditions for efficacy of infection control are satisfied and level of concern about the severity of the mutant strain are satisfied. To gain further insight into how adaptive social behaviour influences the invasion of the more virulent strain, we turn to numerical simulation and generation of time series and parameter planes.

4.3 Time series analysis

We use time series of model simulations to illustrate some of the model's dynamical regimes. We consider the case where $\nu_1 = 0$ and $\nu_2 = 0.25$ and therefore $\mathcal{R}_{0,1} > \mathcal{R}_{0,2}$ while assuming (for simplicity) that $\beta_1 = \beta_2$ and $\mu_1 = \mu_2$. Hence, the mutant strain is more virulent and kills its hosts more quickly, giving it a significantly lower basic reproduction number.

We first consider a scenario where the mutant strain, on account of its greater virulence, is perceived to be ten times more severe than the resident strain ($\omega_2 = 10^5 = 10\omega_1$). Moreover, infection control against the resident strain is much more effective, on account of less being known about the modes of transmission of the mutant strain (baseline values: $\epsilon_1 = 0.7 > \epsilon_2 = 0.4$). In this scenario, the mutant strain invades (Figure 1a). This agrees with the conditions determined in our invasion analysis. We observe that the mutant strain quickly displaces the resident strain and converges to an endemic state where the proportion of protectors x remains relatively high (Figure 1a). On shorter timescales, we see a transient phase at the start of the simulation with a sharp epidemic of the resident strain, followed by periodic epidemics with much lower incidence of the mutant strain (Figure 1b,c). The numerical simulations agree with the values computed from analytical expressions at equilibrium (for sufficiently large values of t).

Decreasing the efficacy of infection control against the resident strain and equating it to that of the more virulent strain ($\epsilon_1 = \epsilon_2 = 0.4$, with all other parameter values at baseline values) prevents the invasion of the mutant strain (Fig. 1d). This occurs because more susceptible individuals will be infected by the resident strain, thereby significantly decreasing the pool of susceptible individuals available for infection by the mutant strain.

A surprising scenario under which the invasion of the mutant strain fails is when both perceived severity of the mutant strain and the efficacy of infection control against are low (Figure 1e,f, $\omega_2 = 10^2$ and $\epsilon_2 = 0.3$ with other parameter values at baseline). It is worth noting in this case that we initially have a few outbreaks of the mutant strain with high incidence. Fig 1f represents the same dynamics as Fig 1e but on a longer time scale. The oscillations in the prevalence of infection and the prevalence of protectors is typical of coupled

behaviour-disease models with adaptive social behaviour [43].

It is difficult for both strains to co-exist without imposing $\omega_1 = 10^5 > \omega_2 = 10^4$. If the resident strain

is perceived to be ten times more severe, then co-existence is achieved via a transient but very long-term

pattern of switching between oscillatory regimes before the system finally converges to an equilibrium of

co-existence (Fig 1g). The system switches between a longer-lived regime with relatively small epidemics of

the resident strain, and a shorter-lived regime with very large epidemics of the mutant strain. Changes in the

proportion adopting contact precautions, x, facilitates the switching. As x rises, it allows a series of periodic

outbreaks of the mutant strain which in turn decreases the proportion of people adopting prevention and

starts a series of outbreaks of the resident strain. This loop continues with diminishing switching-period as

well as amplitude. If we bring back efficacies of infection control to baseline values, this phenomenon persists

but with wilder oscillations in x. This happens because lower values of ϵ increase the effective transmission

rate which in turns leads to rapid changes in x. Figure 1h shows the same dynamics as in Figure 1g but on

a shorter timescale.

We also allowed the perceived severities to be equally high ($\omega_1 = \omega_2 = 10^4$) and we have increased the

efficacies from their baseline values ($\epsilon_1 = 0.9$ and $\epsilon_2 = 0.6$) (Figure 1i). We observe that the mutant strain

fails to invade and the prevalence of the resident strain remains relatively close to the initial condition.

In order to refine our understanding of the influence of social parameters on the invasion of the mutant

strain, we proceed in the next subsection with phase plane analysis that studies the interplay between the

parameters determining regions of invasion.

4.4   Phase plane analysis

Surprisingly, there are parameter regimes where increasing the perceived severity of the resident strain (ω_1)

allows the mutant strain to invade (Figure 2a-c). This occurs across a nontrivial portion of parameter space

despite the fact that $\mathcal{R}_{0,2} < \mathcal{R}_{0,1}$. This regime shift occurs because a sufficiently high perceived severity

of the resident strain creates a large pool of susceptible individuals, and coupled with a higher efficacy of

infection control against the resident strain, this means that the invading mutant strain can take advantage of

the increased pool of susceptible individuals to invade. This effect occurs only when the efficacy of infection

control against the resident strain is relatively high (e.g. $\epsilon_1 = 0.9$ and $\epsilon_2 = 0.6$). However, this phenomenon

does not hold when ϵ_1 and ϵ_2 are low, in which event the model behaves similar to the SI_1I_2R model where

the strain with the higher basic reproductive number invades, as expected. Similarly, increasing ω_2 can push

the system from a regime of co-existence of the two strains to a region where only strain 2 persists.

In $\epsilon_1 = \epsilon_2$ parameter planes we again find parameter regimes where the more virulent strain can invade

due to adaptive social behaviour, despite the fact that $\mathcal{R}_{0,2} < \mathcal{R}_{0,1}$, if there is an imbalance in the perceived

severity of the two strains. When perceived severities are sufficiently low, the mutant strain can never invade

(Figure 2d). But when $\omega_2 >> \omega_1$, the mutant strain can invade and remove the resident strain if ϵ_1 is

sufficiently large and ϵ_2 is sufficiently small (Figure 2e). When $\omega_1 >> \omega_2$, the mutant strain and the resident

strain coexist, when ϵ_1 is sufficiently large and ϵ_2 is sufficiently small (Figure 6f). Increasing the efficacy of

infection control against the resident strain (ϵ_1) or decreasing efficacy of control against the mutant strain

(ϵ_2) can allow the mutant strain to invade (Figure 2e-f). We note again that, surprisingly, invasion can result

in the elimination of the resident strain if the perceived severity of the mutant strain is significantly higher

than that of the resident strain ($\omega_2 >> \omega_1$), but when the opposite applies, coexistence results.

5   Discussion

We have showed how adaptive social behaviour greatly impacts the evolution of virulence in a coupled

behaviour-disease model. If we neglect social behaviour, the basic reproductive numbers of the two strains

are sufficient to predict which of the strains will invade a population. However, adding adaptive social

behaviour to an epidemiological system completely shifts how we view whether a more virulent strain will

be selected for. As we have seen, social behaviour can either act in favour or against the invasion of a

more virulent strain, and we can describe these effects with reference to specific social parameters ($\omega_{1,2}$)

quantifying how concerned individuals are about the two strains, and control parameters ($\epsilon_{1,2}$) quantifying

how well infection control measures like hand-washing work. Most interestingly, adaptive social behaviour

enables invasion of the mutant strain under plausible epidemiological and social conditions even when it has

a lower basic reproductive number.

Future work can build on these observations to understand how behaviour and virulence evolution interact

for specific infectious diseases, by building on existing research on the coupled dynamics of behaviour and

infection transmission. For instance, an increase in the average number of sexual partners of an individual has

been found in a mathematical model to be a stronger indication of increased virulence for HIV [45, 51]. These

models use a fixed parameter to quantify the number of sexual partners, but the number of sexual partners

could be made to evolve dynamically based on the number of infected individuals in a particular population,

similar to seminal work using compartmental models to model core group dynamics [52]. Other models have

explored conditions under which human papillomavirus vaccines could favour increased virulence [44]. Murall

combines probabilities related to the (social) state of an infected individual with evolving transmission rates

to show that rapid (oncogenic) cell-proliferation can circulate between hosts with medium to high numbers

of sexual partners. Finally, in the case of HIV, the increase of sexual partners will decrease the efficacy of

infection control against the more virulent strain and effectively increase its transmission and hence leads to higher virulence.

While the model discussed in this paper serves as a general framework for studying the influence of social behaviour on the evolution of virulence, further research needs to be carried out to understand the interplay between the epidemiological and social parameters. For instance, we did not model virulence evolution explicitly but rather by assuming two strains have already emerged due to mutation and addressing conditions under which the more virulent mutant strain is more fit. Future research could instead model virulence by defining transmission and recovery rates in terms of a virulence parameter, or by using an adaptive dynamics approach. Future research could also explore the interaction between social learning timescales and pathogen evolutionary timescales. We did not study the influence of the social learning parameter κ in this paper, but previous research on other socio-ecological and socio-epidemiological systems suggests that the social learning rate can destabilize interior equilibria [50, 49]. A model that accounts for multiple rounds of mutation would enable studying how pathogen evolutionary timescales interact with social learning dynamics. Finally, we assumed no specific relationship between the perceived severity $\omega_{1,2}$ and the virulence $\nu_{1,2}$ although a non-trivial relationship certainly exists, and future research could explore possible assumptions for their formal relationship.

In conclusion, our model shows how social behaviour can determine the virulence of emerging strains under plausible parameter regimes when using standard models for social and infection dynamics. When analyzing emerging and re-emerging pathogens and continually evolving infectious diseases such as influenza, it is worthwhile further considering aspects of social behaviour in efforts to mitigate serious threats.

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Parameter	Definition	Value
δ	death rate	1/18250 per day, [42].
μ	birth rate	1/18250 per day, [42].
γ_1	recovery rate for strain 1	0.2 per day (assumed).
ν_1	disease death rate for strain 1	0.0 per day (assumed).
γ_2	recovery rate for strain 2	0.2 per day (assumed).
ν_2	disease death rate for strain 2	0.05 per day (assumed).
β_1	transmission rate for strain 1	0.4 per day (assumed).
β_2	transmission rate for strain 2	0.4 per day (assumed.)
κ	sampling rate	1/365 per day, [48].
w_1	perceived severity from strain 1	10000 (assumed)
w_2	perceived severity from strain 2	100000 (assumed)
ϵ_1	efficacy of infection control against strain 1	0.7 (assumed)
ϵ_1	efficacy of infection control against strain 2	0.4 (assumed)

Table 1: Baseline parameter values.

Figure 1: Numerical simulations for the SI_1I_2RX model at various values for the social and infection control parameters. **(a,b,c)** show baseline values where the mutant strain is perceived to be 10 times more severe ($\omega_2 = 10\omega_1 = 10^5$) and where efficacy of infection control against the resident strain is greater $\epsilon_1 = 0.7 > \epsilon_2 = 0.4$. The dynamics are shown at different timescales in **(a)**, **(b)** and **(c)**. **(d)** $\epsilon_1 = 0.4$. **(e,f)** $\omega_2 = 10^2$, $\epsilon_2 = 0.3$. **(g,h)** $\omega_1 = 10\omega_2 = 10^5$. **(i)** $\omega_1 = \omega_2 = 10^4$. $\epsilon_1 = 0.9$, $\epsilon_2 = 0.6$. All other parameters are held at their baseline values. Red line represents prevalence of protectors x. Blue line represents prevalence of the resident strain I_1. Black line represents prevalence of the more virulent mutant strain I_2.

Figure 2: Parameter plane analysis of the SI_1I_2RX model. The epidemiological parameters are at baseline values (Table 1). The social parameters are varied. **(a)** and **(d)** show no invasion of the mutant strain when $\epsilon_1 = 0.2$ and $\epsilon_2 = 0.1$ in the $\omega_1 - \omega_2$ parameter plane **(a)** and when $\omega_1 = \omega_2 = 10^2$ in the $\epsilon_1 - \epsilon_2$ parameter plane **(d)**. **(b)** and **(c)** represent similar qualitative results when for large $\epsilon_1 = 0.9$ we get invasion of the mutant strain in the black region and co-existence with the resident strain in the red region. The invasion region is bigger when ϵ_2 is lower ($\epsilon_2 = 0.1$ in **(b)** and $\epsilon_2 = 0.6$ in **(c)**). Finally, in **(e)** and **(f)** we observe qualitatively different results when we vary ω_2 in the $\epsilon_1 - \epsilon_2$ parameter plane. In **(e)**, $10^8 = \omega_2 > \omega_1$, we have invasion of the mutant strain. In **(f)**, $\omega_1 = 10^6 > \omega_2$, we have co-existence of the strains. The light gray region in the lower-left hand corner of subpanel **(b)** corresponds to both strains being extinct.