1 **Response to "No evidence of functional co-adaptation between clustered microRNAs"**

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Abstract

microRNAs (miRNAs) are a class of endogenously expressed small non-coding RNAs that

regulate target genes at the post-transcriptional level. One significant feature of miRNA is that

their genomic locations are often clustered together in the genome. In a previous study (Wang,

et al. 2016), we proposed a "functional co-adaptation" model to explain how clustering helps

new miRNAs survive and develop functions during long-term evolution. In a manuscript

recently posted at bioRxiv (doi:10.1101/274811), Marco claimed that he re-analyzed our data

and came to a different conclusion. However, we found his analyses were conducted in an

inappropriate approach. He also claimed that the absence of substitution in highly conserved

miRNAs does not support the "functional co-adaption" model based on the misunderstanding

of our model. In summary, the analyses and claims of Marco, which are flawed, do not refute

our model.

Keywords: miRNAs, target, functional co-adaptation, drift-draft

miRNAs are a class of endogenously expressed small noncoding RNAs (~22 nt in length) that down-regulate the expression of target genes at the post-transcriptional level. A salient feature is that many animal miRNAs are clustered into discrete genomic regions (Lagos-Quintana et al. 2001; Lau et al. 2001; Lai et al. 2003; Altuvia et al. 2005; J. Graham Ruby et al. 2007; Marco et al. 2013; Mohammed, Siepel, et al. 2014). The clustering patterns suggest that miRNAs in the same cluster might be co-transcribed (Baskerville and Bartel 2005; Saini et al. 2007; Ozsolak et al. 2008; Wang et al. 2009; Ryazansky et al. 2011) and be functionally related by targeting the same gene or different genes in the same biological pathway (Bartel 2004; Grun, et al. 2005; Kim and Nam 2006; Yu, et al. 2006). For example, the *mir-17~92* cluster plays an important role in mammalian development and tumorigenesis (O'Donnell, et al. 2005; Lu, et al. 2007; Ventura, et al. 2008; Xiao, et al. 2008). Gene deletion experiments suggest members in the *mir-17~92* cluster have essential and overlapping functions (Ventura, et al. 2008). The *mir-106b~93~25* and *mir-222~221* clusters are upregulated and modulate G1/S phase transition in gastric cancer, and members of the two cluster have functional associations by targeting genes in the Cip/Kip family members of Cdk inhibitors (Kim, et al. 2009). The brain specifically expressed *mir-379~410* cluster is required for the activity-dependent development of hippocampal neurons, and multiple miRNAs from the cluster are necessary for the correct elaboration of the dendritic tree (Fiore, et al. 2009). miRNAs in *mir-23a~27a~24-2* cluster also have cooperative effects in various health and diseased conditions (Chhabra, et al. 2010).

We recently proposed a "functional co-adaptation" model to systematically investigate the functional relatedness of clustered miRNAs (Wang, et al. 2016). We provided several lines of evidence to support the "functional co-adaptation" model. First, we found the observed number of genes co-targeted by miRNAs in the same cluster but with different seeds are significantly higher than the number obtained by random permutations. Second, we found genes targeted by multiple miRNAs from the same clusters, in general, have lower expression levels than genes targeted by multiple miRNAs from distinct clusters. Third, we show that the miRNAs in the same cluster with different seeds tend to target genes in the same biological pathways. Fourth, we transfected four members of the *mir-17~92* cluster into human 293FT cells individually and quantified the alteration of mRNA abundance with deep-sequencing, which verified the overlapping of target genes experimentally. Fifth, we experimentally determined the target genes of *miR-92a*, the founding member of the *mir-17~92* in *Drosophila*，and examined the relationship between the target genes of *miR-92a* in *Drosophila* and the target genes of the *mir-17~92* cluster in humans. Our experimental results well supported the "functional co-adaptation" model. Finally, we also conducted evolutionary analysis to show that positive Darwinian

selection drives the evolution of the newly formed miRNA clusters in both primates and

Drosophila.

In a manuscript recently posted at bioRxiv (Marco, 2018; doi:10.1101/274811), Marco claimed

that he re-analyzed our data and found "No evidence of functional co-adaptation between

clustered microRNAs". Marco claimed that the observed overlap of target genes by the

clustered miRNAs are mostly caused by the similarity between two seed sequences in the *miR-*

182/183/96 cluster. Marco argued that clustered miRNAs from different miRNA families do

not share more targets than expected by chance after correcting for these factors. Marco also

argued that our permutation tests by shuffling miRNA-target inactions would lead to spuriously

low *P* values. Moreover, Marco also raised a series of other critiques about the "function co-

adaptation" model in different versions of his comments. Unfortunately, Marco's critiques are

based on flawed analysis and misled concept of miRNA evolution, which are summarized as

follows.

The major concern Marco raised is whether the observed number of genes targeted by at least

two conserved miRNAs with different seeds from the same miRNA clusters is statistically

higher than the number obtained under the assumption of randomness. In our previous study

(Wang, et al. 2016), to test whether miRNAs in the same clusters tend to regulate overlapping

sets of genes, we obtained expression profiles of miRNAs and mRNAs from five tissues of

human males as determined in previous study (Brawand, et al. 2011; Meunier, et al. 2013).

Since the co-adaption of clustered miRNAs is the result of co-evolution between miRNA and

target sites, in the permutation analysis, we first shuffled the co-expressed seed:target pairing

(TargetScan $P_{CT} > 0.5$), and then we tested how many genes were targeted by at least two

miRNAs (with distinct seeds) in the same clusters. These permutation tests were performed for

1,000 replicates. By this way, the conservation level and length of 3' UTR of target mRNAs,

the number of miRNAs for each target gene, and the compositions of each miRNA cluster are

fully controlled. Applying this procedure to the pooled dataset of miRNA-mRNA co-

expression from different tissues, the result of Wang et al. was successfully reproduced (Fig.

1). When the co-expression data of each tissue was analyzed individually, the similar pattern

was still observed (Fig. 1). Importantly, when the *miR-182/183/96* cluster was excluded, we

can still observe similar patterns (Fig. 2).

By contrast, Marco failed to reproduce our results because he only shuffled the location of the

miRNAs and kept the seed: targeting pairing unaltered. Marco obtained a pattern that the

observed number slightly but still significantly higher than the expected number under the

assumption of randomness ($P = 0.0359$). Since the difference between the observed and

expected numbers are quite smaller obtained by Marco compared to what we obtained (Wang,

et al. 2016), Marco argued that our results are mainly caused by the similarity of the targets

between two seed sequences of the *miR-182/183/96* cluster, and "the expected high number of

common targets between pairs of microRNAs that have a large number of targets each".

However, Marco's permutation tests are biased and flawed. Here, the condition to be tested is

whether miRNAs with distinct seeds from the same cluster have more common target genes

than expected under randomness, rather than to test whether miRNAs are clustered as Marco

conducted.

Despite the numerous exchanges between Marco and us on the detailed permutation test

procedures, Marco consistently argued that our permutation tests by shuffling miRNA-target

interactions would lead to spuriously low P values. To show this point, Marco introduced a

hypothetical regulatory network, in which two clustered miRNAs and an additional miRNA

target the same gene "a" and each miRNA has n additional targets (see Figure 2 of Marco, 2018;

doi:10.1101/274811 for details). Marco derived the formula for calculating the probability that

a permutation reports a common target between two clustered microRNAs under randomness

as

$$P = \frac{6(n!)^2(n+1)!}{(3n+3)!} \sim \frac{4\sqrt{3}\pi}{n}(\frac{1}{3})^{3(n+1)}$$

based on "standard combinatorics" (Marco, 2018; doi:10.1101/274811).

Marco argued that based on this formula, one can obtain very small P values even when there

is no enrichment in common genes targeted by clustered microRNAs. Unfortunately, after

careful examination, we found the formula Marco derived is incorrect. The correct formula

for P value should be:

$$P = \frac{4n^2 + 6n + 2}{9n^2 + 9n + 2}$$

,based on basic combinatorics (see Appendix for details).

In Figure 3, we show that the P values calculated by Marco are consistently smaller than the P

values calculated by the formula we derived. To further support our argument, we also followed

the scheme presented in Figure 2 of Marco, 2018 (doi:10.1101/274811) and estimated the

empirical P value by randomly permuting the miRNA:target pairing for 1,000 times at a given

n. As we show in Figure 3, The P values calculated with the correct formula (red curve) are

highly consistent with the empirical P values, while the P values calculated with Marco's

formula are consistently much smaller than the P values obtained by simulations. Therefore,

Marco's argument that our permutation tests by shuffling miRNA-target interactions would lead to spuriously low P values is based on his erroneous formula in calculating the P value. In fact, the correct P value formula indicates shuffling miRNA-target interactions would not generate a significant P value when there is no enrichment in common genes targeted by clustered microRNAs.

Marco also argued that the differences between clustered and non-clustered miRNAs are not significant when he only focused on the pairs of miRNAs that have fewer than 6 common nucleotides at seed regions in a cluster (the Fig. 1C of (Marco 2018)). He argued that the observed overlap between targets in some clustered miRNAs is actually the random consequence of the similarity between their seed sequences, and is not associated with whether the miRNAs are clustered or not. An inspection of his code indicates his critique is based on incorrect calculation of "the fraction of common targets" for a pair of miRNAs. For example, let us suppose that miRA has x targets, miRB has y targets, and z targets are shared between miRA and miRB. Marco calculated the fraction of common targets as $z/\min(x,y)$ in his Fig. 1C, while calculated the fraction of common targets as $z(x+y)/(2xy)$ in his Fig. 1D. Obviously, using the harmonic mean ($z(x+y)/(2xy)$) is more appropriate to calculate the fraction of common targets, as employed by Marco in his Fig. 1D. Interestingly, when we repeated his analysis in Fig. 1C with the harmonic mean ($z(x+y)/(2xy)$) approach as he did in Fig. 1D, we found a pair of miRNAs with seed similarity less than 6 nucleotides have a significantly higher fraction of common targets if the two paired miRNAs are from the same miRNA cluster ($P = 0.008$, Fig. 4). Therefore, the results in the Fig. 1C of (Marco 2018) are based on incorrect analytical procedures.

Notably, both our original analysis (Wang, et al. 2016) and Marco (2018) only considered the evolutionarily conserved target sites of the evolutionarily conserved miRNAs (only miRNAs that have target sites with TargetScan $P_{CT} > 0.5$ were used in the permutation analyses). Here we considered all the miRNAs that have at least one target site (not necessarily conserved) with weighted context++ score (WCC) < -0.3 (Grimson, et al. 2007; Agarwal, et al. 2015). Target sites with WCC < -0.3 are usually located in optimized genomic context for efficient repression of target mRNAs. With the criteria of WCC < -0.3, only 125 (6%) of 2,081 common targets of clustered miRNAs are contributed by *miR-182/183/96*, which would remarkably reduce the potential bias caused by *miR-182/183/96*. We consistently observed that clustered miRNAs have significantly more common target genes than expected before (empirical $P = 0.0037$, Fig. 5A) or after (empirical $P = 0.0088$, Fig. 5B) excluding *miR-182/183/96* cluster in the permutation tests by shuffling miRNA loci as Marco performed. A more significant trend was observed when the permutation tests were performed by shuffling co-expressed seed: target

1 pairs ($P < 0.0001$ in both Fig. 5C and 5D) as conducted in our original study (Wang, et al.
2 2016). Therefore, we reaffirmed the thesis that clustered miRNAs have more common target
3 genes than expected using miRNA targets with WCC < -0.3.
4
Furthermore, it is hard to understand why Marco argued that the targets shared between *miR-*
183 and *miR-96* in the *miR-182/183/96* cluster should be excluded from the analysis. The seeds
of *miR-183-5p* and *miR-96-5p* are very similar: AUGGCAC and UUGGCAC for the former
and latter, respectively. However, BLAST2SEQ analysis between the precursor sequences of
human *mir-183* and *mir-96* does not find significant similarity, suggesting these two miRNA
precursors are unlikely to be duplicated miRNAs. Instead, the functional co-adaptation model
might well explain the large number of target genes shared between these two miRNAs: During
long time evolution, the adaptive changes in miRNA seed region or target sites on mRNAs
drive the clustered miRNAs to regulate the same or functionally related genes. Therefore, this
cluster serves as a strong evidence that convergent evolution has occurred between the seeds of
miR-183 and *miR-96* due to functional coadaptation.
16
Curiously, Marco did not report his re-analysis results of the *miR-17~92* cluster over-expression
data we generated (Wang, et al. 2016). Many previous studies have demonstrated that the *mir-*
17~92 cluster plays an important role in tumorigenesis, development of lungs and immune
systems (O'Donnell, et al. 2005; Lu, et al. 2007; Ventura, et al. 2008; Xiao, et al. 2008), and
deletion of the *mir-17~92* cluster revealed that miRNAs in this cluster have essential and
overlapping functions (Ventura, et al. 2008). Furthermore, we found the conserved target genes
shared between members of the *mir-17~92* cluster is significantly higher than the simulated
ones (Fig. 6). Importantly, we selected four distinct mature miRNAs in the *miR-17~92* cluster
(*miR-17, miR-18a, miR-19a,* and *miR-92a*) and transfected each miRNA mimic as well as the
miRNA mimic Negative Control (NC) into human 293FT cells (Wang, et al. 2016). With high-
throughput mRNA-Seq, we found the predicted target genes (TargetScan $P_{CT} > 0.5$) of each
transfected miRNA are significantly more down-regulated than genes that do not have the target
sites (Figure 4 of Wang et al. 2016). We identified 301, 55, 345 and 268 high-confidence target
genes (TargetScan $P_{CT} > 0.5$) for *miR-17, 18a, 19a* and *92a* respectively that were down-
regulated with log2(FoldChange) < -0.1 in the corresponding miRNA transfection experiments
(totally 775 high-confidence genes after removing overlapping genes, Figure 4I of Wang et al.
2016). Among these 775 high-confidence target genes, 172 were targeted by at least two out of
the four miRNAs, significantly higher than the number obtained by randomness ($P < 0.001$, see
Figure 4I and Table S8 of Wang et al. 2016 for details). These results well support the
"functional co-adaptation model" we proposed. If there is really "No evidence of functional co-

adaptation between clustered microRNAs" as Marco argued, how can one explain these observed

patterns?

Moreover, Marco did not fully understand the "functional co-adaption" model, which led him

to make the argument that "microRNAs in a cluster are primarily under positive selection"

(April/20/2018 version of doi:10.1101/274811). Although our population genetic analysis

suggests Darwinian selection drives the evolution of the newly formed miRNA clusters in

primates and in *Drosophila*, our model does not necessarily suggest all the clustered miRNAs

are driven by positive selection (Wang, et al. 2016). What we proposed is that, new miRNAs

originating nearby a pre-existed miRNA would have a higher chance to be maintained in the

initial stage of cluster formation due to the tight genetic linkage. Then positive Darwinian

selection might drive the newly emerged miRNAs to develop functions related to the pre-

existing miRNAs in the same cluster or drive the evolution of all the new miRNAs in the same

cluster to develop related functions during the long-term evolution. Once the cluster is fully

established, the miRNAs in the same cluster will be maintained by purifying selection and

become highly conserved after that (Wang, et al. 2016). Thus, one could not expect to observe

signature of ongoing positive selection in the well-established clusters such as the *miR-17~92*

or the *miR-182/183/96* cluster which are ancient and conserved after the establishment, as

Marco did. Marco's observation that "both seed sequences (of *miR-183-5p* and *miR-96-5p*)

have been conserved since their origin and, therefore, there is no evidence of substitutions

happening in the seed of these microRNAs for the last 600 million years" could not refute our

model. Marco also used the deep conservation of the clustered miRNAs in other clusters (*mir-*

106b~25 cluster, *mir-23b~24* cluster, and *mir-379~410* cluster of Fig. S1 in the April/20/2018

version of his manuscript) to argue against the "functional co-adaptation" model. The deep

conservation of the seed sequences as Marco showed can only suggest these miRNAs are

conserved due to extremely strong selective constraints during vertebrate evolution. These

observations do not provide any evidence to defy the "functional co-adaptation" model since

one cannot tell whether the miRNAs have changed since emergence as no outgroup sequence

available.

Based on the observation that *Drosophila* new miRNAs often arose around the pre-existing

ones to form clusters, Marco and colleagues proposed a "drift-draft" model which suggests that

the evolution of miRNA clusters was influenced by tight genetic linkage and largely non-

adaptive (Marco, et al. 2013). Under such a model, the motifs of the pre-existing miRNAs

would protect new miRNAs to be transcribed and processed properly since those motifs were

already interacting with the miRNA processing machinery. Thus, the *de novo* formed new

miRNAs are sheltered by the established ones in the same cluster because mutations that abolish the transcription or processing of the new miRNA will affect the pre-existing ones as well and are hence selected against. On the other hand, if a *de novo* formed miRNA is located in a discrete locus, it will have a higher probability to degenerate, either by mutations abolishing its transcription or by mutations impairing its processing. Although Marco argued the "drift-draft" and "functional co-adaptation" models are mutually exclusive, we did not think the "functional co-adaptation" we proposed is strictly "an alternative to the drift-draft model".

Our previous results and others suggest that many newly-emerged miRNAs are evolutionarily transient, with a high birth-and-death rate (Berezikov et al. 2006; Rajagopalan et al. 2006; Lu, Shen, et al. 2008; Lu et al. 2010). Therefore, it is possible that the newly emerged miRNAs in the clusters would be sheltered by the pre-existing established miRNAs. However, the protection effect alone cannot explain why miRNAs in the same cluster have significantly higher numbers of overlapping target genes. Moreover, many *de novo* formed novel miRNAs will degenerate even after they are fixed in the populations if they are not maintained by functional constraints (Berezikov et al. 2006; Lu, Shen, et al. 2008). Thus developing functions related to the pre-existing miRNAs will help the novel miRNAs to survive and stabilize. The "functional co-adaptation" model we proposed well accounts for the evolution and function of *de novo* formed new miRNAs in the clusters (Figure 2D of Wang et al. 2016). Since miRNAs in the same clusters are usually co-transcribed temporally or spatially (see below for details), the newly formed miRNAs might gradually develop functions to target genes that are related to the pre-existing miRNAs in the same cluster; or multiple *de novo* formed new miRNAs in the same cluster interplay to regulate overlapping sets of target genes. Therefore, although miRNAs in the same cluster have independent origins, they might regulate overlapping sets of target genes through convergent evolution. After that, the clustering patterns of miRNAs and the modular regulation of target genes will be stabilized by natural selection during long-term evolution. Of course, the evolutionary process of miRNAs is also companied by the co-evolution of the target sites, which might also potentially affect the base compositions or even the length of a 3' UTR. In a separate study, we also showed the target sites of miRNAs also experienced frequent births and deaths (Luo, et al. 2018). But the evolution of the target sites alone would not cause the clustering pattern of miRNAs. A plausible scenario is that after a new miRNA originates in a cluster, the substitutions that change the sequences and expression of the new miRNAs, the interactions between miRNAs in the same cluster, and the co-evolution between miRNAs and the target sites or the 3' UTRs, jointly affect the evolution of the clustering pattern of miRNAs.

Understanding the molecular mechanisms and evolutionary principles of the miRNA clustering

would deepen our understanding of the regulatory roles of miRNAs in various biological processes or diseases. The "functional co-adaptation" model we propose is well supported by evolutionary and functional genomic data.

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Figures

Figure 1. Permutation analysis of common target genes of miRNAs from the same cluster in

each tissue or pooled data by shuffling co-expressed seed:target pairs. 1,000 replicates were

performed for each panel. The observed number of common targets was indicated with

vertical red line and the proportion of simulations yielding a number larger than observed

value was shown at top right.

2 **Figure 2.** Permutation analysis of common target genes of miRNAs from the same cluster in

3 each tissue or pooled data by shuffling co-expressed seed:target pairs. Similar as Fig. 1 but

4 *miR-182/183/96* cluster was excluded in the analysis.

Figure 3. The comparison between the P values (y axis) obtained by Marco's formula (blue

line) and the formula derived by us (red line) and the simulation results (black points). In a

hypothetical regulatory network, two clustered miRNAs and an additional miRNA target the

same gene "a" and each miRNA has n (*x-axis*) additional targets, and the P value is the

probability that a permutation reports a common target between two clustered microRNAs

under randomness (see Figure 2 of Marco, 2018; doi:10.1101/274811 for details). The P value

calculated with Marco's formula are consistently smaller (< 0.05) even when there is no

enrichment in common genes targeted by clustered microRNAs. However, the P values

calculated with the correct formula (red curve) indicates shuffling miRNA-target interactions

would not generate a significant P value when there is no enrichment in common genes targeted

by clustered microRNAs. The black points are the empirical P value obtained by randomly

permutating the miRNA:target pairing for 1,000 times at a given n. Note our formula (red line)

and simulation results (black points) are highly consistent.

2 **Figure 4**. The distribution of the fraction of common targets for a pair of miRNAs that are from

3 the same cluster (Clustered) or not (Non-clustered). Paired miRNAs with a seed similarity less

4 than or equal to six nucleotides were compared separately with the Wilcoxon rank-sum tests.

6 **Figure 5.** Permutation analysis of common target genes of clustered miRNAs. (**A** and **B**)

7 Permutation analysis by shuffling miRNA loci using miRNA target genes with weighted

context score++ (WCC) < -0.3 before (A) or after (B) excluding *miR-182/183/96* cluster. (**C** and **D**) Permutation analysis by shuffling co-expressed seed: target pairs using miRNA target genes with WCC < -0.3 before (C) or after (D) excluding *miR-182/183/96* cluster. All the human miRNAs and their targets with WCC < -0.3 were analyzed. Only co-expressed miRNA:target pairs in human tissues were considered. 10,000 replicates were performed for each permutation test. The observed numbers of common targets were indicated with red lines. The empirical *P* value was calculated as the fraction of simulations yielding a number of common targets larger than the observed one.

Figure 6. The number of observed (red) and simulated common target genes of conserved miRNAs in *mir-17~92* cluster in the permutation analysis of Fig. 1.

1 **Appendix**

2 In a hypothetical regulatory network where two clustered miRNAs (miR-A and miR-B) and an

3 additional miRNA (miR-C) target the same gene "a" and each miRNA has n additional targets

4 (see Figure 2 of Marco, 2018 doi:10.1101/274811 for detailed description), the total number of

5 all possible pairing between the three miRNAs and $3n + 1$ targets is:

6
$$N = \binom{3n + 3}{n + 1}\binom{2n + 2}{n + 1}\binom{n + 1}{n + 1}$$

7
$$= \binom{3n + 3}{n + 1}\binom{2n + 2}{n + 1}$$

8
$$= \frac{(3n + 3)!}{(2n + 2)!\,(n + 1)!}\frac{(2n + 2)!}{(n + 1)!\,(n + 1)!}$$

9
$$= \frac{(3n + 3)!}{(n + 1)!\,(n + 1)!\,(n + 1)!}$$

"a" is the only gene that could be targeted by more than one miRNA since other targets only

interact with a single miRNA. Since "a" has three interactions, there are three possible scenarios

where both the clustered miR-A and miR-B could target gene "a": (1) two interactions of gene

"a" are taken by miR-A, and the remaining one is taken by miR-B; (2) one interaction of gene

"a" is taken by miR-A, and the remaining 2 are taken by miR-B; (3) Both miR-A and miR-B

takes one interaction of gene "a", and the remaining one is taken by "miR-C". We can obtain

the number of possible combinations under each of the three scenarios as:

17
$$x_{(1)} = \binom{3}{2}\binom{3n}{n - 1}\binom{1}{1}\binom{2n + 1}{n}\binom{n + 1}{n + 1} = 3\binom{3n}{n - 1}\binom{2n + 1}{n}$$

18
$$x_{(2)} = \binom{3}{1}\binom{3n}{n}\binom{2}{2}\binom{2n}{n - 1}\binom{n + 1}{n + 1} = 3\binom{3n}{n}\binom{2n}{n - 1}$$

19
$$x_{(3)} = \binom{3}{1}\binom{3n}{n}\binom{2}{1}\binom{2n}{n}\binom{n + 1}{n + 1} = 6\binom{3n}{n}\binom{2n}{n}$$

20 The total number of combinations where gene "a" is targeted by both miR-A and miR-B is:

21
$$X = x_{(1)} + x_{(2)} + x_{(3)}$$

22
$$= 3\binom{3n}{n - 1}\binom{2n + 1}{n} + 3\binom{3n}{n}\binom{2n}{n - 1} + 6\binom{3n}{n}\binom{2n}{n}$$

23
$$= 3\frac{(3n)!}{(2n + 1)!\,(n - 1)!}\frac{(2n + 1)!}{(n + 1)!\,n!} + 3\frac{(3n)!}{(2n)!\,n!}\frac{(2n)!}{(n + 1)!\,(n - 1)!} + 6\frac{(3n)!}{(2n)!\,n!}\frac{(2n)!}{n!\,n!}$$

1
$$= 6\frac{(3n)!}{(n+1)!\,n!\,(n-1)!} + 6\frac{(3n)!}{n!\,n!\,n!}$$

2
$$= 6(3n)!\left[\frac{1}{(n+1)!\,n!\,(n-1)!} + \frac{1}{n!\,n!\,n!}\right]$$

3   Therefore, the probability that both miR-A and miR-B target gene "a" is:

4
$$P = \frac{X}{N} = 6\frac{(3n)!}{(3n+3)!}\left[\frac{(n+1)!\,(n+1)!\,(n+1)!}{(n+1)!\,n!\,(n-1)!} + \frac{(n+1)!\,(n+1)!\,(n+1)!}{n!\,n!\,n!}\right]$$

5
$$= 6\frac{(3n)!}{(3n+3)!}\left[(n+1)(n+1)n + (n+1)(n+1)(n+1)\right]$$

6
$$= 6\frac{(3n)!}{(3n+3)!}(n+1)(n+1)(2n+1)$$

7
$$= 6\frac{(n+1)(n+1)(2n+1)(3n)!}{(3n+3)(3n+2)(3n+1)(3n)!} = 6\frac{(n+1)(n+1)(2n+1)}{3(n+1)(3n+2)(3n+1)}$$

8
$$= \frac{2(2n+1)(n+1)}{(3n+2)(3n+1)} = \frac{4n^2+6n+2}{9n^2+9n+2}$$