

1 **Relevance of coral geometry in the outcomes of the coral-algal benthic war**

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40 **Abstract:** Corals have built reefs on the benthos for millennia, becoming an essential element in
41 marine ecosystems. Climate change and human impact, however, are favoring the invasion of
42 non-calcifying benthic algae and reducing coral coverage. Corals rely on energy derived from
43 photosynthesis and heterotrophic feeding, which depends on their surface area, to defend their
44 outer perimeter. But the relation between geometric properties of corals and the outcome of
45 competitive coral-algal interactions is not well known. To address this, 50 coral colonies
46 interacting with algae were sampled in the Caribbean island of Curaçao. 3D and 2D digital
47 models of corals were reconstructed to measure their surface area, perimeter, and polyp sizes. A
48 box counting algorithm was applied to calculate their fractal dimension. The perimeter and
49 surface dimensions were statistically non-fractal, but differences in the mean surface fractal
50 dimension captured relevant features in the structure of corals. The mean fractal dimension and
51 surface area were negatively correlated with the percentage of losing perimeter and positively
52 correlated with the percentage of winning perimeter. The combination of coral perimeter, mean
53 surface fractal dimension, and coral species explained 19% of the variability of losing regions,
54 while the surface area, perimeter, and perimeter-to-surface area ratio explained 27% of the
55 variability of winning regions. Corals with surface fractal dimensions smaller than two and small
56 perimeters displayed the highest percentage of losing perimeter, while corals with large surface
57 areas and low perimeter-to-surface ratios displayed the largest percentage of winning perimeter.
58 This study confirms the importance of fractal surface dimension, surface area, and perimeter of
59 corals in coral-algal interactions. In combination with non-geometrical measurements such as
60 microbial composition, this approach could facilitate environmental conservation and restoration
61 efforts on coral reefs.

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64 INTRODUCTION

65 Corals use energy derived from photosynthesis and heterotrophic feeding to build reefs. This has
66 enabled corals to dominate the battle for light and space on the reef benthos for millennia
67 (Kaandorp & Kubler, 2001). However, the combination of overharvesting of herbivorous fish,
68 increased nutrient runoff from land (eutrophication), and ocean warming is stimulating the
69 growth of non-calcifying algae at the expense of corals world-wide (Alevizon & Porter, 2015).
70 The increase in algal coverage is re-routing the energy to alternative trophic pathways that are
71 enhancing the dominance of algae through positive feedback loops, for example, invigorating the
72 growth of opportunistic and virulent microbes at the coral-algal interface (Kline et al., 2006;
73 Smith et al., 2006; Dinsdale & Rohwer, 2011, Silveira et al. 2015). As algal density increases on
74 reefs, competitive coral-algal interactions are becoming more frequent (Barott et al., 2012a,b;
75 Dinsdale & Rohwer, 2011; Haas et al., 2011), and, in order to preserve and restore coral reefs, it
76 is crucial to understand the key factors that determine the outcomes of these interactions.

77 While there has been significant study into the effects of nitrification and changes in
78 herbivore biomass on coral-algal interactions, results have been somewhat equivocal (Smith et
79 al. 2001, McCook et al. 2001, Burkepile et al. 2006, Rasher et al. 2012). This suggests that other
80 factors such as coral colony conditions may contribute to the outcome of coral-algal interactions.
81 In fact, according to the DDAM (DOC-Disease-Algae-Microbes) hypothesis, dissolved organic
82 carbon (DOC) released by fleshy algae stimulates the growth of opportunistic microbes at the
83 coral-algal interface (Dinsdale & Rohwer, 2011). In combination with a shift to inefficient
84 microbial metabolic pathways, this is suggested to lead to hypoxic conditions at the coral-algal

85 interface, weakening and killing coral tissues (Haas et al., 2013; Roach et al., 2017).
86 Simultaneously, the outcome of a competitive interaction with benthic algae depends on the
87 relative algae overgrowth rate as well as the percentage of the coral perimeter in contact with
88 macroalgae (Lirman, 2001). Thus, the coral perimeter and the ability to defend it must be a key
89 factor in determining the coral-algal interaction outcome.

90 A coral colony consists of multiple clonal polyps that are connected by the coenosarc
91 tissue. Polyps along the perimeter of the colony interact with invading non-calcifying algae as
92 well as other benthic organisms (Jackson, 1977 & 1979; Buss & Jackson, 1979; Meesters,
93 Wesseling & Bak, 1996). At any competitive interaction zone a coral can either overgrow (win),
94 be overgrown (lose), or neither overgrow nor be overgrown (neutral) by the interacting species
95 (Figure S1A) (Jackson & Winston, 1982; Barott et al., 2012b; Swierts & Vermeij, 2016).

96 Defending the perimeter requires the allocation of resources. The energy obtained from
97 photosynthesis—carried out by endosymbiotic algae—and heterotrophic feeding (Porter, 1976)
98 is then distributed throughout the colony using the coenosarc tissue (Rinkevich & Loya, 1989;
99 Oren et al., 1997; Henry & Hart, 2005; Schweinsberg et al., 2015). As the colony's surface area
100 increases so does its potential for nutrient acquisition and distribution (Oren et al., 2001). Thus,
101 coral surface area should be another key factor in determining the coral-algal interaction
102 outcome.

103 The resource availability hypothesis (RAH) (Endara & Coley, 2011) predicts that fast
104 growing corals will rely on clonal growth strategies to indirectly outcompete the invading algae.
105 This explains the resilience observed among branching corals, which invest the resources

106 acquired from their large surface areas to grow new polyps rather than to protect their small
107 perimeters (Swierts & Vermeij, 2016). In contrast, RAH predicts that slow growing species tend
108 to face more encounters with competitors and will invest more resources in protecting their
109 perimeters. This has been confirmed for slow growing corals like encrusting and massive corals
110 (Swierts & Vermeij, 2016).

111 The morphology and size of these slow growing corals have been linked to corals' natural
112 competitive edge against most algal groups (Porter, 1976; Tanner, 1995). Massive corals have
113 relatively lower perimeter-to-surface area ratios and demonstrate greater resilience to algal
114 overgrowth compared to encrusting corals with large perimeter-to-surface area ratios (Hughes
115 1989; Tanner 1995; Lirman 2001). A coral-algal survey in the Line Islands observed that small
116 and large corals were more effective winning against algae than medium sized corals (40–80 cm)
117 (Barott et al. 2012b). In contrast, in the South China Sea it was observed that medium size corals
118 won more often than small and large corals (Swierts & Vermeij, 2016). Thus, the influence of
119 the geometrical properties in the outcome of the coral-algal interaction remains unclear.

120 The accurate measurement of the perimeter and surface area in natural objects, however,
121 is usually challenged by the presence of *fractality* (Mandelbrot, 1967, 1977, 1983). Fractals are
122 non-smooth objects that display similar patterns across multiple scales. This makes the perimeter
123 length and surface area to depend on the resolution of the measurement. In particular, the values
124 follow a power law of the scale with an exponent related to the perimeter and surface's fractal
125 dimensions, respectively, (Falconer 2003, Okie, 2013) (see Eq. (S1) in Methods). Higher fractal
126 dimensions lead to more convoluted surfaces or perimeters with a larger number of wrinkles and

127 textures that increase the effective surface and perimeter of corals (Falconer, 2003; Okie, 2013).
128 Previous studies found fractality among corals at different scales (Basillais, 1997; Bradbury &
129 Reichelt, 1983; Knudby & LeDrew, 2007; Martin-Garin et al., 2007; Mark, 1984; Purkis et al.,
130 2006; Reichert et al., 2017; Zawada & Brock, 2009), but the measurements at the coral colony
131 scale of interest in the present study were inconclusive (Mark 1984).

132 Here we hypothesize that larger fractal dimensions and smaller perimeter-to-surface area
133 ratios would favor corals when facing competitive interactions with algae. To characterize the
134 fractal dimension accurately, high-resolution images of corals were necessary (Young et al.,
135 2017), so we applied new imaging and computer rendering technologies to obtain a systematic
136 and accurate analysis of coral geometry in the 1 mm to 1 m range.

137

138 **METHODS**

139 *Field sampling*

140 Photographs of 50 coral colonies in the Caribbean island of Curaçao were taken by
141 SCUBA diving using a Canon Rebel T4i with a 35-mm lens and two Keldan 800 lumen video
142 lights to illuminate the corals uniformly. An in-reef ruler was photographed to set the scale for
143 the digital models; the ruler was placed along the interface of the coral colonies. Additionally,
144 the perimeters of five coral colonies were measured in the field using a chain-link method, using
145 links of sizes 1.5 cm, 5.5 cm, and 10.5 cm. See Supplementary Material for additional details.

146

147 *2D perimeter models and competition outcomes*

148 High-resolution, overlapping images of coral perimeters were stitched together to build a
149 2D perimeter model (see Figures 1 and 2) using Globalmatch and Guimosrenderer software
150 (Gracias & Santos-Victor, 2000, 2001; Lirman et al., 2007, 2010). The minimum threshold
151 resolution was ~0.5 mm. The interaction zones were outlined in separate RGB channels using
152 Adobe® Photoshop® CC 2014 (Figures 1 and 2): red (coral losing), green (coral winning), and
153 blue (neutral). The fraction of red, green, and blue pixels was used, respectively, to obtain the
154 percentage of losing (%L), winning (%W), and neutral (%N) interactions around a coral
155 perimeter. See Supplementary Material for additional details.

156

157 *3D coral models*

158 Autodesk® ReMake®, 2016 was used to create 3D coral models (Burns et al., 2015;
159 Leon et al., 2015) (Figures 1 and 2) to facilitated the accurate measurement of geometric
160 properties of corals, e.g., perimeter, surface area, and volume at multiple scales (Naumann et al.,
161 2009 & Lavy et al., 2015). The resolution of the models ranged from 1.6 mm to 49 mm with an
162 average of 11 mm. See Supplementary Material for additional details.

163

164 *Perimeter and surface fractal dimensions*

165 The fractal dimension was calculated using a box counting method (Falconer 2003). The
166 logarithm of the number of boxes was plotted against the logarithm of the box size, and the
167 fractal dimension D was extracted from the slope of the linear regression using Eq. (S1) (Figure
168 S2). The 95% confidence intervals for the fractal dimension was calculated using a Monte-Carlo

169 non-parametric bootstrap resampling method. The method was tested for the following fractal
170 objects: the Koch curve, Sierpinski triangle, Menger sponge, and kidney vasculature. This lead to
171 an error on the 1–3% range using five bisections (Table S1). The upper value of this range was
172 used as the theoretical error for the fractal dimension. The perimeter fractal dimension (D_P) was
173 calculated from the 2D high-resolution models, which allowed a minimum of ten bisections in
174 the algorithm. The surface fractal dimension (D_S) was calculated from the 3D high-resolution
175 models, which allowed a minimum of five bisections in the algorithm. The null hypotheses $D_P \neq$
176 1 and $D_S \neq 2$ were evaluated using the nonparametric sign test. See Supplementary Material for
177 additional details.

178

179 *Coral geometric properties: perimeter, surface area, volume, and polyp size*

180 The perimeter, surface area, and volume of the 3D models were calculated with the mesh
181 report tool in Autodesk® Remake®, 2016. This approach was previously tested in Naumann et
182 al., 2009 and Lavy et al., 2015. The perimeter of the high-resolution 2D models was obtained
183 using a Richardson algorithm. The values were compared with field values using three physical
184 chain-links (1.5 cm, 5.5 cm, and 10.5 cm) with an errors of 14.5%, 17.5%, and 19.7%,
185 respectively (Table S2). This discrepancy was reasonable taking into the account the projection
186 on the model and the measurement field error. The 2D perimeter used in the analysis was
187 obtained using a 1 mm ruler in the Richardson algorithm. Polyp diameters were also measured
188 from the 2D models using ImageJ 1.47v and averaging 10 polyp diameters per colony. See
189 Supplementary Material for additional details.

190

191

192 *Correlation with single variables*

193 A linear regression (least squares method) was used to compare the percentages of losing
194 (%L) and winning (%W) perimeter with respect depth (d), polyp diameter (P_d), volume (V),
195 surface area (SA), surface area-to-polyp area ratio (SA_{polyp}), perimeter fractal dimension (D_P),
196 surface fractal dimension (D_S), 2D perimeter obtained from Richardson's algorithm (P_R), 3D
197 perimeter length (P_{3D}), 3D perimeter-to-polyp size ratio (P_{polyp}), 2D perimeter-to-surface area
198 ratio (P_R/SA), and 3D perimeter-to-surface area ratio (P_{3D}/SA) (Table S6). The neutral
199 interactions were a small fraction and were not studied in detail.

200

201 *Statistical learning: Random forest*

202 The package randomForest (Liaw & Wiener, 2002) was used to analyze the response of
203 percentage of perimeter losing (%L) and winning (%W) as function of the 13 variables listed
204 above. The package rfPermute (Archer 2016) was used to estimate the significance of
205 importance and p-value. metrics by permuting the dependent variable, producing a null
206 distribution of importance metrics, and calculating the p-value for each predictor variable. The
207 initial global analysis included 13 input variables: Species, depth, polyp diameter, volume,
208 surface area, volume to surface area ratio, surface to polyp diameter square ratio, projected
209 perimeter length, 3D perimeter length, 3D perimeter length to polyp diameter ratio, projected
210 perimeter to surface area ratio, 3D perimeter to surface area ratio, perimeter fractal dimension,

211 and surface fractal dimension. Both rfPermute and randomForest were run five times and
212 averaged separately to rank the variables independently based on the mean increase accuracy
213 error %IncMSE values. The analysis combining the top ranked variables in groups of three, and
214 the combination leading to the largest variance explained was selected for further analysis. The
215 hierarchical visualization of these variables was obtained using the rpart package in R (Terry
216 2017) for %L and %W. See Supplementary Material for additional details.

217

218 *Coral geometric properties across Curaçao regions.*

219 The corals sampled (n) were grouped in three geographical regions in the island of
220 Curaçao: East (n=9), Central (n=37), and West (n=4)—see Figure S3. The four main geometrical
221 indicators for the percentage of losing and winning interactions (fractal surface dimension,
222 surface area, perimeter length, and perimeter-to-surface area ratio) were compared using
223 boxplots.

224

225 **RESULTS**

226 *Coral-algal competition outcomes*

227 On average, coral displayed 60% losing, 29% winning, and 11% neutral interactions
228 along the perimeter with algae (Figures 2a and 2b, and Table S5). Among species that were
229 sampled in five or more colonies, *S. siderea* displayed the largest percentage of losing perimeter
230 (81%), followed by *P. strigosa* (69%), *M. cavernosa* (58%), and *O. faveolata* (56%) (Figure 2c).
231 The species followed the inverse trend regarding the percentage of winning perimeter: *O.*

232 *faveolata* (33%), *M. cavernosa* (23%), *P. strigosa* (19%), *S. siderea* (12%). The percentage of
233 neutral perimeter was smaller and followed a different trend: *M. cavernosa* (19%), *P. strigosa*
234 (12%), *O. faveolata* (11%), *S. siderea* (8%). Thus, corals were generally losing, and the neutral
235 regions represented the smallest fraction of the competitive outcomes. On average, *S. siderea*
236 was the most vulnerable species, while *O. faveolata* was the most resilient.

237

238 *Coral perimeter and surface fractal dimension*

239 The perimeter fractal dimension, D_p , for the 50 corals was very close to the Euclidean
240 value, $D = 1$, and it was contained within the 5% to 95% confidence interval for all corals but
241 three (CUR34, CUR54, and CAS142) (Figure 3a). When considering the theoretical error of the
242 box counting method (3%), these three cases were compatible with the Euclidean value: CUR34
243 ($D_p = 1.00 \pm 0.03$), CUR54 ($D_p = 0.99 \pm 0.03$), and CAS142 ($D_p = 0.99 \pm 0.03$). The average
244 fractal dimension was $\langle D_p \rangle = 0.999 \pm 0.03$ (SE), and the nonparametric sign test evaluated if the
245 individual perimeters were non-fractal as a whole (null hypothesis, $D \neq 1$), yielding a p-value of
246 0.013. This was a conservative analysis, and incorporating the theoretical error (3%) would
247 reduce this p-value even further. Thus, the dimensions of coral perimeters were non-fractal. The
248 perimeters were also analyzed visually, when comparing high ($D_p = 1.01 \pm 0.03$), medium ($D_p =$
249 0.999 ± 0.005), and low ($D_p = 0.988 \pm 0.008$) fractal dimensions (\pm SE), no salient geometric feature
250 distinguished them (Figure 3b).

251 The surface areas and surface fractal dimensions were measured for 50 corals within the
252 1 mm to 1 m range using the 3D coral models (Figure 3a). The 5% to 95% confidence intervals

253 included the Euclidean surface dimension, $D=2$, for all corals except four: CSA017 (CI: 1.94–
254 1.98), CUR34 (CI:1.94–1.95), CUR40-2 (CI:1.90–1.94), CUR9 (CI:1.84–1.88). When
255 considering the theoretical error of the box counting algorithm ($\sim 3\%$), CSA017 ($D_s = 1.94 \pm$
256 0.06) and CUR34 ($D_s = 1.94 \pm 0.06$) were compatible with the Euclidean value, while CUR40-2
257 ($D_s = 1.90 \pm 0.06$) and CUR9 ($D_s = 1.86 \pm 0.06$) remained slightly lower. The average fractal
258 dimension was $\langle D_s \rangle = 2.00 \pm 0.06$ ($\pm SE$) The nonparametric sign test evaluated if the coral
259 surfaces were fractal (null hypothesis, $D \neq 2$); this yielded a p-value of $1.212e-7^{***}$ using the
260 statistical confidence interval. This p-value would have been even smaller if the theoretical error
261 was included. Thus, overall coral surfaces were statistically non-fractal. Figure 3c compares
262 corals with high (2.08 ± 0.04), medium (2.01 ± 0.04), and low (1.90 ± 0.03) mean surface fractal
263 dimensions. Corals with high surface fractal dimension had no holes and their surface texture
264 was more rugose; corals with low fractal dimension instead displayed holes, peninsulas, and
265 smoother surfaces. Thus, coral surfaces were statistically non-fractal, but the mean fractal value
266 captured distinguishable geometrical features.

267

268 *Relationship between outcomes and individual geometric variables*

269 The absence of fractality in corals facilitated the measurement of the geometric properties
270 at a single (high-resolution) scale. The percentage of losing perimeter (%L) was studied as a
271 function of geometric and biological variables using linear regression analysis (see Figure S5 and
272 Table S6). The percentage of losing perimeter (%L) was negatively correlated with the surface
273 area (slope = 8.6 ± 4.2 $1/\log_{10}(\text{cm}^2)$, $R^2 = 0.09$, p-value= 0.045^*) and the surface fractal dimension

274 (slope = -145 ± 45 , $R^2 = 0.18$, p-value = 0.0021**). The opposite was observed for the percentage
275 of winning perimeter (%W): surface area (slope = 8.6 ± 4.2 $1/\log_{10}(\text{cm}^2)$, $R^2 = 0.08$, p-
276 value=0.045*) and surface fractal dimension (slope = 144 ± 45 , $R^2 = 0.18$, p-value = 0.0023**).
277 This is due to %W being negatively correlated with %L (slope = -0.9 ± 0.1 , $R^2 = 0.8$, p-value =
278 2.2×10^{-16} ***) (Figure S4). The percentage of neutral perimeter (%N) was discarded due to its
279 low values (Figure 2b). Thus, two surface properties (area and fractal dimension) were directly
280 correlated with the coral competition outcomes. The fractal dimension displayed the strongest
281 correlation, but only captured 18 % of the variance ($R^2 = 0.18$), and no variables related to the
282 perimeter showed a direct correlation with the outcomes.

283

284 *Importance of combined geometric variables in coral-algal competition outcomes*

285 The combined effect of coral geometric properties in predicting coral-algal competitive
286 outcomes was analyzed using random forest, which estimated the average percentage increase of
287 mean squared error $\langle \% \text{IncMSE} \rangle$ in predicting the losing perimeter (%L) for each coral feature
288 (see Figure S6a). The variance explained using all variables was 4.3 ± 0.6 % (SE). The surface
289 fractal dimension was the most important predictor, and the only one selected statistically against
290 the null hypothesis by rfPermute (p-value < 0.05). The following variables—listed with
291 decreasing importance—were the 3D perimeter, surface area, and perimeter-to-surface ratio. The
292 lowest ranked predictor was the mean perimeter fractal dimension.

293 The top ranked variables were then combined separately and analyzed again using the
294 random forest statistical model (Table S6). The optimal combination was surface fractal

295 dimension, 3D perimeter, and species. This explained $18.7 \pm 0.5\%$ (SE) of the variance, and the
296 3D perimeter ($\langle \%IncMSE \rangle = 11.0 \pm 0.3$, $p\text{-value} = 0.036^* \pm 0.009$) and the surface fractal
297 dimension ($\langle \%IncMSE \rangle = 11.0 \pm 0.4$, $p\text{-value} = 0.021^* \pm 0.007$) were both equally important
298 and statistically significant ($p\text{-value} < 0.05$) (Figure S6a). These two variables alone, however,
299 explained only $\sim 8\%$ of the variance. Combinations with other geometric variables, like the
300 perimeter-to-surface ratio, led to $\sim 17\%$ variance explained (see Table S6). Thus, coral geometry
301 alone explained up 17% of the percentage of losing perimeter, and the surface fractal dimension
302 and 3D perimeter were the most relevant variables.

303 An analogous analysis was done for the %Winning outcome. Figure S6b plots the input
304 variables ranked as a function of their average percentage increase of mean squared error
305 $\langle \%IncMSE \rangle$. Surface area, perimeter-to-surface area ratio, and 3D perimeter were the better-
306 ranked variables, although only the surface area and 3D perimeter to surface area ratio had a
307 significant p-value (0.05). The fractal surface dimension occupied a middle-ranked position,
308 despite displaying a strong direct correlation with %W (Figure S5b); the perimeter fractal
309 dimension was again the least relevant variable. The variance explained using all variables was
310 $19.6\% \pm 0.9\%$ (SE). As in the %Losing case, the most relevant variables were re-analyzed
311 separately (Table S6). The optimal combination corresponded to the 3D perimeter to surface
312 ratio, 3D perimeter, and surface area. This explained $26.6\% \pm 0.5\%$ of the variance. The 3D
313 perimeter to surface area ratio ($12.0\% \pm 0.4\%$, $p\text{-value} = 0.028^* \pm 0.007$) and the 3D perimeter
314 ($10.6\% \pm 0.3\%$, $p\text{-value} = 0.020^* \pm 0.004$) were the most important and significant variables.
315 The surface area had a similar value but the p-value was slightly larger ($p\text{-value} = 0.059 \pm$

316 0.010). The geometrical properties of corals explained ~25% of the variability of %Winning
317 outcomes, and the perimeter to surface area ratio was the strongest predictor.

318

319 *Hierarchical analysis of coral outcomes and coral geometry*

320 To gain insight on the relationship between coral geometrical properties and coral-algal
321 competitive outcomes, regression tree models (rpart package in R, Terry 2017) were generated
322 using the most relevant variables selected by random forest for %L and %W (see previous
323 sections).

324 For the percent losing case (%L), the nodes of the regression tree corresponded to the
325 surface fractal dimension and 3D perimeter (see Figure 4a). Corals with a fractal dimension $D_s <$
326 2 had a higher %L and were classified on the left side of the tree. Among those, corals with 3D
327 perimeters smaller than 318 cm formed the group with the largest percentage of losing perimeter,
328 $\langle \%L \rangle = 79\%$. For the group with $D_s > 2$, a 3D perimeter larger than 549 cm led to the cluster
329 with the lowest percentage of losing perimeter, $\langle \%L \rangle = 44\%$. Figure 4a also displays the %L as
330 a function of the 3D perimeter and surface fractal dimension. The sectors represent the regions
331 selected by the tree. As expected, the bottom-left sector (small D_s and small perimeter) had the
332 highest value of percentage losing perimeter, while the top-right sector (large D_s and perimeter)
333 had the smallest percentage of losing perimeter.

334 For the percentage of winning outcome (%W), the regression tree selected the surface
335 area (SA), 3D perimeter (P_{3D}), and 3D perimeter to surface area ratio (P_{3D}/SA) as the main nodes
336 (Figure 4b). Corals with a large surface area, $SA > 6482 \text{ cm}^2$, had a higher %W and were

337 classified on the right side of the tree. Among those, corals with small perimeter to surface area
338 ratios, $P_{3D}/SA < 0.054 \text{ cm}^{-1}$, formed the group with the largest percentage of winning perimeter,
339 $\langle \%W \rangle = 43\%$. On the left side of the tree, that is, $SA < 6482 \text{ cm}^2$, the secondary node was based
340 on the 3D perimeter instead of the 3D perimeter to surface area ratio. Corals with large
341 perimeters, $P_{3D} > 141 \text{ cm}$, formed the group with the lowest percentage of winning perimeter,
342 $\langle \%W \rangle = 14\%$. Figure S6b also plots the $\%W$ as a function of the surface area and the perimeter
343 to surface area ratio. The sectors represent the regions selected by the regression tree. As
344 expected, the bottom-right sector (large SA and small P_{3D}/SA) had the highest value of
345 percentage winning perimeter, while the top-left sector (small SA and large P_{3D}) had the smallest
346 percentage of winning perimeter. Notice that corals with larger $\%W$ resided in the bottom half of
347 the scatter-plot, that is, the region with smaller perimeter to surface area ratio.

348

349 *Geometric predictors at the species level*

350 The coral-algal competitive outcomes were also analyzed separately for species
351 represented by more than five sampled colonies: *Orbicella faveolata* (n=12), *Montastraea*
352 *cavernosa* (n=10), *Pseudodiploria strigosa* (n=8), and *Siderastrea sidereal* (n=7) (Figures S7,
353 S8, S9, S10). For each species, the average percentage of losing perimeter ($\%L$) as a function of
354 the surface fractal dimension (D_s) and 3D perimeter (P_{3D}) (Figure S9) was compatible with the
355 values obtained for the same regions in the global analysis (Figures 4a). This was also consistent
356 for the percentage of winning perimeter (Figures S10 and 4b). Thus, the outcome averages for
357 the regions selected in the global analysis led to equivalent results at the individual species level.

358

359 *Analysis of coral geometric properties across Curaçao regions.*

360 The corals sampled were grouped in three geographical regions: East, Central, and West
361 (Figure S1). The four main geometrical indicators for the percentage of losing and winning
362 interactions were compared using boxplots (Figure S11). The Central region showed the lowest
363 value for the fractal dimension (median $D_s < 2$) and surface area (Figures S8a and S8b), indicating
364 a higher percentage of corals losing against algae. The East region displayed a relatively large
365 surface dimension, which was comparable to the West region ($D_s > 2$). Additionally, corals in the
366 East region displayed the largest surface area of all.

367

368 **DISCUSSION**

369 Coral geometrical properties are involved in the acquisition of resources as well as the
370 defense of corals against benthic algae, and in this we were interested in determining if larger
371 fractal dimensions and smaller perimeter-to-surface area ratios were favoring corals when facing
372 competitive interactions with algae.

373 *Relation between coral geometry and coral-algal outcomes*

374 Coral geometric properties explained 19–27% of the coral-algal interaction outcomes
375 (Figure S6). The surface fractal dimension was instead the best single indicator for the
376 percentage of perimeter that was losing or winning (p-value = 0.0021** and $R^2 = 0.18$, Figure
377 S5). This is consistent with the coral surface being essential for harvesting energy for growth and
378 competition. To defend its perimeter, a coral colony depends on resources acquired through

379 photosynthesis (carried out by endosymbiotic algae) and heterotrophic feeding (Porter, 1976).
380 Losing corals had lower surface fractal dimensions ($D_s < 2$) and presented holes and large
381 peninsulas, while winning corals had higher surface fractal dimensions ($D_s > 2$) and displayed
382 more compact and rugose surfaces (Figure 3c). Higher perimeter-to-surface area ratios (P/SA)
383 were correlated with winning corals as a secondary indicator when the surface area of corals was
384 large enough (Figures 4b).

385 The multivariate statistical analysis selected the 3D Perimeter (P_{3D}), fractal surface
386 dimension (D_s), and coral species as the most relevant variables for the percentage of losing
387 perimeter (%L) (Figure S6a). These variables combined explained 19% of the variance of
388 outcomes—similar to the variance explained by the surface fractal dimension alone, 18% (Figure
389 S5a). For the percentage of winning perimeter (%W), the variables selected were the 3D
390 perimeter to surface area ratio (P_{3D}/SA), 3D perimeter (P_{3D}), and surface area (SA) (Figure S6b).
391 These variables combined explained 27% of the variance (Figure S5b). Low surface fractal
392 dimensions, $D_s < 2$, were a good proxy for losing corals (Figure 4a), while large surfaces with low
393 perimeter to surface ratios favored winning corals (Figure 4b).

394

395 *Implications of the fractal dimensions of coral colonies*

396 Coral fractal dimensions have been used to differentiate coral species based on the
397 structure and texture of corallites (Martin-Garin et al., 2007), characterize coral rugosity
398 (Knudby and LeDrew, 2007), describe coral and sponge growth (Kaandorp & Kubler, 2001),
399 measure coral mass over multiple scales (Basillais, 1997 & 1998), and distinguish functional

400 groups such as coral rubble and algal flats on large reef scales (Purkis et al., 2005, 2006; Zawada
401 & Brock, 2009). As shown in Figure 5, the perimeter of coral colonies (range 0.5 mm to 1 m)
402 displayed fractal dimensions close to the topological dimension, $D \sim 1$ (current study). Larger
403 colonies (range 0.1 m – 100 m) had slightly larger values, $D \sim 1.2$ (Bradbury and Reichelt, 1983;
404 Mark, 1984), and coral reefs (10 m – 5 km range) displayed values on the order of $D \sim 1.5$ (Purkis
405 et al., 2006). The perimeters of seagrass beds and hard ground patches were similar, suggesting
406 that the topography of the ground may be responsible for the increment of the fractal dimension.
407 The surface fractal dimension of corallite sections adopted $D \sim 0.8$ – 1.0 at the septa range 0.1 mm
408 – 1 mm (texture) and $D \sim 1.2$ – 1.6 at the calicular range 1 mm – 1 cm (structure) (Martin-Garin et
409 al., 2007). The surface of coral colonies (1 mm – 1 m range) adopted fractal dimensions around
410 the topological value, $D \sim 1.85$ – 2.15 . Coral reefs (0.5 m – 5 km range) displayed larger values
411 $D \sim 2.28$ – 2.61 (Zawada and Brock, 2009), which could be associated to the rugosity of the ground
412 as in the case of the perimeter. Thus, the perimeter and surface fractal dimensions increase at
413 larger scales.

414 At the coral colony scale, the perimeter and surface dimensions were compatible with the
415 Euclidean dimensions, $D = 1$ and $D = 2$, respectively (Figure 3). This justifies modeling coral
416 colonies using Euclidean geometries (Meesters & Bak, 1996; Jackson, 1977; Naumann et al.,
417 2009). The mean values of the surface fractal dimension, however, correlated with coral
418 outcomes (Figure S5) and identified salient geometrical features. Corals with mean fractal
419 dimensions smaller than two, $D_s < 2$, displayed surfaces with holes and large peninsulas, while
420 corals with fractal dimensions larger than two, $D_s > 2$, displayed more compact surfaces with

421 richer and more wrinkled textures (Figure 3c). Additional geometric metrics such as rugosity,
422 vector dispersion, multivariate multiscale fractal dimension, and multifractal analysis (Reichert
423 et al., 2017; Young et al., 2017, Chakraborty et al., 2016) might be necessary to refine the coral
424 geometric analysis presented here.

425 The open regions observed in corals with a surface fractal dimensions smaller than two,
426 $D_s < 2$, can represent more space for algae to occupy, thus leading to the DOC-Disease-Algae-
427 Microbes (DDAM) positive feedback loop detrimental for those coral colonies (Dinsdale &
428 Rohwer, 2011; Haas et al., 2011; Barott et al., 2012a, Roach et al., 2017). This lower fractal
429 dimension associated to holes aligns also with the fact that corals have a limited capacity to
430 regenerate lesions, and if they are larger than a certain size they may never be closed (Meesters
431 et al., 1997). In fact, the sites sampled in the Central region of Curacao had a significantly lower
432 surface fractal dimension than the East and West regions (see Figure S11). The combination of
433 the geometrical properties and the decision trees (Figure 4) suggested that the East region is the
434 healthiest region of Curaçao, followed by the West and Central regions. This analysis is
435 consistent with field observations (Barrot et al. 2012c) and confirms the applicability of the
436 geometrical analysis of corals as a proxy to assess coral-algal interactions.

437

438 **Conclusions and Perspectives**

439 The geometrical properties of corals explained 19% to 27% of coral-algal competition
440 outcomes. The perimeter and surface dimensions of coral colonies were non-fractal, but the
441 mean surface fractal dimension displayed the strongest correlation with coral-algal interaction

442 outcomes. Losing corals had low surface fractal dimensions ($D_s < 2$) and displayed holes and
443 large peninsulas, while winning corals ($D_s > 2$) were more compact and displayed more rugose
444 surfaces. Winning corals had larger surface areas with lower perimeter to surface area ratios,
445 confirming that coral surfaces play a key energetic role in sustaining corals against algal attacks.
446 The main geometrical predictors selected from the global analysis partitioned the percentage of
447 losing and winning perimeters of individual species consistently. Additional data for individual
448 species, however, will be necessary to confirm the relationship between geometrical properties
449 and coral-algal interaction outcomes. Surveying the surface area and fractal dimensions of corals
450 in other regions will help validate the generality of these results. Nevertheless, more
451 sophisticated techniques such as multifractal analysis, might be necessary to understand why the
452 surface fractal dimension is statistically non-fractal while displaying the strongest correlation
453 discerning losing and winning corals. Additionally, it will be necessary to incorporate other
454 descriptors that impact coral outcomes such as microbial and viral communities to achieve more
455 accurate predictions.

456

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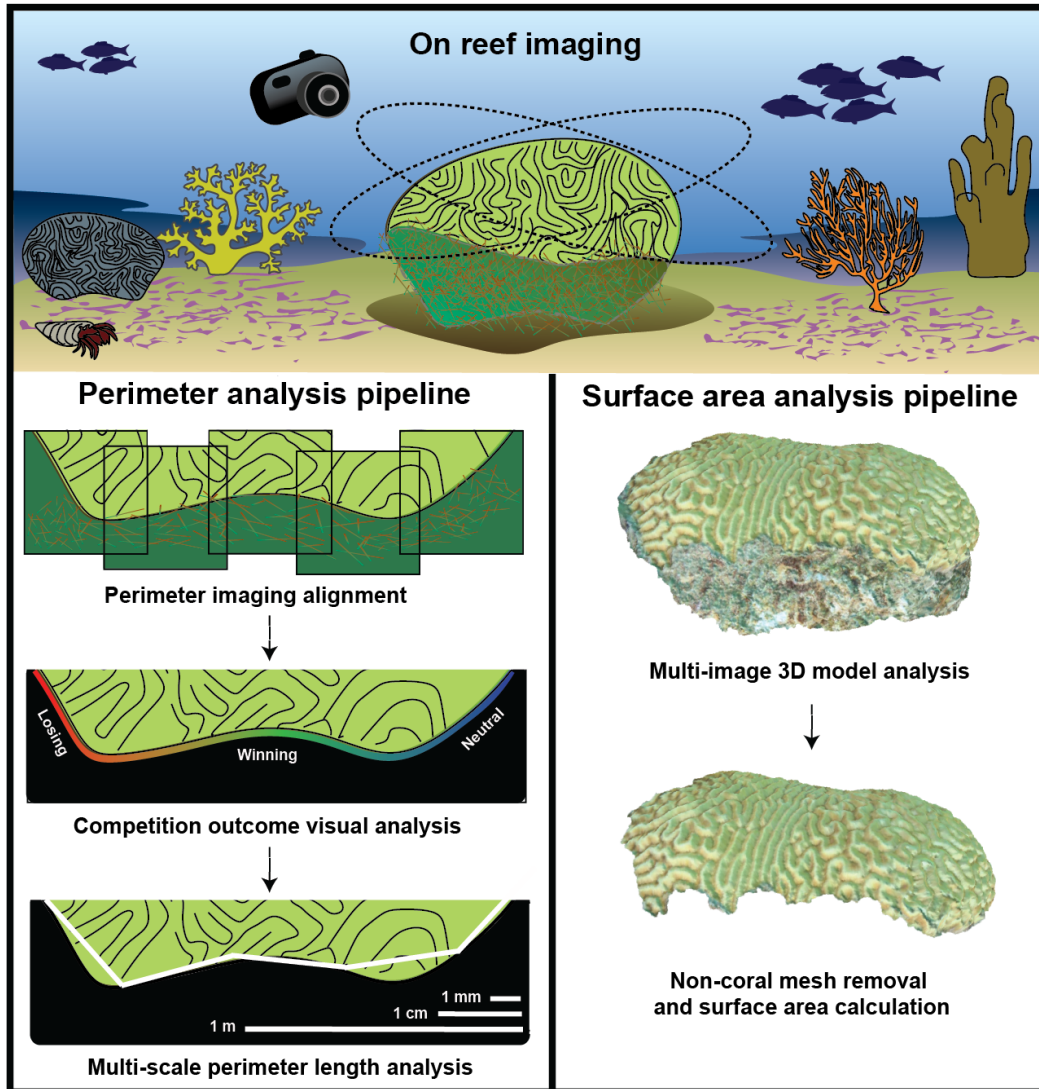
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702 **Figures**

703



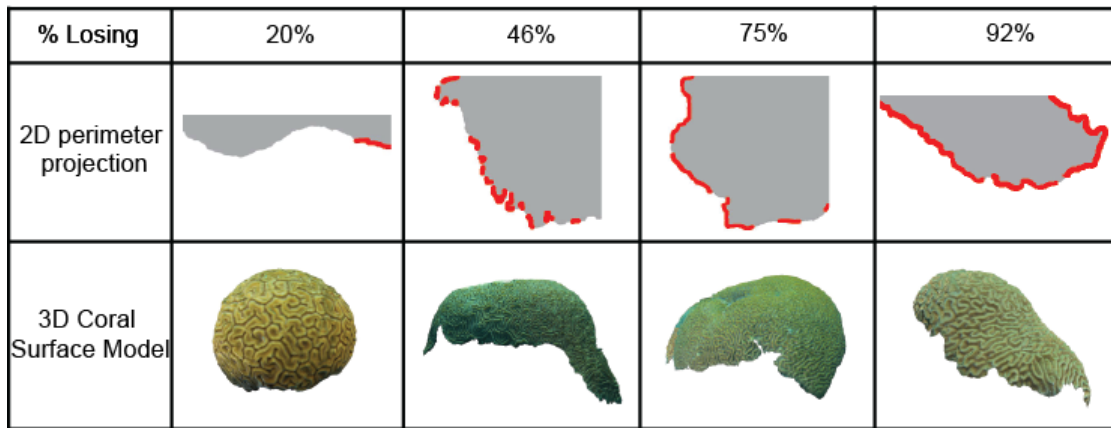
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705 **Figure 1. Coral geometry methods** (Top panel) Corals were photographed from different angles and distances.
706 (Bottom left panel) Close range pictures were stitched together to generate a high-resolution 2D perimeter model.
707 The interactions along the coral perimeter were outlined and the perimeter lengths were measured over a 0.1 mm to
708 1 m scale range. (Bottom right panel) Farther range pictures were processed to create the 3D coral models. Models
709 were calibrated with an in-reef reference; non-coral mesh was removed to measure the coral surface area.

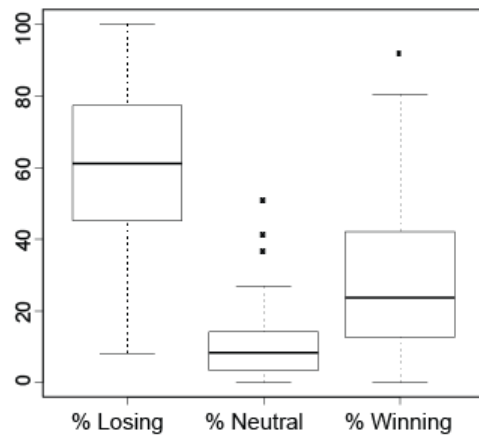
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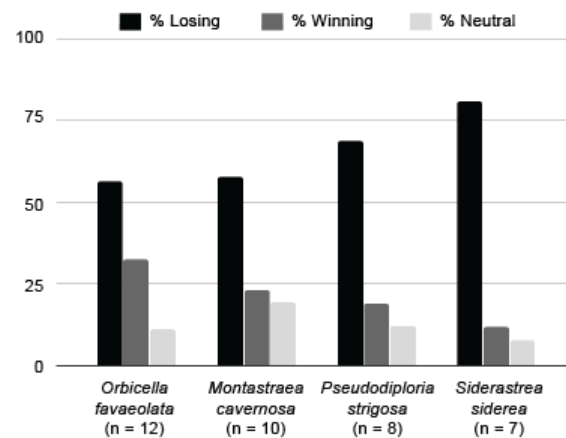
a) 2D and 3D representative models for increasing percentage of losing perimeter



b) Statistics for the competitive outcomes



c) Competitive outcomes across species



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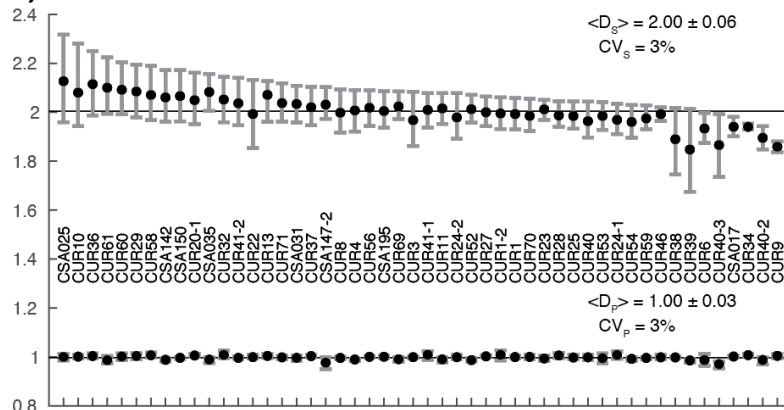
713 **Figure 2. Coral models and statistics for competitive outcomes.** a) 2D and 3D coral models for different
 714 percentages of losing perimeter (%L). The 2D models highlight the losing regions in red. b) Box plot for the three
 715 perimeter outcomes: losing (%L), neutral (%N), and winning (%W). The middle line corresponds to the median, the
 716 range of the box contains from the 25th to the 75th percentile, and each whisker is the minimum (in absolute value)
 717 between the 150% interquartile range (IQR) and the value of the most extreme point in that side of median. Outliers
 718 exceeding the whiskers are included (Table S5). b) Competitive outcomes for species that were sampled in five or
 719 more colonies. The bars correspond to the average percentage of losing perimeter (black), average percentage of
 720 winning perimeter (dark grey), and average percentage of neutral perimeter (light grey).

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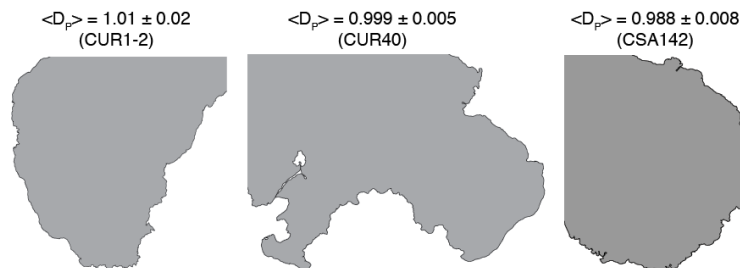
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Coral Fractal Dimensions

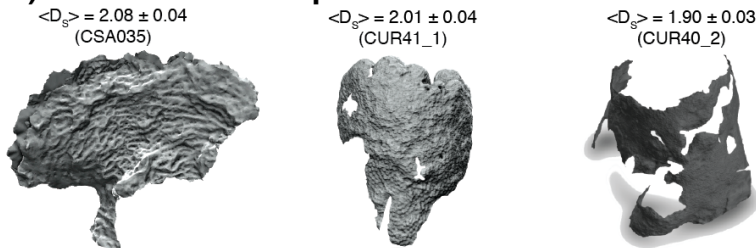
a) Perimeter and surface fractal dimensions



b) Fractal perimeter representatives



c) Fractal surface representatives



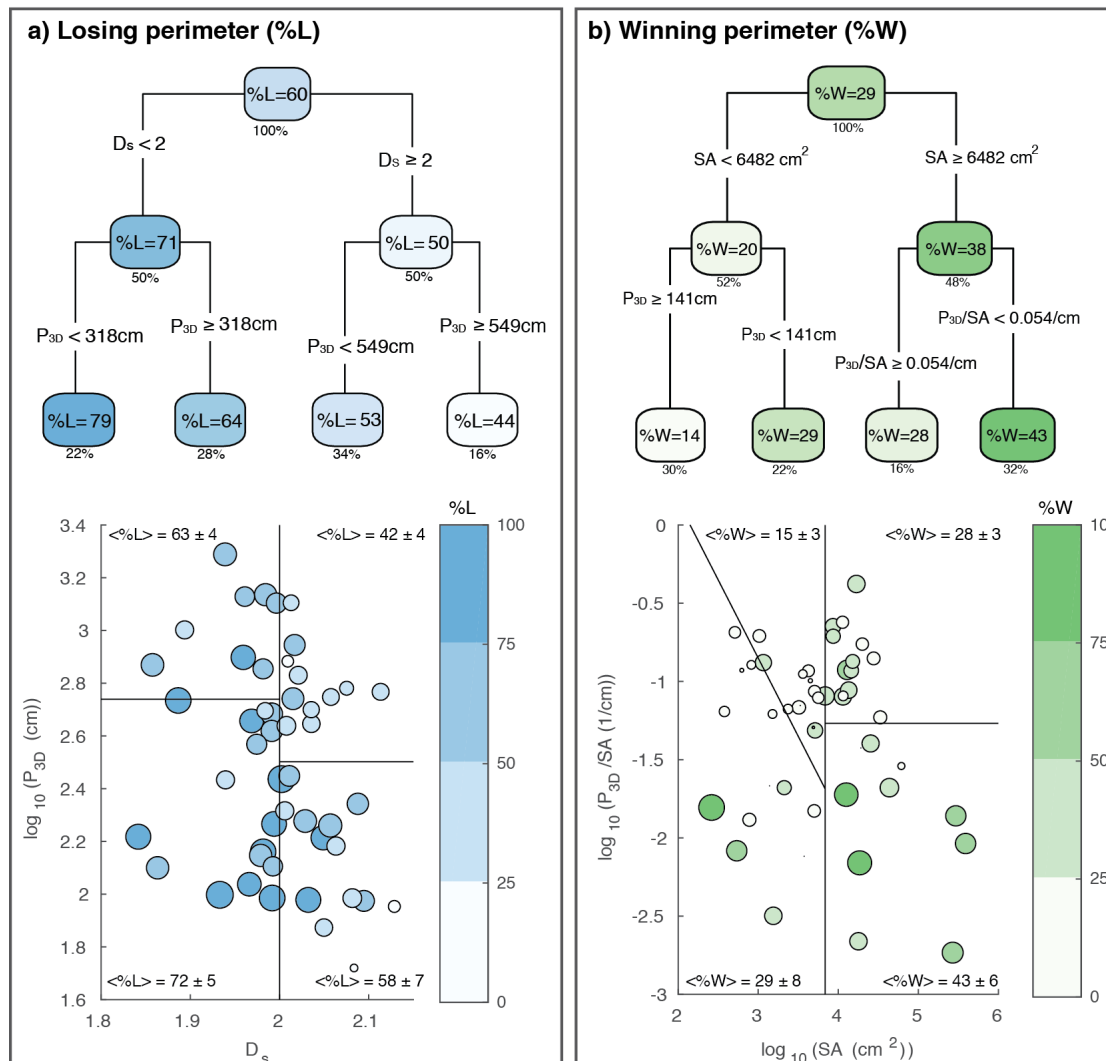
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724 **Figure 3. Coral fractal dimensions.** a) Surface fractal dimensions (top) and perimeter fractal dimensions (bottom)
 725 for all specimens reconstructed digitally. The plot includes the mean (black dot), 5 to 95% confidence intervals
 726 (whiskers), and the label associated to each coral. A solid line provides a reference for the topological dimensions: D
 727 $= 1$ (perimeter) and $D=2$ (surface). The plot includes also the mean values for the fractal dimension of the perimeter
 728 ($\langle D_p \rangle$) and the surface ($\langle D_s \rangle$) (\pm standard deviation) and their respective coefficients of variation ($CV =$ standard
 729 deviation / mean $\times 100$). Panels b) and c) display coral representatives associated with high, medium, and low fractal
 730 dimension for the perimeter (b) and the surface (c).

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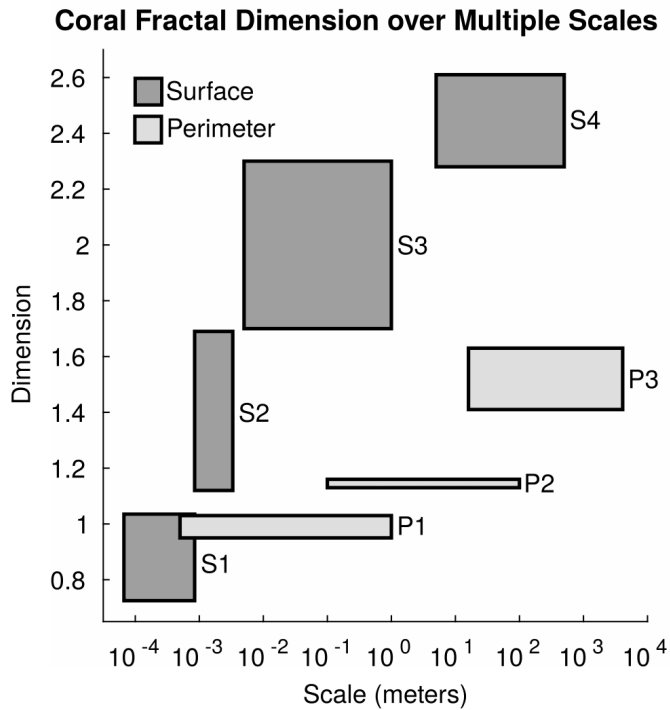
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Interdependence of Optimal Variables in the Prediction of Outcomes



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Figure 4. Interdependence of optimal variables in the predictions of outcomes. a) A regression tree (top panel) generated for the percentage losing perimeter (%L) including the selected variables in the refined Random Forest analysis (Figure S6). Each cluster displays the average outcome. The value below the box indicates the percentage of data contained in the cluster. The bottom panel plots %L as a function of the 3D Perimeter and fractal surface dimension. The shades of blue and circle sizes are proportional to the level of %L. b) The two panels are analogous to a) but using the percentage of winning perimeter (%W) as an output variable. The percentage of winning is in this case proportional to the intensity of green.



742

743 **Figure 5. Coral fractal dimension over multiple scales.** The chart plots the ranges of fractal dimensions measured
744 across scales for different coral studies. The fractal dimensions are grouped in two categories: Surface fractal
745 dimension (dark grey) and perimeter fractal dimension (light grey). For the perimeter, the ranges correspond to coral
746 colonies (P1; current study), larger coral colonies (P2; Bradbury & Rachel, 1983; Mark, 1984), and coral reefs (P3;
747 Purkis et al., 2006). For the surface, the ranges correspond to corallite texture (S1; Martin-Garin et al., 2007),
748 corallite structure (S2; Martin-Garin et al., 2007), coral colonies (S3; current study), and coral reefs (S4; Zawada et
749 al., 2009).

750