Probabilistic variable-length segmentation of protein sequences for discriminative motif mining (DiMotif) and sequence embedding (ProtVecX)

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ABSTRACT

In this paper, we present peptide-pair encoding (PPE), a general-purpose probabilistic segmentation of protein sequences into commonly occurring variable-length sub-sequences. The idea of PPE seqmentation is inspired by the byte-pair encoding (BPE) text compression algorithm, which has recently gained popularity in subword neural machine translation. We modify this algorithm by adding a sampling framework allowing for multiple ways of segmenting a sequence. PPE can be inferred over a large set of protein sequences (Swiss-Prot) and then applied to a set of unseen sequences. This representation can be widely used as the input to any downstream machine learning tasks in protein bioinformatics. In particular, here, we introduce this representation through protein motif mining and protein sequence embedding. (i) DiMotif: we present DiMotif as an alignment-free discriminative motif miner and evaluate the method for finding protein motifs in different settings. The significant motifs extracted could reliably detect the integrins, integrin-binding, and biofilm formation-related proteins on a reserved set of sequences with high F1 scores. In addition, DiMotif could detect experimentally verified motifs related to nuclear localization signals. (ii) ProtVecX: we extend k-mer based protein vector (ProtVec) embedding to variable-length protein embedding using PPE sub-sequences. We show that the new method of embedding can marginally outperform ProtVec in enzyme prediction as well as toxin prediction tasks. In addition, we conclude that the embedding are beneficial in protein classification tasks when they are combined with raw k-mer features.

Availability: Implementations of our method will be available under the Apache 2 licence at http://llp.berkeley.edu/dimotif and http://llp.berkeley.edu/protvecx.

1 Introduction

Bioinformatics and natural language processing (NLP) are research areas that have greatly benefited from each other since their beginnings and there have been always methodological exchanges between them. Levenshtein distance [1] and Smith–Waterman [2] algorithms for calculating string or sequence distances, the use of formal languages for expressing biological sequences [3, 4], training language model-based embeddings for biological sequences [5], and using state-of-the-art neural named entity recognition architecture [6] for secondary structure prediction [7] are some instances of such influences. Similar to the complex syntax and semantic structures of natural languages, certain biophysical and biochemical grammars dictate the formation of biological sequences. This assumption has motivated a line of research in bioinformatics to develop and adopt language processing methods to gain a deeper understanding of how functions and information are encoded within biological sequences [4, 5, 8]. However, one of the apparent

differences between biological sequences and many natural languages is that biological sequences (DNA, RNA, and proteins) often do not contain clear segmentation boundaries, unlike the existence of tokenizable words in many natural languages. This uncertainty in the segmentation of sequences has made overlapping k-mers one of the most popular representations in machine learning for all areas of bioinformatics research, including proteomics [5, 9], genomics [10, 11], and metagenomics [12, 13]. However, it is unrealistic to assume that fixed-length k-mers are units of biological sequences and that more meaningful units need to be introduced. Although in some sequence-labeling tasks (e.g. secondary structure prediction or binding site prediction) sequences are implicitly divided into variable-length segments as the final output, methods to segment sequences into variable-length meaningful units as inputs of downstream machine learning tasks are needed. We recently proposed nucleotide pair encoding for phenotype and biomarker detection in 16S rRNA data [14], which is extended in this work for protein informatics.

Here, we propose a segmentation approach for dividing protein sequences into frequent variable-length sub-sequences, called peptide-pair encoding (PPE). We took the idea of PPE from byte pair encoding (BPE) algorithm, which is a text compression algorithm introduced in 1994 [15] that has been also used for compressed pattern matching in genomics [16]. Recently, BPE became a popular word segmentation method in machine translation in NLP for vocabulary size reduction, which also allows for open-vocabulary neural machine translation [17]. In contrast to the use of BPE in NLP for vocabulary size reduction, we used this idea to increase the size of symbols from 20 amino acids to a large set of variable-length frequent sub-sequences, which are potentially meaningful in bioinformatics tasks. In addition, as a modification to the original algorithm, we propose a probabilistic segmentation in a sampling framework allowing for multiple ways of segmenting a sequence into sub-sequences. In particular, we explore the use of PPE for protein sequences.

Motif mining: In biological sequences (DNA, RNA, and proteins), motifs are short sub-sequences that are presumed to have important biological functions; examples of such patterns are transcription factor binding sites, splice junctions, recruiting enzyme sites, and protein-protein interaction sites [18]. Motif mining has been one of the prominent problems in bioinformatics research. Protein motifs can be either short linear motifs (SLiMs) or larger in some case (e.g. Zinc finger) [19, 20]. Various methods have been proposed for finding protein motifs. These methods mostly framed as finding motifs in a set of similar sequences and usually benefit from sequence alignment algorithms [21], including (but not limited to) MEME Suite [22], QSLiMFinder [23], SLiMSearch [24], and DoReMi [25] as well as hidden Markov model (HMM)-based approaches (e.g., HH-MOTiF [26] and Phylo-HMM [27]). Although most motif mining methods are limited to finding continuous patterns because of their computational complexity, some methods find gapped motifs as well, which is closer to the real scenario [18]. Most of the traditional approaches look for motifs in a set of positive sequences. However, since other randomly conserved patterns may also exist in such sequences, reducing the false positive rate is a challenge for motif mining [28]. In order to address this issue, some studies have incorporated the use of negative samples to increase both the sensitivity and specificity of motif mining. Instances of such approaches are DEME [29] (using a Bayesian framework over alignment columns), discriminative HMM [30, 31], and DLocalMotif [32] (using position and entropy information), as well as deep-learning approaches [33]. General-purpose or specialized datasets are dedicated to maintaining a set of experimentally verified motifs from various resources (e.g., gene ontology). ELM [34] as a general-purpose dataset of SLiM, and NLSdb [35] as a specialized database for nuclear-specific motifs are instances of such efforts. Evaluation of mined motifs can be also subjective. Since the extracted motifs do not always exactly match the experimental motifs, residue-level or site-level evaluations have been proposed [26]. Despite great effort in this area, computational motif mining has remained a challenging task and the state-of-the-art de novo approaches have reported relatively low precision and recall scores, even at the residue level [26].

Protein embedding: Word embedding has been one of the revolutionary concepts in NLP over the recent years and has been shown to be one of the most effective representations in NLP [36, 37, 38]. In particular, skip-gram neural networks combined with negative sampling [39] has resulted in state-of-the-art performance in a broad range of NLP tasks [38]. Recently, we introduced k-mer-based embedding of biological sequences using skip-gram neural network and negative sampling [5], which became popular for protein feature extraction and has been extended for various classifications of biological sequences [40, 41, 42, 43, 44, 45, 46].

In this work, inspired by unsupervised word segmentation in NLP, we propose a general-purpose segmentation of protein sequences in frequent variable-length sub-sequences called PPE, as a new representation for machine learning tasks. This segmentation is trained once over large protein sequences (Swiss-Prot) and then is applied on a given set of sequences. In this paper, we use this representation for developing a protein motif mining framework as well as protein sequence embedding.

(i) **DiMotif**: We suggest a discriminative and alignment-free approach for motif mining that is capable of finding multi-part motifs. We do not use sequence alignment; instead, we propose the use of generalpurpose segmentation of positive and negative input sequences into PPE sequence segments. Subsequently, we use statistical tests to identify the significant discriminative features associated with the positive class, which are our ultimate output motifs. Being alignment free makes DiMotif in particular a favorable choice for the settings where the positive sequences are not necessarily homologous sequences. At the end, we create sets of multi-part motifs using information theoretic measures on the occurrence patterns of motifs on the positive set. We evaluate a shortlist of extracted motifs on the classification of reserved sequences of the same phenotype for integrins, integrin-binding proteins, and biofilm formation proteins, where the phenotype has been detected with a high F1 score. We also evaluate the performance of our method for finding experimentally verified nuclear localization signal (NLS) motifs. However, a detailed analysis of the motifs and their biophysical properties are beyond the scope of this study, as the main focus is on introducing the method.

(ii) **ProtVecX**: We extend our previously proposed protein vector embedding (Protvec) [5] trained on k-mer segments of the protein sequences to a method of training them on variable-length segments of protein sequences, called ProtVecX. We evaluate our embedding via three protein classification tasks: (i) toxin prediction (binary classification), (ii) subcellular location prediction (four-way classification), and (iii) prediction of enzyme proteins versus non-enzymes (binary classification). We show that concatenation of the raw k-mer distributions with the embedding representations can improve the sequence classification performance over the use of either of k-mers only or embeddings only. In addition, combining of ProtVecX with k-mer occurrence can marginally outperform the use of our originally proposed ProtVec embedding together with k-mer occurrences in toxin and enzyme prediction tasks.

2 Material and Methods

2.1 Datasets

Motif mining datasets

Integrin-binding proteins: We extracted two positive and negative lists for integrin-binding proteins using the gene ontology (GO) annotation in the UniProt database [47]. For the positive class, we selected all proteins annotated with the GO term GO:0005178 (integrin-binding). Removing all redundant sequences resulted in 2966 protein sequences. We then used 10% of sequences as a reserved set for evaluation and 90% for motif mining and training purposes. For the negative class, we selected a list of proteins sequences which were annotated with the GO term GO:0005515 (protein binding), but they are annotated as neither integrin-binding proteins (GO:0005178) nor the integrin complex (GO:0008305). Since the resulting set

was still large, we limited the selection to reviewed Swiss-Prot sequences and filtered redundant sequences, resulting in 20,117 protein sequences, where 25% of these sequences (5029 sequences) were considered as the negative instances for training and validation, and 297 randomly selected instances (equal to 10% of the positive reserved set) as the negative instances for the negative part of the reserved set.

Integrin proteins: We extracted a list of integrin proteins from the UniProt database by selecting entries annotated with the GO term GO:8305 (integrin complex) that also had integrin as part of their entry name. Removing the redundant sequences resulted in 112 positive sequences. For the negative sequences, we selected sequences which were annotated for transmembrane signaling receptor activity (to be similar to integrins) (GO:4888) but which were neither the integrin complex (GO:8305) nor integrin-binding proteins (GO:0005178). Selection of reviewed Swiss-Prot sequences and removal of redundant proteins resulted in 1155 negative samples. We used 10% of both the positive and negative sequences as the reserved set for evaluation and 90% for motif mining and training purposes.

Biofilm formation: Similar to integrin-binding proteins, positive and negative lists for biofilm formation were extracted via theri GO annotation in UniProt [47]. For the positive class, we selected all proteins annotated with the GO term GO:0042710] (biofilm formation). Removing all redundant sequences resulted in 1450 protein sequences (90% identity). For the negative class, we selected a list of protein sequences annotated within the parent node of biofilm formation in the GO database that were classified as being for multi-organism cellular process (GO:44764) but not biofilm formation. Since the number of resulting sequences waslarge, we limited the selection to reviewed Swiss-Prot sequences and filtered the redundant sequences, resulting in 1626 protein sequences. Again, we used 10% of both the positive and negative sequences as a reserved set for evaluation and 90% for motif mining and training purposes.

Nuclear localization signals: We used the NLSdb dataset containing nuclear export signals and NLS along with experimentally annotated nuclear and non-nuclear proteins [35]. By using NLSdb annotations from nuclear proteins, we extracted a list of proteins experimentally verified to have NLS, ending up with a list of 416 protein sequences. For the negative class, we used the protein sequences in NLSdb annotated as being non-nuclear proteins. NLSdb also contains a list of 3254 experimentally verified motifs, which we used for evaluation purposes.

Protein classification datasets

Sub-cellular location of eukaryotic proteins: The first dataset we use for protein classification is the TargetP 4-classes dataset of sub-cellular locations. The 4 classes in this dataset are (i) 371 mitochondrial proteins, (ii) 715 pathway or signal peptides, (iii) 1214 nuclear proteins, and (iv) 438 cytosolic protein sequences [48], where the redundant proteins are removed.

Toxin prediction: The second dataset we use is the toxin dataset provided by ToxClassifier [49]. The positive set contains 8093 protein sequences annotated in Tox-Prot as being animal toxins and venoms [50]. For the negative class, we choose the 'Hard' setting of ToxClassifier [49], where the negative instances are 7043 protein sequences in UniProt which are not annotated in Tox-Prot but are similar to Tox-Prot sequences to some extent.

Enzyme detection: On the third we use and enzyme dataset for classification. We download two lists of enzyme and non-enzyme proteins (22,168 protein sequences per class) provided by the 'NEW' dataset of Deepre [51].

2.2 Peptide-pair encoding

PPE training

The input to the PPE algorithm is a set of sequences and the output would be segmented sequences and segmentation operations, an ordered list of amino acid merging operations to be applied for segmenting

Data: Seqs = Set of Swiss-Prot protein sequences, f =minimum number of sequences containing the newly emerged symbol **Result:** S = Divided sequences into variable sub-sequences, $Merge_opt =$ merging operations $Sym = \{A, H, K, T, E, C, V, N, W, Y, F, Q, G, P, D, L, S, R, M, I\};$ S =list of *Seqs*, where each sequence is a list of symbols \in *Sym*; $Merge_opt = stack();$ SymbFreq = mapping symbol pairs in S to their frequencies; $f_{current} = \max$ frequency in *SymbFreq*; while $f < f_{current}$ do sym1, sym2 = argmax (*SymbFreq*); S = merge all consecutive sym1 & sym2 into $\langle sym1, sym2 \rangle$ in S; Sym.push(< sym1, sym2 >);Merge_opt.push(sym1, sym2); update(*SymbFreq*); $current_f = \max$ frequency in *SymbFreq*; end Algorithm 1: Adapted Byte-pair algorithm (BPE) for segmentation of protein sequences

new sequences. At the beginning of the algorithm, we treat each sequence as a list of amino acids. As detailed in Algorithm 1, we then search for the most frequently occurring pair of adjacent amino acids in all input sequences. In the next step, the select pairs of amino acids are replaced by the merged version of the selected pair as a new symbol (a short peptide). This process is continued until we could not find a frequent pattern or we reach a certain vocabulary size (Algorithm 1).

In order to train a general-purpose segmentation of protein sequences, we train the segmentation over the most recent version of the Swiss-Prot database [52], which contained 557,012 protein sequences. We continued the merging steps for T iterations of Algorithm 1, which ensures that we capture the motifs present with a minimum frequency f in all Swiss-Prot sequences (we set the threshold to a minimum of f = 10 times, resulting in $T \approx 1$ million iterations). Subsequently, the merging operations can be applied to any given protein sequences as a general-purpose splitter.

Monte Carlo PPE segmentation

The PPE algorithm for a given vocabulary size (which is analogous to the number of merging steps in the training) divides a protein sequence into a unique sequence of sub-sequences. Further merging steps result in enlargement of sub-sequences, which results in having fewer sub-sequences. Such variations can be viewed as multiple valid schemes of sequence segmentation. For certain tasks, it might be useful to consider a protein sequence as a chain of residues and, in some cases, as a chain of large protein domains. Thus, sticking to a single segmentation scheme will result in ignoring important information for the task of interest. In order to address this issue, we propose a sampling framework for estimating the segmentation of a sequence in a probabilistic manner. We sample from the space of possible segmentations for both motif mining and embedding creation.

Different segmentation schemes for a sequence can be obtained by a varying number of merging steps (N) in the PPE algorithm. However, since the algorithm is trained over a large number of sequences, a single merging step will not necessarily affect all sequences, and as we go further with merging steps, fewer sequences are affected by the newly introduced symbol. We estimat the probability density function

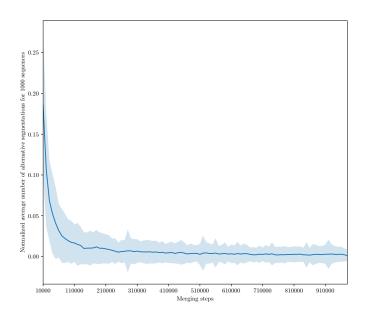


Figure 1. Average number of segmentation alternation per merging steps for 1000 Swiss-prot sequences.

of possible segmentation schemes with respect to *N* by averaging the segmentation alternatives over 1000 random sequences in Swiss-Prot for $N \in [10000, 1000000]$, with a step size of 10000. For each *N*, we count the average number of introduced symbols relative to the previous step; the average is shown in Figure 1. We use this distribution to draw samples from the vocabulary sizes that affected more sequences (i.e. those introducing more alternative segmentation schemes). To estimate this empirical distribution with a theoretical distribution, we fit a variety of distributions (Gaussian; Laplacian; and *Alpha, Beta*, and *Gamma* distributions) using maximum likelihood and found the *Alpha* that fitted the empirical distribution the best. Subsequently, we use the fitted Alpha distribution to draw segmentation samples from a sequence in a Monte Carlo scheme. Consider $\Phi_{i,j}$ as the *l*1 normalized "bag-of-word" representations in sequences" representation of the sequence *i* can be estimated as $\Phi_i = \frac{1}{M} \sum_{i}^{M} \Phi_{i,j}$.

For detecting sequence motifs, we represented each sequence as an average over the count distribution of M samples of segmentation (M=100) drawn from the Alpha distribution. The alternative is to use only the vocabulary size (e.g., the median of Alpha), referred to as the non-probabilistic segmentation in this paper.

2.3 DiMotif protein sequence motif mining

Our proposed method for motif detection, called DiMotif, finds motifs in a discriminative setting via PPE features. We use the false discovery rate-corrected χ^2 test ($\alpha = 0.05$) to identify the most significant discriminative features between the positive and negative classes. Since we are looking for sequence motifs related to the positive class, we filter the selected significant features based on their direction of correlation to ensure we exclud motifs related to the negative class.

We segmented both the training and test datasets with the inferred PPE segmentation in Swiss-Prot (§2.2). We then find the significant discriminative motifs for integrins, integrin-binding proteins, biofilm formation, and NLS proteins by using a χ^2 test over the training dataset.

Classification-based evaluation of integrins, integrin-binding proteins, and biofilm formation motifs: In order to evaluate the obtained motifs, we train linear support vector machine classifiers over the training data, but only use motifs related to the positive class among the top 1000 motifs as well as a short list of features. Next, we test the predictive model on a reserved test set. Since the training and testing sets are disjoint, the classification results are indications of motif mining quality. We use both probabilistic and non-probabilistic segmentation methods to obtain PPE representations of the sequences. We report the precision, recall, and F1 of each classifier's performance.

Literature-based evaluation of NLS motifs: In the case of NLS motifs, we use the list of 3254 experimentally or manually verified motifs from NLSdb. Thus, in order to evaluate our extracted motifs, we directly compare our motifs with those found in earlier verifications. Since for long motifs, finding exact matches is challenging, we report three metrics, the number of motifs with at least three consecutive amino acid overlaps, the number of sequences in the baseline that had a hit with more than 70% overlap (A to B and B to A), and finally the number of exact matches. In addition to Swiss-Prot-based segmentation, in order to see the effect of a specialized segmentation, we also train PPE segmentation over a set of 8421 nuclear protein sequences provided by NLSdb [35] and perform the same evaluation.

2.3.1 Kulback–Leibler divergence to find multi-part motifs

As discussed in § 1, protein motifs can be multi-part patterns, which is ignored by many motif-finding methods. In order to connect the separated parts, we propose to calculate the symmetric Kullback–Leibler (KL) divergence [53] between motifs based on their co-occurrences in the positive sequences as follows:

$$D_{ ext{KL}_{ ext{sym}}}(M_p \| M_q) = \sum_{i}^{N} M_p(i) \log rac{M_p(i)}{M_q(i)} + M_q(i) \log rac{M_q(i)}{M_p(i)},$$

where M_p and M_q are, respectively, the normalized occurrence distributions of motif p and motif q across all positive samples and N is the number of positive sequences. Next, we use the condition of $(D_{\text{KL}_{\text{sym}}} = 0)$ to find co-occurring motifs splitting the motifs into equivalence classes. Each equivalent class indicates a multi-part or a single-part motif. Since we considered a "bag of motifs" assumption, the parts of multi-part motifs are allowed to be far from each other in the primary sequence.

Secondary structure assignment

Using the trained segmentation over the Swiss-Prot sequences, we segment all 385,937 protein sequences in the current version of the PDB [54], where their secondary structure was provided. By segmenting all secondary structures at the same positions as the corresponding sequences, we obtain a mapping from each sequence segment to all its possible secondary structures in the PDB. We use this information in coloring in the visualization of motifs (see Figure 3).

Motif visualization: For visualization purposes DiMotif clusters motifs based on their co-occurrences in the positive class by using hierarchical clustering over the pairwise symmetric KL divergence. The motifs are then colored based on the most frequent secondary structure they assume in the sequences in the Protein Data Bank (PDB). For each motif, it visualizes their mean molecular weight, mean flexibility [55], mean instability [56], mean surface accessibility [57], mean kd hydrophobicity [58], and mean hydrophilicity [59] with standardized scores (zero mean and unit variance), where the dark blue is the lowest and the dark red is the highest possible value (e.g. Figure 3).

2.4 ProtVecX: Extended variable-length protein vector embeddings

We trained the embedding on segmented sequences obtained from Monte Carlo sampling segmentation on the most recent version of the Swiss-Prot database [52], which contains 557,012 protein sequences. Since this embedding is the extended version of ProtVec, we call it ProtVecX. As explained in §2.2 we segment each sequence with the vocabulary size samples drawn from an *Alpha* distribution. This ensures that we consider multiple ways of segmenting sequences during the embedding training. Subsequently, we

train a skip-gram neural network for embedding on the segmented sequences [39]. The skip-gram neural network is analogous to language modeling, which predicts the surroundings (context) for a given textual unit (shown in Figure 2). The skip-gram's objective is to maximize the following log-likelihood:

$$\sum_{t=1}^{M} \sum_{c \in [t-N,t+N]} \log p(w_c \mid w_t), \tag{1}$$

where *N* is the surrounding window size around word w_t , *c* is the context indices around index *t*, and *M* is the corpus size in terms of the number of available words and context pairs. We parameterize this probability of observing a context word w_c given w_t by using word embedding:

$$p(w_c \mid w_t; \theta) = \frac{e^{v_c \cdot v_t}}{\sum_{c' \in \mathscr{C}} e^{v_{c'} \cdot v_t}},$$
(2)

where \mathscr{C} denotes all existing contexts in the training data. However, iterating over all existing contexts is computationally expensive. This issue can be efficiently addressed by using negative sampling. In a negative sampling framework, we can rewrite Equation 1 as follows:

$$\sum_{t=1}^{T} \left[\sum_{c \in [t-N,t+N]} \log \left(1 + e^{-s(w_t, w_c)} \right) + \sum_{w_r \in \mathscr{N}_{t,c}} \log \left(1 + e^{s(w_t, w_r)} \right) \right],\tag{3}$$

where $\mathcal{N}_{t,c}$ denotes a set of randomly selected negative examples sampled from the vocabulary collection as non-contexts of w_t and $s(w_t, w_c) = v_t^{\top} \cdot v_c$ (parameterization with the word vector v_t and the context vector v_c). For training embeddings on PPE units, we used the sub-word level skip-gram, known as fasttext [60]. Fasttext embedding improves the word representations by taking character k-mers of the sub-words into consideration in calculating the embedding of a given word. For instance, if we take the PPE unit *fggagvg* and k = 3 as an example, it will be represented by the following character 3-mers and the whole word, where '<' and '>' denote the start and the end of a PPE unit:

In the fasttext model, the scoring function will be based on the vector representation of k-mers ($2 \le k \le 6$) that exist in textual units (PPE units in this case), $s(w_t, w_c) = \sum_{x \in \mathscr{S}_{w_t}} v_x^\top v_c$.

We used a vector dimension of 500 for the embedding $(v_t$'s) and a window size of 20 (the vector size and the window size have been selected based on a systematic exploration of parameters in protein classification tasks). A k-mer-based ProtVec of the same vector size and the same window size trained on Swiss-Prot is used for comparison.

2.4.1 Embedding-based classification

For the classification, we use a Multi-Layer-Perceptrons (MLP) neural network architecture with five hidden layers using Rectified Linear Unit (ReLU) as the nonlinear activation function. We use the softmax activation function at the last layer to produce the probability vector that could be regarded as representing posterior probabilities. To avoid overfitting, we perform early stopping and also use dropout at hidden layers. As baseline representations, we use k-mers, ProtVec [5], ProtVecX, and their combinations. For both ProtVec and ProtVecX, the embedding of a sequence is calculated as the summation of its k-mers or

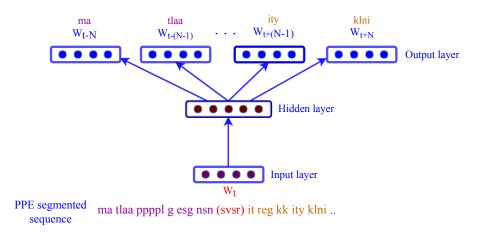


Figure 2. Skip-gram neural network for training language model-based embedding. In this framework the inputs are the segmented sequences and the network is trained to predict the surroundings PPE units.

PPE unit vectors. We evaluate these representation in three protein classification tasks: (i) toxin prediction (binary classification) with the 'Hard' setting in the ToxClassifier database [49], (ii) subcellular location prediction (four-way classification) using the dataset provided by TargetP [48], and (iii) prediction of enzyme proteins versus non-enzymes (binary classification) using the NEW dataset [51]. We report macro-precision, recall, and F-1 score. Macro averaging computes the metrics for each class separately and then simply average over classes. This metric gives equal importance to all categories. In particular we are interested in macro-F1, which makes a trade off between precision and recall in addition to treating all classes equally.

3 Results

3.1 Sequence motifs and evaluation results

Classification-based evaluation of integrins, integrin-binding, and biofilm formation motifs: The performances of machine learning classifiers in phenotype prediction using the extracted motifs as features are provided in Table 2 evaluated in both 10-fold cross-validation scheme, as well as in classifying unseen reserved sequences. Both probabilistic and non-probabilistic segmentation methods have been used to obtain PPE motifs. However, from the top extracted motifs only motifs associated with the positive class are used as features (representation column). For each classification setting we report precision, recall, and F1 scores. The trained classifiers over the extracted motifs associated with the positive class could reliably predict the reserved integrins, integrin-binding proteins, and biofilm formation proteins with F1 scores of 0.89, 0.89, and 0.75 respectively. As described in §2.1 the sequences with certain degrees of redundancy were already removed and the training data and the reserved sets do not overlap. Thus, being able to predict the phenotype over the reserved sets with high F1 scores shows the quality of motifs extracted by DiMotif. This confirms that the extracted motifs are specific and inclusive enough to detect the phenotype of interest among an unseen set of sequences.

For integrin and biofilm formation, the probabilistic segmentation helps in predictions of the reserved dataset. This suggests that multiple views of segmenting a sequences allows the statistical feature selection model to be more inclusive in observing possible motifs. Picking a smaller fraction of positive class motifs still resulted in a high F1 for the test sets. For biofilm formation, the probabilistic segmentation improved the classification F1 score from 0.72 to 0.73 when only 48 motifs were used, where single segmentation even using more features obtained an F1 score of 0.70 (Table 2). This classification result suggests that the

Table 1. Evaluation of the significant nuclear localization signal (NLS) patterns against 3254 experimentally identified motifs. The results are provided for both general purpose and domain specific segmentation of sequences.

PPE training dataset	Probabilistic Segmentation	Medium overlap: Overlapping hits (> 3)	Large overlap: $> 70\%$ sequence overlap	Number of exact matches
Swiss-Prot (General purpose)	True	3253	337	37
Swiss-Prot (General purpose)	False	3162	107	15
Nuclear (Domain specific)	True	3253	381	42
Nuclear (Domain specific)	False	3198	137	21

only 48 motifs mined from the training set are enough to detect bioform formation proteins in the test set. Thus, such a combination can be a good representative of biofilm formation motifs.

Literature-based evaluation of NLS motifs: Since NLSdb provided us with an extensive list of experimentally verified NLS motifs, we evaluated the extracted motifs by measuring their overlap with NLSdb instead of using a classification-based evaluation. However, as discussed in $\S1$ such a comparison can be very challenging. One reason is that different methods and technologies vary in their resolutions in specifying the motif boundaries. In addition, the motifs extracted by the computational methods may also contain some degrees of false negatives and false positives. Thus, instead of reporting exact matches in the experimentally verified set, we report how many of 3254 motifs in NLSdb are verified by our approach using three different degrees of similarity (medium overlap, large overlap, and exact match). The performance of DiMotif for both probabilistic segmentation and non-probabilistic segmentation are provided in Table 1. In order to investigate the performance of phenotype specific versus general purpose segmentation, we also report the results based on using segmentation that is inferred from nuclear proteins, in addition to Swiss-Prot based segmentation (which is supposed to general purpose). Training the segmentation on nuclear proteins resulted in slightly better, but still competitive to the general-purpose Swiss-Prot segmentation. This result shows that the segmentation inferred from Swiss-Prot can be considered as a general segmentation, which is important for low resource settings, i.e. the problem setting that the number of positive samples is relatively small. Similar to integrins and biofilm formation related proteins, the probabilistic segmentation has been more successful in detecting experimentally verified NLS motifs as well (Table 1).

DiMotif Visualization: The top extracted motifs are visualized using DiMotif software and are provided for interested readers, related to integrin-binding proteins (Figure 3), biofilm formation (Figure 4), and integrin complexes (Figure 5). In these visualizations, motifs are clustered according to their cooccurrences within the positive set, i.e. if two motifs tend to occur together (not necessarily close in the linear chain) in these hierarchical clustering they are in a close proximity. In addition, each motif is colored based on the most frequent secondary structure that this motif can assume in all existing PDB structures (described in $\S2.3.1$), the blue background shows loop, hydrogen bound or irregular structures, yellow background shows beta ladders, and red background shows helical structures. Furthermore, to facilitate the interpretation of the found motifs, DiMotif provides a heatmap representation of biophysical properties related to each motif, namely molecular weight, flexibility, instability, surface accessibility, kd hydrophobicity, and mean hydrophilicity with standardized scores (zero mean and unit variance) the dark blue is the lowest and the dark red is the highest possible value. Normalized scores allow for an easier visual comparison. For instance, interestingly in most cases in the trees (Figure 3, Figure 4, and Figure 5), the neighbor motifs (co-occurring motifs) agree in their frequent secondary structures. Furthermore, some neighbor motifs agree in some provided biophysical properties. Such information can assist biologists and biophysicists to make hypotheses about the underlying motifs and mechanisms for further experiments. A detailed serious biophysical investigation of the extracted motifs is beyond

Table 2. Evaluation of protein sequence motifs mined via PPE motif mining for classification of integrin-binding proteins and biofilm formation-associated proteins. Support Vector Machine classifiers are tuned and evaluated in a stratified 10-fold cross-validation setting and then tested on a separate reserved dataset.

Dataset	Probabilistic Segmentation	Representation	10-fold cross-validation			Performance on the test set		
			Precision	Recall	F1	Precision	Recall	F1
Integrin-Binding	True	top 1000 (998 positive)	0.88	0.85	0.87	0.91	0.85	0.88
		top-100 (100 positive)	0.73	0.66	0.69	0.84	0.67	0.75
	False	top 1000 (982 positive)	0.91	0.87	0.89	0.93	0.86	0.89
		top-100 (100 positive)	0.73	0.68	0.70	0.84	0.67	0.75
Integrins	True	top 1000 (1000 positive)	0.94	0.76	0.84	1	0.75	0.86
		top-100 (100 positive)	0.91	0.82	0.86	0.83	0.83	0.83
	False	top 1000 (996 positive)	0.96	0.82	0.89	1	0.83	0.91
		top-100 (100 positive)	0.88	0.83	0.86	0.9	0.75	0.82
Biofilm formation	True	top-1000 (103 positive)	0.89	0.67	0.76	0.82	0.56	0.72
		top-500 (48 positive)	0.81	0.71	0.76	0.76	0.71	0.73
	False	top 1000 (53 positive)	0.79	0.67	0.73	0.74	0.66	0.70
		top-500 (26 positive)	0.78	0.67	0.72	0.73	0.65	0.69

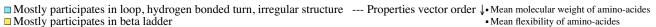
the scope of this study. However, as an example, for integrin-binding proteins, the RGD motif, the most well-known integrin-binding motif was among the most significant motifs in our approach [61, 62, 63]. Other known integrin-binding motifs were also among the most significant ones, such as RLD [62], KGD (the binding site for the $\alpha II\beta$ 3 integrins [64]), GPR (the binding site for $\alpha_x\beta$ 2 [63]), LDT (the binding site for $\alpha_4\beta$ 7 [63]), QIDS (the binding site for $\alpha_4\beta$ 1 [63]), DLLEL (the binding site for $\alpha_\nu\beta$ 6 [63]), [tldv,rldvv,gldvs] (similar motifs to LDV, the binding site for $\alpha_4\beta$ 1 [61]), rgds [65], as well as the PEG motif [66].

3.2 Results of protein classification tasks using embedding

Protein classification results for venom toxins, subcellular location, and enzyme predictions using deep MLP neural network on top of different combinations of features are provided in Table 3. In all these three tasks, combining the embeddings with raw k-mer distributions improves the classification performances (Table 3). This result suggests that k-mers can be more specific than embeddings for protein classification. However, embeddings can provide complementary information to the k-mers and improve the classification performances. Combining 3-mers with either ProtVecX or ProtVec embedding performed very competitively; even for sub-cellular prediction tasks, ProtVec performs slightly better. However, combining 3-mers with ProtVecX resulted in higher F1 scores for enzyme classification and toxin protein classification papers [46], embeddings have been used as the only representation. However, the presented results in Table 3 suggest that k-mer representation, although is a simple approach, but is a tough-to-beat baseline in classification tasks. The ProtVec and ProtVecX embeddings only have added value when they are combined with the raw k-mer representations. black

4 Conclusions

We proposed a new unsupervised method of feature extraction from protein sequences. Instead of fixedlength k-mers, we segmented sequences into the most frequent variable-length sub-sequences, inspired by BPE, a data compression algorithm. These sub-sequences were then used as features for downstream machine learning tasks. As a modification to the original BPE algorithm, we defined a probabilistic



Mostly participates in helix

- Mean DIWV instability index of sequence Mean surface accessibility of amino-acides
- · Mean KD hydrophobicity
- Mean hydrophilicity of amino-acides

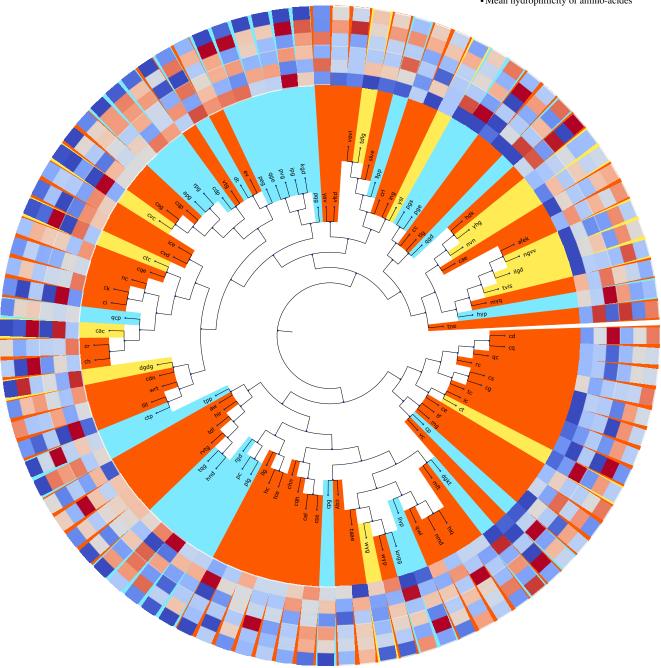
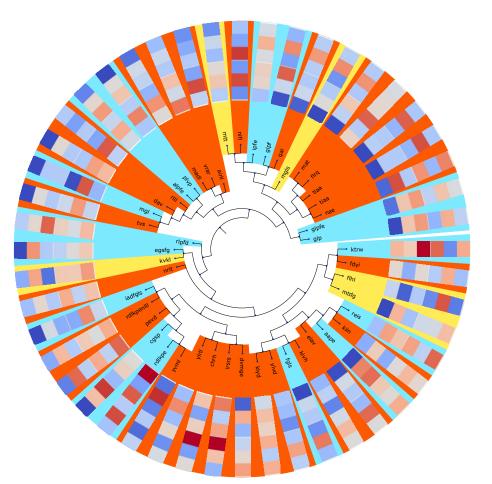


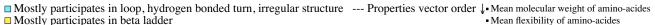
Figure 3. Clustering of integrin-binding-specific motifs based on their occurrence in the annotation proteins. Each motif is colored based on the most frequent secondary structure it assumes in the Protein Data Bank (PDB) structure out of all PDB sequences. For each motif the biophysical properties are provided in a heatmap visualization, which shows from outer ring to inner ring: the mean molecular weight, mean flexibility, mean instability, mean surface accessibility, mean kd hydrophobicity, and mean hydrophilicity with standardized scores (zero mean and unit variance), where the dark blue is the lowest and the dark red is the highest possible value. Motifs are clustered based on their co-occurrences in the integrin-binding proteins.



□ Mostly participates in loop, hydrogen bonded turn, irregular structure --- Properties vector order ↓• Mean molecular weight of amino-acides Mostly participates in beta ladder Mostly participates in helix

- - · Mean flexibility of amino-acides
 - Mean DIWV instability index of sequence · Mean surface accessibility of amino-acides
 - Mean KD hydrophobicity
 - Mean hydrophilicity of amino-acides

Figure 4. Clustering of biofilm formation-specific motifs based on their occurrence in the annotation proteins. Each motif is colored based on the most frequent secondary structure it assumes in the Protein Data Bank (PDB) structure out of all PDB sequences. For each motif the biophysical properties are provided in a heatmap visualization, which shows from outer ring to inner ring: the mean molecular weight, mean flexibility, mean instability, mean surface accessibility, mean kd hydrophobicity, and mean hydrophilicity with standardized scores (zero mean and unit variance), where the dark blue is the lowest and the dark red is the highest possible value. Motifs are clustered based on their co-occurrences in the biofilm formation proteins.



Mostly participates in helix

- Mean DIWV instability index of sequence
- Mean surface accessibility of amino-acides Mean KD hydrophobicity
- Mean hydrophilicity of amino-acides

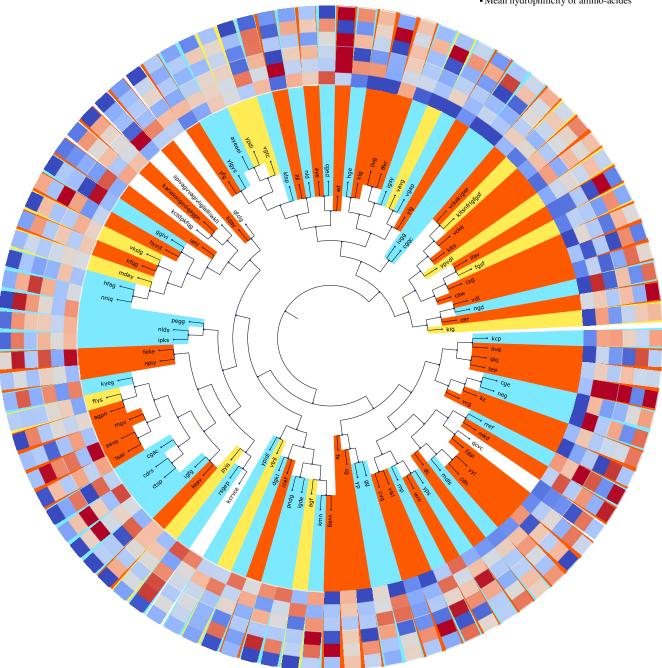


Figure 5. Clustering of integrin-related motifs based on their occurrence in the annotation proteins. Each motif is colored based on the most frequent secondary structure it assumes in the Protein Data Bank (PDB) structure out of all PDB sequences. For each motif the biophysical properties are provided in a heatmap visualization, which shows from outer ring to inner ring: the mean molecular weight, mean flexibility, mean instability, mean surface accessibility, mean kd hydrophobicity, and mean hydrophilicity with standardized scores (zero mean and unit variance), where the dark blue is the lowest and the dark red is the highest possible value. Motifs are clustered based on their co-occurrences in the integrin proteins.

Dataset	Representation	5 fold cross-validation				
Dataset	Representation	macro-Precision	macro-Recall	macro-F1		
	3-mer	0.89	0.89	0.89		
	ProtVec	0.88	0.88	0.88		
Venom toxin prediction	ProtVecX	0.88	0.88	0.88		
venom toxin prediction	3-mer + ProtVec	0.90	0.89	0.89		
	3-mer + ProtVecX	0.90	0.90	0.90		
	3-mer	0.65	0.59	0.60		
	ProtVec	0.60	0.57	0.58		
Subcellular location prediction	ProtVecX	0.57	0.57	0.57		
Subcential location prediction	3-mer + ProtVec	0.68	0.60	0.62		
	3-mer + ProtVecX	0.66	0.60	0.61		
	3-mer	0.70	0.73	0.71		
	ProtVec	0.68	0.70	0.69		
Enzyme prediction	ProtVecX	0.69	0.71	0.70		
Enzyme prediction	3-mer + ProtVec	0.70	0.73	0.71		
	3-mer + ProtVecX	0.71	0.73	0.72		

Table 3. Comparing k-mers, ProtVec, and ProtVecX and their combinations in protein classification tasks. Deep MLP neural network has been used as the classifier.

segmentation by sampling from the space of possible vocabulary sizes. This allows for considering multiple ways of segmenting a sequence into sub-sequences. The main purpose of this work was to introduce a variable-length segmentation of sequences, similar to word tokenization in natural languages. In particular, we introduced (i) DiMotif as an alignment-free discriminative protein sequence motif miner, as well as (ii) ProtVecX, a variable-length extension of protein sequence embedding.

We evaluated DiMotif by extracting motifs related to (i) integrins, (ii) integrin-binding proteins, and (iii) biofilm formation. We showed that the extracted motifs could reliably detect reserved sequences of the same phenotypes, as indicated by their high F1 scores. We also showed that DiMotif could reasonably detect experimentally identified motifs related to nuclear localization signals. By using KL divergence between the distribution of motifs in the positive sequences, DiMotif is capable of outputting multi-part motifs. A detailed biophysical interpretation of the motifs is beyond the scope of this work. However, the tree visualization of DiMotif as a tool, can help biologists to come up with hypotheses about the motifs for further experiments. In addition, although homologous sequences in Swiss-Prot have indirectly contributed in DiMotif segmentation scheme, unlike conventional motif mining algorithms, DiMotif does not directly use multiple sequence alignment information. Thus, it can be widely used in cases motifs need to be found from a set of non-homologous sequences.

We proposed ProtVecX embedding trained on sub-sequences in the Swiss-Prot database. We demonstrated that combining the raw k-mer distributions with the embedding representations can improve the sequence classification performance compared with using either k-mers only or embeddings only. In addition, combining ProtVecX with k-mer occurrences outperformed ProtVec embedding combined with k-mer occurrences for toxin and enzyme prediction tasks. Our results suggest that many recent work in the literature including our previously proposed ProtVec missed serving k-mer representation as a baseline, which is a tough-to-beat baseline. We show that embedding can be used as complementary information to the raw k-mer distribution and their added value is expressed when they are combined with k-mer features.

In this paper we briefly touched motif-mining and protein classification tasks as use cases of peptide pair encoding representation. However, the application of this work is not limited to motif mining or embedding training, and we expect this representation to be widely used in bioinformatics tasks as general purpose variable-length representation of protein sequences.

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