A biologically driven directional change in susceptibility to global-scale glaciation during the Precambrian-Cambrian transition

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Integrated geological evidence suggests that grounded ice sheets occurred at sea level across all latitudes during two intervals within the Neoproterozoic era; the "snowball Earth" (SBE) events. Glacial events at ~730 and ~650 million years ago (Ma) were probably followed by a less severe but nonetheless global-scale glaciation at ~580Ma, immediately preceding the proliferation of the first fossils exhibiting unambiguous animal-like form. Existing modelling identifies weathering-induced CO_2 draw-down as a critical aspect of glacial inception, but ultimately attributes the SBE phenomenon to unusual tectonic boundary conditions. Here we suggest that the evident directional decrease in Earth's susceptibility to a SBE suggests that such a-directional abiotic factors are an insufficient explanation for the lack of SBE events since ~580 Ma. Instead we hypothesize that the terrestrial biosphere's capacity to sustain a given level of biotic weathering-enhancement under suboptimal/declining temperatures, itself decreased over time: because lichens (with a relatively robust tolerance of sub-optimal temperatures) were gradually displaced on the land surface by more complex photosynthetic life (with a narrower temperature window for growth). We use a simple modelling exercise to highlight the critical (but neglected) importance of the temperature sensitivity of the biotic weathering enhancement factor and discuss the likely values of key parameters in relation to both experiments and the results of complex climate models. We show how the terrestrial biosphere's capacity to sustain a given level of silicate-weathering-induced CO_2 draw-down is critical to the temperature/greenhouse forcing at which SBE initiation is conceivable. We do not dispute the importance of low degassing rate and other tectonic factors, but propose that the unique feature of the Neoproterozoic was biology's capacity to tip the system over the edge into a runaway ice-albedo feedback; compensating for the self-limiting decline in weathering rate during the temperature decrease on the approach to glaciation. Such compensation was more significant in the Neoproterozoic than the Phanerozoic due, ultimately, to changes in the species composition of the weathering interface over the course of evolutionary time.

1. Introduction

A. The snowball Earth problem

The snowball Earth (SBE) concept provides a rich framework for quantifying the limits of integrated biogeochemical change (Hoffman & Schrag, 2002). The period between 720-635 Ma is termed the Cryogenian (from Greek words for "cold" and "birth") and an iconic feature of this interval is the presence of radiometrically dated glacial diamictites in over ninety formations worldwide (Evans, 2000, Arnaud et al, 2012, Hoffman et al, 2017). Many such deposits exhibit both the appearance of derivation from glaciers grounded below sea-level and a remnant magnetism indicative of a low paleolatitude (Evans & Raub, 2011). This is widely taken to imply that globally extensive glaciers progressed as far as the equator. Numerous other diamictites are bounded by thick layers of non-skeletal shallow-water

carbonate (Fairchild, 1993, Hoffman & Halverson, 2008) likely derived from the warmest parts of the ocean (Opdyke & Wilkinson, 1993). Equivalently, this is taken to imply that the glacial interval's termination was characterized by an extreme CO_2 greenhouse, which gradually declined as the ocean "titrated" the CO_2 as carbonate. This core idea motivated the original Snowball Earth hypothesis (Kirshvink, 1992, Hoffman et al, 1998) and has remained relatively robust to subsequent scrutiny. Contemporary discussion as to how best to interpret the data motivating SBE centres around the relevance of incompletely oxidized iron-rich rocks (Urban et al, 1992, MacDonald et al, 2010), other evidence pointing to the redox status of the ocean during the glacial interval (Halverson, 2011) and the plausibility of the persistence of habitable refugia for eukaryotes (Hoffman, 2016).

A key conceptual uncertainty within the SBE concept is the degree of dynamism present during the glacial interval. A "slushball-Earth" is a global-scale glaciation with open ocean water towards equatorial latitudes, because an extra (greenhouse) forcing causes the ice-albedo feedback to stabilize dynamically, rather than runaway to an equilibrium, entailing complete ice cover (e.g. Peltier, 2007). The concept of a slushball has historically been defined in opposition, and widely held to be more parsimonious than, a "hard snowball" in which the ice-albedo feedback goes to an equilibrium state. This is because most researchers have tacitly assumed that a slushball is far easier to reconcile with the survival of complex life, and/or that a hard snowball would lead to accumulation of ice sheets too thick to permit deglaciation. Thin ice solutions within global climate models are indeed extremely precarious (Pollard & Kasting, 2005, Lewis et al, 2007), generally hinging on the action of some process within the hydrological cycle (evapotranspiration, dynamic sea ice, wind fields) that can transport ice from the tropics poleward, thereby avoiding the accumulation of irretrievably thick ice sheets at the equator. However, high-pressure-induced melting at the base of extremely thick ice sheets may induce "basal sliding", potentially sustaining a sufficiently dynamic sea ice cycle to permit deglaciation from a hard snowball (Hoffman, 2005, Rignew et al, 2011). Hard snowball solutions within general circulation models can be formulated that permit deglaciation, but this is by no means a foregone conclusion (Abott et al 2013). Again, the reversibility of the hard-snowball state almost always hinges on crucial unpreserved quantities, such as tropical evaporation fluxes (Pollard & Kasting, 2005), heat transfer patterns within the atmosphere above an ice-covered ocean (Benn et al, 2015), or the glacial interval's cloud formation patterns and their contribution to albedo (Abbot et al, 2012). This raises the (pessimistic but very real) possibility that the data do not allow us to distinguish between a hard snowball and slushball solution. Nevertheless, the broad view that emerges from current work with complex climate models is that a hard snowball, with sufficient oceanographic/atmospheric dynamism to keep equatorial ice recoverably thin, is probably closest to the mark (reviewed in e.g. Hoffman, 2018).

In this context the utility of the SBE problem as a theoretical test case for the predictive power of complex climate models becomes apparent, as does the fact that the "hard-snowball versus slushball" distinction cannot be resolved in a hypothesis-driven simple-modelling study such as this. We therefore proceed by remaining agnostic about this distinction. We simply take the label "snowball Earth" to refer to the entry of Earth into a positive feedback between low-latitude ice cover and high planetary albedo, with the result that some form of equilibrium is reached. (In a hard-snowball this would constitute a truer equilibrium in an "energy balance" sense, in a slushball the "equilibrium" might be better described as a

dynamical steady state. The key point is that the ice-albedo feedback reaches a region of "phase space" qualitatively distinct from subsequent milder glaciations).

B. The silicate weathering CO_2-sink, climate stability and the ice-albedo feedback
Weathering of silicates on the land surface removes CO_2 from the atmosphere and inputs bicarbonate anions and silicate-derived (magnesium and calcium) cations into the water table, ultimately leading to precipitation of calcite on the ocean floor in a net CO_2-sink (e.g. Berner et al, 1983):

$$[CaSiO_{3(s)} + 2CO_{2(g)}]_{WEATHERING} \xrightarrow[RUNOFF]{} [CaCO_{3(s)} + SiO_{2(aq)} + CO_{2(aq)}]_{OCEAN}$$

Because the weathering reaction is both temperature-sensitive and a greenhouse gas sink, a silicate weathering "thermostat" was postulated (Walker et al, 1981) to exert a homeostatic influence on Earth's temperature over geologic timescales. A shutdown of this weathering sink during the glacial interval of a snowball Earth is central to the coherence of the original idea (Kirschvink, 1992), because without the resultant CO_2 build-up, the combination of high albedo and low temperature would render global-scale ice cover irreversible (e.g. Pierrehumbert, 2005). Existence of a climatically influential weathering-homeostat presupposes kinetic limitation of weathering rate, at least at first-order, by CO_2 levels. The idea of such limitation is therefore complicated by the fact that weathering rate may in fact frequently be limited by supply of fresh rock from tectonic uplift (West et al, 2005). Consistently, supply rate of silicate rock has been proposed to have controlled the interval between snowball Earth events- because deglaciation requires a high CO_2 greenhouse, which must be removed by the weathering sink before the system becomes susceptible to a subsequent glacial event (Mills et al, 2011).

An ice-covered surface reflects a higher fraction of incoming radiation (has a higher albedo) than an ice-free surface, which leads to a hysteresis (memory of previous system state) in the climate system, by which the greenhouse/radiative forcing necessary to exit the snowball state exceeds the threshold at which the system initially fell into this state (Budyko, 1969, Sellers, 1969). If more than about half of Earth's surface becomes ice-covered, a runaway positive feedback to global glaciation becomes inevitable (Caldeira & Kasting, 1992b). But the precise temperature/greenhouse forcing at which this albedo threshold occurs is non-trivial to calculate even in high-resolution climate models, because it depends on paleogeographic reconstructions, the contribution of cloud albedo, the albedo of ice-free but extremely low temperature ocean water the thickness of sea ice (Warren et al, 2002) and the density of cracks/bubbles in such sea ice (Carns et al, 2016), etc. Thus, it is possible to state that there exists a temperature T_{in} at which a positive feedback between declining temperatures, increasing ice-cover and increasing planetary albedo, will initiate, but the specific value of this temperature threshold is uncertain. Existing studies have taken $T_{in} \approx$ 10°C (Donnadieu et al, 2004, Pierrehumbert et al, 2005, Mills et al, 2011). Below, we parameterize a wider range of values for this threshold, on the basis of uncertainties in the appropriate inputs to the complex climate models from which this value was calculated, as well as uncertainty about what the snowball state actually constitutes in terms of temperature, albedo and greenhouse forcing combination.

C. Biological enhancement of weathering, the evolution of the terrestrial biosphere and the plausibility of Neoproterozoic lichens

The biotic enhancement of weathering (BEW) factor is defined as how much faster the silicate weathering CO_2 sink is under biotic conditions than under abiotic conditions (Schwartzman & Volk, 1989, Schwartzman, 2017). The magnitude of the BEW factor depends on the rock substrate and the principal form of photosynthetic life responsible for the enhancement. Empirical estimates suggest that for vascular plants $BEW \approx 2 - 5$ on basalt (Moulton & Berner, 1998) and $BEW \approx 10 - 18$ on granite (Bormann et al, 1998), for mosses $BEW \approx 1.4 - 3.5$ on granite and $BEW \approx 3.6 - 5.5$ on andesite (Lenton et al, 2012), for lichens $BEW \approx 4 - 16$ on mica schist (Aghamiri & Schwartzman, 2002), $BEW \approx 2.5 - 3.5$ on granite (Zambell et al, 2012) and probably of the order of $BEW \geq 15 - 20$ (with some estimates suggesting significantly higher, up to 70) on basalt (Jackson & Keller, 1970, Brady et al, 1999, Stretch & Viles, 2002). Given the extreme uncertainties in the species composition by biomass of any ancient terrestrial biosphere, as well as in the rock composition of ancient paleo-continents, it is not realistic to formulate a detailed picture of the evolution of the BEW factor over time (although see Schwartzman, 2017). For the purposes of this exercise, we simply note that any enhancement of silicate weathering by lichens is comparable to, and if anything, greater than, that of more morphologically complex terrestrial autotrophs.

Mechanistically, lichens enhance weathering by proton secretion, ice-crystal nucleation and retention of water in the rock surface, secretion of organic acids, and digestion of silicate particles within the fungal hyphae (Jones & Wilson, 1985, Chen et al, 2000, Li et al, 2016). The adaptive value of this activity is likely the acquisition of the $PO_4{}^{3-}$ liberated with the silicate cations (Rogers, 1998, Guidry & McKenzie, 2000). Indeed, the rise of a Neoproterozoic biosphere dominated by lichens has been hypothesized previously, as the explanation for a possible rise in O_2 at the Neoproterozoic-Cambrian boundary (Heckman et al, 2001, Lenton & Watson, 2004).

The first unambiguous fossil lichen is not observed until ~400Ma (Taylor et al, 1995), but fossilized arbuscular mycorrhizae are found from 460 Ma (Redecker et al, 2000), and fungi may have been present much earlier at 1430 Ma (Butterfield, 2005). The presence of Precambrian Lichens is evidentially ambiguous but nevertheless widely postulated (Selosse & Tacon, 1998, Retallack, 1994, Lenton & Watson 2004). The idea is given weight by strong evidence for terrestrial photosynthesizing microbial biota from about 1400 Ma (Horodyski & Knauth, 1994), as well as molecular clock inferences for the presence of lichen-forming fungi from about 1000 Ma (Heckman et al, 2001).

Lichens exhibit a vastly greater ecological range than any other form of macroscopic photosynthetic life. There is no biome on Earth (i.e. including the Arctic) that lacks colonization by lichens. In respect of virtually all physiologically limiting environmental variables the eco-physiological range of lichens significantly exceeds that of vascular plants or mosses (e.g. Nash, 1996). Antarctic lichens have a temperature range in the region of $-2 - 14°C$ (Gannutz, 1967) and are capable of surviving prolonged periods below $-13°C$ (Clark et al, 2001). Heat-adapted lichen species have a similar robustness in the opposite direction, with desert lichens capable of surviving up to $55°C$ (Kershaw, (1985). Thus, the extremes of temperature, water potential and availability of nutrients and rock substrate that characterize the Cryogenian do not preclude the colonization of the land surface by lichens

during intervals of habitability, indeed if anything they increase the strength of the case for their presence (in comparison to that for other forms of photosynthetic life). Nor is it implausible that lichen spores survived non-habitable intervals during the glacial period, for instance lichen spores have been shown to survive in space (Sancho et al, 2007). By contrast, the optimal temperature for photosynthesis in a typical vascular plant is typically in the region of $15 - 20°C$, with a far sharper cut-off outside this optimum than lichens (Hatfield & Prueger, 2015).

D. Key premises
Life can be conceived of as introducing a unique variability to the Earth system (Vernadsky, 1926), on the basis of which we take the qualitative difference in SBE susceptibility between the Earth system before and after the Precambrian-Cambrian boundary, as plausibly biological in origin. The above discussion serves to justify the following basic premises:
1. If any macroscopic photosynthetic land life was present around and immediately after the Cryogenian period, it was likely to be lichens.
2. Any Precambrian lichen-based terrestrial biosphere likely exerted a comparable silicate weathering enhancement to the subsequent Phanerozoic vascular plant-based terrestrial biosphere, possibly a greater one.
3. Any such weathering enhancement factor was likely sustained over a greater physiological range when resulting from lichen activity that other photosynthetic life.

This leads us to the key premise motivating this work: The Precambrian terrestrial biosphere enhanced silicate weathering induced CO_2 draw-down over a significantly wider temperature range than the Phanerozoic terrestrial biosphere, but the overall magnitude of this enhancement was comparable. On the basis of this supposition, we now proceed to model the likely impact of biotic enhancement of silicate weathering on the susceptibility to a SBE glaciation.

2. A conceptual model
The global silicate weathering flux W can be written:

$$W = W_0 \cdot \left(\frac{CO_2}{CO_{20}}\right)^A \cdot e^{(T-T_0)\cdot(B+C)} \quad \text{(1)}$$

Where $W_0 = 6.65 \times 10^{12} molCyr^{-1}$ denotes a baseline silicate weathering flux value, $A = 0.25$, $B = 0.056$ and $C = 0.017$ respectively denote sensitivity to CO_2 (measured in parts per million and normalized to pre-industrial levels $CO_{20} = 280ppm$), Arrhenius temperature kinetic sensitivity, and sensitivity to changes in runoff and hydrology coupled to temperature (Walker et al, 1981). The relationship between silicate weathering and the long-term dynamics of CO_2 can be expressed in its simplest possible form as:

$$\frac{dCO_2}{dt} = \frac{D}{D_0} - \frac{W}{W_0} \cdot \frac{A}{A_0} \quad \text{(2)}$$

Where $\frac{D}{D_0}$ and $\frac{A}{A_0}$ respectively denote the normalized values of the tectonic outgassing rate and the land surface area available for silicate weathering (relative to present day in each case), and CO_2 can therefore be computed as simply $CO_2 = CO_{20} \cdot \int \frac{dCO_2}{dt} dt$ to convert to units of parts per million (ppm). Schwartzman (Schwartzman & Volk, 1989, Schwartzman 1999, 2017) devised a formulation by which biotic enhancement of weathering could be estimated

without explicit parameterization of the hypothetical weathering rate on an abiotic Earth. Setting (2) to steady state, rearranging and labelling $\frac{D}{D_0} = \bar{D}$ and $\frac{A}{A_0} = \bar{A}$, one can write the relative biotic enhancement of the global silicate weathering flux BEW as:

$$BEW = \frac{W_{biotic}}{W_{abiotic}} = \frac{\bar{D}_{biotic}}{\bar{D}_{abiotic}} \cdot \frac{\bar{A}_{abiotic}}{\bar{A}_{biotic}} \tag{3}$$

Schwartzman's formulation entails substituting (1) into (3) then solving for $\frac{W_{0\ biotic}}{W_{0\ abiotic}}$, i.e. the present day biotic enhancement of weathering:

$$BEW_0 = (\frac{CO_{2\ abiotic}}{CO_{2\ biotic\ 0}})^A \cdot e^{(T_{abiotic}\ -T_{biotic\ 0})\cdot(B+C)} \cdot \frac{\bar{D}_{biotic\ 0}}{\bar{D}_{abiotic}} \cdot \frac{\bar{A}_{abiotic}}{\bar{A}_{biotic\ 0}} \tag{4}$$

Where for each term, the zero subscript refers to the boundary conditions necessary for steady state in (2) at present day. The CO_2 and temperature levels given refer to those necessary for steady state in (2) on a planet Earth with and without life. An advantage (Schwartzman, 2017) of (4) is that one can then express the biotic enhancement of weathering relative to its present-day magnitude $\overline{BEW} = \frac{BEW}{BEW_0}$, which allows one to cancel out the abiotic terms. This cancellation entails the assumption that an abiotic planet Earth would have been significantly less variable over its history than the real Earth, such that for each of the above variables; i.e. for $X = (T, W, D, A, CO_2)$, $X_{abiotic} \approx X_{abiotic\ 0}$. Thus, Schwartzman's measure of biological enhancement of silicate weathering relative to that at present day is:

$$\overline{BEW} = (\frac{CO_{2\ biotic}}{CO_{2\ biotic\ 0}})^A \cdot e^{(T_{biotic\ 0}-T_{biotic})\cdot(B+C)} \cdot \frac{\bar{D}_{biotic}}{\bar{D}_{biotic\ 0}} \cdot \frac{\bar{A}_{abiotic\ 0}}{\bar{A}_{abiotic}} \tag{5}$$

The "runaway" nature of the positive feedback between increasing ice cover, increasing planetary albedo and decreasing planetary temperature, means that equilibration of the hydrological cycle processes relevant to a snowball Earth occur over timescales of the order of ~20 years (Pierrehumbert, 2005); i.e. far shorter than the thousand-year timescales relevant to the silicate weathering "thermostat" (Walker et al, 1981, Berner et al, 1983). Consequently, in a simplistic model of geologic timescale changes, it is acceptable to discretize the changes in ice-cover and planetary albedo associated with glacial entry and exit (North, 1975).We therefore set planetary albedo α constant outside the temperature region $T_{out} \leq T \leq T_{in}$ corresponding to the ice albedo instability, whilst if temperature falls below T_{in} from a non-glaciated state the albedo instantaneously jumps to a maximal "snowball Earth" value $\alpha_{sbe} = 0.7$, whereas if temperature enters this unstable region from within a snowball, albedo jumps in the opposite direction to the lower value $\alpha_{non\ sbe} = 0.3$ (Caldeira & Kasting, 1992, Pierrehumbert et al, 2005). The "time derivative" of planetary albedo therefore comprises one of three distinct values, depending on temperature's current value and its trajectory:

$$\frac{\partial \alpha}{\partial t}_{T>T_{in}\ ||\ T<T_{SBE}} = 0$$

$$\frac{\partial \alpha}{\partial t}_{T_{out}\leq T\leq T_{in}\ \&\ \frac{dT}{dt}<0} = \alpha_{sbe} - \alpha_{non\ sbe}$$

$$\frac{\partial \alpha}{\partial t}_{T_{out} \leq T \leq T_{in} \ \& \ \frac{dT}{dt} > 0} = \alpha_{non \ sbe} - \alpha_{sbe} \tag{6}$$

Thus, once temperature falls below a critical threshold T_{IN}, a positive feedback between increasing ice cover and decreasing planetary temperature causes planetary albedo to (geologically) jump from a low value $\alpha_{non \ sbe}$ characteristic of the non-snowball Earth state, to a higher value α_{sbe} characteristic of the equilibrium state at the end of this ice albedo feedback, whilst temperature correspondingly jumps to a minimum value T_{SBE} characteristic of global scale glaciation. The analogous process occurs in the opposite direction once temperature rises above a deglaciation threshold T_{out}.

The equilibrium radiative temperature of a "blackbody" planet Earth is given (in Kelvin) by:

$$T = \left(\frac{(1-\alpha)S}{4\sigma}\right)^{\frac{1}{4}} \tag{7}$$

Where $\sigma = 5.67367 \times 10^{-8} Wm^{-2}$ is the Stefan Boltzmann constant (relating the energy radiated by a surface to the fourth power of its absolute temperature), the factor $\frac{1}{4}$ is the ratio between the area of the disc intercepting incoming solar radiation and the sphere emitting it, S is incoming solar radiation. For the simple first-order arguments we wish to make here, we use a linearized approximation to the radiative component of planetary equilibrium temperature, which gives the actual temperature (in Celsius) when added to a simple formulation of the climate sensitivity (North et al, 1981, North, 1990):

$$T = \frac{1}{D}\frac{S(1-\alpha)}{4} - \frac{E}{D} + \beta \ln\left(\frac{CO_2}{CO_{2\,0}}\right) \tag{8}$$

Where $E = 203.3 Wm^{-2}C^{-1}$, and $D = 2.09 Wm^{-2}C^{-1}$ are derived from the results of complex climate models and represent the effect of water vapour and infrared absorbing gases, and $\beta = 4.33$ corresponds to an equilibrium climate sensitivity of $\beta \ln(2) = 3.002°C$ per doubling of CO_2, which is compatible with sensitivity analyses performed on ensembles of high resolution climate models (Cox et al, 2018). The solar luminosity flux can be related to the time of interest by (Gough, 1981, Kasting, 2005):

$$S_{t_{ybp}} = \frac{S_0}{1 + 0.4\frac{t_{ybp}}{t_{Earth}}} \tag{9}$$

Where $S_0 = 1368 Wm^{-2}$ is the current solar luminosity flux, t_{ybp} is the time in billions of years before present day and $t_{Earth} = 4.6$ is the age of the Earth in billions of years. (For the simulations shown below we set $t_{ybp} = 0.7$). Our objective here is simply to derive a simple relationship between the temperature thresholds relevant to the unstable region of the ice-albedo feedback $T_{out} \leq T \leq T_{in}$ and CO_2, which is satisfactory to inform upon our arguments about biological weathering enhancement. Substituting, we have the CO_2- level corresponding to a prescribed glaciation entry threshold T_{in}, at a given point in Earth history:

$$CO_{2\,in} = CO_{2\,0} \cdot e^{\frac{1}{\beta}\left(T_{in} - \frac{1}{B}\frac{S_{t_{ybp}}(1-\alpha_{non\,sbe})}{4} + \frac{A}{B}\right)} \tag{10}$$

In the first instance, we can examine plausible levels of biological weathering enhancement relevant to the snowball Earth problem by directly substituting $CO_{2\,in}$ and T_{in} into (5), and taking the biotic terms as their present-day baseline values:

$$\overline{BEW}_{SBE} = \left(\frac{CO_{2\,in}}{CO_{2\,biotic\,0}}\right)^A \cdot e^{(T_{biotic\,0}-T_{in})\cdot(B+C)} \cdot \frac{\overline{D}_{SBE}}{\overline{D}_{biotic\,0}} \cdot \frac{\overline{A}_{biotic\,0}}{\overline{A}_{SBE}} \tag{11}$$

Then, setting (2) to steady state and substituting in (1), the temperature T_{in} and $CO_{2\,in}$ combination necessary for the system to move into the unstable region of the ice-albedo feedback and trigger a global scale glaciation event must conform to:

$$W_0 \cdot \left(\frac{CO_{2\,in}}{CO_{20}}\right)^A \cdot e^{(T_{in}-T_0)\cdot(B+C)} = \frac{D}{D_0}\frac{A_0}{A} \tag{12}$$

We can also write the magnitude ε of the enhancement of the silicate weathering flux as a function of a maximal enhancement factor ε_{max}, the deviation that temperature T exhibits from the optimum T_{opt} for the growth of the biota responsible for this weathering enhancement (for the sake of parsimony we assume both positive and negative temperature deviation from optimum are equally detrimental) and the sensitivity k of biological weathering enhancement to this temperature deviation:

$$\varepsilon = \varepsilon_{max} \cdot e^{-k|T-T_{opt}|} \tag{13}$$

In the interests of parsimony and clarity we approximate $T_{opt} \approx 15°C$ as a broad average for optimal productivity and take k as the parameter encompassing the nuances of the distinct ecophysiology of different species. As discussed above, our central hypothesis is that the Neoproterozoic Earth system, in which any biotic weathering rate enhancement was likely driven by lichens and bacteria on the land surface, was characterized by a much lower temperature sensitivity than the Earth system of the Phanerozoic:

$$k_{Precambrian} \ll k_{Phanerozoic} \tag{14}$$

We begin by rewriting Schwartzman's metric in (3)-(5) using a modified silicate weathering flux, i.e. multiplying (1) by (10):

$$W_{biotic} = W_{0\,abiotic} \cdot \left(\frac{CO_2}{CO_{20}}\right)^A \cdot e^{(T-T_0)\cdot(B+C)} \cdot (1 + \varepsilon_{max} \cdot e^{-k|T-T_{opt}|}) \tag{15}$$

A crucial theoretical consideration concerns the relationship between biotic enhancement of silicate weathering and susceptibility to snowball Earth. If life has changed the susceptibility that Earth exhibits to snowball Earth (for a given set of abiotic boundary conditions), then the conditions describing the entry point to a snowball Earth are slightly modified to:

$$W_{0\,abiotic} \cdot \left(\frac{CO_{2\,in}}{CO_{20}}\right)^A \cdot e^{(T_{in}-T_0)\cdot(B+C)}(1 + \varepsilon_{max} \cdot e^{-k|T_{in}-T_{opt}|}) = \frac{D}{D_0}\frac{A_0}{A} \tag{16}$$

Where obviously $\varepsilon_{max} = 0$ causes (16) to revert to the same form as (12). Thus far this is merely a relabelling exercise. But suppose that we set $T_{opt} \approx T_0 \approx 15°C$ (i.e. assume that the optimum temperature for biotic weathering enhancement does not differ significantly from the current planetary average). Then when $T = T_0$ (12) is equal to:

$$W_{0\,abiotic}(1 + \varepsilon_{max}) = W_0 \tag{17}$$

(where W_0 is the above actual value of the silicate weathering flux used as a baseline in simple climate models). We can parameterize:

$$\varepsilon_{max} = \varphi(BEW - 1) \tag{18}$$

(where $2 \leq BEW \leq 5.4$ denotes bulk enhancement of chemical weathering by life, estimated within various existing modelling and empirical studies, discussed in detail by Schwartzman (Schwartzman, 2017), and φ is a tuneable parameter (see figure 2)). Which therefore allows us to estimate the baseline scaling factor for the silicate weathering flux on a hypothetical abiotic planet:

$$W_{0\ abiotic} \approx \frac{W_0}{BEW} \tag{19}$$

Formally therefore, the crux of the hypothesis on which we focus here is that:

$$k_{Precambrian} < k_{in} \ll k_{Phanerozoic} \tag{20}$$

Which amounts to the idea that biological evolution drove changes in the temperature sensitivity of the terrestrial biosphere that caused, under comparable abiotic boundary conditions, Earth to cease to become susceptible to a snowball Earth event after the colonization of the land by vascular plants, and the rise of complex soil surfaces etc, into the Phanerozoic. Using (12) and (16) the following state of affairs describes necessary and sufficient conditions for a difference between the two formulations of biotic enhancement of silicate weathering in respect of susceptibility to SBE inception:

$$W_0 \cdot \left(\frac{CO_{2\ in}}{CO_{20}}\right)^A \cdot e^{(T_{in} - T_0)\cdot(B+C)} \leq \frac{D}{D_0}\frac{A_0}{A} \tag{21}$$

$$\frac{W_0}{BEW} \cdot \left(\frac{CO_{2\ in}}{CO_{20}}\right)^A \cdot e^{(T_{in} - T_0)\cdot(B+C)}(1 + \varepsilon_{max} \cdot e^{-k|T_{in} - T_{opt}|}) = \frac{D}{D_0}\frac{A_0}{A} \tag{22}$$

If (21) is an equality (i.e. the system nearly enters the unstable region of the ice-albedo feedback without biotic weathering enhancement, but fails to do so), (21) and (22) can be equated and we can divide through by the left hand side of (21) and solve for the maximum temperature sensitivity k_{max} at which this "amplification" effect might make a difference:

$$k_{max} = \ln\left(\frac{\varepsilon_{max}}{BEW - 1}\right)^{\frac{1}{|T_{in} - T_{opt}|}} \tag{23}$$

Which obviously requires $\varepsilon_{max} > BEW - 1$ for non-zero k. In summary, we contend that biological evolution has introduced a variability into k_{in} during Earth's history, which has resulted in the weathering system coming into equilibrium with different $CO_{2\ in}, T_{in}$ combinations at distinct points in time.

3. Results
Figure 1 depicts example simulations, figures 2 and 3 sensitivity analysis to key parameters. In light of the above discussion regarding the poor constraints on parameters within even the most sophisticated high-resolution models, we emphasize that the results given here should be viewed as ultimately qualitative and intended to emphasize a key un-investigated quantity. Figure 1 shows the difference between weathering and the product of degassing rate and weatherable continental area, at steady state, at a proscribed value (left hand columns) for the temperature T_{in} at which a runaway ice-albedo feedback to global scale glaciation occurs.

This proscribed value for T_{in} determines (by equation (10)) a corresponding greenhouse threshold for glacial entry $CO_{2\,in}$ (X-variable in the right-hand columns). The red line corresponds to temperature-sensitive biotic silicate weathering enhancement corresponding to equation (16), the blue to Schwartzman's (1999, 2017) original, temperature-"insensitive" (beyond direction kinetic dependence in the baseline reaction rate) corresponding to equation (12). Note that the system becomes less meaningful the further the steady state is from the dashed line, because this corresponds to increasing deviation from steady state. The key quantity of interest is the value of T_{in} at which this threshold (i.e. a triggering of a SBE event) is crossed. A comparison between the red lines in the left column of the upper and lower panels illustrates that at a lower value of k (i.e. lower sensitivity of biotic weathering enhancement to deviation from optimal temperature) reduces the temperature threshold at which a SBE event is induced under equivalent boundary conditions.

This basic idea is robust to changes in the value of k used, as well as to changes in φ (see equation (18)), which measures the sensitivity between the ε_{max} parameter in equation (16) and the baseline biotic enhancement of weathering BEW factor taken from experiments (Schartzman, 2017). A large value of φ corresponds to a larger bulk value for the biotically enhanced weathering flux (across all temperatures, regardless of the biota's sensitivity to deviation from optimum), thus effectively flattens out the curve of the relationship between T_{in} and the SBE entry threshold for a given value of sensitivity k. (This is illustrated by figures 2 and 3, which show results of the form of the left hand column of figure 1, across a wider range of values for these parameters). Also depicted in figures 2 and 3 (purple line) is the threshold value for the temperature sensitivity k_{max} (equation (23)), which imposes a constraint on how high this sensitivity can become whilst biotically enhanced silicate weathering rate still exceeds the baseline abiotic rate (and exhibits an asymptotic decline with T_{in}).

4. Conclusions

As noted above, our intention here is to highlight a key unconstrained relationship that potentially connects biology with a central outstanding problem in climate science. Our key result is the comparison between relatively high and relatively low temperature sensitivities in the biotic weathering enhancement factor (upper and lower rows, figure 1). If biotic enhancement of silicate weathering is driven by a highly temperature sensitive biosphere, contribution of the biota to the initiation of a snowball Earth is only feasible at a relatively high value of T_{in}. Conversely, if such enhancement is relatively temperature insensitive, biology may conceivably increase the likelihood of SBE initiation even when so-doing necessitates tolerance of a relatively low value of T_{in}. The key proposition we make is therefore that any such biological "amplification" of SBE susceptibility was more probable in a lichen-dominated Precambrian Earth system than a Moss and (later) plant-dominated Phanerozoic Earth system.

In essence, we suggest that the upper row of figure 1 is qualitatively representative of the Precambrian biosphere and the lower row of that of the Phanerozoic biosphere. Our core idea is relevant to the snowball Earth problem if (for the parameter choices used), $T_{in} \leq 10°C$, because then only the low-temperature-sensitivity "Precambrian" system can induce a SBE event. Crucially, we suggest that at certain points in Earth's history, the baseline silicate weathering flux (just) self-limited on the approach to a snowball Earth (via the temperature dependence of the weathering reaction), but that biology evolved to overcome this by

compensating for the temperature decrease (due to the intensity of the selection pressure to extract nutrients from rocks etc). This may have been sufficient to tip the system into a snowball Earth state; in a context in which it would otherwise have remained merely at the edge of this state.

Clearly it is not possible to reconstruct the species composition by mass, land surface coverage and temperature tolerances of any (hypothetical) Precambrian land biota. We justify our qualitative statement about temperature tolerance purely on the basis of the unique eco-physiological robustness of lichens. Whilst not wishing to ignore the existence of cold and heat-adapted vascular plants, it is clear that evolutionary adaptation is capable of pushing lichen physiology to a far wider temperature range than vascular plant physiology. Thus, a terrestrial biosphere dominated by vascular plants will necessarily have a far narrower window of tolerance for deviation from the optimal temperature for growth and photosynthetic carbon fixation. This statement will still hold regardless of the uncertainties in estimating such physiological properties in ancient land life.

Previous work has linked lichen-induced weathering to snowball Earth (Lenton & Watson, 2004, Mills et al, 2011, 2017). But these studies have focused on the connection between PO_4^{3-} extraction from the land surface in relation to connections between the marine phosphate reservoir and ancient oxygen levels (Lenton & Watson, 2004), or on changes in degassing rate and their relationship to glacial inception (Mills et al, 2017). The temperature sensitivity of the silicate weathering flux (Walker et al, 1981) implies a self-limitation process for any (biotically or abiotically) weathering-induced glaciation: As T_{in} is approached, weathering necessarily declines, slowing the rate of any such approach. When we use the phrase "biological amplifier" above, we mean to suggest that biotic enhancement of weathering may potentially have compensated for such a decline and permitted entry to the unstable region of the ice-albedo feedback. The boundary conditions relative to which this is possible (temperature, degassing rate, land surface area, hydrological cycle feedbacks) are obviously crucial additional parameters that must be constrained in order to assess whether this is plausible (and are obviously not something we have addressed here). Experiments cross referencing the existing estimates (Schwartzman, 2017) for various forms of biological enhancement of weathering against temperature extremes are urgently needed, so as to determine the sensitivity to temperature of biotic weathering enhancement. If any such sensitivity is significant and differs between lichens and other photoautotrophs and significant weathering-enhancing organisms, then we propose that our arguments here highlight a potentially important missing parameter that should be included in high-resolution models of snowball Earth.

References

Abbot, D.S., Voigt, A., Branson, M., Pierrehumbert, R.T., Pollard, D., Le Hir, G., Koll, D. D. B. "Clouds and snowball Earth deglaciation." Geophys. Res. Lett. 39, L20711 (2012).

Abbot, D.S. Voigt, A., Li, D. Le Hir, G., Pierrehumbert, R.T., Branson, M., Pollard, D., Koll, D.B.B. "Robust elements of Snowball Earth atmospheric circulation and oases for life." J. Geophys. Res. Atmos. 118, 6017–6027 (2013).

Aghamiri R, Schwartzman DW "Weathering rates of bedrock by lichens: a mini watershed study." *Chem Geol* 188: 249-259. (2002).

Arnaud, E., Halverson, G.P. & Shields-Zhou, G. "The Geological record of Neoproterozoic Ice Ages". Geological Society of London. (2011).

Benn, D.I., Le Hir, G., Bao, H., Donnadieu, Y., Dumas, C., Fleming, E.J. Hambrey, M.J., Mcmillan, E.A., Petronis, M.S. Ramstein, G., Stevenson, C.T.E., Wynn, P.M., Fairchild, I.J. "Orbitally forced ice sheet fluctuations during the Marinoan Snowball Earth glaciation". Nat. Geosci. 8, 704–708 (2015).

Berner, R., Lasaga, A. & Garrels, R. "The Carbonate-Silicate Geochemical Cycle and its Effect on Atmospheric Carbon Dioxide over the Past 100 Million Years" (PDF). American Journal of Science. 283: 641–683. (1983).

Bormann BT, Wang D, Bormann FH. "Rapid, plant-induced weathering in an aggrading experimental ecosystem." *Biogeochemistry* 43: 129-155. (1998).

Brady PV, Dorn RI, Brazel AJ. "Direct measurement of the combined effects of lichen, rainfall, and temperature on silicate weathering." *Geochim Cosmochim Acta* 63: 3293-3300. (1999).

Budyko, M.I. "The effect of solar radiation variations on the climate of the Earth." Tellus 21, 611–619 (1969).

Butterfield, N.J. "Probable Proterozoic Fungi". Paleobiology 31(1). 165-182. (2005).

Caldeira, K. & Kasting, J.F. "The life span of the biosphere revisited". Nature 360, 721-723. (1992).

Caldeira, K. and Kasting, J.F. "Susceptibility of the early Earth to irreversible glaciation caused by carbon dioxide clouds. Nature, 359, 226–228. (1992)b

Carns, R.C., Light, B. & Warren, S.G. "The spectral albedo of sea ice and salt crusts on the tropical ocean of snowball Earth II: Optical modelling." J. Geophys. Res. (Oceans). 121. 5217-5230. (2016).

Chamberlain, J.W. "Changes in the planetary heat balance with chemical changes in air". Planetary & Space Science 28. 1011-1018. (1980).

Chen J, Blume H-P, Beyer L. "Weathering of rocks induced by lichen colonization–a review." *Catena* 39: 121-146. (2000).

Clark, B.M., St-Clair, L.L., Mangelson, N.F., Rees, L.B., Grant, P.G., & Bench, G.S. "Characterisation of mycobiont adaptations in the foliose lichen Xanthoparmelia chlorochroa (Parmeliaceae)" Am. Journ. Bot. 88. 1742-1749. (2001).

Cox, G.M., Halverson, G.P., Minarik, W.G., Le Heron, D.P., Macdonald, F.A., Bellefroid, E.J., Strauss, J.V. "Neoproterozoic iron formation: An evaluation of its temporal, environmental and tectonic significance". Chem. Geol. 362, 232–249 (2013).

Cox, P.M., Huntingford, C. & Williamson, M.S.W. "Emergent constraint on equilibrium climate sensitivity from global temperature variability". Nature 553. 319-323 (2018).

Donnadieu, Y., Godderis, Y., Ramstein, G., Nedelec, A.& Meert, J. "A 'snowball Earth' climate triggered by continental break-up through changes in runoff". Nature 428, 303-306 (2004).

Evans, D.A.D. "Stratigraphic, geochronological and paleomagnetic constraints on the Neoproterozoic climate paradox". Am. J. Sci. 300. 347-433. (2000).

Evans, D.A.D. & Raub, T.D. "Neoproterozoic glacial palaeolatitudes: A global update" in "The Geological Record of Neoproterozoic Glaciations", Arnaud, E., Halverson, G.P. & Shields-Zhou, G., Eds. (Geological Society of London, 2011), pp. 93–112.

Fairchild, I.J. "Balmy shores and icy wastes: The paradox of carbonates associated with glacial deposits in Neoproterozoic times", in Sedimentology Review 1, Wright, V.P., Ed. (Blackwell, 1993), pp. 1–16. (1993).

Gannutz, T.P. "Effect of environmental extremes on lichens". Soc. bot. Fr., Colloque sur les Lichens 169-179. (1967).

Gough, D.O. "Solar interior structure and luminosity variations" Solar Phys. 74, 21-34. (1981)

Green, J.S.A. "Reflections on the Earth's albedo: A collection of scattered thoughts". Weather 57, 431-459. (2002).

Guidry, M. W., and F. T. Mackenzie. "Apatite weathering and the Phanerozoic phosphorus cycle" Geology, 28, 631–634. (2000).

Halverson, G.P., Poitrasson, F., Hoffman, P.F. , Nédélec, A., Montel, J.-M., Kirby, J., "Fr isotope and trace

element geochemistry of the Neoproterozoic syn-glacial Rapitan iron formation". Earth Planet. Sci. Lett. 309, 100–112 (2011).

Hatfield, J.L. & Prueger, J.H. "Temperature extremes: Effect on plant growth and development". Weather and climate extremes 10 (A). 4-10. (2015).

Heckman, D. S., Geiser, D.M., Eidell, B.R., Stauffer, R.L., Kardos, N.L. & Hedges, S.B. "Molecular evidence for the early colonization of land by fungi and plants" Science, 293, 1129– 1133. (2001).

Hoffman, P.F. "On Cryogenian (Neoproterozoic) ice-sheet dynamics and the limitations of the glacial sedimentary record." South Afr. J. Geol. 108, 557–577 (2005).

Hoffman, P.F. "Cryoconite pans on Snowball Earth: supraglacial oases for Cryogenian eukaryotes?" Geobiology 14, 531-542. (2016).

Hoffman, P.F., Kaufman, A.J., Halverson, G.P. & Schrag, D.P. "A Neoproterozoic Snowball Earth". Science 281, 1342–1346 (1998).

Hoffman, P.F. & Schrag, D.P. "The snowball Earth hypothesis: Testing the limits of global change". Terra Nova. 14(3). 129-155. (2002).

Hoffman, P.F. & Halverson, G.P. "Otavi Group of the western Northern Platform, the Eastern Kaoko Zone and the western Northern Margin Zone", vol. 2 of "The Geology of Namibia", Miller, R.M., Ed. (Geological Survey of Namibia, 2008), pp. 13.69–13.136. (2008).

Hoffman, P.F., Abott, D.S., Askenazy, Y., Benn, D.I., Brocks, J.J., Cohen, P.A., Cox, G.M., Creveling, J.R.,Donnadieu, Y., Erwin, D.H., Fairchild, I.J., Ferreira, D., Goodman, J.C., Halverson, G.P. Jansen, M.F., Le Hir, G., Love, G.D., Macdonald, F.A., Maloof, A.C., Partin, C.A., Ramstein, G., Rose, B.E.J., Rose, C.V., Sadler, P.M., Tziperman, E., Voigt, A. & Warren, S.G. "Snowball Earth climate dynamics and Cryogenian Geology-Geobiology". Science Advances 3. 1-43. (2017).

Horodyski, R. J., and L. P. Knauth "Life on land in the Precambrian" Science, 263, 494– 498. (1994).

Jackson TA, Keller WD. "A comparative study of the role of lichens and inorganic processes in the chemical weathering of recent Hawaiian lava flows." *Am J Sci* 269: 446-466. (1970).

Jones D. &Wilson M.J. "Chemical activity of lichens on mineral surfaces; a review." *Int Biodeterior* 21: 99-104. (1985).

Kasting, J.F., Whitmore, D.P. & Reynolds, R.T. "Habitable zones around main sequence stars". Icarus 101. 108-128. (1993).

Kasting, J.F. "Methane and climate during the Precambrian Era". Precambrian. Res. 137. 119-129. (2005).

Kershaw, K.A. "Physiological Ecology of lichens". Cambridge. (1985).

Kirschvink, J.L. "Late Proterozoic Low-Latitude Global Glaciation: the Snowball Earth". The Proterozoic Biosphere: A Multidisciplinary Study. J.W. Schopf & C.Klein. Cambridge University Press. pp 51-52. (1992).

Li Z, Liu L, Chen J, Teng HH "Cellular dissolution at `hypha-and spore-mineral interfaces revealing unrecognized mechanisms and scales of fungal weathering." *Geol* 44: 319-322. (2016).

Lenton, T.M. "Land and ocean Carbon cycle feedback effects on global warming in a simple Earth system model". Tellus 52b. 1159-1188. (2000).

Lenton, T.M. & Watson, A.J. "Biotic enhancement of weathering, atmospheric oxygen and carbon dioxide in the Neoproterozoic" Geophys. Res. Lett. 31. L05202. (2004).

Lenton TM, Crouch M, Johnson M, Pires, N. & Dolan, L. "First plants cooled the Ordovician." *Nat Geosci* 5: 86-89. (2012).

Lenton, T.M., Daines, S.J. & Mills, B.J.W. "Copse reloaded: An improved model of biogeochemical cycling over Phanerozoic time". Earth Science Reviews 178, 1-28. (2018).

Lewis, J.P., Weaver, A.J. & Eby, M. "Snowball versus slushball Earth: Dynamic versus non-dynamic sea ice?" J. Geophys. Res. 112, C111014. (2007).

Macdonald, F.A., Strauss, J.V., Rose, C.V., Dudás, F., D. P. Schrag, D.P., Stratigraphy of the Port Nolloth Group of Namibia and South Africa and implications for the age of Neoproterozoic iron formations. Am. J. Sci. 310, 862–888 (2010).

McKay, C.P. & Lorenz, R.D. & Lunine J.I."Analytic solutions for the anti-greenhouse effect: Titan and the early earth" Icarus 137, 56-61. (1999).

Mills, B.M., Watson, A.J., Goldblatt, C., Boyle, R.A. & Lenton, T.M. "Timing of Neoproterozoic glaciations linked to transport-limited global weathering". Nature Geoscience 4. 861-864 (2011).

Mills BJW; Scotese CR; Walding NG; Shields GA; Lenton TM (2017) "Elevated CO_2 degassing rates prevented the return of Snowball Earth during the Phanerozoic", Nature Communications, 8 doi: 10.1038/s41467-017-01456-w

Moulton KL, Berner RA "Quantification of the effect of plants on weathering: studies in Iceland." *Geol* 26: 895-

898. (1998).

Nakajima, S., Hayashi, Y. & Abe, Y. "A study on the "runaway greenhouse effect" with a one dimensional radiative convective equilibrium model" J. Atmos. Sci. 49. 2256-2266. (1992)

North. G.R. "Analytical solution to a simple climate model with diffusive heat transport". J. Atmos. Sci. 32. 1301-1307. B (1975).

North, G.R. Cahalan, R.F., Coakley, J.A. "Energy balance climate models". Rev. Geophys. Space. Phys. 19(1). 91-121. (1981).

North, G.R. "Multiple solutions in energy balance climate models". Paleogeogr. Paleoclim. Paleoecol. 82. 225-235. (1990).

Opdyke, B.N. & Wilkinson, B.H. "Carbonate mineral saturation state and cratonic limestone accumulation". Am. J. Sci. 293, 217–234 (1993).

Pierrehumbert, R.T. "Climate Dynamics of a hard snowball Earth". Journ. Geophys. Res. 110, D01111. (2005).

Pollard, D & Kasting, J.F. "Climate-ice sheet simulations of Neoproterozoic glaciation before and after collapse to Snowball Earth", in "The Extreme Proterozoic: Geology, Geochemistry, and Climate", G. S. Jenkins, M. A. S. McMenamin, C. P. McKay, L. Sohl, Eds. (American Geophysical Union, 2004), pp. 91–105. (2004).

Vernadsky, V. I. The biosphere. New York, NY: Copernicus. (1998, 1926).

Redecker D. Kodner R. & Graham L.E. "Glomalean fungi from the Ordovician." Science 289, 1920-1921. (2000).

Sancho, L.G.,de la Torre, R., Horneck, G., Ascaso, C., de los Rios, A., Pintado, A., Wierzschos, J. & Schuster, M. "Lichens Survive in Space: Results from the 2005 LICHENS Experiment". Astrobiology 7(3). 443-454 (2007).

Schwartzman, D.W. & Volk, T. "Biotic enhancement of weathering and the habitability of Earth". Nature 430. 457-460 (1989).

Schwartzman, D.W. "Life, temperature and the Earth" Columbia University Press (1999).

Schwartzman, D.W. "Life's critical role in the long-term Carbon cycle: The biotic enhancement of weathering" AIMS Geosciences 3(2).216-238. (2017).

Sellers, W.D. "A global climatic model based on the energy balance of the Earth–atmosphere system." J. Appl. Meteorol. 8, 392–400 (1969).

Selosse, M.A. & le Tacon, F. "The land flora: A phototroph-fungus partnership". Trends Ecol. Evol. 13(1). 15-20 (1998).

Stretch RC, Viles HA "The nature and rate of weathering by lichens on lava flows on Lanzarote." *Geomorphol* 47: 87-94. (2002).

Taylor, T.N., Hass, H., Remy, W. & Kerp, H. "The oldest fossil lichen". Nature 378, 244. (1995).

Retallack, G.J. "Were the Ediacaran fossils lichens?" Paleobiology, 20, 523-544. (1994).

Rignot, E. Mouginot & Scheuchl, J.B. "Ice flow of the Antarctic Ice Sheet". Science 333, 1427–1430 (2011).

Rogers, J. R. "Feldspars as a source of nutrients for microorganisms" Am. Mineral., 83, 1532–1540. (1998).

Urban, H., Stribny, B. & Lippolt, H.J. "Iron and manganese deposits of the Urucum District, Mato Grosso do Sul, Brazil. Econ. Geol. 87, 1375–1892 (1992).

Wahlen, M. "The global methane cycle". Ann. Rev. Earth. Plan. Sci. 21. 407-426. (1993).

Walker, JG., Hayes, P.B. & Kasting, J.F. 1981. "Negative feedback mechanism for the long-term stabilisation of Earth's surface temperature". Journ. Geophys. Res. 86. 9776-9782. (1981).

Warren, S.G., Brandt, R.E., Grenfell, T.C., McKay, C.P. "Snowball Earth: Ice thickness on the tropical ocean." J. Geophys. Res. 107, 31-1–31-18 (2002).

West, J.A., Galy, A. & Bickle, M. "Tectonic and climatic controls on silicate weathering". Earth. Plan. Sci. Lett. 235. 211-228. (2005).

Zambell CB, Adams JM, Goring ML. "Effect of lichen colonization on chemical weathering of hornblende granite as estimated by aqueous elemental flux." *Chem Geol* 291: 166-174. (2012).

Figures

Figure 1: Example steady state results given different formulations for biotic enhancement of silicate weathering

The proximity of different steady state results to SBE initiation assuming biotic weathering enhancement of the form given by equation (12) (blue lines) and by equation (16) (red lines). In each row, the left-most column shows the steady mass balances $\frac{W}{W_0} - \frac{D}{D_0}\frac{A_0}{A}$ for the formulations of weathering W given in equation (12) (blue lines) and (16) (red lines), plotted against T_{in} (leftmost column), and against $CO_{2\,in}$ (second from left). The next two columns in each row show the corresponding magnitudes of the silicate weathering fluxes, again plotted against $CO_{2\,in}$ (rightmost column) and T_{in} (second from right). Row A (above) shows a temperature-sensitive biotic enhancement factor with a relatively low sensitivity to deviation from optimal temperature $k = 0.01$, $\varphi = 2$, row B (below) shows a relatively high sensitivity $k = 1$, $\varphi = 2$. The dashed line shows the threshold that must be crossed for biotic weathering to further decrease the temperature from the steady state depicted, thus implicitly trigger a snowball Earth.

Figure 2: Sensitivity analysis focusing on parameters potentially influenced by directional changes in the physiology of the terrestrial biosphere.

Different rows show different values for the proportionality constant φ (see equation (18)) relating the parameter ε_{max} to (the empirically constrained) bulk enhancement of chemical weathering BEW. As shown in equation (18), ε_{max} dictates the magnitude of a theoretical maximum biologically enhanced weathering rate, as opposed to k which dictates the sensitivity of biotic enhancement of silicate weathering to temperature deviating from the biological optimum T_{opt} and different values of which are shown across the three columns. Individual graphs and axis labels are identical to top row of figure 1. Also depicted is the hypothetical maximum value of the biotic-weathering temperature sensitivity k_{max} (equation (23)). If ε_{max} is zero (top row) then active biotically enhanced weathering as we have formulated it here is impossible and reverts to the abiotic rate. Once active weathering enhancement by land life occurs (middle and lower rows), biotic initiation of glaciation is possible, but (as described in the main text), as the biota responsible for this weathering enhancement become increasingly temperature sensitive (lower row, left to right), such initiation becomes less probable. Note the difference in scale on the Y-axis of different rows.

Figure 3 Expanded sensitivity analysis.

As figure 2a, but analysis extended over a wider range of parameter values, illustrating the generality of the conclusions.