Modeling second-order boundary perception: A machine learning approach

Abbreviated Title: Modeling second-order boundary perception

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Abstract

<u>Background</u>: Visual pattern detection and discrimination are essential first steps for scene

analysis. Numerous human psychophysical studies have modeled visual pattern detection and

discrimination by estimating linear templates for classifying noisy stimuli defined by spatial

variations in pixel intensities. However, such methods are poorly suited to understanding sensory

processing mechanisms for complex visual stimuli such as second-order boundaries defined by

spatial differences in contrast or texture.

<u>Methodology / Principal Findings</u>: We introduce a novel machine learning framework for

modeling human perception of second-order visual stimuli, using image-computable hierarchical

neural network models fit directly to psychophysical trial data. We apply this framework to

modeling visual processing of boundaries defined by differences in the contrast of a carrier

texture pattern, in two different psychophysical tasks: (1) boundary orientation identification,

and (2) fine orientation discrimination. We utilize cross-validation analysis to optimize model

hyper-parameters, and demonstrate that our models are able to accurately predict human

performance on novel stimulus sets not used for fitting model parameters. We find that, like the

ideal observer, human observers take a region-based approach to the orientation identification

task, while taking an edge-based approach to the fine orientation discrimination task. We further

investigate how observers integrate contrast modulation across orientation channels, by fitting

psychophysical data with two models representing competing hypotheses, finding a preference

for a model which combines multiple orientations at the earliest possible stage. We argue that

this machine learning approach has much potential to advance the study of second-order visual

processing, and we outline future steps towards generalizing our method to modeling visual

segmentation of natural texture boundaries.

<u>Conclusions / Significance</u>: This study demonstrates that machine learning methodology can be

fruitfully applied to psychophysical studies of second-order visual processing.

Author Summary

Many naturally occurring visual boundaries are defined by spatial differences in features other

than luminance, for example by differences in texture or contrast. Quantitative models of such

"second-order" boundary perception cannot be estimated using the standard regression

techniques (known as "classification images") commonly applied to "first-order", luminance-

defined stimuli. Here we present a novel machine learning approach to modeling second-order

boundary perception using hierarchical neural network models. In contrast to previous modeling

of second-order boundary perception, we directly estimate network parameters using

psychophysical trial data. We demonstrate that our method can reveal different spatial

summation strategies that human observers utilize for different kinds of second-order boundary

perception tasks, and can be used to compare competing hypotheses of how contrast modulation

is integrated across orientation channels. We outline extensions of the methodology to other

kinds of second-order boundaries, including those in natural images.

Introduction

Many of the most common functions of sensory systems involve detection, identification or discrimination of particular stimuli. For example, a critically important ability of early visual processing is to segment images into distinct regions, which may correspond to cohesive surfaces or objects (Marr, 1982). To better understand the underlying mechanisms of visual surface segmentation, it would be desirable to fit biologically plausible models of surface segmentation to psychophysical data, and assess how well such models can account for independent datasets.

A widely used approach to modeling human psychophysics has been to assume that performance can potentially be understood in terms of how well a visual stimulus matches an internal "template", typically modeled as a linear spatial filter. This approach uses high-dimensional regression models fit to data from tasks in which a subject detects or classifies a sensory stimulus presented with superimposed white noise (Ahumada, 1996, 2002; Neri & Levi, 2006; Murray, 2011), to recover an estimate of the linear filter that best accounts for the data. This system-identification (SI) approach to psychophysics, often called "psychophysical reverse correlation" or "classification image analysis", parallels neurophysiology studies that fit linear filter models to neural responses elicited by white noise stimuli (e.g. DeAngelis, Ohzawa, & Freeman 1993; Chichilnisky, 2001). Psychophysical SI methods have been applied in varied problem domains and yielded tremendous insight into perceptual mechanisms (Abbey & Eckstein, 2002; Eckstein, Shimozaki, & Abbey, 2002; Li, Levi, & Klein, 2004; Neri & Levi, 2006; Morgenstern & Elder, 2012; McIlhagga & May, 2012; Kurki, Saarinen, & Hyvarinen, 2014).

One limitation of most previous psychophysical system identification studies has been the use of stimuli that are typically defined by spatial or temporal variations in first-order statistics like luminance or color. However, many natural visual stimuli such as occlusion boundaries (Fig. 1a, top) are defined by spatial variations in higher-order image statistics, e.g. texture or contrast, rather than simple luminance differences (Schofield, 1999; Konishi et al., 2003; Johnson & Baker, 2004, 2005; Martin, Fowlkes, & Malik 2004; DiMattina, Fox, & Lewicki 2012). Such boundaries defined by texture or contrast (Fig. 1a, bottom) are commonly referred to as "second-order" boundaries or edges (Baker, 1999; Landy & Graham, 2004). These stimuli have been of particular interest because their detection cannot be explained by simple

linear filters, and consequently human performance cannot be readily modeled using

conventional psychophysical SI methods. More generally, there is a need for a psychophysical

modeling approach that can handle a broader range of stimuli and tasks.

Here we present a novel machine learning method to extend psychophysical SI to more

complex naturalistic stimuli such as second-order boundaries. Our general approach is to fit

image-computable hierarchical neural network models of second-order vision (Fig. 2) directly to

psychophysical trial data, similar to recent studies using similar hierarchical network models to

characterize nonlinear responses in sensory neurons (Willmore, Prenger, & Gallant, 2010;

Vintch, Movshon, & Simoncelli, 2015; Harper et al. 2016; Rowenkamp & Sharpee, 2017). Our

application of this framework to second-order boundary detection generalizes a popular class of

biologically plausible psychophysical models of second-order vision known as "Filter-Rectify-

Filter" (FRF) models (Landy & Graham, 2004). However, in contrast to previous general

schemes for second-order vision (e.g. Malik & Perona, 1990; Bergen & Landy, 1991; Graham,

Beck & Sutter, 1992) and quantitative models (Zavitz & Baker, 2013; Westrick & Landy, 2013),

we take a machine learning approach in which we estimate the defining parameters of these

models by direct fitting to psychophysical trial data. This permits us to make direct tests of

model predictions on novel datasets in order to validate our models, and to evaluate competing

models.

We focus on contrast-defined second-order boundaries (Fig. 1a, b) since they are well

studied psychophysically (Dakin & Mareschal, 2000; Schofield & Georgeson, 1999, 2003;

Ledgeway & Smith, 1994; Ellemberg, Allen, & Hess 2006), and there are neurons in the early

mammalian visual cortex that give selective responses to contrast modulation stimuli (Mareschal

& Baker, 1998; Tanaka & Ohzawa, 2009; Rosenberg et al, 2010; Li et al., 2014). We model

performance on two tasks making use of contrast-defined boundaries: (1) identification of

boundary orientation, and (2) boundary orientation discrimination (Fig. 1c). We find that

subjects utilize spatial information in markedly different ways for these two tasks, using "region-

based" processing for the orientation identification task and "edge-based" processing for the

orientation discrimination task, in both cases consistent with an ideal observer.

We further demonstrate the power of this methodology for evaluating competing

hypotheses regarding FRF model architecture (Kingdom, Prins, & Hayes, 2003; Motoyoshi &

Nishida, 2004; Motoyoshi & Kingdom, 2007; Westrick & Landy 2013) by comparing the ability

of two different model architectures to fit human performance on a contrast edge detection task

in which the carrier pattern contains elements with two orientations. Post-hoc Bayesian model

comparison (Schwarz, 1978; Kass & Raferty, 1995; Bishop, 2006) demonstrates a preference for

a model in which carrier pattern orientation is integrated across channels by the second-stage

filters, consistent with previous psychophysical studies (e.g., Motoyoshi & Nishida, 2004).

Finally, we discuss potential applications of this methodology to future quantitative

studies of first- and second-order cue integration (Allard & Faubert, 2007; Saarela & Landy,

2012; Hutchinson, Ledgeway, & Baker, 2016) and natural boundary detection (McDermott,

2004; DiMattina et al., 2012). We suggest that the application of machine learning methodology

similar to that presented here can potentially help to better quantify visual processing of natural

occlusion boundaries and complex natural visual stimuli more generally.

Results

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Observers performed two different psychophysical tasks making use of contrast-modulated

boundary stimuli like those shown in Fig. 1 (see Methods). The first task was an orientation-

identification task (Fig. 1c, left) in which observers determined in which of two oblique

orientations (-/+ 45 deg, L/R) a near-threshold contrast boundary was presented, with varying

amounts of contrast modulation (Experiments 1 and 3). We also employed an orientation-

discrimination task (Fig. 1c, right) in which observers indicated the L/R orientation of a supra-

threshold contrast boundary, whose orientation was perturbed slightly from vertical by varying

amounts (-/+ 6-7 deg.) (Experiment 2). Trial-wise responses obtained from these experiments

were used to fit and evaluate a model (Fig. 2) implementing a "Filter-Rectifty-Filter" (FRF)

operation (Landy & Graham, 2004) on each stimulus image, with the goal of characterizing the

nature of spatial summation for perception of contrast boundaries, as well as the shape of the

second-stage filter nonlinearity (Fig. 2, shown in blue). We describe the model in greater depth

before presenting the experimental results.

Modeling framework

The model used to fit psychophysical trial data (Fig. 2) employed a first stage comprised of a

bank of fine-scale Gabor filters that compute local oriented energy in a manner similar to V1

complex cells (Adelson & Bergen, 1985). The second stage consisted of a pair of second-stage

filters, representing the two task alternatives (L/R), each instantiated by a weighted sum of the

normalized outputs of the first-stage filters. In contrast to the first-stage filters, these second-

stage filters analyze the image at a more coarse spatial scale, integrating variations in contrast

across the boundary. Finally, the outputs of these two second-stage filters are passed through a

static non-linearity (power function with exponent α) and then compared to decide on a trial-by-

trial basis if a given stimulus boundary appeared more likely to be tilted left or right (L/R), i.e.

the probability $0 < P(R) < 1$ of the stimulus being classified by the observer as R. The main goal

of Experiments 1 and 2 was to estimate the shapes of these second-stage filters.

To reduce model parameter space dimensionality, we perform downsampling between

the first- and second-stage filters, i.e. pooling of spatially adjacent first-stage filter responses.

Here we implemented three alternative methods: (1) simple averaging (AVG), (2) maximum

(MAX) (Goodfellow, Bengio, & Courville, 2016), and (3) sub-sampling (SUB) (Bergen &

Landy, 1991). In Experiment 1 we considered all three pooling rules; most analyses utilized

16x16 downsampling, but 3 downsampling sizes (22x22, 16x16 and 8x8) were compared. In

Experiments 2 and 3 we considered only AVG pooling and a single downsampling size

(Experiment 2: 22x22, Experiment 3: 12x12).

We implement the model's final (L/R) classification in two alternative ways: In the

deterministic model (DET), if the output of the L filter is larger than that of the R filter (plus the

bias term) so that $P(R) > 0.5$, the stimulus will be classified as R, otherwise it is classified as L.

In the *stochastic* model (STO), the output $P(R)$ specifies only the probability of classifying the

stimulus as R or L, thus introducing randomness to the model without requiring an additional

free parameter.

A common approach to make the estimation problem more tractable is to utilize

reasonable prior constraints on the model parameter space (Mineault, Barthelme, & Pack, 2009;

Wu, David & Gallant, 2006; Park & Pillow, 2011). Here we use two kinds of Bayesian priors:

(1) ridge-regression (Hoerl & Kennard, 1970; Bishop 2006) to penalize large weights (*ridge*),

and (2) ridge-regression combined with an additional smoothness prior (Mineault et al., 2009) to

penalize excessively "rough" second-stage filter weight profiles (*ridge + smooth*). Additional

details of the model are given in Methods.

Experiment 1: Boundary orientation identification

<u>Stimuli and task</u>

Observers were presented with contrast-defined texture boundaries with varying degrees of

modulation depth (Fig. 1b), and performed forced-choice judgments of whether the boundary

was oriented right- or left-oblique (45 degrees clockwise or counterclockwise, Fig.1c left). By

varying the depth of contrast modulation, we could manipulate the task difficulty. In Experiment

1-VAR (7 observers), a method of constant stimuli was used to vary contrast modulation depth

over a range spanning values near threshold but also including some levels producing near-

perfect, or chance, performance. In another version (Experiment 1-FIX, 3 observers) the contrast

modulation depth was held constant at a near-threshold level.

<u>Model fit to representative observers</u>

Fig. 3a shows the results of fitting the model (16x16 downsampling, AVG pooling) to data from

one representative observer (AMA) in Experiment 1-VAR. The top panels show estimated

second-stage filter weights as image maps across the spatial extent of the stimuli, with pixel

color indicating weight values. The black dashed lines in the bottom plots show mean 1-D

profiles, obtained by collapsing the 2-D weight maps orthogonally to the boundary orientations,

whereas thick solid lines (red = *ridge*, green = *ridge + smooth*) show profiles obtained from over

30 bootstrap-resampled training sets. We see that these mean 1-D profiles are nearly

indistinguishable from one another, all resembling a step-like function, consistent with "region-

based" processing. While many of the individual 2-D weights can be quite variable

(Supplementary Fig. S7), the 1-D weight profile magnitudes lie well above zero (Fig. 3, thin

dashed lines show +/- 1 SEM). The addition of the smoothing prior (*ridge + smooth*) results in

weighting functions that are very similar, but are less "noisy" in appearance, consistent with

previous results with classification images and receptive field modeling (Mineault et al., 2009;

Park and Pillow, 2011). Furthermore, all three pooling rules yielded consistent 2-D and 1-D

weight profiles (Supplementary Fig. S8).

Fig. 3b shows the model in Fig. 2 fit to data from a representative observer (JJF) in

Experiment 1-FIX. In this version of the experiment, the contrast modulation depth was kept

constant at approximately threshold level for each observer (Supplementary Table S1), similar to

most previous work in the classification image literature (Abbey & Eckstein, 2002; Murray,

2011). Here we see very similar results as for the observer in Experiment 1-VAR, also observing

evidence in favor of a region-based strategy for this task. As before, this was robust to the

pooling rule (Supplementary Fig. S9).

To assess the extent to which observers were employing the same spatial integration

strategy as an ideal observer, we fit the model to stimulus category labels rather than observer

responses. Fig. 3c shows the 2-D and 1-D profiles obtained for an ideal observer in Experiment

1-VAR, and we see that the ideal strategy is region-based. Similar results for ideal observer fit to

stimulus category labels in Experiment 1-FIX are shown in Supplementary Fig. S10.

<u>Edge-based vs. region-based analysis</u>

When finding a boundary between adjacent textures, the visual system might make use only of

texture elements close to the boundary ("edge-based"), or it might utilize the entirety of both

texture regions ("region-based"). A number of previous studies have investigated this question

for textures defined by orientation differences (Nothdurft, 1985; Gurnsey & Laundry, 1992;

Wolfson & Landy, 1998), but to the best of our knowledge this issue has not been addressed

systematically for contrast-defined textures.

Fig. 4 shows the 1-D averaged profiles of second-stage filter weights for all observers

(thin colored lines) and group average (thick black lines) in Experiment 1-VAR (Fig. 4a) and

Experiment 1-FIX (Fig. 4b). We see that the magnitudes of the 1-D weights are approximately

constant as one moves from the diagonal to the boundary, consistent with region-based

processing, and that these results are consistent for SUB and MAX pooling rules. A plot of the

normalized ideal observer 1-D weight profiles (30 bootstraps) is shown in Fig. 5a as a thick

black line with 95% confidence intervals (+/- 1.96 SEM) for the ideal observer plotted as dashed

black lines. We see that the normalized 1-D weight profiles for individual observers (dashed

color lines), and for means over observers (thick red dashed lines) generally lie within the 95%

confidence intervals of the ideal observer. Therefore, the performance of the human observers is

very much consistent with that of the ideal observer, both of which seem to integrate contrast

information across the whole region.

To test whether our finding of region-based processing was robust to increasing the

carrier spatial frequency, we ran an additional control version of the experiment on 3 naïve

observers (Experiment 1-HFC) in which we reduced the micro-pattern size from 32 to 8 pixels

(while increasing the density by a factor of 4). Such a stimulus would potentially engage many

more contrast-modulation tuned neurons having receptive fields localized to the boundary (Li et

al., 2014), potentially revealing edge-based processing. However, even with the high-frequency

carrier we still observed region-based processing (Fig. 5b), consistent with an ideal observer.

Second-stage filter nonlinearity

In Experiment 1, the best-fit expansive nonlinearity exponent α for the second-stage filters is

greater than unity for all observers, for both the *ridge* and *ridge + smooth* priors. For Experiment

1-VAR with AVG sampling, median α values were around 2 (*ridge*: median = 2.15, min = 1.70,

max = 2.85; *ridge + smooth*: median = 1.95, min = 1.70, max = 3.35, N = 7), and for Experiment

1-FIX we obtained median values closer to 1.5 (*ridge*: median = 1.50, min = 1.40, max = 1.60;

ridge + smooth: median = 1.60, min = 1.60, max = 1.90, N = 3). Similar results were obtained

for other downsampling methods (Supplementary Tables S2, S3), and the ideal observer was also

best fit with an expansive nonlinearity (AVG; Experiment 1-VAR: *ridge*: 4.00; *ridge + smooth*:

3.30; Experiment 1-FIX: *ridge*: 2.20; *ridge + smooth*: 2.30). Plots of the second-stage

nonlinearities for observers AMA, JJF are shown in Supplementary Fig. S11. This finding is

consistent with previous studies suggesting an accelerating nonlinearity following the second-

stage filters (see Discussion).

Analysis of model accuracy

To better assess the meaningfulness of the above model-fitting results, it is important to make

quantitative measures of the fitted models' accuracy in predicting observers' responses to novel

stimuli. Such measures can also address the relative merit of different variants of the estimation

procedure (*ridge* vs *ridge+smooth* prior) and of the model details, such as downsampling method

(AVG, MAX, SUB) and classification rule (DET, STO). In this section we provide an overview

of our analyses of model performance.

Psychometric function agreement

To the extent that the model architecture is appropriate and the data are sufficient to obtain

accurate fitted parameters, then the fitted model should be able to predict each observer's

responses. Consequently, we constructed psychometric functions of proportion correct on the

orientation identification task as a function of the modulation depth across the boundary for

observers in Experiment 1-VAR - three representatives are shown in Fig. 6 (AVG

downsampling). The model predictions (green, red) on the test datasets (which were not used to

train models or optimize hyper-parameters) generally lie within or near the 95% binomial

proportion confidence intervals (+/- 1.96 SEM) of observer performance (Fig. 6, blue dotted

lines). However, for the deterministic model (DET, left column), the model tends to over-predict

performance at larger contrast modulations for some observers. Implementing the model

stochastically (STO, center column) improved the model-observer agreement.

<u>Overall performance agreement</u>

Another way to assess how well fitted models account for observer responses is to compare their

overall performance, i.e. proportion correct, averaged over all modulation depths tested. Fig. 7

shows observer and model performance in Experiment 1-VAR for each individual test fold on

every observer (7 observers, 4 test folds each = 28 total folds). The deterministic model with

AVG pooling (AVG-DET, Fig. 7a, top) somewhat tended to over-predict observer performance,

with the majority (*ridge*: 18/28; *ridge + smooth*: 23/28) of test folds having significantly

different (binomial proportion difference test, 95% CI) proportions correct (Fig. 7b, top). Despite

the systematic over-prediction of observer performance (by about 6-8%), we still observe

significant correlations between predictions and actual performance over both observers (*ridge*: r

$= 0.983, p < 0.001$; *ridge + smooth*: $r = 0.972, p < 0.001$, N = 7) and folds (*ridge*: $r = 0.872, p <$

0.001; *ridge + smooth*: $r = 0.806, p < 0.001$, N = 28).

Implementing the classification stochastically produced much better agreement (AVG-

STO: Fig. 7a, middle), with relatively few (*ridge*: 4/28; *ridge + smooth*: 6/28) test folds having

significantly different proportions (Fig. 7b, middle). As before, strong correlations between

model and observer performance are seen across observers (*ridge*: $r = 0.996, p < 0.001$; *ridge +*

smooth: $r = 0.997, p < 0.001$, N = 7) and folds (*ridge*: $r = 0.890, p < 0.001$; *ridge + smooth*: $r =$

$0.911, p < 0.001$, N = 28). For the deterministic (DET) model, performance was more accurate

for subsampling (SUB-DET: Fig. 7a, bottom) than averaging downsampling (AVG-DET: Fig.

7a, top). In this case, many fewer folds (*ridge*: 10/28; *ridge + smooth*: 8/28) had significantly

different proportions of correct responses (Fig. 7b, bottom). Similar results were obtained for

Experiment 1-FIX (Supplementary Fig. S13).

Double-pass analysis

To obtain an upper bound on the performance of the model, we performed a "double-pass"

analysis (Neri & Levi, 2006; Neri, 2010; Hasan, Joosten, & Neri, 2012) by testing observers

twice on the same set of stimuli, and comparing model-observer agreement (proportion of trials

with consistent responses) on the double-pass set to observer-observer agreement between the

two passes. For 5 observers in Experiment 1-VAR, a fold of 1000 stimuli was used as the

double-pass set, and the model was trained on the remaining 3000 stimuli. The results (Fig. 8)

show that the AVG-DET or MAX-DET models agree with the observer on the two passes as

well as the observer agrees with him/her-self on the two passes. For AVG-DET, both priors give

a small, statistically insignificant (rank-sum test) median difference (*ridge*: median = 0.022, p =

0.063; *ridge + smooth*: median = 0.009, p = 0.313, N = 5), with most or all of the (binomial

proportion difference) confidence intervals bracketing zero (*ridge*: 4/5; *ridge + smooth*: 5/5).

Similarly, MAX-DET gives small median differences (*ridge*: median = 0.018, p = 0.125; *ridge +*

smooth: median = 0.02, p = 0.313, N = 5) with most confidence intervals (*ridge*: 4/5; *ridge +*

smooth: 4/5) including zero. However, SUB-DET (Fig. 8a**,** bottom panels) gives somewhat larger

differences (*ridge*: median = 0.052, p = 0.063; *ridge + smooth*: median = 0.024, p = 0.063, N =

5), although they fail to reach statistical significance. In the SUB-DET case with the *ridge* prior,

0/5 confidence intervals include zero, and 3/5 do so for *ridge + smooth*. In contrast to the DET

decision rule, we found that implementing the decision rule stochastically (AVG-STO) yielded

somewhat poorer double-pass agreement (Fig. 8b).

Decision variable correlation analysis

Although a strong model-observer agreement for the percentage correct is consistent with

accurate modeling of the observer's visual processing, it is not fully compelling. The model and

observer might both choose category A or B the same proportion of trials, without any

correlation between observer and model responses on a trial-by-trial basis. This situation could

arise, for example, if the observer and model were utilizing different stimulus features for their

decisions. To more thoroughly quantify model performance, we implemented a *decision variable*

correlation (DVC) analysis, which estimates the trial-by-trial correlation between a model's

decision variable and the observer's hypothesized decision variable (Sebastian and Geisler,

2018). This method extends standard signal detection theory by hypothesizing that the joint

distribution of model and observer decision variables for each stimulus category (A = left-

oblique/L, B = right-oblique/R) can be modeled as bivariate Gaussian distributions having

correlation parameters ρ_A, ρ_B. Using the proportions of trials on which the observer and model

decisions agree for each stimulus category, ρ_A and ρ_B are estimated using a simple maximum

likelihood procedure (Sebastian & Geisler, 2018).

DVC analysis is most accurate (as measured by bootstrapped estimates of SEM) for large

numbers of trials at a constant stimulus level sufficiently near threshold to give consistent

proportions of the four logical possibilities (model says A/B, observer says a/b) (Sebastian &

Geisler, 2018). Therefore we applied DVC analysis to Experiment 1-FIX, which entailed

thousands of trials (6000) at a single stimulus level for each observer (CJD, MAK, JJF). The

model was trained on 5000 trials and the DVC was computed using the remaining 1000 trials, for

6 choices of hold-out fold. Since the two boundary orientations provide independent estimates of

the DVC , there were 12 estimates of DVC from each observer**.** Fig. 9 shows the resulting DVC

values measured from each observer for AVG downsampling and both choices of prior. These

estimates of DVC are overwhelmingly positive and significantly (> 1.96 SEM) larger than zero.

For AVG downsampling, 32/36 (*ridge*) and 33/36 (*ridge + smooth*) estimates of DVC are

significantly larger than zero, with DVC mean +/- SD of 0.235 +/- 0.094 (*ridge*) and 0.254 +/-

0.095 for (*ridge + smooth*). MAX downsampling gives similar results, where 33/36 (*ridge*) and

35/36 (*ridge + smooth*) estimates of DVC are significantly greater than zero, with DVC mean +/-

SD of 0.245 +/- 0.094 (*ridge*) and 0.263 +/- 0.086 (*ridge + smooth*). Interestingly, SUB

downsampling gives weaker correlations with only 20/36 (*ridge*) and 24/36 (*ridge + smooth*)

estimates of DVC significantly greater than zero, and DVCs have mean +/- SD of 0.147 +/-

0.082 (*ridge*) and 0.164 +/- 0.085 (*ridge + smooth*).

Therefore, we see that not only are the models and observers in agreement about overall

proportions of each category, but they are also correlated in their trial-by-trial decisions,

consistent with the interpretation that the models and human observers are performing similar

processing.

<u>Ideal-observer analysis</u>

To compare the spatial summation and task performance of human observers to those of an ideal

observer, we trained the model on the true stimulus category labels rather than observer

classifications of these stimuli. Notably, the resulting ideal observer models make use of a

region-based spatial summation similar to the human observers (Fig. 3c). Comparing human

performance to that of the deterministic (16x16 AVG-DET) ideal observer in Experiment 1-VAR

(Supplementary Fig. S14) revealed that across 6 observers analyzed, most confidence intervals

(binomial proportion difference test, 95% confidence interval) did not contain zero (*ridge*: 6/24;

ridge + smooth: 3/24), with those containing zero coming mainly from two observers (AMA,

SRS). In contrast, for the stochastic ideal observer (AVG-STO) many more confidence intervals

contained zero (*ridge*: 11/24; *ridge + smooth*: 10/24), suggesting a better agreement with

observer performance. Similar results were observed for the 3 observers tested in Experiment 1-

FIX (Supplementary Fig. S14). Comparing human to deterministic ideal observer (AVG-DET)

performance, most confidence intervals did not contain zero (*ridge*: 3/18; *ridge + smooth*: 4/18),

while for the stochastic ideal observer most did contain zero (*ridge:* 14/18; *ridge + smooth*:

15/18). On the whole, this is similar to our findings for the models fitted to observer data – i.e. a

general tendency for the AVG + MAX models operating deterministically to over-predict

performance, while these models operating stochastically seemed to agree reasonably well.

<u>Correlations between observer performance and model parameters</u>

The different human observers exhibited substantial individual differences in overall

performance as measured by proportion correct (Fig. 7), raising the question whether there might

be corresponding variations in the fitted model parameters. We assessed this possibility for the

results in Experiment 1-VAR, using the 16x16 AVG model.

Although the nonlinearity was always expansive (exponent $\alpha > 1.0$), there was no

compelling evidence across the set of individuals that the magnitude of α explained individual

variations in performance, based on Pearson's *r* (*ridge*: $r = -0.458$, $p = 0.302$; *ridge + smooth: r =*

-0.787, $p = 0.036$, N = 7). The significant result for *ridge + smooth* case was due to the presence

of an outlier - computing these correlations using Spearman's rho revealed no significant effect

(*ridge: rho* = -0.357, *p* = 0.444; *ridge + smooth*: *rho* = -0.214, *p* = 0.662). Results were similar

for MAX and SUB models (Supplementary Table S5).

However, individual variability in observer performance was very strongly related to the

magnitudes of the fitted second-stage filter weights. That is, correlating the sum of the norms of

the filter weights with overall performance across the 7 observers yielded strong, significant

positive correlations (*ridge*: *r* = 0.970, *p* < 0.001; *ridge + smooth*: *r* = 0.993, *p* < 0.001), with

similar results for MAX, SUB models (Supplementary Table S6). Consistent with this, the ideal

observer had a larger filter norm (*ridge*: 5.67; *ridge + smooth*: 5.37) than the human observers

(*ridge*: median = 4.30, min = 2.36, max = 4.59; *ridge + smooth:* median = 4.04, min = 2.27, max

= 4.34, N = 7), as revealed by a sign-rank test (*ridge: p* = 0.018; *ridge + smooth: p* = 0.018).

Experiment 2: Boundary orientation discrimination

The first experiment demonstrated that human observers utilize region-based processing for the

orientation identification task. To see if our modeling method could also reveal situations where

observers utilize edge-based processing, we considered a fine orientation discrimination task

(Fig. 1c, right). The orientation of a second-order boundary was perturbed slightly (JND at 32%

contrast – see Methods) from vertical, and observers judged the direction of perturbation (i.e.

slightly left- vs right-oblique). In one variant of this task (Experiment 2-VAR), contrast

modulation was varied in 9 logarithmic steps from 16% to 64% centered at 32% (plus zero

modulation) to vary the task difficulty. In a second variant (Experiment 2-FIX), contrast

modulation was fixed at 32%. In both variants of Experiment 2, the perturbation of orientation

was fixed near JND for each observer at 32% contrast (CJD: 7 deg., JJF: 6 deg., VHB: 7 deg.), at

32% contrast modulation depth. In the data analysis, a higher downsampling factor (22 x 22) was

used to better reveal fine spatial details, and only AVG pooling was considered, since

Experiment 1 demonstrated substantial robustness of spatial summation to pooling rules.

Fig. 10 shows the second-stage filter weights from an observer (JJF) tested in both

Experiment 2-VAR (Fig. 10a) and Experiment 2-FIX (Fig. 10b). Unlike in Experiment 1, here

observers employ an "edge-based" summation, assigning substantially more weight to texture

regions near the boundary. Bootstrapped significance plots for individual weights are shown

Supplementary Fig. S15. Supplementary Fig. S16 shows consistent results from other observers

in these experiments. The edge-based processing employed by these observers is very similar to

that obtained from an ideal observer (Supplementary Fig. S17). As with Experiment 1, we find a

reasonably strong agreement between model predictions and observed performance on sets of

novel data not used for model parameter estimation (Supplementary Fig. S18), and find an

expansive second-stage filter nonlinearity for Experiment 2 (Supplementary Table S7). Taken

together, Experiments 1 and 2 show that our modeling methodology can reveal different spatial

processing that observers may employ for different kinds of psychophysical tasks.

Experiment 3: Integrating contrast modulation across orientation channels

In Experiments 1 and 2, we considered a particular FRF model architecture and focused on

characterizing the spatial processing that observers employ in different second-order vision tasks.

However, one of the most powerful applications of this methodology is model comparison - i.e.

comparing the ability of alternative models, embodying different assumptions about an FRF

model architecture, to account for psychophysical data. Indeed, a major focus of much of the

second-order vision literature has been to design experiments whose express goal is to test

competing hypotheses of FRF architecture (Motoyoshi & Kingdom, 2003; Motoyoshi & Nishida,

2004; Kingdom, Prins & Hayes, 2003; Motoyoshi & Kingdom, 2007; Westrick & Landy 2013).

We applied our method to ask how second-stage filters for contrast modulation integrate

orientation modulations across multiple kinds of first-stage filters or channels. In many previous

computational studies of second-order processing, the FRF models were "non-opponent", in that

each second-stage filter only analyzes a single orientation/spatial frequency channel (Wilson

1993; Kingdom, Keeble & Moulden 1995; Landy & Oruc, 2002; Zavtiz & Baker 2013).

However, other psychophysical studies have suggested "orientation-opponent" FRF models, in

which second-stage filters integrate contrast modulation across texture (Motoyoshi & Kingdom,

2003; Motoyoshi & Nishida, 2004; Kingdom, Prins, & Hayes, 2003).

To address this question systematically, we used an orientation identification task as in

Experiment 1, but with the carrier pattern containing two orthogonal orientations of

micropatterns (Fig. 1a, bottom), which would be processed by distinct first-stage orientation-

selective channels. Since the nature of spatial summation is not critical to this question, we used

a coarser downsampling factor (12 x 12), and as above, only AVG pooling was used. We

considered two models of how information is integrated by the second-stage filters. In a "non-

opponent" Model 1 (Fig. 11a, top), each first-stage channel is analyzed by its own pair of

second-stage filters (L/R oblique). Alternatively, in an "orientation opponent" Model 2 (Fig. 11a,

bottom), each second-stage filter receives inputs from both first-order channels. As in

Experiments 1 and 2, we find that both the models are in reasonably good agreement with

observer performance on the task (Supplementary Fig. S20). Also there was reassuring

consistency in that both the fitted models exhibited similar region-based weight maps, with an

expansive second-order nonlinearity (Supplementary Table S8).

When comparing Models 1 and 2 using standard model comparison techniques like the

Bayes Information Criterion, or BIC (Schwarz, 1978; Bishop 2006), there is no need to correct

for overfitting since both models have the same number of parameters. This is because when

parameter space dimensionality is equal, the complexity-penalizing terms of the BIC cancel, so

that $\Delta_{BIC} = \ln p_2(D) - \ln p_1(D)$, where $p_i(D)$ denotes the likelihood of the data (D) under

model i evaluated at the MAP estimate of the model parameters. That is, when two models are of

equal complexity and equally likely *a priori*, we simply choose the one with higher log-

likelihood of the data. The difference in log-likelihoods (Δ_{BIC}) is identical to the natural log of

the Bayes factor $B_{21} = \frac{p_2(D)}{p_1(D)}$. Standard effect size conventions state that when $2 \ln B_{21} > 10$

(corresponding to > 150-fold higher probability of model 2), the preference is considered to be

"very strong" (Kass & Raferty, 1995). We see in Fig. 11b that for all three observers tested in

Experiment, the evidence (measured by $2 \ln B_{21}$) in favor of the orientation opponent model

(Model 2) exceeds the standard criterion (10) for a very strong preference. Ideal observer

analysis also revealed a very strong preference for the orientation-opponent model fit to stimulus

category labels ($2 \ln B_{21} = 478.4$).

In the previous analysis, the log-likelihood was calculated on all the available data,

consistent with standard methodology for Bayesian model comparison (Kass & Rafferty, 1995;

Bishop 2006). However, we also wanted to compare the predictive abilities of the two models

using a cross-validation approach, by evaluating their agreement with observer performance on

data not used for training. Therefore we performed a bootstrap analysis in which both models

were fit on a randomly selected sample of 4000 stimuli and tested on the remaining 1000 (50

bootstraps). To optimize the generalization performance of each model, each was trained using

the value of the ridge regression hyperparameter λ which yielded the best generalization, as

determined by k-fold cross validation (Supplementary Figs. S19, S21). The results in Fig. 11c

show a consistent preference across observers for Model 2 (magenta line). Performing a 3 x 2

factorial ANOVA (3 observers, 2 models, 50 observations each) on the test set log-likelihoods

revealed significant main effects of both observer ($F_{2,294} = 201.085$, $p < 0.001$) and model ($F_{2,294}$

$= 39.811$, $p < 0.001$), but no significant interaction ($F_{2,294} = 3.001$, $p = 0.051$). In summary, both

analysis approaches (Figs. 11b, c) show a strong and consistent preference for the orientation-

opponent model (Model 2).

Discussion

Second-order stimuli represent a challenge for computational models of visual processing, as

they do not contain spatial variations in stimulus intensity and cannot be detected by simple

linear filtering operations (Baker, 1999; Baker & Mareschal, 2001). Consequently, standard

linear "classification image" techniques (Ahumada, 1996; Murray, 2011) are not readily

applicable to studies of second-order visual processing. The present study demonstrates that

second-order vision can be fruitfully studied using the same statistical machine learning

framework commonly applied to first-order vision (Neri & Levi, 2006; Murray, 2011) and

sensory neurophysiology (Wu et al., 2006; Willmore et al., 2010; Vintch et al., 2015; Harper et

al., 2016; Antolic et al., 2016).

Here we define a simple hierarchical neural network implementing a Filter-Rectify-Filter

(FRF) model of second-order visual processing (Bovik, Clark, & Geisler, 1990; Malik & Perona,

1990; Bergen & Landy, 1991; Sutter, Beck, & Graham, 1989; Landy & Graham, 2004) and

estimate its parameters directly from psychophysical trial data. We show that this FRF model can

accurately predict observer performance on novel test data not used for training. We demonstrate

the utility of this modeling approach by testing whether observers segment contrast-defined

boundaries using an edge- or region-based processing, finding support for region-based

segmentation in a boundary orientation-identification task (Experiment 1), and edge-based

processing for a boundary discrimination task (Experiment 2). In addition, we show how this

methodology can adjudicate between alternative FRF model architectures (Experiment 3).

Model complexity vs biological realism

A critical limitation of psychophysical system identification is the relatively limited amount of

data that can be collected in an experiment. Although constraints or priors can help alleviate the

demand for data (Knobloch & Maloney, 2008a, b; Mineault et al., 2009), it is also often

necessary to fit simplified models requiring fewer parameters, which omit many known

biological details. Here we discuss several of the modeling simplifications which may need to be

addressed when extending this methodology to more complicated second-order stimuli and tasks.

First-stage filters

In FRF models like those considered here, the initial stage of filtering and rectification is meant

to model computations believed to be taking place in visual area V1 (Mareschal & Baker, 2001).

In the present study, we modeled the first-stage filters using a standard energy model of V1

complex cells with normalization (Adelson & Bergen, 1985; Heeger 1992). Although for our

stimuli a front-end comprised entirely of oriented energy filters was perfectly adequate, for many

texture segmentation tasks it may be necessary to model half-wave rectified filters (both even

and odd phase) as well. For instance, it is well known that one can segment second-order images

using cues of carrier contrast phase (Kingdom, Hayes, & Field, 2001) and polarity (Rentschler,

Hubner, & Caelli, 1988; Malik & Perona, 1990; Hansen & Hess, 2006) , which is not possible

using only complex cell-like energy filters, since their responses are invariant to phase and

polarity (Mechler & Ringach, 2002). Likewise, it may also be desirable to include center-

surround "difference-of-Gaussian" (DOG) filters as well, since early visual cortex has many

neurons with non-oriented receptive fields (Hubel & Livingstone, 1985; Ringach, Shapley, &

Hawken, 2002; Talebi & Baker, 2012). Human psychophysics has indicated that non-oriented

filters may potentially serve as a mechanism for polarity-based segmentation (Motoyoshi &

Kingdom, 2007), and computer vision work on natural image segmentation found it

advantageous to include non-oriented as well as oriented filters (Martin, Fowlkes and Malik,

2004).

In Experiments 1 and 2, we implemented only a single spatial frequency and orientation

channel matched to the carrier, and in Experiment 3 we only considered a single spatial

frequency channel and two orientation channels. This simplification neglects the possible

contributions of off-orientation and off-spatial frequency channels to task performance. Indeed,

previous studies of second-order processing have challenged the notion that contrast-modulation

tuned mechanisms are narrowly tuned for a single first-order channel, with many studies

suggesting broad pooling over carrier spatial frequency (Prins & Kingdom 2002; Graham, Sutter,

& Venkatesan 1993; Westrick & Landy, 2013).

Second-stage filters

The main focus of our study was demonstrating that one could learn the properties (shapes and

non-linearities) of a set of second-stage filters which detect second-order visual features. For our

task involving contrast modulated boundaries (Fig 1c), the simplest possible model involves two

second-stage filters representing the two potential stimulus categories, much like the model

shown in Fig. 2. However, for psychophysical tasks involving more complex second-order

stimuli like natural occlusion boundaries (Fig. 1a, top) defined by multiple cues (e.g. orientation,

spatial frequency, etc…) which differ on opposite sides of the boundary, it may be necessary to

have both a wider variety of first-stage filters as well as several kinds of second-stage filters

sensitive to different feature combinations, as illustrated in Fig. 12. In addition, it may be of

interest to allow direct connections between the first stage of filtering and the output (decision)

stage, since natural region boundaries contain both first and second order cues (Martin et al.,

2004; DiMattina et al., 2012), which are integrated in psychophysical tasks (Rivest &

Cavanaugh, 1996; Saarela & Landy, 2012).

An additional limitation of our model (and many other FRF models) is the assumption

that there is only a single stage of higher-order filtering beyond the first-stage filters. Recent

neurophysiological and fMRI studies have suggested that texture selectivity may develop

gradually as one moves up the visual hierarchy from V1 to V2 to V4 (Freeman et al. 2013; Goda

et. al. 2014; Okazawa, Tajima, & Komatsu, 2015, 2016; Ziemba et al. 2016; Kohler et al. 2016).

In studies using convolutional neural networks to solve image recognition tasks, one often sees

texture-sensitive units develop gradually over several processing layers (Yamins et al. 2014;

Kahligh-Razavi & Kriegeskorte, 2014; Zeiler & Fergus, 2014; Yamins & DiCarlo, 2016).

Furthermore, computer vision work on boundary detection has also employed additional "texton"

layers of processing (Martin et al., 2004). Therefore, it may be of interest for future work to

consider models having additional hidden layers of processing.

Nevertheless, despite these limitations and our numerous modeling simplifications, in

practice we found that for the tasks and the stimuli used here our simple FRF model (Fig. 2) was

able to capture human performance quite well (Figs. 6-9).

Comparison with previous psychophysical modeling

Despite the numerous simplifications made in the present study, it represents a substantial

methodological advance over many previous efforts to model second-order visual perception.

Although previous studies have developed image-computable FRF models, these models have

generally fixed not only the model architecture, but also the shapes of the second-stage filters.

The present study demonstrates how the second-stage filter shapes can be learned directly from

experimental data in order to reveal the spatial integration strategies used in different tasks

(Experiments 1 and 2).

In most previous studies FRF model free parameters are determined by fitting threshold

data (e.g. Zavitz & Baker, 2013). Since thresholds are typically determined at only a few levels

of a 1-dimensional independent variable, this yields relatively few data points, greatly limiting

the number of model parameters one can estimate. In our work, we directly estimate hundreds of

model parameters by fitting stimulus-response data from thousands of psychophysical trials,

enabling us to characterize the shapes of the second-stage filters.

In addition to extending the FRF modeling literature, our work also complements and

extends previous classification image studies, which have generally been applied in the context

of first-order vision (Neri & Levi, 2006; Murray, 2011). Although classification images yield

image-computable predictive models of observer responses, relatively few studies validate these

models by testing their predictive performance on a set of stimuli not used for model estimation

(but see Neri, 2010). We tested model performance on novel stimuli not used for model

estimation using both standard measures like percent correct, as well as more advanced methods

like double-pass analysis (Neri, 2010; Hasan, Joosten & Neri 2012) decision variable correlation

(Sebastian & Geisler, 2018).

Finally, in contrast to most classification image studies, here we systematically address

the issue of model comparison. Psychophysical system identification can be formulated in the

framework of estimating a generalized linear model (Knobloch & Maloney, 2008a,b; Mineualt et

al., 2009), which is unique up to choice of link function. Therefore, issues of model comparison

(beyond coefficient shrinkage) do not naturally arise in this context. In contrast, the FRF models

employed in second-order vision vary greatly in their architectural details (number of filtering

layers, nonlinearities, connectivity, etc…), and model comparison is of great interest. In

Experiment 3, we compare two competing FRF architectures making different assumptions about

how the second-stage filters integrate across orientation channels, finding a preference for a

model with early integration by the second-stage filters, consistent with previous psychophyscial

work (Kingdom, Prins & Hayes, 2003; Prins & Kingdom, 2002; Motoyoshi & Nishida, 2004).

Edge versus region-based segmentation

Although the main focus of the current study is methodological, we applied our methodology to

the biologically interesting question of whether or not observers take a region-based approach or

an edge-based approach to segmenting a contrast boundary (Experiment 1). To the best of our

knowledge, our experiment is the first time the issue of edge/region-based processing has been

addressed for boundaries defined by differences in contrast, as it has for other second-order

boundaries (Nothdurft, 1985; Gurnsey & Laundy 1992; Wolfson & Landy, 1998).

This question is of great interest in light of the fact that numerous studies have revealed possible

neurophysiological mechanisms for contrast-boundary detection (Mareschal & Baker 1998;

Rosenberg & Issa, 2010; Li & Baker 2012; Li et al. 2014; Gharat & Baker, 2016). This body of

work has suggested a population of contrast-modulation (CM) tuned neurons in extra-striate

cortex which exhibits band-pass tuning to both first-order carrier frequency as well as second-

order modulation envelope frequency. Such CM tuning behavior is consistent with a Gabor-

shaped second-stage filter applied to the outputs of a bank of first-stage filters selectively tuned

to the carrier pattern (Baker, 1999).

If CM neurons like those described in the ventral visual pathway were the sole

mechanism responsible for psychophysical detection of CM boundaries, one might expect the 1-

D weighting profiles to have a Gabor profile, placing greater weight on regions near the

boundary. In our investigations, we find that this was not the case and that all areas of the image

are weighted equally for the orientation-identification task (Experiment 1, Figs. 3, 4).

Furthermore, in additional control manipulation where we increased the carrier frequency in

order to make sure CM neurons with smaller RFs would be optimally engaged (Experiment 1-

HFC), we still did not see any change in processing strategy (Fig. 5). These findings are

consistent with at least two distinct possibilities (not mutually exclusive) for the underlying

neural mechanisms. The first possibility is that the task is performed using CM neurons (in V2 or

beyond) with large receptive fields (> 4 dva) encompassing the entire stimulus. Such neurons

would prefer a carrier frequency much higher than their envelope frequency, which is not at all

implausible since previous work in primate V2 has shown CM neurons can have preferred

carrier:envelope ratios of up to 40:1 (Li et al., 2014). The second possibility is that the task is

performed not only with the population of CM neurons, but also by neurons sensitive to texture

('texture-units'), with the responses of such units being modulated by texture contrast. Previous

physiological studies of the ventral visual stream have demonstrated the presence of texture-

tuned units (Hanazawa & Komatsu, 2001; Okazawa et al., 2015, 2016; Ziemba et al., 2016),

making this a reasonable hypothesis.

Clearly, the fact that we can readily distinguish non-juxtaposed textures implies that there

must be mechanisms for texture representation that operate in the absence of a boundary.

However, in some cases texture segmentation can certainly benefit from boundary information,

as in the textural Craik-Cornsweet illusion (Nothdurft, 1985). In one such study (Wolfson &

Landy, 1998), one can observe that direct juxtaposition of textures having different orientations

gives rise to a novel visual cue of a junction or corner. Since there are neurons in the ventral

visual stream which are selective for cues (Hegde & Van Essen, 2000; Anzai, Peng & Van

Essen, 2007), this suggests a possible mechanism for enhanced segmentation in this case.

However, other work on texture segmentation has shown a minimal contribution of

information on the boundary. A study using natural image patches in a task of discriminating

occlusions from textures found that covering up the boundary had little effect on performance

(DiMattina et al., 2012). However, performance on natural occlusion edge and junction detection

tasks can be seriously degraded when textural information, which is by its nature defined over a

region, is removed (McDermott 2004; DiMattina et al., 2012). Similarly, work on segmenting

complex textures defined by letters shows little effect of boundary information (Gurnsey &

Laundry, 1992).

In general, the answer to this question is most likely highly dependent on the particular

stimulus and the nature of the psychophysical task. In our view, the question of "edge" versus

"region"-based processing is somewhat of a false dichotomy, since clearly for a very large

stimulus extending into the far periphery there will be reduced weighting at the largest

eccentricities, for the entirely trivial reason that visual acuity falls off sharply outside of the

fovea. The real question of interest is the exact shape of the fall-off in weight as a function of

stimulus eccentricity, and how this fall-off may relate to putative neural codes. Our method is

well suited to address this issue for many different kinds of second-order boundaries and tasks,

much like standard classification images can be used to address this question for first-order

boundaries.

In Experiment 1 every part of the image is useful for performing the task, and hence the

ideal observer will integrate information from all image regions. In Experiment 2, the only useful

information for performing the task is near the boundary and so an ideal observer will be

indifferent to the stimulus elsewhere. In terms of possible mechanisms, we might expect CM

neurons with larger receptive fields to be engaged in Experiment 1, whereas the most useful

neurons in Experiment 2 would be CM neurons with smaller receptive fields. This is because

CM neurons with large (small) receptive fields would be the ones whose responses best

distinguish the two stimulus categories in Experiment 1 (2).

Integrating heterogeneous first-stage channels

A common ingredient to the wide variety of FRF models proposed to account for psychophysical

data is the analysis of a set of first-stage filters by one or more second-stage filters defined on a

much larger spatial scale. However, one aspect in which models differ is whether or not the

second stage filters analyze first stage filters at a single orientation/spatial frequency, or whether

there is integration across first-stage channels. In one 'standard' model of FRF processing, each

second-stage filter only analyzes the outputs of a single first-stage orientation/spatial frequency

channel (Malik & Perona, 1990; Wilson, 1993; Landy & Oruc, 2002). However, a number of

psychophysical results have called this model into question. One study using a sub-threshold

summation paradigm finds support for a model where there is linear integration across

orientation for detecting contrast modulations (Motoyoshi & Nishida, 2004). Another study

making use of energy-frequency analysis reveals the existence of orientation-opponent

mechanisms in second-order vision (Motoyoshi & Kingdom, 2003). Finally, other work has

suggested at least partly independent mechanisms for detecting second-order modulations

defined by contrast and spatial/frequency orientation, with the suggestion that contrast

modulations may be pooled across first-stage channels (Kingdom, Prins & Hayes 2003). In

Experiment 3 we find support for a model that integrates across orientation channels, consistent

with previous psychophysical studies. Although there is no direct physiological evidence for

integration of carrier orientation in CM neurons (which are tuned for carrier orientation – see Li

et al. 2014), this discrepancy may be due the use of grating carriers rather than multi-orientation

micropatterns. Investigation of CM neuron responses with multi-orientation carriers is an

interesting future research direction.

Conclusions

Statistical machine learning has in recent years become a powerful and widely applied

methodology in vision science and computational neuroscience. Our work demonstrates that the

same machine learning methodology used to characterize neural coding (Wu et al., 2006;

Willmore et al., 2010; Kriegskorte, 2015; Yamins & DiCarlo, 2016; Antolik et al., 2016) and

first-order visual processing (Mineault et al. 2009; Murray, 2011) can be fruitfully applied to

extend psychophysical system identification approaches to complex visual stimuli, including

second-order boundaries. We anticipate that future applications of this methodology may lead to

a better understanding of how multiple first- and second-order cues are combined by human

observers to detect natural boundaries, and hopefully provide insights into neural and

computational mechanisms of image region segmentation.

Methods

Experimental Paradigms

Stimuli and psychophysical task

Contrast-modulated texture boundary stimuli were created similarly to those of Zavitz & Baker

(2013), by multiplying a large (predominantly low spatial frequency) contrast modulation

envelope by a high spatial frequency carrier (texture) pattern (Fig. 1a, b). The carrier patterns

were produced by adding odd-phase Gabor micropatterns at random locations in an over-size

larger image, which was subsequently cropped to the desired size. Only texture patterns having

sufficient uniformity in root-mean-squared (rms) contrast were utilized, using the uniformity

criterion of Zavitz & Baker (2013). To produce contrast-modulated stimuli, carrier textures were

modulated by a half-disc oriented either right oblique (clockwise) or left-oblique (counter-

clockwise), and then multiplied by a circular raised cosine window. The rms contrast of the

carrier patterns was set to 14%, which is 6 dB above previously observed average carrier

detection thresholds (Arsenault, Yonessi & Baker, 2011). Examples of right-oblique boundaries

with varying carrier mircopattern densities and depths of contrast modulation are shown in Fig.

1b. Boundaries between micropattern textures like these have been used in previous

psychophysics studies (Zavitz & Baker, 2013, 2014), and offer flexibility to produce a wide

variety of naturalistic texture patterns amenable to parametric variation.

In all experiments, observers performed a single-interval 2AFC task to determine

whether a briefly displayed (100 msec) boundary stimulus was contrast-modulated in a right-

oblique (clockwise) or left-oblique (counter-clockwise) orientation. Envelope phase was

randomized across trials, to preclude its use as a cue. Visual feedback was provided after each

trial to maximize observer performance. Data was collected over multiple (4-5) sessions of 30-60

minutes, conducted over several days. An initial training session was dedicated to learning the

orientation identification task (+/- 45 degree) by performing a short version (300 trials) at various

micropattern densities (256, 1024, 2048 patterns or 512, 1024, 2048 patterns). Consistent with

previous studies on second-order edge detection (Zavitz & Baker, 2013, 2014), we found in

preliminary experiments that task performance was best for carrier texture patterns having a high

density of micropatterns. Therefore we used relatively high micropattern densities (2048 per

256x256 image for Experiments 1, 2 and 512 for Experiment 3), higher than in previous studies

(Zavitz & Baker, 2013), with the goal of optimizing observer performance.

<u>Psychophysical observers</u>

Observers were author CJD and 7 members of his research group (adult undergraduate students)

who were initially naïve to the experimental purposes. For Experiment 1, 4 additional observers

were recruited from two Psychology classes (EXP-3202, PSB-4002) at Florida Gulf Coast

University (FGCU). All observers had normal or corrected-to-normal acuity. All observers

provided written informed consent and all procedures were approved beforehand by the IRB at

FGCU (Protocol 2014-01) and McGill University (Protocol MED-B-96-279), in accordance with

the Declaration of Helsinki.

<u>Displays and experimental control</u>

FGCU experiments were run in one of two windowless vision psychophysics chambers with no

light sources other than the computer. Chamber 1 contained a factory-calibrated (gamma-

corrected) LCD (Cambridge Research Systems, Display++, 120Hz, 1920x1080 pixels, 100

cd/m^2). Chamber 2 contained a gamma-corrected CRT (SONY FD-500 Trinitron, 75 Hz,

1024x768 pixels, 59.2 cd/m^2) driven by a Bits# stimulus processor (Cambridge Research

Systems). In each chamber the display was controlled by a Dell OptiPlex 9020 with an NVIDIA

GeForce GTX 645 graphics card. Observers viewed the stimuli binocularly, with a chin rest, at a

distance of 133 cm, so that the 256x256 stimulus image subtended approximately 4 deg. visual

angle (dva). McGill data was collected from author CJD for Experiments 2 and 3. Stimuli were

displayed on a CRT (SONY Multiscan G400, 75 Hz, 1024x768 pixels, 53 cd/m^2) with gamma

correction through the color lookup tables. This monitor was driven by an Apple MacPro4 (2.26

GHz Quad Core) hosting an NVIDIA GeForce GT 120 graphics card. Binocular viewing was at

a distance of 125 cm, so that the stimulus subtended 4 deg, and experiments were conducted in a

room with normal lighting. We observed remarkable consistency in our results from the two

sites, despite differences in monitor characteristics and room lighting conditions, so all data was

pooled for analysis. Experiments were controlled using custom-authored software written in the

MATLAB® programming language (MathWorks®, Inc.), making use of routines from the

PsychToolbox® Version 3.0.12 (Brainard, 1997; Pelli, 1997; Kleiner et al., 2007). To speed up

experiments, carrier patterns were pre-computed and stored at 8 bit precision on the host

computer. A unique set of pre-computed carrier patterns was used for each experiment, so that a

given observer never saw the same carrier pattern more than once.

Experiment 1: Orientation identification

The stimuli for Experiment 1 were contrast-modulated discs (Fig. 1b). Stimuli were 256 x 256

pixels in size with a carrier pattern comprised of 2048 randomly placed,vertically oriented (0

degrees) Gabor micropattern stimuli (32 pixels or 0.5 dva.). This carrier was modulated by an

obliquely oriented half-disc, graduated by a cosine taper to avoid introduction of first-order

artifacts. In this task, the two stimulus alternatives had right/left-oblique (+/- 45 deg.)

boundaries.

In the main version of Experiment 1, for 7 observers, contrast modulation depths were

varied across 9 logarithmically spaced levels from 8% to 32%, centered at 16%, plus 0%

modulation (Experiment 1-VAR), using a method of constant stimuli. This set of levels resulted

in trials at or near threshold for most observers, while still including some relatively easy trials.

After an initial training session, observers each performed a total of 4000 trials (4 blocks of 1000

trials, 100 trials per level) over the course of multiple sessions spaced over several days. For one

observer (CJD), 2975 micropatterns were used instead of 2048.

For 3 observers (CJD and naïve observers MAK and JJF), contrast modulation depths

were fixed at a value slightly above each observer's measured threshold (Experiment 1-FIX),

with the goal of obtaining near-threshold task performance of approximately 80% correct

(Supplementary Fig. S12). This is more typical of most classification image literature (Murray,

2011), which often fixes stimulus intensities at or near task performance thresholds. These

observers performed 6000 trials (6 blocks of 1000 trials) over multiple sessions spaced over

several days.

As an additional variant of Experiment 1, we used a carrier texture composed of

micropatterns with a much higher spatial frequency (8 pixels or 0.125 dva.) and a higher density

(8192), with rms contrast remaining at 14%. Experiment 1-HFC was run on three naïve

observers (LJW, JMM, VHB) tested at variable modulation contrasts (same levels as Experiment

1-VAR).

<u>Experiment 2: Fine orientation discrimination</u>

In order to show the general applicability of our methodology to tasks where observers may

employ an edge-based strategy, we ran a fine orientation discrimination task in which observers

determined whether a clearly visible contrast-modulated boundary (same carrier parameters as in

Experiment 1) was tilted slightly left- vs right-oblique relative to vertical. Experiment 2 is

complementary to Experiment 1, in which the orientation difference is very large (+/- 45 degrees

from vertical), while the contrast modulation is near detection threshold, whereas in Experiment

2 the contrast modulation is well above detection threshold, but the orientation difference is very

small. This experiment was run on 2 observers, one of whom (JJF) was naïve to the purpose of

the experiment. In a preliminary experiment at 32% contrast modulation, a method of constant

stimuli was used to measure a just-noticeable-difference (JND) for orientation discrimination

(approximately 75% performance) for each observer (JJF: 6 deg., CJD: 7 deg.). Then in

subsequent sessions, observers performed the fine orientation discrimination at this value for a

set of stimuli whose contrast modulation was varied from 16% to 64% (center = 32%) with a

method of constant stimuli. Observers performed 6000 trials of the task over multiple sessions

spaced over multiple days (6 blocks of 1000 trials, 100 trials per level). We refer to this

experiment as Experiment 2-VAR. For two naïve observers (VHB, JJF) we also ran Experiment

2-FIX, where the orientation difference was fixed at each observer's JND.

<u>Experiment 3: Orientation identification with a more complex carrier texture</u>

Experiment 3 was the same as Experiment 1-VAR except using a carrier texture containing

micropatterns with two orthogonal orientations, as in Fig. 1a (bottom). For this experiment the

micropatterns were elongated (2:1 aspect ratio instead of 1:1 as in Experiments 1, 2), to give a

narrower orientation bandwidth. In addition the density was reduced (512 micropatterns instead

of 2048), to create a stronger percept of oriented structure in the carrier texture.

Modeling approach

Modeling framework

Most previous psychophysical SI methods assume that the decision variable arises from a
weighted linear sum of the values (e.g. pixel luminances) of the sensory stimulus (Ahumada,
2002; Murray, 2011), essentially modeling the entire chain of brain processes involved in
stimulus-processing and decision-making by a single linear filter followed by a threshold. Here
we propose a more general approach which we refer to as *psychophysical network modeling*. In
this scheme, the decision variable is a function of the stimulus-dependent activities of a set of
"hidden units", each of which may be sensitive to different aspects of the stimulus. This idea
closely parallels recent modeling of neural responses by combining the outputs of multiple
nonlinear subunits selective for different stimulus features (Willmore, Prenger & Gallant, 2010;
Vintch, Simoncelli & Movshon, 2015; Harper et al. 2016; Rowenkamp & Sharpee, 2017).

Given a classification task for a stimulus $\mathbf{x} \in \mathbb{R}^d$ which elicits one of two behavioral
alternatives ($b = 1, b = -1$), one may define a generic psychophysical model as

$$p(b = 1 | \gamma, \boldsymbol{\theta}, \mathbf{x}) = \frac{\gamma}{2} + (1 - \gamma)\sigma\big(u(\mathbf{x}, \boldsymbol{\theta})\big), \tag{M.1}$$

$$p(b = -1) = 1 - p(b = 1), \tag{M.2}$$

where σ is a psychometric function, $u(\mathbf{x}, \boldsymbol{\theta})$ denotes the stimulus-dependent input to the
psychometric function whose parameters $\boldsymbol{\theta}$ characterize the sensory processing model, and γ
denotes the lapse rate. The stimulus inputs $\mathbf{x}$ may be either the stimulus parameterization itself
(e.g. pixel luminances), $\mathbf{I}$, or a transformed version of the stimulus parameterization ($\mathbf{x} = \phi(\mathbf{I})$).
We define a *psychophysical network model* by making the additional assumption that the input
$u(\mathbf{x}, \boldsymbol{\theta})$ to the psychometric function is some function of the activities $s_1, \cdots, s_K$ of a set of K
psychophysical hidden units, i.e.

$$u(\mathbf{x}, \boldsymbol{\theta}) = F(s_1, \cdots, s_K, \mathbf{v}), \tag{M.3}$$

where $\mathbf{v}$ is a set of parameters characterizing how the s_i are combined. Perhaps the simplest
combination rule is a weighted linear summation, i.e.

$$F(s_1, \cdots, s_K, \mathbf{v}) = v_0 + \sum_{i=1}^{K} v_i \, s_i, \tag{M.4}$$

990   Note that we can have more than 2 hidden units ($K > 2$) even though there are only two

991   behavioral responses (e.g. model of Fig.10a). We assume that the hidden unit activities are a

992   nonlinear function of the projection of the features $\mathbf{x}$ onto some filter $\mathbf{w}_i$,

$$s_i = h\left(\mathbf{w}_i^{\mathrm{T}}\mathbf{x}, \boldsymbol{\alpha}\right), \tag{M.5}$$

993   where $\boldsymbol{\alpha}$ parameterizes the shape of the nonlinearity. Combining Eq. (M.1), (M.4) and (M.5)

994   yields a final expression for a psychophysical network model with linear cue combination

$$p(b = 1|\gamma, \boldsymbol{\theta}, \mathbf{x}) = \frac{\gamma}{2} + (1 - \gamma)\sigma\left(v_0 + \sum_{i=1}^{K} v_i\, h\left(\mathbf{w}_i^{\mathrm{T}}\mathbf{x}, \alpha\right)\right). \tag{M.6}$$

995   Various standard models used in machine learning are special cases of M.6. For instance,

996   standard binary logistic regression (Bishop, 2006) used for simple yes/no detection corresponds

997   to the case of $\gamma = 0$ and a single hidden unit whose nonlinearity is a simple linear pass-through

998   ($h(u) = u$) with fixed output weight $v_1 = 1$, so that (M.6) reduces to

$$p(b = 1|\boldsymbol{\theta}, \mathbf{x}) = \sigma\left(v_0 + \mathbf{w}_i^{\mathrm{T}}\mathbf{x}\right). \tag{M.7}$$

999   Likewise, with $\gamma = 0$ and the sigmoidal hidden unit nonlinearity $h(u) = 1/(1 + e^{-u})$, this

1000 model (M.6) becomes like a three-layer connectionist neural network (Rumelhart, Hinton, &

1001 McClelland, 1986; Bishop, 2006).

1002

1003   Filter-rectify filter model

1004

A psychophysical network model for detecting whether a second-order edge is oriented in a left-

or right-oblique direction is illustrated in Fig. 2. In this model, the inputs $\mathbf{x}$ are the down-sampled

outputs of a bank of first-stage energy filters resembling V1 complex cells applied to the

stimulus image $\mathbf{I}$, a transformation which we represent as $\mathbf{x} = \phi(\mathbf{I})$. There are two second-stage

filters which serve as inputs to the hidden units. One hidden unit (L) learns a set of filter weights

(blue lines) to detect a left-oblique edges from the pattern of activity in the first-stage subunits,

while the other hidden unit (R) learns a set of filter weights to detect a right-oblique edge. The

filter outputs are passed through a rectified power-law nonlinearity $h(u) = |u|^\alpha$ (blue curve) to

generate the hidden unit activities s_L, s_R. These hidden unit activities are combined, assuming

fixed output weights ($v_R = 1, v_L = -1$), and a bias term v_0 is added to obtain $u = s_R - s_L + v_0$.

The fixed output weights are a consequence of our choice of a power-law nonlinearity, since for

all inputs $\mathbf{x}$, filters $\mathbf{w}$ and output weights v, the term $v|\mathbf{w}^{\mathrm{T}}\mathbf{x}|^\alpha$ is identical for all $v, \mathbf{w}$ satisfying

$v\|\mathbf{w}\|^{\alpha} = C$, where C is some constant and $\|\mathbf{w}\|$ denotes the norm of $\mathbf{w}$ - see Ran & Hu (2017)

and DiMattina & Zhang (2010). Many variants on this basic FRF model architecture shown in

Fig. 2 are possible, and fitting multiple models to a given dataset could permit us to investigate

questions about FRF model architecture (Motoyoshi & Nishida, 2004; Motoyoshi & Kingdom,

2007; Westrick & Landy, 2013).

1022

1023   <u>Model estimation and regularization</u>

1024

1025   We simplify notation by combining all model parameters and the lapse rate into the single

1026   parameter vector $\boldsymbol{\eta}$. Given psychophysical stimulus-response data $D = \{\mathbf{x}_i, b_i\}_{i=1}^{n}$, and prior

1027   constraints $p_0(\boldsymbol{\eta})$ (possibly uninformative) on the model parameters, we pose the estimation as a

1028   machine learning problem of finding the maximum a posteriori (MAP) estimate of $\boldsymbol{\eta}$, given by:

$$\widehat{\boldsymbol{\eta}} = \underset{\boldsymbol{\eta}}{\operatorname{argmax}} \ln p(\boldsymbol{\eta}|D) = \ln p(D|\boldsymbol{\eta}) + \ln p_0(\boldsymbol{\eta}). \tag{M.8}$$

In this framework, the prior constraints $p_0(\boldsymbol{\eta})$ are often used to prevent over-fitting (Bishop,

2006), can be a serious problem due to the relatively large number of parameters (hundreds or

thousands) which need to be estimated from a limited number (generally < 10K) of

psychophysical trials. Various techniques have been applied to help reduce the problems of noise

and over-fitting, including Bayesian priors (Mineault, Barthelme & Pack, 2009), radial averaging

(Abbey & Eckstein, 2002) or using simplified low-dimensional stimuli (Li, Levi & Klein, 2004).

Here we considered two different Bayesian methods for regularization of the second-stage filter

weights. Under a prior assumption that the weights are from a multivariate Gaussian distribution,

a "ridge-regression" penalty (Bishop, 2006) is applied to each of the second-stage filters weight

vectors $\mathbf{w}_i$ (Fig. 2, blue lines) - this encourages small weight magnitudes, to prevent fitting noise.

The prior is given by

$$\ln p_0(w_i) = -\frac{1}{2\lambda} \sum_{j=1}^{d} w_{ij}^2, \tag{M.9}$$

where w_{ij} denotes the j-th element of filter $\mathbf{w}_i$ and the hyperparameter λ controls the strength of

the penalty (smaller λ induces a stronger penalty). Optimizing λ using k-fold cross-validation

(Bishop, 2006), $\lambda = 0.1 - 1.0$ provided a good trade-off between fitting to the training data and

generalizing to novel data in the test set in Experiment 1 - see Supplementary Figs. S1, S2. This

parameter was re-optimized for each of the two models in Experiment 3 (which differed in

architecture from those used in Experiments 1, 2) using the same procedure (Supplementary Fig.

S19).

1047

1048   We also considered the effects of an additional prior $q_0(\mathbf{w}_i)$ favoring second-stage

1049 weights that form a spatially smooth filter (Wilmore & Smyth, 2003). Such a prior was

1050 implemented by constructing a matrix $\mathbf{S_2}$ whose rows are the 2-D Laplace operator

$$\mathbf{L_2} = \begin{bmatrix} 0 & -1 & 0 \\ -1 & 4 & -1 \\ 0 & -1 & 0 \end{bmatrix} \tag{M.10}$$

1051 centered at every point in a $p \times p$ matrix of zeros and unwrapped into a vector of length $d = p^2$,

1052 where p is the down-sampled image dimensionality. This smoothness prior is specified by

$$\ln q_0(\mathbf{w}_i) = -\frac{1}{2\omega}\mathbf{w}^{\mathrm{T}}(\mathbf{S_2^T S_2})\mathbf{w}, \tag{M.11}$$

with hyper-parameter ω controlling the extent to which roughness is penalized (smaller ω induce

a stronger penality). Optimizing ω using k-fold cross-validation with $\lambda = 1$, there was a slight

improvement in generalization when the smoothness prior (M.11) was also included, with the

value of $\omega = 1$ providing a good tradeoff between fitting the data and generalizing to novel test

data in Experiment 1 (Supplementary Figs. S3, S4). Adding this additional smoothness constraint

reduced fitting to the training dataset, but improved generalization of the model to novel data

(Supplementary Figs. S5, S6).

1060

<u>Numerical optimization</u>

Second-stage filter weights $\mathbf{w}_i$ and the exponent α of the hidden unit nonlinearity were estimated

using alternating coordinate ascent in a manner similar to the EM algorithm (Dempster, Laird

and Rubin, 1970). Weights were optimized for one filter $\mathbf{w}_i$ at a time while all other filters $\mathbf{w}_{j \neq i}$

and the power law exponent α were fixed. The filter weights, starting with randomized initial

values, were optimized using a quasi-Newton method (L-BFGS). To estimate the power law

exponent α, all of the second-stage filters were fixed and a 1-D line search was performed over

the range $[0.1, 4.0]$. The optimizations for $\mathbf{w}_i$ and α are not log-concave, which means that local

maxima may be possible (Paninski, Pillow & Lewi, 2007). In practice we usually found robust

and consistent estimates of model parameters across optimization runs starting from several

starting points. We found that sometimes the search converged on a "local maximum" consisting

of only a single non-zero filter. Therefore, as an additional precaution, after the first round of

optimization (of at least 4 total rounds depending on the experiment) we always re-initialized the

search at a point in parameter space where the filter that was smaller in magnitude was set to be

mirror-symmetric to the current value of the larger one. The optimization was then allowed to

proceed as usual for several more rounds before termination. This procedure had the effect of

eliminating any problems with local minima.

In preliminary investigations the estimated lapse rate γ was always zero, so this

parameter was not included in our final model. Previous work has shown the best estimates of

lapse rates when a large number of easy trials are included (Prins, 2012). This was not the case in

our study, nor in the general classification image literature, which tends to use near-threshold

stimuli and does not typically estimate lapse rates (Murray, 2011).

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1440   **Figure Legends**

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Figure 1: Examples of second-order boundary stimuli, with varying texture density and

modulation depth. **(a)** *Top:* A natural occlusion edge having similar luminance on both sides,

but clearly visible differences in texture. *Bottom:* A contrast-defined edge with identical mean

luminance in each region, but different contrasts of the texture elements. In this example the

contrast modulation envelope has a left-oblique (-45 deg. w.r.t vertical) orientation. **(b)**

Examples of contrast-modulated micropattern stimuli, for three densities and three modulation

depths, all having a right-oblique (+45 deg.) boundary orientation. **(c)** Schematic illustration of

the two psychophysical tasks (*orientation identification*: Experiments 1 and 3, *orientation*

discrimination: Experiment 2).

1451

Figure 2: Neural network implementing a FRF (Filter-Rectify-Filter) arrangement for texture

segmentation. Parameters shown in blue are learned from data, those in black are fixed. Stimulus

image **I** is filtered by a bank of first-stage energy filters, resembling V1 complex cells, whose

down-sampled responses provide a feature vector input **x** to two second-stage filters. An

optimization algorithm adjusts connection weights $\mathbf{w}_L$, $\mathbf{w}_R$ (blue lines), to produce second-stage

filters which are selective for left-oblique (L) or right-oblique (R) contrast-defined boundaries, to

produce responses consistent with psychophysical data. The output of each second-stage filter is

passed through a non-linearity $h(u) = |u|^{\alpha}$ (blue curve) whose shape parameter α is also

estimated from the psychophysical data. Fixed output weights $v_R = +1$, $v_L = -1$ lead to the

decision variable $u = s_R - s_{L} + v_0$, which is input to a sigmoid function to determine the probability

of the observer classifying a given edge as being right-oblique.

1463

Figure 3: Second stage filter weights for two representative observers in Experiment 1. **(a)**

Second-stage filter weights learned by the model for representative observer AMA in

Experiment 1-VAR for two different priors (left: *ridge*; right: *ridge + smooth*) with 16x16 AVG

down-sampling. Top panels show the 2-D filter weights (averaged over 4 training folds) and

bottom panels show these 2-D weights collapsed into a 1-D profile (black dashed lines) by

averaging along the matrix diagonals (left-oblique subunit) or anti-diagonals (right-oblique

subunit). Thick lines (red: *ridge*; green: *ridge + smooth*) denote average over 30 resampled

bootstrapped training sets, and thin lines dashed lines show +/- 1 SEM.. **(b)** Same as (a) but for

observer JJF in Experiment 1-FIX. **(c)** Ideal observer for Experiment 1-VAR. Organization as in

(a), (b) except here thick black line denotes average over 4 training folds and thin dashed lines

show fits to individual folds.

1475

1476   **Figure 4:** 1-D profiles of the second-stage filter weights for all individual observers in

1477   Experiment 1. **(a)** 1-D profiles for observers in Experiment1-VAR (colored lines) plotted with

1478   the average across observers (thick black lines) for three sampling rules and both priors. **(b)**

1479   Same as (a) but for Experiment 1-FIX.

1480

1481   **Figure 5:** Normalized 1-D profiles of the average second-stage filter weights (30 bootstrapped

1482   re-samples) for the ideal observer (thick black lines).Thin black dashed lines indicate +/- 1.96

1483   SEM, and colored lines indicate normalized individual human observer profiles. **(a)** Experiment

1484   1-VAR (top) and Experiment 1-FIX (bottom). **(b)** Experiment 1-HFC.

1485

Figure 6: Psychometric functions for three representative observers in Experiment 1-VAR. Blue

lines denote observer performance on the test set (stimuli not used for model estimation) as a

function of modulation depth, together with 95% binomial proportion confidence intervals (+/-

1.96 SEM, blue dashed lines). Red and green lines denote model predictions for test stimuli as a

function of contrast modulation depth for both priors (red: *ridge*; green: *ridge + smooth*). Left

column shows model operating deterministically (DET), right column shows model operating

stochastically (STO).

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Figure 7: Analysis of model accuracy for Experiment 1-VAR. (**a**) Plots of observer performance

(horizontal axis) and model performance (vertical axis) averaged across observers (left sub-

panels, circles, N = 7) or test folds (right sub-panels, solid symbols, N = 28). Observer and

model performance was compared on a set of novel test stimuli (N = 500) not used for model

estimation or hyper-parameter optimization. *Top:* Deterministic model with AVG down-

sampling (AVG-DET). Correlation coefficients are color coded for each choice of Bayesian

prior (red: *ridge*; green: *ridge + smooth*). *Middle:* Stochastic model with AVG down-sampling

(AVG-STO). *Bottom:* Deterministic model with SUB down-sampling (SUB-DET). (**b**)

Difference between observer and model performance (observer - model) for all for each

individual test fold (4 folds per subject) for all models shown in (a). Lines show 95% confidence

intervals of the difference (binomial proportion difference test). Colors indicate different choices

of Bayesian prior (red: *ridge*; green: *ridge + smooth*).

1506

Figure 8: Double-pass analysis for N = 5 observers in Experiment 1-VAR. (**a**) Models operating

in deterministic (DET) mode for three different down-sampling rules. *Left panels:* Observer-

observer (horizontal axis) and observer-model (vertical axis) proportion agreement on the

double-pass set. Thin lines denote 95% binomial proportion confidence intervals. *Right panels*:

Difference between observer-observer and observer-model proportion agreement for all

observers. Lines denote 95% binomial proportion difference confidence intervals. (**b**) Model

with AVG down-sampling operating in stochastic mode (AVG-STO). Organization is the same

as (a).

1515

1516   **Figure 9:** Decision variable correlation analysis. Decision variable correlation (DVC) computed

1517   on 6 test folds (two measurements per fold) for three observers (CJD = blue, MAK = magenta,

1518   JJF = black) in Experiment 1-FIX for both priors. Thin lines denote +/-1 SEM (200 bootstrap re-

1519   samples).

1520

1521   **Figure 10:** Second-stage filter weights for one representative observer from Experiment 2. **(a)**

1522   Observer JJF in Experiment 2-VAR. *Top:* 2-D profiles averaged over $k = 4$ training folds.

1523   *Bottom:* 1-D profiles showing mean weight magnitude (thick lines), averaged over 30

1524   bootstrapped re-samplings. Thin dashed lines show +/- 1 SEM. **(b)** Observer JJF in Experiment

1525   2-FIX.

1526

Figure 11: Model comparison for Experiment 3. **(a)** Two competing models of FRF architecture

fit to psychophysical trial data in Experiment 3. *Top:* Model 1 ("non-opponent") assumes that

each first-stage orientation channel is analyzed by its own pair of (L/R) second-stage filters.

Bottom: Model 2 ("orientation opponent") assumes that each (L/R) second-stage filter integrates

over both first-stage channels.

(**b**) Bayesian model comparison making use of all data reveals a strong consistent preference (as

measured by the Bayes factor – see text) for Model 2 (orientation-opponent) for all three

observers (color lines and symbols). Thick black line indicates the conventional criterion for a

"very strong" preference for Model 2. (**c**) Bootstrapping analysis where model likelihood is

evaluated on novel data not used for model training also reveals a preference for Model 2.

1537

1538   **Figure 12:** Hypothetical extension of our modeling framework with additional second-stage

1539   filters and a more complete implementation of the first-stage filters. Such a model can potentially

1540   be fit to human observer performance on boundary perception tasks involving complex stimuli

1541   like natural occlusion boundaries.

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Figure 1

Figure 2

first stage (fixed)　　　second stage (learned)　　　output stage

$\mathbf{x} = \phi(\mathbf{I})$　　　$s_i = h(\mathbf{w}_i \cdot \mathbf{x}, \alpha)$

$\mathbf{I}$

$\mathbf{w}_R$

$\mathbf{w}_L$

$v_R = +1$

$v_L = -1$

P(R)

$u = s_R - s_L + v_0$

stimulus　　　features　　　filters　　　non-linearity　　　decision variable

Figure 3

Figure 4

Figure 5

a

b

Figure 6

Figure 7

Figure 8

Figure 9

Figure 10

a

b

Figure 11

Figure 12